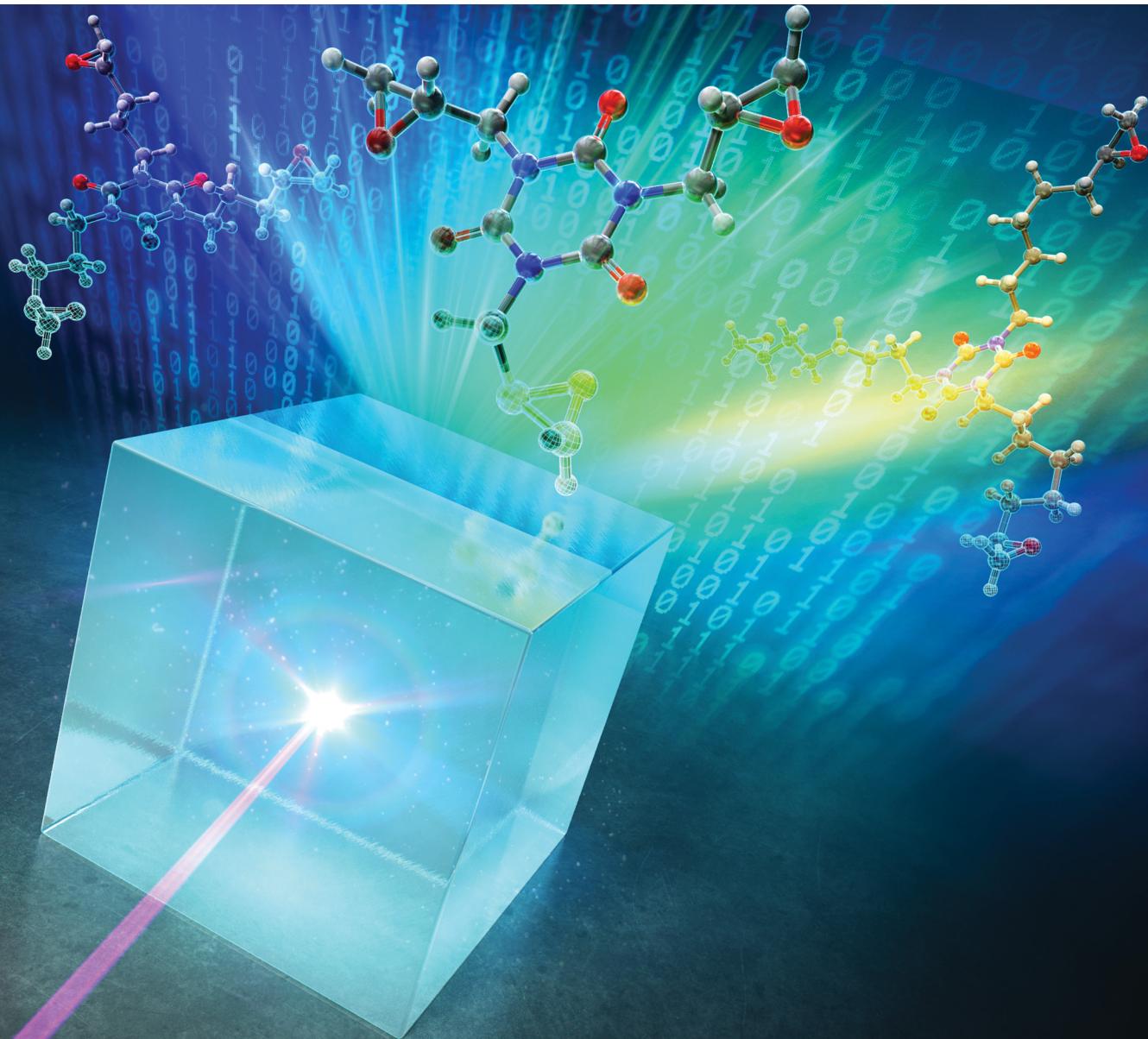


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ISSN 1463-9076

**PAPER**

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Effects of the chain length of nonaromatic epoxy resins on thermomechanical and optical properties: experiments, and *ab initio* and molecular dynamics simulations



Cite this: *Phys. Chem. Chem. Phys.*,  
2024, 26, 24250

## Effects of the chain length of nonaromatic epoxy resins on thermomechanical and optical properties: experiments, and *ab initio* and molecular dynamics simulations

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Epoxy resin has been extensively used in the field of advanced electronic materials as an adhesive and encapsulant owing to its excellent material properties. However, recently, there has been a demand for further improvement in heat resistance, high transparency, environmental resistance, and enhanced handling properties for high-brightness light-emitting diodes. Conventional aromatic epoxy resins lack light resistance; therefore, a colorless and transparent epoxy resin without aromatic rings is desirable. In this study, tris(2,3-epoxypropyl) isocyanurate (TEPIC) was used as a nonaromatic epoxy resin, and three types of TEPIC with different side-chain lengths were prepared. The ultraviolet (UV)-visible absorption properties of TEPIC were evaluated using time-dependent density functional theory, and the practicality of the numerical prediction of light resistance was verified. TEPIC yields a UV absorbance spectrum with a lower intensity than those of conventional aromatic epoxy resins, suggesting that TEPIC is expected to have high light resistance. In addition, their thermomechanical properties and the influence of molecular structure were evaluated using both molecular dynamics (MD) simulations and experiments. The MD simulation and experimental results were in good agreement, indicating that the long side chains of TEPIC suppress triaxial deformation-induced failure and improve ductility instead of decreasing strength and stiffness. In addition, the longer side chains form a dense molecular structure with less free volume. These results indicate that numerical approaches can be used to predict various properties of epoxy resins and interpret them from the molecular structure. Accordingly, these approaches can be used to aid the material development process.

Received 10th June 2024,  
Accepted 29th July 2024

DOI: 10.1039/d4cp02357a

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### 1 Introduction

Thermoset resins, such as epoxy resins, have been extensively used in the field of advanced electronic materials as adhesives and encapsulants owing to their excellent material properties, such as high adhesion, high electrical insulation, high heat

resistance, low volume shrinkage, high water resistance, and high solvent resistance. However, the recently used high-brightness light-emitting diodes require further improvements in heat resistance, transparency, and environmental resistance while achieving high handling performance. Although conventional bisphenol epoxy resins are extensively used owing to their low cost and good handling properties, these aromatic epoxy resins lack light resistance, and yellowing occurs. This yellowing effect has been reported to be due to the aromatic rings which transform to quinone methide upon exposure to ultraviolet (UV) light.<sup>1</sup> Therefore, studies have been conducted to develop cured resins without aromatic rings.<sup>2,3</sup>

In contrast, epoxy resins containing aromatic rings, such as benzene and polycyclic aromatic rings, exhibit high-heat resistance and a low coefficient of thermal expansion (CTE) owing to  $\pi-\pi$  stacking of the aromatic rings.<sup>4,5</sup> Therefore, a tradeoff exists between light and heat resistance. Multifunctional epoxy resins containing triazine rings have been developed to solve this problem. The triazine ring is known to have a structure

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with high heat resistance,<sup>6,7</sup> and it is expected to have a molecular structure with light and heat resistance. In this study, tris(2,3-epoxypropyl) isocyanurate (TEPIC) was used as a nonaromatic epoxy resin containing a triazine ring. TEPIC is often used as an additive to improve thermomechanical properties. Xie *et al.* used TEPIC as a reactive compatibilizer in a poly(butylene adipate-co-terephthalate) (PBAT)/poly(propylene carbonate) (PPC) blend.<sup>8</sup> The addition of TEPIC has been reported to improve the compatibility of PBAT and PPC, and improve thermal stability, strength, and ductility. Di *et al.* introduced TEPIC into a collagen matrix and reported that the hydrothermal, thermal, and enzyme degradation properties were stabilized by the three-dimensional crosslinked structure formed by reacting with TEPIC.<sup>9</sup> In addition, several modified TEPIC monomers have been developed to improve the handling properties. However, there is room for discussion regarding the thermal and mechanical properties of the cured resins (in which TEPIC is mainly used as a base resin) as well as their mechanisms. A thorough understanding of their properties is necessary to predict accurately and interpret their effects as an additive.

In addition to conventional macroscopic mechanical experiments, interpreting material properties from a microscopic perspective, that is, at the molecular scale, is very powerful. One such method is based on molecular dynamics (MD) simulations. MD simulations have successfully revealed the influence of the molecular structure and functional groups on the polymeric material properties, such as the elastic modulus,<sup>10–12</sup> strength,<sup>13</sup> thermal conductivity,<sup>14–17</sup> thermal stability,<sup>18</sup> rheology,<sup>19</sup> and polymer/solid adhesion.<sup>20,21</sup> Because cured TEPIC resins involve chemical reactions, evaluating both the formation of crosslinks and the mechanical properties of the resin is necessary. Okabe *et al.*<sup>22,23</sup> proposed a reaction model based on quantum chemical calculations for curing MD simulations, which has been extensively used in various resin systems.<sup>24–28</sup> In this study, we explored the cross-linking reaction paths using *ab initio* calculations, simulated the curing reaction, evaluated the mechanical properties of the cured TEPIC resin using MD simulations, and clarified the relationship between the molecular structure and mechanical properties.

The light resistance of transparent resins is strongly related to their optical properties. Aromatic epoxies exhibit high light-absorption properties in the UV-to-visible light range, thus resulting in yellowing effects. Absorption properties are often experimentally determined by ultraviolet visible (UV-vis) spectrophotometry<sup>29</sup> and analytically by UV-vis spectral analysis using quantum chemical calculations.<sup>30</sup> In this study, we performed an *ab initio* UV-vis spectral analysis of TEPIC and conventional aromatic epoxy monomers to identify their absorbance properties.

## 2 Experiments

### 2.1 Material preparation

In this study, three types of TEPIC (Nissan Chemical Corporation) were used as the base resins, as shown in Fig. 1(a). TEPIC-

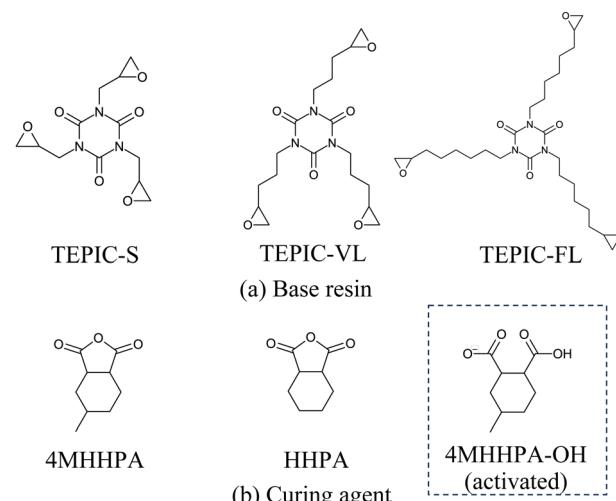


Fig. 1 Base resins and curing agents.

S had a basic structure, whereas TEPIC-VL and TEPIC-FL had longer chains in the epoxy group. The curing agent was MH-700 (New Japan Chemical Co., Ltd), which is a mixture of 4-methyl hexahydrophthalic anhydride (4MHHPA) and hexahydrophthalic anhydride (HHPA) at a 7:3 ratio. HHPA was added to improve the handling properties of the curing agents. In experiments, tetrabutylphosphonium *o,o*-diethylphosphorodithioate (PX-4ET, Nippon Chemical Industrial Co., Ltd) was added as a reaction initiator. Ionized PX-4ET initiated the ring opening of 4MHHPA or HHPA, which in turn initiated the reaction with the epoxy group. PX-4ET was incorporated at the end of the crosslinked structure and did not contribute to the primary structure. The reaction pathways are discussed in detail in a subsequent section.

TEPIC, MH-700, and PX-4ET were weighed at a molar ratio of 1:3:0.006. TEPIC was heated to 130 °C and stirred for 60 min in an oil bath. TEPIC was cooled to 80 °C and MH-700 was added and stirred. PX-4ET was added to the mixture and was then mixed and degassed (70 °C for 15 min) using a planetary centrifugal vacuum mixer (ARV-310P, AR-100; Thinky, Japan). The mixture was poured into a glass mold with a release film and cured in an electric oven. The temperature profile during curing was as follows: heating to 100 °C (1.7 °C min<sup>-1</sup>), holding at 100 °C (2 h), heating to 150 °C (1.7 °C min<sup>-1</sup>), holding at 150 °C (6 h), and cooling in an oven.

Fig. 2 illustrates the specimens used for the tensile tests described below. TEPIC-S and TEPIC-VL were clear, colorless cured resins, whereas TEPIC-FL was slightly yellowish.

### 2.2 Characterization

**2.2.1 Cure characterization.** The cure conversion of the samples was evaluated using Fourier-transform infrared spectroscopy (FTIR, Nicolet iS20, Thermo Fisher Scientific). The spectral peaks of the pentameric rings in MH-700 (1800 cm<sup>-1</sup>) decreased with curing, and the peak of the unchanged triazine ring (1700 cm<sup>-1</sup>) was utilized. The pentameric ring peak intensity  $h_{\text{pentameric}}$  was normalized to the triazine ring peak intensity  $h_{\text{triazine}}$ , and the cure conversion  $\alpha$



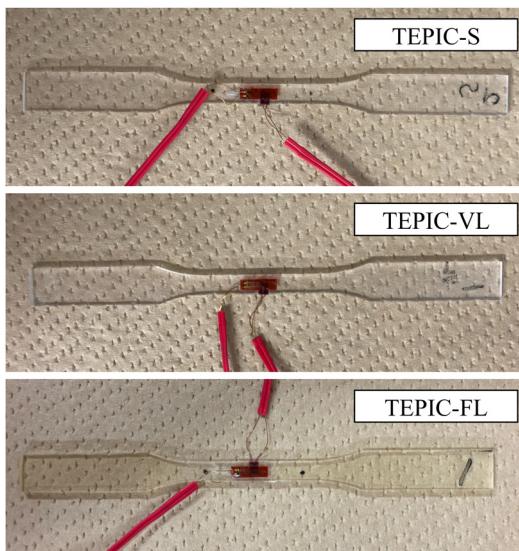


Fig. 2 Cured resin specimens.

was calculated as follows:

$$\hat{h} = \frac{h_{\text{pentameric}}}{h_{\text{triazine}}} \quad (1)$$

$$\alpha = 1 - \frac{\hat{h}_{\text{cured}}}{\hat{h}_{\text{uncured}}} \quad (2)$$

where  $\hat{h}_{\text{cured}}$  and  $\hat{h}_{\text{uncured}}$  are the normalized intensities before and after curing, respectively.

**2.2.2 Mechanical properties.** Uniaxial tensile tests were performed using an Instron 5982 (5 kN) testing machine. The tensile rate was  $1 \text{ mm min}^{-1}$ , in accordance with the standard based on JIS K 7161-2. Strain gauges (Kyowa Electronic Instruments Co., Ltd, Japan) were attached to the dog-bone-shaped specimens (Fig. 2). In addition, the strain was measured using a noncontact video extensometer Instron 2663-902. The tensile test was conducted three times for each resin sample, and the average values were used. Young's modulus was calculated from the slope of the stress-strain curve when the strain was between 0.05% and 0.25%.

Uniaxial compressive tests were performed according to previous studies.<sup>13,31</sup> The sample size was  $2 \text{ mm} \times 5 \text{ mm} \times 5 \text{ mm}$ , and the load was applied along the 2 mm thickness direction at a rate of  $2 \text{ mm min}^{-1}$ . The compressive tests were conducted three times for each resin. An Instron 5982 (100 kN) instrument was used as the testing apparatus. To relieve the friction between the specimen and the platens, polyethylene films were applied on both the front and back surfaces of the specimens.

**2.2.3 Thermal mechanical analysis.** The glass transition temperature ( $T_g$ ) and linear coefficient of thermal expansion (CTE) were measured using thermomechanical analysis (TMA, Hitachi High-Tech TMA7300, Japan), in which the temperature was increased from room temperature to  $T_g + 30 \text{ }^\circ\text{C}$  at a heating rate of  $2 \text{ }^\circ\text{C min}^{-1}$  under nitrogen flow conditions

( $200 \text{ mL min}^{-1}$ ). The sample size was  $2 \text{ mm} \times 10 \text{ mm} \times 10 \text{ mm}$ . Before each run, the sample was preheated to  $T_g + 30 \text{ }^\circ\text{C}$  to remove thermal history.

### 2.3 WAXS measurement

Wide-angle X-ray scattering (WAXS) was used to quantitatively estimate the interior molecular structure. The WAXS measurements were performed at BL08W in NanoTerasu (Miyagi, Japan). 2D-WAXS patterns were recorded using the 2D HPC detector Eiger2 R (Bruker K.K.). WAXS measurement was performed at the camera length of 70 mm, where the calibration was carried out with cerium dioxide.

### 2.4 Free volume evaluation

Positron annihilation lifetime spectroscopy (PALS) is extensively used for probing the free volume of polymeric materials. Positron lifetime histograms were measured using a positron surface analyzer (TOYO SEIKO Co., Ltd),<sup>32</sup> and the mean void diameters were obtained using the Tao-Eldrup model.<sup>33</sup> The sample size is approximately  $2 \text{ mm} \times 15 \text{ mm} \times 15 \text{ mm}$ .

## 3 Numerical methods

### 3.1 *Ab initio* calculation

**3.1.1 Calculation of reaction routes.** Ionized PX-4ET acted as a reaction initiator and did not contribute to the crosslinking structure of the cured resin. Therefore, as shown in Fig. 1(b), activated 4MHHPA-OH, which is ring-opened and terminated with OH at one end, was introduced to investigate the curing reaction route of TEPIC. Herein, 4MHHPA-OH mimicked the ring-opened 4MHHPA by reacting with ionized PX-4ET. The reaction routes are shown in Fig. 3. In the first step of the reaction, the  $\text{COO}^-$  group of activated 4MHHPA-OH reacts with the epoxy group producing  $\text{O}^-$ . In the second step, the  $\text{O}^-$  formed in the first reaction reacts with either unopened 4MHHPA or HHPA to generate  $\text{COO}^-$ . The reaction between the  $\text{COO}^-$  contained in the second reaction product and the epoxy group is considered to be the same as that in the first step of the reaction.

The reaction routes for determining the activation energy and heat of formation were calculated using global reaction route mapping (GRRM),<sup>34-39</sup> an accurate reaction path search package aided by *ab initio* quantum calculations using a Gaussian program. The detailed procedure for the reaction path search using GRRM is summarized in ref. 40. In this study, we assumed a benzene solvent environment using a polarizable continuum model (PCM) in the GRRM calculations,<sup>41</sup> enabling the exploration of reaction routes involving ions, which was performed at the B3LYP/6-31G(d) theory level.

**3.1.2 Calculation of UV-vis absorption spectrum.** UV-vis spectral analysis was performed based on the time-dependent density functional theory (TD-DFT) using the Gaussian16<sup>42</sup> and the GaussView<sup>43</sup> programs. Three TEPIC and a typical aromatic epoxy resin, diglycidyl ether of bisphenol A (DGEBA), were used



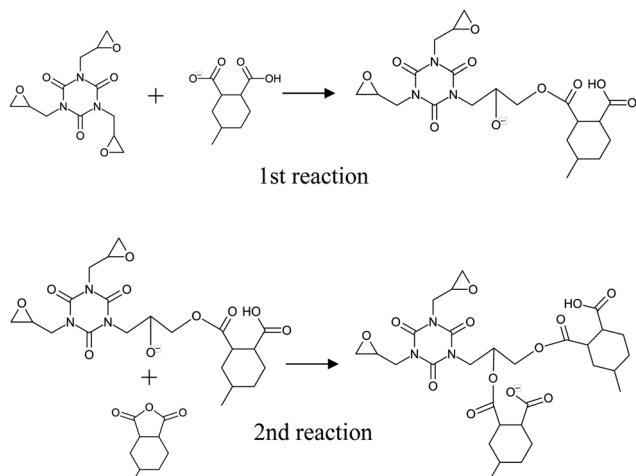


Fig. 3 Schematic of two-step reaction between TEPIC and MH700.

to compare the absorbance properties of the base resins. TEPIC-S, 4MHPA, 4MHPA-OH, and the first reaction product were also analyzed to evaluate the absorbance properties before and after curing. The site  $O^-$  in Fig. 3 was terminated with H to render the activated 4MHPA-OH and the product was neutral to evaluate the properties of the cured resin, excluding the effects of ionization. Each molecule was optimized using DFT at the B3LYP/6-31G(d) level, and excited-state calculations were performed using the TD-DFT method at CAM-B3LYP/cc-pVDZ for 40 excited states.

### 3.2 MD simulations

**3.2.1 Curing simulations.** The molecules were randomly arranged at 423.15 K (150 °C) in an initial simulation box with dimensions of  $300 \text{ \AA} \times 300 \text{ \AA} \times 300 \text{ \AA}$ . The molecular ratio of the base resin to the curing agent was set at 1 : 3. In the case of TEPIC-S, the numbers of molecules of TEPIC-S and the curing agent were 400 and 1200, respectively, and consisted of 680 molecules of 4MHPA, 160 molecules of activated 4MHPA-OH, and 360 molecules of HHPA. The same number of  $\text{Na}^+$  ions was introduced as counter ions as that in the activated 4MHPA-OH to maintain the neutrality of the system. The counter ions did not react with other molecules. Periodic boundary conditions were applied in all the directions. A uniform artificial compression of the simulation box was applied until the density reached  $0.8 \text{ g cm}^{-3}$  at a constant temperature. Subsequently, an NPT simulation was conducted for 200 ps at 423.15 K and 1 atm to obtain an uncured initial state.

The reaction model proposed by Okabe *et al.*<sup>22</sup> was used to perform the curing MD simulation. Two reaction criteria exist: the distance between reaction sites and the reaction probability. When the distance was within the reaction cutoff, this site became a reaction candidate, and 7.3 Å was used as the cutoff based on the minimum distance between the epoxy groups in TEPIC-S. The Arrhenius-type reaction probability  $p$  was determined using the activation energy  $E_a$  and

local temperature  $T_{\text{local}}$  as follows:

$$p = A \exp\left(-\frac{E_a}{RT_{\text{local}}}\right), \quad (3)$$

where  $R$  is the gas constant, and  $A$  is the acceleration constant required to reproduce the cure reactions within a realistic computational time. In this study, to achieve almost the same final cure conversion as the experiments,  $A$  was set to  $10^{16}$ , which is within the range of values used in previous studies.<sup>44,45</sup>

For  $a < p$ , where  $a$  is a generated uniform random number ranging from 0 to 1, a crosslink was formed that justified the occurrence of the reaction. For structural relaxation, minimization by a conjugate gradient algorithm, and NPT (15 ps, 423.15 K, 1 atm), and NVT simulations (1 ps, 423.15 K) were performed. Finally, the atomic velocities among the reacted sites were scaled to remain at  $K_{\text{after}} = K_{\text{before}} + H_f$ , where  $K_i$  is the sum of the kinetic energies before and after the reaction. The curing process was terminated when the curing reaction reached saturation.

In this study, all MD simulations were performed using LAMMPS,<sup>46</sup> and cross-link formation was performed using an in-house Python code. A DREIDING force field<sup>47</sup> was used with Gasteiger atomic charges.<sup>48</sup> Therefore, it is necessary to update the atomic charge during crosslinking. Based on the new bonding structure, only the atomic charges of the atoms around the reaction site were updated, leaving the other charges intact, as shown in Fig. 4. Any excess or deficient charge from the original charge was partially distributed on the carbon atoms of cyclohexane. The van der Waals (vdW) interaction was expressed by the Lennard-Jones potential with a cutoff of 12 Å, and the electrostatic interactions were calculated using the particle-particle particle-mesh method.<sup>49</sup> The reversible reference system propagator algorithm was used for the time integrator<sup>50</sup> using time steps of 0.2 fs (bond and angle) and 1.0 fs (dihedral, improper, vdw, and electrostatic interactions). The NVT and NPT simulations were performed using a Nosé-Hoover chain thermostat and barostat, respectively.<sup>51</sup> For each resin type, five cured systems with different initial arrangements were simulated, and the predicted properties described below are averages of the five systems. The molecular visualizations were produced by the OVITO,<sup>52</sup> and Marvin<sup>53</sup> was used for drawing the chemical structures.

**3.2.2 Evaluation of mechanical properties.** A sufficiently cured resin model was annealed at 300 K.<sup>16,54</sup> Young's modulus and Poisson's ratio were evaluated using a uniaxial tensile simulation with a strain rate of  $5 \times 10^8 \text{ s}^{-1}$ . The values were calculated by linear fitting of the stress-strain and strain-strain curves up to 3%. Tensile failure of thermoset resins is generally caused by localized dilatation due to internal defects and inhomogeneities. Therefore, the deformation modes of uniaxial tensile simulations of homogeneous MD systems are strictly different from the actual deformation modes leading to failure. In this study, the failure behavior was not discussed using uniaxial tensile simulations, and the strength was predicted using the following approach.

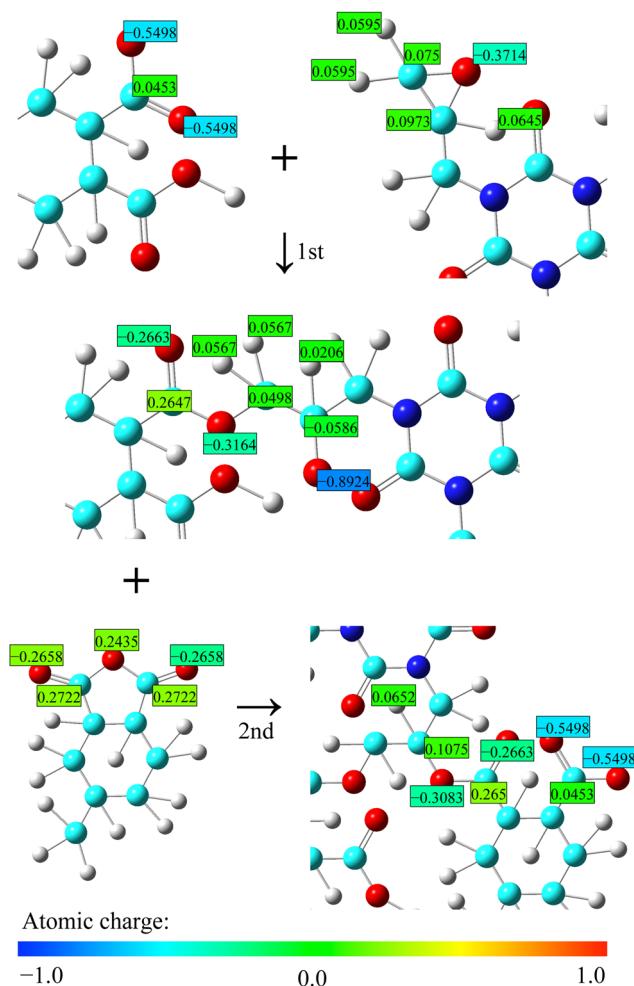


Fig. 4 Schematics of atomic charge update.

In general, the strain rate in the MD simulations is quite large compared to the experimental strain rate. Therefore, the strength is overestimated by the rheological behavior of the resin in the MD simulations at high strain rates. Therefore, in this study, the uniaxial tensile/compressive strength was evaluated using the approach proposed by Watanabe *et al.*<sup>13</sup> In this approach, the strengths were estimated by combining uniaxial compressive, triaxial tensile, and quasistatic uniaxial tensile simulations, Argon theory,<sup>55–57</sup> and Christensen's failure criterion.<sup>58,59</sup>

The brittle/ductile failure behavior of the resins can be described using Christensen's criterion as follows,

$$3 \left( 1 - \frac{T}{C} \right) \hat{\sigma}_m + \hat{\sigma}^2 \leq \frac{T}{C} \quad (4)$$

where  $T$  and  $C$  are the tensile and compressive strengths, respectively, and  $\hat{\sigma}_m = \sigma_m/C$  and  $\hat{\sigma} = \bar{\sigma}/C$  are the hydrostatic and von Mises stresses, respectively, which are nondimensionalized by  $C$ . Materials with a larger  $T/C$  exhibit a more ductile behavior. When hydrostatic loading leads to resin

failure,  $\sigma_m = \sigma_m^y$ ,  $\hat{\sigma} = 0$ , and eqn (4) is transformed as follows:

$$\frac{T}{C} = \frac{3\sigma_m^y}{C + 3\sigma_m^y} \quad (5)$$

where  $\sigma_m^y$  denotes the triaxial tensile yield stress. From uniaxial compressive and triaxial tensile simulations,  $C$  and  $\sigma_m^y$  can be estimated. Although these strength values include a strain-rate dependence, the ratio  $T/C$  is known to be independent of the temperature and strain rate; therefore, the strengths from the MD simulations can be directly used to estimate the ratio  $T/C$  using eqn (5).

The compressive strength  $C$ , excluding the strain rate dependence at arbitrary temperatures, is expressed by the following equation:

$$C(T) = aT_{\text{system}} + C_{0\text{K}} \quad (6)$$

where  $T_{\text{system}}$  is the system temperature and  $a$  represents the slope of the compressive strength-temperature linear relation obtained from uniaxial compressive simulations at different temperatures. Using Argon theory, the compressive strength excluding the strain rate dependency at 0 K is given by

$$C_{0\text{K}} = \frac{0.077\sqrt{3}E_{0\text{K}}}{2(1 - \nu_{0\text{K}})(1 + \nu_{0\text{K}})} \quad (7)$$

where  $E_{0\text{K}}$  and  $\nu_{0\text{K}}$  are, respectively, Young's modulus and Poisson's ratio at 0 K obtained using the quasistatic uniaxial tensile simulation. By multiplying  $C$  excluding the strain-rate dependence obtained from eqn (6) by the ratio  $T/C$  in eqn (5), we can indirectly estimate the tensile strength  $T$  excluding the strain-rate dependence. For the detailed settings for each simulation, please refer to ref. 13.

**3.2.3 Evaluation of thermal properties.** The linear CTE and glass transition temperature  $T_g$  were evaluated using a heating/cooling simulation in the NPT ensemble. The system was heated to 700 K and then cooled from 700 to 200 K in 20 K intervals. Equilibration for 500 ps was performed at each temperature, and the temperature–volume relationship was obtained. The linear CTE in the glassy and rubbery states were calculated from two linear fittings of the temperature–volume relationship and  $T_g$  from their intersections.

**3.2.4 Evaluation of structural properties.** To evaluate the atomic-scale structures, we computed the partial radial distribution functions<sup>60,61</sup>  $g_{\alpha\beta}(r)$  of the cured resins after annealing.

$$g_{\alpha\beta}(r) = \frac{N_{\alpha\beta}(r)}{4\pi r^2 n_{\beta} dr} \quad (8)$$

where  $N_{\alpha\beta}(r)$  is the number of pairs between species  $\alpha$  and  $\beta$  within the distance range from  $r$  to  $r + dr$ , and  $n_{\beta}$  is the average number density of species  $\beta$ .

The coherent scattering intensity,  $I_{\text{coh}}$ , can be calculated by using the Fourier transformation of the partial radial



distribution functions as follows:<sup>60,61</sup>

$$\frac{I_{\text{coh}}(q)}{N} = \sum_{i=1}^n c_i f_i^2(q) + \sum_{i=1}^n \sum_{j=1}^n c_i c_j f_i(q) f_j(q) n_0 \int_0^\infty 4\pi r^2 (g_{ij}(r) - 1) \frac{\sin qr}{qr} dr \quad (9)$$

where  $N$  is the total number of atoms,  $c_i = N_i/N$  is the atomic fraction of the  $i$ th species,  $f_i(q)$  is the atomic scattering factor in X-ray scattering,<sup>62</sup>  $n_0$  is the average total number density, and  $q = 4\pi \sin \theta/\lambda$  is the length of the scattering vector  $\mathbf{q}$ , where  $\lambda$  is the wavelength of the incident radiation and  $2\theta$  is the diffracted radiation.

In addition, the free volume of a thermoset resin is an important factor that determines its microscopic structural and mechanical properties.<sup>63–65</sup> In the MD simulations, the free volume was calculated using the algorithm proposed by Li and Strachan.<sup>65</sup> The simulation box was divided into cubic grids with a cell size of 0.5 Å. If the  $\alpha$ th grid point satisfies the following equation for all atoms, then this grid is included in the free volume.

$$|\mathbf{r}_\alpha - \mathbf{r}_i| > (D_p - D_i^{\text{vdW}})/2 \quad (10)$$

where  $i$  denotes all the atoms, and the left-hand side represents the distance between the  $\alpha$ th grid and the  $i$ th atom. The probe diameter  $D_p$  is set to 2.8 Å, which is a typical value for a water molecule. The vdW diameter  $D_i^{\text{vdW}}$  of the  $i$ th atom was obtained from the DREIDING force field. After obtaining the free-volume grids, cluster analysis was performed for all free-volume grids with respect to connectivity to quantify the void cluster.

## 4 Results and discussion

### 4.1 Optical properties

Fig. 5(a) shows the calculated UV-vis spectrum and the highest oscillator strength for the conventional aromatic epoxy (DGEBA) and the three types of TEPIC. The most intense electronic transitions for DGEBA, TEPIC-S, TEPIC-VL, and TEPIC-FL occur at 185.58 nm, 169.09 nm, 168.16 nm, and 168.82 nm, respectively. No peaks were observed in the visible-light region (380–780 nm) in any of the resin types. The aromatic epoxy, DGEBA, exhibited broad and intense peaks in the UV region. In contrast, all three TEPIC resins exhibited low absorbances in the UV region, and the maximum oscillator strengths were smaller than that of DGEBA.

Fig. 6 visualizes the molecular orbital (MO) of the main conformation in the excited state at the maximum oscillator strength for DGEBA and TEPIC-S. In DGEBA, the benzene ring is excited at a wavelength of 185.58 nm and the number of nodal planes in MO at the benzene rings increases upon electron excitation. In TEPIC-S, the triazine ring is excited at a wavelength of 169.09 nm. These results suggest that the

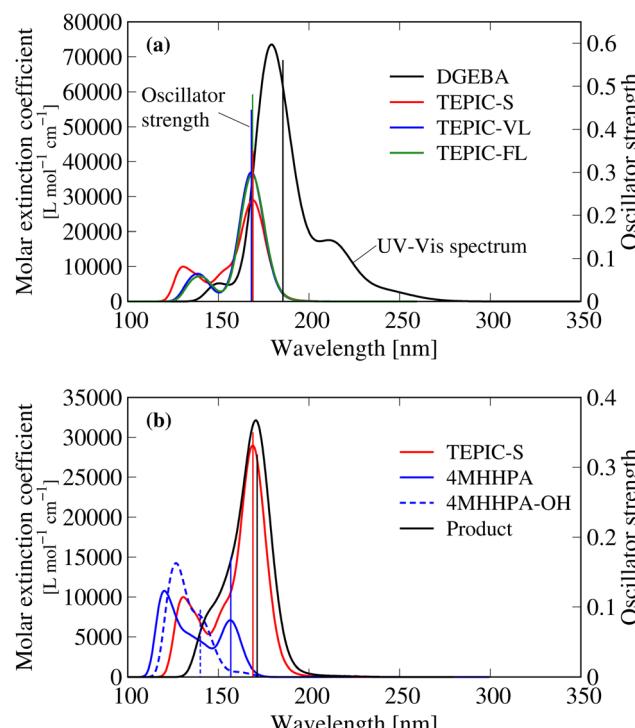


Fig. 5 Calculated ultraviolet-visible spectrum. (a) Conventional aromatic epoxy (DGEBA) and three types of TEPIC resins. (b) Reactants and product.

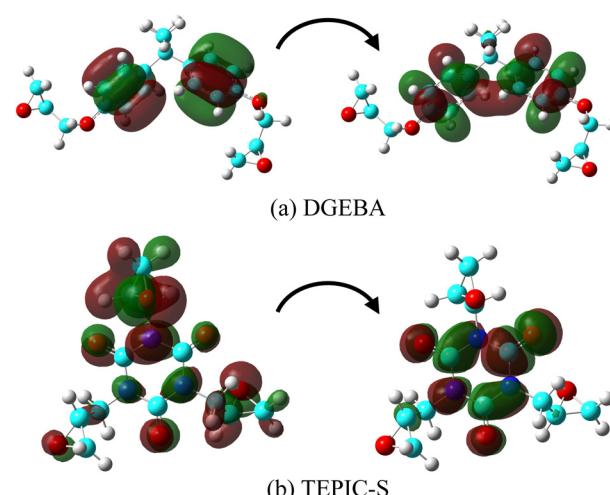


Fig. 6 Main configuration MO of the excited state at maximum oscillator strength for (a) DGEBA and (b) TEPIC-S.

triazine ring of TEPIC is less easily excited by UV light than the benzene ring of aromatic epoxy and has high light resistance.

Fig. 5(b) shows the results of the reactants and product. All the base resins, curing agents, and product molecules have low light absorption properties; thus, the spectral analysis suggests that the HHPA-cured TEPIC resin considered here has high transparency and light resistance.

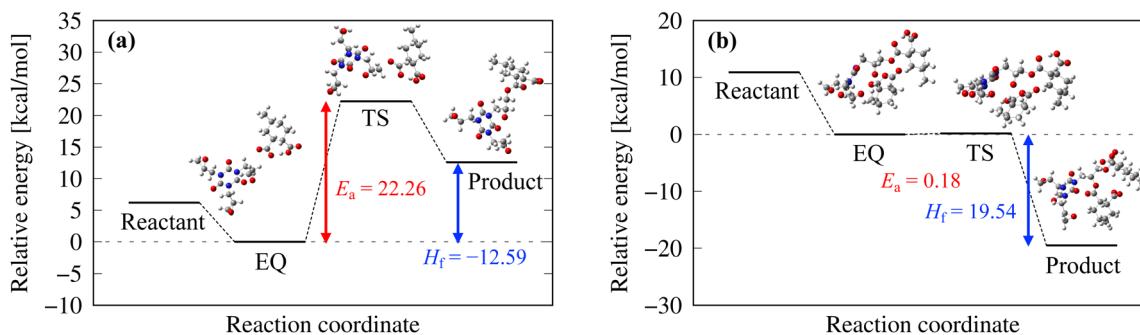


Fig. 7 Reaction pathways and reaction energies of the (a) first and (b) second reactions.

#### 4.2 Curing reaction properties

Fig. 7 shows the pathways for the first and second reactions as shown in Fig. 3. For the first reaction between the epoxy group and  $\text{COO}^-$ , the activation energy was  $22.26 \text{ kcal mol}^{-1}$  (with zero-point energy correction at 0 K) and the heat of formation was  $-12.59 \text{ kcal mol}^{-1}$ , which indicates an endothermic reaction. For the second reaction between  $\text{O}^-$  and 4MHPA, the reaction barrier barely appears and the heat of formation is  $19.54 \text{ kcal mol}^{-1}$ , indicating an exothermic reaction. Therefore, it is an exothermic reaction when considered as a three-molecule system with a two-step reaction pathway. These reaction properties were incorporated into the curing MD simulations using eqn (3).

#### 4.3 Thermomechanical properties

The thermomechanical properties of the cured resins were discussed from both experimental and simulation perspectives. Fig. 8 shows the stress-strain curves obtained in the unitensile experiment. For TEPIC-S and VL, the strain was obtained from strain gauges, and for TEPIC-FL, the strain was obtained from a video extensometer. In particular, brittle-ductile properties differed significantly depending on the length of the side chains. TEPIC-FL had approximately 80% of the strength of TEPIC-S, whereas the failure strain increased to almost three times that of TEPIC-S, making it a ductile material.

Table 1 summarizes the thermomechanical properties obtained from experiments and MD simulations. Failure strain

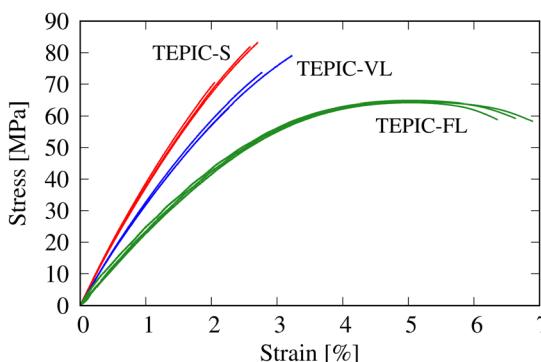


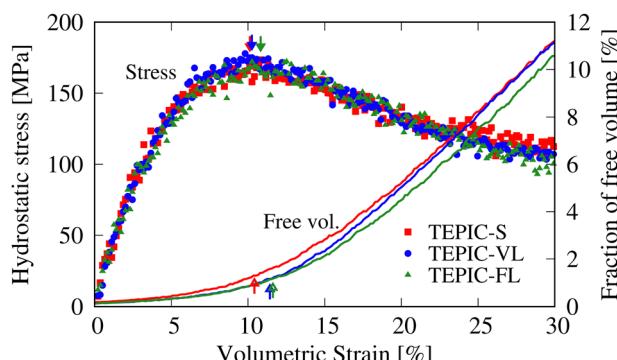
Fig. 8 Stress-strain curves in the unitensile experiment.

values were not available for the MD simulations because the uniaxial tensile strength was not determined directly. The cure conversion and crosslink densities are listed in Table 1. Only the values obtained from the MD simulations are shown for the crosslink density. The characteristics predicted from the MD simulations were in qualitative agreement with the experiments, and quantitative agreement was also confirmed for many items, thus confirming the validity of the simulations.

The stiffness and strength decreased at increasing side-chain lengths. This is because the crosslink density decreases as the side chains become longer, which is consistent with the trend observed in a previous study conducted with different resin types.<sup>45</sup> Conversely, predicted and experimental  $T/C$  show that ductility increases with increasing side-chain length. This corresponds to the experimental results for the failure strain. Fig. 9 shows the hydrostatic stress-volumetric strain curve and the change in the free volume fraction in the triaxial tensile simulation averaged over the five cases for each resin. The downward arrows indicate the strain values at yielding, that is, peak stress; additionally, the upward arrows indicate the strain values at the inflection point of the free volume fraction changes, which were determined as the intersection of two linear fittings in the strain ranges of 0–3% and 15–18%. The stress-strain curve peaks when the free volume rapidly

Table 1 Summary of the thermomechanical properties obtained from MD simulations and experiments. Young's modulus  $E$ , Poisson's ratio  $\nu$ , tensile strength  $T$ , compressive strength  $C$ , ductility  $T/C$ , failure strain, glass transition temperature  $T_g$ , CTE in glassy state, cure conversion, and crosslink density

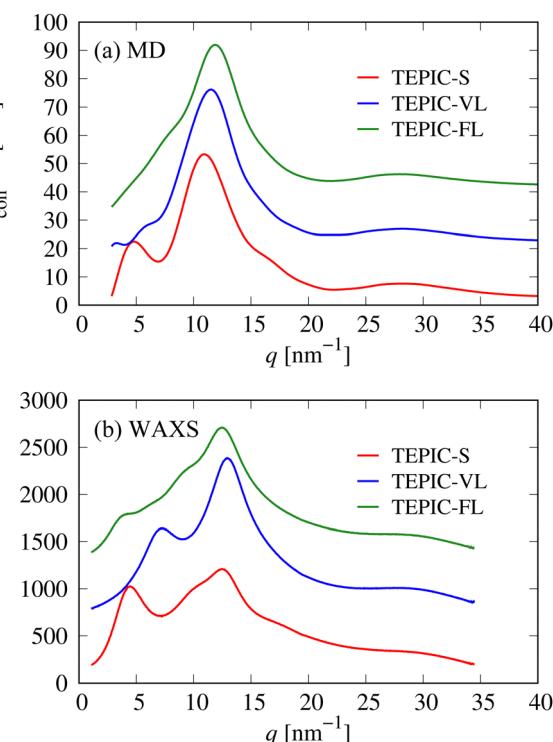
|   | TEPIC-S |       | TEPIC-VL |       | TEPIC-FL |      |
|---|---------|-------|----------|-------|----------|------|
|   | MD      | Exp.  | MD       | Exp.  | MD       | Exp. |
| $E$ [GPa]   | 3.40    | 4.09  | 3.33     | 3.50  | 3.12     | 2.75 |
| $\nu$ [—]   | 0.31    | 0.34  | 0.31     | 0.35  | 0.33     | 0.37 |
| $T$ [MPa]   | 112.8   | 76.5  | 98.3     | 76.4  | 82.9     | 64.4 |
| Failure strain [%]  | —       | 2.45  | —        | 3.00  | —        | 6.64 |
| $C$ [MPa]   | 185.6   | 164.4 | 154.0    | 138.6 | 129.4    | 90.0 |
| $T/C$   | 0.60    | 0.47  | 0.63     | 0.55  | 0.64     | 0.72 |
| $T_g$ [°C]  | 193.6   | 194.9 | 152.7    | 146.7 | 120.3    | 92.4 |
| CTE [ $10^{-6} \text{ }^{\circ}\text{C}^{-1}$ ]                 | 73.0    | 62.4  | 80.3     | 64.9  | 85.0     | 82.2 |
| Cure conversion [%]   | 90.1    | 95.9  | 88.8     | 89.3  | 89.4     | 93.4 |
| Crosslink density [ $\times 10^{-3} \text{ } \text{\AA}^{-3}$ ] | 2.28    | —     | 1.94     | —     | 1.61     | —    |



**Fig. 9** Stress–strain curves and free volume fraction changes in triaxial tensile simulations. The downward arrows indicate strain values at yielding and the upward arrows indicate strain values at the inflection point estimated from two linear fittings.

increases and at the time of coalescence. Fig. 10 shows snapshots of the free volume distributions of the three resin types at the same strain level (10.5%). The white areas in the snapshots represent the free volume. In addition, the fraction of free volume and the maximum diameters of the volume-equivalent spheres of each free-volume cluster are shown. In TEPIC-S with shorter side chains, the free volume was relatively connected, and both the free volume fraction and maximum diameter were large. In contrast, for TEPIC-FL with longer side chains at the same deformation, the free volume was dispersed, and the free volume fraction and maximum diameter were small. Longer side chains suppress the free volume growth under triaxial deformation conditions. In many thermoset resins, tensile fracture is initiated by void growth owing to localized triaxial stress. The suppression of free volume growth by long side chains, confirmed by simulations, supports the brittle–ductile properties of the mechanical experiments.

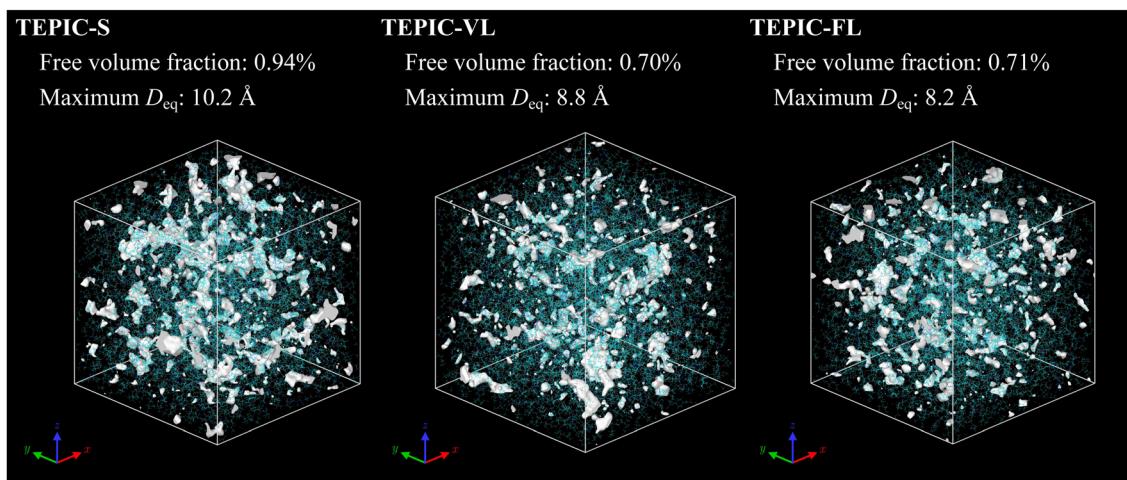
The longer the side chain, the lower the  $T_g$ , and the higher the CTE. Because  $T_g$  and CTE are also highly dependent on the crosslink density, the side-chain elongation results in a decrease in the thermal properties of TEPIC.



**Fig. 11** Comparison of X-ray scattering intensities of three types of resins obtained from (a) MD simulations and (b) WAXS.

#### 4.4 Structural properties

In this section, the structural properties (in the absence of deformation) are discussed. Fig. 11 shows the comparison of scattering intensities obtained from the MD simulations and WAXS measurements. The intensity patterns of TEPIC-S exhibits three peaks at approximately  $q = 5, 10$ , and  $30 \text{ nm}^{-1}$ ; this trend is the same as that of conventional amine-cured aromatic epoxy resins such as DGEBA/DETA.<sup>25,66</sup> In the amine-cured epoxy resin, the first peak represents the locally ordered structure in the resin, which is attributed to two-dimensional growth, in which resins start to form linear structures and then



**Fig. 10** Snapshots of free volume distributions of three resin types at the same strain level in triaxial tensile simulations.

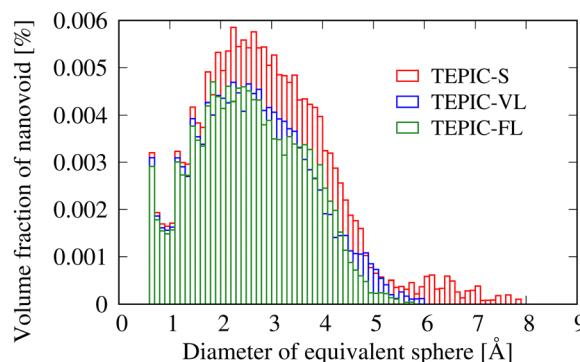


Fig. 12 Size distributions of the free volumes of three types of resins in terms of the diameters of the volume-equivalent spheres.

branched structures at the amine groups. Although TEPIC-S has a branched structure, it also has a rigid two-dimensional molecular structure based on triazine rings with short side chains. This two-dimensional structure was crosslinked by a curing agent; this resulted in the appearance of the same peak, which originated from the growth process, as that of conventional epoxy resins. Conversely, the first peak became smaller for TEPIC-VL, which has a moderately long side chain and almost disappeared for TEPIC-FL, which has the longest side chain. This may be because the TEPIC monomer with longer side chains can easily form an appropriate three-dimensional structure and does not undergo two-dimensional cross-link growth. The peaks around  $q = 10\text{--}15\text{ nm}^{-1}$  are typical amorphous halos attributed to intermolecular correlations. The peak positions and peak decreasing trends of the scattering intensities are consistent between the MD simulations and WAXS, which indicates that the structures of the cured resin models for the three types of resin modeled in the MD simulations are reasonable.

Fig. 12 shows the size distributions of the free volumes of the three types of resins. The abscissa represents the diameter of the volume-equivalent sphere of the free-volume cluster. Table 2 shows the fraction of the free volume and volume average equivalent diameter obtained from the MD simulations and the void diameter measured by PALS. Note that the free volume values obtained from the MD simulations are strongly dependent on the probe diameter used; therefore, a qualitative comparison was made. The PALS and MD simulations are in agreement, with the free volume decreasing as the side chains become longer, and their average sizes decreasing. As the monomer size increases, the free volume during curing has been reported to increase.<sup>44,63</sup> This is because larger monomer

Table 2 Summary of the free volume analysis. Fraction of free volume and volume average equivalent diameter obtained in MD simulations and void diameter measured by PALS

| Type     | Fraction (MD) [%] | Diameter (MD) [Å] | Diameter (PALS) [Å] |
|----------|-------------------|-------------------|---------------------|
| TEPIC-S  | 0.176             | 2.89              | $5.44 \pm 0.07$     |
| TEPIC-VL | 0.135             | 2.64              | $5.28 \pm 0.06$     |
| TEPIC-FL | 0.130             | 2.59              | $5.27 \pm 0.06$     |

molecules have greater steric hindrance. However, as mentioned earlier, in the case of TEPIC, the soft side chains reduce the effect of steric hindrance, resulting in the opposite trend. This could be a new guideline for molecular design to reduce the free volume.

## 5 Conclusions

In this study, the optical, thermomechanical, and structural properties of the triazine ring-based nonaromatic epoxy resin TEPIC were experimentally and numerically evaluated. Three resins with different side-chain lengths were used: TEPIC-S, TEPIC-VL, and TEPIC-FL. UV-vis spectral analysis using TD-DFT demonstrated that TEPIC had a lower UV absorbance and higher light resistance than conventional aromatic epoxy resins. Evaluation of the thermomechanical properties using both experiments and MD simulations revealed that shorter side chains resulted in higher stiffness, strength, and heat resistance, indicating the brittle nature of the resin. The MD simulations showed that longer side chains suppressed void growth under triaxial deformation that constitutes the starting point of failure and improved the ductility of the resin. In addition, structural properties were evaluated using MD simulations, WAXS, and PALS. Longer side chains (*i.e.*, larger molecular sizes) had denser molecular structures and lower free volumes; this contrasts with the conventional trend. These findings are expected to aid in the understanding of the features of nonaromatic epoxy resins at the molecular scale and promote the development of high-performance resins for advanced electronic components.

## Data availability

The code for LAMMPS and curing python code can be found at <https://www.lammps.org/#gsc.tab=0> and <https://www.cosmic.plum.mech.tohoku.ac.jp/>, respectively.

## Conflicts of interest

The authors declare no conflicts of interest.

## Acknowledgements

This research was supported by the Japan Society for the Promotion of Science KAKENHI grant (Grant Number 21K14415 and 23H01291). Numerical simulations were performed using the “AFI-NITY” supercomputer system at the Advanced Fluid Information Research Center, Institute of Fluid Science, Tohoku University and supercomputing resources at Cyberscience Center, Tohoku University. We would like to express our gratitude to all the members of QST NanoTerasu Center and PhoSiC for their support in utilizing NanoTerasu.



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