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# First-principles investigation on multi-magnesium sulfide and magnesium sulfide clusters in magnesium-sulfide batteries

Xiaoli Jiang, Jianbao Wu, \* Panyu Zhang, Liyuan Jiang, Shuhan Lu, Xinxin Zhao and ZhiXiang Yin

Because of the abundance of magnesium and sulfur and their low cost, the development of magnesium sulfur batteries is very promising. In particular, the battery performance of nanoscale  $(\text{MgS})_n$  clusters is much better than that of bulk sized MgS. However, the structures, stability, and properties of  $\text{Mg}_x\text{S}_y$  and  $(\text{MgS})_n$  clusters, which are very important to improve the performance of Mg–S batteries, are still unexplored. Herein, the most stable structures of  $\text{Mg}_x\text{S}_y$  ( $x = 1-8$ ,  $y = 1-8$ ) and  $(\text{MgS})_n$  ( $n = 1-10$ ) are reliably determined using the structure search method and density functional theory to calculate. According to calculation results,  $\text{MgS}_3$  and  $\text{Mg}_6\text{S}_8$  may not exist in the actual charging and discharging products of magnesium sulfide batteries. The  $(\text{MgS})_n$  ( $n \geq 5$ ) clusters exhibit intriguing cage-like structures, which are favorable for eliminating dangling bonds and enhancing structural stability. Compared to the MgS monomer, each sulfur atom in the clusters is coordinated with more magnesium atoms, thus lengthening the Mg–S bond length and decreasing the Mg–S bond activation energy. Notably, with the increase of dielectric constant of electrolyte solvent, compared to the DME ( $\epsilon = 7.2$ ), THF ( $\epsilon = 7.6$ ) and  $\text{C}_2\text{H}_4\text{Cl}_2$  ( $\epsilon = 10.0$ ),  $\text{Mg}_x\text{S}_y$  and  $(\text{MgS})_n$  clusters are most stable in the environment of  $\text{C}_3\text{H}_6\text{O}$  ( $\epsilon = 20.7$ ). It can delay the transformation of magnesium polysulfide to the final product MgS, which is conducive to improving the performance of Mg–S batteries. The predicted characteristic peaks of infrared and Raman spectra provide useful information for *in situ* experimental investigation. Our work represents a significant step towards understanding  $(\text{MgS})_n$  clusters and improving the performance of Mg–S batteries.

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## 1. Introduction

In modern society, rechargeable lithium-ion batteries and lithium-sulfur batteries are some of the most advanced electric energy storage technologies with high energy density, and have been widely used in many fields.<sup>1,2</sup> However, the application of large-scale energy storage of lithium batteries is limited by the small natural reserves of lithium, high production cost and safety issues. Magnesium, as the element on the diagonal line of lithium in the periodic table, has the characteristics of cheap price, no pollution to the environment and high safety.<sup>3,4</sup> In addition, magnesium ions also have a higher valence state than lithium ions, and magnesium sulfur batteries have a higher volume-theoretical capacity than lithium sulfur batteries (3833 vs. 2062 mA h  $\text{cm}^{-3}$ ).<sup>5-7</sup> The reserves of magnesium in Earth's crust are much higher than lithium (2.9% vs. 0.002%),<sup>8,9</sup> and magnesium and sulfur are easily obtained from by-products of a variety of minerals. Therefore, the combination of magnesium

and sulfur is also considered a promising electrochemical system.<sup>10,11</sup>

However, the development of magnesium sulfide batteries is still in the preliminary stage. One of the main obstacles is that during the discharge process, sulfur in the positive electrode and magnesium negative electrode form MgS solid on the magnesium surface,<sup>12</sup> resulting in the formation of a passivation layer on the surface of the magnesium negative electrode that is not conductive to the magnesium ion, which hinders the reversible deposition/dissolution of the magnesium ion.<sup>13-15</sup> Secondly, the compatibility between magnesium electrode and existing electrolyte is poor, many solvents and salts are easy to be reduced on the magnesium negative electrode.<sup>4,16</sup> Until now, the structure and electrochemical mechanism of polysulfide produced in the charge and discharge process of magnesium sulfide batteries have not been cleared. In 2014, Zhao *et al.*<sup>17</sup> proposed for the first time a three-step electrochemical reaction formula in magnesium sulfide battery based on the electrochemical performance of magnesium sulfide battery and XPS analysis of cathode. In the first step, solid elemental sulfur was converted into liquid  $\text{MgS}_8$ , which was dissolved in electrolyte and further transformed into  $\text{MgS}_4$  through electrochemical

School of Mathematics, Physics and Statistics, Shanghai University of Engineering Science, 333 Longteng Road, Shanghai 201620, China. E-mail: wujianbao@sues.edu.cn



reaction. The second step is a reduction from low order polysulfide magnesium such as  $\text{MgS}_4$  to  $\text{MgS}_2$ . In the final step,  $\text{MgS}_2$  is reduced to  $\text{MgS}$ . In 2019, Xu *et al.*<sup>18</sup> studied the evolution of chemical substances in the cathode of magnesium sulfide battery through *in situ* and non-*in situ* XAS experiments, measured the Mg : S ratio in  $\text{MgS}_x$  ( $x \geq 3$ ) through experiments, and then calculated by density functional theory (DFT) to obtain the polysulfide ( $\text{Mg}_x\text{S}_8$ ,  $x = 1, 2, 3$  and 8). They believe that finding a method to decompose inactive  $\text{MgS}$  and low polysulfides and promoting the conversion of  $\text{MgS}$  to low order  $\text{MgS}_x$  is the key to solve the problem of rapid capacity decline in magnesium sulfur batteries.<sup>19</sup>

To explore the structure and electrochemical mechanism of polysulfide in the charge and discharge process of magnesium sulfide batteries, activation of unreacted  $\text{MgS}$  by using electrolytes may be an important factor in improving the performance of Mg–S batteries, and the battery performance of nanoscale  $(\text{MgS})_n$  clusters may be much better than that of bulk sized  $\text{MgS}$ . However, until now, the structure, relative stability and electronic properties of  $(\text{MgS})_n$  clusters have not been determined. In addition, the growth pattern of  $(\text{MgS})_n$  clusters can provide necessary guidance for the design of larger clusters. This motivation drives us to conduct further theoretical calculations of  $(\text{MgS})_n$  ( $n \leq 10$ ) clusters. To obtain detailed bond length data and precise electronic properties, which are necessary prerequisites for optimizing its performance and understanding its discharge process. Few electrolytes are compatible with both Mg and  $\text{S}_8$ , and none are ideal. Organo-magnesium-based electrolytes, commonly used in Mg– $\text{Mo}_6\text{S}_8$  batteries, are likely too nucleophilic and will react with electrophilic  $\text{S}_8$ .<sup>20</sup> Efforts have therefore focused on the development of non-nucleophilic electrolytes. Understanding these fundamental questions is critical to addressing the obstacles to translating this promising electrochemical system into a useable technology.

In this article, the structure of magnesium polysulfide was predicted. The structure, stability and properties of  $(\text{MgS})_n$  clusters, which are very important for improving the performance of Mg–S batteries, are investigated. We also provided the structural evolution of magnesium sulfide in the discharge process. In addition, the calculation of infrared and Raman spectra provides the description of characteristic spectral lines for the three basic structural units of  $\text{MgS}$ ,  $\text{Mg}_2\text{S}$  and  $\text{Mg}_3\text{S}$ , and also provides useful information for experimental research. The solvation energy of magnesium polysulfide in electrolyte DME ( $\epsilon = 7.2$ ), THF ( $\epsilon = 7.6$ ),  $\text{C}_2\text{H}_4\text{Cl}_2$  ( $\epsilon = 10.0$ ) and  $\text{C}_3\text{H}_6\text{O}$  ( $\epsilon = 20.7$ ) was calculated. With the increase of dielectric constant, the solvent energy of magnesium polysulfide gradually decreases, indicating that magnesium polysulfide is more stable in the electrolyte environment with large dielectric constant. It can promote the transformation of long chain magnesium polysulfide to short chain magnesium polysulfide, and delay the transformation of magnesium polysulfide to the final product  $\text{MgS}$ , which is conducive to improving the performance of Mg–S batteries. The work in this paper provides a good mechanism and theoretical support for understanding  $(\text{MgS})_n$  clusters and improving the performance of Mg–S batteries.

## 2. Computational methods

In order to find the preferred structures of  $\text{Mg}_x\text{S}_y$  ( $x = 1-8, y = 1-8$ ) and  $(\text{MgS})_n$  clusters ( $n = 1-10$ ), we employed the swarm-intelligence based ABCluster structure prediction method,<sup>21,22</sup> which can efficiently search for the stable structures of given cluster sizes. Furthermore, a global search should be an effective method to avoid missing candidates of ground state structures. To improve the search efficiency, point group symmetry and the bond characterization matrix technique were included to eliminate similar structures. The validity of the ABCluster method in cluster structure prediction has been demonstrated by its application for a series of cluster systems.

The underlying local structure optimization and electronic property calculations were performed at the density functional theory (DFT) level using the B3LYP<sup>23</sup> hybrid functional as implemented in the Gaussian 09 package. Since there are thousands of structures generated during the structure search, an economic basis set, *i.e.* 6-311G for Mg and S, was chosen to optimize these structures. These settings are enough for evaluating the relative energies of the generated structures. After the structure search, the accurate basis set of 6-311+G(d) was used for the refined structure optimization and vibrational frequency calculation for the isomers with low-lying energies. The absence of an imaginary frequency confirms that the predicted structures are stability.

First, we calculated the binding energy per atom, the formation energies were defined as

$$E_b = (E_{\text{Mg}_x\text{S}_y} - xE_{\text{Mg}} - yE_{\text{S}})/(x + y) \quad (1)$$

where  $E_{\text{Mg}_x\text{S}_y}$  is the lowest energy of structure  $\text{Mg}_x\text{S}_y$ ,  $E_{\text{Mg}}$  and  $E_{\text{S}}$  are the energy of magnesium atom and sulfur atom respectively.

The solvent energy,  $\Delta E_b^{\text{solven}}$ , was computed to measure the interaction strength between  $\text{Mg}_x\text{S}_y$  and electrolytes, the formula is as follows:

$$\Delta E_b^{\text{solven}} = (E_{\text{Mg}_x\text{S}_y}^{\text{vacuum}} - E_{\text{Mg}_x\text{S}_y}^{\text{solven}})/(x + y) \quad (2)$$

In cluster physics,  $\Delta^2 E_n$ , which was calculated as follows

$$\Delta^2 E_n = E_{n+1} + E_{n-1} - 2E_n \quad (3)$$

The second-order energy difference is a sensitive physical quantity that reflects the relative stability of considered clusters and can also be directly compared with the experimental relative abundance.










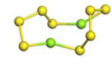
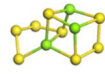
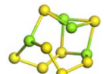
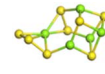
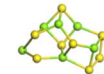
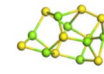
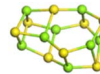
## 3. Results and discussion

### 3.1. Structural and thermal analysis of $\text{Mg}_x\text{S}_y$ and $(\text{MgS})_n$

The stability structures of  $\text{Mg}_x\text{S}_y$  molecule was determined by using the structure search method combined with density functional theory calculation and Gauss structure optimization.<sup>23</sup> As shown in Table 1, It can be seen that  $\text{MgS}_y$  is mainly plane chain structure and  $\text{Mg}_x\text{S}_8$  is mainly cross ring structure. This can improve structural stability. In order to verify whether intermediate products exist in actual charge and discharge, we calculated  $E_b$ , as shown in Fig. 1.



Table 1 Fully optimized structures of the  $Mg_xS_y$ 

$MgS_y$								
Length of Mg–S bond	MgS 2.16 Å	MgS <sub>2</sub> 2.26 Å	MgS <sub>3</sub> 2.45 Å	MgS <sub>4</sub> 2.46 Å	MgS <sub>5</sub> 2.34 Å	MgS <sub>6</sub> 2.32 Å	MgS <sub>7</sub> 2.36 Å	MgS <sub>8</sub> 2.38 Å
$Mg_xS_8$								
Length of Mg–S bond	MgS <sub>8</sub> 2.38 Å	Mg <sub>2</sub> S <sub>8</sub> 2.40 Å	Mg <sub>3</sub> S <sub>8</sub> 2.46 Å	Mg <sub>4</sub> S <sub>8</sub> 2.46 Å	Mg <sub>5</sub> S <sub>8</sub> 2.43 Å	Mg <sub>6</sub> S <sub>8</sub> 2.45 Å	Mg <sub>7</sub> S <sub>8</sub> 2.44 Å	Mg <sub>8</sub> S <sub>8</sub> 2.43 Å

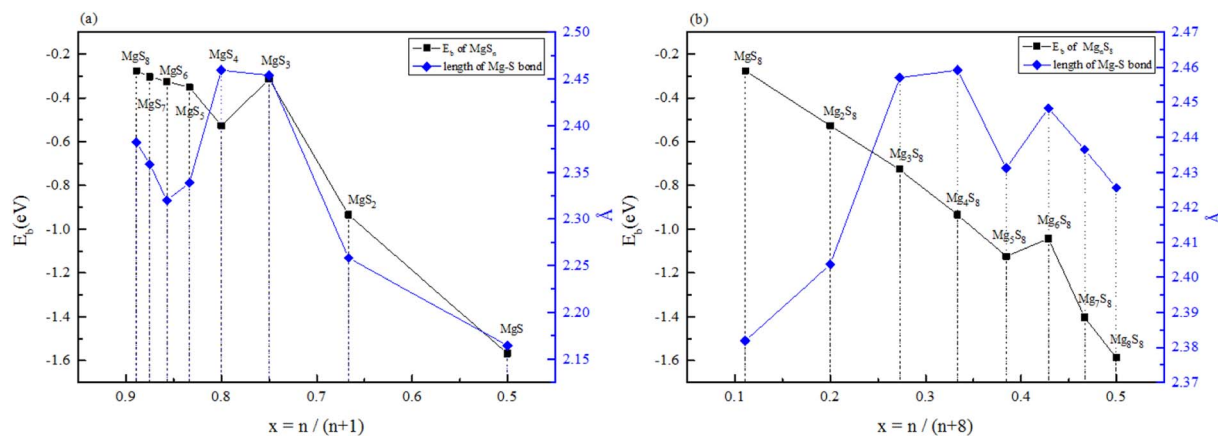
Fig. 1 (a) Binding energy and Mg–S bond length of  $MgS_y$ . (b) Binding energy and Mg–S bond length of  $Mg_xS_8$ .

Fig. 1(a) shows the binding energy and average Mg–S bond length of  $MgS_y$ . It can be seen that the binding energy of  $MgS_3$  is higher than that of  $MgS_2$  and  $MgS_4$ , this indicates that  $MgS_3$  may not exist in the actual charging and discharging products of magnesium sulfide batteries, and the trend of average bond length of magnesium sulfide is basically consistent with that of  $MgS_y$ . Fig. 1(b) shows the binding energy and average Mg–S bond length of  $Mg_xS_8$ . It can be seen that the binding energy of  $Mg_6S_8$  is higher than that of  $Mg_5S_8$  and  $Mg_7S_8$ , so  $Mg_6S_8$  may not exist in the actual charging and discharging products of magnesium sulfur batteries. It can be seen that with the increase of the number of magnesium atoms, the trend of Mg–S average bond length is in good agreement with the trend of binding energy of  $Mg_xS_8$ .

The structures of  $(MgS)_n$  clusters ( $n = 1-10$ ) are completely optimized under vacuum environment. Based on thermodynamic stability analysis, the formation of  $(MgS)_n$  clusters are favorable. The lowest energy structure of  $(MgS)_n$  clusters determined by DFT structure optimization is shown in Fig. 2. An example of the simplest structure of  $(MgS)_n$  clusters is MgS. At the level of B3LYP/6-31+G(d), the shortest Mg–S bond length calculated is 2.65 Å, which is basically consistent with the 2.60 Å crystal bond length described in the literature.<sup>24</sup> According to the obtained  $(MgS)_n$  cluster complex structure, the analysis was conducted, as shown in Fig. 2(a). When  $n$  equals 5, the lowest energy structure underwent structural changes from two to three dimensions. With the

further increase of cluster size ( $n \geq 5$ )  $(MgS)_n$  clusters presented cage structure, which could improve the structural stability to a certain extent. In addition, the coordination number of sulfur atoms increases with the increase of cluster size. Specifically, the coordination number of the sulfur atom is 1 in the MgS monomer and 2 in  $(MgS)_2$  and  $(MgS)_3$ ; the highest is 3, which occurs in  $n = 5, 6, 7, 8, 9$ , and 10. The increase of coordination number also helps to improve structural stability. As shown in Fig. 2(b), the average Mg–S bond length in Mg-sulfur clusters is significantly larger than that in monomers. For example, the average Mg–S bond length in  $(MgS)_5$  is 2.48 Å, while the average Mg–S bond length in MgS is 2.17 Å. Longer Mg–S bonds indicate reduced bond energy, which means that Mg–S bonds in the cluster are more easily dissociated, which is consistent with the lower activation energy of the  $(MgS)_n$  cluster as the cathode. In addition, we also calculated that the Mg–Mg bond length is about 2.64–2.88 Å, which is smaller than the Mg–Mg bond length (3.2 Å) in the crystal.<sup>25</sup> As shown in Fig. 2(b), the binding energy in the cluster is calculated with the formula (1). The relative stability of  $(MgS)_n$  clusters can be determined by analyzing their energy. The left ordinate of Fig. 2(b) shows the relationship between  $E_b$  of  $(MgS)_n$  clusters and the number of MgS units.  $E_b$  decreases monotonically with the increase of cluster size, indicating that the formation of  $(MgS)_n$  clusters is favorable.

The free energy of MgS unit of the clusters with the lowest energy structure is calculated. As shown in Fig. 3(a), the energy of MgS unit tends to converge with  $n$  increases. For example, the



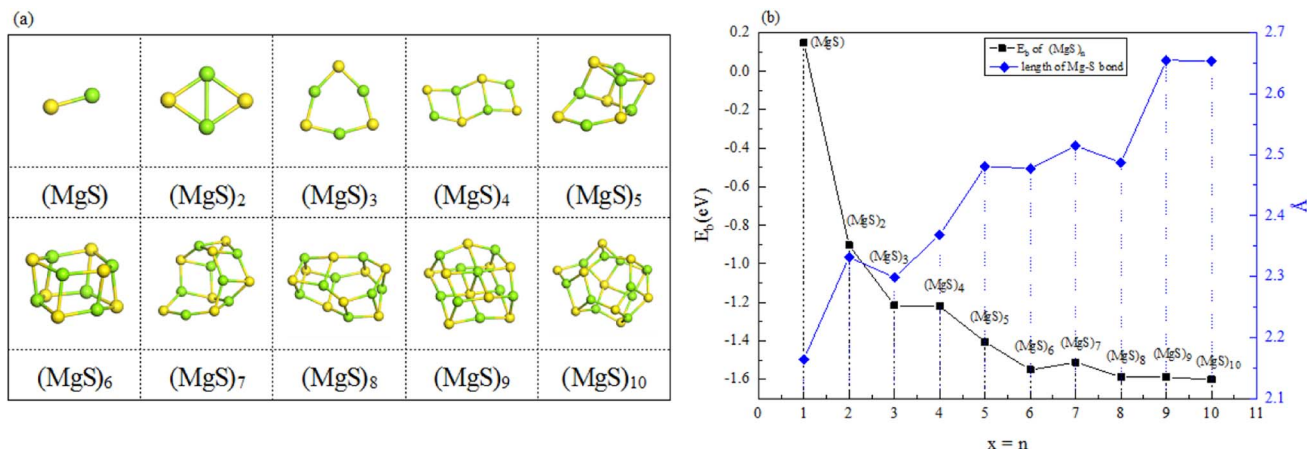


Fig. 2 (a) Optimized structures of magnesium sulfide clusters; (b) binding energy of magnesium sulfide clusters ( $n = 1-10$ ) and bond length of Mg-S bonds in the clusters.

difference in binding energy between  $(\text{MgS})_6$  and  $(\text{MgS})_{10}$  is only 0.10 eV. In the physics of atomic clusters, the second-order energy difference, is a sensitive physical quantity that reflects the relative stability of the clusters under consideration and can also be compared directly with the experimental relative abundance. Fig. 3(b) shows the second-order energy difference as a function of cluster size. The results show that the second order energy difference shows an obvious odd-even oscillation when  $n = 5$  is taken as the dividing line. The largest second-order energy difference is observed in clusters with  $n = 6$ . Therefore, among the clusters considered,  $(\text{MgS})_6$  should have a relatively high abundance.

The structural evolution of magnesium sulfide in the discharge process are organized as shown in the Fig. 4(a) and (b),  $\text{MgS}_8$  is first produced during the discharge of a magnesium sulfur battery, and the final product is  $\text{MgS}$  solid. There are two different processes shown in Fig. 4 respectively. Sulfur atoms undergo a reduction reaction, during which electrons are

gradually obtained and the valence is gradually reduced. Fig. 4(a) shows the number of magnesium atoms does not change, Fig. 4(b) shows the number of sulfur atoms does not change, and the final product is  $\text{MgS}$  unit. We hope that our work can provide some basis for the experiment and provide some help for the subsequent magnesium sulfide clusters and their applications.

### 3.2. Infrared absorption (IR) and Raman spectra of $\text{Mg}_x\text{S}_y$ and $(\text{MgS})_n$

To provide some useful information in experiment of Mg-S batteries, we simulated and calculated infrared absorption (IR) and Raman spectra. It is found that the shape of the Raman spectra strongly correlate with the size of the  $(\text{MgS})_n$  ( $n = 1-10$ ) clusters as Fig. 5 shown.

Fig. 5(a) and (b) are the Raman spectra of  $(\text{MgS})_n$  clusters, Fig. 5(c) and (d) are the IR spectra of magnesium sulfide clusters. The calculation of infrared and Raman spectra provides

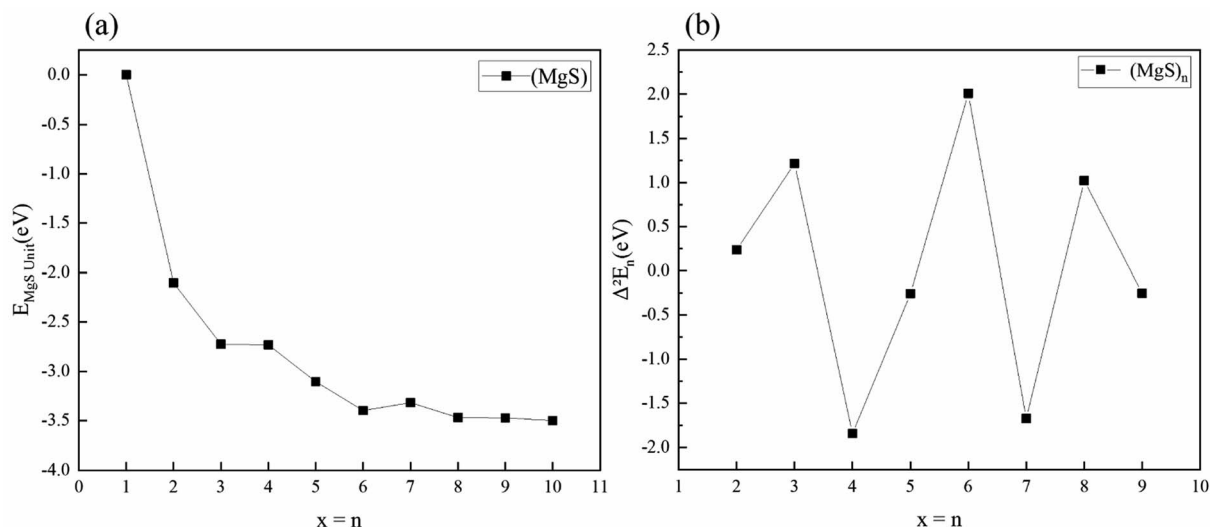


Fig. 3 (a) Free energy of  $\text{MgS}$  unit of magnesium sulfide clusters (b) second-order energy difference  $\Delta^2 E_n$  in magnesium sulfide clusters.



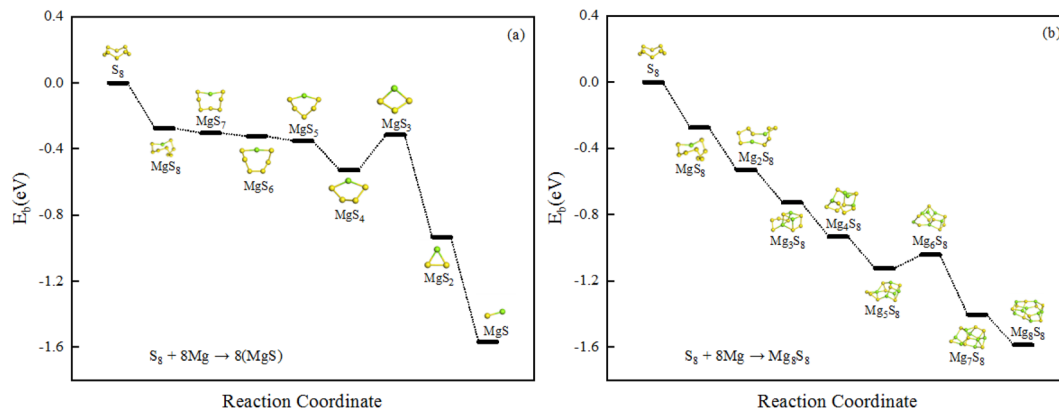


Fig. 4 (a) and (b) The structural evolution of magnesium sulfide in the discharge process.

the description of characteristic spectral lines for the three basic structural units of  $\text{MgS}$ ,  $\text{Mg}_2\text{S}$  and  $\text{Mg}_3\text{S}$ , and also provides useful information for experimental research. By observing Raman spectra, we preliminarily guess that the corresponding frequency of the component unit  $\text{MgS}$  is about  $500\text{ cm}^{-1}$ . When  $n = 2$ , there are peaks around  $300\text{ cm}^{-1}$ , especially when  $(\text{MgS})_n$  ( $n \geq 5$ ), the frequency of the main peaks is concentrated around

$300\text{ cm}^{-1}$ . We guess that the corresponding frequency of  $\text{Mg}_2\text{S}$  may be about  $300\text{ cm}^{-1}$ , and  $\text{Mg}_3\text{S}$  can be considered to be composed of multiple  $\text{Mg}_2\text{S}$ , and the intensity of the peaks is related to the number of  $\text{Mg}_3\text{S}$ . But this theory has yet to be tested experimentally.

We simulate infrared absorption (IR) and Raman absorption spectra. By observing the infrared spectrum in Fig. 5, we can see

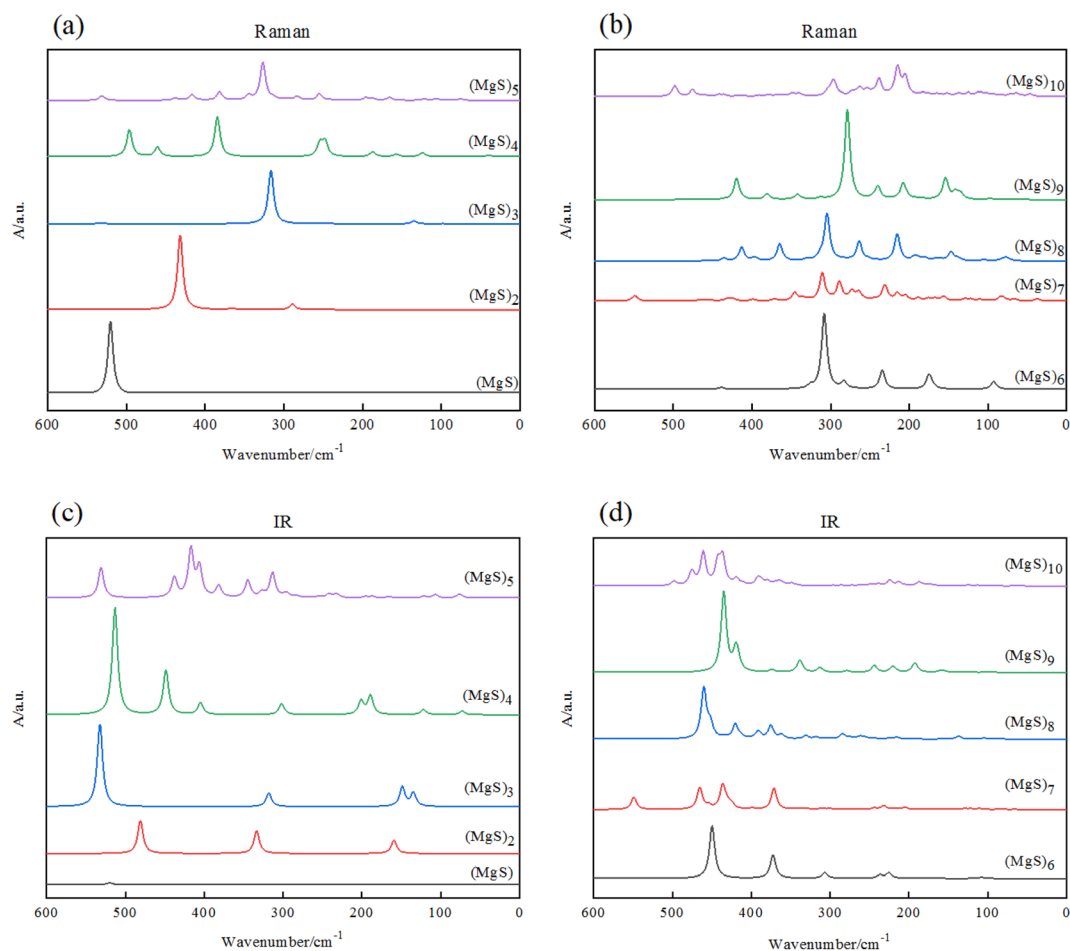


Fig. 5 (a) and (b) Raman spectra of  $(\text{MgS})_n$  clusters; (c) and (d) infrared spectra of  $(\text{MgS})_n$  clusters.



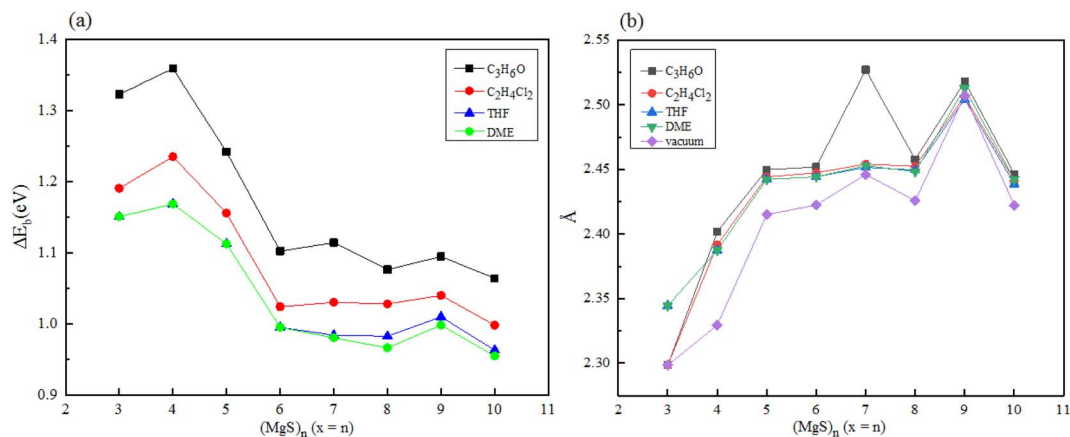


Fig. 6 Solvation energy of (a)  $(MgS)_n$  in different electrolyte solvents (b) average Mg-S bond length of  $(MgS)_n$  in different electrolyte solvents.

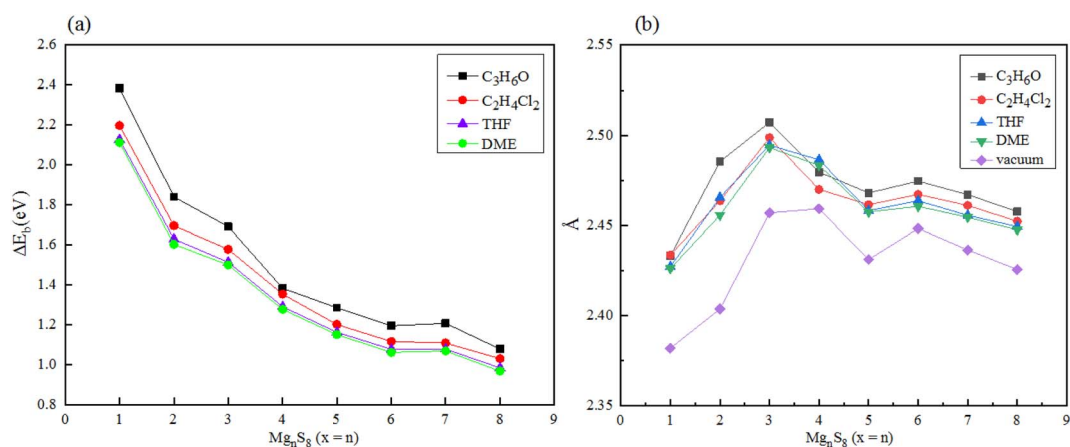


Fig. 7 (a) Solvation energy of  $Mg_nS_8$  in different electrolyte solvents (b) average Mg-S bond length of  $Mg_nS_8$  in different electrolyte solvents.

that the main characteristic peaks of  $(MgS)_n$  cluster are concentrated in the mid-infrared region ( $400\text{--}4000\text{ cm}^{-1}$ ). And with the increase of  $n$ , the main characteristic peaks of  $(MgS)_n$  cluster produced a blue shift. It is found that the shape and intensity of infrared spectra are closely related to the size of  $(MgS)_n$  ( $n = 1\text{--}10$ ) clusters. For example, the most stable cluster  $(MgS)_6$ , shows a strong band near  $450\text{ cm}^{-1}$ , with many weak peaks in the wave number range of  $100\text{ to }400\text{ cm}^{-1}$ . This is in sharp contrast to the strong peak of  $MgS$  monomer ( $525\text{ cm}^{-1}$ ).

### 3.3. Solvent effect on the $Mg_nS_8$ and $(MgS)_n$ clusters

Since magnesium sulfide battery needs to work in electrolyte environment in practical application, we carried out density functional calculation on a series of magnesium sulfide clusters and polymagnesium sulfide products in vacuum state. The solvation energy and Mg-S bond length of magnesium sulfide clusters and polymagnesium sulfide in electrolyte DME, THF,  $C_2H_4Cl_2$  and  $C_3H_6O$  solvents were analyzed. In ether-based electrolyte solvents, sulfur reduction and polysulfide formation occur at higher discharge voltages. However, the solvent properties of the dielectric constant may have a significant

effect on the oxidation-reduction reaction of sulfur. In low dielectric constant solvents such as DME, the amount of polysulfide substances formed through chain growth and disproportionation reactions is expected to be large because of the low stability of these substances in such solvents.<sup>9</sup>

Firstly, magnesium sulfide clusters were optimized under four types solvent condition, and the solvation energy of magnesium sulfide clusters was calculated, as shown in Fig. 6(a). Compared with the energy of  $(MgS)_n$  clusters under vacuum, the cluster energy under solvent conditions was lower, indicating that the cluster stability in solvent environment was higher, and with the increase of dielectric constant of solvent, The solvation energy of the clusters decreases gradually. When  $n \geq 6$ , it is obvious that solvation energy converges to about 1.0 eV. Secondly, the Mg-S bond length of magnesium sulfide clusters in the electrolyte environment was statistically analyzed. The average Mg-S bond length of the clusters in the electrolyte solvent increased with the increase of  $n$ , and with the increase of  $n$ , the average bond length remained at about 2.45 Å. In addition, the average Mg-S bond length of the same cluster increases with the increase of dielectric constant in the electrolyte solvent.



In addition, the solvation energy of polysulfide  $\text{Mg}_n\text{S}_8$  was calculated, as shown in Fig. 7(a). With the increase of the dielectric constant of the solvent DME, THF,  $\text{C}_2\text{H}_4\text{Cl}_2$  and  $\text{C}_3\text{H}_6\text{O}$ , the solvation energy of  $\text{Mg}_n\text{S}_8$  decreased gradually. These results indicate that  $\text{Mg}_n\text{S}_8$  has lower energy and more stable structure in solvents with high dielectric constant coefficient, and the solvation energy of the same polysulfide decreases with the increase of dielectric constant in different solvents. In addition, with the increase of the number of magnesium atoms in the same solvent, the solvation energy gradually converges and finally stabilizes around 1.0 eV. As shown in Fig. 7(b), the average Mg–S bond length of polysulfide  $\text{Mg}_n\text{S}_8$  under different electrolyte solvents was calculated. It can be seen that compared with the average Mg–S bond length of polysulfide under vacuum, the average Mg–S bond length of polysulfide under electrolyte solvent increased, and increased with the increase of electrolyte dielectric constant. In addition, with the increase of the number of Mg atoms, the average bond length of Mg–S converges to about 2.46 Å when the number of Mg atoms is greater than or equal to 5.

## 4. Conclusions

The structure search method combined with density functional theory was used to predict the configuration of polysulfide magnesium, and the stable structure of polysulfide  $\text{Mg}_x\text{S}_y$  and  $(\text{MgS})_n$  ( $n = 1-10$ ) clusters was determined. The structure, stability and properties of  $(\text{MgS})_n$  clusters, which are very important for improving the performance of Mg–S batteries, are investigated. The most stable structure, second order energy difference, binding energy, IR spectrum, Raman spectrum and solvation energy of the clusters are discussed. Second-order energy difference and gap analysis show that  $(\text{MgS})_6$  cluster is more stable than adjacent cluster. The weakening of the Mg–S bond means that  $(\text{MgS})_n$  is more easily activated than the MgS monomer. We also provide a description of the structural evolution of magnesium sulfide in the discharge process,  $\text{MgS}_8$  is first produced during the discharge of a magnesium sulfur battery, and the final product is MgS solid. The calculation of infrared and Raman spectra provides the description of characteristic spectral lines for MgS,  $\text{Mg}_2\text{S}$  and  $\text{Mg}_3\text{S}$ , and also provides useful information for experimental research. In addition, the solvation energy of magnesium polysulfide in electrolyte DME, THF,  $\text{C}_2\text{H}_4\text{Cl}_2$  and  $\text{C}_3\text{H}_6\text{O}$  was calculated. With the increase of dielectric constant DME ( $\epsilon = 7.2$ ), THF ( $\epsilon = 7.6$ ),  $\text{C}_2\text{H}_4\text{Cl}_2$  ( $\epsilon = 10.0$ ) and  $\text{C}_3\text{H}_6\text{O}$  ( $\epsilon = 20.7$ ), the solvent energy of magnesium polysulfide gradually decreases, indicating that magnesium polysulfide is more stable in the electrolyte environment with large dielectric constant. It can promote the transformation of long chain magnesium polysulfide to short chain magnesium polysulfide, and delay the transformation of magnesium polysulfide to the final product MgS, which is conducive to improving the performance of Mg–S batteries. The work in this paper provides a good theoretical support for the understanding of  $(\text{MgS})_n$  clusters, and the research results have a certain guiding significance for further improving the performance of magnesium sulfide batteries.

## Conflicts of interest

There are no conflicts to declare.

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