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Pressure-induced physical properties in topological semi-metal TaM_2 ($M = As, Sb$)[†]

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In this study, DFT based first principles calculations are used for measuring the structural, elastic, mechanical, electronic, optical and thermodynamic features of topological semimetal TaM_2 ($M = As, Sb$) under various pressures. We conducted the first investigation into the physical properties of the topological semimetal TaM_2 ($M = As, Sb$) under pressure. Formation energy and Born stability criteria justify the compound's thermodynamic and mechanical stability. We used elastic constants, elastic moduli, Kleinman parameter, machinability index, and Vickers hardness to investigate the mechanical properties of topological semimetal TaM_2 . Poisson's and Pugh's ratios reveal that both compounds change from brittle to ductile in response to pressure. The increasing nature of elastic moduli suggests that TaM_2 becomes stiffer under stress. The pressure has a significant effect on the anisotropy factor for both materials. Band structure analysis shows that both compounds are Weyl semi-metals and the d orbital contributes significantly to the formation of the Fermi level, as shown by the density of states (DOS) analysis. Investigation of electronic characteristics provides important support for dissecting optical performance. Both the reflectivity and absorption spectra shift upwards in energy when pressure is increased. The refractive index value decreases and becomes flat in the higher energy region. Based on their refractive indices, both of these materials demonstrate as a high-density optical data storage medium when exposed to the right light source. The thermodynamic properties including sound velocity, and Debye temperature all exhibit an increasing nature with applied pressure. Due to their high Debye temperatures, the components under study have a rather high melting point.

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1. Introduction

Topological semimetals and metals have emerged as a new area in quantum materials research. They exhibit novel macroscopic quantum phenomena that are not only of basic interest but may have some important technological applications.^{1,2} In earlier times, various topological semimetals have exhibited superconductivity through different methods such as applying pressure,^{3–6} doping,^{7,8} and the effect of proximity.^{9,10} Interestingly, superconductivity was observed in point contacts between ends of normal metal and various non-superconducting topological materials exhibiting Dirac points,^{11,12} Weyl points,^{13–16} triply degenerate points,^{17,18} and nodal lines.^{19,20} It is intriguing that many topological materials, including type II Weyl semimetals like $MoTe_2$ (ref. 21) and WTe_2 ,^{22,23} Dirac semimetals like Cd_3As_2 (ref. 24) and $ZrTe_5$,²⁵ and topological insulators like Bi_2Se_3 ,²⁶ Bi_2Te_3 (ref. 27) and Sb_2Te_3 ,²⁸ undergo superconducting phase transitions when subjected to high pressure. Even though

the process of tip-induced superconductivity (TISC) remains unknown, this method offers an innovative and practical method to investigate TISC. Many researchers believe that bulk bands¹⁵ or topological surface states¹⁶ are responsible for their creation. Therefore, it is highly desired to conduct TISC inspections across a wide range of materials with adjustable properties.

Recently, a new class of topological semimetals, the transition-metal di-pnictides MPn_2 ($Pn = Sb, As, P; M = Nb, Ta$), have attracted widespread interest.^{27–34} When spin-orbit coupling (SOC) ignored, band structures exhibit nodal lines; however, when SOC is considered, the band anti-crossings become completely gapped, releasing an array of electrons and crossing hole band at the Fermi level and specifying weak Z_2 topological invariants in the bulk.^{27–29} However, due to the low Z_2 number, surface states are extremely sensitive to the crystal orientation with no topological protection. In contrast, there is a great deal of similarity between the band structures of the individuals of the same family. Consequently, realizing TISC on various MPn_2 members or crystallographic planes and comparing their superconducting properties may lead to important insights about how to explain induced superconductivity. Another intriguing aspect of the MPn_2 family is the

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possibility of inducing Weyl points using a magnetic field.³⁵ Studying $M\text{Pn}_2$ at high pressure is enticing because its monoclinic structure is stable at very high pressure.³⁶

The nonmagnetic semimetal TaAs_2 reportedly displays a very large negative magnetoresistance due to some unknown scattering mechanism, as demonstrated by Luo *et al.*⁴⁵ Using first-principles calculations, Xu *et al.*⁴⁷ have explored the electronic structures and topological features of TaAs_2 and TaSb_2 semimetals. They show that nodal lines are present in all of these compounds because spin-orbit coupling is absent in the band structure. The effects of pressure on structural and transport characteristics of TaSb_2 single crystal were studied by Y. Zhou *et al.*⁴⁸ Although the synthesis and remarkable properties of the topological semimetal TaM_2 ($M = \text{As}, \text{Sb}$) have been described in recent papers, a comprehensive theoretical investigation of their physiochemical properties is still absent.

In this work, we provide a thorough evaluation of the pressure-dependent physical properties in the topological semimetals TaAs_2 and TaSb_2 . We systematically analyzed several fundamental features of TaM_2 ($M = \text{As}, \text{Sb}$) as a function of pressure, including the structural, elastic, mechanical, electronic, optical, and thermodynamic properties. We hope that this work will be useful in advancing high-pressure study and production of topological semi metals.

2. Computational methods

2.1 Density functional theory (DFT)

First principles calculations were carried out utilizing the DFT-based CASTEP algorithm.³⁷ The simplified Perdew–Burke–Ernzerhof model was applied to characterize exchange–correlation energies in the GGA.³⁸ The following valence electrons were taken into account during pseudo-atomic simulations: $\text{Ta}-5d^3 6s^2$, $\text{As}-4s^2 4p^3$, and $\text{Sb}-5s^2 5p^3$ for topological semi-metal TaM_2 ($M = \text{As}, \text{Sb}$). We computed the optimized

structure and total energy by fixing the k -point to $5 \times 10 \times 5$ and the cut-off energy to 520 eV, respectively. The Monkhorst–Pack technique confirmed that the k -points are in the Brillouin region.³⁹ In order to determine the best configuration, we employed the Broyden–Fletcher–Goldfarb–Shanno (BFGS) technique.⁴⁰ Tolerance factors for convergence have been calculated to be 1×10^{-5} eV \AA^{-1} total energy per atom, with maximum displacement, force, and stress be 1×10^{-3} \AA , 0.03 eV \AA^{-1} and 0.05 GPa respectively, all based on recent simulations of geometry optimization. In this study, the process of optimizing the structure involves slowly raising applied pressure from 0 to 40 GPa with 10 GPa difference. Most reliable crystal structures can be made with the help of the VESTA programme.⁴¹ When calculating the electrical and optical properties, the same parameters used to optimise the structure are applied. The ‘stress-strain’ approach of the CASTEP algorithm is used to calculate elastic moduli and constants.⁴² The ELATE programme can generate anisotropic contour plots in three dimensions (3D).⁴³

3. Results and discussion

3.1 Structural properties

The topological semi-metal TaAs_2 and TaSb_2 materials retain monoclinic crystallographic configuration including space group $C2/m$.⁴⁴ There are a spread of TaAs_2 bond length range from 2.72–2.56 \AA and TaSb_2 bond distances ranging from 2.92–2.73 \AA . Fig. 1 depicts the 2D and 3D structure of topological semi-metal TaM_2 ($M = \text{As}, \text{Sb}$). In the ESI, Table S1† displays the calculated and several experimental structural parameters of the semi-metal TaM_2 ($M = \text{As}, \text{Sb}$). We validate our DFT-based simulation by finding good agreement between our estimated and experimental values for the structural parameters TaM_2 ($M = \text{As}, \text{Sb}$). Fig. 2(a)–(c) shows that hydrostatic pressure has an effect on the lattice parameters, pressure causes a decrease in

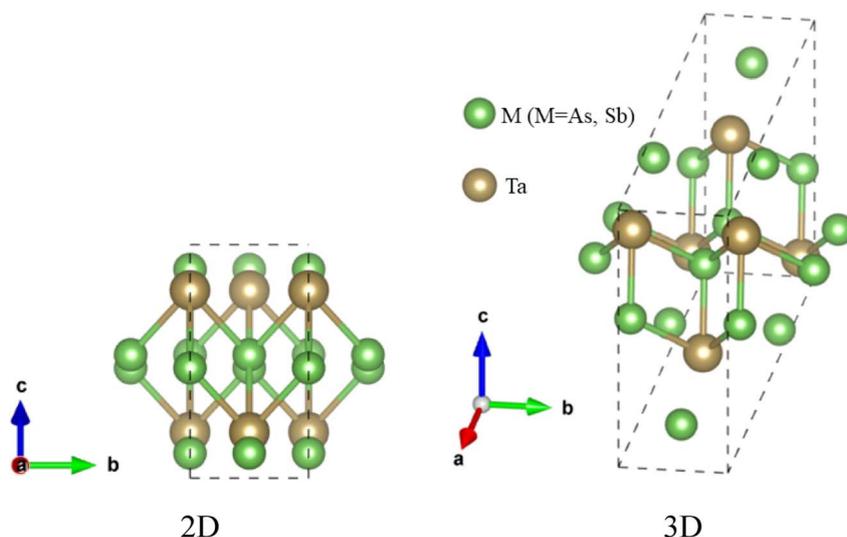


Fig. 1 The crystal 2D and 3D structure of topological semi-metal TaM_2 ($M = \text{As}, \text{Sb}$).



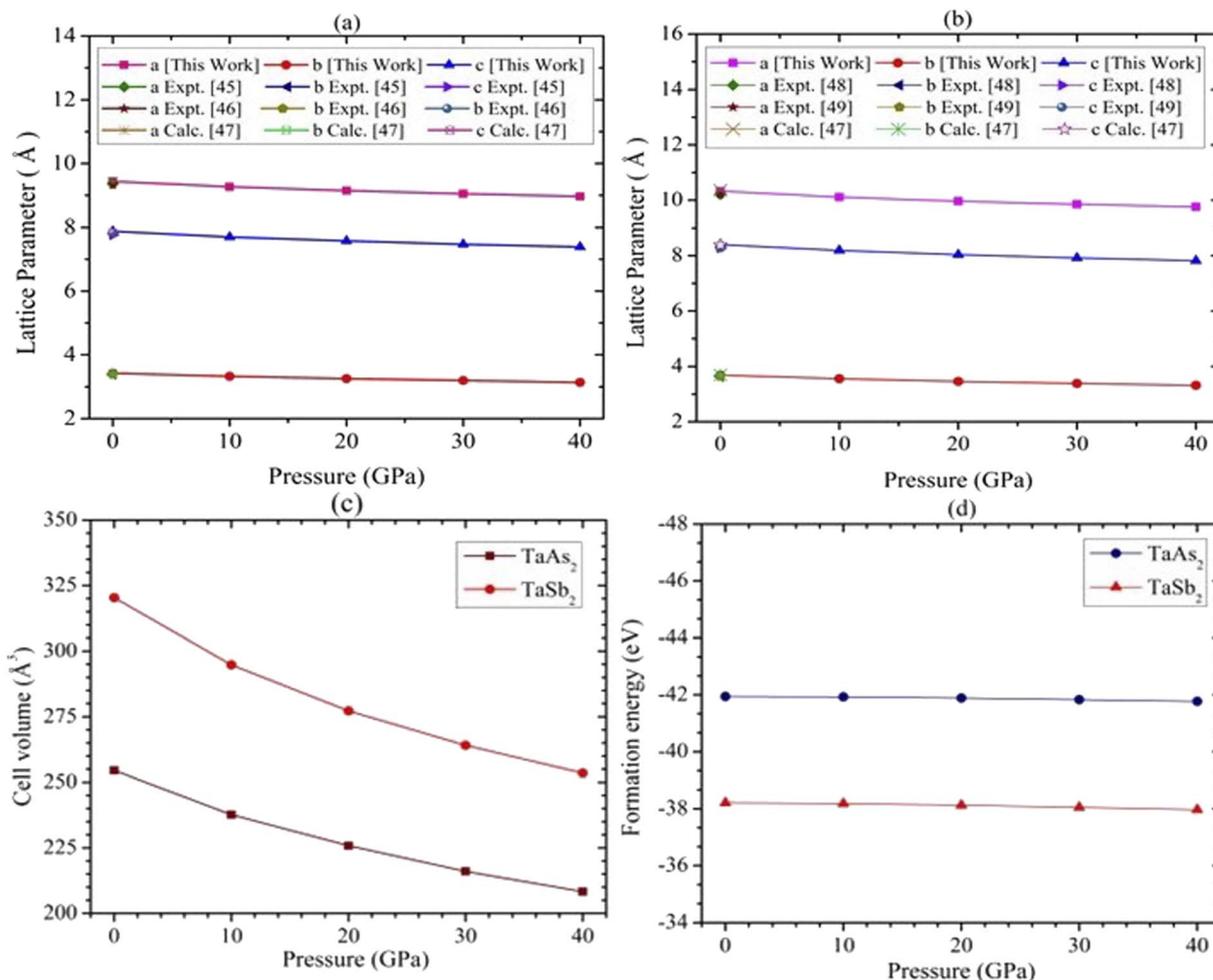


Fig. 2 Pressure-dependent structural distortion in (a) lattice parameter for TaAs₂ (b) lattice parameter for TaSb₂, (c) cell volume, and (d) formation energy of TaM₂ (M = As and Sb) semi-metal.

both the volume of the unit cell and lattice parameter. Our simulated lattice parameters exhibit excellent concordance with other experimental and calculated values^{45–49} which was depicted in Fig. 2(a) and (b) for TaAs₂ and TaSb₂, respectively. This clearly justify the validity of our work. The variation of cell volume as a function of pressure is depicted in Fig. 2(c). To evaluate the materials phase stability under pressure, the formation energy of TaM₂ (M = As, Sb) is calculated using the below equation:

$$\Delta E_f(\text{TaM}_2) = \frac{E_{\text{tot}}(\text{TaM}_2) - E_s(\text{Ta}) - E_s(\text{M})}{N}; \quad (\text{M} = \text{As, Sb}) \quad (1)$$

Here, $E_s(\text{Ta})$, $E_s(\text{M})$, and $E_{\text{tot}}(\text{TaM}_2)$ represent the energy of Ta, M, and TaM₂, whereas (M = As and Sb) and N denotes the number of atoms in the unit cell. Each substance needs a negative formation energy to be thermodynamically stable.⁵⁰ The calculated values of ΔE_f are shown in Fig. 2(d). Therefore, TaM₂ (M = As, Sb) compounds are thermodynamically stable, as evidenced by the negative values of ΔE_f under hydrostatic stress.

3.2 Mechanical properties

Due to comprehend the nature of bonds between nearby atoms and the cohesiveness of a material, a thorough examination of elastic characteristics is required.⁵¹ Hence, studying the elastic constants is crucial for gaining insight into the mechanical properties of topological semi-metal TaM₂ (M = As, Sb) and its response to pressure. Hooke's law provides a framework for determining elastic constants from the stress–strain relationship.⁵² In the case of the monoclinic phase, there are thirteen elastic constants, which are designated as follows: C_{11} , C_{22} , C_{33} , C_{44} , C_{55} , C_{66} , C_{12} , C_{23} , C_{35} , C_{46} , C_{13} , C_{15} , and C_{25} , respectively.⁵³

A material's length elasticity, shape elasticity, and resistance to shear deformation can be represented by C_{11} , C_{12} and C_{44} , respectively. The estimated elastic constants of topological semi-metal TaAs₂ and TaSb₂ are represented in Tables S2 and S3 [see ESI†], respectively.

The Born stability criterion for the monoclinic structure are as follows:^{54,55}

$$C_{22} - P > 0, C_{44} - P > 0, C_{66} - P > 0, C_{11} - P > 0, C_{33} - P > 0, C_{55} - P > 0, 2C_{12} + 2C_{13} + 2C_{23} + C_{11} + C_{22} + C_{33} + 3P > 0, (C_{11}$$



$$\begin{aligned}
 -P)(C_{33} - P) > C_{35}^2, (C_{66} - P)(C_{44} - P) > C_{46}^2, (C_{33} + C_{22} - \\
 2C_{23} - 4P) > 0, 2(C_{23} - P)C_{25}C_{35} + (C_{22} - P)[(C_{55} - P)(C_{33} - \\
 P) - C_{35}^2] > (C_{55} - P)(C_{23} + P)^2 + C_{25}^2(C_{33} - P), 2C_{15}C_{35}[(C_{13} \\
 + P)(C_{22} - P) + 2C_{15}C_{25}[(C_{12} + P)(C_{33} - P) - (C_{23} + P)(C_{13} + \\
 P)] - (C_{23} + P)(C_{12} + P)] + 2C_{25}C_{35}[(C_{12} + P)(C_{11} - P) - (C_{13} + \\
 P)(C_{12} + P)] - C_{15}^2[(C_{33} - P)(C_{22} - P) - (C_{23} + P)^2] - C_{25}^2 \\
 [(C_{33} - P)(C_{11} - P) - (C_{13} + P)^2] - C_{35}^2[(C_{22} - P)(C_{11} - P) - \\
 (C_{12} + P)^2] + (C_{55} - P)[(C_{22} - P)(C_{13} - P)(C_{33} - P) - (C_{13} + P)^2 \\
 (C_{22} - P) - (C_{11} - P) - (C_{23} + P)^2 - (C_{12} + P)^2(C_{33} - P) + 2(C_{13} \\
 + P)(C_{12} + P)(C_{23} + P)] > 0 \quad (2)
 \end{aligned}$$

All of the estimated elastic constants satisfy Born stability criterion conforming mechanical stability of our investigated compounds even when subjected to high levels of stress. In Tables S2 and S3† shows the impact of stress on elastic constants of topological material TaM₂ (M = As, Sb). It was seen that the calculated values of elastic constant expand with rising the stress, so our studied materials become stiffer and more resistance to deformation, which can be used in different engineering applications.

Using the Voigt–Reuss–Hill averaging approach, we may extrapolate these characteristics from the calculated elastic constants.⁵⁶ Resistance against plastic deformation due to applied pressure and shear stress can be measured by materials bulk modulus and shear modulus.^{55–57} Tables S4 and S5† listed the calculated values of the Pugh's and Poisson's ratio, as well as for elastic moduli the pressure-treated topological semi-metal TaM₂ (M = As, Sb) and the impact of pressure on elastic moduli depicted in Fig. 3(a) and (b). When the pressure is raised, the bulk and shear both increases. That means at higher pressure, monoclinic crystal TaM₂ (M = As, Sb) exhibits a larger resistance to compression. We also demonstrate that pressure has a smaller effect on the shear modulus than bulk modulus. One of the most important mechanical properties of any given material is its Young's modulus. In tensile loading, it's all about the stress-to-strain ratio.⁵⁸ Rough stiffness is often associated with a high Young's modulus, and is well known in the scientific

community. From Fig. 3, it is evident that as pressure is increased, the *E* values for TaM₂ (M = As, Sb) materials increase, suggesting that pressure significantly affects their hardness.

Tables S4 and S5† listed the calculated values of the elastic moduli for the pressure-treated topological semi-metal TaM₂ (M = As, Sb).

Fig. 4(a) depicts the Pugh's ratio for TaM₂ semi-metals, that is equal to *B/G* and is a measure of how ductile or brittle a material is. Pugh's ratio states that a small (large) *B/G* value⁵⁹ is related to a brittle (ductile) solid's nature. When this ratio becomes close to 1.75, brittle materials become easily identifiable as opposed to ductile ones. Fig. 4(a) demonstrates that the value of *B/G* rises with increasing pressure. Meanwhile, at equal or above 30 GPa the TaM₂ (M = As, Sb) material become ductile. Below this pressure, the material is brittle. So, there is brittle and ductile transition, which suggests that pressure enhances TaM₂'s ductility.

Poisson's ratio is another criterion for measuring ductility; its critical value is 0.26.⁶⁰ For a wide range of stress, *ν* > 0.26 indicating the ductility of TaM₂ (M = As, Sb) compounds. As seen in Fig. 4(b), the value of *ν* for both materials rise as a function of stress. Brittle-ductile transition occur for both the materials at 30 GPa pressure.

Vickers hardness (*H_v*) as well as *E*, *G*, *B*, *ν* and *G/B* can be used to determine hardness of a material.⁶¹ The relations are:

$$H_1 = 0.0963B \quad (3)$$

$$H_2 = 0.0607E \quad (4)$$

$$H_3 = 0.1475G \quad (5)$$

$$H_4 = 0.0635E \quad (6)$$

$$H_5 = -2.899 + 0.1769G \quad (7)$$

$$H_6 = \frac{(1 - 2\nu)B}{6(1 + \nu)} \quad (8)$$

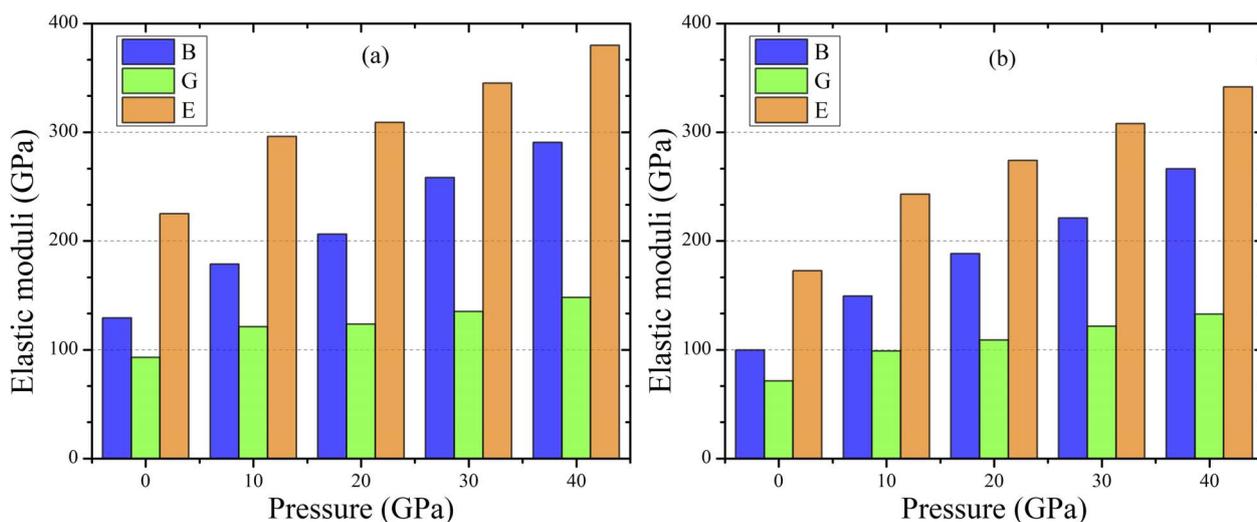


Fig. 3 Variation of elastic moduli for topological semi-metal TaM₂ (M = As, Sb) under pressure.



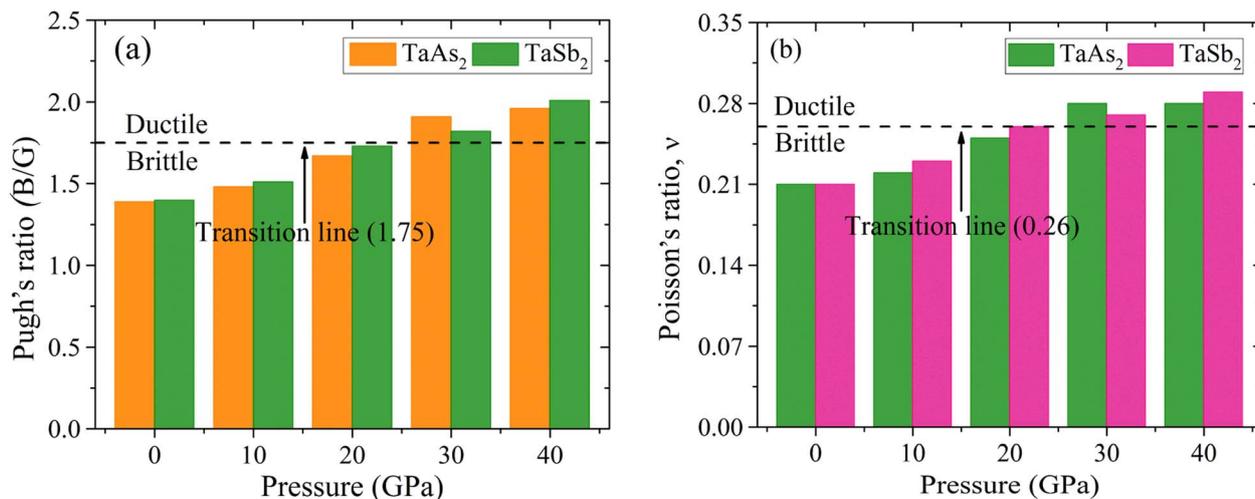


Fig. 4 Effect of pressure on (a) Pugh's and (b) Poisson's ratio of topological semi-metal TaM₂ (M = As, Sb).

$$H_7 = \frac{(1 - 2\nu)E}{6(1 + \nu)} \quad (9)$$

$$H_8 = 2(k^2G)^{0.585} - 3 \quad \text{here, } k = \frac{B}{G} \quad (10)$$

The hardness values of TaM₂ (M = As, Sb) are shown in Table 1. As pressure rises, both compounds hardness value begins to grow. According to the findings, applying pressure makes elastic and plastic deformation more complex. Hardness measurements clearly show that TaAs₂ is harder than TaSb₂.

For monoclinic phase,⁶²⁻⁶⁴

$$A^U = 5 \frac{G_V}{G_R} + \frac{B_V}{B_R} + 6 \geq 0 \quad (11)$$

$$A^G = \frac{G_V - G_R}{G_V + G_R} \quad (12)$$

$$A^B = \frac{B_V - B_R}{B_V + B_R} \quad (13)$$

Similarly, A^{eq} is the equivalent Zener anisotropy factor.⁶⁴

$$A^{eq} = \left(1 + \frac{5}{12}A^U\right) + \sqrt{\left(1 + \frac{5}{12}A^U\right)^2 - 1} \quad (14)$$

From log Euclidean formula the universal log-Euclidean index can be written as,⁶⁵

$$A^L = \sqrt{\left[\ln\left(\frac{B_V}{B_R}\right)\right]^2 + 5 \left[\ln\left(\frac{C_{44}^V}{C_{44}^R}\right)\right]^2} \quad (15)$$

Here, the C_{44} values for Voigt (C_{44}^V) and Reuss (C_{44}^R) determined as-

$$C_{44}^R = \frac{5}{3} \frac{C_{44}(C_{11} - C_{12})}{3(C_{11} - C_{12}) + 4C_{44}} \quad (16)$$

$$C_{44}^V = \frac{3}{5} \frac{(C_{11} - C_{12} - 2C_{44})^2}{3(C_{11} - C_{12}) + 4C_{44}} \quad (17)$$

The Kleinman parameter, which is denoted by ζ often lies between 0 and 1. This index measures how much bonds can extend relative to other types of securities. This metric assesses a material's tensile and flexural stress resistance. For a compound, the following form may be used:^{66,67}

Table 1 Pressure dependent hardness of topological semi-metal TaM₂ (M = As, Sb)

P (GPa)	Semi-metal	H ₁	H ₂	H ₃	H ₄	H ₅	H ₆	H ₇	H ₈
0	TaAs ₂	12.45	13.66	13.71	14.29	13.55	10.33	17.98	38.67
	TaSb ₂	9.59	10.47	10.49	10.95	9.69	7.96	13.77	32.94
10	TaAs ₂	17.20	17.98	17.85	18.81	18.51	13.66	22.66	49.33
	TaSb ₂	14.40	14.75	14.58	15.43	14.59	10.94	17.78	44.58
20	TaAs ₂	19.86	18.76	18.23	19.62	18.96	13.75	20.60	58.01
	TaSb ₂	18.13	16.63	16.07	17.40	16.37	11.95	17.39	56.06
30	TaAs ₂	24.86	20.94	19.92	21.91	20.99	14.79	19.77	72.19
	TaSb ₂	21.28	18.70	17.92	19.56	18.59	13.34	18.60	63.80
40	TaAs ₂	27.99	23.06	21.85	24.13	23.31	16.65	21.77	78.82
	TaSb ₂	25.65	20.73	19.58	21.68	20.58	14.45	18.53	76.01



$$\zeta = \frac{C_{11} + 8C_{12}}{7C_{11} + 2C_{12}} \quad (18)$$

When bonds are stretched, ζ tends towards 1, whereas when bonds are bent, ζ tends towards 0. Calculated values of ζ confirm our studied materials are bending type. Tables 2 and 3 demonstrate the effect of stress on the Kleinman parameter. In terms of potential engineering applications, the machinability index, $\mu_M = B/C_{44}$, is an important performance indicator. The slicability of a solid is represented by the μ_M value. If μ_M is high, then dry lubrication and modifications are simpler.⁶⁸

$$\mu_M = \frac{B_H}{C_{44}} \quad (19)$$

The μ_M value of TaM_2 ($M = \text{As, Sb}$) is presented in Table 2 for TaAs_2 and Table 3 for TaSb_2 at various pressures, as pressure increases, this value also rises. Therefore, TaM_2 ($M = \text{As, Sb}$) compounds are less machinable. Tables 2 and 3 display the calculated values of various anisotropy factors under applied pressures for TaAs_2 and TaSb_2 , respectively. The computed equivalent Zener anisotropy factor A^{eq} suggests that TaM_2 ($M = \text{As, Sb}$) materials are highly anisotropic and become more anisotropic with applying pressure. Both A^{G} and A^{B} have values between 0 and 1, with 0 denoting isotropy and 1 denoting anisotropy, respectively. TaM_2 ($M = \text{As, Sb}$) is anisotropic in our study because $A^{\text{G}} > A^{\text{B}} > 0$, characterized by a greater degree of shear anisotropy than compressibility anisotropy. Because strongly anisotropic crystals are less common than A^{U} crystals, A^{L} is a measure of a crystalline substance's absolute anisotropy. The main drawback of A^{U} is that it only provides a qualitative description of the degree to which a material is anisotropic.

A graphic representation of three-dimensional change in E , β , G , and ν were created using ELATE algorithm.⁶⁹ Anisotropy values of E , β , G , and ν in TaM_2 semi-metals are presented at 0 GPa and 40 GPa depending on the matrix that is provided to

Table 2 The Voigt and Reuss values of C_{44}^{R} & C_{44}^{V} (in GPa), A^{eq} , A^{G} , A^{B} and A^{L} of TaAs_2 compounds at different applied pressures

P	C_{44}^{R}	C_{44}^{V}	A^{eq}	A^{U}	A^{G}	A^{B}	ζ	μ_M
0	31.64	0.54	12.04	12.15	0.01	0.01	0.42	1.44
10	42.32	0.04	12.18	12.31	0.03	0.01	0.44	1.43
20	43.10	0.39	12.42	12.60	0.05	0.02	0.48	1.67
30	53.11	0.04	12.23	12.38	0.03	0.01	0.48	1.64
40	51.96	0.96	12.11	12.23	0.02	0.01	0.51	1.98

Table 3 The Voigt and Reuss values of C_{44}^{R} & C_{44}^{V} (in GPa), A^{eq} , A^{G} , A^{B} and A^{L} of TaSb_2 compounds at different applied pressures

P	C_{44}^{R}	C_{44}^{V}	A^{eq}	A^{U}	A^{G}	A^{B}	ζ	μ_M
0	25.31	0.00	12.35	12.52	0.05	0.02	0.46	1.31
10	34.80	0.86	12.27	12.42	0.04	0.01	0.50	1.32
20	40.72	0.25	12.37	12.54	0.05	0.01	0.50	1.48
30	43.48	0.67	12.44	12.62	0.05	0.02	0.51	1.79
40	50.41	0.13	12.44	12.63	0.06	0.01	0.55	1.72

the ELATE programme. Fig. 5 depicts the change in elastic moduli along different axes. A 3D sphere plot displays isotropy, whereas a non-sphere plot illustrates anisotropy.⁷⁰ Elastic anisotropy in the studied materials is present in all directions, as shown by non-spherical three-dimensional shapes.

3.3 Electronic properties

Conduction and valence band electrons can be utilized in order to determine band diagrams of materials, which in turn reveals useful information about the solid's physiochemical properties. Inside the Brillouin zone, dispersion of electron energy along $L-M-A-G-Z-V$ directions, have a substantial impact on their behavior. Fig. 6 and 7 illustrate the band structure of TaM_2 ($M = \text{As, Sb}$) at 0 and 40 GPa pressure. Where dashed black line represents Fermi level (E_{F}). The red circle in the band structure was covered to demonstrate the narrowing band gap from 0 to 40 GPa. These results indicate the Weyl semi metallic characteristics of our studied compound. Moreover, topological semimetals have surface states or Fermi arcs, which make it possible to make new electronic devices with high mobility and low dissipation.

TDOS is a crucial determinant of whether a material is metallic, superconducting, or insulating. Fig. S1 [see ESI†] shows the TDOS values from 10 to 40 GPa for topological semi-metal (a) TaAs_2 and (b) TaSb_2 , respectively. The electronic properties of TaM_2 are obtained TDOS and PDOS. At 0 GPa, computed TDOS value of TaAs_2 is 0.33 states per eV per f.u., while 0.48 states per eV per f.u. for TaSb_2 . This value do not changes noticeably as the pressure increases. Fig. 8(a) and (b) display the determined TDOS and PDOS for TaM_2 materials at 0 and 40 GPa pressures, respectively. The atomic contributions to band formation in these materials are clearly illustrated by the figures. According to DOS, n-type carriers are present in the studied materials,⁷¹ as the peak for the electron crossing at E_{F} is very strong. Formation of DOS in the valence band near E_{F} is primarily attributable to the Ta, As and Sb states. For TaAs_2 the DOS of Ta, and As at E_{F} at 0 GPa are ~ 0.34 , and ~ 0.21 states per eV per f.u., respectively, and for TaSb_2 , Ta and Sb have DOS at E_{F} at 0 GPa are ~ 0.34 and ~ 0.14 states per eV per f.u., respectively. For both materials, the DOS value do not significantly change as pressure is applied. This observation demonstrates that Ta and As atoms are the primary contributors to the formation of DOS at E_{F} . The Ta-5d states significantly contribute to the energy of the valence band between 0 and -7.09 eV, while the As-4p and Sb-5p states also significantly contribute to this energy at 0 GPa. Both compounds have no discernible impact on their PDOS at 40 GPa.

3.4 Optical properties

The optical characteristics of a substance give essential details, especially for applications using optoelectronic components. The response of various materials to electromagnetic fields is an important area to study. Here we investigate the optical properties in response with photon energy. These properties include reflectivity (R), optical absorption (α), real (σ_1) and imaginary (σ_2) components of optical conductivity, real (n) and imaginary



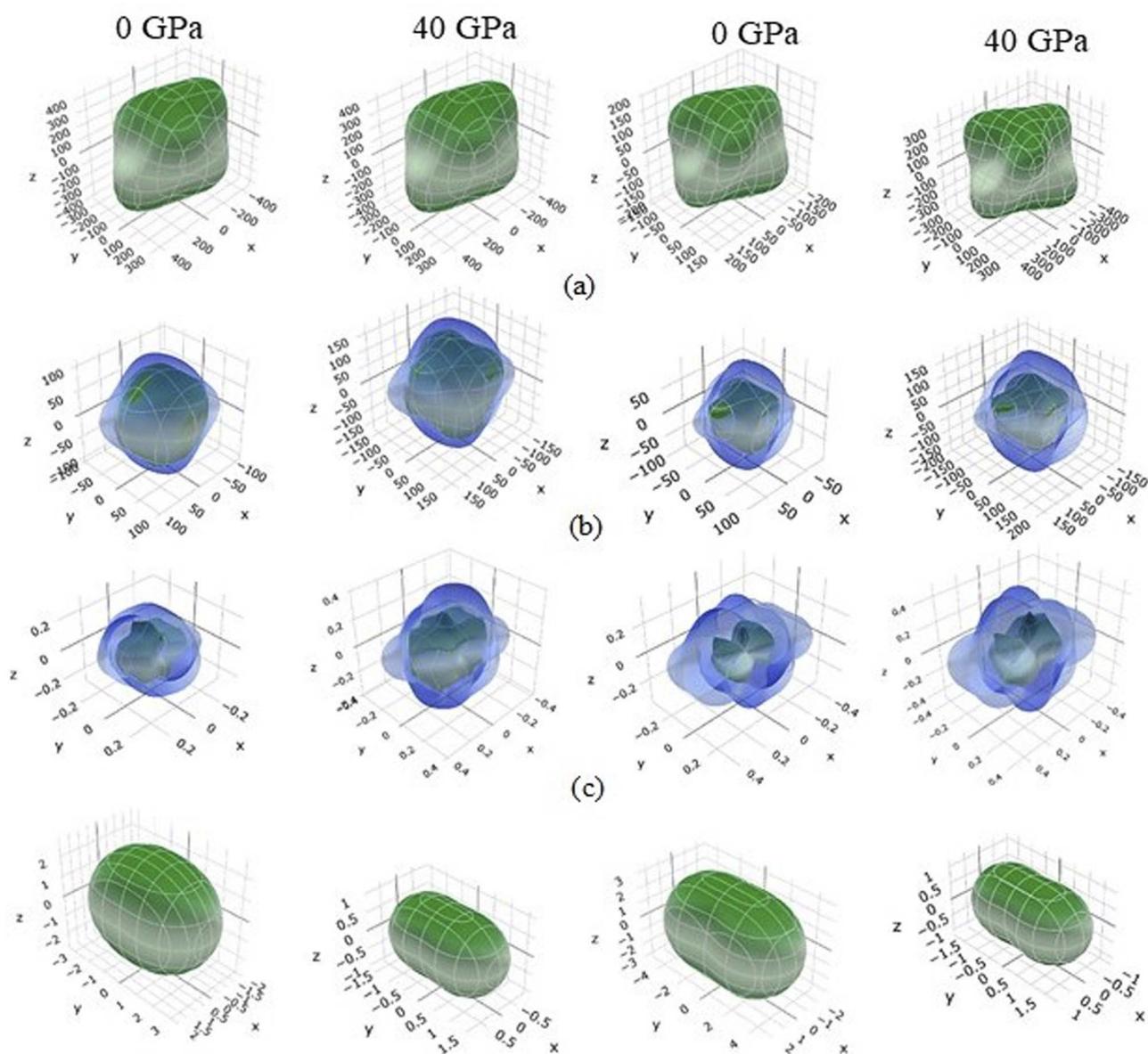


Fig. 5 3D contour plots of (a) Young's modulus, (b) shear modulus, (c) Poisson's ratio, and (d) linear compressibility at 0 and 40 GPa for topological semi-metal TaAs₂ and TaSb₂, respectively.

(k) components of refractive index, and real (ϵ_1) and imaginary (ϵ_2) parts of dielectric functions. This research is primarily concerned with the optical functions along the [100] polarization direction.

Absorption coefficients are used to calculate how much light is lost when travelling through various materials. In general, a material's transparency to radiation increases with decreasing absorption coefficient. Absorption of topological semi-metal TaAs₂ and TaSb₂ are shown in Fig. 9(a) and 10(a). There is an initial increase in optical absorption as the photon energy increases, a maximum value of about 8.82 eV and 8.07 eV for TaAs₂ and TaSb₂, respectively. It is interesting to observe that for photon energies more than or equal to 8.90 eV and 8.20 eV,

as pressure is increased, a shift is seen in the absorption spectra, which favors greater energy.

In contrast to radiation, the dielectric function considers the actual and hypothetical permittivity properties of the materials against frequency. Dielectric functions (real and imaginary portions) as a function of pressure are shown in Fig. 9(b), (c), 10(b) and (c) up to 30 eV of photon energy for topological semi-metal TaAs₂ and TaSb₂, respectively. For TaAs₂ the real part of dielectric function has a highest value ~ 39.30 with zero photon energy and reduces gradually while rising the energy. In case of TaSb₂, the highest dielectric constant value is ~ 98.60 (real) at 0 eV, that also reduces with incident photon energy. However, in the high-energy area, the real and imaginary parts get close to



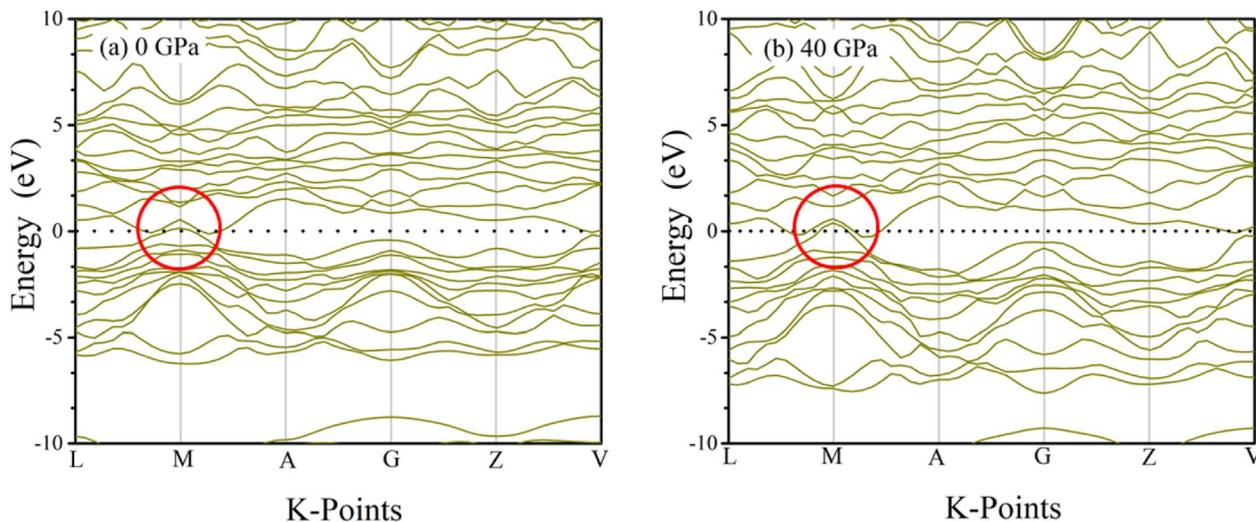


Fig. 6 Simulated electronic band structures of topological semi-metal TaAs₂ at 0 and 40 GPa pressure.

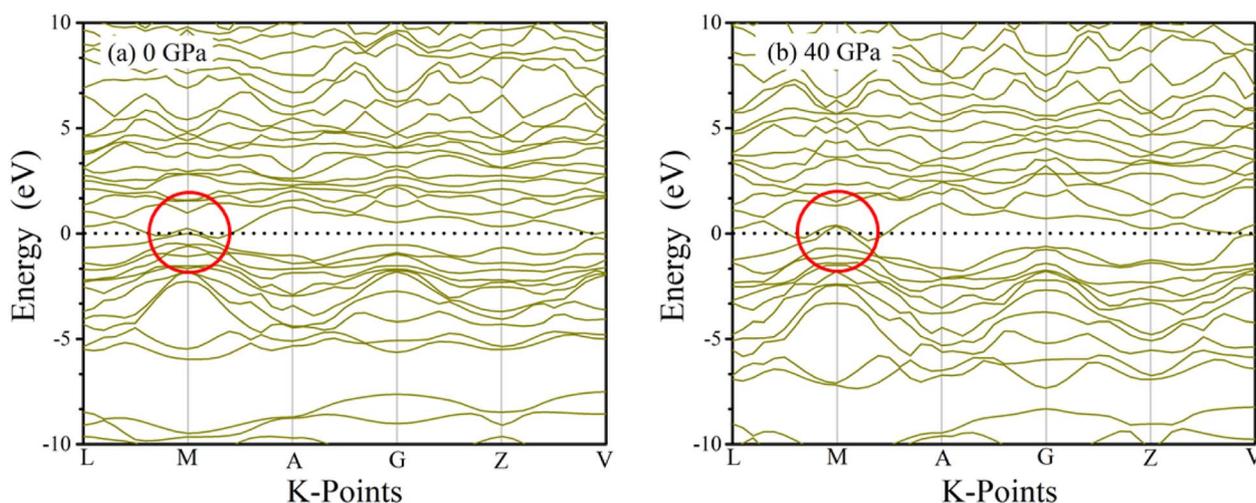


Fig. 7 Simulated electronic band structures of topological semi-metal TaSb₂ at 0 and 40 GPa pressure.

zero for all of the compounds. In this region, TaAs₂ acts similarly to other transparent materials. The substance's dielectric properties hardly change when applied with external pressures. The imaginary component of dielectric function intrinsically linked to the optical absorption profile.⁷² Because of how little pressure affects a dielectric's absorption spectra, dielectric functions are practically pressure-invariant.

The reflectivity curve provides crucial information regarding a material's suitability as a reflector. Fig. 9(d) and 10(d) show the reflectivity spectra up to 30 eV photon energy for TaM₂ (M = As, Sb) material's under different applied pressures. For TaAs₂ reflectivity starts with 0 eV and rises while increasing photon energy, reaching a highest value at ~8.80 eV. It becomes flat towards 9–17 eV, which belongs to the UV area. Above 17 eV, it diminishes and eventually goes to zero. For TaSb₂, the photon energy at which reflection is maximal is zero, and it decreases precipitously to its minimum at about 1.36 eV. After reaching a maximum at 7.67 eV, the reflectance remains constant

throughout a large portion of the ultraviolet spectrum, from 8 to 16 eV, before decreasing at 16 eV. Based on these findings, TaM₂ (M = As, Sb) can be used as an effective reflector throughout a broad spectrum of ultraviolet light.

The optical conductivity of topological semi-metal TaM₂ (M = As, Sb) under different pressures up to 30 eV photon energies are shown in Fig. 9(e), (f), 10(e) and (f) in both real and imaginary portions respectively. The acquired optical photoconductivity spectra exhibit both a maximum and a minimum within the studied energy range. For TaAs₂ and TaSb₂, their highest values are at 5.25 eV and 4.70 eV, respectively, and at energies above 5.30 eV and 4.90 eV, *i.e.*, conductivity changes to the greater energy area as a function of pressure. The conductivity then gradually decreases and drops to a minimum with rising photon energy. For both substances, the imaginary component of the conductivity follows the same behavior upon incoming radiation before flattening off at higher energies. According to



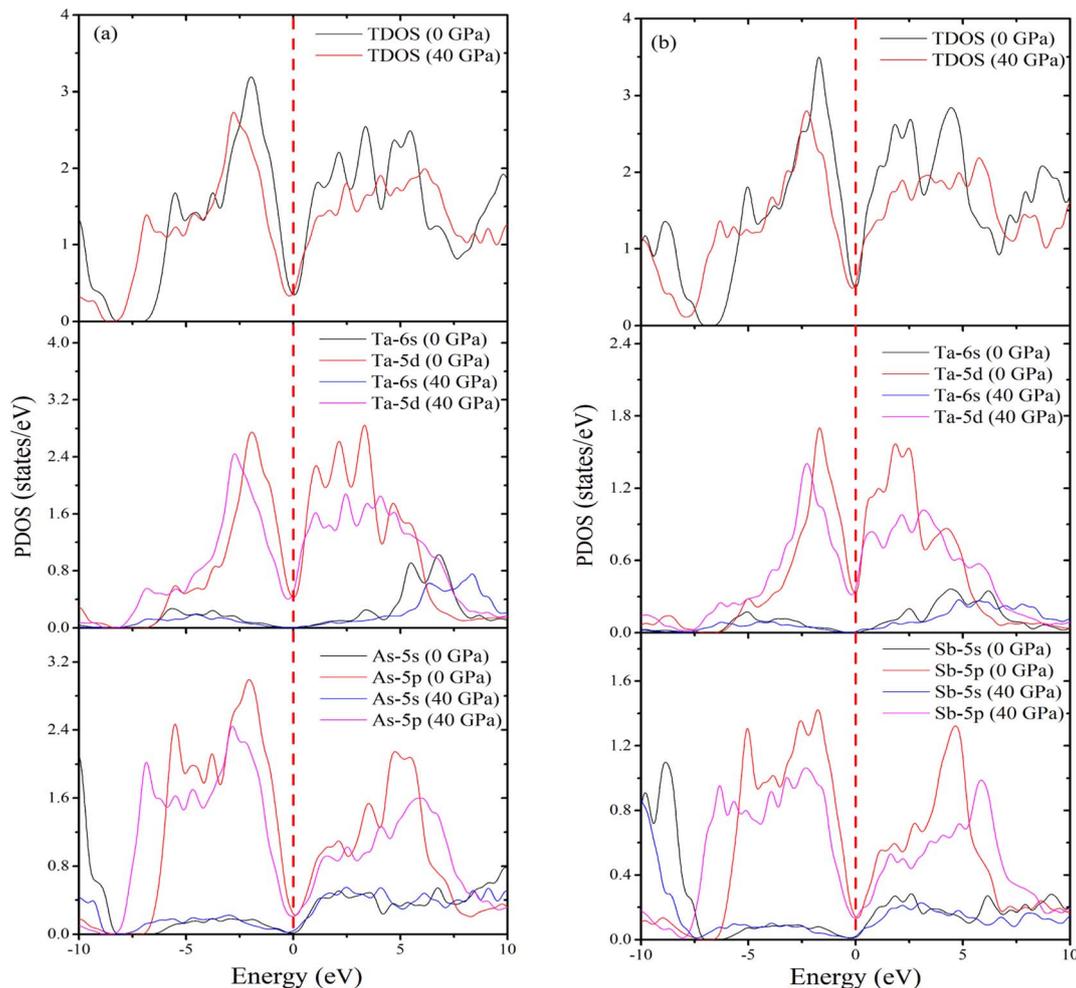


Fig. 8 Calculated (a) TDOS and PDOS (Ta and As) of TaAs₂ and (b) TDOS and PDOS (Ta and Sb) of TaSb₂ as a function of pressure.

this study, photon absorption improves the photoconductivity of TaM₂ (M = As, Sb) compounds.⁷³

The loss function determines how much energy of an electron loses as it moves in the whole substance. Fig. 9(g) and 10(g) display the energy loss curve for TaM₂ (M = As, Sb) compounds. The energy loss function shows how an electron loses energy as it moves quickly in a material.⁷⁴ The maximum loss function is linked to the plasma oscillation and plasma frequency ω_p .⁷⁵ The maximum loss function for TaAs₂ is found to be 23.23 eV for 40 GPa. Similarly, these value for TaSb₂ is 21.75 eV at 40 GPa. The plasma frequency of TaM₂ (M = As, Sb) molecules is inferred from these measurements. When the light's frequency is higher than the frequency of the plasma, the TaM₂ materials become transparent. In addition, a metallic system's optical characteristics transform into a dielectric-like behavior above the plasma energy.⁷⁶ As pressure rises, the peak of the loss function moves to a greater energy level. This makes it possible to study the optical reflectivity and absorption profile. When the peak moves to higher energies due to more pressure, the number of effective electrons for intraband and interband transitions gradually decreases.⁷⁷ The refractive index of

a material is a non-dimensional metric that is used to describe how fast light moves through it. The real portion of the refractive index is equivalent to the phase velocity, while the imaginary portion is similar to the extinction coefficient. Its imaginary portion also describes a material's dissipation of energy before complete absorption. The real and imaginary components of the refractive index for the topological semi-metal TaM₂ (M = As, Sb) are shown in Fig. 9(h), (i), 10(h) and (i) with zero photon energy, the real component of the refractive indices is found to have a maximum value of approximately 6.28 for TaAs₂ and 15.27 for TaSb₂. Above this energy, the real component declines and reaches a minimum value of about 18.06 and 12.57 before becoming flat for both substances in the upper energy area. In the imaginary parts, the refractive index values start to rise and reaches maximum values at 4.88 and 4.38 for TaAs₂ and TaSb₂, respectively. At a higher energy region, these values decrease and become flat.

3.5 Thermodynamic properties

Thermodynamic parameters play a crucial role in the study of modern solid-state physics and thermodynamic sciences.⁷⁸ The



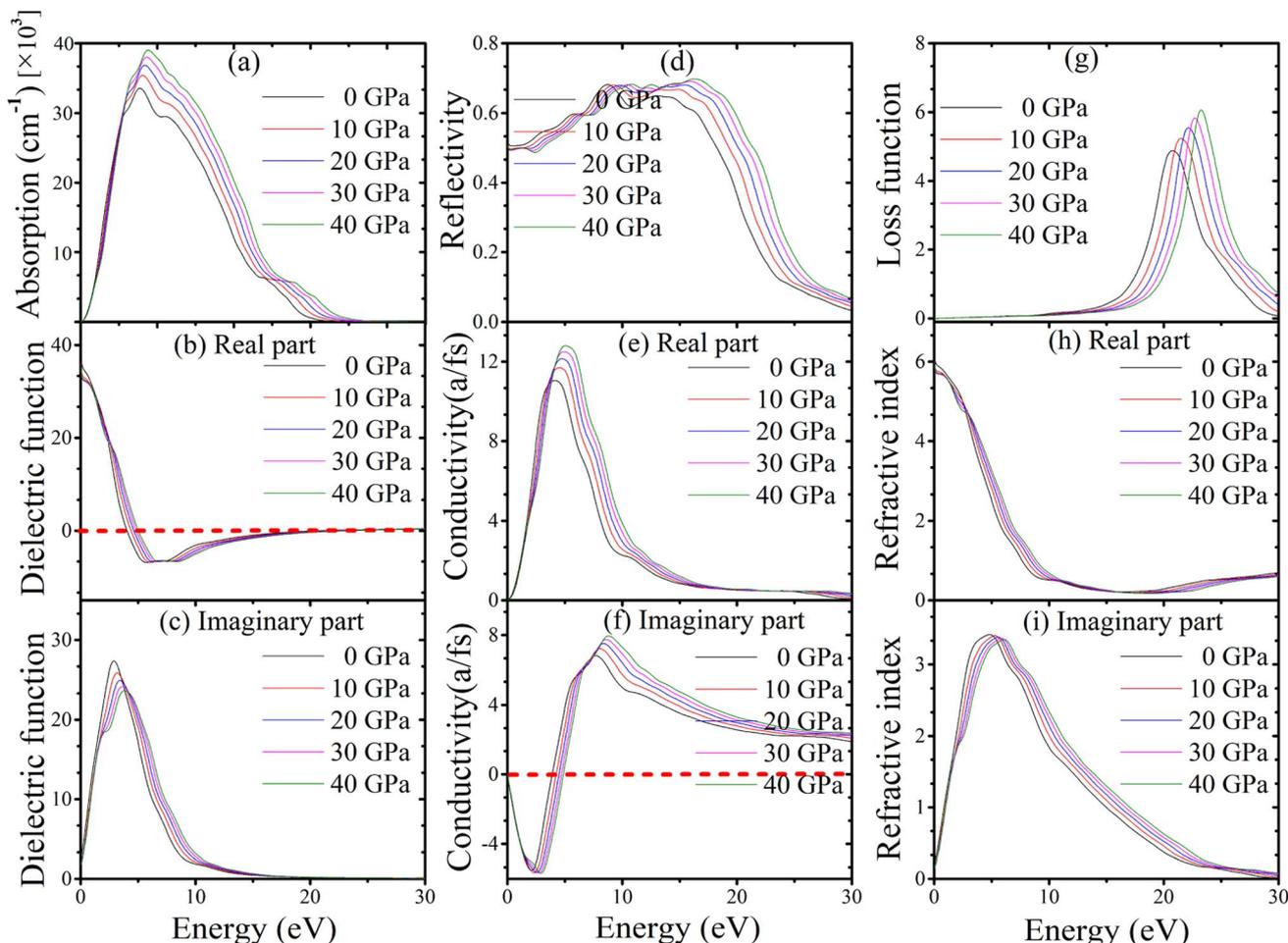


Fig. 9 (a) Absorption, (b and c) dielectric function, (d) reflectivity, (e and f) conductivity, (g) loss function, (h and i) refractive index of topological semi-metal TaAs₂ in [100] direction as a function of pressure.

melting point, bond strength, thermal expansion, specific heat, and elastic constants are only few of the numerous physical properties of materials that are intimately connected to the Debye temperature.⁷⁹ It demonstrates how the crystal responds to vibration. Here, we use optimized crystal properties to determine the Debye temperature of the topological semi-metal TaM₂ (M = As, Sb) under pressure. The θ_D can be measured *via* the equation:⁸⁰

$$\theta_D = \frac{h}{k} \left[\frac{3n}{\pi} \left(\frac{N_A \rho}{M} \right) \right]^{\frac{1}{3}} v_m \quad (20)$$

Using the following equation, the average sound velocity v_m can be calculated:⁸¹

$$v_m = \left[\frac{1}{3} \left(\frac{2}{v_t^3} + \frac{1}{v_l^3} \right) \right]^{-\frac{1}{3}} \quad (21)$$

The transverse sound velocity v_t and longitudinal sound velocity v_l can be determined using Navier's relation:⁸²

$$v_t = \left(\frac{G}{\rho} \right)^{\frac{1}{2}} \quad (22)$$

and

$$v_l = \left(\frac{3B + 4G}{3\rho} \right)^{\frac{1}{2}} \quad (23)$$

here h represent Planck's constant, n represent the number of atoms in a molecule, k represent Boltzmann's constant, N_A represent the Avogadro number, ρ is the density of the solid, M is the weight of the molecule, and v_m is the average speed of sound in a given medium.

The calculated values of ρ , v_t , v_l , and θ_D at various applied pressures are shown in Table S9.† From Table S9† it is evident that v_t , v_l , and θ_D rise with rising pressure for all the studied compounds, whereas for TaAs₂ the v_l (m s⁻¹) and v_m (m s⁻¹) values slightly decrease at 20 GPa. The ground state density ρ , transverse velocity v_t , longitudinal velocity v_l , mean sound velocity v_m , and Debye temperature θ_D of different topological semi-metals are listed in Table S10.† These values demonstrate a comparison between the results of



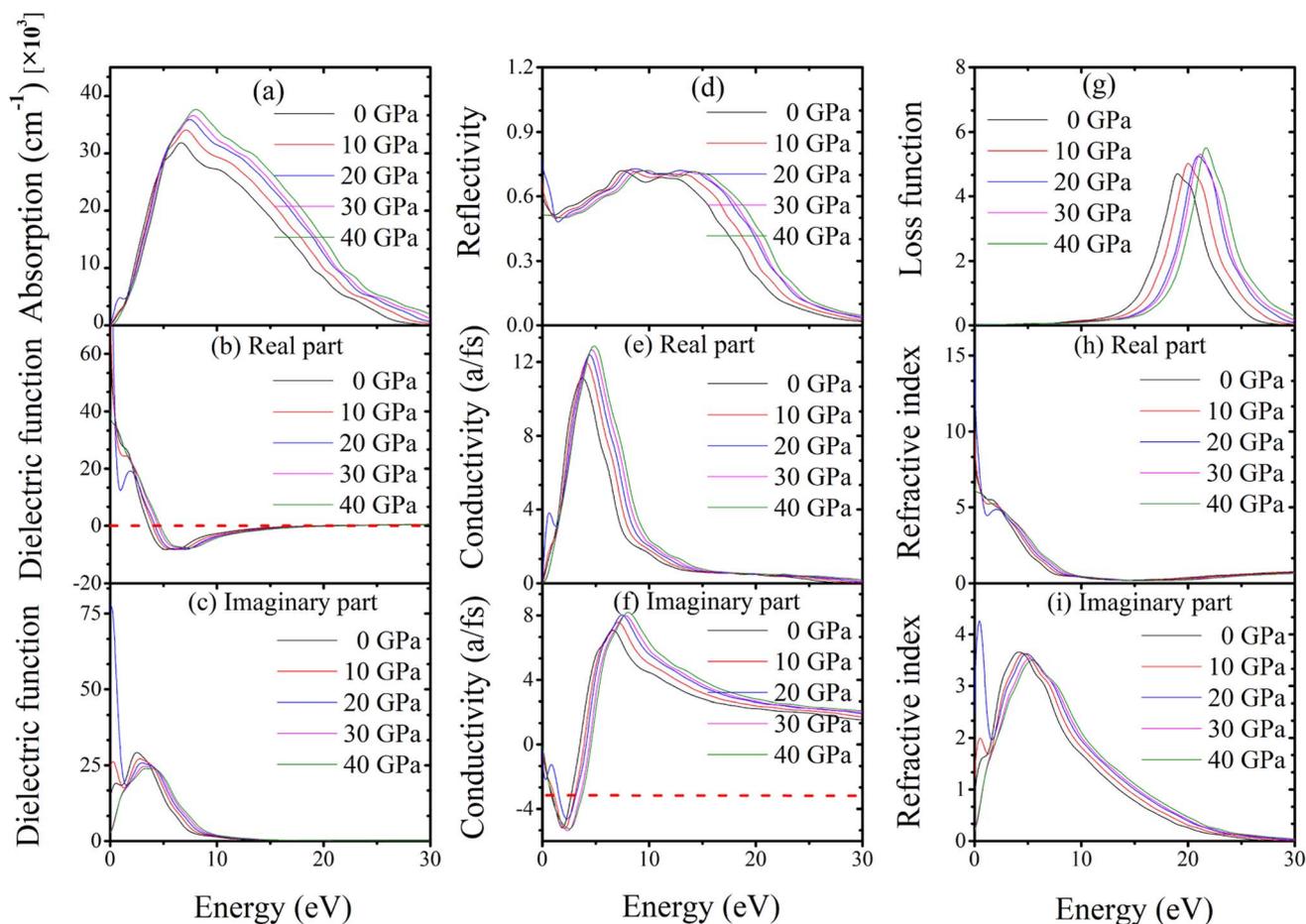


Fig. 10 (a) Absorption, (b and c) dielectric function, (d) reflectivity, (e and f) conductivity, (g) loss function, (h and i) refractive index of topological semi-metal TaSb₂ in (100) direction, as a function of pressure.

this work and those obtained from simulations of several topological semi-metals. Fig. 11(a) and (b) shows the fluctuation in Debye temperature θ_D as a function of hydrostatic

pressure. The predicted Debye temperature for both compounds was high, indicating that high melting points will be found.

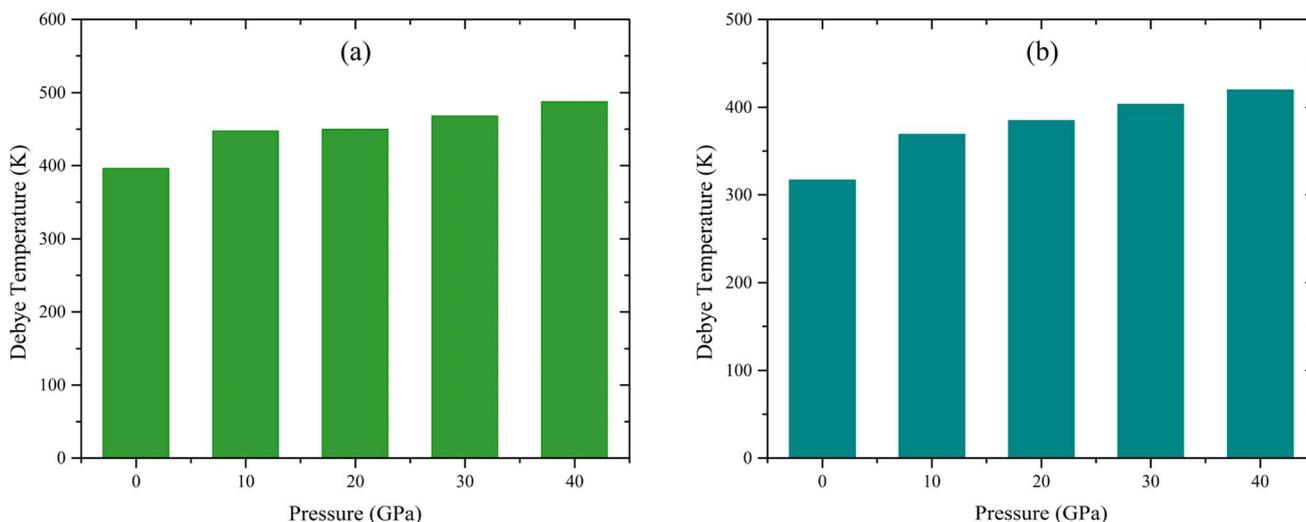


Fig. 11 Influence of pressure on Debye temperature, θ_D for (a) TaAs₂ and (b) TaSb₂ respectively.



4. Conclusion

In this work, we used first-principles DFT-based calculations in the generalized gradient approximation to study the topological semimetal TaM_2 ($M = As, Sb$) at pressures up to 40 GPa to look at a wide range of physical features (structural, elastic, mechanical, optical, electronic, and Debye temperatures). The lattice constants and the unit cell volume both decrease as the pressure is increased because of the decreasing interatomic distances. There is a strengthening of the ionic, covalent, and metallic bonding in compounds under pressure. The formation energy and Born stability criterion verified the mechanical and thermodynamic stability of the investigated molecules. As pressure increases, elastic constant values increase, making materials stiffer and more resistant to deformation, which can be employed in engineering applications. Poisson's and Pugh's ratio indicating both materials are brittle at ambient pressure but become increasingly ductile from 30 GPa to 40 GPa. The hardness value of both compounds improves with increasing pressures, but $TaAs_2$ is significantly harder than $TaSb_2$. Many direction-dependent characteristics of the compounds demonstrate their anisotropy (shear anisotropy, bulk anisotropy, equivalent Zener anisotropy, universal anisotropy). We also examine and explain several mechanical properties for all the studied compounds using the relevant formulas. Direction-dependent contour graphs show that pressure enhances TaM_2 ($M = As, Sb$) anisotropy. TaM_2 ($M = As, Sb$) are Weyl semi-metals due to the small band gap between the valence and conduction bands, which makes it possible to make new electronic devices with high mobility and low dissipation. The DOS indicates a substantial peak for electron crossing at the Fermi level and pressure has no influence on it for both materials. With rising external pressure, absorption coefficient and reflectivity increase. The dielectric function hardly changes with the applied pressure. The reflectance remains constant across a large portion of the ultraviolet spectrum, making it a good reflector across a wide range of ultraviolet light. For both compounds, an increase in pressure causes a rise in the measured density, sound velocity and the Debye temperature, signifying a strengthening of the covalent bonds. As a result, this analysis suggests that applying pressure is a thermodynamically efficient and ecologically favorable way to change material's physical characteristics for the advancement of electrical and spintronic applications.

Conflicts of interest

The authors declare no conflict of interests.

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