

Cite this: *J. Mater. Chem. A*, 2023, 11, 10901Co-alloying of Sn and Te enables high thermoelectric performance in Ag_9GaSe_6 †Min Li,^{ab} Hexige Wuliji,^c Zhengyang Zhou,^a Pengfei Qiu,^a Kunpeng Zhao ^{*c} and Xun Shi ^{*ab}

As a typical liquid-like material, the argyrodite-type Ag_9GaSe_6 has attracted considerable attention in the past decade due to its liquid-like characteristics, complex crystal structures, and high carrier mobility. However, the carrier concentration of pristine Ag_9GaSe_6 is still not optimal while the thermal conductivity remains to be further reduced. Herein, we simultaneously optimize the electrical and thermal properties of Ag_9GaSe_6 via alloying Sn at the Ga sites and Te at the Se sites. It is found that the crystal symmetry is well maintained, while the phase transition temperature is reduced and local chemical bonding is altered after alloying. Due to the nominally reduced Ag content and the change of chemical bonding, the carrier concentration is reduced by two orders of magnitude, giving rise to a largely improved Seebeck coefficient. Meanwhile, the lattice thermal conductivity κ_L of $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ is significantly suppressed by the strong phonon scattering from point defects. An ultralow κ_L of $\sim 0.25 \text{ W m}^{-1} \text{ K}^{-1}$, which approaches the theoretical minimum κ_L , is attained at room temperature in the alloyed samples. Consequently, the zT value is boosted to 1.4 for the $x = 0.1$ sample, which represents an improvement of 75% over that of pristine Ag_9GaSe_6 .

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1. Introduction

Thermoelectric (TE) technology, which enables direct energy conversion between heat and electricity, is believed to play a key role in alleviating the energy crisis and environmental pollution.^{1–3} The energy conversion efficiency of a TE material is mainly governed by the dimensionless TE figure of merit

$zT = \frac{S^2\sigma}{\kappa}T$, where S , σ , κ , and T are the Seebeck coefficient, electrical conductivity, total thermal conductivity, and absolute temperature, respectively. κ mainly consists of two parts: the lattice thermal conductivity (κ_L) and electronic thermal conductivity (κ_e). Since the parameters S , σ and κ_e are strongly interrelated via the carrier concentration and scattering mechanism, it is really challenging to boost the TE performance. Considerable efforts have been devoted to either enhancing the electronic performance or reducing the lattice thermal conductivity. The former can be realized by approaches like band convergence,^{4,5} resonant doping,⁶ and disorder-induced electronic localization,^{7,8} while the latter can

be achieved by all-scale hierarchical structuring,^{9,10} introduction of liquid-like ions,^{11,12} entropy engineering,^{13,14} or structural modularization.¹⁵

Rational design of ordered and disordered sublattices in the crystal structure is one of the most effective strategies for regulating the TE properties at present. A highly ordered crystal lattice is conducive to the free transport of electrons, whereas a disordered crystal lattice enables strong scattering of heat-carrying phonons.¹⁶ Integration of ordered and disordered sublattices into a single material may induce some intriguing new effects,^{8,17} and is expected to decouple the electrical and thermal transports. Hybrid materials, such as liquid-like materials,^{18,19} meta-phases,^{8,20} and filled skutterudites,^{21,22} are successful examples in this regard. Particularly, liquid-like materials, which consist of an ordered rigid framework and disordered liquid-like cations, have stimulated keen interest in the past few years. Liquid-like ions can not only strongly scatter the phonons but also eliminate part of the transverse vibrational modes, giving rise to extremely low thermal conductivity and high thermoelectric performance.^{11,23–25}

Among all the known liquid-like materials, argyrodite-type compounds stand out due to their unique features of earth-abundant components, complex order-disorder structures, and unusual TE properties.^{26–37} The argyrodites contain dozens of types of compounds with the general chemical formula of $\text{A}^{+}_{12-y}\text{B}^+_y\text{C}^{2-}_6$, where A, B, and C could be Ag/Cu/Li, Al/Ga/Si/Ge/Sn/P, and S/Se/Te, respectively.³⁸ The crystal structures, phase transitions, and TE properties of argyrodites can thus be readily regulated and controlled by the richness of composition.

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Argyrodite-type compounds generally undergo one or two phase transitions. At low temperature, they usually crystallize in a low-symmetry ordered structure, such as monoclinic, orthogonal, or hexagonal structure, where both anions and cations are in long-range ordered (LRO) distribution. As the temperature goes up to the phase transition point, they transform into a high-symmetry disordered structure, where A ions are situated in a highly disordered manner in the rigid sublattice formed by B cations and C anions. Owing to the unique structural feature of crystallinity–amorphicity duality, argyrodites show intrinsically ultralow κ_L and good thermoelectric performance. Taking the representative Ag_9GaSe_6 as an example, it has an amorphous-like κ_L of $0.3 \text{ W m}^{-1} \text{ K}^{-1}$ and a high zT value of 1.1 at high temperature.³³ Further optimization of the carrier concentration by introducing slight Se-deficiency leads to an increased zT of 1.3 in $\text{Ag}_9\text{GaSe}_{5.99}$.³³ Through alloying Te at Se sites, the good electrical transport properties were maintained while the lattice thermal conductivity was reduced, resulting in a high zT of 1.6 at 850 K for $\text{Ag}_9\text{GaSe}_{5.53}\text{Te}_{0.45}$.³⁴ Besides, alloying Cu at the Ag site could effectively decrease the carrier concentration and improve the maximum zT value to 1.6 at 824 K.³⁹

Inspired by the aforementioned peer work, herein we aim to reduce the carrier concentration and suppress the lattice thermal conductivity simultaneously by co-alloying Sn and Te in Ag_9GaSe_6 . Our results show that the nested order–disorder structural feature of Ag_9GaSe_6 is well maintained, while the phase transition temperature is reduced and the local chemical bonds are slightly changed after alloying Sn at the Ga sites and Te at the Se sites. The κ_L is largely reduced due to the extra phonon scattering by the strong mass and strain fluctuations. Combining the optimized carrier concentration, a maximum zT of 1.4 was finally achieved in the $(\text{Ag}_9\text{GaSe}_6)_{0.9}(\text{Ag}_8\text{SnTe}_6)_{0.1}$ sample.

2. Experimental details

2.1. Synthesis

A series of Sn and Te co-alloyed $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ samples, *i.e.*, $(\text{Ag}_9\text{GaSe}_6)_{1-x}(\text{Ag}_8\text{SnTe}_6)_x$ ($x = 0, 0.05, 0.075, 0.1, 0.125, 0.15, 0.2$), were synthesized by the melting–annealing–sintering technique. Mixtures of the five elements (Ag, Ga, Se, Sn and Te) with purity of more than 99.999% (Alfa Aesar) were weighed out in stoichiometric proportions and loaded into silica vacuum tubes for melting. The melting was conducted at 1373 K for 12 h under vacuum, followed by annealing at 873 K for 72 h. After cooling down to room temperature (RT), the ingots were ground into fine powders and then sintered using a hot press system in a graphite die at a peak temperature of $\sim 873 \text{ K}$ and a pressure of 57 MPa for 2 h. The relative densities of all the obtained bulk samples were larger than 99%. The bulk samples with sizes of about $2 \times 2 \times 9 \text{ mm}^3$ were cut out for electrical measurements, and samples with sizes of $\phi 10 \times 1 \text{ mm}^2$ for thermal diffusivity measurement.

2.2. Characterization

To identify the phase purity and crystal structure, the powder X-ray diffraction (PXRD) data for all synthesized samples were

collected on a powder X-ray diffractometer (D8 Advance) with Cu K α radiation ($\lambda = 1.5406 \text{ \AA}$). Four samples ($x = 0, 0.05, 0.1, 0.15$) were selected to record the high-quality synchrotron diffraction data ($\lambda = 0.6887 \text{ \AA}$) at beamline BL14B1 at the Shanghai Synchrotron Radiation Facility (SSRF), China. Phase composition and microstructure analysis were carried out by scanning electron microscopy (SEM) using a ZEISS Supra 55 equipped with an energy dispersive spectrometer (EDS, Oxford Horiba 250). The heat capacity at constant pressure was measured to analyze phase transition characteristics in the range of 150 K–550 K using a differential scanning calorimeter (DSC, Netzsch 200 F3). The electrical transport measurements (σ and S) from RT to 850 K were conducted in a helium atmosphere using an ULVAC-RIKO ZEM-3 instrument system. The thermal diffusivity (D) above 300 K was measured by the laser flash method using a Netzsch LFA 457 instrument in an argon atmosphere, and all the samples were pre-coated with graphite spray before the measurement. Measurement uncertainty for σ , S , and D is $\pm 3\%$, $\pm 4\%$, and $\pm 3\%$, respectively. The Dulong–Petit rule was used to estimate the heat capacities (C_p) above RT. The sample density d was measured using Archimedes' method. The thermal conductivity above RT was then calculated based on the equation $\kappa = dDC_p$. The transverse and longitudinal sound velocities at RT were obtained by using the ultrasonic pulse method on an Advanced Ultrasonic Measurement System (UMS, TECLAB). Then the TE figure of merit (zT) can be calculated using the obtained parameters mentioned above. The electrical conductivity, thermal conductivity, and heat capacity in the low temperature range (3–300 K) were measured using a Physical Property Measurement System (PPMS, Quantum Design). Hall coefficients (R_H) were measured by using a four-probe configuration in PPMS with a sweeping magnetic field from -3 T to 3 T . The Hall mobility (μ) and carrier concentration (n) were calculated according to the equations $\mu = |R_H|\sigma$ and $n = 1/(eR_H)$, respectively, where e is the electron charge.

2.3. Theoretical calculations

First-principles calculations were carried out with the Vienna *Ab initio* Simulation Package (VASP) code by utilizing the projector augmented wave (PAW) method for the interaction between ion cores and valence electrons.⁴⁰ The low temperature ordered cubic structure of $\alpha\text{-Ag}_9\text{GaSe}_6$ was used for calculation. One fourth of the Ga and Se atoms were randomly substituted by Sn and Te, respectively, and one thirty-sixth of the Ag was removed (see Fig. S1[†]), corresponding to the chemical composition of $\text{Ag}_{8.75}\text{Ga}_{0.75}\text{Sn}_{0.25}\text{Se}_{4.5}\text{Te}_{1.5}$. Both the atomic coordinates and lattice vectors were fully relaxed until the force-convergence criterion reached 0.01 eV \AA^{-1} for pure and doped Ag_9GaSe_6 structures. The Perdew Burke Ernzerhof (PBE) functional within Generalized gradient approximation (GGA) was used for treating the electronic exchange and correlation potential. The deformation charge density was obtained by subtracting atomic charge density from total charge density. The plane wave energy cutoff was set to 400 eV for all calculations. The projected crystal orbital Hamilton population (pCOHP) was calculated through the LOBSTER code⁴¹ based on a ground state self-consistent



calculation from VASP. The Brillouin zone was sampled by $3 \times 3 \times 3$ Γ -centered k mesh for structural relaxations and charge density calculations, and by $9 \times 9 \times 9$ Γ -centered k mesh for COHP calculations. A rotationally invariant Hubbard U correction was adopted to describe the on-site Coulomb interactions among Ag 4d orbital electrons ($U = 2.0$ eV). The Bader charge was analyzed using the Bader code from the Henkelman research group.⁴²

3. Results and discussion

The pristine Ag_9GaSe_6 undergoes an order-to-disorder phase transition at around 281 K.^{43,44} Below 281 K, it adopts a cubic structure (α -phase, space group $P2_13$) with all atoms in a long-range ordered (LRO) distribution (Fig. 1a). Above 281 K, Ag_9GaSe_6 crystallizes in a higher-symmetry cubic structure (β -phase, space group $F43m$) with the Ag ions melting down to disordered distribution (Fig. 1b). The distribution of Ga and Se is very similar, and the coordination environment and bond lengths are also very close in both structures. Herein we synthesized a series of Sn and Te co-alloyed $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ samples, *i.e.*, $(\text{Ag}_9\text{GaSe}_6)_{1-x}(\text{Ag}_8\text{SnTe}_6)_x$, with x ranging from 0 to 0.2. The measured room temperature powder XRD patterns are shown in Fig. 1c and S2.† All the diffraction peaks (Fig. 1c) can be well indexed to the high temperature β -phase of Ag_9GaSe_6 without any visible impurity peaks. The refined lattice parameters increase linearly with increasing Sn and Te alloying content, well obeying Vegard's law. Though Sn has a larger atomic size than Ga, the lattice parameters of Sn and Te co-alloyed samples are nearly the same as the Te alloyed samples. This may be attributed to the low Ag content in our $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ samples, which shrinks the crystal lattice to a certain extent. Fig. S3† shows the SEM images and EDS mappings measured on the polished surfaces for the $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ samples. All samples are dense with no observable pores or cracks. All elements, including Ag, Ga, Se, Sn, and Te, are homogeneously distributed in the materials. The measured chemical compositions are very close to the nominal ones (Table S1†). These results indicate the successful substitution of Sn and Te at the lattice sites of Ga and Se.

Fig. 1e shows the temperature dependent heat capacity C_p for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ samples. One endothermic peak can be observed clearly in each curve, corresponding to the phase transition from the ordered α -phase to the disordered β -phase. Based on the C_p data, we calculated the latent heat (E) during phase transition. It was found that the E is reduced from 6.33 J g^{-1} for pristine Ag_9GaSe_6 to 1.23 J g^{-1} for the $x = 0.15$ sample, indicating that the enthalpy difference between the α -phase and β -phase gets smaller after alloying Sn and Te. The detected phase transition temperature T_p for pristine Ag_9GaSe_6 is around 288 K, which is slightly higher than the reported T_p (281 K) from ref. ³⁴. With increasing alloying content of Sn and Te, the T_p is gradually reduced, in contrast with the increasing trend in single element alloyed $\text{Ag}_9\text{Ga}(\text{Se}_{0.9967-x}\text{Te}_x)_6$ samples (see Fig. 1f). These results

suggest that Sn alloying plays a key role in suppressing the phase transition temperature.

The chemical bonding characteristics of $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ were investigated by analyzing the Bader charge, deformation charge density, and projected crystal orbital Hamilton population (pCOHP). As shown in Fig. 2a, Bader charge analysis shows that for Ag_9GaSe_6 each Se atom receives 0.4–0.6 electrons, while each Ag and Ga atom loses 0.26 and 0.97 electrons, respectively. The relatively low Bader charge, *i.e.*, low charge transfer, suggests that the ionic component of chemical bonds in Ag_9GaSe_6 is very low. After alloying Sn and Te, the Bader charge of Se remains the same, while the Bader charge of Ag is reduced from 0.26 to 0.24. The Bader charge of Te is lower than that of Se, indicating that the ionic component between Ag and anions (Se/Te) is further weakened. Meanwhile, the ionic component of Sn–Se bonds is stronger than that of Ga–Se bonds due to the smaller Bader charge of Sn as compared with Ga. This is reasonable since Sn (1.96) is more electronegative than Ga (1.81). Fig. 2b shows the deformation charge density for $\text{Ag}_{8.75}\text{Ga}_{0.75}\text{Sn}_{0.25}\text{Se}_{4.5}\text{Te}_{1.5}$. As can be seen, the charge density between Ga and Se is very high, indicative of strong covalent interaction. The substitution of Sn at Ga sites leads to a slightly weakened covalent interaction, as evidenced by the low charge density between Sn and Se. On the other hand, the charge density between Ag and neighboring Se or Te is very low, pointing to weak covalent bonds. This is further confirmed by the pCOHP results. As shown in Fig. 2c, large antibonding (destabilizing) states below the Fermi level are observed for the Ag–Se bonds, and the bonding energy (−0.69 eV) calculated from the integral pCOHP is also very low. In contrast, the Ga–Se bond has a high bonding energy of −4.45 eV, which is consistent with the results of deformation charge density. After alloying Sn and Te, the bonding energies of Ag–Se/Te and Ga/Sn–Se bonds are slightly changed (Fig. 2d).

Briefly, all calculation results reveal that the Ag–Se chemical bonds, including both ionic component and covalent component, are very weak, while the Ga–Se bonds are very strong. The Ag ions are thus loosely bonded to the rigid sublattice formed by Ga and Se. Due to the high content of the weakly bonded Ag ions, the overall chemical bonds in Ag_9GaSe_6 are still very weak. The alloying of Sn and Te has an unremarkable but observable impact on the chemical bonds, which may change the local lattice defects.

Fig. 3 presents the thermal transport properties for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$. The total thermal conductivity (κ) of pristine Ag_9GaSe_6 is around $0.5 \text{ W m}^{-1} \text{ K}^{-1}$, which is reduced to $0.3 \text{ W m}^{-1} \text{ K}^{-1}$ in the alloyed samples (Fig. 3a). All samples show a weak temperature dependency of κ , which is a common phenomenon observed in liquid-like TE materials, for instance, Cu_2Se ,¹¹ $\text{Ag}_9\text{FeSe}_{6-x}\text{Te}_x$,⁴⁵ and Cu_7PSe_6 ,³⁷ to name a few. Besides, an evident upward inflection is observed at about 700 K for $x = 0$ –0.075 samples, which is mainly caused by an increase of electronic thermal conductivity resulting from the intrinsic excitation. The lattice thermal conductivity (κ_L) was derived by subtracting the electronic contribution (κ_e) from the total κ via the Wiedemann–Franz relationship, $\kappa_e = L\sigma T$, where L is the Lorenz number.⁴⁶ As shown in Fig. 3b, the calculated κ_L of



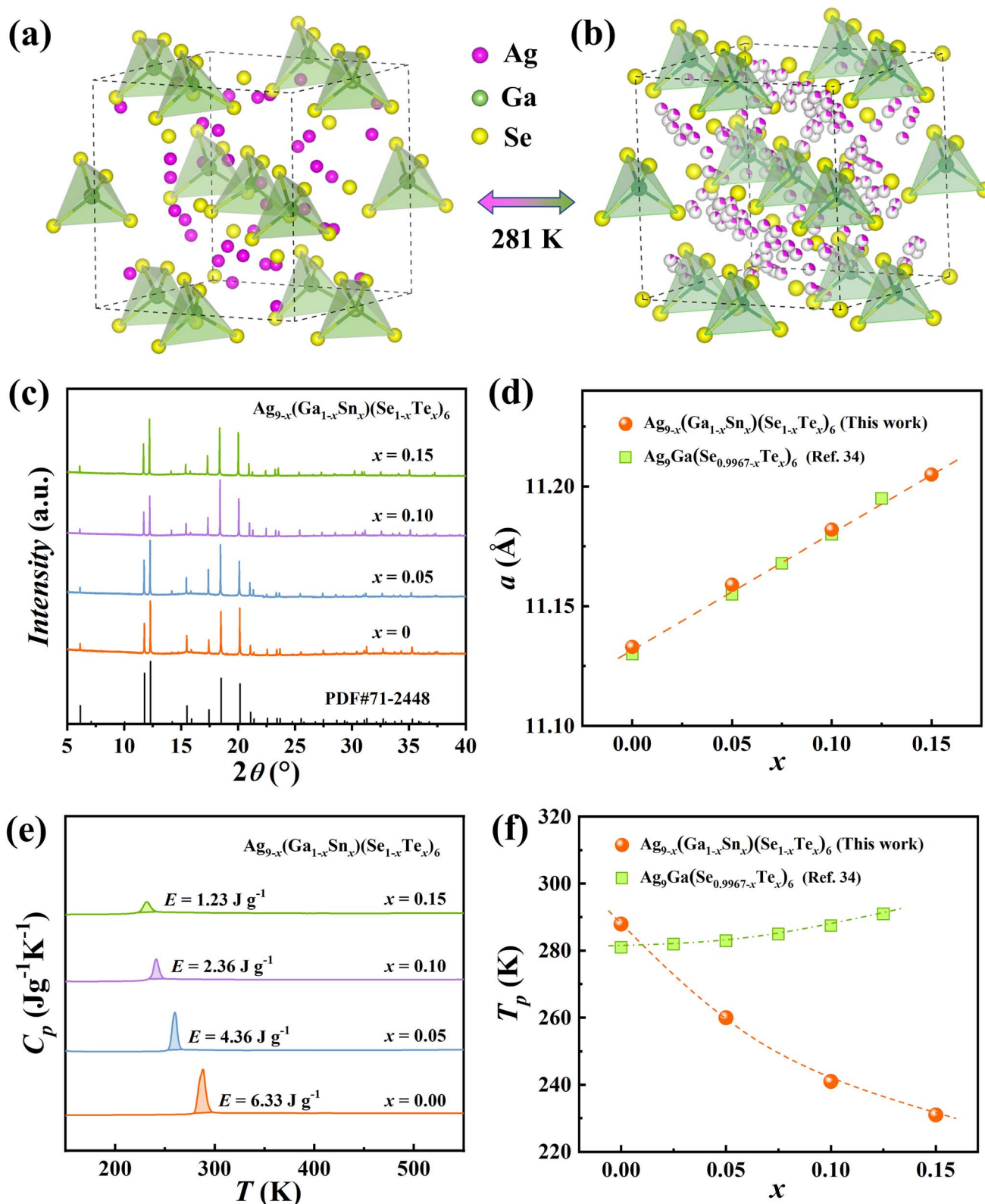


Fig. 1 (a) Low-temperature and (b) high-temperature crystal structures for Ag_9GaSe_6 . (c) Synchrotron powder X-ray diffraction patterns for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ ($x = 0, 0.05, 0.1, 0.15, 0.2$). (d) Lattice parameter a as a function of alloying content x for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$. (e) Temperature dependence of heat capacity C_p . (f) Phase transition temperature as a function of alloying content x . The green square symbols represent the data for $\text{Ag}_{9-x}\text{Ga}(\text{Se}_{0.9967-x}\text{Te}_x)_6$.³⁴

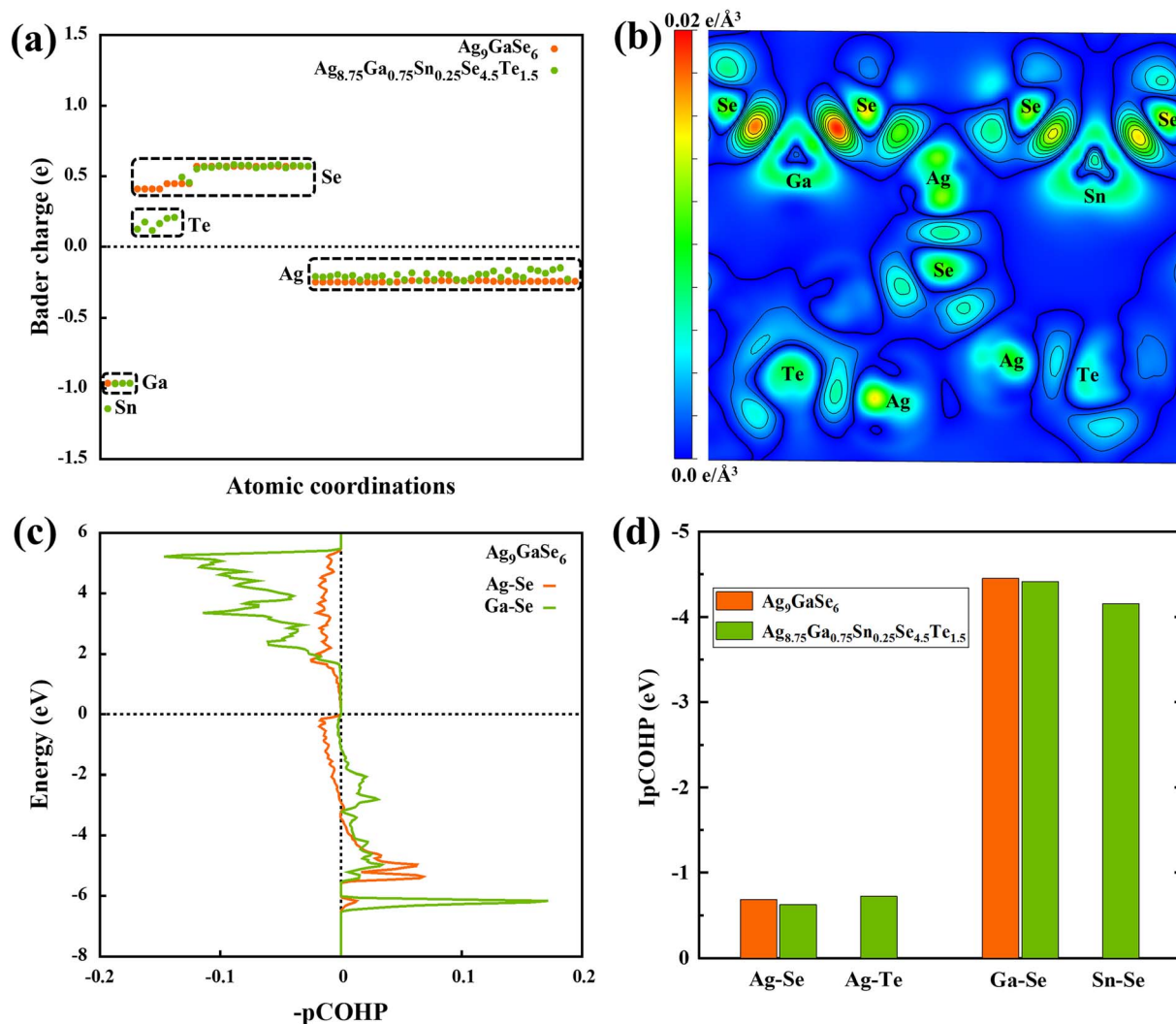


Fig. 2 (a) Bader charge for the different elements in Ag_9GaSe_6 and $\text{Ag}_{8.75}\text{Ga}_{0.75}\text{Sn}_{0.25}\text{Se}_{4.5}\text{Te}_{1.5}$. (b) Deformation charge density at the (101) plane for $\text{Ag}_{8.75}\text{Ga}_{0.75}\text{Sn}_{0.25}\text{Se}_{4.5}\text{Te}_{1.5}$. (c) The projected crystal orbital Hamilton population (pCOHP) of Ag–Se and Ga–Se bonds for Ag_9GaSe_6 . The Fermi level is represented by the horizontal dashed line. The bonding orbital has negative pCOHP, while the antibonding orbital has positive pCOHP. (d) Integrated pCOHP (IpCOHP) for the chemical bonds in Ag_9GaSe_6 and $\text{Ag}_{8.75}\text{Ga}_{0.75}\text{Sn}_{0.25}\text{Se}_{4.5}\text{Te}_{1.5}$.

Ag_9GaSe_6 is about $0.4 \text{ W m}^{-1} \text{ K}^{-1}$ at room temperature and gradually decreased above 600 K. After alloying Sn and Te, the room temperature κ_L of $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ is further reduced to $\sim 0.25 \text{ W m}^{-1} \text{ K}^{-1}$ owing to the enhanced phonon scattering by point defects. The abnormally low κ_L above 750 K likely stems from the strong liquid-like effects at high temperature and the overestimation of the electronic thermal conductivity, especially for the samples having high electrical conductivities. The low κ_L in $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ is comparable to those observed in other liquid-like materials, but much lower than those observed in the state-of-the-art TE materials like Bi_2Te_3 ,⁴⁷ Mg_3Sb_2 ,^{48,49} and half-Heuslers.^{50,51}

Based on the measured sound velocities, we estimated the theoretical minimum $\kappa_{L,\text{min}}$ for this material system using Cahill's model⁵² (see details in the ESI†). Our experimental κ_L data are obviously lower than the Cahill's limit ($0.37 \text{ W m}^{-1} \text{ K}^{-1}$), which means it is inadequate to capture the phonon

transports by only considering the lattice complexity and anharmonicity based on the Cahill's model. Recently, a diffuson-dominated model was reported by Bernges *et al.*,⁵³ in which the ion transport was also included to explain the thermal transport properties of disordered materials. Through a two-channel lattice dynamics modeling, Bernges *et al.* pointed out that the majority of Ag^+ vibrations in liquid-like argyrodites have a non-propagating diffuson-like character, resulting in the diffuson-mediated thermal transport.⁵³ Since Ag_9GaSe_6 is a typical liquid-like material, we adopt the diffuson-dominated model to calculate a diffuson limit (see details in the ESI†). It is found that the κ_L of our alloyed samples approaches this limit ($0.23 \text{ W m}^{-1} \text{ K}^{-1}$), demonstrating the strong liquid-like behavior and the presence of diffusons in $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$.

Fig. 3c shows the temperature-dependent κ_L for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ below 300 K. Similar to the normal



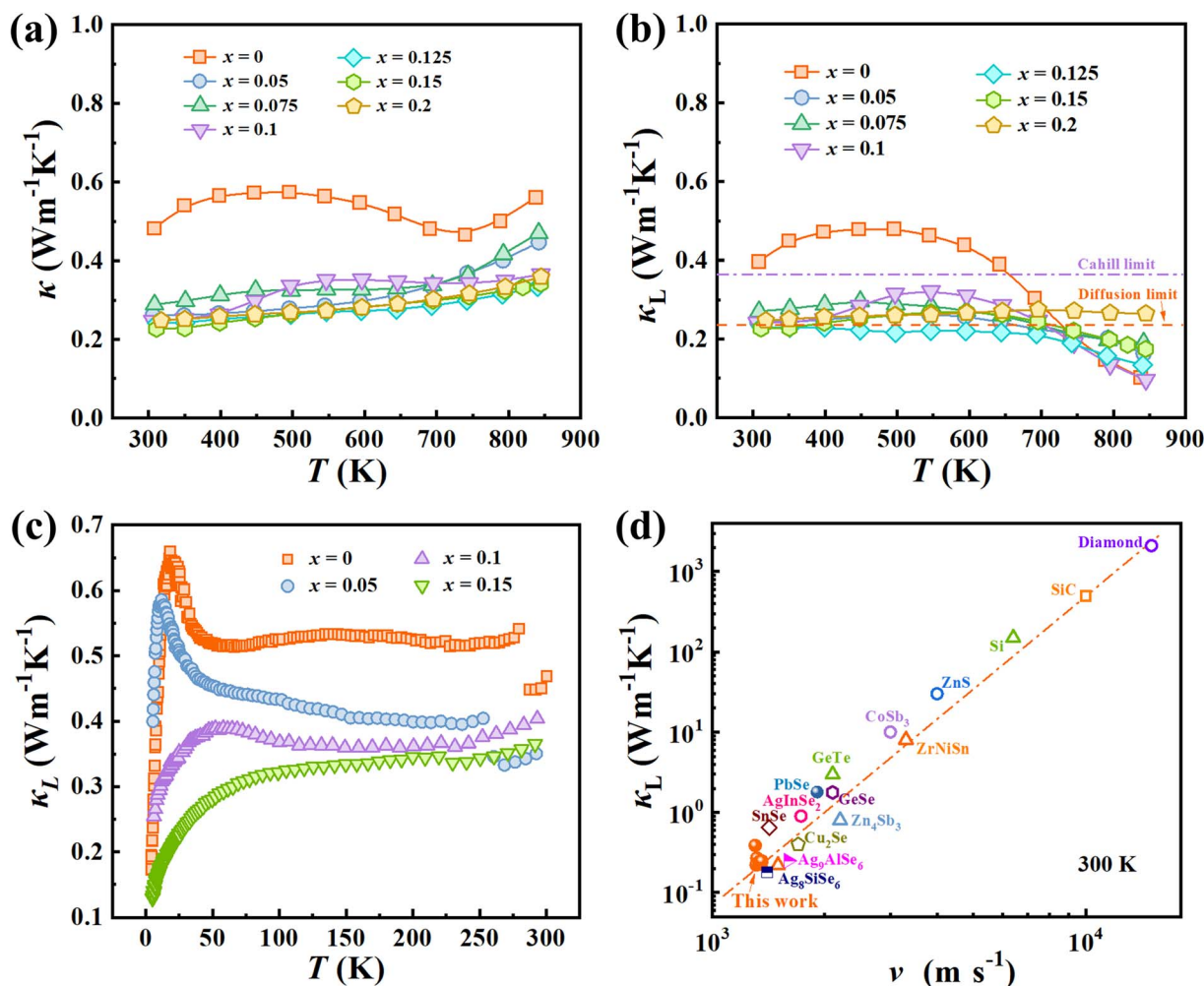


Fig. 3 Temperature dependence of (a) total thermal conductivity (κ) and (b) lattice thermal conductivity (κ_L) from 300 K to 850 K for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ ($x = 0, 0.05, 0.075, 0.1, 0.125, 0.15$, and 0.2). (c) Lattice thermal conductivity (κ_L) below 300 K. (d) Room temperature κ_L versus sound velocity for well-known TE materials.^{26,32,36,57–63}

crystalline materials, the κ_L of $x = 0$ and $x = 0.05$ samples shows a pronounced Umklapp peak at around 10 K. In contrast, κ_L of the $x = 0.15$ sample monotonously increases during the entire temperature range without a peak, which is more like the behavior of amorphous materials. The distinct temperature dependency of κ_L is ascribed to the different contributions from the structural disorder and low-lying multi-Einstein oscillators, as has been discussed in detail in the $\text{Ag}_9\text{FeS}_{6-x}\text{Te}_x$ materials.⁴⁵ Note that the κ_L of $x = 0$ and $x = 0.05$ samples are dramatically reduced at about 280 K and 260 K, respectively, which should be associated with the order-to-disorder phase transition. Though the Ag ions are weakly bonded in both α -phase and β -phase, the distribution of Ag becomes highly disordered and liquid-like in the β -phase, leading to the extra scattering of phonons and the elimination of part transverse vibration modes.

The most prominent feature related to the extremely low κ_L is the low sound velocities (ν) for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$. According to the Debye–Callaway model,^{54,55} κ_L scales approximately with the cube of sound velocity above the Debye temperature. A low sound velocity fundamentally gives rise to

a low κ_L .⁵⁶ The measured transverse and longitudinal sound velocities for our samples are respectively around 1150 m s^{-1} and 2800 m s^{-1} , both of which are among the lowest values of all known solid materials (Fig. 3d).^{26,32,36,57–63} The Debye temperature, calculated based on the sound velocities, is only 140 K, while the Gruneisen parameter is as large as 2.6 (see Table 1). These results can be traced back to the weak bonding of Ag to its surrounding Se/Te atoms. Co-alloying of Sn and Te in $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ scarcely alters the sound velocity, which is reasonable since the crystal structure and chemical bonding do not change much.

Fig. 4 shows the electrical transport properties for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$. The electrical conductivity σ of the pristine Ag_9GaSe_6 decreases from $1.7 \times 10^4 \text{ S m}^{-1}$ at room temperature to $1.1 \times 10^4 \text{ S m}^{-1}$ at 600 K before it increases to $3.5 \times 10^4 \text{ S m}^{-1}$ at 850 K. The inflection point at 600 K is indicative of the intrinsic excitation of carriers. After alloying Sn and Te, the σ is roughly decreased and much lower than those of Te alloyed samples (see Fig. S4a†). Besides, the inflection point of σ after alloying Sn and Te is shifted to a lower temperature,



Table 1 Transverse (ν_t), longitudinal (ν_l) and mean sound velocity (ν_m), bulk module (B), shear module (G), Gruneisen parameter (γ), and Debye temperature (T_D) for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$

Samples	ν_t (m s ⁻¹)	ν_l (m s ⁻¹)	ν_m (m s ⁻¹)	B (GPa)	G (GPa)	γ	T_D
$x = 0.000$	1150.7	2855.4	1303.2	45.9	9.5	2.66	139.0
$x = 0.050$	1159.8	2734.4	1311.2	40.8	9.7	2.52	140.0
$x = 0.075$	1165.5	2706.2	1316.8	39.6	9.8	2.47	140.5
$x = 0.100$	1180.1	2771.3	1333.9	41.8	10.0	2.50	142.0
$x = 0.125$	1181.2	2796.6	1335.6	42.8	10.0	2.53	142.5
$x = 0.150$	1195.9	2820.3	1352.1	43.4	10.3	2.52	144.0
$x = 0.200$	1201.7	2848.0	1358.8	44.4	10.4	2.53	145.0

suggesting a lower carrier concentration and smaller band gap. The negative S values indicate that electrons are the dominant charge carriers, which is further confirmed by the Hall measurements. The temperature dependency and composition dependency of S are opposite to the electrical conductivity. A maximum $|S|$ of 615 $\mu\text{V K}^{-1}$ is achieved at 300 K for the $x = 0.15$ sample, which is three times larger than that of pristine Ag_9GaSe_6 . The improvement of S is significantly larger in our Sn

and Te co-alloyed samples, as compared with the single element alloyed $\text{Ag}_9\text{Ga}(\text{Se}_{1-x}\text{Te}_x)_6$ samples (see Fig. S4b†).

The variations of σ and S are mainly caused by the modified carrier concentrations (n) and mobility (μ) of $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$. As shown in Fig. 4c, the Hall carrier concentration decreases dramatically from $2.18 \times 10^{18} \text{ cm}^{-3}$ for pristine Ag_9GaSe_6 to $1.5 \times 10^{16} \text{ cm}^{-3}$ for the $x = 0.15$ sample. Such a decreased trend in n is mainly related to two aspects. On

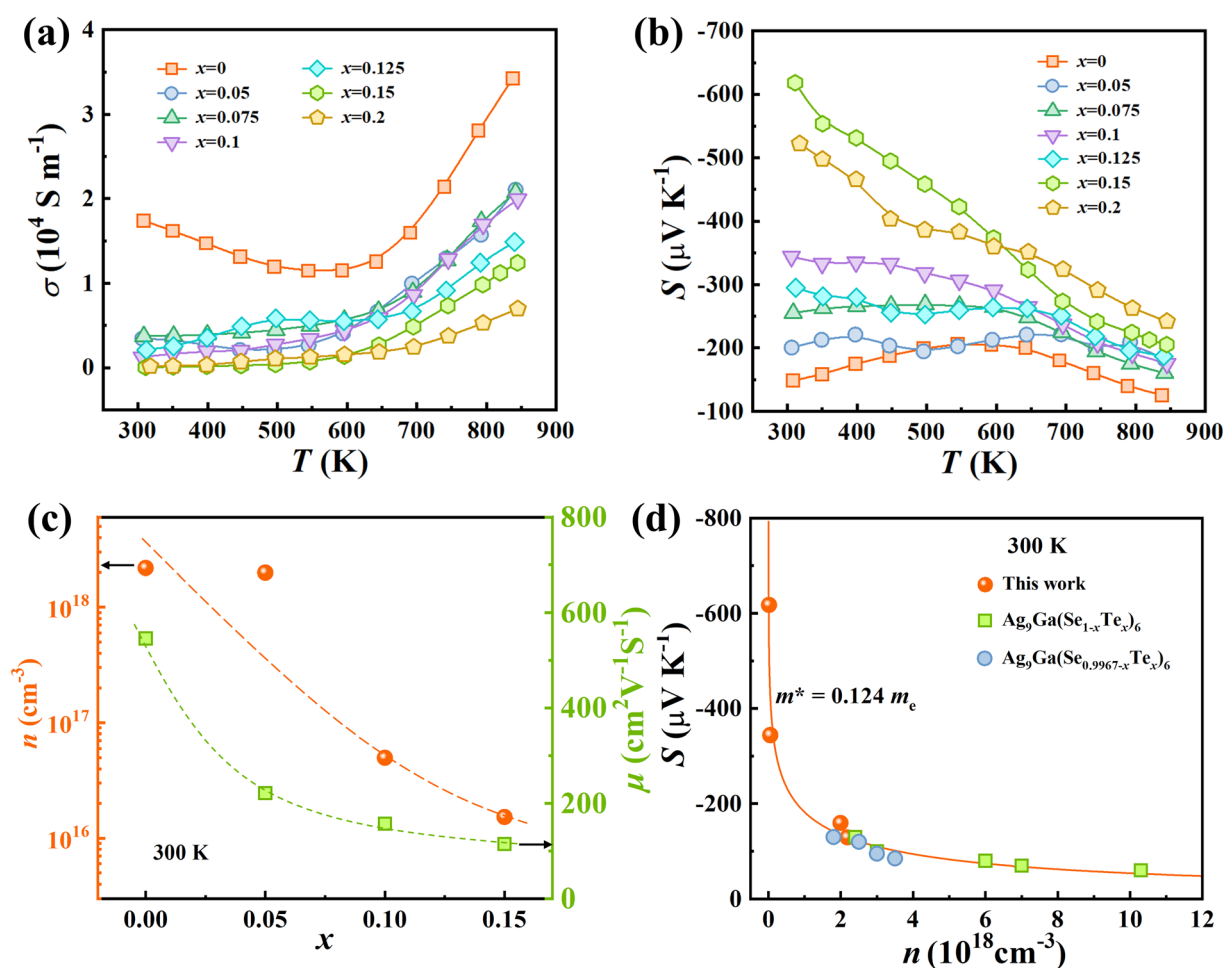


Fig. 4 Temperature dependence of (a) electrical conductivity σ and (b) Seebeck coefficient S for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ ($x = 0, 0.05, 0.075, 0.1, 0.125, 0.15, 0.2$). (c) Room temperature Hall carrier concentration n and carrier mobility μ as a function of alloying content x . (d) Seebeck coefficient S as a function of carrier concentration n . The reported data of $\text{Ag}_9\text{Ga}(\text{Se}_{1-x}\text{Te}_x)_6$ and $\text{Ag}_9\text{Ga}(\text{Se}_{0.9967-x}\text{Te}_x)_6$ are included for comparison.^{29,34} The Pisarenko plot (S vs. n) is derived from the single parabolic band (SPB) model.



one hand, the nominally Ag content during preparation is reduced, which could decrease the donor concentration of Ag interstitials. On the other hand, the defect formation energy of Ag interstitials or anion vacancies could be improved due to the change of local chemical bonds,⁶⁴ which may lead to a lower n as well. With increasing alloying content, the carrier mobility is also gradually decreased owing to the strengthened scattering of electrons by the chemical bond fluctuation and the ensuing extra potential field introduced by Sn and Te alloying. Specifically, the μ for pristine Ag_9GaSe_6 is $546 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ and decreased to $115 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ for the $x = 0.15$ sample. The decreasing trend of carrier mobility for our co-alloyed samples is opposed to the well maintained carrier mobility in $\text{Ag}_9\text{Ga}(\text{Se}_{1-x}\text{Te}_x)_6$ (ref. 29) (shown in Fig. S4d†), suggesting that Sn alloying drastically strengthens the scattering of carriers. Nevertheless, the reduced carrier mobility is still higher than most p-type liquid-like materials, such as Cu_2Se ($20 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$),⁶⁴ Cu_8GeSe_6 ($16 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$),⁶⁵ and Cu_8GeSe_6 ($0.23 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$).¹⁹

The experimental data of S as a function of n for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ are shown in Fig. 4d. For comparison, the reported data of $\text{Ag}_9\text{Ga}(\text{Se}_{1-x}\text{Te}_x)_6$ and $\text{Ag}_9\text{Ga}(\text{Se}_{0.9967-x}\text{Te}_x)_6$ are also given here. Based on the single parabolic band (SPB) model under the assumption that the charge carriers are mainly scattered by acoustic phonons, a Pisarenko plot (S vs. n) with effective mass m^* of $0.124m_e$ was calculated, where m_e is the effective mass of the electron. Clearly, the experimental data fall right around the theoretical Pisarenko plot, indicating that the alloying of Sn or Te merely shifts the Fermi level towards the valence band, but has little impact on the band edge of the electronic structure. The small effective mass is one of the reasons for the high μ in $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$.

Combining the measured S , σ and κ , we calculated the power factor (PF) and figure of merit zT as a function of temperature. As shown in Fig. 5a, the power factor is slightly increased from $\sim 5 \mu\text{W cm}^{-1} \text{ K}^{-2}$ for pristine Ag_9GaSe_6 to $\sim 5.5 \mu\text{W cm}^{-1} \text{ K}^{-2}$ for the $x = 0.05$ sample. With further increasing the alloying content, the PFs at low temperatures are gradually decreased. The maximum PF achieved for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ is only $6.3 \mu\text{W cm}^{-1} \text{ K}^{-2}$, which is not high as compared with the conventional TE materials like Bi_2Te_3 ,⁴⁷ GeTe ,^{5,66} and CoSb_3 .^{21,67} Nevertheless, relying on the optimized carrier concentration,

reduced thermal conductivity (both κ_L and κ_e), and largely increased Seebeck coefficient, a promising peak zT of 1.4 is attained at 840 K for the $x = 0.1$ sample (Fig. 5b), which is comparable to, if not superior to that of other argyrodite-type compounds.

4. Conclusion

In summary, a series of $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ samples are successfully synthesized and the effects of Sn and Te co-alloying on the crystal structures, phase transition, chemical bonds, and thermoelectric properties are systematically studied. It is found that the crystal symmetry of Ag_9GaSe_6 is well maintained, while the phase transition temperature is suppressed and the overall weak chemical bonds are slightly altered after alloying Sn and Te. The high carrier concentration in pristine Ag_9GaSe_6 is effectively reduced and the Seebeck coefficient is thereby largely improved. Due to the overall weak chemical bonds, Ag_9GaSe_6 shows ultralow sound velocities and lattice thermal conductivity. Upon alloying Sn and Te, the lattice thermal conductivity is further suppressed to $\sim 0.25 \text{ W m}^{-1} \text{ K}^{-1}$, which approaches the diffuson limit. Finally, a peak zT value of 1.4 is achieved in the $x = 0.1$ sample, which is much higher than that of pristine Ag_9GaSe_6 .

Conflicts of interest

There are no conflicts to declare.

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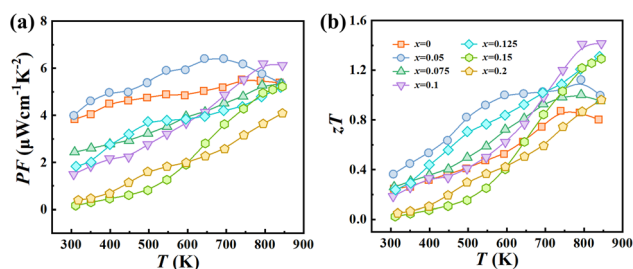


Fig. 5 Temperature dependence of (a) power factors PF and (b) TE figure of merit zT for $\text{Ag}_{9-x}(\text{Ga}_{1-x}\text{Sn}_x)(\text{Se}_{1-x}\text{Te}_x)_6$ ($x = 0, 0.05, 0.075, 0.1, 0.125, 0.15, 0.2$).



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