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# Fluid interfaces laden by force dipoles: towards active matter-driven microfluidic flows

Kuntal Patel \*\* and Holger Stark \*\*

In recent years, nonlinear microfluidics in combination with lab-on-a-chip devices has opened a new avenue for chemical and biomedical applications such as droplet formation and cell sorting. In this article, we integrate ideas from active matter into a microfluidic setting, where two fluid layers with identical densities but different viscosities flow through a microfluidic channel. Most importantly, the fluid interface is laden with active particles that act with dipolar forces on the adjacent fluids and thereby generate flows. We perform lattice-Boltzmann simulations and combine them with phase field dynamics of the interface and an advection-diffusion equation for the density of active particles. We show that only contractile force dipoles can destabilize the flat fluid interface. It develops a viscous finger from which droplets break up. For interfaces with non-zero surface tension, a critical value of activity equal to the surface tension is necessary to trigger the instability. Since activity depends on the density of force dipoles, the interface can develop steady deformation. Lastly, we demonstrate how to control droplet formation using switchable activity.

## I. Introduction

Rapid advancement in processing fluids on the micron scale has given rise to various applications in chemical analyses,<sup>1</sup> biology, 2,3 medical diagnosis, 4,5 and many more. Such miniaturized flow-control platforms are referred to as microfluidic lab-on-a-chip devices. 6-8 Typically, microfluidic flows occur at low Reynolds numbers and, therefore, obey kinematic reversibility, which sets restrictions on the realizable flows and their applications.9 To extend the use of microfluidic devices, one needs to introduce nonlinearities, for example, through inertial microfluidics or viscoelastic fluids. 9,10 This field of nonlinear microfluidics has opened new avenues for droplet generation<sup>11-13</sup> and cell sorting applications. <sup>14-18</sup> In addition, nonlinear processes in microfluidic devices are also initiated by an external electric field, which induces electroosmotic flows, 19-21 and acoustic fields, which generate surface acoustic waves traveling along substrates. 22,23 Furthermore, microfluidic devices with compliant structures are known to cause a nonlinear response of the flow rate to the pumping pressure.<sup>9,24</sup> Aside from nonlinear microfluidics, the development of other microfluidic techniques has immensely contributed to the overall progress of the field. Two such examples are lightdriven<sup>25</sup> and digital microfluidics<sup>26</sup> for manipulating droplets. In this article we introduce yet another mechanism to design

Institut für Theoretische Physik, Technische Universität Berlin, Hardenbergstr. 36, 10623 Berlin, Germany. E-mail: kuntal.h.patel@tu-berlin.de

and control microfluidic flow by introducing active particles at fluid interfaces.

We investigate a microfluidic system in combination with ideas from the field of active matter. This is a relatively new and less explored strategy to control and shape fluid flow at low Reynolds numbers. The entities of living or artificial active systems consume the ambient free energy to propel themselves and exert forces. 27-30 In practice, the scale of active matter systems ranges from nanometers to meters.31,32 A bacterial suspension is one example that belongs to a micron-sized active matter system. It is well known now that the collective motion of bacteria can generate chaotic flow structures called active turbulence. 33-35 Researchers have also demonstrated that such a bacterial bath can drive the continuous rotation of microscopic gears, which can be utilized as microfluidic mixers or energy harvesters. Another interesting system is a suspension of flexible active filaments made, e.g., by mixing microtubule with motor proteins40 and termed active nematic fluid. 29,41 Without activity it assumes an isotropic ground state. However, tuning the activity beyond a critical value, a hydrodynamic instability occurs and the fluid begins to flow. 42 Later, using numerical simulations, Chandragiri et al. 43 demonstrated that the turbulent flow becomes unidirectional in sufficiently narrow microchannels resulting in the net transport of fluid along the channel. Hence, active fluids are an alternative for driving fluid flow without using microfluidic pumps. Recently, Rorai et al.44 studied the channel flow of active nematics with hybrid alignment at the channel walls. Within microfluidic applications, we also mention theoretical work on active matter

logic<sup>45</sup> and experimental work on active matter in circular channels46 and driven by light.47

In this article, we take up the idea of combining microfludic flow with active entities. We focus on a multi-component microfluidic setup, in contrast to the systems with a single fluid component described in the last paragraph. Earlier, Alonso and Mikhailov<sup>48</sup> employed interfacial active molecules to generate turbulence at the liquid-air interface of a thin liquid film. They noted that the destabilization of the interface occurs only for a sufficiently high value of particle concentration and activity. Following this, Pototsky et al. 49 looked at the dynamics of a micron-sized thin liquid film with selfpropelling point-like swimmers, which act as insoluble surfactants. As a result of the upward motion of swimmers against the film interface, they observed interesting interfacial patterns in their numerical simulations. Most recent experiments by Adkins et al.50 revealed a highly dynamic fluid interface between an active and passive fluid, which is caused by the chaotic flow within the active fluid. They also reported that a gradual increase in activity eventually disrupts the fluid interface, which results in the formation of active emulsions. Further examples of active surfaces are described in ref. 51 and 52. Although there have been some efforts to leverage active matter into microfluidics, developing such a strategy for multi-component microfluidic systems remains scarce. In the present study, we introduce theoretical ideas as early steps for designing multi-component microfluidic flow devices fueled by active matter. The practical realization of these concepts holds great potential to impact a broad spectrum of applications, e.g., cell encapsulation,<sup>53</sup> drug delivery,<sup>54</sup> and particle synthesis.<sup>55</sup>

In the present work, we consider a microfluidic channel that contains two fluid layers separated by a fluid interface with surface tension  $\sigma$ . The fluids have identical densities but different viscosities. Most importantly, we cover the fluid interface with active particles that act with force dipoles on the surrounding fluid, one of the typical characteristics of active matter systems. The setup with two fluid layers is of fundamental relevance and ubiquitous in various microfluidic devices.<sup>56</sup> We study the flow induced by the interfacial force dipoles and its effect on the fluid interface using hybrid lattice-Boltzmann finite-difference simulations, where the fluid interface is described by a phase field model. Our numerical results show that contractile force dipoles destabilize the flat fluid interface so that multiple breakups occur, where droplets form. In contrast, when laden with extensile dipoles, the interface stays flat. For interfaces with non-zero surface tension, we derive the critical value of activity necessary to trigger the instability. Since activity depends on the density of force dipoles, the interface can develop a steady deformation. Finally, we show how to control droplet formation with a switchable activity.

The outline of the article is as follows. In Section II we first introduce our microfluidic configuration with an active fluid interface, followed by the explanation of the governing laws and numerical methodology. The simulation results of our systematic investigations are presented in Section III. We conclude our work with final remarks in Section IV.

## II. Methods

#### Setup of active microfluidics

The schematic of our computational setup is depicted in Fig. 1. We consider a two-dimensional microfluidic channel by placing two parallel walls at a distance w from each other in the y-direction while along the x-direction periodic boundary conditions are used [see Fig. 1(a)]. The channel is filled with two fluid layers of thickness h (bottom layer) and w-h (top layer), respectively. Both fluid layers have identical densities  $\rho$ while the bottom fluid (fluid 1) is more viscous than the top fluid (fluid 2), which we quantify by the viscosity contrast  $m = \mu_1/\mu_2 > 1$ . Finally, the fluid interface separating fluids 1 and 2 has surface tension  $\sigma$ . In the following, it is disturbed by imposing an interfacial perturbation of wavelength  $\lambda$ .

The important feature of the present problem is that the fluid interface contains active particles, as shown in Fig. 1(b). The activity of these particles gives rise to force dipoles as depicted in Fig. 1(b) that generate flows in the fluids adjacent to the interface. We assume that the active particles are much smaller than the channel width w, so that they can be considered as point particles. The dipole-laden interface in a continuum approximation is shown in Fig. 1(c), where the two opposing forces of the dipole are represented by red and blue colors. We impose the following constraints on the active particles to simplify the present problem:

- They are tied to the fluid interface, while they are free to slide along it, and
- They are always oriented perpendicular to the fluid interface. The notion of active particles residing at the fluid interface is inspired by insoluble surfactants found in practice, which get adsorbed at the interface.<sup>57</sup> Motivated by this, Alonso and

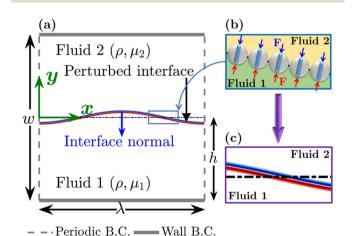


Fig. 1 (a) A microfluidic channel of width w contains two fluids of the same density  $\rho$  but different viscosities  $\mu_1$  and  $\mu_2$  ( $\mu_1 > \mu_2$ ). The interface separating the top and bottom fluids is initially perturbed by a sinusoidal modulation with wavelength  $\lambda$ . (b) The sketch shows the zoomed-in view of the fluid interface covered with active particles, which are oriented in the direction normal to the interface. The red and blue arrows indicate the force dipole induced by active particles. (c) The equivalent of (b) in the continuum limit. The red and blue stripes represent the magnitude of the force dipole density

Mikhailov<sup>48</sup> and Pototsky et al.<sup>49</sup> also implemented interfacial active agents. In addition, two-fluid setups with Janus particles trapped at the interface have also been widely studied. 58-60 The surface of Janus particles can be treated to have different wettabilities so that the top and bottom halves of particles prefer opposite fluids adjoining the interface, orienting particles perpendicular to the interface. 61 The wettability contrast suppresses perturbations in the orientation and reorients particles perpendicular to the interface, as shown by Gao et al. 62 This justifies our simplification of the particle orientation.

The force dipoles at the interface generate stresses, which we describe by the active stress tensor<sup>63</sup>

$$T_{ij}^{a} = WC(\mathbf{x}, t) n_{i} n_{j} \delta_{s}, \tag{1}$$

where  $C(\mathbf{x},t)$  is the areal concentration of active particles and W is the force dipole moment so that  $WC(\mathbf{x},t)$  quantifies the strength of activity with unit of force × distance per unit area. Moreover, the force dipoles are oriented along the interface normal **n** and  $\delta_s$ approximates the delta function, which is situated at the fluid interface such that  $T_{ii}^a$  varies smoothly across the interface.

Thus, the fluid interface is not a sharp boundary but we describe it with the help of a phase field  $\phi$  that is represented by a smooth step function varying between  $\phi = 0$  (fluid 2) and  $\phi$  = 1 (fluid 1). The dynamics of  $\phi$  follows a phase field equation as we detail in Section II B [see eqn (7)]. The interface normal is then given by  $\mathbf{n} = \nabla \phi / |\nabla \phi|$  and  $\delta_s = \mathbf{n} \cdot \nabla \phi = |\nabla \phi|$ . Note that  $\delta_s$  is normalized to one, as it should, since  $\phi$  varies between 0 and 1.

By taking the divergence of the active stress tensor, the effect of activity can also be formulated as an active body force

$$\mathbf{F}^a = \nabla \cdot \mathbf{T}^a = f^a \mathbf{n},\tag{2}$$

where the magnitude  $f^a$  is obtained by projecting the divergence of the active stress tensor on the normal direction:  $f^a = T$  $a_{ii,i}n_i$ . A tangential component is negligible since the phase field eqn (7) approximately keeps the equilibrium profile for the deforming interface. Upon setting W > 0 in our model, we obtain contractile force dipoles  $\frac{\downarrow}{\uparrow}$  [see Fig. 1(b)] and extensile

force dipoles  $\int_{-1}^{1}$  for W < 0.63 The flowchart in Fig. 2 describes

how our system evolves in the presence of a non-zero active body force  $\mathbf{F}^a$ . To fully describe such a system, we need laws that govern the concentration of active particles at the interface as well as the motion of the interface and the flow of the bulk fluids. Since the interface implicitly determines the orientation of active particles, we do not need an additional equation to describe the orientation of active particles. We now proceed to discuss the required governing laws and numerical methods to solve them using computer simulations.

#### B. Governing equations

The flow arising in the bottom and top fluids due to the force dipoles (see Fig. 1) is governed by the continuity equation (conservation of mass)

$$\nabla \cdot \mathbf{u} = 0 \tag{3}$$

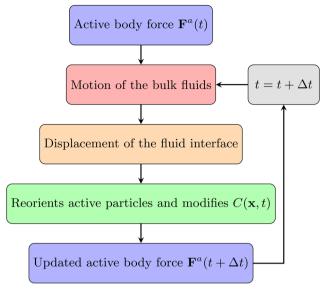


Fig. 2 Time evolution of the fluid interface in the active microfluidic setup (see Fig. 1). The active body force drives fluid flow via eqn (4), which displaces and deforms the interface described by phase field  $\phi$  and its dynamics in eqn (7). This reorients the force dipoles and modifies their density C via eqn (6), so that the body force needs to be updated via eqn (2).

and the Navier-Stokes equation for the flow field u (conservation of momentum).

$$\rho\left(\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u}\right) = -\nabla p + \mu \nabla^2 \mathbf{u} + \mathbf{F}^a + \mathbf{F}^s,\tag{4}$$

where the viscosity is given by  $\mu^{-1} = \phi \mu_1^{-1} + (1 - \phi)\mu_2^{-1}$  so that it varies smoothly between fluid 1 and  $2^{13,64}$  and  $\mathbf{F}^s$  is the body force arising from the surface tension when the interface bends [see eqn (11)].

Since in our model the total number of active particles along the deforming fluid interface S(t) is conserved,

$$N = \int_{S(t)} C(\mathbf{x}, t) ds = \text{const.},$$
 (5)

the concentration  $C(\mathbf{x},t)$  obeys a continuity equation with advective and diffusive currents. So the resulting interfacial advection-diffusion equation reads:65

$$\frac{\partial C}{\partial t} + \nabla_{\mathbf{s}} \cdot (C\mathbf{u}_{\mathbf{s}}) + C\kappa(\mathbf{u} \cdot \mathbf{n}) = D\nabla_{\mathbf{s}}^{2} C, \tag{6}$$

where  $\nabla_s = \left(\underline{\underline{I}} - \mathbf{n} \otimes \mathbf{n}\right) \cdot \nabla$  is the gradient operator and  $\mathbf{u}_s = \left(\underline{\mathbf{I}} - \mathbf{n} \otimes \mathbf{n}\right) \cdot \mathbf{u}$  the velocity vector, both projected onto the fluid interface. The third term on the left-hand side arises since any curvature  $\kappa = \nabla_{s} \cdot \mathbf{n} = \nabla \cdot \mathbf{n}$  of the fluid interface enhances the surface area and thereby changes the concentration. Since we are working with a smooth interface, one can show that eqn (6) is still valid with C replaced by  $C\delta_s$  and the projection (index s) is not needed.66

The presence of finite-sized particles at the fluid interface deforms the interface due to their weight, giving rise to **Paper** Soft Matter

capillary interactions. 67,68 Nevertheless, capillary interactions can be safely neglected for micron or submicron-sized particles with smooth surfaces.<sup>67</sup> Furthermore, closely placed active particles that induce force dipoles undergo hydrodynamic interactions. <sup>69,70</sup> The leading-order hydrodynamic interactions drive particles closer (extensile dipoles) or away (contractile dipoles) from each other and reorient them.<sup>71</sup> In the dilute limit, hydrodynamic interactions between active particles can be neglected. Moreover, since we consider the fixed particle orientation with respect to the fluid interface, it is sufficient to use the interfacial advection-diffusion equation [eqn (6)] to describe particle dynamics.

As introduced earlier, the phase field  $\phi$  describes the diffuse interface between fluid 1 and 2 centered around the isoline with  $\phi = 0.5$  (see Fig. 3). Its time evolution is governed by the conservative advection equation 13,64,72

$$\frac{\partial \phi}{\partial t} + \nabla \cdot (\phi \mathbf{u}) = S_{\phi}. \tag{7}$$

The interfacial source term

$$S_{\phi} = \nabla \cdot \left[ M \left( \nabla \phi - \frac{1 - 4(\phi - 0.5)^2}{\xi} \mathbf{n} \right) \right], \tag{8}$$

which is zero in the bulk fluids, is chosen such that in equilibrium one recovers the typical hyperbolic tangent profile for the phase field or order parameter,

$$\phi^{\text{eq}}(\zeta) = \frac{1}{2} + \frac{1}{2} \tanh\left(\frac{2\zeta}{\zeta}\right). \tag{9}$$

Here,  $\zeta$  is the coordinate normal to the interface with the origin  $\zeta = 0$  located in the center of the interface and  $\xi$  is the width of the profile.

Now, choosing the mobility M in eqn (8) sufficiently large, the equilibrium shape of the profile is approximately preserved even if the system becomes dynamic. 73,74 Note that the hyperbolic tangent profile agrees with the equilibrium solution of the Cahn-Hilliard phase field equation, which has been derived using physical arguments.<sup>75</sup> In the following we will use the

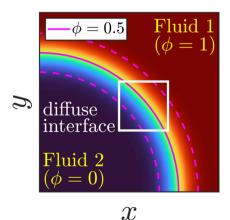


Fig. 3 One-fluid representation of the current multi-component system with density  $\rho(\mathbf{x},t)$  and viscosity  $\mu(\mathbf{x},t)$  in the framework of a diffuse interface using the phase field  $\phi$ .

modified phase field eqn (7) since the computational implementation of the second-order differential equation is relatively simple compared to the fourth-order Cahn-Hilliard equation.

To formulate an equation for the body force  $\mathbf{F}^s$  related to surface tension, we start with a two-fluid free-energy functional that captures the energy of the fluid interface, 76-78

$$F[\phi] = \int 12 \frac{\sigma}{\xi} \Big[ \phi^2 (\phi - 1)^2 + (\xi/4)^2 |\nabla \phi|^2 \Big] d^3 x.$$
 (10)

The minima of the double-well potential of the first term in the integrand correspond to fluid 1 and 2, respectively, and the gradient term guarantees a smooth interface of width  $\xi$ . Indeed, the equilibrium profile  $\phi^{eq}$  of eqn (9) minimizes the free-energy functional:  $\delta F[\phi^{eq}]/\delta \phi = 0$ . Moreover, the free energy  $F[\phi^{eq}]$  in the interface per surface area  $A_s$ , is a measure for the surface tension  $\sigma = F[\phi^{eq}]/A_s$ .

Deforming a plane interface, generates a surface-tension body force, which can be given as 79,80

$$\mathbf{F}^{s} = \frac{\delta F}{\delta \phi} \nabla \phi. \tag{11}$$

Using the interface curvature

$$\kappa = n_{i,i} = \frac{1}{|\nabla \phi|} \left[ \frac{\partial^2 \phi}{\partial x_j \partial x_j} - \frac{\partial^2 \phi}{\partial x_l \partial x_m} n_l n_m \right], \tag{12}$$

one can rewrite this as

$$\mathbf{F}^{s} = -\frac{3}{2}\sigma\xi\kappa|\nabla\phi|^{2}\mathbf{n}$$

$$+12\frac{\sigma}{\xi}\left[4\phi(\phi-0.5)(\phi-1) - \frac{\xi^{2}}{8}\frac{\partial^{2}\phi}{\partial x_{i}\partial x_{j}}n_{i}n_{j}\right]\nabla\phi.$$
(13)

Now, for fluid interfaces moving slowly compared to the relaxation time associated with the dynamics of the phase field  $\phi$ , the interface profile is approximately given by  $\phi^{eq}$ . Then, one can show that the term in the square brackets is small against the first term in eqn (13). Thus the surface-tension body force can be approximated by  $\mathbf{F}^s \approx -\frac{3}{2}\sigma\xi\kappa|\nabla\phi|^2\mathbf{n}$ . We will use this later for some qualitative arguments, while in the simulations we employ the full expression of eqn (13).

#### C. Numerical methodology

We employ a hybrid lattice-Boltzmann finite-difference scheme to solve the governing equations numerically. Specifically, the lattice-Boltzmann method<sup>81</sup> is applied to determine the fluid flow [eqn (3) and (4)] and to simulate the interface dynamics [eqn (7)], while the interfacial advection-diffusion equation [eqn (6)] is discretized and solved using the finite-difference scheme. The details of the lattice-Boltzmann implementation can be found in our recent work. 13 The same approach is used for the current solver. To implement the finite-difference solver for eqn (6), we follow the methodology proposed by Teigen et al.66 This approach solves eqn (6) in the entire domain by extending the interfacial concentration  $C(\mathbf{x},t)$  as a constant in the direction normal to the fluid interface, such that  $\int_{S(t)} C dS =$  $\int_{V} C \delta_{s} dV$ , where V is the domain volume. Furthermore, we use

the modified Crank-Nicolson method<sup>82</sup> to integrate in time and the 5th-order accurate WENO (Weighted Essentially Non-Oscillatory) scheme<sup>83</sup> to handle the advection term.

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In the simulations we use 512 grid points across the channel width w and set the interface width  $\xi$  to 4 lattice units. In our earlier work,13 we successfully tested and used the same grid resolution (derived using grid convergence) for a similar geometry and fluid parameters but with two interfaces and without activity. There, the problem was even more complex because of the high inertia of the background flow and complex interface topology (see Fig. 18 and 21 of ref. 13). For the remaining discussion, all fluid properties and parameters related to the activity (i.e.,  $\rho$ ,  $\mu$ ,  $\sigma$ , C, D, and W) are in units of the lattice-Boltzmann method. To non-dimensionalize thickness h, perturbation wavelength  $\lambda$ , amplitude  $A(\tau)$ , and time  $\tau$ , we use channel width w and viscous time scale  $w^2 \rho/\mu_m$ , where  $\mu_m =$  $2\mu_1\mu_2/(\mu_1 + \mu_2)$  is the mean viscosity. Unless stated otherwise,

we fix the thickness of the bottom fluid layer to h = 0.5 and the

diffusivity of active particles to D = 0.11, which guarantees a uniform distribution of the active particles along the deforming interface.

## III. Results and discussion

#### Activity-induced instability of the interface

To understand the role of active interfacial stresses in our system, we start with two fluids with a viscosity ratio of m = 30. Furthermore, we select an initial active particle concentration of  $C(\mathbf{x},0) = 0.5$  and set interfacial tension  $\sigma$  to zero, so that one can clearly notice the effect of activity (a discussion on the influence of  $\sigma$  will follow in Section III B). On perturbing the fluid interface by a sinusoidal modulation of wavelength  $\lambda = 0.5$ , we observe that the interface covered with contractile force dipoles of force dipole moment  $W = 2 \times 10^{-5}$  becomes unstable. In contrast, extensile force dipoles with  $W = -2 \times 10^{-5}$ 

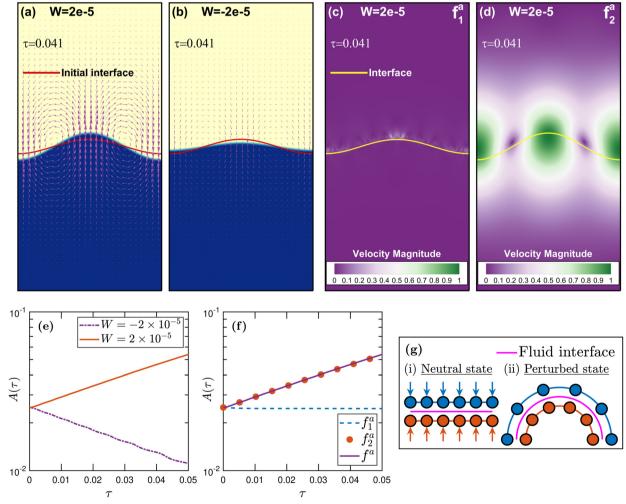


Fig. 4 Snapshots of the fluid interface and flow field at time  $\tau = 0.041$  for (a)  $W = 2 \times 10^{-5}$  and (b)  $W = -2 \times 10^{-5}$ . In (c) and (d) the snapshots for  $W = 2 \times 10^{-5}$  $10^{-5}$  show the effect of force components  $f_1^0$  and  $f_2^0$ , respectively. The velocity magnitude is given in units of the maximum flow velocity  $|\mathbf{u}|_{max}$  induced by the component  $f_2^0$  at  $\tau = 0.041$ . (e) The amplitude of the interfacial perturbation plotted vs. time for  $W = \pm 2 \times 10^{-5}$ . (f) For  $W = 2 \times 10^{-5}$  the amplitude is plotted for the total active force P and its two components P<sub>1</sub> and P<sub>2</sub>. (g) Schematic to understand the interfacial instability caused by contractile force dipoles  $\frac{1}{4}$  in (a). The remaining parameters are  $\lambda = 0.5$ ,  $m = \mu_1/\mu_2 = 30$ ,  $\sigma = 0$ , and  $C(\mathbf{x}, 0) = 0.5$  (N = 131).

attenuate the interfacial perturbation [see Fig. 4(e)]. The contractile dipoles drive a vortex pair that lets the interfacial perturbation grow, as shown in Fig. 4(a). The vortex pair consists of counterclockwise and clockwise circulation zones situated halfway between the peak and the two valleys of the interfacial height profile. For extensile force dipoles, the direction of circulation reverses [see Fig. 4(b)], driving the system back to the flat fluid

To qualitatively explain the activity-driven instability, we consider the schematic shown in Fig. 4(g). The neutral state represents the flat fluid interface laden by contractile force dipoles. Orange and blue-colored circles represent the two forces in the dipole. They are of the same magnitude and act normal to the interface on the respective fluids as indicated by the arrows. On bending the fluid interface the density of the outer forces (blue) decreases, while the density of the inter forces (red) increases. This generates a normal stress across the interface that drives the destabilizing flow for W > 0. One can compare this with the Laplace pressure acting across the interface, which balances the interfacial tension due to the increased interface. Later, in Section III B, we will elaborate more on the similarities and differences between the destabilizing active force and the stabilizing surface-tension force.

We further substantiate our qualitative explanation using mathematical reasoning. The magnitude of the active body force  $f^a$  already introduced in eqn (2) can be written in expanded form as

$$f^{a} = \underbrace{WCn_{j}\left(\frac{\partial \delta_{s}}{\partial x_{j}}\right)}_{f_{1}^{a}} + \underbrace{WC\kappa\delta_{s}}_{f_{2}^{a}} + \underbrace{W\delta_{s}n_{j}\left(\frac{\partial C}{\partial x_{j}}\right)}_{f_{3}^{a}=0}.$$
 (14)

The force  $f_3^a$  vanishes since the areal concentration  $C(\mathbf{x},\tau)$  only varies along the interface and not perpendicular to it. Moreover, for a flat interface the force  $f_2^a$  proportional to the curvature  $\kappa = n_{i,i}$  is zero, which corresponds to the neutral state shown in Fig. 4(g). We investigated the effect of the force components,  $f_1^a$  and  $f_2^a$ , on the observed interfacial instability by setting the other component to zero in our simulations. It turns out that for  $W = 2 \times 10^{-5}$  the magnitude of the flow induced by  $f_1^a$  is very marginal compared to the flow initiated by  $f_2^a$ , as Fig. 4(c) and (d) show. As a result, the component  $f_1^a$  does not contribute to the growth of the interfacial perturbation [see Fig. 4(f)]. Hence, the instability is solely driven by the force component  $f_2^a$  proportional to the interface curvature  $\kappa$ . This confirms our qualitative explanation using the schematic of Fig. 4(g).

We further quantify the interfacial instability using dispersion curves. As before, we employ the same viscosity ratio m = 30 and force dipole moment  $W = 2 \times 10^{-5}$  and set the interfacial tension  $\sigma$  to zero. We start from a flat fluid interface and impose single-mode interfacial perturbations with the rescaled wavenumber  $k/2\pi = \lambda^{-1}$  ranging from one to eight and an amplitude  $A = 2.5 \times 10^{-2}$ . Here,  $k = 2\pi$  corresponds to a wavelength  $\lambda$  equal to the channel width w. The flat interface is initially covered by contractile force dipoles with the areal

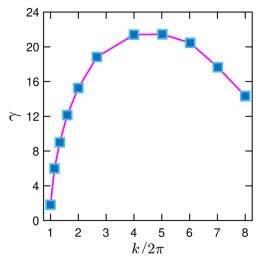


Fig. 5 Growth rate  $\gamma$  plotted *versus* wavenumber k in units of  $2\pi$  for an areal concentration of  $C(\mathbf{x}) = 0.5$  of the flat interface. The remaining parameters are  $m = \mu_1/\mu_2 = 30$ ,  $\sigma = 0$ ,  $W = 2 \times 10^{-5}$ , and  $A(0) = 2.5 \times 10^{-2}$ 

concentration of  $C(\mathbf{x}) = 0.5$ . Note that otherwise we always choose  $C(\mathbf{x},0)$  as the initial areal concentration along the perturbed interface. Upon increasing the wavenumber, the growth rate  $\gamma$  rises and peaks at  $k/2\pi = 4$  as shown in Fig. 5. This is because for larger wavenumbers (or smaller wavelengths) the interface curvature  $\kappa$  increases and with it the destabilizing active force component  $f_2^a$  in eqn (14). Then, the growth rate  $\gamma$  declines for  $k/2\pi > 4$  as the area of the perturbed interface increases with k. Therefore, the force-dipole concentration along the perturbed interface and thus the destabilizing force decreases. Note that the growth rate does not tend to zero for  $k \to 0$  as expected for vanishing curvature. Instead, it approaches zero at  $k/2\pi = \lambda^{-1} \approx 1$ . We attribute this to the nearby channel walls, which hinder the destabilizing flow to develop fully.

Dispersion curves identify and quantify the unstable modes. They are determined in a linear stability analysis, which we performed here by direct numerical simulations. Now, we observe how the most unstable mode at  $k/2\pi = 4(\lambda = 0.25)$ evolves further in time. We choose N = 131 active dipoles, which gives a concentration  $C(\mathbf{x},0) = 0.94$  at the interface, nearly twice as large compared to the linear stability analysis. Increasing the concentration of the force dipoles speeds up the instability and thereby helps to reduce the computational cost. We observe that as the instability evolves, the symmetry of the interfacial perturbation about the channel centerline breaks because of the viscosity contrast. Ultimately, the more viscous bottom fluid invades the less viscous top fluid, and the fluid interface takes the form of a finger, as shown in Fig. 6. The continued elongation of the finger results in its breakup near the tip and generates a droplet. We call this a droplet breakup via active tip streaming. A similar interface dynamics has also been observed in electrohydrodynamic (EHD) flows (see Fig. 1 of ref. 84), commonly known as EHD tip streaming. Later, in Section III C we will demonstrate how one can exploit the breakup process in Fig. 6 to systematically form droplets.

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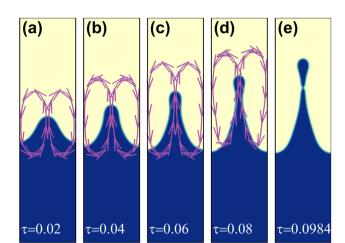


Fig. 6 Evolution of an interfacial perturbation of wavelength  $\lambda = 0.25$  into a viscous finger and its breakup for the viscosity ratio  $m = \mu_1/\mu_2 = 30$ . The streamlines show the flow induced by the activity at the interface, which generates the finger. The remaining parameters are  $C(\mathbf{x},0) = 0.94(N = 131)$ ,  $W = 2 \times 10^{-5}$ , and  $\sigma = 0$ .

Recently, Ruske and Yeomans<sup>85</sup> reported the formation of fingerlike protrusions in three-dimensional active nematic droplets due to the active flow around disclination lines near the interface. The formation of fluid fingers also occurs in hydrodynamic instabilities such as Rayleigh-Taylor86 and Saffman-Taylor,87 which, however, have different origins. The Saffman-Taylor instability originates when a less viscous fluid is continuously pumped against a more viscous stagnant fluid in a Hele-Shaw cell. Thus, it exhibits fingers that consist of a less viscous fluid, opposite of that in Fig. 6 for the present instability. This distinction arises because curved regions of the active interface penetrate the less viscous top fluid with relative ease than the more viscous bottom fluid. Moreover, unlike the Saffman-Taylor instability, the activity-driven instability prevails in the absence of viscosity contrast (m = 1)since it is solely driven by the interface curvature  $\kappa$ , as previously discussed. The presence of the viscosity contrast in our two-fluid setup enables us to realize the asymmetric interface height profile about the channel centerline, which lets us systematically deposit droplets in the top fluid, as described later in Section III C.

We further studied the influence of the viscosity ratio mon the breakup dynamics. On increasing the viscosity ratio by decreasing the viscosity of the top fluid, the bottom fluid displaces the top fluid more easily. Hence, the instability develops faster as demonstrated in Fig. 7(a). This, in turn, speeds up the breakup of the finger. However, we also observe that the size of the emitted droplet is slightly smaller [compare insets of Fig. 7(a)]. To quantify the influence of the viscosity ratio m on the growth rate, we first rescale time by  $m^{-1}$ , which results in a master curve for the amplitudes  $A(\tau)$  at early times [see inset of Fig. 7(b)]. This is expected for the linear regime of the interface dynamics. Deviations occur at later times in the nonlinear regime when approaching the breakup point. On introducing a weakly nonlinear scaling,  $\tau \propto m^{-1.25}$ , we obtain a master

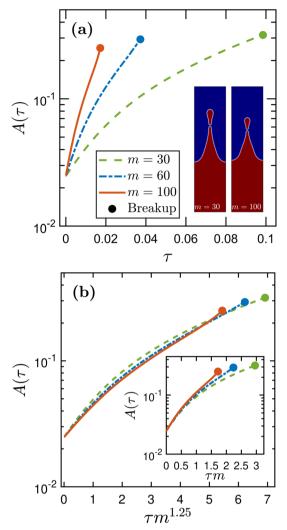


Fig. 7 (a) Amplitude of the interfacial perturbation plotted *versus* time  $\tau$ for different viscosity ratios m. The remaining parameters are  $\lambda = 0.25$ ,  $C(\mathbf{x},0) = 0.94(N = 131), W = 2 \times 10^{-5}, \text{ and } \sigma = 0. \text{ Insets: Interface after}$ breakup for the viscosity ratios of  $m = \mu_1/\mu_2 = 30$  (left) and 100 (right). (b) Master curves for the time evolution of the amplitudes obtained by rescaling time by  $m^{-1.25}$  (main plot) or by  $m^{-1}$  (inset).

curve with a good agreement near the breakup point [see main plot of Fig. 7(b)]. At early times, we see a slight deviation from the master curve for m = 30.

Next, we investigate how the activity-driven interfacial instability progresses after the first breakup. We consider a relatively thin layer of the bottom fluid with thickness h = 0.1. This allows sufficient room for the interface to penetrate the top fluid at later times. Furthermore, we set the viscosity ratio to m = 100 where the instability grows fastest [see Fig. 7(a)]. The other simulation parameters are kept the same. Snapshots from a long enough simulation run in Fig. 8(a)-(g) reveal the formation of droplets through multiple breakup events. The time variation of the perturbation amplitude  $A(\tau)$  in Fig. 8(h) (main plot) shows that these breakup events are not regular, i.e., the time elapsed between two successive breakups is not unique. The second breakup in Fig. 8(b) follows quickly

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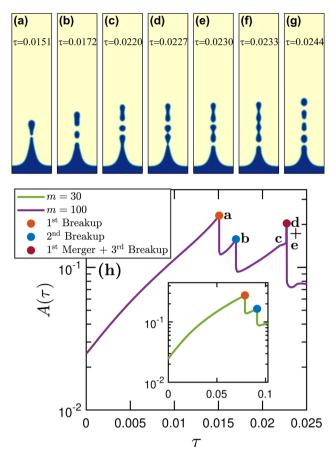


Fig. 8 (a)-(g) Activity-assisted generation of viscous droplets via the breakup of a relatively thin (bottom) fluid layer of thickness h = 0.1 and viscosity ratio  $m = \mu_1/\mu_2 = 100$ . (h) Time evolution of the interfacial perturbation  $A(\tau)$  with the marked breakup and merger events for m =100 (main plot) and m = 30 (inset). The remaining parameters are  $\lambda = 0.25$ ,  $C(\mathbf{x},0) = 0.94(N = 131), W = 2 \times 10^{-5}, \text{ and } \sigma = 0.$ 

after the first [see Fig. 8(h)]. After the second breakup, the perturbation amplitude continues to grow and the interface pushes the separated pair of droplets further up. Eventually, the

fluid interface regains a height similar to that during the first breakup [compare Fig. 8(a) and (c)]. Then a third droplet forms, merges with the preceding droplet, and bow-tie-shaped viscous ligaments form, which ultimately form a fluid chain by merging together [see Fig. 8(d)-(f)]. However, the newly formed fluid chain is unstable and disintegrates into a train of droplets [see Fig. 8(g)]. We add two comments. For the present case, where we implemented a thin bottom film, the first breakup occurs faster than with a thick bottom layer for the viscosity ratio of m = 30 [compare the case of m = 30 in the inset of Fig. 8(h) with Fig. 7(a)]. We attribute this to the presence of the channel wall. For the higher viscosity ratio of m = 100, the speedup in the breakup is very marginal.

### B. Influence of interfacial tension on the activity-induced instability

So far we set the surface tension  $\sigma$  of the interface to zero. For  $\sigma \neq 0$ , perturbing a plane interface, enhances its area and thereby its surface energy. So the non-zero surface tension always tries to damp the perturbation. Thus, for a fluid interface covered with contractile force dipoles (W > 0), surface tension and active body forces compete against each other and we expect that below a critical value  $\sigma^*$  the interface becomes unstable.

To determine  $\sigma^*$ , we recall that the relevant part of the surface-tension body force  $\mathbf{F}^s$  in eqn (13) is

$$\mathbf{F}^{s} \approx -\frac{3}{2}\sigma\xi\kappa|\nabla\phi|^{2}\mathbf{n} \simeq -\sigma\kappa|\nabla\phi|\mathbf{n}.$$
 (15)

To arrive at the expression on the right, we used that only the integral of F<sup>s</sup> over the interface profile is important and that for the equilibrium profile of eqn (9) we have

$$\int_{-\infty}^{\infty} \frac{3}{2} \zeta |\nabla \phi|^2 d\zeta = \int_{-\infty}^{\infty} |\nabla \phi| d\zeta = 1.$$
 (16)

Using the dominating curvature contribution  $f_2^a \mathbf{n} = WC\kappa |\nabla \phi| \mathbf{n}$ for the active body force from eqn (14), where  $\delta_s = |\nabla \phi|$ , we can immediately state that the fluid interface is unstable for

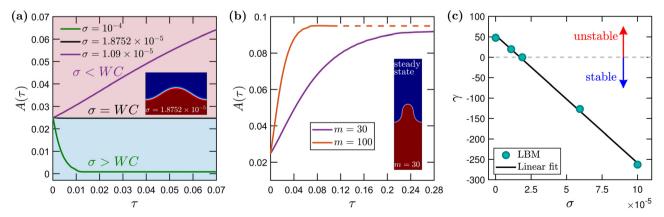


Fig. 9 (a) Amplitude of an interfacial perturbation  $A(\tau)$  plotted *versus* time  $\tau$  for three values of surface tension  $\sigma$  (below, equal to, and above  $WC(\mathbf{x},0)$ ) and a viscosity ratio  $m = \mu_1/\mu_2 = 30$ . (b) Amplitude  $A(\tau)$  at later times for  $\sigma = 1.09 \times 10^{-5} < WC(\mathbf{x}, 0)$  and  $m = \{30,100\}$ . (c) Growth rate  $\gamma$  plotted versus  $\sigma$ for m=30. Insets: Steady-state shape of the fluid interface for (a)  $\sigma=1.8752\times10^{-5}=WC$  and (b) m=30. The remaining parameters are  $\lambda=0.25$ ,  $C(\mathbf{x},0) = 0.94(N = 131)$ , and  $W = 2 \times 10^{-5}$ 

 $\sigma < \sigma^* = WC$ . To verify the expression for  $\sigma^*$  we conduct three different simulation runs with  $\sigma \ge WC(\mathbf{x}, 0)$ . Furthermore, we set the perturbation wavelength and viscosity ratio to  $\lambda = 0.25$ and m = 30, respectively.

The outcome of the direct numerical simulations is illustrated in Fig. 9(a), where we show the time evolution of the perturbation amplitude. Indeed, for an interface with strong enough surface tension ( $\sigma > WC$ ), the perturbation dies out, while for  $\sigma$  < WC we observe the interfacial instability. As predicted, on setting  $\sigma = WC(\mathbf{x},0)$ , the initial interfacial perturbation remains static, as illustrated in the inset of Fig. 9(a). Now, studying the instability for  $\sigma < WC(\mathbf{x},0)$  for a longer duration, we find that the amplitude of the interfacial perturbation eventually reaches a plateau [see the main plot and inset in Fig. 9(b)]. Similarly, for a higher viscosity ratio of m = 100, the instability also comes to a halt after an even shorter period. The reason for reaching a statically deformed interface is because the area of the growing interface increases and thus the areal concentration  $C(\mathbf{x},\tau)$  continuously drops. Ultimately, when  $\sigma = WC(\mathbf{x}, \tau^{eq})$  is reached at time  $\tau^{eq}$ , the motion of the fluid interface is arrested. We also note that the steady-state amplitude of the perturbation is a bit higher for m = 100compared to m = 30 because the viscous finger is slightly more pointed. Fig. 9(c) summarizes the instability controlled by the surface tension. Below  $\sigma^*$  the growth rate of the interfacial perturbation is positive, while the perturbation is damped for  $\sigma > \sigma^*$ . The qualitative nature of the dispersion curve in Fig. 5 also holds for unstable active interfaces with non-zero surface tension (WC >  $\sigma$ ) since the stabilizing surface tension force  $\mathbf{F}^s$  and the destabilizing active force  $f_2^a\mathbf{n}$  have the same mathematical form.

Formally, one can interpret contractile force dipoles (W > 0)as imparting a negative surface tension -WC to the fluid interface and vice versa for extensile force dipoles (W < 0). Then, for contractile force dipoles the instability is triggered when the total surface tension becomes negative. This is reminiscent of the effectively negative surface tension, which

is induced by the overpopulation of surfactants at the fluid interface as reported in ref. 88.

### C. Controlling droplet production using particles with switchable activity

Till now, we discussed two cases with contractile force dipoles: the breakup of droplets from a fluid interface at zero surface tension and the stabilizing property of the surface tension. Here, we demonstrate that by varying the destabilizing activity at the fluid interface, one can control the formation of microfluidic droplets. Such droplets can be utilized in various practical applications, e.g., as chemical reactors on lab-on-achip platforms.89

We select the parameter combination  $\{\lambda, m, W, N\} = \{0.25,$ 30,  $2 \times 10^{-5}$ , 131} and two values of interfacial tension  $\sigma = 10^{-8}$ and  $10^{-6}$ . Since both values always satisfy  $\sigma < WC$ , the interfacial perturbation grows with time and a droplet breaks up from the fluid interface, as shown in Fig. 10(a). Once the breakup is detected in our simulation, we switch off the activity by setting W = 0. As a result, the viscous finger retracts due to the stabilizing surface-tension force and leaves the droplet behind in the top fluid layer [see snapshots of fluid interface at different time instances in the insets of Fig. 10(a)]. Hence, one droplet-generation cycle consists of forming a viscous finger, the breakup of a droplet, and the damping of the interfacial perturbation due to surface tension once the activity is switched off. Increasing the surface tension from  $\sigma = 10^{-8}$ to  $10^{-6}$  does not significantly impact the finger formation. However, it dramatically speeds up the retraction of the interface [see Fig. 10(a)]. The idea of switching off activity is inspired by light-switchable active particles and surfactants, 25,91 which are used in practice. In theory, one can realize the continuous formation of droplets by periodically switching on and off the activity. However, after each droplet-formation cycle, the strength of activity at the main interface will weaken because of the gradual reduction in the areal concentration C since the droplets carry away active particles.

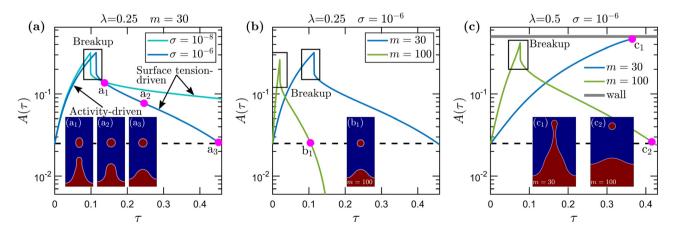


Fig. 10 Droplet generation cycle consisting of an activity-driven growth of the interfacial perturbation and droplet breakup, followed by a retraction of the viscous finger when activity is switched off immediately after breakup. Effect of (a) surface tension  $\sigma$ , (b) viscosity contrast  $m = \mu_1/\mu_2$ , and (c) a larger wavelength  $\lambda = 0.5$ . The relevant parameters are indicated in the plots. Insets: Snapshots of interface configurations as indicated by the pink bullets for  $(a_1)-(a_3)$   $\sigma=10^{-6}$ ,  $(b_1)-(c_2)$  m=100, and  $(c_1)$  m=30. The remaining parameters are N=131, and  $W=2\times10^{-5}$ .

The generation of a droplet speeds up considerably for the higher viscosity ratio of m = 100, as shown in Fig. 10(b). Furthermore, upon increasing the perturbation wavelength to  $\lambda = 0.5$  in Fig. 10(c), we observe droplet formation for m = 100but not for m = 30. In the latter case, a long finger with a broad basis and a thin tip develops, but the breakup of a droplet is hindered by the upper wall as the inset of Fig. 10(c) shows. Interestingly, we find that the droplet radius  $R_d$  remains nearly unchanged irrespective of the studied perturbation wavelength  $\lambda$  and viscosity ratio m. For the different combinations we find  $\{\lambda, m, R_d\} = \{0.25, 30, 0.037\}, \{0.25, 100, 0.031\}, \text{ and } \{0.5, 100, 0.031\}, \text{$ 0.039}.

## IV. Concluding remarks

Designs of microfluidic lab-on-a-chip devices have continuously evolved to meet practical requirements as well as to increase robustness and efficiency. In contrast to mainstream design ideas, we proposed a fairly novel approach that relies on active matter to generate microfluidic flows in a multicomponent setting. Our microfluidic setup consists of an active fluid interface separating two fluids of different viscosities. The activity is due to interfacial particles that exert dipolar forces on the two fluids close to the interface. In our numerical study, we use lattice-Boltzmann simulations to determine fluid flow, which is coupled to a phase field equation for the dynamics of the interface. In addition, an advection-diffusion equation governs the active-particle density at the curved interface.

Our direct numerical simulations uncovered that flat fluid interfaces laden with contractile force dipoles can become unstable, while extensile force dipoles never destabilize the interface. The instability is driven by the interface curvature, which creates an imbalance between the densities of the two dipolar force components at the interface. For zero surface tension of the interface, a viscous finger develops which breaks up into multiple droplets. For non-zero surface tension, a sufficiently large active-force density is needed to destabilize the flat interface ( $WC > \sigma$ ). Since the active-force density decreases for a deformed interface, a static deformation can develop. For sufficiently large active forces, a droplet breakup occurs. Using switchable activity, we show how one can control droplet formation.

To realize the activity-driven droplet formation, one needs to fulfill  $WC > \sigma$ . Typical values for the surface tension of the fluid interface are close to  $\sigma = 10^{-4} \text{ N m}^{-1}.92$  To estimate the force-dipole strength, we follow ref. 93 and take  $W \sim \mu U l_s^2$ , where  $l_s$  is the length of the active particle and U its swimming speed. A good estimate for the concentration is  $C \sim g^2/l_s^2$ , where g refers to the aspect ratio of the active particle, and one finds  $WC \sim g^2 \mu U$ . For larger rodlike microswimmers such as Bacillus subtilis with  $U = 100 \mu \text{m s}^{-1}$  and  $g = 10^{33}$  and a more viscous fluid such as silicone oil with  $\mu = 10^{-2} \text{ kg ms}^{-1}$ , 94 one obtains indeed  $WC \sim \sigma$ . Another strategy to fulfill  $WC > \sigma$  is to use fluid interfaces with an ultra-low surface tension such as  $\sigma = 10^{-6} \,\mathrm{N \ m^{-1}}$  reported in ref. 95. This allows to reduce the size

of the active particles and the viscosity. Finally, the fluid interface is also unstable under Poiseuille flow, 13 which can help to induce the droplet formation.

Microfluidic lab-on-a-chip systems often take advantage of the inherent nonlinearities of viscoelastic flows to systematically steer<sup>17</sup> and encapsulate<sup>96</sup> particles. Likewise, incorporating viscoelastic fluids in the proposed active microfluidic setup may extend the utility of the current design. For example, characterizing the response of the active interface in the presence of a neighboring viscoelastic fluid can open up a new way to implicitly determine the rheological properties of viscoelastic fluids in practice. There already exists microfluidic rheometers, which employ the crossstream particle migration in viscoelastic channel flows<sup>97</sup> and stagnation point flows in cross-slot geometries<sup>98</sup> to assess the elasticity of viscoelastic fluids. Devising such microfluidic rheometers is one of the topical microfluidic applications with immense practical value.

The present work on active fluid interfaces provides theoretical insights into how to combine microfluidics and active matter. More importantly, our results on the activity-driven formation of droplets are convincing enough that active-matter microfluidics is a promising concept for multi-component flows on the micron scale. Bringing these theoretical ideas to life will have far-reaching consequences due to their utility in lab-on-a-chip applications. For example, having solute particles in the more viscous fluid, one can controllably encapsulate them into droplets. Active-matter microfluidics is still an emerging field. We hope our work will motivate experiments that explore the potential of combining multi-component microfluidics with active matter.

## Conflicts of interest

There are no conflicts of interest to declare.

# Appendix A: Validation of the interfacial advection-diffusion solver

The benchmarking of our finite difference implementation for the interfacial advection-diffusion equation [eqn (6)] is carried out using two different test cases proposed by Teigen et al.82 In the first test case, we consider a static interface in the absence of the background flow to check the correctness of the numerical implementation of the diffusion term in eqn (6). For the second test case, we set the diffusivity D to zero and impose a predefined flow field to verify the advection-driven transport of active particles. Moreover, in the second test case, the interface location is known analytically at all times. Thus we do not need to solve the phase field equation. The time step is set to  $\Delta t = 10^{-4}$  in both test cases. The outcome of our test cases is compared with the analytical solution proposed by Teigen et al. 82 As plotted in Fig. 11, excellent agreement is found between the analytical and present numerical results.

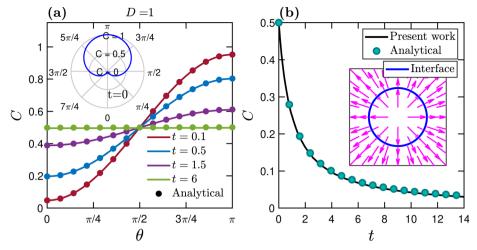


Fig. 11 (a) Diffusion-driven [ $\mathbf{u}(\mathbf{x},t) = 0$ ] temporal evolution of the areal concentration  $C(\theta,t)$  along a circular interface [centered at (0,0)] of radius r = 1 in a square domain of the size L = 4. The computational domain is discretized using 256 grid points in each direction. The polar plot in the inset shows the angular variation of C at time t = 0. (b) Advection-driven (D = 0) temporal evolution of the areal concentration C(t) for a circular interface [centered at (0,0), initial radius r(t=0)=1] expanding at a constant speed in a square domain of the size L=32. The computational domain is discretized using 320 grid points in each direction. Inset: Vector plot corresponding to the flow field employed in the present test case:  $\mathbf{u}(\mathbf{x},t) = (\cos\theta,\sin\theta)$ .

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