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# Can range-separated functionals be optimally tuned to predict spectra and excited state dynamics in photoactive iron complexes?†

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Density functional theory is an efficient computational tool to investigate photophysical and photochemical processes in transition metal complexes, giving invaluable assistance in interpreting spectroscopic and catalytic experiments. Optimally tuned range-separated functionals are particularly promising, as they were created to address some of the fundamental deficiencies present in approximate exchange-correlation functionals. In this paper, we scrutinize the selection of optimally tuned parameters and its influence on the excited state dynamics, using the example of the iron complex  $[\text{Fe}(\text{cpmp})_2]^{2+}$  with push-pull ligands. Various tuning strategies are contemplated based on pure self-consistent DFT protocols, as well as on the comparison with experimental spectra and multireference CASPT2 results. The two most promising sets of optimal parameters are then employed to carry out nonadiabatic surface-hopping dynamics simulations. Intriguingly, we find that the two sets lead to very different relaxation pathways and timescales. While the set of optimal parameters from one of the self-consistent DFT protocols predicts the formation of long-lived metal-to-ligand charge transfer triplet states, the set in better agreement with CASPT2 calculations leads to deactivation in the manifold of metal-centered states, in better agreement with the experimental reference data. These results showcase the complexity of iron-complex excited state landscapes and the difficulty of obtaining an unambiguous parametrization of long-range corrected functionals without experimental input.

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## 1 Introduction

Transition metal complexes are widely applied as catalysts, photosensitizers, and dyes.<sup>1–3</sup> Popular examples are six-coordinated ruthenium(II) and iridium(III) polypyridine complexes that have found numerous applications in photocatalysis and light-harvesting technologies, including dye-sensitized solar cells. However, due to the costs of rare metals, there is a significant effort to switch to the more Earth-abundant and economic copper- or iron-based complexes.<sup>4,5</sup> Unfortunately, the usage of iron in polypyridine complexes is still limited due to the fast deactivation of metal-to-ligand

charge-transfer (MLCT) states *via* metal-centered (MC) ones to the ground state.<sup>6,7</sup> This relaxation prevents utilizing the initial charge separation in MLCT states for further redox reactions. In order to find novel complexes with long-lived MLCT states, the excited-state behavior of such compounds needs to be carefully rationalized.<sup>8–10</sup> An atomistic picture of the excited-state reactivity can be obtained by simulating the photodynamics of transition metal complexes.<sup>11</sup> If the reaction coordinates of the problem at hand are known and comprise only a few degrees of freedom, it is possible to simulate excited-state processes with high accuracy using quantum wave packet dynamics.<sup>12</sup> By contrast, if too many degrees of freedom are involved or the relevant ones cannot be guessed *a priori*, a widely used strategy is to apply *ab initio* molecular dynamics methods, such as trajectory surface hopping (TSH).<sup>13</sup> The latter simulate the photodynamics of a molecule in full dimensionality leveraging approximate classical trajectories for the nuclear motion instead of quantum wave packets.

Regardless of quantum wave packets or classical trajectories, the motion of the nuclei is governed by the topology of the potential energy surfaces (PESs), so that this will be meaningful, only if the underlying electronic states are accurately described. Transition metal complexes, with their high density of low-lying

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excited states of different characters, pose intricate challenges to electronic structure methods. Due to its moderate computational costs, efficiency, and “black-box” character, density functional theory (DFT) and its linear-response time-dependent extension (TDDFT) enjoy great popularity.<sup>14</sup> For dynamics simulations, where a large number of single-point calculations are required, using formally higher-ranked theoretical methods is not yet an alternative. However, DFT suffers from errors imbued in the approximate nature of the exchange-correlation functionals.

A common problem of many approximate functionals is the erroneous description of charge transfer (CT) states due to unphysical electronic self-interaction.<sup>15,16</sup> This problem can be alleviated by including exact exchange interaction from Hartree-Fock theory in the functional. While hybrid functionals such as B3LYP do this in a fixed manner, a more balanced inclusion is realized in range-separated functionals. They include the exact exchange weighted with a damping function that depends on the inter-electronic distance, ensuring a smooth transition from the short- to the long-range domain.<sup>17–19</sup> This approach aims at minimizing the spurious electron's self-interaction energy<sup>20,21</sup> and mitigating the (de) localization error.<sup>22</sup> It remains then only necessary to determine the steepness of the damping function, a feature that can be obtained for the individual system by tuning the energetic positions of highest occupied (HOMO) and lowest unoccupied molecular orbitals (LUMO) to fit the *ab initio* ionization potential (IP) and electron affinity (EA).

Despite the fact that tuned range-separated functionals have been shown to be very useful for describing properties related to fundamental and optical energy gaps,<sup>22–32</sup> it can be non-trivial to obtain a unique set of range-separation parameters,<sup>25</sup> particularly if one needs to describe both CT and locally excited states on the same footing. Furthermore, it is far from obvious whether different parameters would ultimately lead to the same relaxation mechanisms after light irradiation. Therefore, in this work, we critically examine the performance of several range-separation parameters on the absorption spectrum, PESS, and ultimately on the excited state dynamics of the Fe(II) complex [Fe(cpmp)<sub>2</sub>]<sup>2+</sup> (see Fig. 1), where cpmp = 6,2''-carboxypyridyl-2,2'-methylamine-pyridyl-pyridine is a push-pull ligand used

previously in an analogous ruthenium(II) compound.<sup>33</sup> This complex, recently synthesized and experimentally characterized,<sup>34</sup> follows two strategies for achieving long-sought long-lived MLCT states:<sup>35</sup> forming a close to octahedral coordination of the central iron that maximizes the ligand-field splitting and destabilizing the MC states by electron-rich ligands while simultaneously stabilizing the MLCT states by  $\pi$ -acceptor groups, such as in other iron(II) push-pull complexes.<sup>36–40</sup>

We first investigate different routes to tune the range-separation parameters of the LC-BLYP functional<sup>18</sup> (Section 2). The accuracy of different sets of range-separation parameters is benchmarked against experimental data and the more accurate multi-reference wave function based method CASPT2 (Section 3). We then use the two most promising sets of range-separation parameters to parametrize the PESS on which TSH molecular dynamics simulations are carried out (Section 4). To our surprise, the simulated photodynamics delivers strikingly different mechanisms that can be traced back to the different electronic characters of the states obtained with the two sets of parameters. In order to determine the correct mechanism, we need time-resolved spectroscopic experiments. This study highlights how theory alone can struggle to provide the correct dynamical picture and how easily one can be led astray.

## 2 Tuning of the DFT functional

### 2.1 $\Delta$ SCF tuning for the electronic ground state

The range-separation parameters  $\alpha$  and  $\omega$  have been tuned for the generalized form (eqn. (1)) of the LC-BLYP functional based on the following partitioning of the Coulomb operator:<sup>18</sup>

$$\frac{1}{r_{12}} = \frac{1 - [\alpha + \beta \times \text{erf}(\omega r_{12})]}{r_{12}} + \frac{\alpha + \beta \times \text{erf}(\omega r_{12})}{r_{12}} \quad (1)$$

With this, the initial exchange kernel in DFT is complemented with the exact Hartree-Fock exchange, which has the correct asymptotic behavior. The  $\omega$  parameter defines the switching rate between short and long-range exchange, and its inverse is proportional to a characteristic interelectron distance. The second (dimensionless) parameter  $\alpha$  sets a global

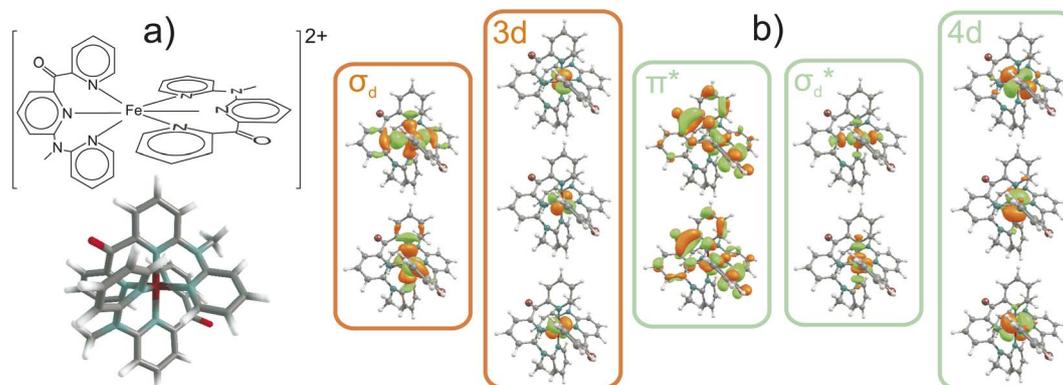


Fig. 1 (a) Schematic and 3D view of [Fe(cpmp)<sub>2</sub>]<sup>2+</sup> (cpmp = 6,2''-carboxypyridyl-2,2'-methylamine-pyridyl-pyridine). (b) Active space for multireference calculations. The occupied and vacant orbitals in the ground state are marked with orange and green boxes, respectively.



$r_{12}$ -independent exact-exchange contribution. We assume  $\beta = 1 - \alpha$  to ensure that self-interaction is asymptotically canceled by the exact exchange. Thus, the range-separated part of the LC-BLYP functional depends on the parameters ( $\alpha$ ,  $\omega$ ) that we can exploit for tuning. The particular functional LC-BLYP has been chosen for tuning, as it is the most similar one to the popular B3LYP that we have applied for the purpose of comparison. Note that other functionals like BNL or PBE could be a possible option too, see *e.g.* ref. 22 and 29.

The tuning most commonly follows the  $\Delta$ SCF method.<sup>21,41,42</sup> Here, the energetic positions of the HOMO and LUMO of a given system are tuned to the ionization potential (IP) and electron affinity (EA) according to Koopmans' theorem. To find the optimal range-separation parameters, we computed the tuning function  $J^*$ , which is the measure of violation of Koopmans' theorem for both the HOMO and the LUMO, on a grid of ( $\alpha$ ,  $\omega$ ) pairs using the LC-BLYP functional and 6-31G(d) basis set<sup>43,44</sup> at the B3LYP<sup>45</sup>/def2TZVP<sup>46,47</sup> optimized  $S_0$  ground-state geometry. Additional computational details are reported in Section S1.1 and the general strategy employed in our optimal tuning calculations is explained in Section S2. In this study, we focus on the ranges [0.0–0.3] for  $\alpha$  and [0.00–0.25] for  $\omega$ , which are typical values for organometallic systems with conjugated ligands.<sup>48–58</sup>

The resulting two-dimensional plot of  $J^*(\alpha, \omega)$  presented in Fig. 2 displays a global minimum of  $J^*$  at (0.00; 0.14); exemplary 1D-cuts at  $\alpha = 0$  are in Fig. S1.† This minimum is located in the minimal valley of points marked with white circles in Fig. 2(a), while other  $\alpha$  values correspond to near-optimal ( $\alpha, \omega$ ) choices. We analyzed the deviations from piecewise-linearity<sup>59,60</sup> for fractional electron charges (Section S2.1) to further scrutinize different points along the minimal valley on  $J^*(\alpha, \omega)$ , where again, the (0.00; 0.14) parameters without short-range exchange performed best.

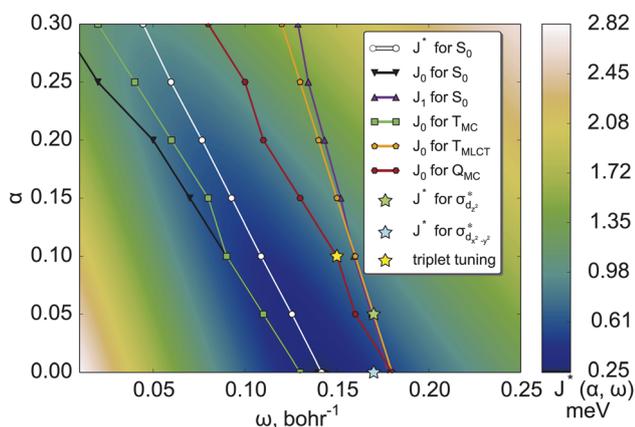


Fig. 2  $J^*(\alpha, \omega)$  (measure of violation of Koopmans' theorem for both the HOMO and the LUMO (see detailed explanation in Section S2) for  $[\text{Fe}(\text{cpmp})_2]^{2+}$  in the ground electronic state. White points denote the minima of  $J^*(\alpha, \omega)$  at constant  $\alpha$  values for the ground  $S_0$  state. Black, green, orange and red points denote the corresponding minima for IP-tuning only for  $S_0$ ,  $T_{\text{MC}}$ ,  $T_{\text{MLCT}}$ , and  $Q_{\text{MC}}$  states, respectively. Optimal points for triplet tuning and MC-tuning are also presented, see the text for more details.

The variational stability of all combinations of parameters was investigated and no convergence towards other electronic states was observed. Thus,  $\Delta$ SCF tuning of the  $S_0$  state suggests the global minimum of  $J^*$  found at (0.00; 0.14) as the optimal range-separation parameters. In the following, this will be abbreviated as set A. We note, however, that the  $J^*$  tuning delivers only a compromise between the  $J_0$  (HOMO/IP) and  $J_1$  (LUMO/EA) tuning. It can be seen from Fig. 2, showing that the minimal values of  $J_0$  and  $J_1$  (black and blue lines) do not coincide.

## 2.2 “MC-tuning” for the electronic ground state

The standard  $\Delta$ SCF<sup>21,41,42</sup> approach is designed for the adjustment of the positions of HOMO and LUMO energies. Thus, for complexes where the frontier orbitals are localized on both the metal and ligands, it results in a better description of MLCT states. To better reproduce the transition energies of MC states, we follow the same approach as above but instead of using the LUMO localized on ligands, we use  $\sigma_{d_{z^2}}^*$  and  $\sigma_{d_{x^2-y^2}}^*$  orbitals localized on the iron center, see Fig. 1. Using this “MC-tuning” leads to the optimal range-separation parameter pairs of (0.05, 0.17) and (0.0, 0.17) for both  $\sigma^*$ -orbitals (see green/blue stars in Fig. 2). The sets of parameters for both MC-tuning variants are quite close to each other. Both points, however, lie quite apart from the HOMO/IP tuning condition ( $J_0$ ) which appears unexpected. It is noteworthy that the influence of the LUMO/EA condition ( $J_1$ ) in this approach is much larger than for the standard scheme which likely explains the different HOMO/IP results.

## 2.3 $\Delta$ SCF tuning of electronic excited states

The study of photophysical properties requires to have a balanced description of multiple electronic states. Our optimal tuning considered so far only the electronic ground state, although we have used different LUMOs to target electronic states of different characters. The transferability of the tuned parameters to electronically excited states is investigated, performing optimal-tuning calculations for the two lowest triplet excited states of MC ( $T_{\text{MC}}$ ) and MLCT characters ( $T_{\text{MLCT}}$ ) as well as the lowest excited quintet state also of MC character ( $Q_{\text{MC}}$ ). For the excited states, we considered only tuning the HOMO/IP condition  $J_0$  and show thus, only the minimum valleys of this function for the different electronic states in Fig. 2.

As can be seen, the position of optimal ( $\alpha, \omega$ ) pairs is sensitive to both the multiplicity and character of the electronic state. For the  $T_{\text{MC}}$  state, the resulting set of ( $\alpha, \omega$ ) pairs (green points) is close to the HOMO/IP curve for the ground state (black curve). This behavior is due to the HOMO being located on the central iron atom in the ground state. Analogously, the optimal parameters for  $T_{\text{MLCT}}$  are close to the LUMO/EA set where the ligand-localized LUMO is considered. For the  $Q_{\text{MC}}$  excited state, a double MC excitation, the results are more complicated. Its optimal parameters (dark red curve in Fig. 2) are closer to the HOMO/IP condition than to the LUMO/EA one. This fact might be connected with the higher multiplicity, where strong exchange plays a greater role. Importantly, the



optimal parameters of the (full)  $J^*$  tuning (HOMO/IP + LUMO/EA) of the electronic ground state fall in the middle of the HOMO/IP valleys of the different excited states, thus representing a compromise between multiple electronic states.

## 2.4 Triplet tuning

As an additional option, we have considered the recently suggested “triplet tuning” scheme<sup>55</sup> based on the assumption that  $\Delta$ SCF and TDDFT approaches with the exact exchange-correlation functional should yield the same energy of the first triplet excited state. We located the global minimum at (0.10; 0.15); see the yellow star in Fig. 2. In general, the nature of the lowest triplet states can change depending on the range-separation parameters. In the present case, the triplet tuning parameters are similar to the  $\omega$  value of the HOMO/IP minimum in the  $T_{\text{MLCT}}$  state for  $\alpha = 0.10$ ; compare the position of the yellow asterisk and nearest green circle in Fig. 2. Fortunately, in this range of parameters, the MLCT state is the lowest one such that the tuning results are consistent with each other.

## 3 Performance of range-separation parameters in stationary calculations

**3.1 Vertical and adiabatic excitation energies.** Using the  $\Delta$ SCF method, we obtained an optimal set of range-separation parameters of ( $\alpha = 0.00$ ;  $\omega = 0.14$ ) (set A) considering the electronic ground state. Applying the  $\Delta$ SCF method to different electronic states showed that while set A is a good compromise among electronic states of different characters, for individual states, other range-separation parameters are optimal. Studies of similar iron complexes typically recommended including a certain portion of constant exchange in the functional, *i.e.*,  $\alpha \neq 0$ .<sup>54,56</sup> Furthermore, for photoemission spectra of various compounds including copper phthalocyanine, it was shown that tuned functionals with  $\alpha > 0$  led to better mitigation of short-range one-electron self-interaction errors and therefore to a better description of spectra.<sup>29,61</sup> Thus, it is interesting to investigate the influence of the range-separation parameters on the static properties of  $[\text{Fe}(\text{cpmp})_2]^{2+}$ .

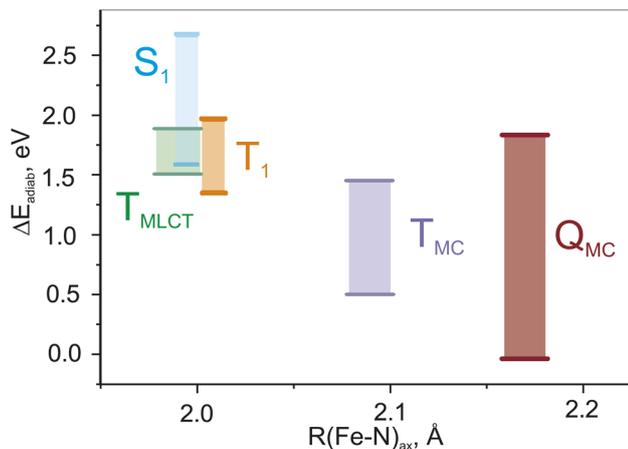


Fig. 3 Changes of adiabatic and vertical ( $S_1$  and  $T_1$ ) energies for all lowest excited states in the whole range of  $\alpha$  and  $\omega$  parameters.

Fig. 3(a) shows the ranges of the vertical  $S_1$  and  $T_1$  excitation energies at the  $S_0$  geometry as well as the adiabatic  $T_{\text{MC}}$ ,  $T_{\text{MLCT}}$ , and  $Q_{\text{MC}}$  excitation energies over the whole set of parameters. These energy ranges are plotted against the Fe–N bond length, which is the main geometric difference between these electronic states. We note that the energies of the  $T_{\text{MLCT}}$  state have the smallest dependence on the tested range-separation parameters, whereas both MC states vary substantially. The influence of the range-separation parameters on the  $Q_{\text{MC}}$  state is even larger than for the  $T_{\text{MC}}$  state. For a certain domain of parameters, the  $Q_{\text{MC}}$  is lower than the singlet ground state, see Fig. S3.† This fact is not surprising since the exchange energy plays a more important role for the MC states than for the MLCT state, as the unpaired spins are located on the same moiety, *i.e.*, the iron center, and not separated by a relatively large distance as in the case of MLCT states.

## 3.2 Comparison to multireference calculations

To evaluate the correctness of the parameters for LC-BLYP, we use the high-level wave-function based method CASPT2 (Section S1.2†). The active space (Fig. 1) is able to describe both MC and MLCT states. The energies of the lowest singlet and triplet states are summarized in Fig. 4 and compared to the TDDFT results obtained for different parameter pairs from the minimum valley. The points are placed on the graph according to the value of the constant exact exchange ( $\alpha$ ); the respective  $\omega$ -values can be found in Fig. 2. In addition, we show results obtained with B3LYP that uses only a constant amount of exchange of 0.2.

Before comparing the TDDFT and CASPT2 energies of the corresponding MC and MLCT states, we note the influence of the range-separation parameters on the state characters. For this, we show the amount of contribution of MLCT and MC configurations to the state vector by the red and blue boxes, respectively, in the upper and lower panels in Fig. 4. As can be seen, states assigned to MLCT (upper panel) possess a clear dominant MLCT character of 60–80% throughout the different range-separation parameters tested. States of predominant MC character (bottom panel) possess a more diverse mixture with notable MLCT admixture. Upon increasing the exact exchange  $\alpha$ , however, the MC character increases leading to a clearer assignment of both singlet and triplet states to MC ones, highlighting the importance of exact exchange for MC states.

When calculating singlet excited states, CASPT2 predicts the MC state (blue line) above the MLCT state (red line). This situation is independent of the IPEA shift,<sup>62,63</sup> as discussed in more detail in Section S3.† The same state ordering as in CASPT2 is found in TDDFT for  $\alpha \leq 0.20$ , while the best agreement between TDDFT and CASPT2 is reached for small exact exchanges  $\alpha \leq 0.10$ . For triplet excited states (right part of Fig. 4), the situation is different: while CASPT2 predicts the MC state (blue line) below the MLCT state (red line), this state ordering is only found for larger exact exchanges  $\alpha \geq 0.20$  in TDDFT calculations, *i.e.*, opposite to the singlet states. Only for one tested range-separation parameter set, (0.2; 0.08), the order of both singlet and triplet lowest states in the TDDFT calculations agrees with CASPT2 results. In consequence, these



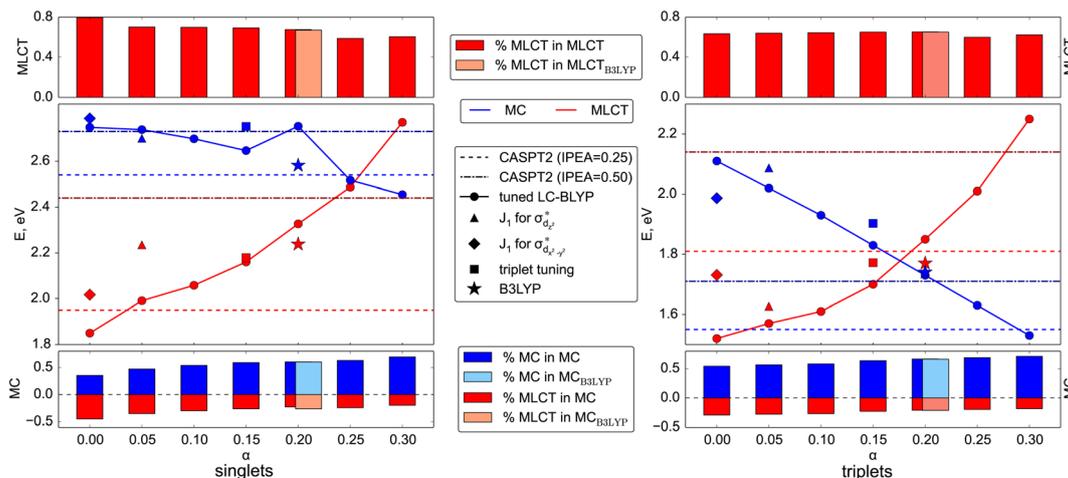


Fig. 4 Energies of the lowest MC and MLCT states in the singlet (left panel) and triplet (right panel) manifolds predicted by various LC-BLYP variants, as well as B3LYP, and CASPT2 reference. Additionally, the energies of the corresponding states calculated with tuned LC-BLYP according to triplet tuning and MC tuning procedures. The percentage of the main character of the states is provided in upper (MLCT) and lower (MC) parts of both panels. Note the different energy scales of both main panels: the triplet energies are less susceptible to changes in optimal parameters.

parameters, marked in the subsequent discussion as set B, also provide the best agreement between CASPT2 and TDDFT excitation energies with differences of 0.1–0.3 eV. Meanwhile the (0.20; 0.08) parameter set B is also located in the minimal valley of optimal tuning (see Fig. 2), but its values differ notably from the optimal-tuned set A of (0.00; 0.14). To describe spectroscopic observables, three essential but not equivalent criteria for the functional should be considered: piecewise linearity, freedom from self-interaction, and an exact asymptotic potential. While the first and third conditions are fulfilled by optimally tuned functionals by construction, the second one is achieved only asymptotically.<sup>61</sup> For this reason, the local  $\sigma$ -orbitals should suffer from uncompensated self-interaction error more than delocalized  $\pi$ -orbitals.<sup>27,64</sup> Thus, within the numerical accuracy, among optimally tuned functionals with comparably good fulfillment of Koopmans' and Janak' theorems (first and third conditions), those with a portion of exact exchange in the short range allow for better mitigation of self-interaction error and a more balanced description and energy ordering of differently localized orbitals and, thus, excited states of different nature.<sup>27,61,64</sup> For both selected sets of parameters A and B, the degree of localization of orbitals is visually indistinguishable. However, the energetic position of  $\sigma$  orbitals is more sensitive to the portion of exact exchange in the short range than those of  $\pi$ -orbitals, see Fig. S2.†

In an effort to investigate further the influence of the different parameter sets, we analyze the consequences of using both sets beyond the Franck–Condon region. First, we evaluate the agreement of the absorption spectra with the experimental data. Second, we investigate the behavior of the potential energy curves along the important Fe–N bond length. And finally, we simulate the excited-state dynamics of the complex in solution.

### 3.3 Comparison to experimental absorption spectrum

While the  $\Delta$ SCF approach is a non-empirical method for tuning functionals, experimental results can also provide valuable

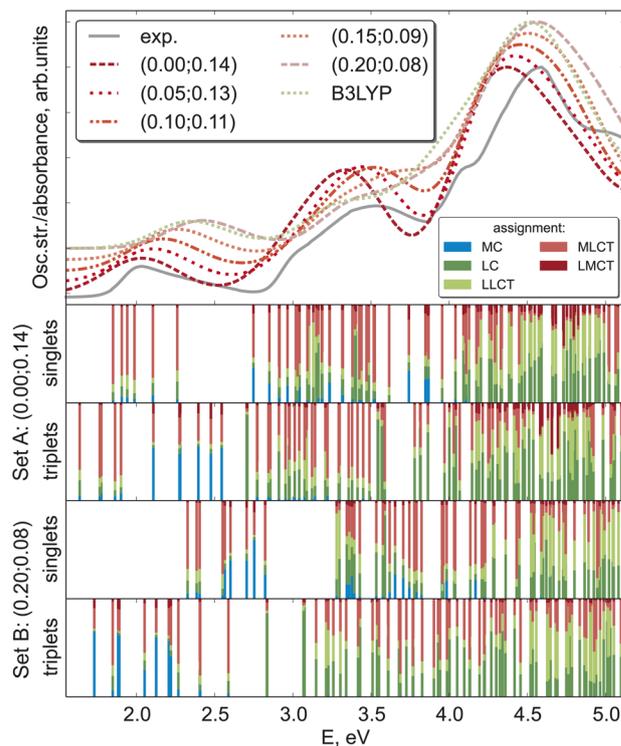


Fig. 5 Absorption spectrum of  $[\text{Fe}(\text{cpmp})_2]^{2+}$  in acetonitrile predicted by various DFT variants as compared to experimental data. The  $(\alpha, \omega)$  pairs of parameters for tuned LC-BLYP are given in the legend. Theoretical spectra are shifted vertically according to the  $\alpha$ -parameter. The lower 4 panels show the density-matrix analysis of the corresponding excited states computed with two sets of optimal parameters.



guidance for justifying the chosen computational scheme.<sup>25</sup> As excited state properties are of particular interest for such complexes, the natural choice of the experimental reference is the absorption spectra. Fig. 5 compares the experimental absorption spectrum<sup>34</sup> against spectra computed with LC-BLYP and combinations of  $(\alpha, \omega)$  along the minimal valley in the optimal-tuning plot as well as with the popular B3LYP functional. For set A and set B of optimal parameters, the transition-density-matrix analysis of singlet and triplet spectra is also shown.

All theoretical spectra agree well with the experiment, with the first feature around 2.0 eV being better reproduced by LC-BLYP with a smaller constant portion of the exact exchange  $\alpha$ . Upon increasing  $\alpha$ , all three band maxima are shifted to higher energies, a behavior observed for bright local and charge-transfer states previously.<sup>48</sup> MC states may exhibit an opposite behavior (see above), but usually they possess considerably smaller oscillator strengths. The B3LYP and LC-BLYP (0.20; 0.08) functionals with the same portion of global exact exchange give very similar spectra. As the experimental spectrum of  $[\text{Fe}(\text{cpmp})_2]^{2+}$  has rather broad bands without any fine structure, it leaves some ambiguity in identifying the best computational scheme for  $[\text{Fe}(\text{cpmp})_2]^{2+}$ .

### 3.4 Potential energy surfaces

Based on the analysis of Huang-Rhys factors, we identified that the most important tuning mode corresponds to the Fe–N breathing mode (ground-state frequency is  $210 \text{ cm}^{-1}$ ). Therefore, we obtained one-dimensional potential energy profiles for this mode for the two sets of range-separation parameters A and B. Interestingly, there is a prominent difference between both sets of obtained energy profiles, as shown in Fig. 6. Most notably, the MLCT states (those with energy minima near  $Q = 0.0$ ) shift to higher energies for the larger  $\alpha$ , whereas the MC states (with a minimum at  $Q \sim 0.8$

$\text{bohr} \cdot (\text{a.m.u.})^{1/2}$ ) shift to lower energies. This result already indicates that both sets of  $(\alpha, \omega)$  pairs could lead to different photodynamics due to the character of the lowest excited states, as it will be investigated next.

## 4 Performance of range-separation parameters in nonadiabatic dynamics

### 4.1 Electronic state populations

We showed that the selection of the range-separation parameters significantly affects the nature of the lowest excited states at the Franck–Condon geometry (Fig. 5) as well as the PESs of the breathing mode of  $[\text{Fe}(\text{cpmp})_2]^{2+}$  (Fig. 6). We now investigate its effect on the photodynamics by using TSH nonadiabatic simulations on linear vibronic coupling (LVC) parametrized potentials<sup>65,66</sup> along the 213 vibrational degrees of freedom of  $[\text{Fe}(\text{cpmp})_2]^{2+}$ . The LVC potentials were set up for the range-separation parameters of set A and set B, including 11 singlet/20 triplet states and 9 singlet/14 triplet states, respectively, corresponding to the number of electronic states in the energy range of the lowest-energy absorption band (up to 2.5 eV, Fig. 5). Full computational details are reported in Section S1.3†.

The resulting TSH dynamics in the LVC electronic potentials from both sets of range-separation parameters is shown in Fig. 7 for the first 500 fs. We performed SH dynamics for a total of 2 ps (Fig. S5†), but during the first 500 fs, the dynamics reached a steady state (for set A) or ended all previously started processes (for set B).

The time evolution of the adiabatic state populations is shown in Fig. 7(a and b). For set A, the dynamics starts by exciting  $[\text{Fe}(\text{cpmp})_2]^{2+}$  into higher-lying singlet states  $S_N$  ( $N \geq 2$ , orange curve), from which most of the population undergoes ultrafast intersystem crossing to higher-lying triplet states  $T_N$  ( $N \geq 3$ , violet curve). Within the triplet manifold, further relaxation to  $T_2$  (light-blue curve) and  $T_1$  (dark-blue curve) occurs on sub-100 fs time scales. After *ca.* 300 fs, the population is stable in the  $T_1$ ,  $T_2$ , and  $T_N$  states. As a minor reaction channel, the population initially decays from the  $S_N$  to the  $S_1$  state (red curve) on a 2 ps time scale, from where also the  $T_N$  states are reached.

By contrast, the dynamics employing parameters of set B is very different. Despite mostly starting also in the higher-lying singlet states  $S_N$ , the adiabatic population bifurcates in a 2 : 1 ratio. The smaller portion decays to the  $S_1$  state – also initially populated by 15% – from where the whole singlet population relaxes to the adiabatic ground state  $S_0$  (green curve), all within a *ca.* 100 fs time scale. The majority of the  $S_N$  population undergoes intersystem crossing to higher-lying triplet states  $T_N$  ( $N \geq 2$ ), which rapidly reach the  $T_1$  state. From the  $T_1$  state, the system undergoes back-intersystem crossing to the adiabatic ground-state  $S_0$ , however, at a slower rate on a sub-1 ps time scale. This adiabatic  $S_0$  state does not correspond to the diabatic  $S_0$  state, *i.e.*, the  $S_0$  state in the Franck–Condon geometry, at least at early simulation times, as discussed in more detail in Section S4.6.†

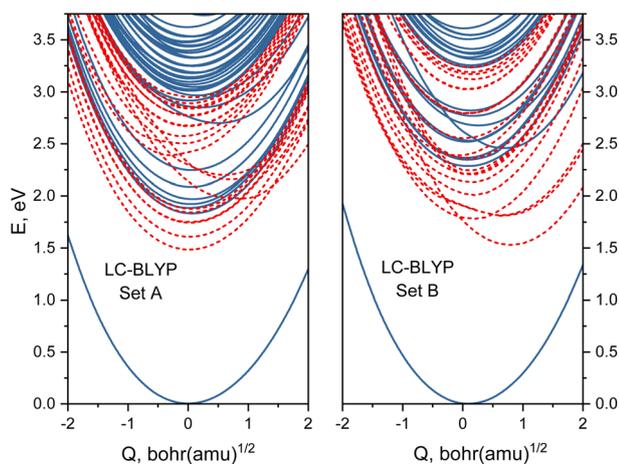


Fig. 6 Potential energy sections along the breathing mode computed with optimally tuned LC-BLYP with different range-separation parameters  $(\alpha, \omega)$  left-hand side: set A (0.0; 0.14); right-hand side: set B (0.20; 0.08). Blue solid lines denote singlet states while red dashed curves show triplet states.



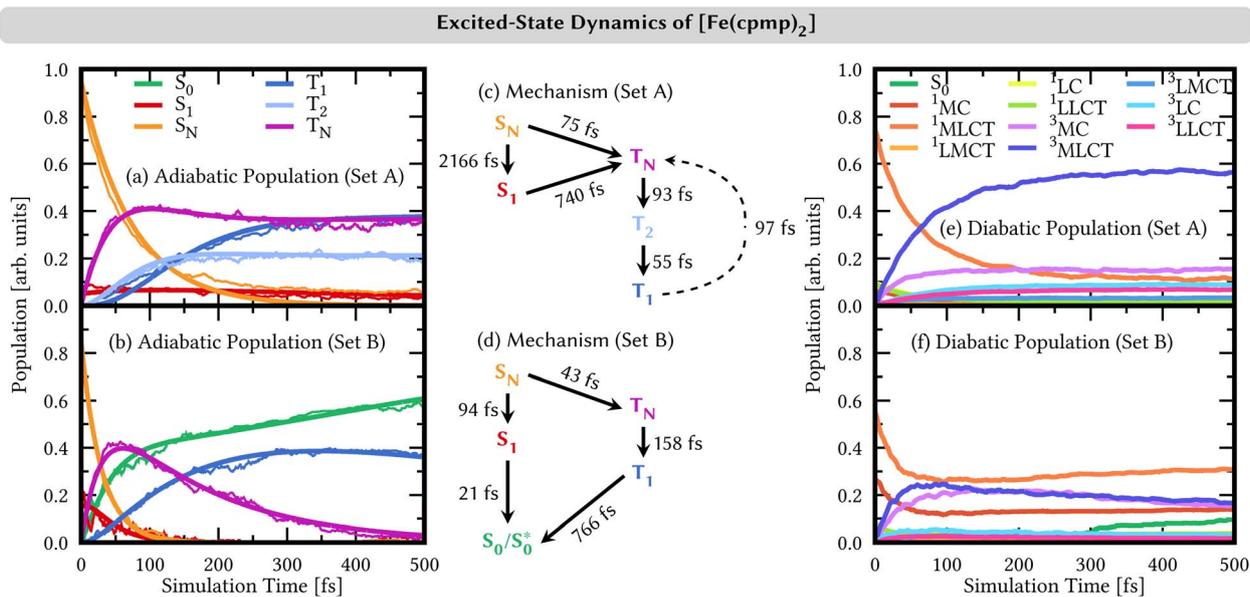


Fig. 7 (a and b) Time evolution of adiabatic electronic state populations (thin lines) and fits based on the mechanisms shown in (c/d) from linear-vibronic coupling/surface hopping (LVC/SH) dynamics simulations. Higher-lying singlet states  $S_N$  are combined into one line for  $N \geq 2$  and higher-lying triplet  $T_N$  into one line for  $N \geq 3$  (set A) and  $N \geq 2$  (set B). (c and d) Mechanisms of the nonadiabatic dynamics in the basis of adiabatic electronic states. (e and f) Time evolution of diabatic electronic state populations based on a transition-density matrix analysis.

## 4.2 Character of the electronic states

The two sets of range-separation parameters lead to qualitatively different relaxation mechanisms; see Fig. 7(c and d) and also Section S4.2† for a more-detailed derivation of the mechanism. Most notably, set A leads to the population of long-lived triplet states stable within our simulation window, while set B leads to deactivation to the ground-state  $S_0$  via both the singlet and the triplet manifolds. In order to understand the different excited-state behaviors, we analyzed the character of the electronic states involved in the dynamics in a diabatic representation using the transition-density matrix analysis of the electronic states in the Franck–Condon geometry as a reference. The corresponding time evolution of the diabatic state populations is shown in Fig. 7(e and f). Using set A, the initially excited states are mainly (74%) of  $^1\text{MLCT}$  character (orange curve in Fig. 7(e)). The remaining character is evenly distributed over the other singlet excitation characters, *i.e.*,  $^1\text{MC}$ ,  $^1\text{LMCT}$  (ligand-to-metal charge transfer),  $^1\text{LC}$  (ligand-centered), and  $^1\text{LLCT}$  (ligand-to-ligand charge-transfer). In the adiabatic representation, we observed an ultrafast intersystem crossing into the triplet manifold. This analysis in the diabatic representation reveals that the populated triplet states are of predominant  $^3\text{MLCT}$  character (dark blue curve) of up to 55% after 500 fs. The second largest contribution to the triplet states is given by  $^3\text{MC}$  configurations (violet curve) with 15% after 500 fs. The admixture of  $^3\text{MLCT}$  and  $^3\text{MC}$  characters in the diabatic state population is due to state mixing rather than the system traversing two different pathways, as is discussed in Section S4.4 in the ESI†.

The time evolution of the diabatic state populations of the dynamics using the range-separation parameters of set B is

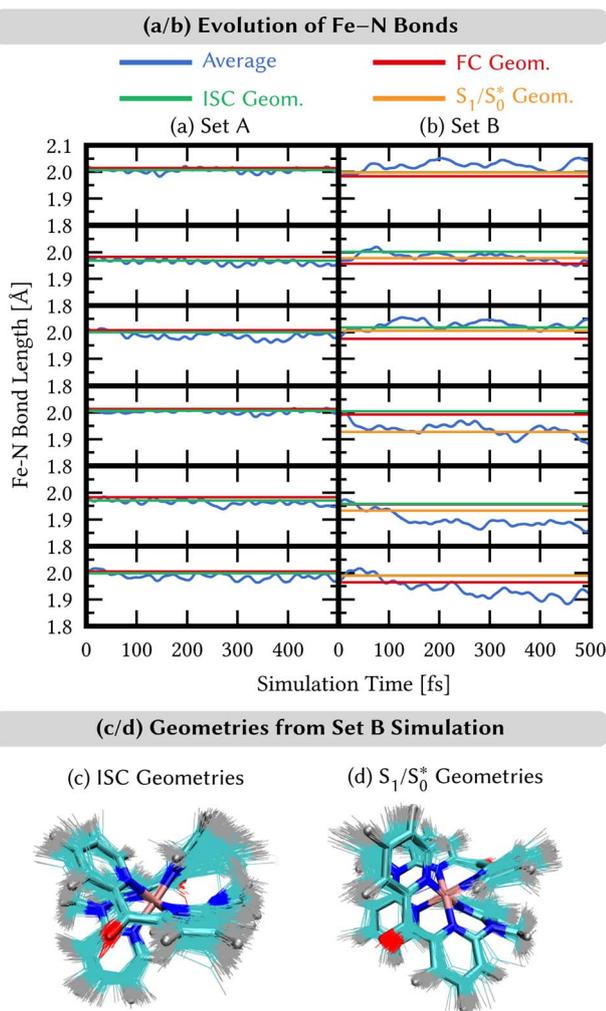
shown in Fig. 7(f). As can be seen, in addition to the initial  $^1\text{MLCT}$  character (orange curve, 55%), there is already a substantial portion of  $^1\text{MC}$  character (red curve, 25%) in the electronic state wave functions of the trajectories. Both characters decrease by about half their initial amounts, and contribution is transferred with almost equal shares to states of  $^3\text{MLCT}$  (dark blue) and  $^3\text{MC}$  (violet) characters. The triplet characters reach a maximum after *ca.* 100 fs. At later simulation times, the  $^3\text{MLCT}$  and  $^3\text{MC}$  characters in the population slowly decrease again, while  $^1\text{MLCT}$  and  $^1\text{MC}$  characters rise. After 300 fs, a notable increase in the diabatic  $S_0$  character (green curve) is visible.

The initial population and subsequent depopulation of diabatic  $^3\text{MLCT}$  and  $^3\text{MC}$  states mirror the ultrafast  $S_N$  to  $T_N$  intersystem crossing and  $T_N$  to  $S_0$  back-intersystem crossing established for the adiabatic electronic states in Fig. 7(d). Interestingly, the population of the diabatic  $S_0$  population is much smaller than the adiabatic  $S_0$  population – compare Fig. 7(b) and (f). These states are defined in different manners, and thus, their populations may differ. The adiabatic  $S_0$  state collects all states that are the lowest-energy singlet state in their respective geometry. In contrast, the diabatic  $S_0$  state refers to the singlet state with the exact electronic character as the adiabatic  $S_0$  at the Franck–Condon geometry, and the diabatic  $S_0$  populations collect their components in the trajectories during the dynamics. The difference between the adiabatic and diabatic  $S_0$  populations can be understood by investigating the behavior of the trajectories undergoing deactivation within the singlet manifold (Section S4.6)†.

## 4.3 Nuclear motion

We analyze here the nuclear motion during the nonadiabatic dynamics simulations, focusing on the motion involving the





**Fig. 8** (a and b) Time evolution of the average distances Fe–N between the central iron and the ligating nitrogen atoms from SH/LVC trajectories (blue curves) compared to the distances in the Franck–Condon (FC) geometry (red lines), distances in the ISC hopping geometries (green lines), and distances in the  $S_1/S_0^*$  geometries (orange curves, only set B). Green lines in the top and bottom panels in (b) are hidden behind the orange lines. (c and d) Superposition of geometries (thin bonds) from the ISC hopping points (c) and  $S_1/S_0^*$  geometries (d) on top of the Franck–Condon geometry (thick bonds).

central iron atom and the directly coordinating ligand atoms. The evolution of the six different Fe–N bond lengths during the dynamics is displayed in Fig. 8a and b (blue curves), along with the reference bond length in the Franck–Condon geometry (red line). For set A, the average Fe–N bond length stays close to the reference values in the Franck–Condon geometry (Fig. 8(a)). This behaviour is a direct consequence of the  $^3\text{MLCT}$  electronic states that control this simulation. These states involve an excitation from a non-bonding  $t_{2g}$  orbital of the  $d^6$  iron configuration to the  $\pi$  system of the organic ligands, leaving the bonding between the iron center and its ligating nitrogen atoms unaffected. In addition, Fig. 8(a) shows the average Fe–N bond distances in the geometries where intersystem crossing occurs (green line). As can be seen, also during intersystem crossing, the Fe–N bond lengths remain nearly constant.

By contrast, in the simulation using set B, large displacements of the average Fe–N bond lengths along the trajectories are visible with respect to their Franck–Condon reference (Fig. 8(b)). This observation is the result of populating  $^1\text{MC}$  and  $^3\text{MC}$  states. The MC states of closed-shell iron(II) compounds involve the excitation of an electron from a non-bonding  $t_{2g}$  orbital to an antibonding  $e_g^*$  orbital, which directly affects the metal–ligand bond lengths. The changes in the Fe–N bond lengths are up to 0.10–0.15 Å, a typical value for hexaaqua iron(II) compounds.<sup>67</sup> Additionally, also during the intersystem crossing, some Fe–N bonds display pronounced differences of up to 0.05 Å compared to the Franck–Condon values. These differences are likely due to the admixture of MC character to the set B trajectories (recall Fig. 7(f)). In general, there is substantial motion required to reach intersystem crossing geometries as is shown by the superposition of all intersystem crossing geometries of the set B simulation in Fig. 8(c).

Finally, for set B, we also show the average Fe–N bond lengths of the geometries, where  $S_1/S_0^*$  transitions occur (orange lines) in Fig. 8(b). The average Fe–N distances differ to a similar extent to the values at the intersystem crossing geometries from their Franck–Condon references. The large variation in the geometries in this set is also displayed as a superposition of structures in Fig. 8(d). This highlights the large extent of the region on the potential energy surface, where polyatomic molecules can undergo transitions between electronic states. Note that no average Fe–N bond lengths are shown for the set A simulations in Fig. 8(a), as the corresponding dynamics did not exhibit any  $S_1/S_0^*$  transitions. This absence is a direct result of the different shapes of the potential energy curves obtained with the different range-separation parameters (Fig. 6).

#### 4.4 Relaxation mechanisms

As we have seen, the two sets of parameters lead to two different relaxation mechanisms, intimately connected to the character of the lowest-excited states originating from the different range-separation parameters. Using set A produces low-lying  $^3\text{MLCT}$  states, which leads to long-lived triplet states, while set B leads to dynamics dominated by re-population of a hot  $S_0^*$  state through the singlet manifold as well as the diabatic  $S_0$  state *via* the triplet manifold, both *via* states involving MC character. The obvious question now is which of the two models describes the behavior of  $[\text{Fe}(\text{cpmp})_2]^{2+}$  correctly? In order to solve this problem, we leverage transient absorption spectroscopy (TAS).

Our recorded TA spectra (see Section S6†) reveal a single monoexponential decay of the ground-state bleach and, thus, the recovery of the ground state with a time constant of  $\tau_A = 550$  ps. A similar long-lived signal with  $\tau_3 = 472$  ps is observed in related TAS experiments of  $[\text{Fe}(\text{cpmp})_2]^{2+}$  in ref. 34. Those experiments<sup>34</sup> report two additional time constants for the excited-state decay, *i.e.*,  $\tau_1 < 200$  fs and  $\tau_2 = 30 - 40$  ps. The ultrafast  $\tau_1$  could, in principle, also contribute to the TA signal in our experiments, which have a time resolution of *ca.* 100 fs. However, due to a limited signal-to-noise ratio in our experiments, a weak sub-200 fs component might not be



resolved, in particular, since it is most clearly seen in the near-infrared region, which is outside the detection range of our setup. In ref. 34, the  $\tau_1$  component is associated with small spectral changes and ascribed to the lifetime of the  $^3\text{MLCT}$  state due to the decay into MC states. Note that it was not possible to spectroscopically differentiate between triplet and quintet MC states. The longer time-scale process described by  $\tau_2$  associated with the near-infrared region in ref. 34 is outside of the present detection range. It is ascribed to cooling and solvent reorganization processes when the system is already in MC states. Finally, ref. 34 ascribes the long-lived signal to the lifetime of the lowest-energy MC state, which is in line with our transient absorption spectra (see Section S6†).

At first glance, the experimental time constants appear to agree with the results based on set A, where ultrafast intersystem crossing from the initially excited singlet states and subsequent internal conversion populate  $T_1$  states of predominant  $^3\text{MLCT}$  character on a  $\sim 200$  fs time scale. The  $T_1/^3\text{MLCT}$  state is then stable on our ps simulation time. This result is seemingly in line with the TAS observation, which shows that the electronic ground state is repopulated within only a 500 ps time scale. However, the rapid disappearance of the MLCT signal in ref. 34 suggests that the long-lived state cannot be of MLCT nature, and, thus has to be an MC state. This finding contradicts the results of the set A simulation.

The set B simulations also predict fast initial dynamics involving intersystem crossing as well as relaxation dynamics within the singlet manifold that can account for the  $\tau_1$  component. Notably, the simulations of set B feature more pronounced MC character in the low-lying populated electronic states. While the set B simulation shows relaxation to the lowest-energetic state on a picosecond time scale, this process does not correspond to the full deactivation of the system. Instead, in the singlet pathway, a hot  $S_0^*$  state is populated that still shares the character of excited singlet states. Furthermore, this state stays close in energy to other excited states. Similar behavior is observed for trajectories relaxing *via* the triplet manifold. At this point, one may wonder about the role that quintet states play in the excited-state dynamics. Unfortunately, it is not possible to include quintet states in surface hopping studies with the presently used setup, as quintet states are not accessible from singlet ground states using linear-response TDDFT and, furthermore, spin-orbit couplings involving quintet states for TDDFT have also not been implemented yet. Because of the behavior described above, trajectories in either singlet or triplet states which remain for extended times in regions of a high density of electronic states could traverse to the quintet manifold and end up in low-lying  $^5\text{MC}$  states. Such states are the lowest-lying excited states, as shown in ref. 34, and they have been assigned to the experimentally observed long-lived signal.

Thus, we conclude that set B represents the best choice to simulate the dynamics of  $[\text{Fe}(\text{cpmp})_2]^{2+}$ . While it did not represent the optimal choice from the  $\Delta\text{SCF}$  tuning (set A), the range-separation parameters from set B also fall in the minimal valley in  $\Delta\text{SCF}$  tuning, thus indicating that it is a good parameter choice from an *ab initio* point of view. Furthermore, set B could

give good agreement with the experimental absorption spectrum. More importantly, however, set B provided the only range-separation parameters that predicted the lowest-energy states in the same order as multi-reference CASPT2 calculations.

The mechanism of set B simulations of relaxing *via*  $^3\text{MC}$  and possibly  $^5\text{MC}$  states shows that inserting a bridge between neighboring pyridyl units does not change the deactivation processes found for iron(II)polypyridyl complexes.<sup>68–75</sup> Thus, the introduction of push-pull ligands results only in a small increase of ligand-field splitting. Ligand-field splitting large enough to destabilize the MC states to the extent that long-lived  $^3\text{MLCT}$  states can be populated seems to require strong- $\sigma$  donating ligands such as NHCs.<sup>72,76–80</sup> The  $[\text{Fe}(\text{cpmp})_2]^{2+}$  complex falls into the line of  $[\text{Fe}(\text{dcpp})(\text{ddpd})]^{2+}$ ,  $[\text{Fe}(\text{dcpp})_2]^{2+}$  and  $[\text{Fe}(\text{ddpd})_2]^{2+}$  complexes,<sup>81</sup> where dcpp and ddpd are electron-withdrawing and electron-donating tri-pyridyl ligands bridged with two CO or NMe units, respectively. Among these complexes,  $[\text{Fe}(\text{dcpp})(\text{ddpd})]^{2+}$  and  $[\text{Fe}(\text{dcpp})_2]^{2+}$  also showed relaxation to the  $^5\text{MC}$  states after photoexcitation. In contrast, whereas in  $[\text{Fe}(\text{ddpd})_2]^{2+}$   $^3\text{MC}$  states were populated, no sign of further dynamics into the quintet manifold was seen experimentally.<sup>81</sup>  $[\text{Fe}(\text{cpmp})_2]^{2+}$  thereby behaves more similar to  $[\text{Fe}(\text{dcpp})(\text{ddpd})]^{2+}$  and  $[\text{Fe}(\text{dcpp})_2]^{2+}$ , which also feature a CO-bridged dcpp ligand, than to the  $[\text{Fe}(\text{ddpd})_2]^{2+}$  complex featuring NMe-bridged ligands. Thus, one can conclude that a more promising design concept to increase ligand-field splitting in pyridyl-iron(II) complexes is to introduce only electron-donating ligands (ddpd) rather than electron-withdrawing ligands (dcpp) or combinations that establish push-pull systems (cpmp or dcpp + ddpd).

## 5 Conclusions and outlook

The theoretical study of the photodynamics of transition-metal complexes is an intricate task. In particular, complexes bearing organic ligands with extended  $\pi$ -systems feature electronic states of very different nature, such as MC and MLCT states, that can be both accessible during excited-state dynamics simulations and need a reliable prediction. This complexity applies not only to their relative energies, but importantly also to their electronic character that ultimately controls the excited-state dynamics.

Here, we assessed the performance of optimally tuned range-separated DFT for a prototypical iron compound,  $[\text{Fe}(\text{cpmp})_2]^{2+}$  that, having push-pull ligands, exhibits an increased lifetime of the MLCT states compared to simple iron polypyridyl complexes such as  $[\text{Fe}(\text{bpy})_3]^{2+}$ . We systematically employed different tuning schemes, including “classical” ground-state fundamental gap tuning, ionization potential tuning in the triplet and quintet excited states, electron affinity tuning targeting metal-localized  $\sigma^*$  orbitals, and the so-called triplet tuning. We found that the range-separation parameters strongly influence vertical and adiabatic excitation energies and, importantly, also the nature of the lowest excited states. Thus, an unambiguous choice of the tuning parameters for such molecules is not straightforward.



Aided by comparison with the experimental absorption spectra and CASPT2 calculations, we found two suitable sets of range-separation parameters that were subsequently used for excited-state dynamics simulations. Using the set of optimal parameters from the  $\Delta$ SCF method (set A) for dynamics simulations results in the population of  $^3$ MLCT states that are stable within our 2 ps simulation time. This result is in contrast to TAS experiments,<sup>34</sup> which show the depopulation of MLCT states within 200 fs. Using the set which is in agreement with multi-reference CASPT2 calculations (set B) leads to relaxation processes within both the singlet and triplet manifolds. The participating electronic states in this deactivation mechanism show pronounced MC character. Throughout the deactivation – and even upon reaching the hot  $S_0^*$  state – the system stays in regions of a high density of states, suggesting the possibility for further transfer into quintet states. We thus conclude that only set B, in agreement with multi-reference calculations, can describe the electronic states of  $[\text{Fe}(\text{cpmp})_2]^{2+}$  well.

In summary, we illustrate the intricacies of choosing a suitable DFT computational protocol to model the photodynamics of a transition metal complex. Optimal tuning of a range-separated DFT functional is not a black-box method,<sup>30</sup> and the nature of the involved states is unpredictable. The large difference in the predicted photodynamics resulting from the different range-separation parameters can be ascribed to the different response of MC vs. MLCT states with changing the portion of exact-exchange in the short range. The local  $\sigma$ -orbitals are more suspected to the self-interaction error than delocalized  $\pi$ -orbitals and, thus, the inclusion of a certain portion of global exact exchange leads to a better mitigation of self-interaction error.<sup>27,64,64</sup> This observation hints towards the importance of a balanced approach. Testing the performance of range-separation parameters for describing the excited states of transition-metal complexes only for the properties of the (bright) MLCT states, *e.g.*, by solely considering absorption spectra, will overlook the influence of (dark) MC states, that can drive the outcome of photodynamics as we observed for  $[\text{Fe}(\text{cpmp})_2]^{2+}$ . In general, the combination of experimental absorption spectra and photorelaxation timescales, multi-reference calculations, and nonadiabatic dynamics simulations allowed the identification of a suitable set of tuning parameters. Fortunately, such all-encompassing endeavors are possible nowadays, as time-resolved spectroscopic experiments have become main-stream characterization techniques of transition-metal complexes and nonadiabatic dynamics methods have evolved to be computationally feasible.

## Data availability

The parameter for the linear vibronic coupling used in the dynamics simulations are given in the ESL.<sup>†</sup> All other data is available from the corresponding authors upon reasonable request.

## Author contributions

LG, SIB, and OK conceived the research and acquired funding. OSB performed all optimal-tuning calculations, JPZ and OB

performed current and preliminary dynamics simulations, and AK recorded the transient-absorption spectra. OSB, JPZ, and SIB wrote the manuscript. All authors reviewed and edited the paper.

## Conflicts of interest

There are no conflicts to declare.

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## Notes and references

- 1 C. Stephenson and T. Yoon, *Acc. Chem. Res.*, 2016, **49**, 2059–2060.
- 2 V. Venkatraman, R. Raju, S. P. Oikonomopoulos and B. K. Alsberg, *J. Cheminf.*, 2018, **10**, 18.
- 3 R. D. Costa, E. Ortí, H. J. Bolink, F. Monti, G. Accorsi and N. Armaroli, *Angew. Chem., Int. Ed.*, 2012, **51**, 8178–8211.
- 4 H. Junge, N. Rockstroh, S. Fischer, A. Brückner, R. Ludwig, S. Lochbrunner, O. Kühn and M. Beller, *Inorganics*, 2017, **5**, 14.
- 5 O. S. Wenger, *Chem.–Eur. J.*, 2019, **25**, 6043–6052.
- 6 G. Vankó, A. Bordage, M. Pápai, K. Haldrup, P. Glatzel, A. M. March, G. Doumy, A. Britz, A. Galler, T. Assefa, D. Cabaret, A. Juhin, T. B. van Driel, K. S. Kjær, A. Dohn, K. B. Møller, H. T. Lemke, E. Gallo, M. Rovezzi, Z. Németh, E. Rozsályi, T. Rozgonyi, J. Uhlig, V. Sundström, M. M. Nielsen, L. Young, S. H. Southworth, C. Bressler and W. Gawelda, *J. Phys. Chem. C*, 2015, **119**, 5888–5902.
- 7 C. Bressler, C. Milne, V.-T. Pham, A. ElNahas, R. M. van der Veen, W. Gawelda, S. Johnson, P. Beaud, D. Grolimund, M. Kaiser, C. N. Borca, G. Ingold, R. Abela and M. Chergui, *Science*, 2009, **323**, 489–492.
- 8 I. M. Dixon, G. Boissard, H. Whyte, F. Alary and J.-L. Heully, *Inorg. Chem.*, 2016, **55**, 5089–5091.
- 9 D. C. Ashley and E. Jakubikova, *Coord. Chem. Rev.*, 2017, **337**, 97–111.
- 10 P. Chábera, L. Lindh, N. W. Rosemann, O. Prakash, J. Uhlig, A. Yartsev, K. Wärnmark, V. Sundström and P. Persson, *Coord. Chem. Rev.*, 2021, **426**, 213517.
- 11 J. P. Zobel and L. González, *JACS Au*, 2021, **1**, 1116–1140.
- 12 *Quantum Chemistry and Dynamics of Excited States: Methods and Applications*, ed. L. González and R. Lindh, John Wiley & Sons, 2021.
- 13 R. Crespo-Otero and M. Barbatti, *Chem. Rev.*, 2018, **118**, 7026–7068.
- 14 A. D. Laurent and D. Jacquemin, *Int. J. Quantum Chem.*, 2013, **113**, 2019–2039.
- 15 A. Dreuw and M. Head-Gordon, *Chem. Rev.*, 2005, **105**, 4009–4037.



- 16 M. J. G. Peach, P. Benfield, T. Helgaker and D. J. Tozer, *J. Chem. Phys.*, 2008, **128**, 44118.
- 17 A. Savin, in *Theoretical and Computational Chemistry*, Elsevier, 1996, vol. 4, pp. 327–357.
- 18 H. Iikura, T. Tsuneda, T. Yanai and K. Hirao, *J. Chem. Phys.*, 2001, **115**, 3540–3544.
- 19 R. Baer, E. Livshits and U. Salzner, *Annu. Rev. Phys. Chem.*, 2010, **61**, 85–109.
- 20 P. Mori-Sánchez, A. J. Cohen and W. Yang, *Phys. Rev. Lett.*, 2008, **100**, 146401.
- 21 E. Livshits and R. Baer, *Phys. Chem. Chem. Phys.*, 2007, **9**, 2932–2941.
- 22 J. Autschbach and M. Srebro, *Acc. Chem. Res.*, 2014, **47**, 2592–2602.
- 23 S. Refaely-Abramson, R. Baer and L. Kronik, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2011, **84**, 075144.
- 24 M. P. Borpuzari and R. Kar, *J. Comput. Chem.*, 2017, **38**, 2258–2267.
- 25 T. Möhle, O. S. Bokareva, G. Grell, O. Kühn and S. I. Bokarev, *J. Chem. Theory Comput.*, 2018, **14**, 5870–5880.
- 26 K. Hirao, H.-S. Bae, J.-W. Song and B. Chan, *J. Phys. Chem. A*, 2021, **125**, 3489–3502.
- 27 S. Refaely-Abramson, S. Sharifzadeh, N. Govind, J. Autschbach, J. B. Neaton, R. Baer and L. Kronik, *Phys. Rev. Lett.*, 2012, **109**, 226405.
- 28 T. Körzdörfer, J. S. Sears, C. Sutton and J.-L. Brédas, *J. Chem. Phys.*, 2011, **135**, 204107.
- 29 D. A. Egger, S. Weissman, S. Refaely-Abramson, S. Sharifzadeh, M. Dauth, R. Baer, S. Kümmel, J. B. Neaton, E. Zojer and L. Kronik, *J. Chem. Theory Comput.*, 2014, **10**, 1934–1952.
- 30 A. Karolewski, L. Kronik and S. Kümmel, *J. Chem. Phys.*, 2013, **138**, 204115.
- 31 A. Ramasubramaniam, D. Wing and L. Kronik, *Phys. Rev. Mater.*, 2019, **3**, 084007.
- 32 M. Brütting, H. Bahmann and S. Kümmel, *J. Chem. Phys.*, 2022, **156**, 104109.
- 33 J. Moll, C. Wang, A. Pöpcke, C. Förster, U. Resch-Genger, S. Lochbrunner and K. Heinze, *Chem.–Eur. J.*, 2020, **26**, 6820–6832.
- 34 J. Moll, R. Naumann, L. Sorge, C. Förster, N. Gessner, L. Burkhardt, N. Ugur, W. Nürnberger, P. Seidel, C. Ramanan, M. Bauer and K. Heinze, *Chem.–Eur. J.*, 2022, **28**, e20221858.
- 35 O. S. Wenger, *Chem.–Eur. J.*, 2019, **25**, 6043–6052.
- 36 A. K. C. Mengel, C. Förster, A. Breivogel, K. Mack, J. R. Ochsmann, F. Laquai, V. Ksenofontov and K. Heinze, *Chem.–Eur. J.*, 2015, **21**, 704–714.
- 37 A. K. C. Mengel, C. Bissinger, M. Dorn, O. Back, C. Förster and K. Heinze, *Chem.–Eur. J.*, 2017, **23**, 7920–7931.
- 38 A. Britz, W. Gawelda, T. A. Assefa, L. L. Jamula, J. T. Yarranton, A. Galler, D. Khakhulin, M. Diez, M. Harder, G. Doumy, A. M. March, E. Bajnóczi, Z. Németh, M. Pápai, E. Rozsályi, D. Sárosiné Szemes, H. Cho, S. Mukherjee, C. Liu, T. K. Kim, R. W. Schoenlein, S. H. Southworth, L. Young, E. Jakubikova, N. Huse, G. Vankó, C. Bressler and J. K. McCusker, *Inorg. Chem.*, 2019, **58**, 9341–9350.
- 39 J. Moll, C. Förster, A. König, L. M. Carrella, M. Wagner, M. Panthöfer, A. Möller, E. Rentschler and K. Heinze, *Inorg. Chem.*, 2022, **61**, 1659–1671.
- 40 L. L. Jamula, A. M. Brown, D. Guo and J. K. McCusker, *Inorg. Chem.*, 2014, **53**, 15–17.
- 41 T. Stein, L. Kronik and R. Baer, *J. Am. Chem. Soc.*, 2009, **131**, 2818–2820.
- 42 T. Stein, L. Kronik and R. Baer, *J. Chem. Phys.*, 2009, **131**, 244119.
- 43 G. A. Petersson, A. Bennett, T. G. Tensfeldt, M. A. Al-Laham, W. A. Shirley and J. Mantzaris, *J. Chem. Phys.*, 1988, **89**, 2193–2218.
- 44 G. A. Petersson and M. A. Al-Laham, *J. Chem. Phys.*, 1991, **94**, 6081–6090.
- 45 A. D. Becke, *J. Chem. Phys.*, 1993, **98**, 5648–5652.
- 46 F. Weigend and R. Ahlrichs, *Phys. Chem. Chem. Phys.*, 2005, **7**, 3297.
- 47 F. Weigend, *Phys. Chem. Chem. Phys.*, 2006, **8**, 1057.
- 48 S. I. Bokarev, O. S. Bokareva and O. Kühn, *J. Chem. Phys.*, 2012, **136**, 214305.
- 49 O. S. Bokareva, G. Grell, S. I. Bokarev and O. Kühn, *J. Chem. Theory Comput.*, 2015, **11**, 1700–1709.
- 50 S. I. Bokarev, O. S. Bokareva and O. Kühn, *Coord. Chem. Rev.*, 2015, **304–305**, 133–145.
- 51 S. Fischer, O. S. Bokareva, E. Barsch, S. I. Bokarev, O. Kühn and R. Ludwig, *ChemCatChem*, 2016, **8**, 404–411.
- 52 O. Bokareva, T. Möhle, A. Neubauer, S. Bokarev, S. Lochbrunner and O. Kühn, *Inorganics*, 2017, **5**, 23.
- 53 A. Friedrich, O. S. Bokareva, S.-P. Luo, H. Junge, M. Beller, O. Kühn and S. Lochbrunner, *Chem. Phys.*, 2018, **515**, 557–563.
- 54 G. Prokopiou and L. Kronik, *Chem.–Eur. J.*, 2017, 5173–5182.
- 55 Z. Lin and T. Van Voorhis, *J. Chem. Theory Comput.*, 2019, **15**, 1226–1241.
- 56 O. S. Bokareva, O. Baig, M. J. Al-Marri, O. Kühn and L. González, *Phys. Chem. Chem. Phys.*, 2020, **22**, 27605–27616.
- 57 P. Dierks, A. Pöpcke, O. S. Bokareva, B. Altenburger, T. Reuter, K. Heinze, O. Kühn, S. Lochbrunner and M. Bauer, *Inorg. Chem.*, 2020, **59**, 14746–14761.
- 58 J. P. Zobel, O. S. Bokareva, P. Zimmer, C. Wölper, M. Bauer and L. González, *Inorg. Chem.*, 2020, **59**, 14666–14678.
- 59 J. P. Perdew, R. G. Parr, M. Levy and J. L. Balduz, *Phys. Rev. Lett.*, 1982, **49**, 1691–1694.
- 60 M. Dauth, F. Caruso, S. Kümmel and P. Rinke, *Phys. Rev. B*, 2016, **93**, 121115.
- 61 L. Kronik and S. Kümmel, *Phys. Chem. Chem. Phys.*, 2020, **22**, 16467–16481.
- 62 G. Ghigo, B. O. Roos and P.-Å. Malmqvist, *Chem. Phys. Lett.*, 2004, **396**, 142–149.
- 63 J. P. Zobel, J. J. Nogueira and L. González, *Chem. Sci.*, 2017, **8**, 1482–1499.
- 64 F. Rissner, D. A. Egger, A. Natan, T. Körzdörfer, S. Kümmel, L. Kronik and E. Zojer, *J. Am. Chem. Soc.*, 2011, **133**, 18634–18645.



- 65 F. Plasser, S. Gómez, M. F. S. J. Menger, S. Mai and L. González, *Phys. Chem. Chem. Phys.*, 2019, **21**, 57–69.
- 66 J. P. Zobel, M. Heindl, F. Plasser, S. Mai and L. González, *Acc. Chem. Res.*, 2021, **54**, 3760–3771.
- 67 A. Cannizzo, C. J. Milne, C. Consani, W. Gawelda, C. Bressler, F. van Mourik and M. Chergui, *Coord. Chem. Rev.*, 2010, **254**, 2677–2686.
- 68 A. Moguilevski, M. Wilke, G. Grell, S. I. Bokarev, S. G. Aziz, N. Engel, A. A. Raheem, O. Kühn, I. Y. Kiyani and E. F. Aziz, *ChemPhysChem*, 2017, **18**, 465–469.
- 69 W. Zhang, R. Alonso-Mori, U. Bergmann, C. Bressler, M. Chollet, A. Galler, W. Gawelda, R. G. Hadt, R. W. Hartsock, T. Kroll, K. S. Kjær, K. Kubiček, H. T. Lemke, H. W. Liang, D. A. Meyer, M. M. Nielsen, C. Purser, J. S. Robinson, E. I. Solomon, Z. Sun, D. Sokaras, T. B. van Driel, G. Vankó, T.-C. Weng, D. Zhu and K. J. Gaffney, *Nature*, 2014, **509**, 345–348.
- 70 S. G. Shepard, S. M. Fatur, A. K. Rappé and N. H. Damrauer, *J. Am. Chem. Soc.*, 2016, **138**, 2949–2952.
- 71 M. C. Carey, S. L. Adelman and J. K. McCusker, *Chem. Sci.*, 2019, **10**, 134–144.
- 72 T. Duchanois, T. Etienne, C. Cebrián, L. Liu, A. Monari, M. Beley, X. Assfeld, S. Haacke and P. C. Gros, *Eur. J. Inorg. Chem.*, 2015, 2469–2477.
- 73 D. Leshchev, T. Harlang, L. A. Fredin, D. Khakhulin, Y. Liu, E. Biasin, M. G. Laursen, G. E. Newby, K. Haldrup, M. M. Nielsen, K. Wärnmark, V. Sundström, P. Persson, K. S. Kjær and M. Wulff, *Chem. Sci.*, 2018, **9**, 405–414.
- 74 G. Vankó, A. Bordage, M. Pápai, K. Haldrup, P. Glatzel, A. M. March, G. Doumy, A. Britz, A. Galler, T. Assefa, D. Cabaret, A. Juhin, T. B. van Driel, K. S. Kjær, A. Dohn, K. B. Møller, H. T. Lemke, E. Gallo, M. Rovezzi, Z. Németh, E. Rozsályi, T. Rozgonyi, J. Uhlig, V. Sundström, M. M. Nielsen, L. Young, S. H. Southworth, C. Bressler and W. Gawelda, *J. Phys. Chem. C*, 2015, **119**, 5888–5902.
- 75 S. M. Fatur, S. G. Shepard, R. F. Higgins, M. P. Shores and N. H. Damrauer, *J. Am. Chem. Soc.*, 2017, **139**, 4493–4505.
- 76 L. Liu, T. Duchanois, T. Etienne, A. Monari, M. Beley, X. Assfeld, S. Haacke and P. C. Gros, *Phys. Chem. Chem. Phys.*, 2016, **18**, 12550–12556.
- 77 L. A. Fredin, M. Pápai, E. Rozsályi, G. Vankó, K. Wärnmark, V. Sundström and P. Persson, *J. Phys. Chem. Lett.*, 2014, **5**, 2066–2071.
- 78 P. Chábera, K. S. Kjær, O. Prakash, A. Honarfar, Y. Liu, L. A. Fredin, T. C. B. Harlang, S. Lidin, J. Uhlig, V. Sundström, R. Lomoth, P. Persson and K. Wärnmark, *J. Phys. Chem. Lett.*, 2018, **9**, 459–463.
- 79 Y. Liu, K. S. Kjær, L. A. Fredin, P. Chábera, T. Harlang, S. E. Canton, S. Lidin, J. Zhang, R. Lomoth, K.-E. Bergquist, P. Persson, K. Wärnmark and V. Sundström, *Chem.–Eur. J.*, 2015, **21**, 3628–3639.
- 80 H. Tatsuno, K. S. Kjær, K. Kunnus, T. Harlang, C. Timm, M. Guo, P. Chábera, L. A. Fredin, R. W. Hartsock, M. E. Reinhard, S. Koroidov, L. Li, A. A. Cordones, O. Gordivska, O. Prakash, Y. Liu, M. G. Laursen, E. Biasin, F. B. Hansen, P. Vester, M. Christensen, K. Haldrup, Z. Németh, D. S. Szemes, E. Bajnóczi, G. Vankó, T. B. Van Driel, R. Alonso-Mori, J. M. Glowina, S. Nelson, M. Sikorski, H. T. Lemke, D. Sokaras, S. E. Canton, A. O. Dohn, K. B. Møller, M. M. Nielsen, K. J. Gaffney, K. Wärnmark, V. Sundström, P. Persson and J. Uhlig, *Angew. Chem., Int. Ed.*, 2020, **59**, 364–372.
- 81 A. K. C. Mengel, C. Förster, A. Breivogel, K. Mack, J. R. Ochsmann, F. Laquai, V. Ksenofontov and K. Heinze, *Chem.–Eur. J.*, 2015, **21**, 704–714.

