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## Settling velocity variation induced by a sphere moving across a two-layer stratified fluid with different rheological characteristics

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Particle settling in stratified fluids is widespread in chemical and pharmaceutical processes, and how to effectively regulate the particle velocity is the key to optimizing the above process technology. In this study, the settling of individual particle in two stratified fluids, water–oil and water–PAAm was studied using the high-speed shadow imaging method. In the Newtonian stratified fluid of water–oil, the particle penetrates the liquid–liquid interface and forms unsteady entrained drops of different shapes, and the settling velocity becomes smaller. In contrast, in water–PAAm stratified fluids, the shear-thinning and viscoelasticity of the lower fluid will cause the entrained drops of the particle to appear a stable sharp cone shape, and the particle can thus obtain a smaller drag coefficient ( $C_D^* < 1$ ) and a significantly enhanced settling velocity ( $U^* > 1$ ) compared to the uncovered PAAm solution (PAAm solution without overlayer oil). This study can provide a new path for the development of new particle velocity regulation techniques.

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## 1 Introduction

Particle settling is widespread in nature and industry, such as the flow of pollutant particles in the atmosphere,<sup>1</sup> the movement of particles in the respiratory tract,<sup>2</sup> and the petroleum industry,<sup>3</sup> which are involved in the movement of particles and are currently a hot issue in the above-mentioned fields. In the geophysical environment, both miscible and immiscible fluids involve particle settling through fluid layered interfaces. Many of the characteristics of these systems are primarily due to density gradients caused by differences in temperature or salinity between fluids. Combining particle settling with stratified fluids is essential in many environmental processes and geophysical contexts, such as urban pollution,<sup>4</sup> sediment fluxes in the ocean,<sup>5</sup> and carbon sequestration.<sup>6</sup> In oceanography, the presence of stratification phenomena such as temperature and salinity layers can affect the spread, survival, and growth of small biota.<sup>7</sup> Liquid–liquid interfaces are widespread in industrial processes such as extraction, separation, or mixing. Therefore, particles crossing liquid–liquid interfaces have a high research value. Nevertheless, most research studies consider the movement of particles towards deformable interfaces, focusing on coalescence<sup>8</sup> or motion near the interface,<sup>9</sup>

and only a few studies are devoted to liquid–liquid interface fracture.

The question of how particles penetrate the interface has been a hot topic for researchers. Ding *et al.*<sup>10</sup> and Raufaste *et al.*<sup>11</sup> studied the formation process of cavities in gas–liquid interfaces by spherical and cylindrical particles impacting them and revealed the relationship between contact line pinning and subsequent cavity evolution. Maru *et al.*<sup>12</sup> pointed out that whether a particle passes through an interface must also surely depend on surface energy and density difference, as much as critical radius. Geller *et al.*<sup>13</sup> demonstrated two different liquid surface strain modes through numerical simulations: one is the Film Drainage Mode (FDM),<sup>8,14,15</sup> in which the fluid is discharged in front of the particle, leaving a thinning film, and the other is the Tailing Mode (TM),<sup>12</sup> in which the particle passes through a deformable interface while still being wrapped by the surrounding fluid. In most cases, particles passing through the stratified interface will increase the resistance of the fluid to particle motion.<sup>16</sup> In the low Reynolds number range, the increased resistance to particles settling in linearly stratified fluids is due to the viscous entrainment of the fluid in the high-density layer and the formation of a lighter fluid shell behind the particles.<sup>17</sup> At  $1.5 < Re < 15$ , particles tend to drag the lighter fluid into the lower fluid, greatly increasing its drag; within  $3 < Fr < 10$ , the drag coefficient in the stratified fluid is found to be an order of magnitude larger than that of the uniform fluid<sup>18</sup> (the definition of Reynolds numbers (Re) and Froude numbers (Fr) is explained in Chapter 3). As the presence of stratification leads to a significant increase in the drag force of individual

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particles during settling, the particle settling velocity is significantly inhibited,<sup>19</sup> and particles are even suspended in fluids lighter than themselves.<sup>20</sup> Magnaudet *et al.*<sup>21</sup> found that particles usually pull the upper fluid to the lower layer, and the resulting column settling kinetic properties are highly dependent on fluid density, viscosity, and Re.

Nevertheless, previous studies have paid less attention to particle settling when the lower fluid is a viscoelastic non-Newtonian fluid and rarely noticed the phenomenon of particle velocity enhancement in it. Zenit *et al.*<sup>22</sup> found that in a non-Newtonian fluid, viscous force, inertial force, and surface tension all change. In this study, we will focus on the effects of key factors such as entrained drop shape, drag coefficient, and Re number on the variation of particle settling velocity in Newtonian-non-Newtonian stratified fluid.

## 2 Experimental method

The experimental setup is shown in Fig. 1. The water tank is a sunken rectangular container of 1000 mm in height and 150 mm × 150 mm cross-section. The particle release device is a vacuum ejector to ensure that the initial velocity of the particles is zero. Two high-speed cameras (FASTCAM Mini UX 50, Photron), two LED arrays, and a computer connected to the cameras were used in the experiments to form a high-speed shadowgraph binocular-imaging system. The system can track the trajectory of particles in the x-y and x-z planes. Six types of spherical particles with less than a 0.25  $\mu\text{m}$  diameter variation and spherical error and 0.02  $\mu\text{m}$  of surface roughness were used in the experiments. The system includes polytetrafluoroethylene (PTFE) particles with diameters of 5 mm, 6.35 mm, 8 mm, and 9.53 mm, respectively, and also includes silicon nitride ceramic ( $\text{Si}_3\text{N}_4$ ) and zirconium oxide ceramic ( $\text{ZrO}_2$ ) particles with diameters of 5 mm. Mineral oil (Sigma-Aldrich M5904) was used as the upper fluid, and water and 0.5 wt% polyacrylamide (PAAm, supplied by Shanghai Macklin Biochemical Co., Shanghai, China) were selected as the lower fluid, respectively, thus constituting two types of stratified

fluids. The shear thinning and viscoelastic properties of the PAAm solution are specifically described in our recent paper.<sup>23</sup>

The density of the PAAm solution is 1005 kg m<sup>-3</sup>, which is very close to that of water. The shear thinning and viscoelastic properties of 0.5% PAAm solution are shown in Fig. 2. Considering the variation of temperature on the properties of the fluid, each experiment was controlled at room temperature, and the temperature of the experimental fluid was measured using a standard thermostat with an error of  $\pm 0.1$  °C to keep the temperature range at  $20 \pm 5$  °C.

Fig. 2a shows the rheological curves of the shear stress  $\tau$  to the shear rate  $\dot{\gamma}$  with a steady state in the PAAm solution and water, where the slope of the curves represents the fluid viscosity ( $\eta$ ). Fig. 2b indicates that the storage modulus  $G'$  and loss modulus  $G''$  increased with the increasing frequency, which indicates the yield behavior of the test solution.

Boundary extraction of the particles and extraction of kinetic parameters such as displacement and velocity were performed using ImageJ and a self-written MATLAB code. In this paper, the capillary effect is overcome by increasing the particle density so that the particles are sufficient to cross the interface and the particles all reach the final velocity before reaching the liquid–liquid boundary.

## 3 Results and discussion

### 3.1 Force analysis

Firstly, gravity and buoyancy are analyzed. For a spherical particle with radius  $R$ , the particle density is  $\rho_s$ , and the densities of the upper and lower fluids are  $\rho_1$  and  $\rho_2$ , respectively, where  $\rho_s$  is greater than  $\rho_1$  and  $\rho_2$ . Fig. 3 shows a simple force model for an individual particle. The presence of liquid droplets attached to the tail of the settling particle after the particle settles through the stratified interface leads to a change in the overall force on the particle.

Firstly, the forces on the particle in the upper fluid are analyzed, where the gravity and buoyancy of the particle are constant. The gravity of the particle in the upper fluid layer is

$$F_g = mg = \frac{1}{6}\pi(2R)^3\rho_s g \quad (1)$$

The buoyancy of the particle during the settling process is

$$F_f = V\rho_1 g = \frac{1}{6}\pi(2R)^3\rho_1 g \quad (2)$$

Since the fluid has inertia, it will exhibit a reaction force on the particle, and the additional mass force is expressed as<sup>24</sup>

$$F_m = \frac{c_m\pi}{6}(2R)^3 \rho_1 \left( \frac{dv_1}{dt} - \frac{dv_z}{dt} \right) \quad (3)$$

where the additional mass coefficient  $c_m$  is related to the particle shape, for spherical particle  $c_m = 0.5$ ;  $\rho_1$  is the density of the fluid;  $v_1$  is the flow velocity of the fluid;  $v_z$  represents the settling velocity of the particle. The additional mass force is negligible when the acceleration of the particle motion is not large.

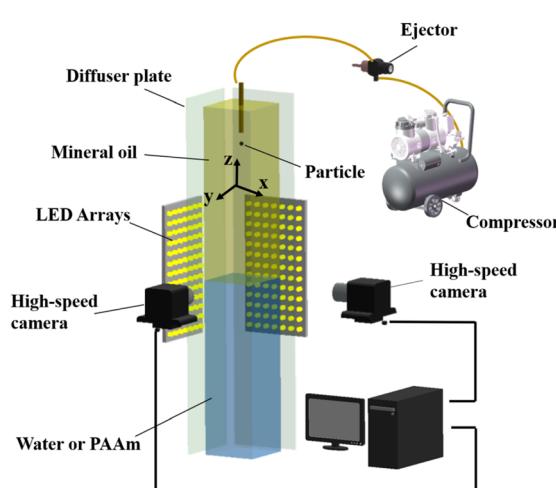


Fig. 1 Schematic diagram of the experimental setup.



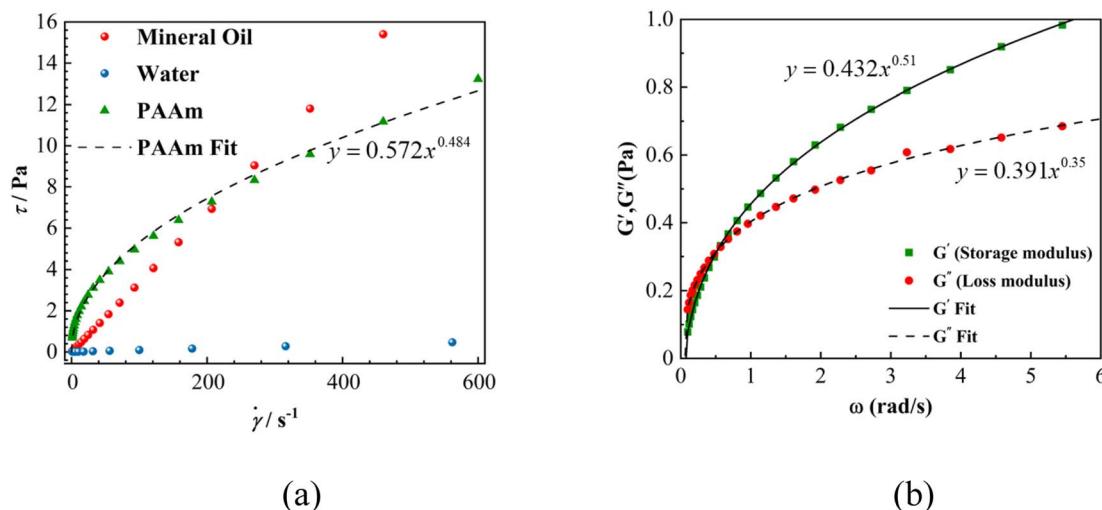


Fig. 2 (a) Rheogram of 0.5 wt% PAAm solution, water, and mineral oil. (b) Viscoelastic modulus of PAAm solution as a function of frequency.

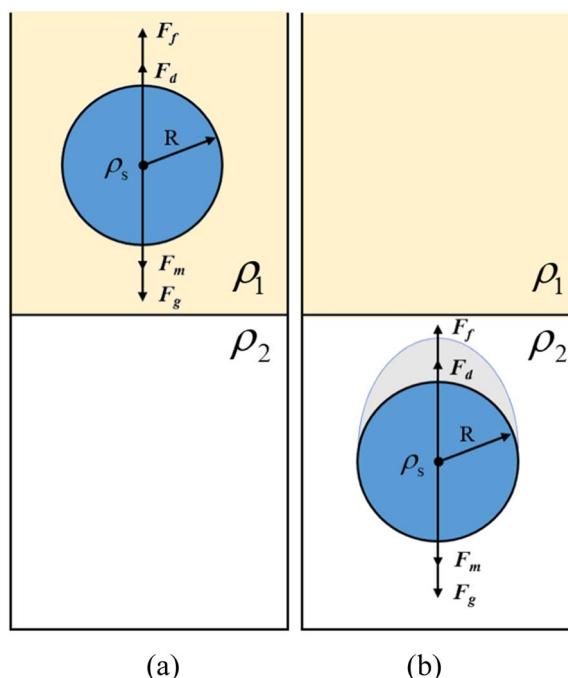


Fig. 3 Schematic diagram of individual particle forces. (a) Schematic diagram of the upper layer fluid force, (b) schematic diagram of the lower layer fluid force.

According to D'Alembert's principle

$$F_m + F_g = F_f + F_d \quad (4)$$

For the force on the particle in the lower fluid, the presence of droplets attached to the tail of the particle leads to a change in the force on the particle, mainly gravity, buoyancy, and drag.

The gravity of the particle in the lower fluid is

$$F_g = \frac{1}{6}\pi(2R)^3\rho_s g + \rho_1 V_1 g \quad (5)$$

The buoyancy of the particle in the lower fluid is

$$F_f = \frac{1}{6}\pi(2R)^3\rho_2 g + \rho_2 V_1 g \quad (6)$$

The shape of the droplet in the experiment of oil-PAAm stratified fluids is mostly conical. According to the equivalent volume method, the volume of the droplet is obtained by subtracting the volume of the hemisphere from the volume of the cone and is expressed as

$$V_1 \approx \frac{1}{12}\pi(2R)^3 \quad (7)$$

In non-Newtonian fluids, the dynamical model that has been widely used in previous work to describe the fluid has the following form<sup>24</sup>

$$\tau = k\dot{\gamma}n \quad (8)$$

where  $k$  is the consistency index and  $n$  is the power-law exponent.

For the 0.5 wt% PAAm solution,  $n$  is 0.484, and  $k$  is 0.572 (goodness-of-fit is 0.997) obtained by fitting the above equation and rheogram of 0.5 wt% PAAm solution.<sup>23</sup>

The Reynolds number (Re) is defined as

$$Re = \frac{2\rho v_z R}{\mu} \quad (9)$$

The modified Reynolds number (Re\*) of the settling particle in the shear-thinning fluid is<sup>25</sup>

$$Re^* = \frac{(2R)^n v_z^{2-n} \rho_1}{k} \quad (10)$$

In a Newtonian fluid, the drag force can be expressed as

$$F_d = \frac{1}{2}C_D A_f \rho_1 v_z^2 \quad (11)$$

where  $A_f$  is the windward area,

$$A_f = \frac{1}{4}\pi(2R)^2; \quad (12)$$

By the above equation,  $C_D = 8Rg(\rho_s - \rho_1)/(3\rho_1v_z^2)$  in the upper fluid layer, and  $C_D = 4Rg(2\rho_s + \rho_1 - 3\rho_2)/(3\rho_2v_z^2)$  in the lower fluid layer.

In shear thinning fluid, the drag force can be expressed as<sup>26</sup>

$$F_d = 12\pi(2R)^2 \left( \frac{v_z}{4R} \right) F(n) \quad (13)$$

The drag coefficient is

$$C_D = \frac{24}{Re^*} F(n) \quad (14)$$

By the above equation,  $C_D = 8Rg(\rho_s - \rho_1)/(3\rho_1v_z^2)$  in the upper fluid layer, and  $C_D = 4kR^2g(2\rho_s + \rho_1 - 3\rho_2)/(3\rho_2v_z^{3-n})$  in the lower fluid layer.

In addition, the Froude number (Fr) was introduced

$$Fr = \frac{v^2}{gL} \quad (15)$$

where  $L$  is the characteristic length (Table 1).

Table 1 Initial and final Re of the particle in the stratified fluid

Particle	Density ( $\text{g cm}^{-3}$ )	Oil-water stratification		Oil-PAAm stratification	
		Oil (Re)	Water (Re)	Oil (Re)	PAAm (Re*)
5 mm PTFE	2.2	35.4	1316.0	35.2	1.14
5 mm $\text{Si}_3\text{N}_4$	3.2	53.9	2594.0	54.3	5.26
5 mm $\text{ZrO}_2$	6.0	89.8	3933.1	90.8	20.43
6.35 mm PTFE	2.2	57.6	2122.5	57.4	3.44
8 mm PTFE	2.2	92.5	3524.7	92.8	9.89
9.53 mm PTFE	2.2	126.2	4518.9	127.6	19.16

### 3.2 Morphology

The evolutionary pattern of different particles near the oil–water interface is given in Fig. 4. As the particle penetrates the layered interface, a film of upper fluid is attached to the front of the particle, and the upper fluid near the surface of the particle is carried simultaneously into the lower fluid by inertia, and a cone-shaped column of fluid is entrained at the end of the particle.<sup>27,28</sup> The cone-shaped column is elongated as the particle settles, and at a certain critical distance, the column breaks under the combined effect of surface tension and lower hydrostatic pressure. The droplet remains attached to the tail of the particle after the column has broken (Fig. 4). The shape of the entrained drop varies with the initial Re, tending to a hat-shaped cap (Re = 35), a gyroscopic shape (Re = 54) or a platform shape (Re = 58, Re = 93) under surface tension and vortex dynamics.

As the initial Re number increases, it is possible for the light fluid attached at the tail of the particle to take on a different geometry. The elongation of the liquid column maintains an axisymmetric geometry until it breaks, independent of the viscosity of the lower fluid. The shape of the trailing entrained drops of the settling particle, the volume of the cone-shaped liquid column, and the distance of the column break also vary with the Re number. Also, the process is related to the inertia, viscosity, buoyancy, and capillary effects of the particle.<sup>28</sup>

As shown in Fig. 5, unlike the cone-shaped liquid column formed at the interface of the oil–water stratification, the particle crosses the oil–PAAm layered interface, and an elongated cylindrical column is formed in the lower fluid, indicating that the capillary effect plays little role in this process<sup>21</sup> and suggesting a shear thinning effect in the lower fluid. With the particle settling, the cylindrical liquid column

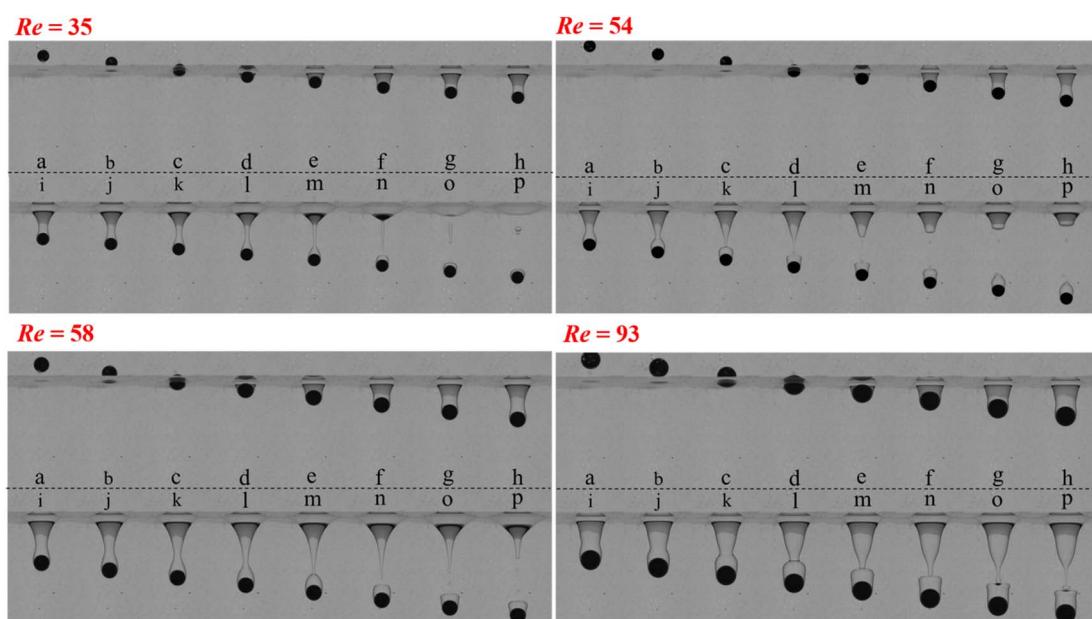


Fig. 4 Modal diagram of particle evolution at the oil–water stratified interface.



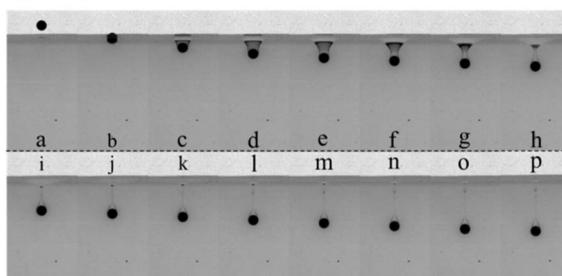
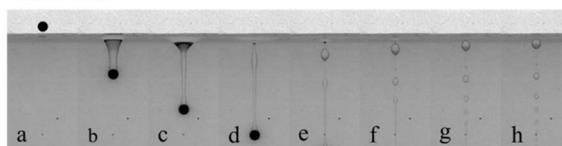
**Re = 35****Re = 54**

Fig. 5 Modal diagram of particle evolution at the oil–PAAm stratified interface.

entrapped at the end of the particle becomes thinner and thinner, relaxing and taking on multiple necking under the combined effects of capillary, viscous, and buoyancy. The break in necking is accompanied by the production of multiple droplets, which may be due to the classical mechanism of capillary wave instability or to a surface tension-driven contraction process.<sup>28</sup> The entrained drops show a sharp cone shape under the viscoelasticity of the lower fluid (PAAm solution), which directly confirms the presence of a negative tail of the particle.<sup>29</sup>

### 3.3 Sedimentation trajectory

For particle settling, many studies have been done before.<sup>30</sup> Particles form vortex rings and streamwise vortices in their wake during settling, and the shedding of vortices leads to the movement of individual particles that do not have a stable path and can be broadly classified as inclined linear, vertical linear, and zigzag oscillatory settling.

From the diagram of the settling trajectory of the oil–water layer (Fig. 6a), it can be seen that the particle mostly shows a straight line movement in the upper layer (oil). As the initial Re increases, the path of the particle shows instability before reaching the delamination interface, which is due to the shedding of the vortices during the settling process of the particle, causing their motion instability. After entering the lower fluid, the particle shows mostly non-linear motion, with the most unstable settling trajectory at Re = 35. This is due to the fact that during each motion cycle, the particle generates four vortex rings in different directions.<sup>30</sup> However, the particle settling paths in the lower fluid of the oil–PAAm stratification fluid (Fig. 6b) almost always show straight lines. If the particle is entering the lower fluid at a large inclination angle (with respect to the direction of gravity,  $z$  direction), the particle will slowly change to a linear motion in the direction of gravity in the PAAm solution. This is mainly due to the specific shear thinning properties of the PAAm solution,<sup>31</sup> in contrast to the significant lateral migration that occurs in oil–water stratified fluids.

### 3.4 Analysis of particle settling velocity in stratified fluids

Fig. 7 shows the variation in settling velocity and lateral migration of a single particle in stratified fluids. At about  $t = 0.3$  s, all

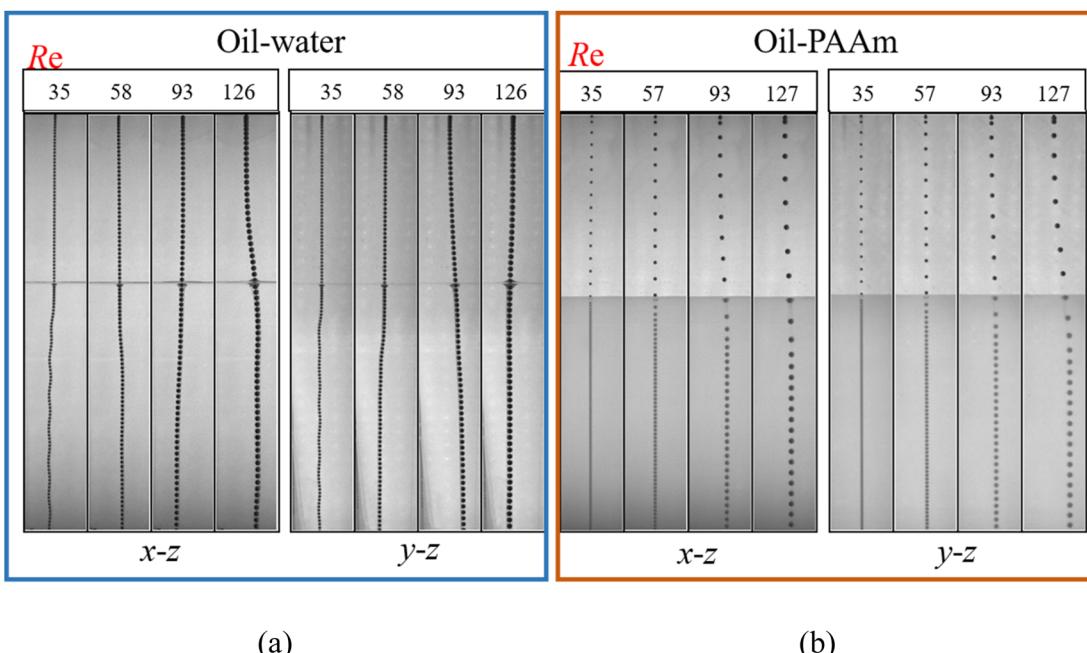


Fig. 6 (a) Particle settling trajectory in oil–water stratification ( $x$ – $z$  plane and  $y$ – $z$  plane), particle interval time  $\Delta t = 0.02$  s, (b) particle settling trajectory ( $x$ – $z$  plane and  $y$ – $z$  plane) in oil–PAAm stratification, particle interval time  $\Delta t = 0.08$  s, where  $x$ – $z$  and  $y$ – $z$  represent the two vertical orthogonal planes, respectively, and the numbers represent the initial Re.



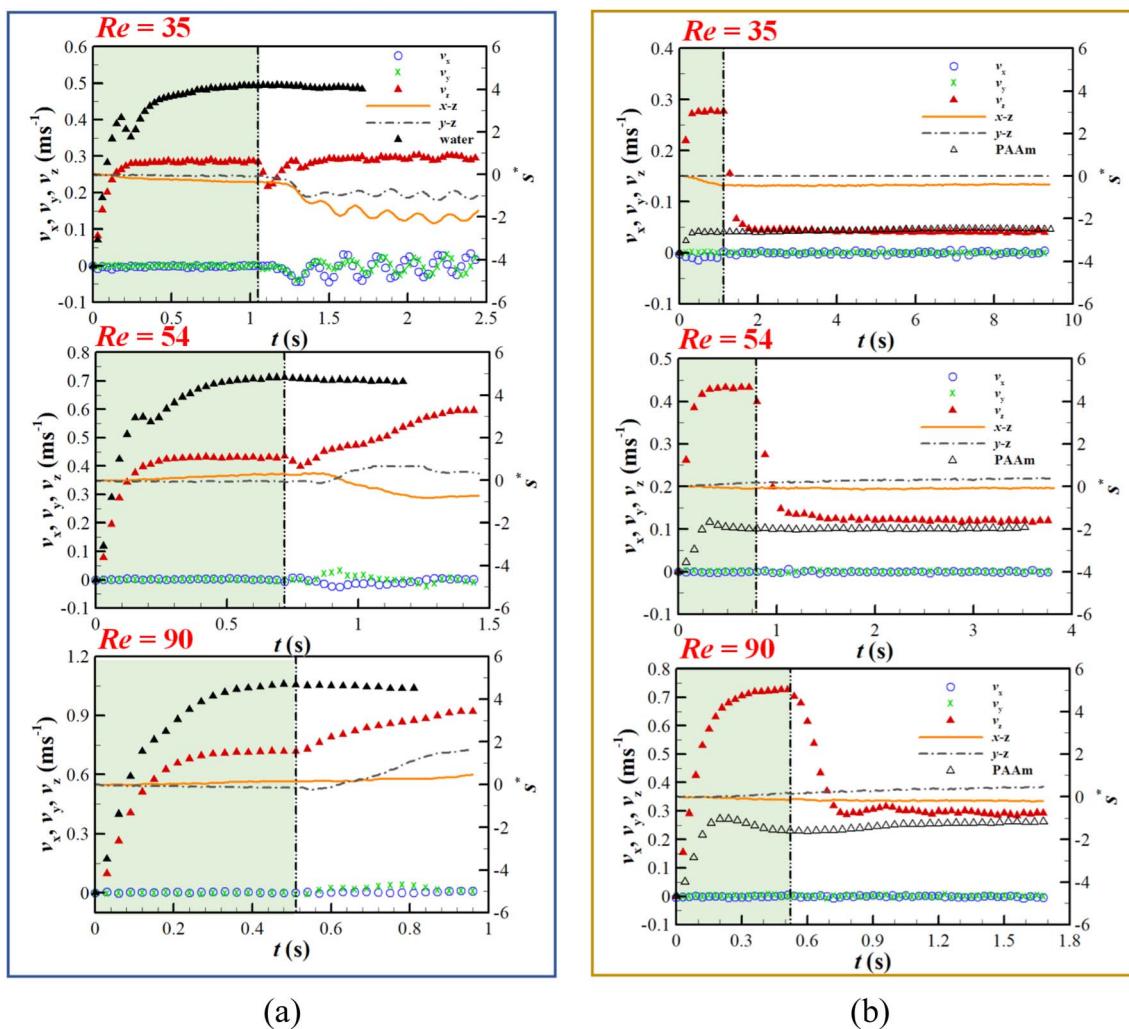


Fig. 7 (a) Motion characteristics of individual particle settling process in oil–water stratified fluids, (b) motion characteristics of individual particle settling process in oil–PAAm stratified fluids, where  $v_x$ ,  $v_y$ , and  $v_z$  in the legend represent the settling velocity of the particle in the gravity direction during the falling process, the lateral migration velocity in the  $x$ -direction and the  $y$ -direction, respectively. In addition,  $x$ - $z$  and  $y$ - $z$  are the lateral migration of the particle in two orthogonal planes,  $s^*$  ( $s^* = s/(2R)$ ). Water and PAAm are the settling velocity in uncovered water and in uncovered PAAm solution, respectively.

particles almost reach their final steady velocity in the upper fluid (oil). This is due to the fact that the particle crosses the interface and entrains the upper fluid into the lower fluid, forming a column of fluid connected to the upper fluid. The dragging by the liquid column on the particle leads to a period of decelerated motion, which is consistent with previous results.<sup>28</sup> The subsequent breakage of the liquid column leads to a reduction in drag, and the particle velocity in the water increases firstly with time and then stabilises, reaching its final steady velocity. In Fig. 7a, comparing the settling velocity of the particle in an oil–water stratified fluid and uncovered water, it is found that the particle settling is at smaller velocities in the stratified fluid than in water alone. This is due to the particles that have entrained drops on their tails when settling in the lower fluid (water), resulting in increased buoyancy and drag forces on the particle. At the same time, it was found that the final steady velocity in oil–water fluids increased with increasing initial  $Re$ .

As shown in Fig. 7b, the particle settling velocity decreases rapidly after crossing the oil–PAAm interface and tends to a final steady velocity in the uncovered PAAm solution. This deceleration shows a different pattern to that of the oil–water stratified fluid. Unexpectedly, the settling velocity of the particle in the lower fluid (PAAm solution) was enhanced compared to the uncovered PAAm solution fluid. The larger the initial  $Re$ , the stronger the inertial effect of the particle and the faster the settling velocity. After entering the lower fluid, the shear effect of the PAAm solution fluid increases, the viscosity decreases, and the drag force decreases. On the other hand, the droplets are sharp cone-shaped by the viscoelasticity of the lower fluid, and the overall shape of the particles and droplets tends to be more streamlined, making them less subject to the drag force. There is a significant lateral migration of particle settling in the lower fluid of the oil–water stratified fluid, whereas almost vertically in the oil–PAAm stratified fluid, with



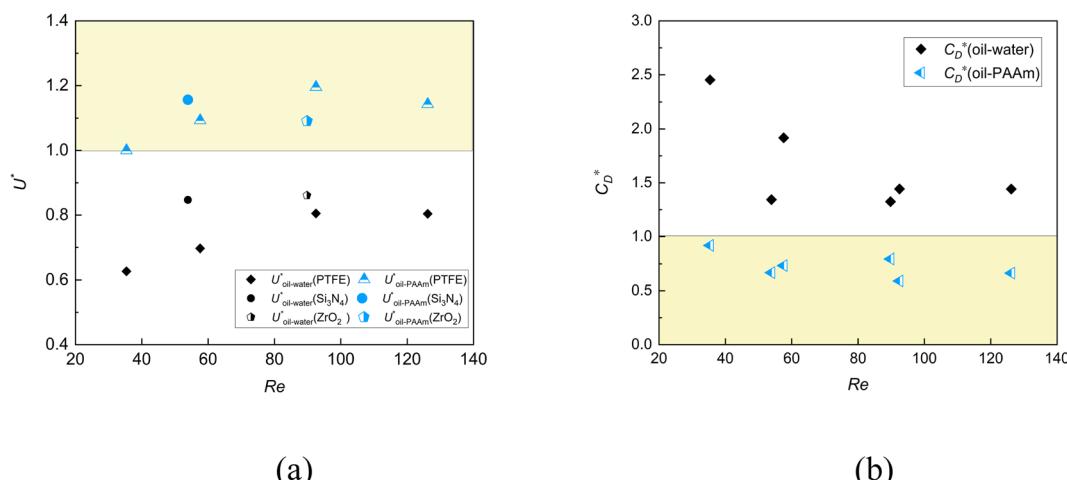


Fig. 8 (a) The ratio of the final steady velocity of the particle in the stratified fluid to the corresponding uncovered fluid,  $U^*$  ( $U^* > 1$ , i.e., the velocity increases). (b) The ratio of the drag coefficient of the particle in the stratified fluid to the corresponding uncovered fluid,  $C_D^*$  ( $C_D^* < 1$ , i.e., the drag coefficient decreases).

$v_x$  and  $v_y$  always fluctuating around zero and almost independent of the initial  $Re$ .

In the lower layer of the oil-water stratified fluid, the entrained drops of the particle take the shape of the hat, gyroscope, and platform, while in the oil-PAAm stratified fluid, the shear-thinning and the viscoelasticity of the lower fluid cause the entrained drops of the particle to take the shape of a stable sharp cone. The change in velocity is actually due to the introduction of entrained drops, which changes the drag coefficient of the composite particle formed by the combination of particle and entrained drops. The internal mechanism of velocity enhancement is illustrated by comparing the change of particle drag coefficient in uncovered PAAm solution or in water with that in stratified fluid. As shown in Fig. 8, in the lower layer of the oil-PAAm stratified fluid, the particle obtains a smaller drag coefficient ( $C_D^* < 1$ ), which significantly enhances the settling velocity ( $U^* > 1$ ) compared to the uncovered PAAm solution fluid.

## 4 Conclusions

In this paper, the settling characteristics of an individual particle in oil-PAAm stratified and oil-water stratified fluids and the evolution law near the stratification interface during this process are studied using high-speed shadow imaging. The results show that the lateral migration velocity fluctuations of the particle in shear-thinning viscoelastic fluids (PAAm solution) are smaller, and the path is more stable compared to Newtonian fluids (water). The particle penetrating the stratified interface will drag the upper fluid into the lower fluid to form a liquid column. The shape and fracture position of the liquid column are closely related to the  $Re$  and the type of stratified fluid. When the lower fluid is water, the liquid column is conical and breaks near the top of the particle; when the lower fluid is PAAm solution, the liquid column appears as an elongated column under the effect of shear-thinning characteristics and

weak surface tension. At this time, the particle-entrapped liquid column will undergo multiple necking and rupture, resulting in a series of discrete droplets. The particle tail entrained drops are sharp cone-shaped under the influence of viscoelasticity and shear-thinning characteristics. The sharp cone shape of the entrained drops reduces the drag coefficient of the particle and accelerates the settling of the particle. This is very different from the general Newtonian stratified fluid. The results of this study will help to deepen the understanding of particle settling laws in Newtonian-non-Newtonian stratified fluids and develop new particle settling velocity regulation techniques for chemical and other engineering applications.

## Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

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