

**Highlighting a study on the battery cycling and atomic structure stability of the metastable 'R' polymorph of  $\text{Nb}_2\text{O}_5$  from Professor Megan M. Butala's laboratory in the Department of Materials Science and Engineering at the University of Florida (United States).**

$R\text{-Nb}_2\text{O}_5$  has an 'idealized'  $\text{V}_2\text{O}_5$  structure and Wadsley-Roth-like structural stability during Li-ion battery cycling

With Wadsley-Roth-like 'slabs' and an 'idealized'  $\text{V}_2\text{O}_5$  structure, metastable  $R\text{-Nb}_2\text{O}_5$  bridges two well-studied families of Li-ion battery electrodes. Inter- and intrapolyhedral connectivity stabilize the structure against polyhedral rotations during lithiation and delithiation, providing excellent reversibility with negligible structure changes during cycling.

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# *R*-Nb<sub>2</sub>O<sub>5</sub> has an 'idealized' V<sub>2</sub>O<sub>5</sub> structure and Wadsley–Roth-like structural stability during Li-ion battery cycling†

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The adoption of batteries across diverse applications requires electrode materials with a wider range of performance metrics, such as cost, safety, and material availability. Along the path to discovering new commercially viable materials, a fundamental understanding of chemical and atomic structure features that provide structural stability and effective ion transport is essential. In support of new understanding, we report the cycling behavior of metastable *R*-Nb<sub>2</sub>O<sub>5</sub>. *R*-Nb<sub>2</sub>O<sub>5</sub> adopts an 'idealized' V<sub>2</sub>O<sub>5</sub> structure, in which [NbO<sub>6</sub>] octahedra alternate in edge- and corner-sharing resulting in ReO<sub>3</sub>-like slabs, whereas Wadsley–Roth materials have ReO<sub>3</sub>-like blocks, linked through edge-sharing octahedra at intersecting crystallographic shear planes. We find that this slab structure is stable during cycling, with minor atomic structure changes and cycling curves that are symmetric on discharge and charge, resembling the behavior of Wadsley–Roth materials more than other related materials, such as ReO<sub>3</sub>, V<sub>2</sub>O<sub>5</sub>, or Nb<sub>2</sub>O<sub>7</sub>F. Based on our findings, *R*-Nb<sub>2</sub>O<sub>5</sub> can serve as a 'structural bridge' between Wadsley–Roth block structures and V<sub>2</sub>O<sub>5</sub>, through which we can relate inter- and intra-polyhedral structures to cycling behavior and structural stability during cycling.

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## 1 Introduction

Early transition metal oxides featuring crystallographic shear planes are a technologically and fundamentally compelling family of Li-ion battery electrode candidates. These materials, sometimes referred to as Wadsley–Roth or Magnéli phases,<sup>1–5</sup> have demonstrated excellent performance as high potential anodes. With operating potentials between 1 V and 1.5 V and excellent rate capabilities, they offer a pathway to safe, high-power Li-ion batteries as alternatives to graphite and Li<sub>4</sub>Ti<sub>5</sub>O<sub>12</sub>.<sup>6–8</sup> Wadsley–Roth (WR) materials can also have multi-electron redox, in which more than one redox reaction occurs per redox active transition metal, contributing to high energy densities, *e.g.*, reduction of Nb<sup>5+</sup> to Nb<sup>3+</sup>, allowing for storage of >1 mol Li per transition metal, M.<sup>5,9–12</sup>

In addition to being technologically relevant, WR materials provide a foundation for identifying atomic and electronic structure features that support effective transport of ions and electrons.<sup>9,13,14</sup> WR materials have ReO<sub>3</sub>-like blocks, in which [MO<sub>6</sub>] octahedra are corner-sharing (Fig. 1a and c) with square

channels that provide fast Li transport. These blocks are connected across crystallographic shear planes, at which [MO<sub>6</sub>] octahedra are edge-sharing (Fig. 1b and c). During lithiation of ReO<sub>3</sub>, [ReO<sub>6</sub>] octahedra rotate around corner-sharing vertices.<sup>4,15</sup> In contrast, in WR materials, the edge-sharing octahedra at crystallographic shear planes stabilize against this rotation, keeping square channels accessible for fast Li<sup>+</sup> transport.<sup>9,11</sup> In addition to structural stability, edge-sharing octahedra have a favorable overlap of d-electron orbitals, which results in high electronic conductivity upon even minor reduction, contributing to their high-rate capabilities.<sup>11,16,17</sup>

Among WR and related materials studied as battery electrodes, there are many niobates,<sup>16,18</sup> including those with the chemical formula Nb<sub>2</sub>O<sub>5</sub>.<sup>17,19–24</sup> We report here, for the first time, the cycling behavior and charge storage mechanism of yet another polymorph *R*-Nb<sub>2</sub>O<sub>5</sub>. '*R*' represents a "neutral designation",<sup>19,25,26</sup> and is not related to the crystal system or preparation conditions. This metastable polymorph adopts an idealized V<sub>2</sub>O<sub>5</sub> structure (Fig. 1f and 2)<sup>2</sup> and was first identified by Gruehn.<sup>25</sup> *R*-Nb<sub>2</sub>O<sub>5</sub> can be described relative to WR block structures as having ReO<sub>3</sub>-like slabs (rather than blocks) connected by parallel (rather than perpendicular) shear planes (Fig. 2a).<sup>2,27</sup>

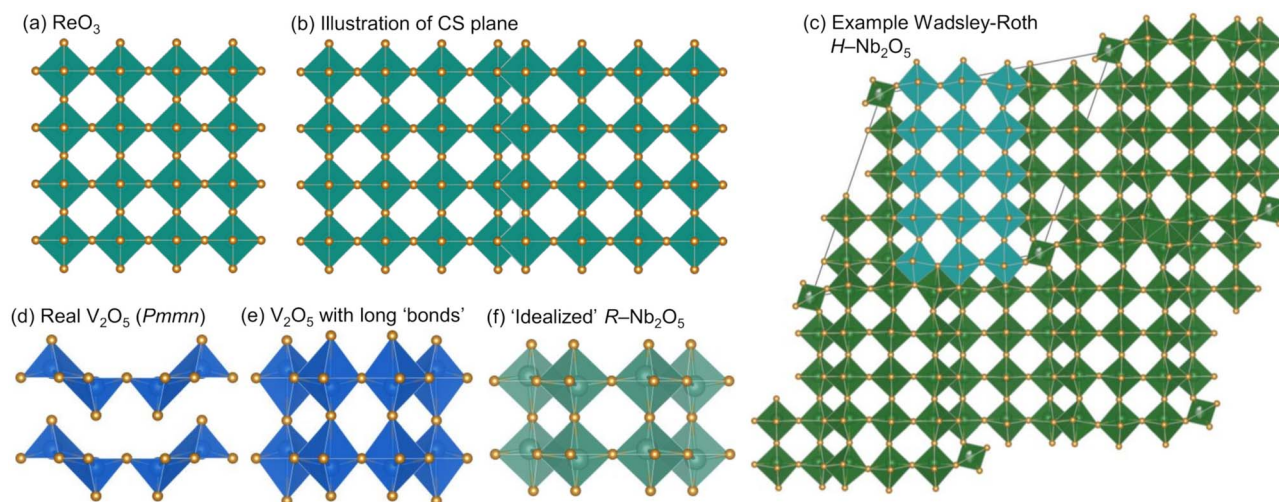
WR block structures can be described by the connectivity of [MO<sub>6</sub>] octahedra, specifically in terms of the number of corner-sharing octahedra in a given direction. For example, a block that is *m* corner-sharing octahedra wide, *n* high, and infinite in the third direction would be represented as (*m* × *n*)<sub>∞</sub>.<sup>3</sup> For *H*-Nb<sub>2</sub>O<sub>5</sub>, this representation would be (3 × 5)<sub>∞</sub> (Fig. 1c).

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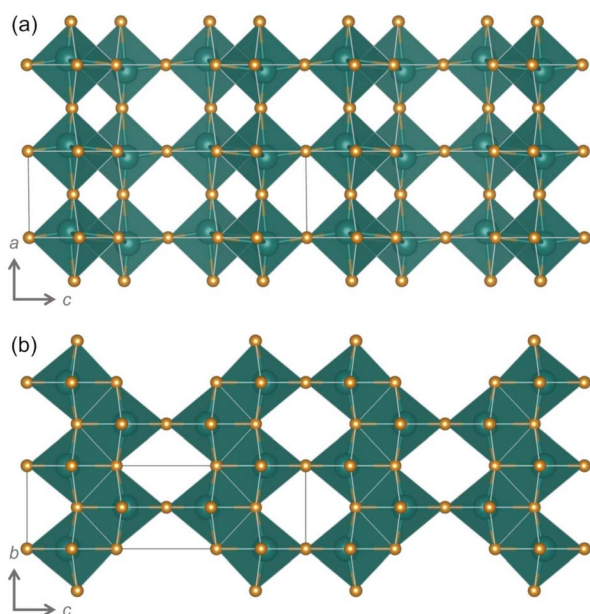
† Electronic supplementary information (ESI) available: Additional details and results from Rietveld refinements of atomic structure models as well as cycling data in Swagelok cells, representative of cycling from which *ex situ* discharged and charged powders were prepared, and coin cells cycled at C/10 and 1C. See DOI: <https://doi.org/10.1039/d2ta08653k>







**Fig. 1** (a)  $\text{ReO}_3$  has only corner-sharing  $[\text{MO}_6]$  octahedra. (b) Adjacent  $\text{ReO}_3$ -like blocks offset by  $\frac{1}{2}$  an octahedron in 2 directions make a crystallographic shear (CS) plane with edge-sharing  $[\text{MO}_6]$  octahedra. (c) Wadsley–Roth structures are comprised of  $\text{ReO}_3$ -like blocks connected by intersecting CS planes;  $H\text{-Nb}_2\text{O}_5$  is shown as an example. (d)  $\text{V}_2\text{O}_5$  has layers of edge- and corner-sharing  $[\text{VO}_5]$  square pyramids. (e) Connecting the long V–O distance across the layers, a relationship between (d) real and (f) ‘idealized’  $\text{V}_2\text{O}_5$  structures can be visualized. (f) Metastable polymorph  $R\text{-Nb}_2\text{O}_5$  adopts an idealized  $\text{V}_2\text{O}_5$  structure with edge- and corner-sharing octahedra.



**Fig. 2** Visualizations of  $R\text{-Nb}_2\text{O}_5$  based on the original report (ICSD collection code 25765)<sup>25</sup> viewed along the (a)  $[010]$  and (b)  $[100]$  directions.

Borrowing the WR structure notation,<sup>3</sup> the structure of  $R\text{-Nb}_2\text{O}_5$  can be represented as  $(2 \times \infty)_\infty$ .

Both  $\alpha\text{-V}_2\text{O}_5$  and  $\text{ReO}_3$  can be considered as ‘parent structures’ for  $R\text{-Nb}_2\text{O}_5$ .<sup>27,28</sup> Like  $\text{ReO}_3$ ,  $\text{V}_2\text{O}_5$  also undergoes polyhedral rotations during lithiation that result in extensive atomic structure changes.<sup>29,30</sup>  $\text{V}_2\text{O}_5$  has layers composed of edge- and corner-sharing  $[\text{VO}_5]$  square pyramids (Fig. 1d). Across the layers, there is a long V–O distance ( $\approx 2.8 \text{ \AA}$ ); when a ‘bond’ is drawn between these atoms,  $\text{V}_2\text{O}_5$  can be visualized as a three-dimensionally-connected structure (Fig. 1e). The larger ionic radius of Nb

relative to that of V results in the octahedral, rather than square-pyramidal, coordination of Nb in  $R\text{-Nb}_2\text{O}_5$ , approaching a relatively idealized structure.<sup>2,31</sup> Given the different atomic structure evolutions and stabilizations of  $\text{ReO}_3$  and WR block structures, we analogously find that  $R\text{-Nb}_2\text{O}_5$  has improved structural stability upon lithiation relative to  $\text{V}_2\text{O}_5$ . In addition to being stable against polyhedral rotation during lithiation, we also find that  $R\text{-Nb}_2\text{O}_5$  has minimal atomic structure evolution during cycling, akin to the relatively small changes in WR materials, for example, unit cell volume changes  $\leq 6\%$ .<sup>10,11</sup>

The ‘ideality’ of  $R\text{-Nb}_2\text{O}_5$  relative to that of  $\alpha\text{-V}_2\text{O}_5$  can be illustrated by comparing their distributions of M–O distances. For  $R\text{-Nb}_2\text{O}_5$ , they range from 1.7 Å to 2.3 Å (this work); this is narrower than the range for  $\text{V}_2\text{O}_5$ , which is from 1.58 Å to 2.8 Å,<sup>32</sup> and broader than that for  $\text{ReO}_3$ , in which there is a single Re–O bond length of 1.9 Å.<sup>33</sup>  $\text{Nb}_3\text{O}_7\text{F}$  is another slab structure, denoted as  $(3 \times \infty)_\infty$ , that has also been studied as a Li-ion electrode<sup>15</sup> and has a similar distribution as  $R\text{-Nb}_2\text{O}_5$ , from 1.85 Å to 2.2 Å.<sup>34</sup>

Overall, we find that the cycling behavior and structural stability of  $R\text{-Nb}_2\text{O}_5$  are more similar to WRs than to  $\text{ReO}_3$ ,<sup>4,35</sup>  $\alpha\text{-V}_2\text{O}_5$ ,<sup>29</sup> or  $\text{Nb}_3\text{O}_7\text{F}$ .<sup>15</sup>  $R\text{-Nb}_2\text{O}_5$  has symmetric discharge and charge profiles that do not significantly change between the first and later cycles. In addition, atomic structure changes are minimal, with no evidence of the polyhedral rotation that  $\text{ReO}_3$  or  $\text{V}_2\text{O}_5$  undergo during lithiation. We observed unit cell changes of less than 5% and a reduced off-centering of Nb in cycled products.<sup>9–11</sup>

## 2 Results and discussion

### 2.1 Synthesis and characterization of $R\text{-Nb}_2\text{O}_5$

The  $R$  polymorph of  $\text{Nb}_2\text{O}_5$  was prepared through soft chemical methods, specifically, through the drying and decomposition of



hydrated precursor  $\text{H}_3\text{ONb}_3\text{O}_8$ .<sup>36</sup>  $\text{H}_3\text{ONb}_3\text{O}_8$  was produced from  $\text{KNb}_3\text{O}_8$ , a layered niobate, through ion-exchange in nitric acid.<sup>36–38</sup>  $\text{KNb}_3\text{O}_8$  was prepared using molten salt synthesis in an excess of KCl, which facilitates the mass transport among precursors to form a phase pure product.<sup>18,39</sup>

Bragg peak positions of the prepared  $R\text{-Nb}_2\text{O}_5$  are consistent with the structure originally reported by Gruehn,<sup>25</sup> which is evident in neutron diffraction data (POWGEN at Oak Ridge National Laboratory, Fig. 3) as well as high-resolution synchrotron X-ray diffraction (XRD) data (11-BM at Argonne National Laboratory, Fig. S1†). In both types of diffraction data, peak broadening is evident. Scanning electron microscope (SEM) images show anisotropic particles with sub-micron features in two dimensions and one longer axis in the order of microns (Fig. 4c and d). This indicates that finite size effects give rise to the reflection-dependent broadening in diffraction data.

Gruehn's reported  $R\text{-Nb}_2\text{O}_5$  structure was used as a starting model for refinements of the atomic structure model against neutron and X-ray diffraction data [International Crystal Structure Database (ICSD) collection code 25765].<sup>25</sup> Rietveld refinement against neutron diffraction data resulted in minor changes to lattice parameters and atom positions, resulting in a fit that captures the data well (Fig. 3). Similar parameters were found from the refinement of synchrotron XRD data (Fig. S1†). Details of refinement parameters and the resulting structures are provided in Tables S1 and S2.†

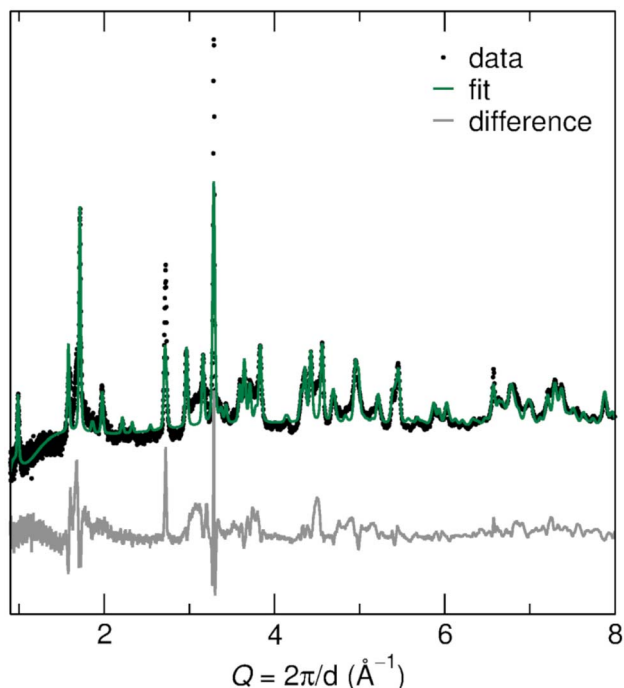


Fig. 3 Rietveld refinement against neutron diffraction data for the prepared  $R\text{-Nb}_2\text{O}_5$  shows good agreement between the measured and calculated patterns. The largest differences occur in regions with diffuse scattering, as well as for two reflections that are underestimated in the calculated data. Details of the refined structure parameters are provided in the ESI.†

The differences between the measured data and calculated fit have two primary origins: diffuse scattering near  $Q$  of  $1.5 \text{ \AA}^{-1}$  and  $3 \text{ \AA}^{-1}$ , and peak intensity mismatch near  $Q$  of  $2.9 \text{ \AA}^{-1}$  and  $3.25 \text{ \AA}^{-1}$  (Fig. 3). The diffuse scattering features suggest low crystallinity, disorder, or a combination. Even after accounting for anisotropic particle shape in refinements, there is a remaining intensity mismatch for the (113), (11 $\bar{3}$ ), and (020) reflections, which are especially narrow and accordingly must be associated with the long axis of the particles. Similar reflection-dependent broadening has also been identified for  $\text{KNb}_3\text{O}_8$ ,<sup>18</sup> the precursor from which this  $R\text{-Nb}_2\text{O}_5$  was prepared (Fig. 4a).

The elongated rectangular morphology of  $R\text{-Nb}_2\text{O}_5$  comes from the morphology of the  $\text{KNb}_3\text{O}_8$  and  $\text{H}_3\text{ONb}_3\text{O}_8$  precursors (Fig. 4a and b). The layered nature of the  $\text{KNb}_3\text{O}_8$  atomic structure drives preferential growth along specific crystallographic directions.<sup>18</sup> The underlying particle shape is retained through ion-exchange and low temperature heating of the prepared product. This synthetic route did not allow for the preparation of larger or more isotropic  $R\text{-Nb}_2\text{O}_5$  particles, which was beyond the scope of this work, but variations of particle size and shape may be accessible from more isotropic  $\text{KNb}_3\text{O}_8$  precursors or through alternative synthetic methods.

A notable feature of the crystal structure of  $R\text{-Nb}_2\text{O}_5$  is the off-centering of Nb within the octahedra, as well as the pattern of displacements from the center between neighboring octahedra. In  $\text{V}_2\text{O}_5$ , the nearest neighbor V–O distances range from  $1.58 \text{ \AA}$  to  $2.8 \text{ \AA}$ , and off-centering of  $\text{V}^{5+}$  away from the center of an octahedron occurs as pairs (two displaced lower, two displaced higher, Fig. 1d).<sup>32</sup> In  $R\text{-Nb}_2\text{O}_5$ , Nb is also off-centered in the octahedra, but with a narrower distribution of Nb–O distances, ranging from  $1.7 \text{ \AA}$  to  $2.3 \text{ \AA}$ . In addition, off-centering occurs in a zig-zag pattern, alternating up and down for each octahedron, along the  $c$  direction (Fig. 2a).

## 2.2 Battery cycling behavior

$R\text{-Nb}_2\text{O}_5$  was cycled against Li metal in coin cells at various rates. At a relatively slow cycling rate of C/20 (based on the reaction of 2 mol Li per mol  $\text{Nb}_2\text{O}_5$  in 20 h), galvanostatic cycling shows a plateau at  $\approx 1.8 \text{ V}$  for  $0 \leq x \leq 1$ , and a sloping region at low potentials (Fig. 5a), suggestive of two-phase and solid solution lithiation mechanisms at high and low potentials, respectively. The plateau for  $R\text{-Nb}_2\text{O}_5$  is slightly higher than that for  $H\text{-Nb}_2\text{O}_5$ , which is at  $\approx 1.6 \text{ V}$ .<sup>20</sup> Over the first  $\approx 55$  cycles, unoptimized coin cells show gradual capacity fade (Fig. 5a).

Between the first and second discharge of  $R\text{-Nb}_2\text{O}_5$ , there are minor differences in the cycling profiles. Specifically, there is additional capacity before the plateau in the first discharge compared to later discharges. This difference is likely related to the irreversible capacity over the first cycle, with  $\approx 0.3 \text{ mol Li}$  per mol  $\text{Nb}_2\text{O}_5$  remaining at the end of the first charge. This type of slight irreversibility is common in WR and related materials,<sup>18</sup> and has been previously attributed to sluggish diffusion of  $\text{Li}^+$  from specific sites within WR-type structures, as well as an electronic transition from an initially electronic



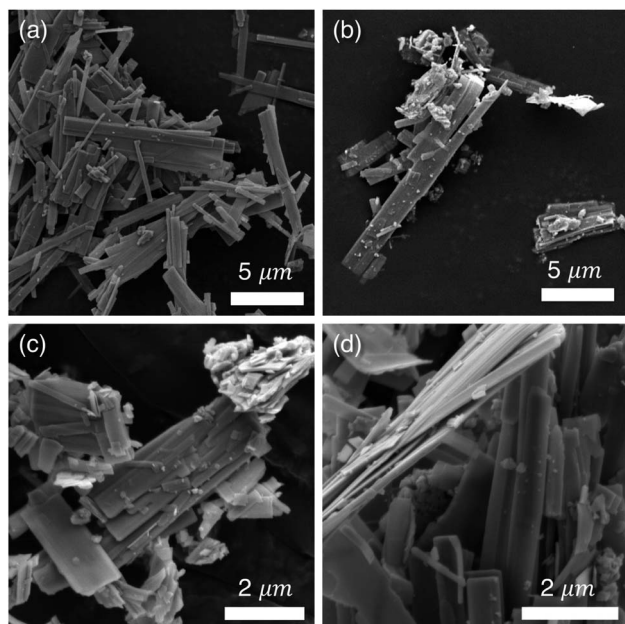


Fig. 4 SEM images of (a) precursor  $\text{KNb}_3\text{O}_8$ , (b) intermediate product of ion-exchange,  $\text{H}_3\text{ONb}_3\text{O}_8$ , and (c, d)  $R\text{-Nb}_2\text{O}_5$ . The elongated, rectangular particles of  $R\text{-Nb}_2\text{O}_5$  result from its precursors. The anisotropic particle size has crystallographic origins and results in the reflection-character-dependent broadening in the diffraction data (Fig. 3).

insulator to having delocalized electron states upon slight Nb reduction.<sup>10,11,17</sup> Additionally, the differential capacity plot highlights minor differences in the shape of the first discharge curve relative to that of later cycles (Fig. 5). Even so, discharge and charge curves are generally symmetric, indicating similar reaction pathways on discharge and charge. This is evident in the positions of plateaus and sloped regions in galvanostatic cycling (Fig. 5a), and the corresponding peaks and diffuse features in the differential capacity plot (Fig. 5b). The symmetric cycling processes on discharge and charge are in contrast to those of the 'parent' compounds of  $R\text{-Nb}_2\text{O}_5$ ,  $\text{ReO}_3$  and  $\text{V}_2\text{O}_5$ , in which extensive and irreversible atomic structure changes during the first lithiation result in significant differences in the profile shape of the first discharge and following cycles.<sup>29,30,35</sup>

At faster cycling rates, electrochemical curves show good reversibility and similar electrochemical features to those after cycling at slower rates, as well as lower capacities and higher overpotentials. Changes in cycling features with increasing rate are evident in Fig. 6a, which shows the second cycle at each rate from variable rate galvanostatic cycling. The increased overpotential and more sloped nature of the cycling curves with increasing rate are highlighted in the differential capacity plot (Fig. 6b).  $R\text{-Nb}_2\text{O}_5$  has excellent reversibility and good capacity retention, visible in cycling at  $C/10$  and  $1C$  in the ESI† (Fig. S3 and S4).

The decrease in capacity with increasing rate is more significant for  $R\text{-Nb}_2\text{O}_5$  than for typical block Wadsley–Roth materials. The reversible capacity of  $\approx 150 \text{ mA h g}^{-1}$  at  $C/20$  reduces to about  $50 \text{ mA h g}^{-1}$  at  $5C$  (Fig. 6c), whereas typical WR block materials, e.g.,  $\text{TiNb}_2\text{O}_7$  and  $\text{PNb}_9\text{O}_{25}$ , maintain more capacity with proportional increases in cycling rates.<sup>11,40</sup> While

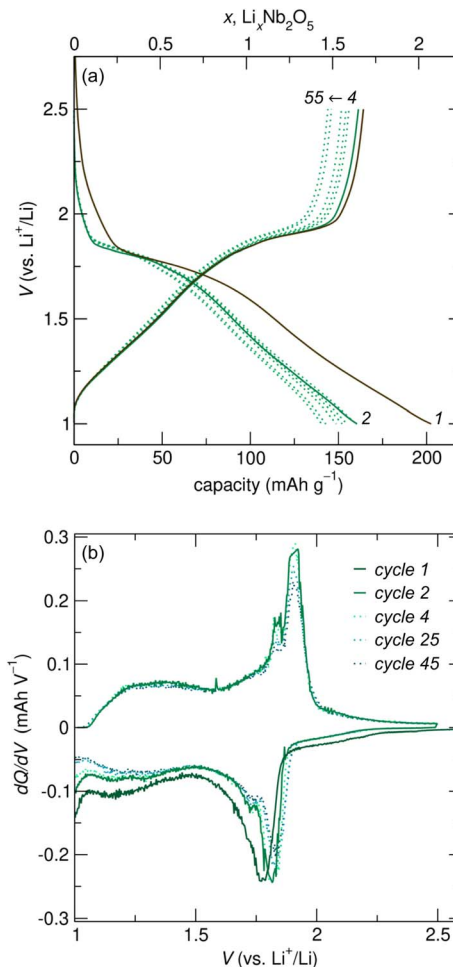


Fig. 5 (a) Galvanostatic cycling for coin cells cycled against Li metal at a rate of  $C/20$ . (a) A combination of plateaus and slopes in cycling profiles indicates two-phase and solid solution lithiation mechanisms, (b) exhibited as peaks and diffuse features in the differential capacity plot. Both plots indicate the symmetry of discharge and charge features, and their stability with cycling. In (a), the first and second cycles are represented with solid lines, and every tenth cycle following is represented by dashed lines, as numbered.

the capacities and rate capabilities of  $R\text{-Nb}_2\text{O}_5$  do not meet those of typical WR block materials, they do exceed the reversibility and capacity retention of other related materials, such as  $\text{ReO}_3$ ,<sup>4,35</sup> and even 'slab' material  $\text{Nb}_3\text{O}_7\text{F}$ .<sup>15</sup>

Considering that  $R\text{-Nb}_2\text{O}_5$  has an 'idealized'  $\text{V}_2\text{O}_5$  structure, there is a significant difference between their electrochemical behaviors during lithiation. The asymmetry observed in the charge and discharge profiles for  $\alpha\text{-V}_2\text{O}_5$  during lithiation, due to phase transformations into  $\epsilon$ -,  $\delta$ -, and  $\gamma$ - polymorphs, is significantly different than that in the highly symmetric profiles we find for  $R\text{-Nb}_2\text{O}_5$ .<sup>29,41</sup> The origins of these differences are discussed further in the following section.

### 2.3 Structural evolution with cycling

To understand the structural stability and cycling mechanism of  $R\text{-Nb}_2\text{O}_5$ , we analyzed *ex situ* synchrotron XRD data after the





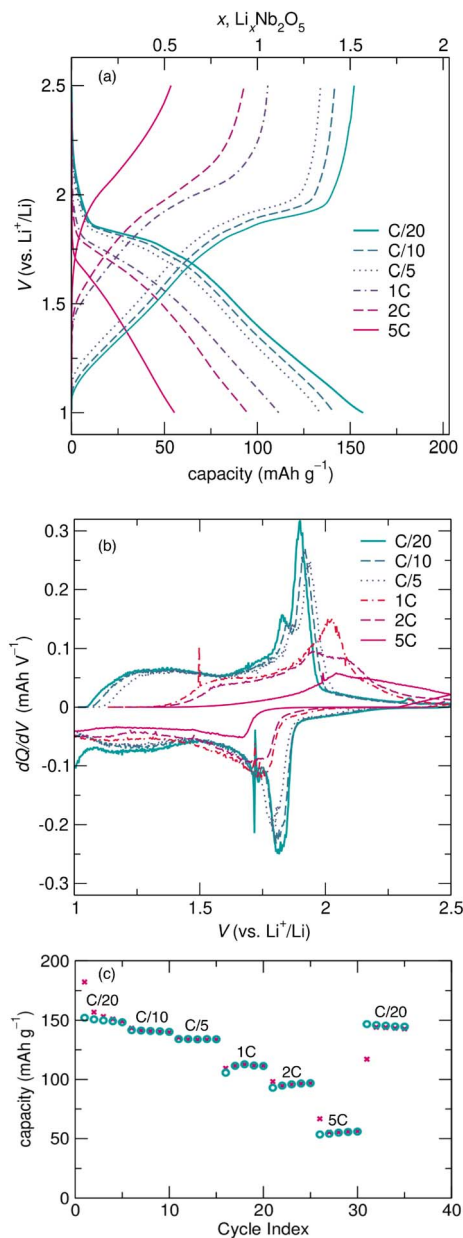


Fig. 6 (a) Galvanostatic cycling profiles and (b) differential capacity plots for coin cells cycled against Li metal at variable rates from C/20 to 5C. In (a), profiles are shown for the second cycle at each rate. (c) Capacity per cycle is shown for each rate, including the capacity recovered at C/20.

first discharge and the first charge (Fig. 7). For this, loose powder cathodes were cycled in Swagelok cells at C/20 and extracted after the first discharge (to 0.5 V,  $\text{Li}_3\text{Nb}_2\text{O}_5$ ) and first charge (to 2.5 V,  $\text{LiNb}_2\text{O}_5$ ). Cycling for loose powder Swagelok cells is qualitatively similar to that from coin cells (Fig. S2<sup>†</sup>). The deeper discharge relative to that of coin cells resulted in a higher first discharge capacity, but a similar reversible capacity, which suggests that the low potential capacity is associated with the formation of a solid-electrolyte interphase, storage by a conductive carbon additive, or a combination thereof.<sup>42,43</sup>

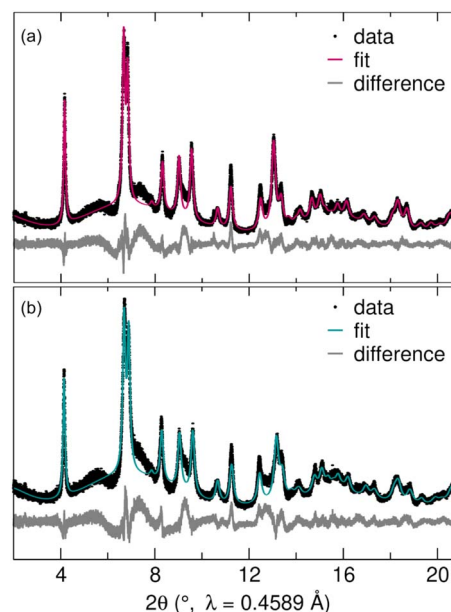


Fig. 7 Rietveld refinements of high-resolution synchrotron XRD data following (a) the first discharge and (b) the first charge of  $R\text{-Nb}_2\text{O}_5$  indicating agreement between the measured and calculated patterns. Due to the poor sensitivity of X-rays to light elements, Li was excluded from the structural model and only the Nb–O framework was refined (Table 1).

Synchrotron XRD data of cycling products were used in Rietveld refinements of atomic structure models to determine the nature of these minor structural changes. For both states of charge, the  $R\text{-Nb}_2\text{O}_5$  structure refined against neutron diffraction data of the prepared powder was used as the starting model. Due to the poor sensitivity of X-rays to light elements, Li was not included in the structural model, with an emphasis instead on the Nb–O framework. As in the pristine  $R\text{-Nb}_2\text{O}_5$ , reflection-dependant broadening was captured using isotropic crystallite size parameters, with a mix of Lorentzian and Gaussian shapes, and the preferred orientation (modeled with spherical harmonics) to account for the broadening caused by the anisotropic crystallite size. Additional information on Rietveld refinements and refined structures are provided in the ESI<sup>†</sup> (Tables S1, S2, S3, and S4).

There were no new reflections in the first discharge and charge products compared to pristine  $R\text{-Nb}_2\text{O}_5$  (Fig. 3 and 7). Rather, changes in lattice parameters resulted in shifted peak positions, with the Nb–O framework retained through  $\text{Li}^+$  intercalation and deintercalation. As in the pristine  $R\text{-Nb}_2\text{O}_5$ , XRD data of cycled products have diffuse scattering and broad peaks. The qualitative similarity of diffraction data for the pristine and cycled products is reflected in the quantitative results of Rietveld refinements (Table 1 and Fig. 8). Lattice parameters undergo minor contraction ( $a$  and  $c$ ) and expansion ( $b$ ), resulting in 4.66% and 3.56% increases in the unit cell volume ( $V_{\text{uc}}$ ) of the discharge and charge products, respectively, relative to those of pristine  $R\text{-Nb}_2\text{O}_5$ .



**Table 1** Refined unit cell parameters for pristine, discharged, and charged  $R\text{-Nb}_2\text{O}_5$  reflect the minimal changes that result from lithiation and delithiation. In addition, changes in the size and degree of distortion of octahedra over the three states show a decrease in distortion as Nb is reduced

| Composition                              | Pristine $\text{Nb}_2\text{O}_5$ | Discharged $\text{Li}_3\text{Nb}_2\text{O}_5$ | Charged $\text{LiNb}_2\text{O}_5$ |
|--|----------------------------------|---|-----------------------------------|
| $a$                                      | 3.9752(6) Å                      | 3.94788(19) Å                                 | 3.9313(3) Å                       |
| $b$                                      | 3.8233(3) Å                      | 4.04267(15) Å                                 | 4.0058(2) Å                       |
| $c$                                      | 12.7064(19) Å                    | 12.6633(7) Å                                  | 12.6987(10) Å                     |
| $\beta$                                  | 90.603(13)°                      | 90.0034(10)°                                  | 89.966(11)°                       |
| $V_{\text{uc}}$                          | 193.11(4) Å <sup>3</sup>         | 202.107(17) Å <sup>3</sup>                    | 199.98(2) Å <sup>3</sup>          |
| % Change $V_{\text{uc}}$ <sup>a</sup>    | —                                | 4.66%   | 3.56%                             |
| Octahedral volume                        | 10.437 Å <sup>3</sup>            | 10.81 Å <sup>3</sup>                          | 10.6955 Å <sup>3</sup>            |
| Octahedral distortion index <sup>b</sup> | 0.073                            | 0.024   | 0.029                             |

<sup>a</sup> Percent change relative to that of the pristine one. <sup>b</sup> Baur's distortion index (based on bond length variation)<sup>44</sup> calculated with VESTA.<sup>45</sup>

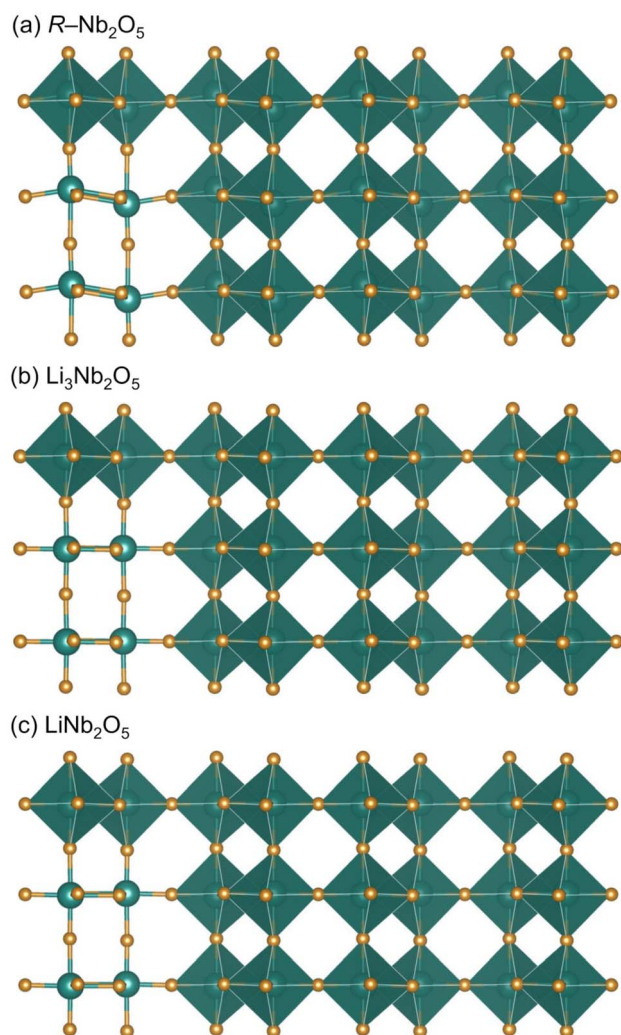
While lattice parameters are similar for pristine and cycled  $R\text{-Nb}_2\text{O}_5$ , there are notable differences in the  $[\text{NbO}_6]$  octahedra for the pristine and cycled products (Fig. 8). As mentioned, Nb in  $R\text{-Nb}_2\text{O}_5$  is less off-centered than V in  $\text{V}_2\text{O}_5$  (Fig. 1d and f), but still

has a range of Nb–O bond lengths. Baur's distortion index is a single-value quantity that can be used to describe deviations from a perfect octahedron, with 6 M–O bonds of the same length, which would have a Baur's index of 0.<sup>44</sup> Specifically, Baur's index represents octahedral (or tetrahedral) distortions as the deviation of bond lengths from an average bond length.<sup>44</sup> In the cycled products, the reduction in Baur's index reflects the decrease in Nb off-centering with the reduction of  $\text{Nb}^{5+}$  during lithiation (Fig. 8). In pristine  $\text{Nb}_2\text{O}_5$ ,  $\text{Nb}^{5+}$  has an electronic configuration  $[\text{Kr}]5s^24d^0$ ; at the *ex situ* states of charge evaluated, there is at least some reduction of Nb away from this  $d^0$  electron configuration. The reduced oxidation state of Nb relieves the second-order Jahn-Teller distortion,<sup>10,11,17</sup> which is commonly active for fully oxidized early transition metals, such as Nb.<sup>46</sup> The reduction of Nb, and thus Nb off-centering, following discharge and charge results in nearly identical crystal structures at these states of charge (Fig. 8, Tables 1, and S1, S2, S3, and S4).

In contrast to  $\text{ReO}_3$  and  $\text{V}_2\text{O}_5$ ,  $R\text{-Nb}_2\text{O}_5$  has minimal structure evolution during the first discharge (Fig. 8).<sup>29,35</sup> The difference in cycling behavior and structural stability between  $R\text{-Nb}_2\text{O}_5$  and  $\text{Nb}_3\text{O}_7\text{F}$  is especially interesting as both have slab structures with  $\text{ReO}_3$ -like regions connected by parallel, non-intersecting crystallographic shear-planes.<sup>27</sup> The difference in their behavior is most likely a consequence of the difference in the width of their slabs. The extended-defect-based structures can be described as  $(2 \times \infty)_\infty$  for  $R\text{-Nb}_2\text{O}_5$ , and  $(3 \times \infty)_\infty$  for  $\text{Nb}_3\text{O}_7\text{F}$ .<sup>3</sup>

### 3 Conclusions

Based on our findings,  $R\text{-Nb}_2\text{O}_5$  can serve as a 'structural bridge' between Wadsley–Roth block structures and  $\text{V}_2\text{O}_5$  in terms of polyhedral distortions, polyhedral connectivity, and the consequences thereof for structural stability during cycling. Relative to  $\text{V}_2\text{O}_5$ , we show that bridging layers to form a three-dimensionally connected structure, as in its 'idealized' structure, stabilizes it against polyhedral rotations associated with irreversible structural changes. For WR structures, this work demonstrates for the first time that a  $(2 \times \infty)_\infty$  slab structure, with only parallel (rather than intersecting) shear planes, is stable against polyhedral rotations at corner-sharing vertices during electrochemical cycling. This is in contrast to what has



**Fig. 8** Refined structures of (a)  $R\text{-Nb}_2\text{O}_5$ , and (b) lithiated product of the first discharge to 0.5 V, and (c) the following first charge to 2.5 V.



been found for  $\text{Nb}_3\text{O}_7\text{F}$ , in which non-intersecting crystallographic shear planes that link three-octahedron-wide slabs, denoted as  $(3 \times \infty)_\infty$ , do not provide structural stability during lithiation. Thus, the combination of three-dimensionally connected polyhedra and non-intersecting shear planes with a smaller slab width results in the stability of  $R\text{-Nb}_2\text{O}_5$  against unfavorable distortions, making it a high voltage anode candidate, and moreso, a link between heavily studied material families.

In the context of published work on related structures, we illustrate how lithiation in isotypic materials induces varying degrees of structural changes and phase transformations, which have direct impacts on  $\text{Li}^+$  diffusion pathways. The highly symmetric charge discharge profile for  $R\text{-Nb}_2\text{O}_5$  indicates that similar sequences of phase transformations occur during lithiation and delithiation. Furthermore, the minimal structural changes result in the retention of square channels that resemble the fast  $\text{Li}^+$  transport pathways in WR block structures. Future work to further characterize  $\text{Li}^+$  and electronic conduction, as well as long-term cycling stability, will provide additional insights into bridge classes of early transition metal oxide electrode materials, including Wadsley–Roth block structures and  $\text{V}_2\text{O}_5$ .

## 4 Experimental

### 4.1 Synthesis

Phase pure  $R\text{-Nb}_2\text{O}_5$  was prepared from precursors synthesized using the molten salt reaction by ion-exchange methods adapted from reported methods.<sup>18,36,47</sup> Precursor  $\text{KNb}_3\text{O}_8$  was prepared by ball-milling  $\text{K}_2\text{CO}_3$  (Sigma Aldrich,  $\geq 99\%$ ),  $\text{Nb}_2\text{O}_5$  (Sigma Aldrich, 99.99%), and  $\text{KCl}$  (Sigma Aldrich,  $\geq 99\%$ ) in molar ratios of 1:3:12 in ethanol (Thermo Fisher, reagent grade) for 30 min. Ethanol was evaporated under ambient conditions and the resulting mixture was heated in a covered alumina crucible at 800 °C for 5 h in air, with a heating rate of 3°  $\text{min}^{-1}$  and allowed to cool passively with a furnace. The reacted powder was washed with warm deionized (DI) water to remove  $\text{KCl}$ ; the mixture was centrifuged and decanted to isolate  $\text{KNb}_3\text{O}_8$  powder, which was dried in air.

The prepared  $\text{KNb}_3\text{O}_8$ ,  $\approx 1$  g, was stirred in 100 mL of 7 M  $\text{HNO}_3$  for 3 days to prepare  $\text{H}_3\text{ONb}_3\text{O}_8$  *via* ion-exchange.<sup>36</sup> As before, the solid product was isolated and washed using DI water, centrifugation, and decanting. After drying at room temperature,  $\text{H}_3\text{ONb}_3\text{O}_8$  powder was heated in air at 600 °C for 2 h, yielding  $R\text{-Nb}_2\text{O}_5$ .<sup>36</sup> Engineering controls (*i.e.*, ventilation hood) and personal protective equipment should always be used when handling hazardous materials, such as strong acids.

### 4.2 X-ray and neutron diffraction

The phase purity of the intermediates and final products was initially evaluated using Rigaku Miniflex and Panalytical X'Pert Powder diffractometers. High-resolution synchrotron XRD was carried out through mail-in from beamline 11-BM at the Advanced Photon Source at Argonne National Laboratory. Synchrotron X-rays had a calibrated wavelength of 0.4589 Å and

powders were measured in transmission mode in 0.8 mm diameter Kapton capillaries sealed with epoxy at both ends.

For *ex situ* synchrotron XRD of cycled  $R\text{-Nb}_2\text{O}_5$ , powder cathodes (8:2 mass ratio of  $\text{Nb}_2\text{O}_5$  and SuperP) were extracted from Swagelok half-cells cycled to a specified state of charge. The powders were washed with dimethyl carbonate (DMC), dried under vacuum, and ground with an agate mortar and pestle in an Ar-filled glove box. The samples were sealed under Ar in secondary containment for shipping and removed just prior to measurements to minimize exposure to moisture.

Neutron diffraction data of the as-prepared  $R\text{-Nb}_2\text{O}_5$  were collected using a POWGEN diffractometer at the Spallation Neutron Source (SNS) at Oak Ridge National Laboratory (ORNL) through the mail-in program. The powders were loaded into a 6 mm diameter vanadium can. Data were collected in time-of-flight for 2 h with a center wavelength of 1.5 Å.

Structural data were refined using GSAS-II<sup>48</sup> and Topas Academic v7.<sup>49</sup> VESTA was used to visualize the crystal structures and for quantitative descriptions of  $[\text{NbO}_6]$  octahedra.<sup>45</sup>

### 4.3 Electron microscopy

Scanning electron microscopy (SEM) was carried out using a TESCAN MIRA3 microscope with a beam voltage of 8 keV and a working distance of 15 mm. The samples were prepared on carbon tape and sputtered with a thin layer of gold to prevent charging.

### 4.4 Battery assembly and electrochemical studies

$R\text{-Nb}_2\text{O}_5$  was cycled in half-cell batteries with a Li metal anode (MTI, 99.9%). For preliminary cycling and *ex situ* synchrotron XRD, loose powder cathodes ( $\text{Nb}_2\text{O}_5$  and SuperP in 8:2 mass ratio, mixed in an agate mortar and pestle) were assembled in Swagelok cells. For coin cells, cast cathode films were prepared by mixing  $R\text{-Nb}_2\text{O}_5$  with Ketjen Black (MSE Supplies) and polyvinylidene fluoride (PVDF) in a 7.5:1.5:1 mass ratio, respectively; *N*-methyl-2-pyrrolidone was used as a solvent for PVDF during casting on copper foil (MSE Supplies) using a 15  $\mu\text{m}$  doctor blade.

For both cell configurations, the electrolyte was 1 M  $\text{LiPF}_6$  in a mixture (1:1 by volume) of ethylene carbonate and DMC. For Swagelok cells, the cathode and anode were separated by two Whatman glass filter dryer (GFD) disks; for coin cells, the separator was polypropylene (Celgard 2500, 25  $\mu\text{m}$ ). The cells were assembled in an Ar-filled glovebox. Swagelok cells were cycled galvanostatically at various rates in terms of C, such that C is based on the reaction of 2 mol of Li. Coin cells were cycled galvanostatically at rates of C/20, C/10 and 1C with an upper potential limit of 2.5 V and a lower potential limit of 1 V. Additionally, cells were cycled with varying cycling rates of C/20, C/10, C/5, 1C, 2C, and 5C for 5 consecutive cycles, and a final set at C/20.

## Author contributions

KP: conceptualization; data curation; formal analysis; investigation; visualization; writing – original draft, reviewing and





editing. ADL: investigation; especially synthesis and initial characterization (laboratory XRD). SG: investigation; especially characterization (SEM imaging). MMB: conceptualization; formal analysis; project administration; resources; supervision; visualization; writing – original draft, reviewing and editing.

## Conflicts of interest

There are no conflicts to declare.

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