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# Tunable ultra-broadband terahertz metamaterial absorber based on vanadium dioxide strips

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A simple design of an ultra-broadband metamaterial absorber (MMA) of terahertz (THz) radiation based on vanadium dioxide (VO<sub>2</sub>) configurations is proposed. The system is composed of a top pattern representing orderly distributed VO<sub>2</sub> strips, a dielectric spacer and an Au reflector. Theoretical analysis based on the electric dipole approximation is performed to characterize the absorption and scattering properties of an individual VO<sub>2</sub> strip. The results then are used to design an MMA composed of such configurations. It is shown that the efficient absorption characteristics of the Au–insulator–VO<sub>2</sub> metamaterial structure can be ensured in a broad spectrum of 0.66–1.84 THz with an absorption band relative to the center frequency reaching as high as 94.4%. The spectrum of the efficient absorption can be easily tuned via the corresponding choice of strip dimensions. Wide polarization and incidence angle tolerance for both transverse electric (TE) and transverse magnetic (TM) polarizations are ensured by adding an identical parallel layer rotated by 90 degrees in respect to the first one. Interference theory is applied to elucidate the absorption mechanism of the structure. The possibility of modulation of the electromagnetic response of MMA relying on the tunable THz optical properties of VO<sub>2</sub> is demonstrated.

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## Introduction

During the past two decades, the rapid development of high-frequency communication, medical, and sensing technologies attracted huge attention towards the terahertz spectrum of electromagnetic waves.<sup>1,2</sup> Various metamaterial structures, representing periodic arrays of subwavelength unit cells, have been proposed to fill the technological gap of devices working in this spectrum. In particular, numerous metastructures for the amplitude and phase manipulation of the electromagnetic waves with applications in perfect absorption,<sup>3–5</sup> sensing,<sup>6–8</sup> focusing, filtering, polarization conversion,<sup>9–14</sup> imaging,<sup>15</sup> and modulation<sup>16,17</sup> have been developed. Among these, perfect absorbers play a significant role in applications spanning from energy harvesting and detection to thermal emission.<sup>18,19</sup> Depending on the spectral characteristics of the absorptance, single band, multiband and broadband MMAs are distinguished. To engineer an absorption band with various spectral properties, several common strategies are employed. For instance, single-band absorption can be easily ensured by simple unit-cell configurations, such as split-ring resonators, patches, and cut wires. Multi-band or broadband absorption characteristics can be engineered either by combining elements which are identical in shape but individually vary in size or different in shape.<sup>20–23</sup> Moreover, the resonators can be

arranged whether on the top surface of a unit cell (all in one plane) or stacked in a vertical direction. In ref. 23 the authors designed a polarization-insensitive MMA, where the relatively broad absorption band is due to merging the individual resonances of the double-open rectangular ring and strip cross-shape resonators both arranged on a unit-cell surface. On the contrary, in ref. 24 broadband absorption is engineered by utilizing a number of conductive bars of varying lengths stacked on three polyimide layers. Finally, the MMA presented in ref. 25 demonstrates broadband absorption by dividing the complete square ring structure into four sections and varying the characteristic size of each section. In general, the design of metamaterial absorbers includes metals as a reflector or resonator material. Although in the visible or infrared range, metals are characterized by high dispersion, at terahertz frequencies the conductivity of most metals is of the order of 10<sup>6</sup>–10<sup>7</sup> S m<sup>−1</sup>, which does not provide wide control possibilities. In order to dynamically control the response of a metamaterial in the terahertz range, materials sensitive to an external stimulus (temperature, voltage, *etc.*) are used either as a spacer or resonator medium.<sup>26</sup> For example, several semiconductors, such as Si and GaAs are characterized by pronounced photoactivity, making their material properties sensitive to external optical pumping.<sup>27,28</sup> Graphene is another material whose conductivity can be effectively manipulated by an external voltage.<sup>26,29</sup> Another way to achieve tunable electromagnetic response is by making use of a phase-changing material. VO<sub>2</sub> is a common phase-changing material exhibiting an insulator-to-metal

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transition near  $\sim 67^\circ\text{C}$  temperature resulting in a high conductivity of about  $2 \times 10^5 \text{ S m}^{-1}$ . Consequently, by controlling the temperature, it is possible to change the conductivity of  $\text{VO}_2$  in a wide range, which gives wide control over metamaterials.<sup>30,31</sup>

In this paper efficient broadband terahertz (THz) absorption of an elongated elliptical subwavelength configuration made of  $\text{VO}_2$  is investigated. The electric-dipole approximation is used to demonstrate the absorption enhancement of an elongated ellipsoid arising due to configurational resonance associated with a special combination of material properties and geometrical parameters. Finite element method-based simulations are conducted for a rectangular strip as an equivalent configuration for elongated oblate ellipsoid. It is shown that ordered arrangement of such strips on a surface of an Au-backed dielectric layer provides an absorption band exceeding 90% in a wide frequency range from 0.66 to 1.84 THz with the absorption bandwidth (BW) of  $\sim 1.18$  THz. The bandwidth relative to the center frequency of the absorption band (RBW) is  $\sim 94.4\%$ . Owing to controllable THz optical conductivity of  $\text{VO}_2$  the absorbance can be modulated from 0 up to 100% by varying the surrounding temperature.  $\text{VO}_2$  also provides an efficient platform for optimization and establishing prospective material characteristics for near-perfect absorption. Interference theory is applied to reveal the absorption mechanism.

## Theory

Let a prolate ellipsoid with semi-axes  $a_z \gg a_y > a_x$ , complex dielectric permittivity  $\varepsilon_1$  and embedded in a lossless dielectric medium  $\varepsilon_2$  be illuminated by a plane wave polarized along the largest semi-axis  $a_z$ . Considering the configuration in the quasi-static limits, *i.e.*, when the largest semi-axis of a prolate ellipsoid satisfies the inequality condition  $ka_z \ll 1$ , where  $k$  is the wavenumber in the surrounding medium  $\varepsilon_2$ , the dipole moment of a configuration is determined as:<sup>32</sup>

$$\mathbf{p} = \varepsilon_0 \varepsilon_2 V \chi \mathbf{E}, \quad (1)$$

where  $\varepsilon_0$  is the dielectric constant of vacuum,  $V$  is the configuration volume,  $\mathbf{E}$  is the incident wave electric field and  $\chi$  is defined as<sup>33,34</sup>

$$\chi = \frac{\varepsilon_1 - \varepsilon_2}{\varepsilon_2 + (\varepsilon_1 - \varepsilon_2)n^{(i)}}. \quad (2)$$

Here  $n^{(i)} \approx \eta \gamma \ln(1.5/\eta)$  depends only the shape and sizes of a configuration,  $\gamma = a_x/a_z$  and  $\eta = a_y/a_z$ . The electric dipole polarizability of a configuration then has the following form:

$$\alpha = \varepsilon_0 V \chi \approx \frac{4\pi\varepsilon_0}{3} \times \frac{a_z^3}{\ln(1.5/\eta)} \times \frac{(\varepsilon_1 - \varepsilon_2)\eta\gamma \ln(1.5/\eta)}{\varepsilon_2 + (\varepsilon_1 - \varepsilon_2)\eta\gamma \ln(1.5/\eta)}. \quad (3)$$

The absorption and scattering cross-sections of a particle can be defined as follows:<sup>32</sup>

$$\sigma_{\text{abs}} = \frac{k}{\varepsilon_0} \text{Im}(\alpha), \quad (4)$$

$$\sigma_{\text{scat}} = \frac{k^4}{6\pi\varepsilon_0^2} |\alpha|^2. \quad (5)$$

For quantitative analysis the absorption and scattering properties are normalized by the longitudinal geometrical cross-section area  $S = \pi a_y a_z$ . The corresponding quantities called absorption and scattering efficiencies are:<sup>35</sup>

$$Q_{\text{abs}} = \frac{\sigma_{\text{abs}}}{S} \text{ and } Q_{\text{scat}} = \frac{\sigma_{\text{scat}}}{S}. \quad (6)$$

## Results and discussion

Analysis of the interaction of the elongated ellipsoidal sub-wavelength particles with plane electromagnetic waves shows that maximum absorption and minute scattering are achieved when the magnitude of the real part and the imaginary part of the dielectric permittivity of the spheroid medium are of the same order. Conductivities, and hence the imaginary part of the dielectric permittivities of common metals (such as Au, Ag, Cu, *etc.*) noticeably exceed the real part in magnitude as the frequency decreases. However, phase-changing materials can be exploited as their THz optical properties can be effectively manipulated by an external stimulus. Particularly,  $\text{VO}_2$  can undergo reversible phase transition from an insulator phase at the room-temperature to a 'poor' metallic phase at characteristic temperatures of  $\sim 65\text{--}75^\circ\text{C}$ . The complex dielectric permittivity of  $\text{VO}_2$  in its metallic phase in the THz spectrum can be described according to Drude model,<sup>31</sup>

$$\varepsilon(\omega) = \varepsilon_\infty - \frac{(\omega_p(\sigma_1))^2}{\omega^2 + i\gamma\omega}, \quad (7)$$

$$\omega_p^2(\sigma) = \frac{\sigma}{\sigma_0} \omega_p^2(\sigma_0), \quad (8)$$

where  $\varepsilon_\infty$  is the high-frequency permittivity,  $\omega_p(\sigma)$  is the conductivity-dependent plasma frequency,  $\gamma$  is the collision frequency,  $\omega_p(\sigma_0) = 1.4 \times 10^{15} \text{ rad s}^{-1}$  and  $\sigma_0 = 3 \times 10^5 \text{ S m}^{-1}$ . The real (black, left axis) and imaginary (red, right axis) part of the dielectric permittivity of the  $\text{VO}_2$  in its metallic phase at THz frequencies are shown in inset of Fig. 1, where experimentally derived values for the high-frequency permittivity, plasma frequency and damping factor were used:<sup>31</sup>  $\sigma = 2 \times 10^5 \text{ S m}^{-1}$ ,  $\omega_p = 1.14 \times 10^{15} \text{ rad s}^{-1}$ , and  $\gamma = 5.75 \times 10^{13} \text{ rad s}^{-1}$ . It is seen that for the chosen conditions, the real part of the dielectric permittivity of  $\text{VO}_2$  is negative indicating its metallic nature.

Analytical relation (3) derived within the quasistatic limits represents the depolarization factor of an oblate ellipsoid whose scattering and absorption efficiencies are shown in Fig. 1 by red and black solid lines, respectively.  $\text{VO}_2$  is used as a strip material and the surrounding medium is air.

Both the absorption and scattering efficiencies gradually increase as the frequency increases, however, the absorption is noticeably larger than the scattering and is around 10 at frequencies above 1 THz, whereas the  $Q_{\text{scat}}$  is about 0.3. This



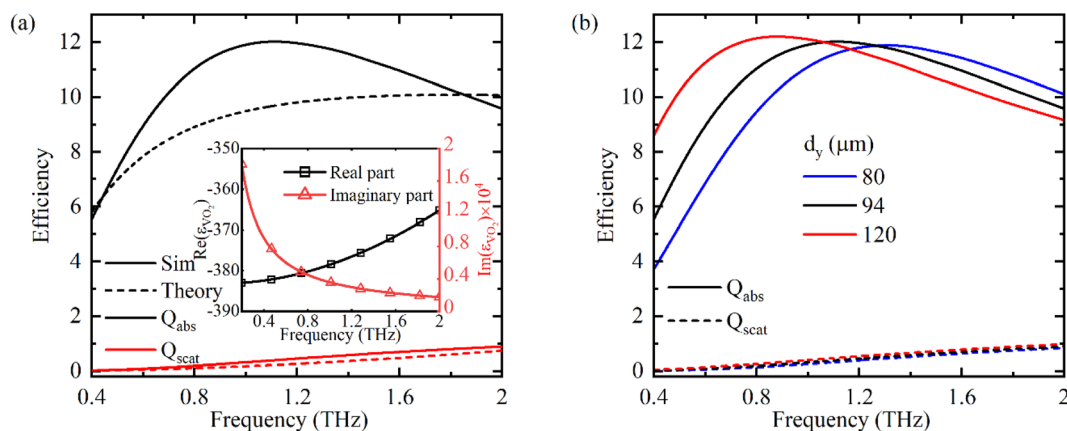


Fig. 1 (a) Theoretical (dashed) and simulated (solid) absorption (black) and scattering (red) efficiency factors of ellipsoid- and strip-like VO<sub>2</sub> configurations. The geometrical parameters for ellipsoid-strip are:  $a_x = d_x/2 = 0.5 \mu\text{m}$ ,  $a_y = d_y/2 = 47 \mu\text{m}$  and  $a_z = d_z/2 = 100 \text{ nm}$ . (b) Absorption (solid lines) and scattering (dashed lines) efficiency spectra of strips with different height  $d_y$ . Other geometrical sizes were kept constant.

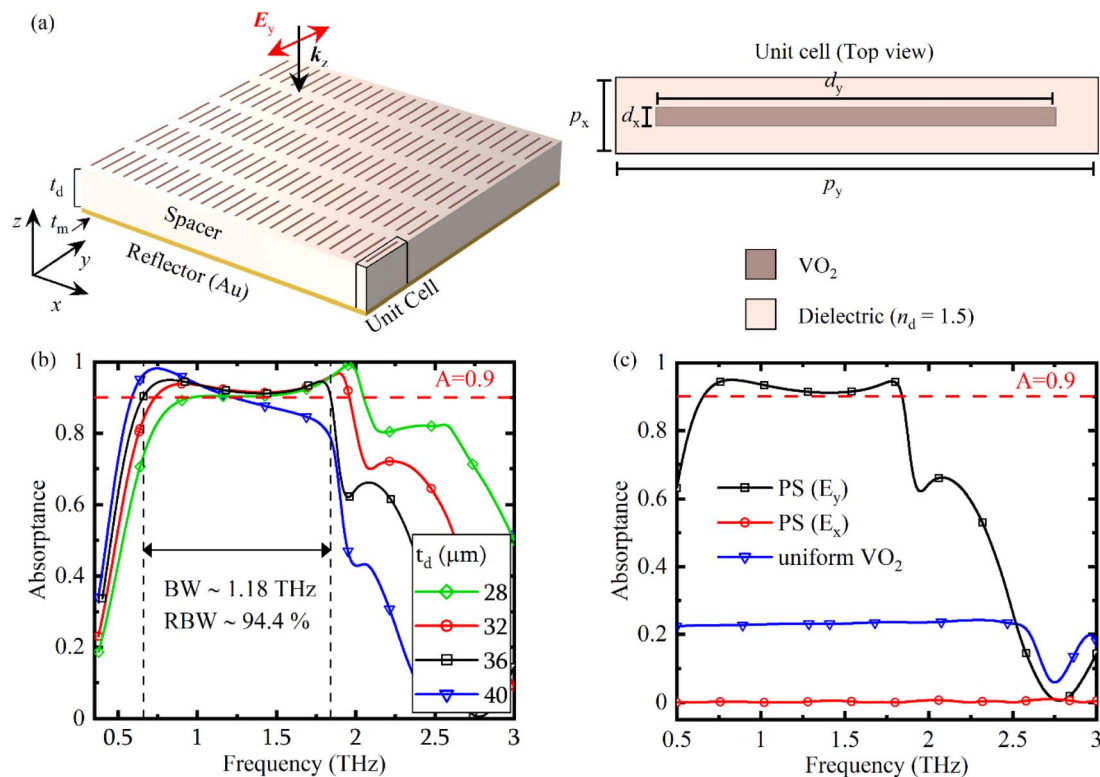
means that the functional scattering surface of the configuration is much smaller than its geometrical cross-section. However, from a standpoint of integration with planar surfaces, a strip-like configuration can be promising also due to the fact that it is more straightforward for possible fabrication. Hence, hereinafter we use a strip-like configuration with identical geometrical parameters as those of an ellipsoid: the side lengths of the strip  $d_i$  in each coordinate direction are related to the semi-axes  $a_i$  of the ellipsoid by the relation  $d_i = 2a_i$ , where  $i = x, y, z$ .

Three-dimensional full-wave numerical simulations based on the finite element method were conducted to analyze the absorption and scattering properties of a VO<sub>2</sub> strip. Absorption and scattering efficiencies of a strip are shown in Fig. 1 by black and red dashed lines, respectively. While the scattering properties of both configurations are similar, certain differences are observed between the absorption spectra. In particular, the absorption efficiency spectrum of a strip has resonant nature with a maximum value of about 12 at 1 THz. Here one should note that although the difference between the lateral cross-section areas of a strip and an ellipsoid is small, the volume of a strip is almost twice as large as that of the ellipsoid, which results in an increased absorption efficiency. Comparison of the simulated absorption and scattering properties of VO<sub>2</sub> strips with  $d_y$  values of 80, 94 and 120 μm are shown in Fig. 1(b). Solid lines stand for the absorption and dashed lines – for the scattering efficiency. As expected, a spectral shift towards lower frequencies is observed as  $d_y$  increases. At the same time, the peak value of the absorption efficiency is almost constant and is around 12. Moreover, the scattering efficiency is negligibly small even when at the largest considered case of  $d_y = 120 \mu\text{m}$  and barely reaches 0.4 at the peak frequency of 0.8 THz. In these calculations,  $d_x$  and  $d_z$  are as for Fig. 1(a). Once the conditions for the enhanced absorption dominating over the scattering are established for an individual strip-like configuration, we used the results above to design a VO<sub>2</sub>-dielectric-metal metamaterial for near-perfect broadband absorption of the THz irradiation. The metamaterial is composed of planar layers of an Au reflector and a dielectric spacer with  $n_d = 1.5$ . We want to

mention that the dielectric properties of a number of polymer materials, such as polypropylene<sup>36</sup> and polyethylene cyclic olefin copolymer<sup>37</sup> are suitable to use as a spacer. The third layer represents an array of VO<sub>2</sub> strips periodically distributed on the top surface of a dielectric layer. A three-dimensional view of a metamaterial and the top view of the unit cell are depicted in Fig. 2(a).  $t_m$  and  $t_d$  are the thicknesses of the bottom reflector and spacer, respectively,  $p_x$  and  $p_y$  are periodicities along the indicated directions, and  $d_x$  and  $d_y$  are the lateral dimensions of the strip. We used the optimized dimensions for strips and changed the periodicities and spacer thickness to achieve an efficient broad absorption band corresponding to the absorbance equal to or larger than 90%. Generally, the absorbance of the metamaterial is defined as  $A = 1 - R - T$ , where  $R$  and  $T$  are reflectance and transmittance. The latter are defined *via* frequency-dependent scattering parameters as  $R = |S_{11}(f)|^2$  and  $T = |S_{21}(f)|^2$ . Since the transmission through the structure is blocked by a 3 μm-thick bottom Au layer ( $T = 0$ ), which is much larger than its skin-depth ( $\delta_{s,Au} \sim 100 \text{ nm}$  around 1 THz), the absorption coefficient is expressed only through the reflectance as  $A(f) = 1 - R(f)$ . The absorption performance of the proposed system is investigated under the y-polarized plane wave. Fig. 2(b) plots the absorption spectrum for spacer thicknesses of 28 μm (green, diamonds) 32 μm (red, rings), 36 μm (black, squares) and 40 μm (blue, triangles). The sizes of a strip are chosen as in Fig. 1. As the spacer thickness decreases, the absorbance at lower frequencies drops below 0.9 level and a rising tendency of the absorbance at higher frequencies is observed. For instance, the efficient absorption band ( $A \geq 0.9$ ) for  $t_d = 28 \mu\text{m}$  is  $\sim 1.11 \text{ THz}$  (from 0.94 up to 2.05 THz), and that of  $t_d = 40 \mu\text{m}$  is  $\sim 0.72 \text{ THz}$  (from 0.59 up to 1.31 THz).

A compromise between the efficient absorption bandwidth and average absorbance above 0.9 is achieved for  $t_d = 36 \mu\text{m}$ . In this case, efficient absorption is achieved from 0.66 up to 1.84 THz with the absorption BW  $\sim 1.18 \text{ THz}$ . The average absorbance is about 0.93. Another criterion for the absorption performance is the relative bandwidth defined as  $\text{RBW} = \text{BW}/f_c \times 100\%$ , which is about 94.4%. Although at  $t_d = 32 \mu\text{m}$  the absolute absorption BW (1.22 THz) is slightly larger than that of





**Fig. 2** (a) 3D schematic of the periodic structure composed of an Au reflector, dielectric spacer with  $n_d = 1.5$  and rectangular VO<sub>2</sub> strips as a unit-cell element; and the top-view of the unit cell,  $t_m$  and  $t_d$  are the thickness of the reflector and spacer, respectively. (b) The absorption spectrum as a function of the thickness of the dielectric spacer. The geometrical parameters are as follows:  $t_d = 36 \mu\text{m}$ ,  $t_m = 3 \mu\text{m}$ ,  $p_x = 6 \mu\text{m}$ ,  $p_y = 114 \mu\text{m}$ ,  $d_x = 200 \text{ nm}$ ,  $d_y = 94 \mu\text{m}$ . (c) The absorption spectra of the periodic structure (PS) under x- and y-polarized plane waves (red and black lines, respectively), and the planar structure with strips replaced by a uniform VO<sub>2</sub> layer (blue line).

$t_d = 36 \mu\text{m}$  (1.18 THz), our choice of the optimal spacer thickness of  $36 \mu\text{m}$  is conditioned by the larger RBW and average absorbance of about 94.4% and 0.93, respectively, in contrast to 90% and 0.92 of the former case. Note that the total thickness of the optimized structure is  $39.2 \mu\text{m}$ , which is around one-sixth of the centre wavelength of the efficient absorption band.

The structural asymmetry of the unit cell element dictates certain polarization dependence of the absorbance. Shown in Fig. 2(c) in red (circles) and black (squares) are the absorption spectra of the PS under x- and y-polarized plane waves. It is noted that near-perfect broadband absorption is achieved only when the incident field polarization is parallel to the longest side of strips, whereas, under cross-polarized radiation, strips do not interact with electromagnetic waves which are completely reflected from the bottom Au layer. To find out how the strip-like pattern of the top interface affects the absorption characteristics of the system, in Fig. 2(c) we compared the absorbance of the main design of the MMA with that of a planar Au–dielectric–VO<sub>2</sub> structure (from bottom to top) shown by a blue-triangles line. The absorbance of the dielectric spacer sandwiched by  $3 \mu\text{m}$ -thick Au and  $200 \text{ nm}$ -thick VO<sub>2</sub> layers is around 0.22 at the entire considered spectrum up to 2.5 THz, whereas introducing rectangular strips noticeably enhances the absorbance ensuring near-perfect absorption characteristics. The absorption here is mainly conditioned by

the attenuation of the electromagnetic waves while passing forward and backward through a thin and lossy VO<sub>2</sub> top layer.

The next step includes optimization of the lateral sizes of the unit cell while keeping the strip sizes constant. The absorption spectra for different values of periodicities  $p_x$  and  $p_y$  are shown in Fig. 3(a) and (b), respectively. The absorption performance alters in a similar manner when either of the periodicities is increased, namely, the bandwidth is decreased and the overall absorbance is increased. The values of  $p_x = 6 \mu\text{m}$  and  $p_y = 114 \mu\text{m}$  were found to be optimal to ensure a broad efficient absorption band. Starting from  $p_y = 114 \mu\text{m}$ , a solid broad efficient absorption band is formed, and at larger values of  $p_y$  the average absorption constantly increases and the BW decreases. Such a behaviour can be attributed to reducing the coupling between neighbouring strips when their distance increases, which results in dominant configuration resonances of individual strips. Since all strips are identical, the resonance conditions also match. When the distance between strips is too large to establish coupling between neighbouring strips with a different frequency of the coupled system, resonant absorption bandwidth decreases.

From the results presented in Fig. 1(b), one sees that the corresponding choice of the strip dimensions can alter the absorption spectrum. Fig. 3(c) sums up the tunability of the efficient absorbance spectrum of the MMA by varying the unit





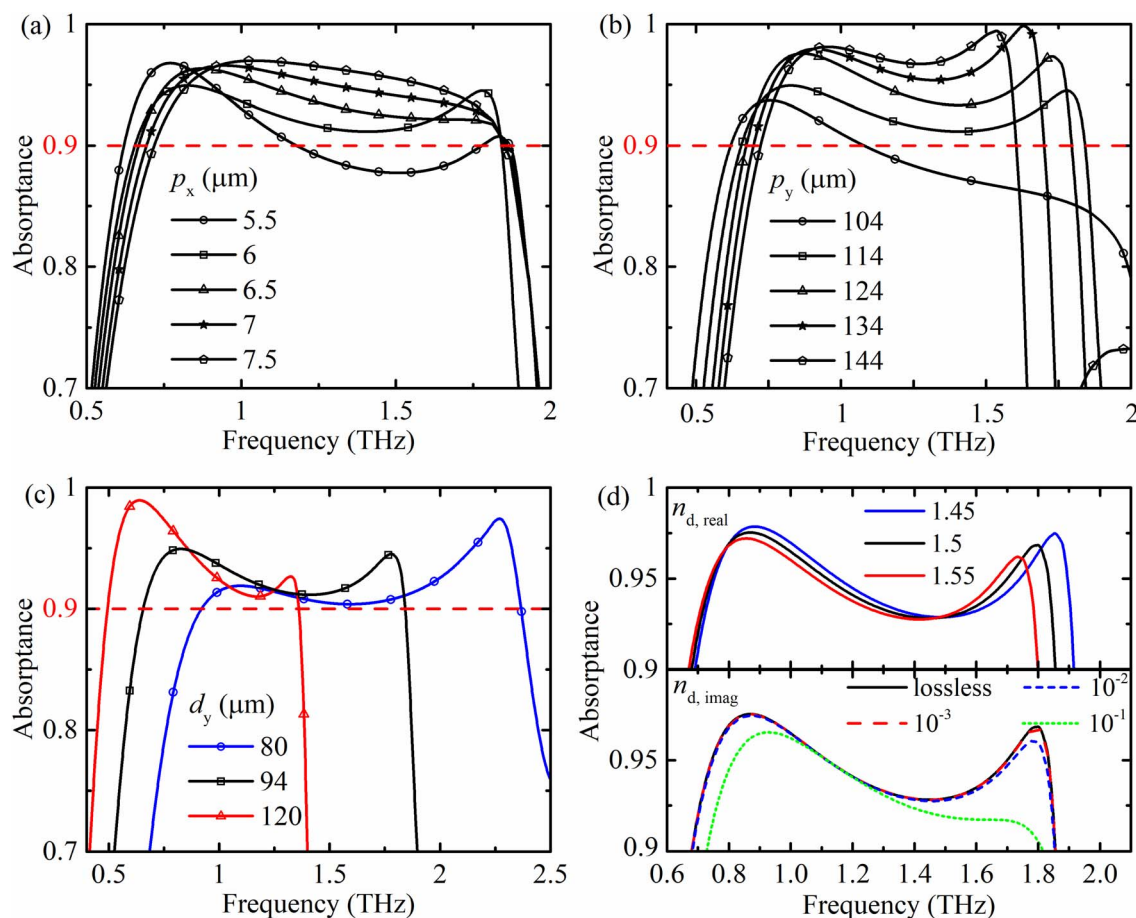


Fig. 3 The absorption spectrum at different values of unit-cell periodicities (a)  $p_x$  (5.5, 6, 6.5, 7, 7.5  $\mu\text{m}$ ) and (b)  $p_y$  (104, 114, 124, 134 and 144  $\mu\text{m}$ ). (c) Absorption spectra of the optimized periodic structures with strips having different  $d_y$  sizes. (d) The absorption spectra at different values of the real (top) and imaginary (bottom) parts of the spacer refractive index. The spacer is lossless in the top plot and the real part is 1.5 – in the bottom. The optimized sizes are: (i)  $d_y = 120\ \mu\text{m}$ ,  $p_y = 140\ \mu\text{m}$ ,  $t_d = 44\ \mu\text{m}$ , (ii)  $d_y = 80\ \mu\text{m}$ ,  $p_y = 95\ \mu\text{m}$ ,  $t_d = 26\ \mu\text{m}$ . Other parameters are as above.

cell element sizes. First, a strip length is chosen with other geometrical parameters of the strip fixed and then the unit-cell dimensions were optimized to achieve a relatively broad absorption band. In particular, shown by red (triangles), black (squares) and blue (rings) lines (symbols) are the absorption spectra for the MMA with  $d_y$  of 80, 94 and 120  $\mu\text{m}$ , respectively. One notes that the efficient absorption spectrum gradually shifts to the higher frequencies as the strip length decreases, also resulting in the broadening of the absorption band. For instance, at  $d_y = 120\ \mu\text{m}$  the absorption band lays in 0.49–1.36 THz, with the corresponding BW (RBW) of 0.87 THz (94%). On the other hand, the efficient absorption band at  $d_y = 80\ \mu\text{m}$  expands from 0.92 up to 2.37 THz, with BW (RBW) of 1.45 THz (88%). These results clearly demonstrate the tunability of the suggested periodic structure, in all the considered cases achieving relative bandwidths around 90%. Finally, the top and bottom plots in Fig. 3(d) show the absorption spectra at different values of the real and imaginary parts of the spacer refractive index, respectively. Although the absorption BW slightly increases as the real part of the refractive index decreases, our choice of the real part of the substrate refractive index is 1.5 since it is characteristic of many commercially

available polymers in the THz spectrum, such as polypropylene,<sup>36</sup> high-density polyethylene,<sup>36</sup> polyethylene cyclic olefin copolymer.<sup>37</sup> On the other hand, the absorption spectrum is mainly independent of the spacer dielectric losses, hence supporting the practical implementation and widening the possible choice of spacer materials.

To examine the physical concept of the absorption mechanism and theoretically validate our results, we adopt interference theory based on the modified Fabry–Perot resonant model. In this theory, a metamaterial absorber is represented as a Fabry–Perot resonator, where the ground reflector serves as a perfect mirror and the top interface of strips is a partially reflective mirror.<sup>38</sup> The schematic of the multiple reflections model within a metamaterial absorber is illustrated in Fig. 4(a). The plane electromagnetic wave impinging on the top interface of the metamaterial is partially reflected back to the air region and transmitted into the dielectric spacer with corresponding complex coefficients of  $r_{11} = |r_{11}|\exp(i\varphi_{11})$  and  $t_{21} = |t_{21}|\exp(i\varphi_{21})$ . The latter waves are then totally reflected from the ground reflector and then divide into reflected and transmitted waves upon incidence on the top interface from the spacer side with the transmission coefficient of  $t_{12} = |t_{12}|\exp(i\varphi_{12})$  and



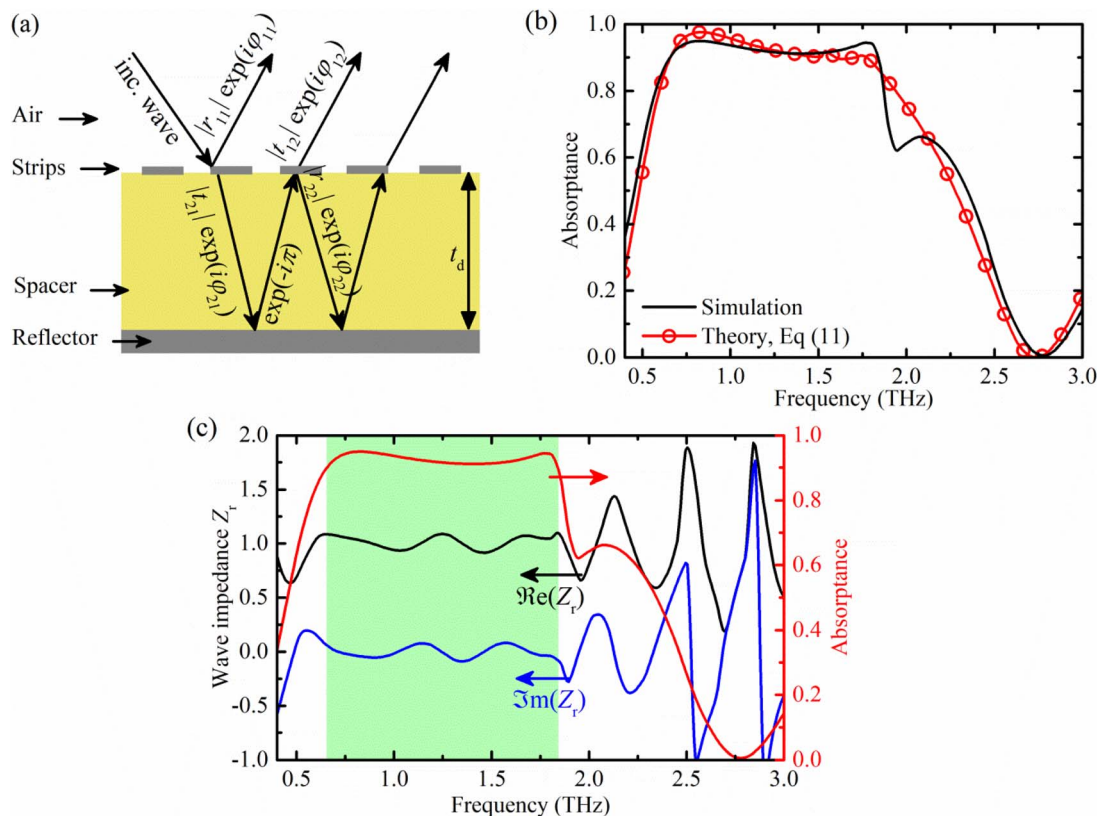


Fig. 4 (a) The schematic of the multiple reflections model within a metamaterial absorber. (b) Comparison of the absorptance of the proposed MMA derived via numerical simulations (black) and calculated by the interference theory, eqn (11) (red-rings). (c) The real and imaginary parts of the relative effective wave impedance of the absorber (left axis) and absorptance spectrum (right axis). The highlighted region corresponds to the efficient absorption spectrum.

reflection coefficient of  $r_{22} = |r_{22}|\exp(i\varphi_{22})$ . Here  $\varphi_{ij}$  represent the corresponding phase shift. The propagation phase is  $\beta = kh$ , where  $k$  is the wavenumber in the spacer and  $h$  is the path length of the beam inside the spacer. For a normal incidence  $h = t_d$ . According to the wave propagation theory in multilayer structures the total reflection coefficient of the layered system is determined as:<sup>38</sup>

$$r_{\text{total}} = r_{11} + t_{12}e^{-i\beta}r_{23}e^{-i\beta}t_{21} + t_{21}e^{-i\beta}r_{23}e^{-i\beta}t_{12}(r_{22}e^{-i\beta}r_{23}e^{-i\beta})^1 + \dots + t_{21}e^{-i\beta}r_{23}e^{-i\beta}t_{12}(r_{22}e^{-i\beta}r_{23}e^{-i\beta})^m. \quad (9)$$

Assuming that the reflection coefficient from the ground plane  $r_{23} = -1$  and applying some mathematical manipulations with the interaction number  $m \gg 1$ , the total reflection coefficient can be simplified to

$$r_{\text{total}} = r_{11} + \frac{t_{12}t_{21}e^{-i(2\beta+\pi)}}{1 - r_{22}e^{-i(2\beta+\pi)}}. \quad (10)$$

The absorption hence is conditioned by the destructive interference between all  $r_{11}$  and  $t_{12}$  waves (multiple transmissions from spacer–strips interface to air). Since the transmittance from the ground metal layer  $T = 0$ , the total absorptance of the metamaterial is defined as

$$A(\omega) = 1 - R(\omega) = 1 - |r_{\text{total}}|^2. \quad (11)$$

The complex reflection/transmission coefficients used in the interference theory were calculated via the so-called decoupled model.<sup>38</sup> The spectrum of the absorptance of the MMA calculated by eqn (7) of the interference theory and its comparison to that of obtained by simulation is shown in Fig. 4(b) by red-rings and solid black lines, respectively. One sees that the numerically and theoretically obtained results are in good agreement.

According to the impedance matching theory, a metamaterial structure perfectly absorbs the incident electromagnetic radiation when its complex effective wave impedance is matched to that of the wave impedance of the environment.<sup>31,38</sup> Hence, when the total reflectance  $R(\omega)$  of the structure approaches zero ( $A(\omega)$  approaches 1), the wave impedance tends to match that of the free space. The relative impedance can be calculated by the following expression

$$Z_r = \frac{Z(\omega)}{Z_0} = \pm \sqrt{\frac{(1+r(\omega))^2 - t^2(\omega)}{(1+r(\omega))^2 + t^2(\omega)}} \quad (12)$$

where  $r = S_{11}$ ,  $t = S_{21}$  are complex reflection and transmission coefficients,  $Z(\omega) = \sqrt{\mu(\omega)/\epsilon(\omega)}$  is the effective impedance of the metamaterial structure,  $\mu$  and  $\epsilon$  are the effective complex magnetic permeability and dielectric permittivity of the

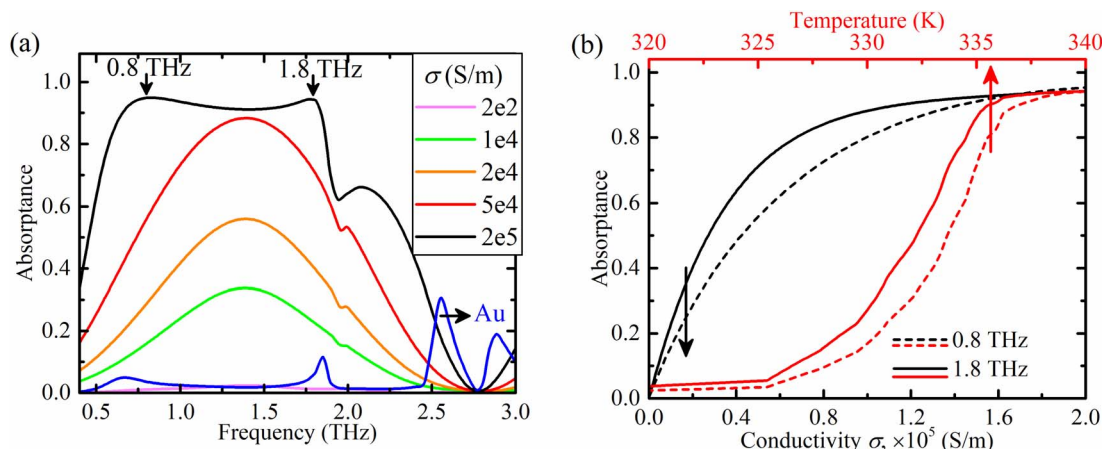


Fig. 5 (a) The spectrum of the absorbance for different values of the VO<sub>2</sub> conductivity and that for the Au strip. (b) Dependence of the absorbance on the conductivity  $\sigma$  of VO<sub>2</sub> (black, bottom axis) and temperature (red, top axis) at 0.8 THz (dashed lines) and 1.8 THz (solid lines).

absorber, respectively, and  $Z_0 \approx 377 \Omega$  is the wave impedance of air. In order to ensure efficient absorption in a given spectral range, the real part of the relative impedance  $\mathcal{R}e(Z_r)$  need to approach 1, whereas the imaginary part  $\mathcal{I}m(Z_r)$  needs to be equal to 0. Fig. 4(c) plots the real (black) and imaginary (blue) parts of the relative wave impedance  $Z_r$  linked to the left axis, whereas the right axis shows the absorbance spectrum. The green highlighted region corresponds to the spectral region of the efficient absorption ( $A(\omega) \geq 0$ ). It is seen that in the highlighted spectrum from 0.64 up to 1.81 THz  $\mathcal{R}e(Z_r) \sim 1$ , whereas  $\mathcal{I}m(Z_r) \sim 0$ , demonstrating the impedance matching of the absorber with the free space. Once the real and imaginary parts strongly deviate from those of the free space (below 0.64 THz and above 1.81 THz), the absorbance decreases noticeably. The main advantage of employing VO<sub>2</sub> in THz technologies is that its conductivity can be controlled by temperature, allowing for a phase transition from dielectric to metallic states. Hence, the influence of the conductivity of the strip on the performance of

MMA is also explored and the results are shown in Fig. 5(a). Here the conductivity  $\sigma$  of VO<sub>2</sub> was changed from  $200 \text{ S m}^{-1}$  (insulating phase) to  $2 \times 10^5 \text{ S m}^{-1}$  (metallic phase). It is seen that in the insulating phase of strips, the absorbance of the periodic system is around 0 and MMA acts as a perfect mirror due to the bottom Au reflector. The absorbance gradually increases as the conductivity increases, with the absorbance spectrum having a Gaussian-like shape with a maximum at a constant frequency of 1.4 THz. When the VO<sub>2</sub> strips are in a fully conductive state ( $\sigma = 2 \times 10^5 \text{ S m}^{-1}$ ), a broad efficient absorption band is formed.

Two maxima are observed in the efficient absorption band at 0.8 THz and 1.8 THz both having absorbance peak values of  $\sim 0.94$ . Shown by a blue line in Fig. 5(a) is the absorption spectrum of a system with Au strips, where a  $4.56 \times 10^7 \text{ S m}^{-1}$  value for the THz conductivity was used.<sup>39</sup> No broadband absorption is observed for highly conductive strip material but only several absorption peaks are present with the highest one

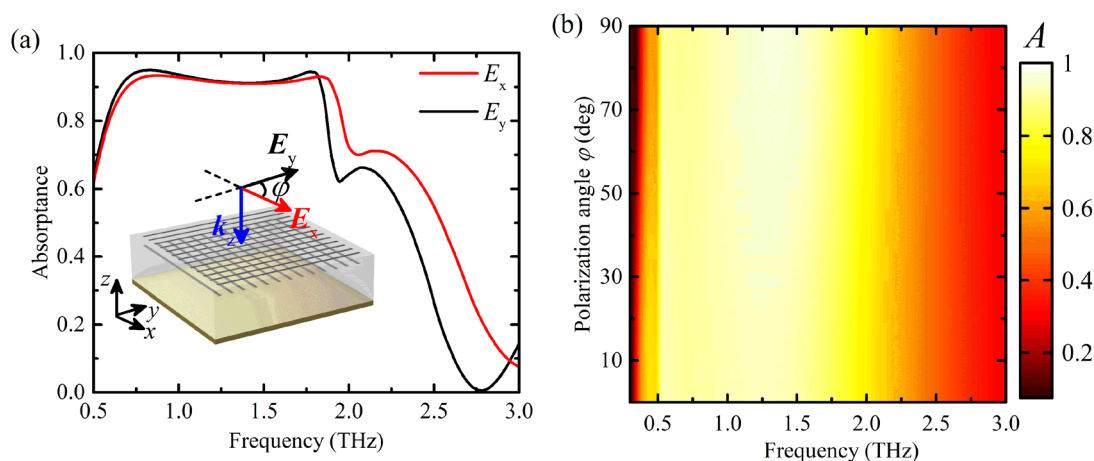


Fig. 6 (a) The absorption spectrum of the system with two cross-oriented layers of strips under x- and y-polarized normally incident plane waves. The inset depicts the schematic of the super-cell. (b) The color map plot of absorbance spectrum as a function of the polarization angle  $\phi$ .



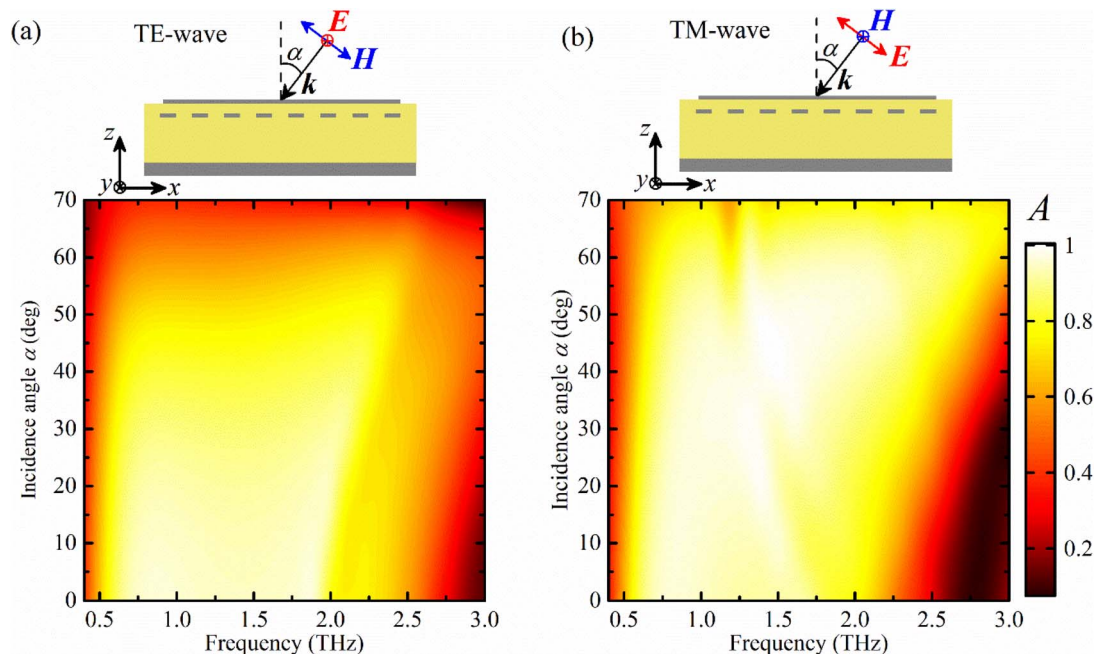


Fig. 7 Absorptance spectrum of the structure as a function of the incidence angle  $\alpha$  in the case of (a) TE-polarized waves and (b) TM-polarized waves with the corresponding schematic illustrations.

at around 2.55 THz and a peak value of about 0.32. The dependence of the absorptance on the conductivity of VO<sub>2</sub> (bottom axis, black) and temperature (top axis, red) are plotted in Fig. 5(b) at frequencies of 0.8 THz and 1.8 THz by dashed and solid lines, respectively. At both frequencies, the absorptance sharply increases by increasing the conductivity and starting from  $1.14 \times 10^5 \text{ S m}^{-1}$  at 0.8 THz and  $1.42 \times 10^5 \text{ S m}^{-1}$  at 1.8 THz the absorptance exceeds 90%. Since the conductivity of VO<sub>2</sub> is proportional to the temperature, analogous dependence is also expected when the temperature is varied. Effective absorption is provided at temperatures above 336.9 and 335.6 K at frequencies of 0.8 and 1.8 THz, correspondingly. Thus, the absorptance can be effectively changed from 0.03 at (0.05) at 325

K to 0.95 (0.94) at 340 K when the frequency of the incident radiation is 0.8 THz (1.8 THz). This fact opens up the possibility to realize modulation of the amplitude of THz radiation. Moreover, the modulation depth can be tuned by controlling the temperature of the MMA structure.

In the above analysis, we chose an incident wave having a polarization parallel to the longest dimension of the strip to ensure efficient absorption. On the other hand, rotating the polarization by 90° in the lateral plane produces no absorption and all the electromagnetic waves are reflected. In other words, due to structural asymmetry, the absorption performance is sensitive to the incident field polarization. Polarization-insensitive absorption characteristics can be ensured by

Table 1 Comparison of performance of the suggested MMA absorber with other metamaterial absorbers operating in the same spectrum

Ref.	90% absorption band (BW) in THz	RBW (%)	Unit cell sizes ( $\mu\text{m}^3$ )	Materials (layers)	Structure
40	0.39–0.72 (0.33)	60	$174 \times 174 \times 70.52$	Au, SiO <sub>2</sub> , VO <sub>2</sub> (4)	Metallic cross resonators on SiO <sub>2</sub> –VO <sub>2</sub> –SiO <sub>2</sub> planar structure
41	0.457–1 (0.543)	74.5	$150 \times 150 \times 50.4$	Aluminium, polyimide (3)	Two symmetrical L-shaped metallic resonators
20	1.58–2.22 (0.642)	33.7	$120 \times 120 \times 20.8$	Au, polyimide (5)	Two layers of four different sized square metallic patches
22	0.61–1.36 (0.75)	76.1	$120 \times 120 \times 66$	SiO <sub>2</sub> , VO <sub>2</sub> , Au (3)	Ring and cross-like resonators with different sizes combined in a unit-cell and embedded in a dielectric layer
42	1.33–2.43 (1.1)	58.5	$100 \times 100 \times 13.2$	Au, SiO <sub>2</sub> (3)	Two double square split-ring resonators combined with three double circular split-ring resonators with different orientations
This paper	0.66–1.84 (1.18)	94.4	$114 \times 114 \times 39.2$	VO <sub>2</sub> , polymer, Au (4)	Rectangular strips





adding an additional parallel layer with strips oriented perpendicular to the first layer elements. The schematic of a super-cell of such an absorber and its absorption spectra under *x*- and *y*-polarized plane waves are shown in Fig. 6(a) and a two-dimensional map of the absorptance as a function of the frequency and polarization angle at normal incidence is shown in Fig. 6(b). Since the second layer of strips is closer to the Au reflector and is completely embedded in the dielectric spacer, a small difference is seen between absorption spectra of *x*- and *y*-polarized plane waves, as follows from Fig. 6(a). One sees that an efficient absorption band with a constant bandwidth is achieved for the entire range of polarization angles from 0° up to 90° [Fig. 6(b)]. The total optimized sizes of a supercell are  $t_d = 36 \mu\text{m}$ ,  $p_x = 6 \mu\text{m}$ ,  $p_y = 114 \mu\text{m}$ ,  $d_z = 200 \text{ nm}$ ,  $d_x = 1 \mu\text{m}$  and  $d_y = 94 \mu\text{m}$ , and the distance between two layers of strips is 3  $\mu\text{m}$ . Finally, the performance of the polarization-insensitive design of the absorber under oblique incident TE and TM waves is shown in Fig. 7(a) and (b), respectively, with the corresponding illustrations of orientations of the electromagnetic field components.

Under the oblique incident TE-polarized waves the system preserves its broadband absorption performance for angles of incidence up to 40°, and the further increase in  $\alpha$  gradually decreases the absorptance. Under TM polarized waves a continuous efficient absorption band is observed at incidence angles up to 55°.

Table 1 compares the performance of the proposed MMA with several structures reported in the literature which work in the same spectrum. The comparison criteria are 90% absorption band, BW, RBW, unit cell sizes, materials used and structural layers, as well as a short description on the unit-cell configurations used.

## Conclusions

Thus, an ultra-broadband MMA of THz radiation based on VO<sub>2</sub>-insulator-metal configuration is proposed. The top pattern of MMA represents orderly distributed VO<sub>2</sub> strips separated by a dielectric spacer from the bottom Au reflector. Theoretical analysis based on the electric dipole approximation is performed to characterize the absorption and scattering properties of individual elements. Finite element method-based simulations are carried out for a rectangular strip as an equivalent configuration for an elongated oblate ellipsoid. It is shown that the ordered distribution of such strips on a surface of an Au-backed planar dielectric provides absorptance exceeding 90% in a wide frequency range from 0.66 to 1.84 THz with a BW of about 1.18 THz. The corresponding relative bandwidth with respect to the centre frequency of the absorption band is ~94.4%. Tunability of the absorption spectrum by varying dimensions of VO<sub>2</sub> strips is demonstrated. The possibility of achieving wide polarization and incidence angle tolerance for both TE and TM polarizations is shown by making use of two parallel layers of VO<sub>2</sub> strips rotated by 90 degrees with respect to each other. Controllable THz optical conductivity of VO<sub>2</sub> opens up the prospects for modulation of the absorptance from 0 up to 100% by varying the surrounding temperature from 320 K to

340 K. Interference theory is applied to reveal the absorption mechanism and impedance-matching conditions for efficient absorption are clarified. We believe that our results can serve as a practical guideline for establishing suitable material and geometrical parameters of a simple MMA design capable of efficient broadband absorption in various parts of the EM spectrum.

## Author contributions

The authors have contributed to this article in the following way: Lilit Gevorgyan designed the tunable ultra-broadband terahertz metamaterial absorber based on vanadium dioxide strips using numerical simulation software and wrote the paper. Hovhannes Haroyan oversaw the entire process of organizing work, providing theoretical and simulation guidance and reviewing the manuscript. Henrik Parsamyan supervised the construction of the simulation model, proposed effective options for the design of the absorber, carried out the simulation and theory calculation, and wrote the article. Khachatur Nerkararyan conceived the presented idea, performed theoretical calculations, and analysed the results.

## Conflicts of interest

There are no conflicts of interest to declare.

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