



# Origin of anisotropic thermal transport in CsPbBr<sub>3</sub>†

 Wilarachchige D. C. B. Gunatilleke,<sup>id</sup>\* Oluwagbemiga P. Ojo<sup>id</sup> and George S. Nolas<sup>id</sup>

 Cite this: *Chem. Commun.*, 2024, 60, 14200

 Received 27th September 2024,  
 Accepted 6th November 2024

DOI: 10.1039/d4cc05037a

[rsc.li/chemcomm](https://rsc.li/chemcomm)

**We reveal the specific structural and bonding features that result in anisotropic thermal transport for CsPbBr<sub>3</sub> by directional single-crystal measurements and elucidate the bases for the low Debye temperature and speed of sound. This work enhances the research on perovskites and reveals the structural features governing the thermal properties.**

Perovskites are a broad class of materials with different structure types and compositions, and continue to be of scientific interest as well as of technological importance for a diverse range of applications including solar-cell absorbers,<sup>1–3</sup> photocatalysts for solar water splitting,<sup>4,5</sup> nonlinear optics,<sup>6,7</sup> radiation detection,<sup>8,9</sup> topological insulators,<sup>10</sup> thermoelectrics,<sup>11</sup> magneto-optic and magneto-ferroics.<sup>12,13</sup> This is primarily due to continued advances in synthetic chemistry and characterization techniques that allow for an understanding of the structure–property relationships that govern the different physical properties of interest.

In advancing our fundamental understanding of the perovskite materials currently of interest, whether reports of new materials with superior properties have been published or if advances towards device development have been initiated, an in-depth understanding of the thermal properties is of paramount importance for any application of interest.<sup>14,15</sup> Moreover, specific structural features and related scattering mechanisms can directly affect the thermal properties of crystalline solids. For example, a complex lattice accommodating many atoms, and atoms of differing size and mass, will affect the thermal transport.<sup>16,17</sup> Anharmonic processes associated with the crystal structure are intrinsic to the lattice and directly affect bonding and therefore thermal properties.<sup>18–20</sup> Directional and structural variations can also significantly affect thermal properties.<sup>18</sup> Thus, an understanding of such effects is essential in developing a fundamental understanding of the thermal properties of any crystalline solid.

The perovskite CsPbBr<sub>3</sub> has been investigated as a high-performance radiation detector.<sup>21,22</sup> It has also been reported to possess low thermal conductivity above room temperature making it of interest for thermoelectric applications.<sup>23,24</sup> This is not surprising, given the heavy constituent atoms as well as soft modes that contribute to enhanced phonon scattering within the crystal lattice.<sup>25</sup> Nevertheless, an in-depth investigation of the thermal properties and understanding the anisotropic thermal transport, not previously reported to the best of our knowledge, has not been undertaken. Herein we investigate the thermal properties of single-crystal orthorhombic (*Pnma*) CsPbBr<sub>3</sub>. In addition to analysis of the directional temperature-dependent thermal conductivity,  $\kappa$ , we investigate and model the specific heat,  $C_p$ , and evaluate the Debye temperature,  $\theta_D$ , speed-of-sound,  $v$ , and anharmonicity in providing insight into the origins of the thermal properties as well as the structural and bonding features that result in the anisotropic thermal transport and ultra-low thermal conductivity this material possesses. There have been several theoretical investigations regarding the origins of the lattice anharmonicity in CsPbBr<sub>3</sub>, and we utilize this work in our analyses. Nevertheless, these theoretical investigations utilize  $\kappa$  data from CsPbBr<sub>3</sub> nanowires,<sup>26</sup> and in this work, directional single-crystal thermal transport was investigated to determine the anisotropic  $\kappa$  and anharmonicity in addition to the intrinsic thermal properties of this material.

The perovskite crystal structure of CsPbBr<sub>3</sub> (Fig. 1) consists of chains of corner sharing Pb–Br<sub>1</sub>Br<sub>2</sub>Br<sub>4</sub> octahedra rotated on the *a*–*b* plane and tilted out-of-phase away from the *c*-axis compared to the tetragonal phase that exists above 361 K,<sup>27</sup> providing CsPbBr<sub>3</sub> with unique structural and vibrational properties as described below.<sup>28</sup> The arrangement of Pb–Br–Pb chains forms a three-dimensional network of anion cages that consists of corner sharing octahedra capable of encompassing Cs<sup>+</sup> in an environment formed by four Br1 and eight Br2. The Cs atoms are loosely bonded to Br with highly varying bond distances and occupy the void spaces between the octahedra with strong polar covalent bonds between Pb and Br.<sup>29</sup> Such an arrangement may result in significant bonding heterogeneity.

Department of Physics, University of South Florida, Tampa, FL 33620, USA.

 E-mail: [gnolas@usf.edu](mailto:gnolas@usf.edu)

 † Electronic supplementary information (ESI) available. See DOI: <https://doi.org/10.1039/d4cc05037a>

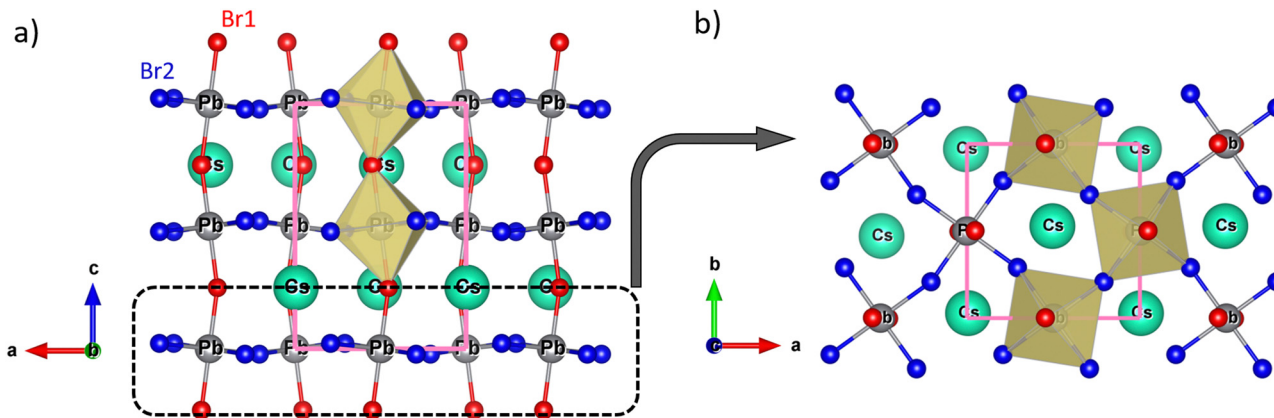



Fig. 1 Crystal structure of CsPbBr<sub>3</sub> highlighting the (a) out-of-phase tilting and (b) in-phase tilting of PbBr<sub>6</sub> octahedra. The unit cell is marked with a solid pink line.

Furthermore, the out-of-phase tilting of the octahedra will influence the thermal properties of CsPbBr<sub>3</sub> under different temperature regimes. Moreover, the octahedral tilting increases with decreasing temperature and the structure distortion due to octahedral rotation results in negative thermal expansion of the *b* lattice parameter of the unit cell.<sup>30</sup> Below 10 K the structure distortion reaches a limit in the octahedral rotation, thus an inconsistent variation of the lattice constants is observed.<sup>30</sup>

Fig. 2 shows the directions of  $\kappa$  measurements with respect to the crystal structure and associated crystallographic planes. The Pb–Br1–Pb chains lie on the *a*–*c* plane, that is perpendicular to the (204) plane, as shown in Fig. 1(a). However, the Pb–Br2–Pb chains do not lie on the same plane. The out-of-phase tilting of PbBr<sub>6</sub> octahedra away from the *c*-axis leads to tilting of the Pb–Br2–Pb chains above and below the *a*–*b* plane, *i.e.*, 18.78°–29.73° away from the (204) plane. As shown in Fig. 3, there is large anisotropy in  $\kappa$  with an increase in the anisotropy in  $\kappa$  along the measured directions at lower temperatures, *i.e.*,  $\kappa$  measured parallel to (204) is significantly higher than that along the direction perpendicular to (204). This suggests that the Pb–Br1–Pb chains (characterized by out-of-phase tilted PbBr<sub>6</sub> octahedra) play an important role in thermal transport

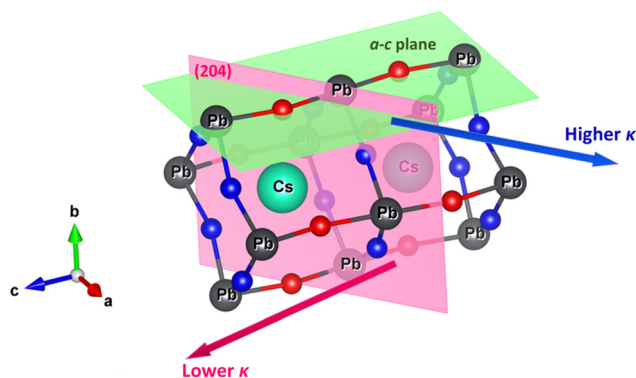


Fig. 2 Orientation of the (204) crystallographic plane with respect to the crystal structure of CsPbBr<sub>3</sub> and the directions of the measurements of  $\kappa$ .

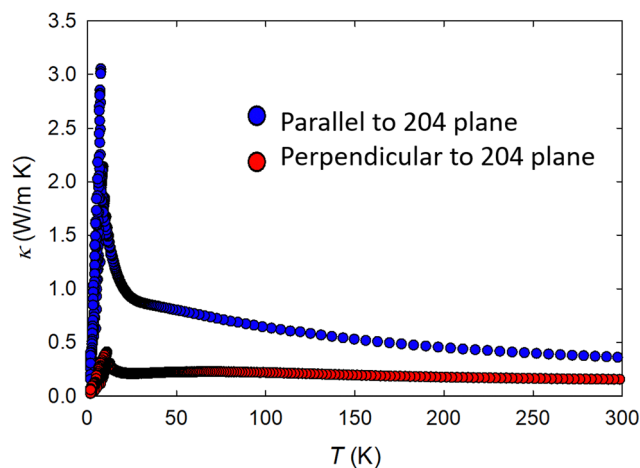


Fig. 3 Temperature dependent  $\kappa$  data parallel (blue) and perpendicular (red) to the (204) plane.

perpendicular to the (204) plane resulting in ultra-low  $\kappa$  while Pb–Br2–Pb chains dominate that parallel to the (204) plane (characterized by in-phase tilted PbBr<sub>6</sub> octahedra) leading to comparatively higher  $\kappa$ . Very recently it was reported that the low frequency modes that correspond to out-of-phase tilting of the PbBr<sub>6</sub> octahedra are at a significantly lower frequency range than those that correspond to in-plane-tilting.<sup>28</sup> This correlates with the lower  $\kappa$  values perpendicular to the (204) plane at low temperatures, and is attributable to enhanced phonon scattering by these low frequency modes resulting from the out-of-phase tilting of the octahedra. At higher temperatures, particularly near room temperature, there exists anisotropy in thermal transport along both directions. However, the effect of low-frequency modes on thermal transport at high temperatures may not be as dominant as they are at low temperatures. Our structural analyses (see ESI†) provide insight to the observed anisotropy in thermal properties. These results emphasize the importance of thermal displacement of the octahedral framework at high temperatures on the thermal transport, and are in agreement with the analyses by Songvilay *et al.*<sup>31</sup> At 300 K the



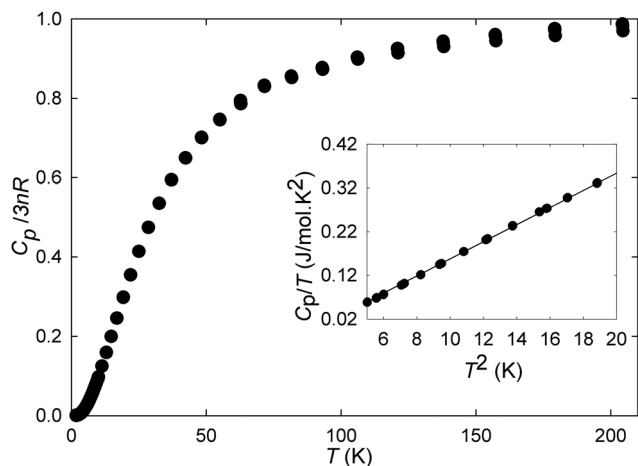


Fig. 4 Temperature dependent  $C_p$  data. The inset shows the low temperature data fit of the for  $C_p/T$  vs.  $T^2$ .

anisotropic atomic displacement parameters,  $U_{ij}$ , for Br1 and Br2 are significantly large along certain directions compared to the other directions. Specifically, the  $U_{11} = 0.141$  (7) Å and  $U_{22} = 0.163$  (7) Å for Br1 correspond to atomic displacements along the  $ab$ -plane that are significantly larger than the atomic displacements on the  $c$ -axis ( $U_{33} = 0.0282$  (25)). In contrast,  $U_{11} = 0.072$  (29) Å and  $U_{22} = 0.0687$  (30) Å for Br2 are smaller than  $U_{33} = 0.122$  (4) Å indicating larger atomic displacements along the  $c$ -axis compared to those along the  $ab$ -plane. However, the difference between  $U_{33}$  and  $U_{11}$  or  $U_{22}$  for Br2 is not as large as that for Br1, leading to ultra-low  $\kappa$  perpendicular to the (204) plane. Nevertheless, the relatively large  $U_{ij}$  values for Br2 result in low  $\kappa$  parallel to (204) plane, as shown in Fig. 3.

To further investigate the thermal properties of CsPbBr<sub>3</sub>, we investigated temperature dependent  $C_p$ , as shown in Fig. 4. The  $C_p$  data approach the Dulong–Petit limit above 100 K indicating that the majority of acoustic and optic mode frequencies are excited at this relatively low temperature. The solid line in the inset of Fig. 4 is a linear fit to the low temperature data, modeled by the equation  $C_p = \alpha T + \beta T^3$ , where the first and second terms represent the Sommerfeld coefficient and the lattice contribution, respectively.<sup>32</sup> Using the relation  $\theta_D = (12\pi^4 R n_a / 5\beta)^{1/3}$ ,  $\theta_D$  can be determined from the low temperature  $C_p$  data, where  $n_a$  is the number of atoms per formula unit and  $R$  is the universal gas constant. A value of 80 K for  $\theta_D$  was obtained from the data fit. The average speed of sound ( $v = 914$  m s<sup>-1</sup>) was obtained using the relation  $\theta_D = v(h/k_B)(3n_a N_a d / 4\pi M_w)^{1/3}$ , where  $h$  is Planck's constant,  $k_B$  is the Boltzmann constant,  $N_a$  is Avogadro's constant,  $d$  is the density, and  $M_w$  is the molecular weight. The value for  $v$  is low, in reasonable agreement with a previously reported value,<sup>33</sup> and is indicative of the weak bonding interactions within the crystal-line lattice possibly due to the tilting of the PbBr<sub>6</sub> octahedra leading to asymmetric bonding around the cation sites. For insulators or large bandgap semiconductors where the lattice contribution to  $\kappa$  dominates phonon transport,  $\kappa$  is related to the Grüneisen parameter,  $\gamma$ , by  $\kappa = BMv^{1/3}/\theta_D^3/n^2/3\gamma^2T$ , where  $B = 2.43 \times 10^{-8}/(1-0.514/\gamma + 0.228/\gamma^2)$ ,  $M$  is the average mass of

an atom in the crystal (amu),  $V$  is the volume of the unit cell,  $n$  is the number of atoms per primitive cell, and  $T$  is absolute temperature.<sup>34–36</sup> The obtained room temperature  $\gamma$  values of 2.13 and 1.38 perpendicular and parallel to (204) plane, respectively, indicate large anisotropy in the anharmonicity. *Ab initio* simulations performed by Sadok *et al.*<sup>37</sup> indicated large anisotropy between the longitudinal and transverse speed of sound in CsPbBr<sub>3</sub>. This anisotropy in lattice anharmonicity due to the in-plane and out-of-plane tilting of PbBr<sub>6</sub> octahedra, as well as the weak interactions of the Cs cations within the voids of PbBr<sub>6</sub> octahedral sublattice,<sup>37</sup> can lead to the anisotropic properties in the lattice.

In summary, a large single crystal, grown from the melt using optimized Bridgman growth conditions, was used to investigate the origins of anisotropic thermal transport in CsPbBr<sub>3</sub>. The  $\kappa$  measured in the parallel and perpendicular directions relative to the (204) plane indicated large anisotropy in the thermal transport. The difference in  $\kappa$  along the two directions significantly increases at lower temperatures. The alignment of Pb–Br1–Pb chains predominantly perpendicular to the (204) plane leads to low-frequency modes resulting from out-of-phase tilted PbBr<sub>6</sub> octahedra,<sup>33,35</sup> which contribute to phonon scattering, particularly at low temperatures, giving rise to large anisotropy in the thermal transport. The low values for  $\theta_D$  and  $v$  indicate relatively weak bonding, an observation that is in accord with the specific bonding nature of Pb–Br and Cs–Br, and in agreement with theoretically predicted values for CsPbBr<sub>3</sub>.<sup>38</sup> Moreover, there is anisotropy in the lattice anharmonicity perpendicular and parallel to the (204) plane, supporting these findings.

Wilarachchige D. C. B. Gunatilleke: data curation, investigation, formal analysis, visualization, writing – original draft. Oluwagbemiga P. Ojo: data curation, investigation, formal analysis. George S. Nolas: conceptualization, investigation, supervision, writing – review & editing, project administration.

The authors gratefully acknowledge support from Amethyst Research, Inc., USA.

## Data availability

The data supporting this article have been included as part of the ESI.†

## Conflicts of interest

There are no conflicts to declare.

## References

- Q. Xu, D. Yang, J. Lv, Y.-Y. Sun and L. Zhang, *Small Methods*, 2018, **2**, 1700316.
- A. Krishna, S. Gottis, M. K. Nazeeruddin and F. Sauvage, *Adv. Funct. Mater.*, 2019, **29**, 1806482.
- C. Ortiz-Cervantes, P. Carmona-Monroy and D. Solis-Ibarra, *ChemSusChem*, 2019, **12**, 1560–1575.
- Y. Huang, J. Liu, Y. Deng, Y. Qian, X. Jia, M. Ma, C. Yang, K. Liu, Z. Wang, S. Qu and Z. Wang, *J. Semicond.*, 2020, **41**, 011701.



- 5 G. Zhang, G. Liu, L. Wang and J. T. S. Irvine, *Chem. Soc. Rev.*, 2016, **45**, 5951–5984.
- 6 J. Xu, X. Li, J. Xiong, C. Yuan, S. Semin, T. Rasing and X.-H. Bu, *Adv. Mater.*, 2020, **32**, 1806736.
- 7 Y. Zhou, Y. Huang, X. Xu, Z. Fan, J. B. Khurgin and Q. Xiong, *Appl. Phys. Rev.*, 2020, **7**, 041313.
- 8 G. Kakavelakis, M. Gedda, A. Panagiotopoulos, E. Kymakis, T. D. Anthopoulos and K. Petridis, *Adv. Sci.*, 2020, **7**, 2002098.
- 9 K. R. Dudipala, T.-H. Le, W. Nie and R. L. Z. Hoye, *Adv. Mater.*, 2024, **36**, 2304523.
- 10 H. Wei, C. Yang, Y. Wu, B. Cao, M. Lorenz and M. Grundmann, *J. Mater. Chem. C*, 2020, **8**, 15575–15596.
- 11 M. A. Haque, S. Kee, D. R. Villalva, W.-L. Ong and D. Baran, *Adv. Sci.*, 2020, **7**, 1903389.
- 12 J. P. Velev, S. S. Jaswal and E. Y. Tsymlal, *Philos. Trans. R. Soc., A*, 2011, **369**, 3069–3097.
- 13 Y. Lv, Y. Wang, X. Ma, Y. Xu, L. Wang, X. Wang, M. Xiao and C. Zhang, *Adv. Phys.: X*, 2023, **8**, 2258951.
- 14 A. K. Roy, B. L. Farmer, V. Varshney, S. Sihni, J. Lee and S. Ganguli, *ACS Appl. Mater. Interfaces*, 2012, **4**, 545–563.
- 15 Y. Lin, Y. Jia, G. Alva and G. Fang, *Renewable Sustainable Energy Rev.*, 2018, **82**, 2730–2742.
- 16 G. S. Nolas and H. J. Goldsmid, in *Thermal Conductivity*, ed. T. M. Tritt, Springer, US, 2004, pp. 105–121.
- 17 W. D. C. B. Gunatilleke, A. F. May, H. Wang and G. S. Nolas, *Appl. Phys. Lett.*, 2020, **117**, 092101.
- 18 T. Ghosh, M. Dutta, D. Sarkar and K. Biswas, *J. Am. Chem. Soc.*, 2022, **144**, 10099–10118.
- 19 G. S. Nolas, G. Fowler and J. Yang, *J. Appl. Phys.*, 2006, **100**, 043705.
- 20 Y. Dong, A. R. Khabibullin, K. Wei, J. R. Salvador, G. S. Nolas and L. M. Woods, *Chem. Phys. Chem.*, 2015, **16**, 3264–3270.
- 21 Y. He, L. Matei, H. J. Jung, K. M. McCall, M. Chen, C. C. Stoumpos, Z. Liu, J. A. Peters, D. Y. Chung, B. W. Wessels, M. R. Wasielewski, V. P. Dravid, A. Burger and M. G. Kanatzidis, *Nat. Commun.*, 2018, **9**, 1609.
- 22 L. Pan, Z. Liu, C. Welton, V. V. Klepov, J. A. Peters, M. C. De Siena, A. Benadia, I. Pandey, A. Miceli, D. Y. Chung, G. N. M. Reddy, B. W. Wessels and M. G. Kanatzidis, *Adv. Mater.*, 2023, **35**, 2211840.
- 23 Z. Yao, W. Cao, Z. Wang, L. Miao, J. Shi and R. Xiong, *Phys. Chem. Chem. Phys.*, 2023, **25**, 26236–26244.
- 24 X. Wang, Z. Gao, G. Zhu, J. Ren, L. Hu, J. Sun, X. Ding, Y. Xia and B. Li, *Phys. Rev. B*, 2023, **107**, 214308.
- 25 T. Lanigan-Atkins, X. He, M. J. Krogstad, D. M. Pajeroski, D. L. Abernathy, G. N. M. N. Xu, Z. Xu, D.-Y. Chung, M. G. Kanatzidis, S. Rosenkranz, R. Osborn and O. Delaire, *Nat. Mater.*, 2021, **20**, 977–983.
- 26 W. Lee, H. Li, A. B. Wong, D. Zhang, M. Lai, Y. Yu, Q. Kong, E. Lin, J. J. Urban, J. C. Grossman and P. Yang, *Proc. Natl. Acad. Sci. U. S. A.*, 2017, **114**, 8693–8697.
- 27 C. C. Stoumpos, C. D. Malliakas, J. A. Peters, Z. Liu, M. Sebastian, J. Im, T. C. Chasapis, A. C. Wibowo, D. Y. Chung, A. J. Freeman, B. W. Wessels and M. G. Kanatzidis, *Cryst. Growth Des.*, 2013, **13**, 2722–2727.
- 28 A. E. J. Hoffman, R. A. Saha, S. Borgmans, P. Puech, T. Braeckvelt, M. B. J. Roefsaers, J. A. Steele, J. Hofkens and V. Van Speybroeck, *APL Mater.*, 2023, **11**, 41124.
- 29 S. Thakur and A. Giri, *ACS Appl. Mater. Interfaces*, 2023, **15**, 26755–26765.
- 30 C. A. López, C. Abia, M. C. Alvarez-Galván, B.-K. Hong, M. V. Martínez-Huerta, F. Serrano-Sánchez, F. Carrascoso, A. Castellanos-Gómez, M. T. Fernández-Díaz and J. A. Alonso, *ACS Omega*, 2020, **5**, 5931–5938.
- 31 M. Songvilay, N. Giles-Donovan, M. Bari, Z.-G. Ye, J. L. Minns, M. A. Green, G. Xu, P. M. Gehring, K. Schmalzl, W. D. Ratcliff, C. M. Brown, D. Chernyshov, W. van Beek, S. Cochran and C. Stock, *Phys. Rev. Mater.*, 2019, **3**, 093602.
- 32 C. Kittel and P. McEuen, *Introduction to Solid State Physics*, John Wiley & Sons, 2018.
- 33 G. A. Elbaz, W.-L. Ong, E. A. Doud, P. Kim, D. W. Paley, X. Roy and J. A. Malen, *Nano Lett.*, 2017, **17**, 5734–5739.
- 34 D. T. Morelli and G. A. Slack, in *High Thermal Conductivity Materials*, ed. S. L. Shindé and J. S. Goela, Springer, New York, NY, 2006, pp. 37–68.
- 35 G. A. Slack, in *Solid State Physics*, eds. H. Ehrenreich, F. Seitz and D. Turnbull, Academic Press, 1979, vol. 34, pp. 1–71.
- 36 C. L. Julian, *Phys. Rev.*, 1965, **137**, A128–A137.
- 37 R. Ben Sadok, A. Muñoz, P. Rodríguez-Hernández, H. Djani and D. Hammoutène, *J. Solid State Chem.*, 2022, **314**, 123402.
- 38 F. Bridges, J. Gruzdas, C. MacKeen, K. Mayford, N. J. Weadock, V. U. Baltazar, Y. Rakita, L. Waquier, J. A. Vigil, H. I. Karunadasa and M. F. Toney, *Phys. Rev. B*, 2023, **108**, 214102.

