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Predicting the Na⁺ ion transport properties of NaSICON materials using density functional theory and Kinetic Monte Carlo†

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The efficiency of all-solid-state Na⁺ ion batteries crucially depends on the applied electrolyte, among which sodium super ionic conductors (NaSICONs) show high ionic conductivities. However, the experimental data on ionic conductivities available in the literature vary by several orders of magnitude depending on composition and sample preparation. Hence, a comprehensive understanding of Na⁺ transport properties is still lacking. In this study, we investigate the multi-cationic NaSICONs Na_{1+x}M₂Si_xP_{3-x}O₁₂ (with M = Zr⁴⁺, Hf⁴⁺, Sn⁴⁺, and 0 ≤ x ≤ 3) by combining state-of-the-art computational tools, namely density functional theory calculations to analyse the structure at the atomic level and Kinetic Monte Carlo simulations to study the ion transport on the macroscopic level. The results show that there is no simple correlation between structural properties and the Na⁺ ion transport as often described in the literature. Rather the interplay of the ratio of unoccupied to occupied charge carrier sites, interactions between Na⁺ ions and adjacent cations, and Na⁺ migration barriers, which are influenced by both the M-cation and the degree of substitution, must be considered. Our study provides a detailed picture of the complex ion transport in NaSICONs of variable composition.

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1 Introduction

Although Na⁺ ion conducting NaSICON materials were discovered more than 50 years ago^{1–3} and have been intensively studied in recent years,^{4–12} the examined compositional range of NaSICONs is still limited, and a thorough understanding of Na⁺ ion transport seems to be lacking.

NaSICONs are attractive candidates among solid-state electrolytes (SSEs) because they exhibit good thermal and (electro)chemical stability, high three-dimensional ionic conductivity at room temperature,^{13–19} and demonstrate promising performance for all-solid-state sodium-ion batteries (NIBs).^{20–33} NIBs are considered a complementary system to the market-leading lithium-ion batteries, especially for large-scale energy storage, due to the similar chemical properties of sodium and lithium, the long-term resource availability of sodium, and the cost reduction of NIBs.^{34–48} In addition, all-solid-state NIBs using SSEs are characterized by a long device lifetime, potentially high safety, wide operating temperature range, and high energy and power density depending on the cell architecture.^{13,17–19,49–52}

Various review articles summarize the developments and challenges of NaSICON materials for all-solid-state NIBs.^{4–12} NaSICON structures with the general formula Na_xM₂(AO₄)₃, exhibit a flexible framework in which various M and A cations can be incorporated. Therefore, they offer a large compositional diversity allowing a wide range of applications, but also leading to ionic conductivities that vary over orders of magnitude. Ma *et al.* reported one of the highest total conductivities among NaSICONs to date of 5.2 × 10^{−3} S cm^{−1} at 25 °C for Na_{3.4}Zr₂Si_{2.4}P_{0.6}O₁₂, which is comparable with state-of-the-art liquid-based electrolytes for NIBs and highlights the promising potential of NaSICONs as SSEs.²⁶

Substitution of both M and A cations has been shown to be an effective strategy for modifying the (electro)chemical and structural properties, and thus the ionic conductivity of NaSICONs. However, the ionic conductivity of NaSICONs depends not only on the composition but also on the sample preparation and the measurement techniques.^{9,18,53,54} Due to the large scatter of experimental data currently available, a thorough understanding of Na⁺ transport properties based on these data is difficult.¹⁸ Computational methodologies can be utilized to elucidate the microscopic properties, such as the structure and the migration energy profile of ionic pathways, and their influences on the macroscopic transport behaviour.^{54–59} To date, however, the focus of computational studies has been mainly on the parent composition Na_{1+x}Zr₂Si_xP_{3-x}O₁₂,^{1–3} which is not sufficient for an adequate understanding of NaSICONs.^{53,60–69} Therefore, there is a need to investigate various substituted

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structures over entire compositional ranges using reliable, low-effort computational techniques. Thus, a more comprehensive understanding of the influences of microscopic Na^+ ion motion on macroscopic transport properties can be obtained, guiding the material design of NaSICON solid-state electrolytes.

In our previous study, we proposed a first-principles based Kinetic Monte Carlo (KMC) model considering the local ionic environment and the migration energies of the charge carriers which is highly suitable to describe Na^+ ion transport in the NaSICON structure.⁷⁰ On the one hand, the model is based on Density Functional Theory (DFT) calculations, ensuring a reliable description of the structure at the microscopic level. On the other hand, the KMC simulations allow the investigation of transport properties both on long timescales and in large crystalline systems capturing a great number of ion transport events and accounting for statistical variances. However, the approach comes along with a high amount of DFT calculations and is thus not applicable to a broad range of elements.⁷⁰ Nevertheless, the suitability of this approach was recently confirmed by the study of Deng *et al.* using a combination of local-cluster expansion, DFT-NEB migration barriers, and KMC.⁵³

In the present study, we show an improved approach based on our previously proposed KMC model that requires DFT calculations with minimized computational effort, yet provides higher accuracy by considering a wider range of the local ionic environment. Hence, this approach is suitable for the study of the influence of various substituents and temperatures on the ionic diffusion of multi-element NaSICONs of arbitrary compositions.

We demonstrate the suitability of the approach by studying $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ (with $\text{M} = \text{Zr}^{4+}, \text{Hf}^{4+}, \text{Sn}^{4+}$ and $0 \leq x \leq 3$) as example compositions for multi-element NaSICON-type conductors. These M-cations were selected to investigate structures that exhibit rhombohedral symmetry over a wide temperature range and show the same migration mechanism for Na^+ ions. Not only the influence of Si^{4+} substitution on P^{5+} sites, but also the influence of chemical and structural factors of homovalent M^{4+} substitution on Na^+ ion transport is investigated.

2 Structure and ionic migration

The original NaSICON material with composition $\text{Na}_{1+x}\text{Zr}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ exhibits rhombohedral structure ($R\bar{3}c$) (see Fig. 1) but shows a monoclinic ($C2/c$) distortion for $1.6 \leq x \leq 2.4$ at room temperature.^{2,3,53,71-76} However, at temperatures above 150 °C only the rhombohedral phase exists.^{53,72,77,78}

In this study, we focus on the rhombohedral structure. On the one hand, this phase exists over a larger compositional and temperature range. On the other hand, we have shown in our previous study that bond distances, ionic interaction energies, and migration energies are very similar in the monoclinic and rhombohedral structures. Therefore, the following analysis and conclusions can be adopted for the monoclinic structure.⁷⁰

As shown in Fig. 1, the rhombohedral structure consists of a rigid three-dimensional framework of corner-sharing MO_6 octahedra and PO_4 tetrahedra.^{1-3,61,62,74,75,79,80} Two distinct sodium

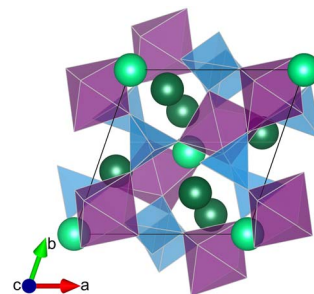


Fig. 1 The primitive rhombohedral NaSICON structure $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$. Key: Na1 (light green), Na2 (dark green), MO_6 (purple), PO_4/SiO_4 (blue).

ion sites, the Na1 (6b) and Na2 (18e) sites, are located in the scaffold cavities. The Na1 site is energetically more favourable and the sublattice is fully occupied at all substitution degrees x .^{1-3,53,62,64,67,68,73-76,79-82} As x increases, Si^{4+} substitute P^{5+} ions and the amount of Na^+ ions on Na2 sites increases to maintain the overall charge neutrality.^{2,3} Transient metastable mid-Na sites located between Na1 and Na2 sites have been reported.^{61,66,75,76,83} However, the occupation of the mid-Na sites is negligible and tends to zero at high Na^+ concentrations, since the occupation of the Na1 and Na2 sites excludes the occupation of the mid-Na sites due to the small distance.^{61,66,68,76} Therefore, we focus on the equilibrium sodium sites, Na1 and Na2, in this work.

The NaSICON structure, which has a large number of Na^+ ion sites and thus a high charge carrier concentration, exhibits fast, three-dimensional Na^+ ion diffusion within the rigid framework.^{2,3,66} As illustrated in Fig. 2, Na2 ions move towards occupied Na1 sites and push the Na1 ions onto adjacent unoccupied Na2 sites.^{2,3,53,61,63,64,66,68,74,84-86} This correlated pushing-out mechanism is based on Coulomb repulsion and the potential energy transfer from ions at energetically higher Na2 sites to ions at lower Na1 sites.^{3,53,58,66,68,87,88} Bottlenecks of the migration pathway are formed by PO_4^- and ZrO_6 -polyhedra edges, depicted as red triangles.^{2,3,69,84,85,89,90} At high substitution concentration, a local minimum occurs along the migration path corresponding to the transient mid-Na site allowing fast Na^+ ion diffusion.^{61,66,68,75,76,83} Three different migration pathways of 80°,

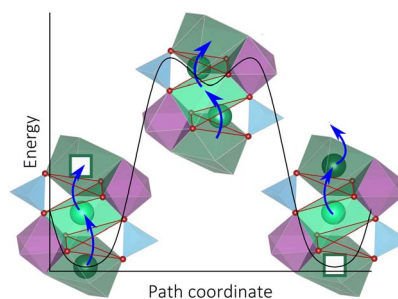


Fig. 2 Correlated pushing-out mechanism shown with blue arrows. One Na2 ion moves towards a Na1 ion pushing it onto an adjacent unoccupied Na2 site. The bottlenecks depicted as red triangles are formed by PO_4^- and ZrO_6 -polyhedra edges. The occupation of the opposing mid-Na sites by the migrating Na^+ ions corresponds to a local minimum at high substitution concentration. Key: Na1 (light green), Na2 (dark green), MO_6 (purple), PO_4/SiO_4 (blue), O (red).

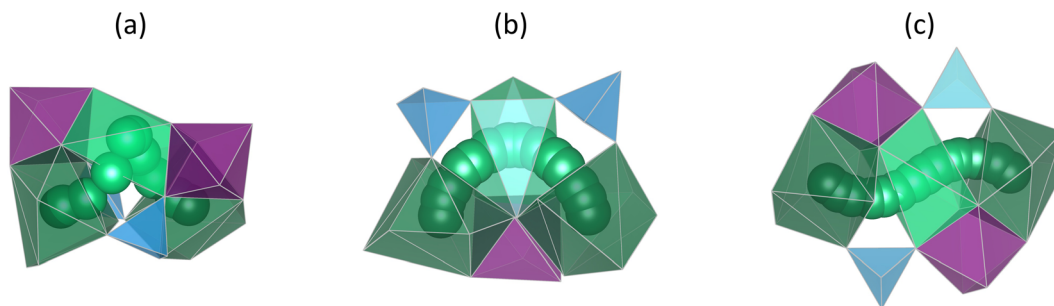


Fig. 3 The different Na⁺ migration pathways according to the angle between the Na2–Na1–Na2 sites involved in the migration of (a) 80°, (b) 90°, and (c) 180°. Key: Na1 (light green), Na2 (dark green), MO₆ (purple), PO₄/SiO₄ (blue).

90° and 180° are distinguished according to the angle between the Na2–Na1–Na2 sites involved in the migration, as depicted in Fig. 3.^{68,70} We have previously shown that the high conductivity and low activation energy of compositions with $1.8 \leq x \leq 2.5$ ^{3,72} is not only attributed to (i) favourable ratio of charge carrier and vacancy concentration,^{6,26,53,66,69,76,81,87,91,92} (ii) high Na⁺–Na⁺ coulombic repulsion which enhances the correlated migration,^{2,58,66,68,69,76,83,87} and (iii) widening of the bottleneck^{6,68,69,73,74,84,85,89,90} as described in the literature, but also to (iv) percolation of sodium ions in favourable silicon rich environments.^{53,70}

3 Methods

3.1 Density functional theory calculations

3.1.1 General computational setup. All calculations were performed by Kohn–Sham DFT^{93,94} with the Vienna *Ab Initio* Simulation Package (VASP).^{95–98} The Generalized Gradient Approximation (GGA) functional parametrized by Perdew–Burke–Ernzerhof (PBEsol) was implemented.⁹⁹ The projector augmented wave (PAW) method was applied.¹⁰⁰ The electronic and ionic relaxation convergence criteria were set to 10^{−4} eV and 0.01 eV Å^{−1}, respectively. A *k*-point mesh centred at the gamma point according to the Monkhorst–Pack scheme was used to sample the Brillouin zone.¹⁰¹ The 2p⁶3s¹ electrons of sodium, the 3s²3p³ electrons of phosphorus, the 3s²3p² electrons of silicon, the 2s²2p⁴ electrons of oxygen, the 5s²4d¹⁰5p² electron of tin, the 5p⁶6s²5d² electrons of hafnium and the 4s²4p⁶4d²5s² electron of zirconium were considered as valence electrons.

3.1.2 Cell transformation. First, the relaxation of the rhombohedral primitive cell of Na₁M₂P₃O₁₂ (M = Zr⁴⁺, Hf⁴⁺, Sn⁴⁺) with 36 atoms was performed with a 2 × 2 × 2 *k*-point mesh and plane waves with an energy cut-off of 520 eV. The volume, ion positions and stress tensors were relaxed simultaneously. The optimized primitive cell was then transformed into a cubic cell with 144 atoms according to the rotation matrix:

$$P = \begin{pmatrix} 1 & 1 & -1 \\ -1 & 1 & 1 \\ 1 & -1 & 1 \end{pmatrix}$$

The Na1 sublattice was fully occupied in all cells while the Na2 sublattice was empty. As described below, the optimisation of the ion positions was performed using 1 × 1 × 1 *k*-point mesh and plane waves with an energy cut-off of 400 eV.

3.1.3 Site energies. The influence of the local environment on the Na⁺ site energies was investigated for the composition Na₁M₂P₃O₁₂ (M = Zr⁴⁺, Hf⁴⁺, Sn⁴⁺). The cubic cell was enlarged to 576 atoms to mitigate finite size effects. Two Na⁺ ions were introduced on Na2 sites to investigate Na⁺–Na⁺ interactions. A homogenous background charge was taken into account compensating the introduced defect charge of +2. To investigate the Na⁺–Si⁴⁺ interactions, one P⁵⁺ ion was substituted by a Si⁴⁺ ion and one Na⁺ ion was introduced on the Na2 site to maintain the charge neutrality.

3.1.4 Coulomb energies. The introduction of a Si⁴⁺ ion on a P⁵⁺ site creates a −1 charged defect, while the introduction of a Na⁺ ion on a vacant Na2 site corresponds to a +1 charged defect.

The Coulomb energies between the introduced defects at a distance *d* were calculated according to eqn (1) using the relative permittivity ϵ_r and the Born effective charges q_B determined in the primitive cells Na₁M₂P₃O₁₂ (M = Zr⁴⁺, Hf⁴⁺, Sn⁴⁺) with 37 atoms by Density Functional Perturbation Theory (DFPT) (Tables S4 and S5[†]).^{102–104}

$$E = \frac{q_1 q_2}{4\pi\epsilon d} \quad (1)$$

The permittivity is defined as $\epsilon = \epsilon_r \epsilon_0$ with the permittivity of the vacuum ϵ_0 . The defect charges are defined as $q = q_{B,rel}e$ with the Born effective charge of the substituted lattice site $q_{B,rel}$ calculated according to eqn (2).

$$q_{B,rel} = q_{B,sub} - q_{B,org} \quad (2)$$

Here, $q_{B,org}$ and $q_{B,sub}$ is the Born effective charge of the original ion and the substituent, respectively.

3.1.5 Migration energies. The correlated migration of two sodium ions was calculated in the cubic cell for Na_{1+x}M₂Si_xP_{3−x}O₁₂ (M = Zr⁴⁺, Hf⁴⁺, Sn⁴⁺) with $x = 0$ and $x = 3$. In the case of the unsubstituted structure ($x = 0$), one additional Na⁺ ion was introduced on the Na2 site resulting in cells with 145 atoms. In the case of the fully substituted structure ($x = 3$), one vacancy was created by removing one Na⁺ ion from a Na2 site resulting in a cell

with 167 atoms. The defect charges were compensated by a uniform background charge. The minimum energy migration paths in 80°, 90° and 180° were determined by the Climbing Image Nudged Elastic Band (CI-NEB) method with five interpolated images.^{105–107}

3.2 Kinetic Monte Carlo

The KMC method was used to simulate the macroscopic sodium ion long-range transport in the NaSICONs by evaluating large stochastic ensembles of sodium ion jumps.^{55,57,108,110} According to transition state theory, the ionic jump is defined by the energy wells of its stable initial and final state, which are separated by an energy barrier E_{mig} . E_{mig} is the difference between the saddle point and the ground state of the energy surface along the migration path and corresponds to the unstable intermediate transition state.^{57,110,111} The Boltzmann distribution gives the probability P for the success of the jump, *i.e.*, for the Na⁺ ions to overcome E_{mig} when possessing sufficiently large kinetic energy.

$$P = \exp\left(-\frac{E_{\text{mig}}}{k_{\text{B}}T}\right) \quad (3)$$

Here, k_{B} is the Boltzmann constant and T the temperature.

The frequency Γ of the sodium ion jump is given by eqn (4).^{57,110,111}

$$\Gamma = \nu \cdot \exp\left(-\frac{E_{\text{mig}}}{k_{\text{B}}T}\right) \quad (4)$$

In this study, the attempt frequency associated with the ion vibration is assumed to be $\nu = 10^{13}$ Hz.¹¹⁰

The mobility of Na⁺ ions μ_{Na} resulting from successful jumps is evoked when an external electric field \vec{E} is applied and the Na⁺ ions move parallel to the direction of \vec{E} . μ_{Na} is given by the drift velocity \vec{u}_{Na} , *i.e.*, the average ionic displacement $\Delta\vec{x}_{\text{Na}}$ per unit time t , in the applied electric field \vec{E} .

$$\mu_{\text{Na}} = \frac{|\vec{u}_{\text{Na}} \cdot \vec{E}|}{|\vec{E}|^2} = \frac{|\Delta\vec{x}_{\text{Na}} \cdot \vec{E}|}{|\vec{E}|^2 \cdot t} \quad (5)$$

The simulated time t is defined by the number of charge carriers N_{Na} , their number of jump attempts N_{attempt} as well as averaged number of jump possibilities N_{jump} , and the attempt frequency ν .

$$t = \frac{N_{\text{attempt}}}{N_{\text{Na}} \cdot \langle N_{\text{jump}} \rangle \cdot \nu} \quad (6)$$

The ionic conductivity σ_{Na} results from the Na⁺ ion concentration c_{Na} and mobility μ_{Na} , and the charge q_{Na} .

$$\sigma_{\text{Na}} = c_{\text{Na}} \cdot \mu_{\text{Na}} \cdot |q_{\text{Na}}| \quad (7)$$

According to Ohm's law, the drift velocity \vec{u}_{Na} and thus the current density \vec{j}_{Na} , is proportional to \vec{E} with μ_{Na} or σ_{Na} , respectively, being the constant of proportionality.

$$\vec{u}_{\text{Na}} = \mu_{\text{Na}} \cdot \vec{E} \quad (8)$$

with

$$\vec{u}_{\text{Na}} = \frac{\vec{j}_{\text{Na}}}{|q_{\text{Na}}| \cdot n_{\text{Na}}} \quad (9)$$

$$\vec{j}_{\text{Na}} = \sigma_{\text{Na}} \cdot \vec{E} \quad (10)$$

Thus, the Na⁺ ion conductivity must be independent of the constant external field which is ensured at the field strength of $\vec{E} = 107$ V m⁻¹ applied in the KMC simulations (Fig. S1†).⁷⁰

KMC simulations were performed in $10 \times 10 \times 10$ cells of Na_{1+x}M₂Si_xP_{3-x}O₁₂ (M = Zr⁴⁺, Hf⁴⁺, Sn⁴⁺) for the compositional range of $0.2 \leq x \leq 2.8$ and temperature range of $450 \text{ K} \leq T \leq 700 \text{ K}$ using the program MOCASSIN with the null-event algorithm.¹⁰⁹

4 KMC model

As shown in eqn (3), the migration barrier must be known for KMC simulations. However, different local environments of the migrating Na⁺ ions lead to different energies of the initial and final states making the energy barrier E_{mig} dependent on the jump directions. Thus, E_{mig} of each jump is defined by the energy of the end states E_{conf} and the directional independent migration energy $E_{\text{mig},0}$.^{57,110,112}

$$E_{\text{mig}} = \frac{E_{\text{conf},f} - E_{\text{conf},i}}{2} + E_{\text{mig},0} \quad (11)$$

In our previous study, we investigated the configurational energy E_{conf} and migration energy $E_{\text{mig},0}$ for Na_{1+x}Zr₂Si_xP_{3-x}O₁₂ ($x = 0, 1, 2, 3$) using DFT.⁷⁰ The calculation of the exact energy of all possible configurations exceeds the computational limit. However, we have shown that they can be predicted with sufficient accuracy based on the DFT calculations of a few compositions using the models described below.⁷⁰

4.1 Configurational energy

The configurational energy E_{conf} describes the energy of the cell resulting from the sum of sodium site energies. The sodium site energies depend on the local cationic environment and thus on the distribution of Si⁴⁺/P⁵⁺ ions and the occupation of Na2 sites. E_{conf} is described by a pair interaction model according to eqn (12).⁷⁰

$$E_{\text{conf}} = \sum_{i=2} N_{\text{Na}}^i \cdot E_{\text{Na}}^i + \sum_{i=1} N_{\text{Si}}^i \cdot E_{\text{Si}}^i \quad (12)$$

Here, N_{Na}^i and N_{Si}^i is the number of Na⁺-Na⁺ pairs and Na⁺-Si⁴⁺ pairs in i NN distance, respectively, with the corresponding interaction energies E_{Na} and E_{Si} . The Na1 sites located in 1NN distance are omitted as we assume them to be fully occupied as described in literature.^{1–3,53,62,64,67,68,73–76,79–82}

4.2 Migration energy

The migration energy $E_{\text{mig},0}$ depends on the migration pathway and the substitution degree. $E_{\text{mig},0}$ of the migration in 80° , 90° and 180° of all substitution fractions can be described by the interpolation between the migration energies in the non-substituted cell with $x = 0$ and the fully substituted cell with $x = 3$ according to eqn (13).⁷⁰

$$E_{\text{mig},0}(x) = \frac{x(E_{\text{mig},0}(x=3) - E_{\text{mig},0}(x=0))}{3} + E_{\text{mig},0}(x=0) \quad (13)$$

5 Investigation at the atomistic level

5.1 Configurational energies

The configurational energies are described by the simple pair interaction model according to eqn (12). We have shown in our previous study that the pair interaction energies can be determined by fitting many different configurations of $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ with $0 \leq x \leq 3$.⁷⁰ However, this approach requires a large computational effort and is therefore not feasible for the exploration of compositions with various M-cationic species. In contrast, in this study we calculate the $\text{Na}^+ - \text{Na}^+$ and $\text{Na}^+ - \text{Si}^{4+}$ pair interaction energies depending on the Na^+ -cation distances in larger cells with minimal substitution

concentration. In this way, the pair interactions can be investigated individually without considering additional compositional effects. This approach allows the study of Na^+ -cation interactions with a greater range while requiring less computational effort. Here, the $\text{Na}^+ - \text{Na}^+$ and $\text{Na}^+ - \text{Si}^{4+}$ pair interactions are investigated for the composition $\text{Na}_1\text{M}_2\text{P}_3\text{O}_{12}$ ($\text{M} = \text{Zr}^{4+}$, Hf^{4+} , Sn^{4+}). For this purpose, a pair of a Na^+ ion and another cation (Na^+ or Si^{4+}) are introduced into the unsubstituted cell. The pair interaction energy is calculated relative to the cell with the furthest Na^+ -cation distance.

Finite size effects are assumed to be negligible when describing the pair interaction energies. Even in the case of the cell with the farthest distance between the introduced cations, the distance to these cations in the neighbouring imaged cells is nevertheless much larger ($d_{\text{Na}^+ - \text{cation}} > 19 \text{ \AA}$).

5.1.1 $\text{Na}^+ - \text{Na}^+$ pair interaction. Fig. 4 shows the interaction energies (red circles, blue triangles, green squares) and Coulomb energies (pink lines) as a function of the Na2–Na2 distance in $\text{Na}_1\text{M}_2\text{P}_3\text{O}_{12}$ ($\text{M} = \text{Zr}^{4+}$, Hf^{4+} , Sn^{4+}). For all compositions, the Na2–Na2 repulsion decreases with distance and is negligible for distances greater than 9.9 \AA .

The Na2–Na2 interaction energies are in good agreement with the Coulomb energies indicating that electrostatic effects are dominant. However, the cation arrangement also affects the interaction energies when the Na2 ions are in the same coordination environment, *i.e.*, at small Na2–Na2 distances, leading

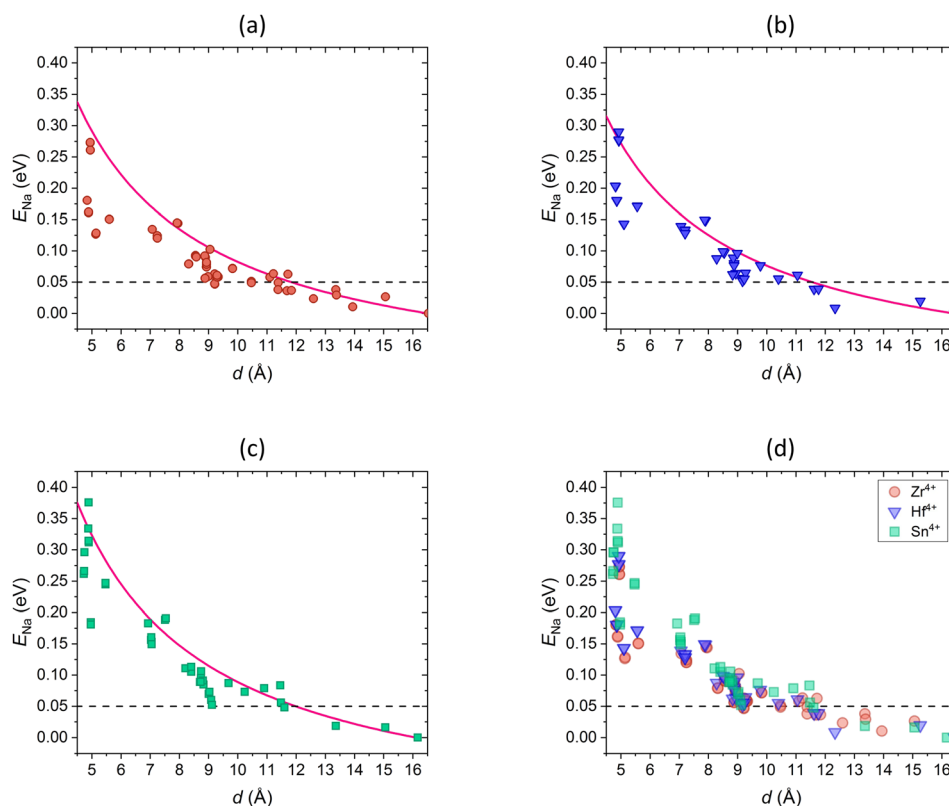


Fig. 4 $\text{Na}^+ - \text{Na}^+$ Coulomb energies (pink line) and interaction energies E_{Na} of the structure $\text{Na}_1\text{M}_2\text{P}_3\text{O}_{12}$ with (a) $\text{M} = \text{Zr}^{4+}$ (red), (b) $\text{M} = \text{Hf}^{4+}$ (blue), (c) $\text{M} = \text{Sn}^{4+}$ (green), and (d) comparison of E_{Na} of all compositions dependent on Na2–Na2 distances d . The dotted line shows the energy limit of $E_{\text{Na}} = 0.05 \text{ eV}$ below which pair interactions are neglected.

to the largest deviations between the Na2–Na2 interaction energies and the Coulomb energies.

The compositions $\text{Na}_1\text{M}_2\text{P}_3\text{O}_{12}$ with $\text{M} = \text{Zr}^{4+}$ (Fig. 4a) and $\text{M} = \text{Hf}^{4+}$ (Fig. 4b) exhibit similar pair interaction energies due to the similar ionic radii of $r_{\text{Zr}^{4+}} = 0.72 \text{ \AA}$ and $r_{\text{Hf}^{4+}} = 0.71 \text{ \AA}$ ¹¹³ and thus similar cell volumes (Fig. S2†) and bond distances (Table S1†).

In the composition with $\text{M} = \text{Sn}^{4+}$ (Fig. 4c) the interaction energies of Na2–Na2 ions at smaller distances are larger than in the compositions with $\text{M} = \text{Zr}^{4+}$, Hf^{4+} but align at larger distances. The volume of the cell with $\text{M} = \text{Sn}^{4+}$ is smaller than that of the cells with $\text{M} = \text{Zr}^{4+}$, Hf^{4+} due to the smaller ionic radii of $r_{\text{Sn}^{4+}} = 0.69 \text{ \AA}$ (Fig. S2†).¹¹³ Therefore, the bond distances in the structure with $\text{M} = \text{Sn}^{4+}$ are smaller (Table S2†) which has a stronger effect on the interactions energies the smaller the distances of Na2–Na2 pairs are.

5.1.2 Na^+ – Si^{4+} pair interaction. Fig. 5 shows the relative energies (red circles, blue triangles, green squares) and the Coulomb energies (pink lines) in dependence on the Na2–Si distance of all compositions ($\text{M} = \text{Zr}^{4+}$, Hf^{4+} , Sn^{4+}). As expected, the attractive Na2–Si pair interactions weaken with increasing distances and are negligible for distances beyond 8.7 \AA .

The calculated interaction energies cannot be described sufficiently by the Coulomb energies. Since the SiO_4 tetrahedra are part of the structural framework, Si^{4+} may not be considered a point defect due to its high covalent bonding character. Thus,

the pair interaction energies may depend not only on electrostatic effects but also on elastic effects describing deformation or distortions of the lattice, as also observed in doped zirconia¹¹⁴ and ceria.^{115,116} The elastic effects are expected to be stronger when the Na2–Si distance is small and the coordination environments of the introduced Na^+ and Si^{4+} ion affect each other. With increasing distances, the elastic effects may be less pronounced and differences between interaction and coulombic energies are smaller.

The Na2–Si interaction energies in the compounds with $\text{M} = \text{Zr}^{4+}$ (Fig. 5a) and $\text{M} = \text{Hf}^{4+}$ (Fig. 5b) agree due to similar structural properties as discussed above. Moreover, Zr^{4+} and Hf^{4+} are both transition elements and exhibit the same valence electron configuration of d^0 .

In comparison, the composition with $\text{M} = \text{Sn}^{4+}$ (Fig. 5c) exhibits stronger Na2–Si interactions at a small distance. On the one hand, this can be attributed to the smaller cell volume and thus smaller bond distances as described above. On the other hand, Sn^{4+} is a main-group element with a different valence electron configuration of d^{10} , which may have an additional impact. Rodrigo *et al.* stated that unoccupied orbitals as in the compositions with $\text{M} = \text{Zr}^{4+}$, Hf^{4+} exhibiting d^0 valence electron configuration allow greater structural flexibility. In contrast, fully occupied d-orbitals as in the compositions with $\text{M} = \text{Sn}^{4+}$ lead to more rigid bonds.¹¹⁷ Thus, cells containing d^0 M-cations may accommodate substituents with lower energy cost

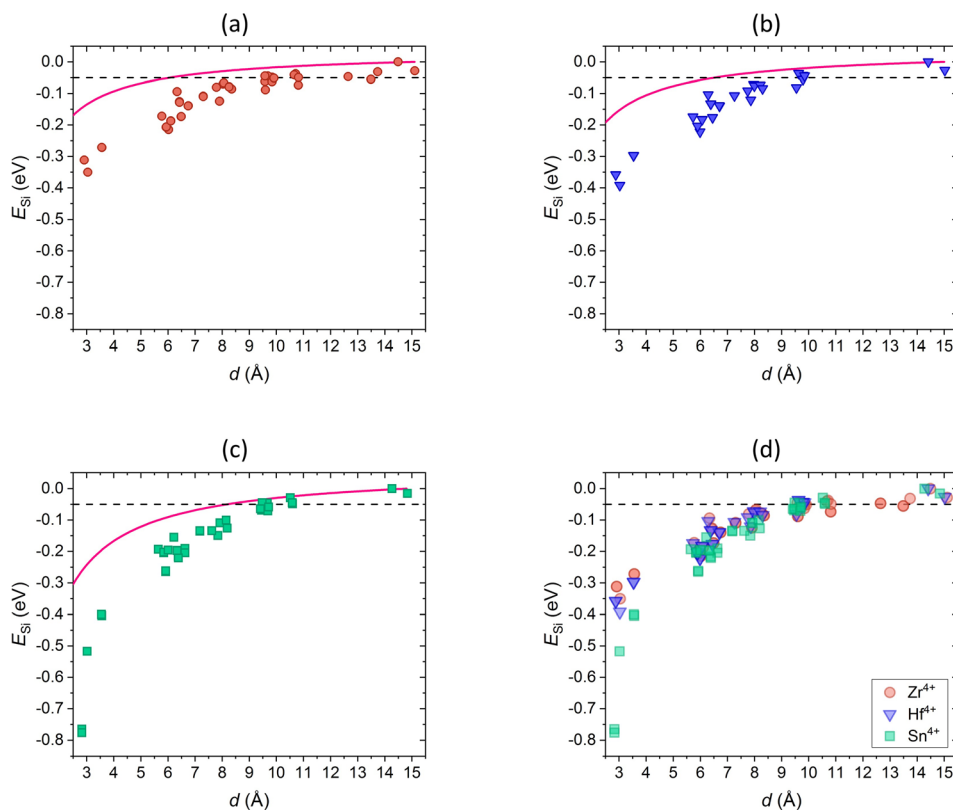


Fig. 5 Na^+ – Si^{4+} Coulomb energies (pink) and interaction energies E_{Si} of the structure $\text{Na}_1\text{M}_2\text{P}_3\text{O}_{12}$ with (a) $\text{M} = \text{Zr}^{4+}$ (red), (b) $\text{M} = \text{Hf}^{4+}$ (blue), (c) $\text{M} = \text{Sn}^{4+}$ (green), and (d) comparison of E_{Si} of all compositions dependent on Na2–Si distances d . The dotted line shows the energy limit of $E_{\text{Si}} = -0.05 \text{ eV}$ below which pair interactions are considered.

compared to cells with d^{10} M-cations. Influences of the different electronic structure of the M-cations on structure and crystal symmetry among $\text{Na}_x\text{M}_{2-x}\text{M}_x^{3+}(\text{PO}_4)_3$ have also been observed in other studies.^{117–122}

In summary, the comparison of NaSCION structures with different M-cations shows that the compounds with $\text{M} = \text{Zr}^{4+}$, Hf^{4+} are not only isovalent but also isostructural, whereas this is not true for the structure with $\text{M} = \text{Sn}^{4+}$, which is in agreement with previous studies.^{117,120,122,123}

In our previous approach to determine configurational energies, only Na2–Na2 pairs in a distance up to 5.1 Å and Na2–Si pairs up to 3.7 Å were considered due to the small size of the cell with 168 atoms. We described the pair interaction energies only dependent on the distance by grouping cations according to similar distance from the Na2 ions. The pair interaction energies of $\text{Na}_{1+x}\text{Zr}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ ($0 \leq x \leq 3$) were fitted according to eqn (12) taking into account 754 configurations whose energies were calculated using DFT.⁷⁰ However, in this study, we show that Na2–Na2 pairs in distances up to 9.9 Å and Na2–Si pairs in distance up to 8.7 Å affect the configurational energy of the cell. The pair interaction energies depend not only on electrostatic effects but also on the cationic coordination and elastic effects at small Na-cation distances and must be considered to describe the configurational energy accurately. We show that calculating only 50 structures with the least substitution and varying Na2-cation distances is sufficient to individually determine all pair interaction energies that affect the overall configurational energy, and thus be able to predict E_{conf} . Additionally, structures with composition $\text{Na}_4\text{M}_2\text{Si}_3\text{O}_{12}$ ($\text{M} = \text{Zr}^{4+}$, Hf^{4+} , Sn^{4+}) in which one P^{5+} ion was introduced onto a Si^{4+} site creating one vacancy on Na2 site (V_{Na}) were investigated. By varying the distance between the P^{5+} and the V_{Na} , the Na^+ – Si^{4+} interaction in highly substituted systems can be deduced as the number of corresponding pairs changes. The results show the expected trend for all compositions: The cells in which P^{5+} is in the nearest neighbour position to V_{Na} are energetically more favourable than the cells in which P^{5+} and V_{Na} are far apart, implying that the configurational energy is lowered by Si^{4+} near the Na2 positions (Table S3†).

Overall, despite the computation of larger cells of 578 atoms, this approach can significantly reduce the computational effort

and therefore allows the study of NASICON materials with a wide range of compositions.

5.2 Migration energies

The different migration pathways of about 80° , 90° and 180° were calculated for the unsubstituted ($x = 0$) and the fully substituted ($x = 3$) system $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ ($\text{M} = \text{Hf}^{4+}$, Sn^{4+}). The results for Zr^{4+} are taken from our previous study.⁷⁰ The energy profiles of the different migration paths in all compositions are shown and discussed in more detail in Section 4 in the ESI.† The migration energies $E_{\text{mig},0}$ of $x = 0$ and $x = 3$ were calculated according to eqn (11) and then predicted for arbitrary substitution concentrations x by linear interpolation according to eqn (13), as shown in Fig. 6.

5.2.1 Dependence on migration path. In all compositions $E_{\text{mig},0}$ decreases with increasing angle of migration pathway due to less steric hindrance of the migrating Na^+ ions. Moreover, the decrease of the migration energy with x is the most for the 80° migration and the least for the 180° migration. Hence, the differences in $E_{\text{mig},0}$ for different angles are largest for $x = 0$ and decrease with increasing x . As the substitution level increases, the influence of the ions adjacent to the migration path becomes greater, as explained below.

5.2.2 Dependence on substitution degree. With increasing x , P^{5+} is replaced by larger Si^{4+} and the amount of Na^+ increases. This leads to three main factors affecting the migration energy, which have been emphasized in previous studies on Na^+ mobility and conductivity in NASICONs: (i) increasing attractive interactions of the migrating Na^+ ions and surrounding Si^{4+} ions,^{53,63,64} (ii) increasing repulsive interactions of the migrating Na^+ ions and surrounding Na^+ ions,^{2,66,68,69,76,83} (iii) increasing size of the bottleneck.^{6,68,69,73,74,84,85,89,90,124} In the following, these factors are examined in more detail to evaluate their impact on the migration energy.

(i) The amount of Si^{4+} near the migration pathway in the structure $\text{Na}_1\text{Zr}_2\text{P}_3\text{O}_{12}$ ($x = 0$) was gradually increased to determine the influence of the interactions between the migrating Na^+ and surrounding Si^{4+} on the migration energy. The Si^{4+} sites to be occupied are illustrated in Fig. S5.† Fig. 7 shows the resulting migration energies dependent on the number of Si^{4+} near the migration pathway. With increasing Si^{4+}

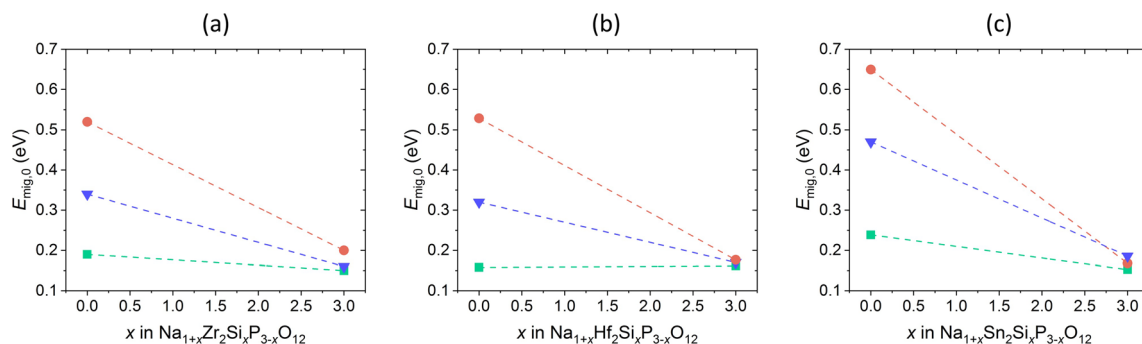


Fig. 6 Interpolated migration energies $E_{\text{mig},0}$ dependent on the substitution degree x of $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ with (a) $\text{M} = \text{Zr}^{4+}$ (taken from ref. 70), (b) $\text{M} = \text{Hf}^{4+}$, (c) $\text{M} = \text{Sn}^{4+}$ of the pathway in 80° (red), 90° (blue) and 180° (green) according to eqn (13).

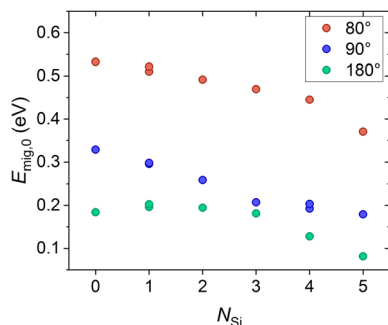


Fig. 7 Migration energy $E_{\text{mig},0}$ of the pathways in 80° (red), 90° (blue) and 180° (green) dependent on the amount of Si^{4+} $N_{\text{Si}^{4+}}$ adjacent to the migration pathway in the structure with composition $\text{Na}_1\text{Zr}_2\text{P}_3\text{O}_{12}$.

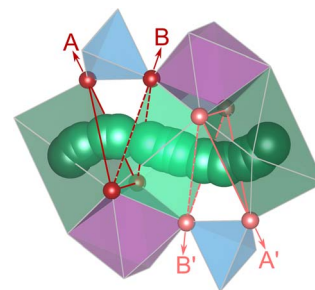


Fig. 9 Bottlenecks of the 180° migration path in $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ formed by three O^{2-} ions of SiO_4/PO_4 tetrahedra and MO_6 octahedra. Key: Key: Na1 (light green), Na2 (dark green), O (red), SiO_4/PO_4 (blue), M/MO_6 (purple).

content the migration energy decreases which is in agreement with the results of Deng *et al.*⁵³ The attractive interactions between the migrating Na^+ ion and the Si^{4+} substituents seem to lower the migration energy due to the stabilization of the transition state.

(ii) To determine the influence of the $\text{Na}^+ - \text{Na}^+$ interactions on the migration energy, the amount of Na^+ near the migrating Na^+ ions was gradually increased in the structure $\text{Na}_1\text{Zr}_2\text{P}_3\text{O}_{12}$ ($x = 0$). The Na^+ positions adjacent to the migration pathway are depicted in Fig. S6,† and the resulting migration energies are shown in Fig. 8. There is no clear dependence of the migration energies on the number of Na^+ ions near the migration pathway. Again, our results agree with the findings of Deng *et al.* explaining the non-monotonic behaviour of migration energy in dependence on Na^+ concentration by a combination of local electrostatic repulsion and local charge imbalance.⁵³ In addition, our results show that the migration energies may depend on the arrangement of the Na^+ ions adjacent to the migration path as explained in detail in Section 5.2 in the ESI.† However, due to the large number of Na^+ sites in the lattice structure, it is not feasible to unambiguously describe the influence of Na^+ site occupation on the migration energy using DFT calculations.

(iii) During the migration, the Na^+ ions pass through different bottlenecks formed by three O^{2-} ions of SiO_4/PO_4 tetrahedra and ZrO_6 octahedra as illustrated in Fig. 9 for the 180° migration path. The bottlenecks A and A' are located near

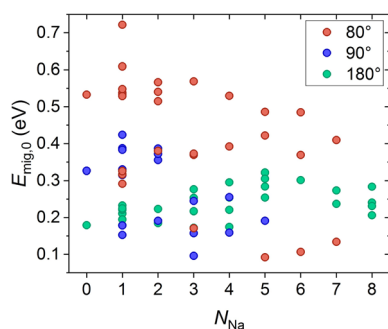


Fig. 8 Migration energy $E_{\text{mig},0}$ of the pathways in 80° (red), 90° (blue) and 180° (green) dependent on the amount of Na^+ N_{Na^+} adjacent to the migration pathway in the structure with composition $\text{Na}_1\text{Zr}_2\text{P}_3\text{O}_{12}$.

the Na2 sites, while the bottlenecks B and B' are located near the Na1 site.^{68,83,85,90} The four different bottlenecks of the migration path are characterized by the size of their area.⁹⁰ As shown in Fig. S9,† bottleneck A is the smallest in most cases, consistent with the literature.^{68,69,89,90} In all compositions the bottleneck areas A and A' increase for $x = 3$ compared to $x = 0$ whereas B and B' do not change. Larger bottlenecks may facilitate Na^+ ion migration resulting in lower migration energy.

In conclusion, our results show that (i) increasing Si^{4+} concentration lowers the migration energy $E_{\text{mig},0}$ due to increasing attractive interactions of the migrating Na^+ ions and surrounding Si^{4+} ions stabilizing the transition state, (ii) there is no clear correlation between $E_{\text{mig},0}$ and the repulsive interactions of the migrating Na^+ ions and surrounding Na^+ ions, and (iii) $E_{\text{mig},0}$ may decrease with increasing size of the bottleneck areas A and A'.

5.2.3 Dependence on M-cations. The comparison of $E_{\text{mig},0}$ of the compositions with different M-cations shows that $E_{\text{mig},0}$ is similar for $\text{M} = \text{Zr}^{4+}$ (Fig. 6a) and $\text{M} = \text{Hf}^{4+}$ (Fig. 6b) but higher in $\text{M} = \text{Sn}^{4+}$ (Fig. 6c). The differences are largest at small substitution content x .

At small x , the $\text{Na}^+ - \text{O}^{2-}$ bond distances are smaller in $\text{M} = \text{Sn}^{4+}$ due to the smaller cell volume. Therefore, the fractional volume of the migrating Na^+ ions in $\text{M} = \text{Sn}^{4+}$ is smaller than in $\text{M} = \text{Zr}^{4+}$, Hf^{4+} , leading to higher steric hindrance and thus higher $E_{\text{mig},0}$. However, at large x , there are no significant differences in the bond distances of the different compositions (Table S6†).

Moreover, the smaller cell volume in $\text{M} = \text{Sn}^{4+}$ leads to smaller bottlenecks (see Fig. S10†) which may also explain the higher migration energies $E_{\text{mig},0}$ in accordance with the literature.^{82,89,124} However, at high x , the differences in $E_{\text{mig},0}$ are small and the results on the effect of the bottleneck on Na^+ migration behaviour must be interpreted with caution. Furthermore, Martínez-Juárez *et al.* have shown that the migration depends strongly on the size of the bottleneck only if it is smaller than the migrating ion, otherwise, it is influenced by the interactions between the migrating ion and the lattice.¹²⁴

In addition, Sn^{4+} exhibits a different electronic structure than Zr^{4+} , Hf^{4+} , as mentioned above. The framework of the structures containing d^0 transition metals (Zr^{4+} , Hf^{4+}) is more

flexible compared to the one with d^{10} main-group elements (Sn^{4+}), and thus may better accommodate the migrating Na^+ ions resulting in lower $E_{\text{mig},0}$.¹¹⁷ Urban *et al.* have elucidated that d^0 transition metals tolerate site distortion with low energy costs.¹²⁵ The local geometry may be different depending on the electronic structure, which could additionally modify the geometry of the bottleneck.^{119,120}

6 Investigation at the macroscopic level

KMC simulations were performed based on the DFT-derived energies from the previous section to clarify the influence of composition on Na^+ conductivity in $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ with $\text{M} = \text{Zr}^{4+}, \text{Hf}^{4+}, \text{Sn}^{4+}$ and $0.01 \leq x \leq 2.8$. As explained before, the simulations require knowledge of the configuration energies predicted by eqn (12) using pair interaction energies individually calculated and the migration energies determined by eqn (13) using the migration energies of the unsubstituted and fully substituted structure (Section 5.2).

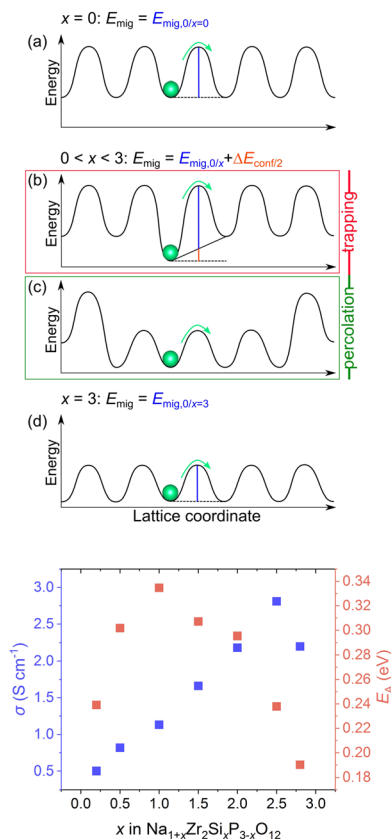


Fig. 10 (Top) Energy landscape of Na^+ positions and migration barrier E_{mig} in the lattice $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ dependent on the substitution content x . (a) Non-substituted structure ($x = 0$) with uniform energy landscape, (b) low substituted structure where Na^+ ions are trapped in Si^{4+} rich environments, (c) high substituted structure where Na^+ ions percolate between Si^{4+} rich environments, (d) fully substituted structure ($x = 3$) with uniform energy landscape. (Bottom) Resulting ionic conductivity σ at 573 K and activation energy E_A in dependence of substitution content x in $\text{Na}_{1+x}\text{Zr}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$. Values are taken from ref. 70.

In our previous study of $\text{Na}_{1+x}\text{Zr}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$, we have already revealed the behaviour of the conductivity and the activation energy is strongly influenced by the local ionic environment of the Na^+ sites, as illustrated in Fig. 10.⁷⁰ The conductivities simulated at 573 K and activation energies of $\text{Na}_{1+x}\text{Zr}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ obtained in this earlier work are shown in the bottom plot of Fig. 10.⁷⁰ In the non-substituted structure the migration barrier E_{mig} only depends on the migration energy $E_{\text{mig},0}$ as the energy landscape is uniform (Fig. 10a). However, due to the introduction of substituents, E_{mig} depends on the migration energy $E_{\text{mig},0}$ and the configurational energy E_{conf} (Fig. 10b). At small x , Na^+ ions are trapped in low energy states near the introduced Si^{4+} ions due to favourable attractive interactions. The depth of the traps increases with the number of adjacent Si^{4+} leading to low conductivities and an increase in activation energy. But, with increasing x , percolation paths are formed due to the large number of Si^{4+} (Fig. 10c), which explains the increase in Na^+ conductivity and the decrease in the activation energy. In the fully substituted structure, the energy landscape is uniform and E_{mig} only depends on the migration energy $E_{\text{mig},0}$ (Fig. 10d). Here, the activation energy is lowest, since $E_{\text{mig},0}$ decreases with x . However, at very high substitution content, the number of vacant sodium sites is insufficient leading to a decrease in ionic conductivity.

In this study, we investigate the influence of different M-cations on the Na^+ diffusion behaviour in NaSICONs. The Na^+ ion conductivities, mobilities, and activation energies obtained from the KMC simulations are discussed below.

Fig. 11 shows the ionic conductivity dependent on x in $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ with $\text{M} = \text{Zr}^{4+}, \text{Hf}^{4+}, \text{Sn}^{4+}$. As expected, the conductivity increases with temperature in all compositions. The conductivities of the compounds with $\text{M} = \text{Zr}^{4+}$ (Fig. 11a) and $\text{M} = \text{Hf}^{4+}$ (Fig. 11b) show similar dependence on x as explained above and differ only slightly at higher x due to small differences in the migration energy $E_{\text{mig},0}$. In both structures, the maximum conductivity is reached at $x = 2.5$. For $\text{M} = \text{Sn}^{4+}$ (Fig. 11c), the ionic conductivities are up to three orders of magnitude lower at small x in accordance with the literature.^{89,120} In this structure, the attractive $\text{Na}^+-\text{Si}^{4+}$ interactions are much stronger at small distances resulting in deeper traps of Na^+ ions, and the migration energies are higher at small x . The conductivity increases strongly at around $1.0 \leq x \leq 1.5$ due to the decrease in $E_{\text{mig},0}$ and reaches the maximum at $2.0 \leq x \leq 2.5$. Compared to $\text{M} = \text{Zr}^{4+}, \text{Hf}^{4+}$, the maximum of conductivity is, first, lower by one order of magnitude because the Na^+ ions are trapped even at higher substitution levels. Second, the maximum shifts to lower substitution concentration due to the strong Na^+-Na^+ repulsion, leading to unfavourable Na^+ site energies and thus to a sharp decrease in conductivity.

In short, when comparing NaSICONs with different M-cations, the amplitude and maximum of the Na^+ conductivity are mainly determined by the Na^+ -cation pair interactions. This hypothesis is verified by the results of KMC simulations, where the Na^+ -cation pair interactions are not considered, as shown in Fig. S11.† Here, the conductivities of the composition with $\text{M} = \text{Sn}^{4+}$ are only slightly lower compared to those of the composition with $\text{M} = \text{Zr}^{4+}, \text{Hf}^{4+}$, which is due to the higher migration energies $E_{\text{mig},0}$.

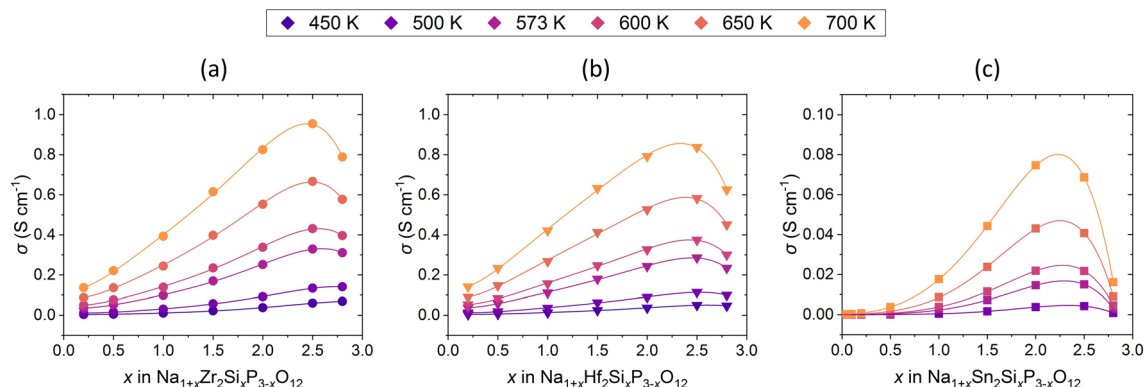


Fig. 11 Na^+ conductivity σ dependent on substitution content x of $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ with (a) $\text{M} = \text{Zr}^{4+}$ ($0.2 \leq x \leq 2.8$), (b) $\text{M} = \text{Hf}^{4+}$ ($0.2 \leq x \leq 2.8$), (c) $\text{M} = \text{Sn}^{4+}$ ($0.01 \leq x \leq 2.8$) in $10 \times 10 \times 10$ cells in the temperature range of $450 \text{ K} \leq T \leq 700 \text{ K}$.

The comparison of conductivities obtained in this work and the total conductivities reported in the literature are shown in Fig. 12. The conductivities of compositions with $\text{M} = \text{Zr}^{4+}$ (Fig. 12a) and $\text{M} = \text{Hf}^{4+}$ (Fig. 12b) are in good agreement with experimental results at small and intermediate x , but are larger at high x and the maximum shifts to larger x values. However,

the literature data scatter widely.^{9,18,53} The total conductivity is composed of the bulk conductivity and the grain boundary conductivity, the latter being strongly influenced by the sample preparation process.^{18,26,53,126} Poor microstructure, density, size of grains *etc.* lead to significantly low grain boundary conductivities, which determine the overall conductivity.^{53,126} By

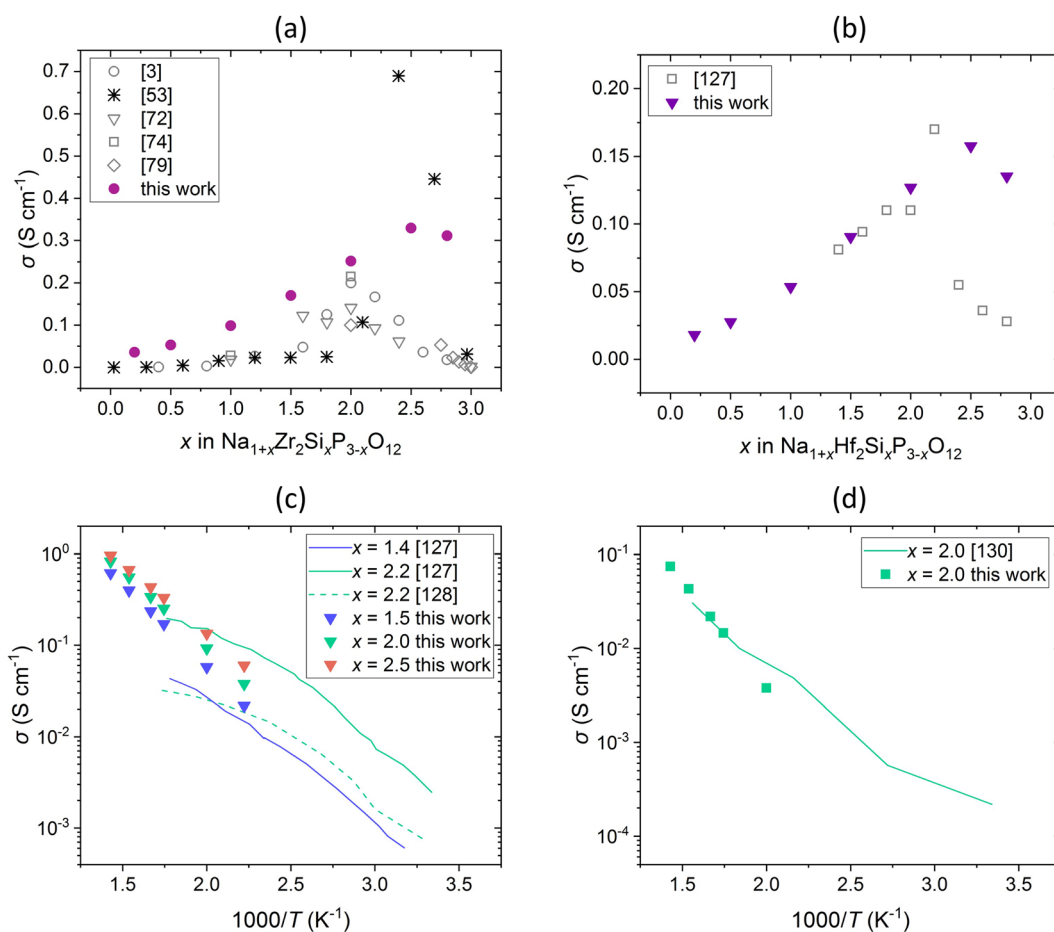


Fig. 12 Comparison of Na^+ conductivity σ in dependence on (a and b) substitution content x and (c and d) temperature T of $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ with (a) $\text{M} = \text{Zr}^{4+}$, (b and c) $\text{M} = \text{Hf}^{4+}$, and (d) $\text{M} = \text{Sn}^{4+}$ in $10 \times 10 \times 10$ cells. Literature data of experimental studies^{3,72,74,79,127,128,130} as well as KMC simulations⁵³ are shown.

optimizing the microstructure, and thus decreasing grain boundary resistance, the bulk conductivity gains influence and the total conductivity increases.^{26,126} Ma *et al.* revealed that the total conductivity is largely underestimated in literature and reported high bulk conductivity of $1.5 \times 10^{-2} \text{ S cm}^{-1}$ at room temperature for substitution content of $x = 2.4$ when optimizing the microstructure, which is in agreement with our results.²⁶ It is also worth mentioning that the interpolated migration energies $E_{\text{mig},0}$ may be underestimated at large x compared to $E_{\text{mig},0}$ calculated with DFT, as shown in our previous study for $\text{Na}_{1+x}\text{Zr}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$, and thus the conductivities may be overestimated.⁷⁰ However, the conductivities are in the same order of magnitude and the dependence on the substitution content is described accurately. A similar behaviour was found in a recent study by Deng *et al.* who investigated the ionic conductivity in $\text{Na}_{1+x}\text{Zr}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ using KMC simulations based on local-cluster expansion and DFT-NEB migration barriers.⁵³ Moreover, the simulated temperature dependence of the ionic conductivity of $M = \text{Hf}^{4+}$ (Fig. 12c) and $M = \text{Sn}^{4+}$ (Fig. 12d) agrees with experimental values. However, the values reported in different studies for the composition with $M = \text{Hf}^{4+}$ and $x = 2.2$ also vary, which could be due to similar reasons as those discussed above.^{127,128} Besides, similar conductivities for the compounds with

$M = \text{Zr}^{4+}, \text{Hf}^{4+}$ have been reported in previous studies, which coincide with our results.^{6,120,123,127,129} Overall, the good agreement of our results with the literature data confirms the suitability of this method for studying conductivity in NaSCION-type structures.

Fig. 13 shows the Na^+ ion mobility in $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ with $M = \text{Zr}^{4+}, \text{Hf}^{4+}, \text{Sn}^{4+}$ dependent on the substitution level. In this way, the Na^+ ion diffusion behaviour is described without considering the increase of the charge carrier. Thus, the assumptions about the effects of the percolation paths formed by Si^{4+} and the low migration energy at high x are verified. The mobility shows a similar dependence on x as the conductivity. The maximum mobility is observed at $2.0 \leq x \leq 2.5$ in the compositions with $M = \text{Zr}^{4+}, \text{Hf}^{4+}$ and at $x = 2$ in the composition with $M = \text{Sn}^{4+}$. The differences in the mobility are similar to those for conductivity and can be explained by the stronger attractive $\text{Na}^+ - \text{Si}^{4+}$ and repulsive $\text{Na}^+ - \text{Na}^+$ interactions in the structure with $M = \text{Sn}^{4+}$, as described in detail above.

The temperature dependence of the ionic conductivities follows an Arrhenius behaviour (Fig. S12†). Fig. 14a shows the obtained activation energies E_A of all investigated $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ compositions. In the non-substituted and fully substituted composition, E_A depends only on $E_{\text{mig},0}$ as the energy landscape is uniform (see Fig. 10a and d). However, the introduction of

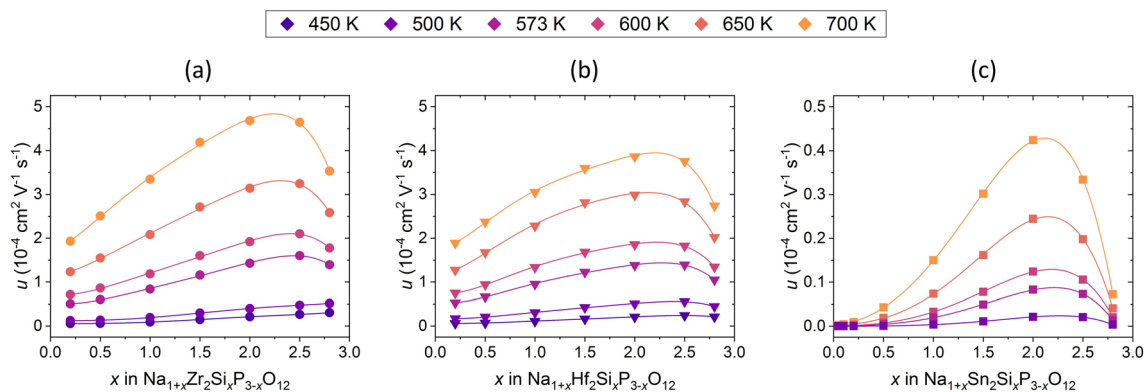


Fig. 13 Na^+ mobility u dependent on substitution content x of $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ with (a) $M = \text{Zr}^{4+}$ ($0.2 \leq x \leq 2.8$), (b) $M = \text{Hf}^{4+}$ ($0.2 \leq x \leq 2.8$), (c) $M = \text{Sn}^{4+}$ ($0.01 \leq x \leq 2.8$) in $10 \times 10 \times 10$ cells in the temperature range of $450 \text{ K} \leq T \leq 700 \text{ K}$.

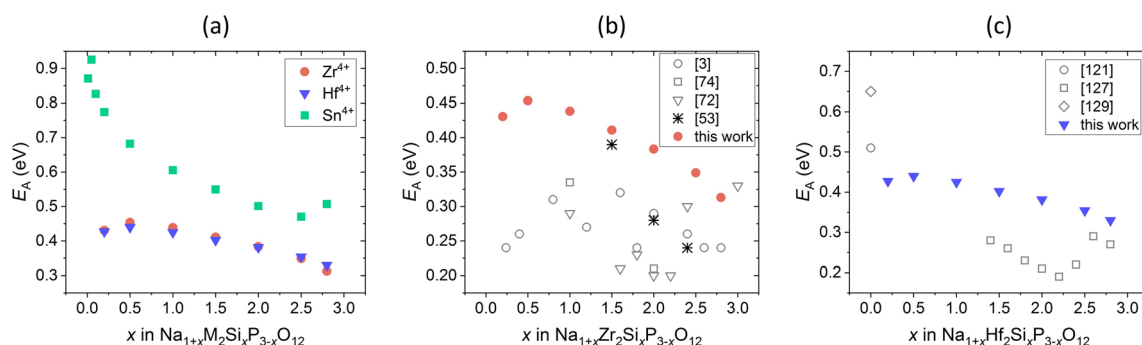


Fig. 14 (a) Activation energies E_A dependent on substitution content x of $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ with $M = \text{Zr}^{4+}$ ($0.2 \leq x \leq 2.8$) (red), Hf^{4+} ($0.2 \leq x \leq 2.8$) (blue), and Sn^{4+} ($0.01 \leq x \leq 2.8$) (green) obtained from Arrhenius plots (Fig. S12†). (b) Comparison of E_A of $\text{Na}_{1+x}\text{Zr}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ ($0.2 \leq x \leq 2.8$) (orange) with values obtained from experiments (grey)^{3,72,74} and computational studies (black).⁵³ (c) Comparison of E_A of $\text{Na}_{1+x}\text{Hf}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ ($0.2 \leq x \leq 2.8$) (orange) with values obtained from experiments (grey).^{120,127,129}

substituents leads to states with different energy (see Fig. 10b and c) and E_A depends also on the different cationic environments which are considered in the KMC simulations. As explained in Fig. 10, E_A is high at small x as Na^+ ions are trapped in low energy states. At higher x , E_A decreases because Na^+ ions percolate between favourable Si^{4+} -rich positions and the migration energy $E_{\text{mig},0}$ decreases.

While E_A of the compositions $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ with $\text{M} = \text{Zr}^{4+}$, Hf^{4+} are similar with a maximum around $x = 1.0$, E_A for $\text{M} = \text{Sn}^{4+}$ is much higher with a maximum at $x \approx 0.05$. This is due to stronger attractive $\text{Na}^+-\text{Si}^{4+}$ interactions (see Fig. 5) which lead to more effective trapping even for small x . He *et al.* have elucidated that a locally flat energy landscape and low barriers of the high-energy site, *i.e.* the Na2 site, facilitates the concerted migration.⁵⁸ However, due to the stronger $\text{Na}^+-\text{Si}^{4+}$ interactions in the structure with $\text{M} = \text{Sn}^{4+}$, which lowers the Na2 site energy, the local energy landscape becomes less uniform and the energy barriers increase, resulting in higher E_A . The E_A of all compositions and the differences between them decrease with increasing x , as the decreasing migration energies $E_{\text{mig},0}$, which have the dominant impact, converge (see Fig. 6). Moreover, the energy landscape becomes more uniform with increasing Si^{4+} content, with the differences in $\text{Na}^+-\text{Si}^{4+}$ interactions losing influence on the migration barrier and thus on E_A . At a high substitution level, E_A of the composition with $\text{M} = \text{Sn}^{4+}$ increases slightly caused by highly unfavourable repulsive Na^+-Na^+ interactions (see Fig. 4) which may increase the Na2 site energy strongly.

As shown in Fig. 14b, the activation energies of $\text{Na}_{1+x}\text{Zr}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ determined in this study are higher than those obtained from a.c. conductivity measurements and *ab initio* molecular dynamics simulations, especially at small substitution contents. However, the experimental values vary widely as discussed above. The calculated activation energies of $\text{Na}_{1+x}\text{Hf}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ are higher than the literature data at intermediate x and agree well at high x , as Fig. 14c shows. In general, the activation energies determined in this work are in reasonable accordance with the literature values. However, there are only a few or strongly fluctuating data in the literature, thus the comparison should be made with caution.

It can be concluded that the Na^+ transport properties mainly depend on the trapping of Na^+ by the introduced Si^{4+} at small x , the migration energy $E_{\text{mig},0}$ at high x , and strong Na^+-Na^+ repulsion at very high x . The Na^+ -cation interactions and thus the Na^+ transport properties can be influenced by the choice of M cations. Moreover, the ionic conductivity and mobility depend on the ratio of occupied to vacant sodium sites. Thus, our study points out that no simple correlation can be established to describe the ionic conductivity. The maximum of Na^+ mobility and conductivity is reached at a high substitution content of $2.0 \leq x \leq 2.5$ due to low migration energy and optimal ratio of unoccupied to occupied charge carrier sites.

7 Conclusion

We studied the influences of the Si^{4+} substitution concentration x , M-cation and temperature on Na^+ ion transport in the multi-

element NaSICON-type structure $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ ($\text{M} = \text{Zr}^{4+}$, Hf^{4+} , Sn^{4+} and $0 \leq x \leq 3$). Therefore, we combined accurate DFT calculations and KMC simulations for the investigation at both atomistic and macroscopic levels with affordable computational effort.

The DFT calculations show that the Na^+ site energy depends on Na^+-Na^+ interactions resulting mainly from electrostatic effects and $\text{Na}^+-\text{Si}^{4+}$ interactions resulting from both electrostatic and elastic effects. Lower Na^+ and higher Si^{4+} content in the local environment leads to lower Na^+ site energy. However, the size and electronic structure of the M-cation must also be considered when describing the configurational energies. Smaller and more rigid MO_6 octahedra result in stronger pair interactions.

Moreover, we have shown that the migration energy $E_{\text{mig},0}$ depends on various factors for different x : At low x , $E_{\text{mig},0}$ is mainly influenced by the migration pathway. However, with increasing x , the ions adjacent to the migration path gain influence. $E_{\text{mig},0}$ decreases with increasing Si^{4+} concentration because of favourable attractive interactions of the migrating Na^+ ions and surrounding Si^{4+} ions. In addition, the increasing size of the bottleneck may lower $E_{\text{mig},0}$. Furthermore, $E_{\text{mig},0}$ depends on the M-cation. The size of the M-cation affects the size of the bottleneck, and the electronic structure of the M-cation affects the flexibility of the structural framework. Smaller bottlenecks and more rigid MO_6 octahedra may increase $E_{\text{mig},0}$ and could explain the highest values for compositions with $\text{M} = \text{Sn}^{4+}$.

Based on DFT-derived energies, we performed KMC simulations to investigate the macroscopic Na^+ conductivity. Using $\text{Na}_{1+x}\text{M}_2\text{Si}_x\text{P}_{3-x}\text{O}_{12}$ as an example, we showed that the Na^+ transport properties in NaSICON structures are determined by (i) the Na^+ trapping by introduced Si^{4+} at small x , (ii) the migration energy $E_{\text{mig},0}$ at intermediate to high x , and (iii) the availability of vacant Na^+ site as well as the Na^+-Na^+ repulsion at very high x . Thus, the conductivity of compositions with $\text{M} = \text{Zr}^{4+}$, Hf^{4+} reaches the maximum at $x = 2.5$ due to percolation pathways formed by Si^{4+} rich environments, low $E_{\text{mig},0}$ and optimal density of charge carrier sites. For the composition with $\text{M} = \text{Sn}^{4+}$, the ionic conductivities are significantly lower because of the stronger attractive $\text{Na}^+-\text{Si}^{4+}$ interactions which form deeper traps for the Na^+ ions. In addition, the conductivity maximum is shifted to lower substitution concentrations of $2.0 \leq x \leq 2.5$ due to the stronger Na^+-Na^+ repulsion leading to unfavourable Na^+ site energies and thus to a sharp decrease in conductivity at high x .

The resulting activation energies depend on the local cationic environments of the Na^+ sites. E_A is high at small x because the Na^+ ions are trapped in low energy states, whereas E_A decreases at higher x due to the Na^+ percolation between favourable Si^{4+} rich positions as well as the decrease of $E_{\text{mig},0}$. The activation energy of the composition with $\text{M} = \text{Sn}^{4+}$ is higher and the maximum appears at lower x compared to the compositions with $\text{M} = \text{Zr}^{4+}$ and Hf^{4+} because of the more effective trapping due to stronger attractive $\text{Na}^+-\text{Si}^{4+}$ interactions.

Our results show that the Na⁺ ion transport in NaSICONs can be modified by different cation substitution strategies in the host lattice Na₁M₂PO₁₂.

A rising number of Na⁺ ions supports the correlated ionic migration as high energy sites are occupied, and also leads to an increase in ionic conductivity. One way to adjust the concentration of the Na⁺ charge carrier is to incorporate excess Na⁺ into the NaSICON compounds. Indeed, few studies have investigated the influences of excess Na⁺ in NaSICONs^{90,91,131–133} revealing that conductivity increases and activation energy decreases, based on the increase in Na⁺ charge carrier^{91,133} and enhanced mobility by the widening of the bottlenecks.^{90,133}

The amount of Na⁺ charge carrier can also be modified when the M⁴⁺ and P⁵⁺ sites are substituted with cations with various valence. As shown in this study, the substitution with subvalent cations leads not only to the increase in Na⁺ concentration but also to the decrease in Na⁺ ion migration energy due to the lower electrostatic repulsion with the migrating Na⁺ ions. Therefore, the introduction of divalent or trivalent substituents could potentially further increase the Na⁺ ion conductivity in NaSICONs. However, subvalent substituents could also cause a stronger trapping effect which in turn decreases the Na⁺ ion mobility.

Furthermore, iso- and aliovalent substituents with bigger ionic sizes could enlarge the cell volume and thus the bottlenecks, possibly leading to an increase in Na⁺ ion mobility.

Various studies have shown that the aliovalent substitution of M⁴⁺ by divalent cations, such as Mg²⁺,^{22,66,134–138} Zn²⁺,^{32,139,140} Co²⁺,¹³⁹ Ca²⁺,^{29,141} and trivalent cations, such as In³⁺,^{119,142,143} Sc³⁺,^{92,119,143–147} Y³⁺,^{139,140,143,148} La³⁺,^{24,148} Pr³⁺, Eu³⁺, Lu³⁺,¹⁴⁹ improves the Na⁺ mobility and conductivity due to an increase in Na⁺ ions coupled with enhanced correlated Na⁺ ion migration but also due to the modification of the phase purity and microstructure of the ceramics.

Based on our results, another way to optimize the Na⁺ ion transport in NaSICONs could be to completely substitute P⁵⁺ ions by Si⁴⁺ ions while introducing M⁵⁺ ions to ensure that sufficient unoccupied Na⁺ sites are available. Supervalent M-substitution in NaSICONs materials has been poorly investigated, but studies of Na_{1+x-y}M_yZr_{2-y}Si_xP_{3-x}O₁₂ with M⁵⁺ = V, Nb, Ta show promising conductivities up to 5.5 × 10⁻³ S cm⁻¹ for Na_{3.3}Zr_{1.9}Nb_{0.1}Si_{2.4}P_{0.6}O₁₂.^{135,140,150}

Additionally, the Na⁺ ion mobility can be influenced by Na⁺-cation interactions, which are determined by the valence electron configuration of the M cations. In this study, we have shown that d⁰ valence orbitals induce weaker Na⁺-cation interactions compared to d¹⁰ valence orbitals, resulting in weaker Na⁺ ion trapping and thus higher Na⁺ ion mobility. Thus, the introduction of M cations exhibiting d⁰ valence electron configuration, such as Mg²⁺, Sc³⁺, Ce⁴⁺, V⁵⁺, appears to provide a sound strategy to optimize the Na⁺ ion mobility.

In summary, the method proposed in this study is suitable to investigate various NaSICON compositions over large length and time scales with low computational effort. Our results provide a comprehensive explanation of the Na⁺ diffusion behaviour in NaSICONs to optimize the ionic conductivity.

Conflicts of interest

There are no conflicts to declare.

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