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# Investigation of a two-dimensional photovoltaic thermal system using hybrid nanofluids and a rotating cylinder

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This article focuses on a numerical investigation aimed at enhancing the electrical performance of a two-dimensional photovoltaic thermal system (PV/T) through the application of cooling using hybrid nanofluids. The hybrid nanofluids consist of titanium oxide and silver nanoparticles suspended in water, while the PV/T system is based on polycrystalline silicon, copper, and a flow channel with a rotating cylinder. PV/T devices generate electricity from sunlight, but their performance degrades over time due to the heat generated by solar radiation. Therefore, nanofluids can be circulated through the bottom flow channel to cool the device. This study utilizes 2D incompressible Navier–Stokes equations to control fluid flow and energy equations to manage energy distribution. The COMSOL 6.0 finite element software is employed for comprehensive modeling and simulation. To enhance the performance of the PV/T system, a parametric study is conducted by varying the Reynolds number (ranging from 100 to 1000), cylinder rotational speed (varying from 0.01 to 0.2 m s<sup>−1</sup>), and silver volume fraction (ranging from 0.01 to 0.2). The results show that increasing the Reynolds number and the volume fraction of silver leads to a reduction in the maximum temperature of the cell. The maximum temperature of the cell also decreases with the rotational speed of the cylinder but only for high Reynolds numbers. By applying the present model, the cell's efficiency is improved by 5.93%.

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## 1. Introduction

It is evident that in the development of any country, particularly those in the process of development, electrical energy plays a pivotal role in running both governmental and private industries. Traditionally, energy has been generated using fossil fuels, a practice that raises global environmental concerns and contributes to global warming.<sup>1–4</sup> However, as we consider the growing demand for electrical energy, it becomes apparent that the availability of fossil fuel resources for electricity generation is limited and poses challenges for developing nations. Hence, there is an urgent need to transition to renewable and sustainable energy sources that are environmentally friendly.<sup>5–7</sup> Harnessing electrical power from solar energy stands out as

a highly sustainable and renewable alternative, surpassing other available options. This transition is particularly advantageous for countries with abundant sunlight throughout most of the year, as it can provide a consistent source of energy.

Photovoltaic thermal systems represent a highly advanced method for electricity generation using direct solar radiation. However, when a PV/T module is exposed to sunlight, the surrounding atmospheric temperature can adversely affect its performance, leading to a reduction in the solar panel's electrical efficiency.<sup>8–10</sup> To address this issue, a flow channel is integrated behind the PV/T module, allowing a coolant such as water, air, or nanofluids to circulate and effectively lower the temperature of the PV/T system. The heated fluid produced by this process can also serve other heating purposes, particularly in industrial settings. A photovoltaic thermal system is designed to simultaneously produce both heat and electricity. Numerous research articles have focused on enhancing and advancing photovoltaic systems by introducing new designs and configurations.<sup>11–15</sup> Due to its ability to efficiently harness both electrical and thermal energy through various techniques, the photovoltaic thermal system has gained significant recognition as a prominent tool within the realm of solar energy production.

A variety of PV/T systems have been subjected to numerical investigations by Zondag *et al.*<sup>16</sup> to enhance their efficiency. The

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electrical efficiency of nine distinct photovoltaic thermal systems was evaluated to offer valuable insights to journal reviewers. The results revealed that the system employing a sheet and tube configuration demonstrated exceptional performance, primarily due to its streamlined construction process. Selmi and colleagues<sup>17</sup> employed Computational Fluid Dynamics (CFD) software to analyze a solar collector comprising a flat plate immersed in water. In this numerical investigation, they focused on heat transfer through convection and radiation. To validate their findings with the CFD simulation model, an experimental setup for a PV/T system with a similar configuration was conducted.

Siddiqui *et al.*<sup>18</sup> developed a comprehensive three-dimensional numerical model for photovoltaic/thermal (PV/T) systems. They combined multiple electrical and thermal components to explore the cooling system of PV/T through simulation. The study investigated the impact of various parameters such as inlet velocity, temperature, radiation absorption, and thermal resistance on the cooling system's performance. The results highlighted the exceptional advantages of these systems in regions with high solar radiation and ambient temperatures. Prototype PV/T systems were installed in a building to provide hot water for domestic use and validate the computational model with experimental data. Corbin and Zhai<sup>19</sup> reported that this experiment led to a 5.3% increase in cell efficiency and an overall maximum electrical plus thermal efficiency of 34.9%. Bhattarai *et al.*<sup>20</sup> developed a numerical model to assess the performance of a photovoltaic/thermal (PV/T) system employing a tube and sheet configuration, comparing it to another type of solar collector. However, their research was conducted in one dimension and focused on solving the principles of energy conservation for different components of the systems. They achieved favorable numerical results that were in good agreement with experimental data, demonstrating that the solar collector exhibited a daily thermal performance surpassing PV/T by an impressive margin of 18%.

Syafiqah *et al.*<sup>21</sup> employed ANSYS software to enhance the electrical performance of a PV thermal system. They separately utilized both air and water cooling in their numerical approach. The study aimed to investigate the weather conditions in Dhahran, Saudi Arabia. The researchers found that the highest recorded ambient temperature in the area was 21 °C, with solar intensity peaking at 979 W m<sup>-2</sup>. This investigation concluded that using water as the coolant in a PV/T system is more effective than using air.

Soltani *et al.*<sup>22</sup> conducted a comprehensive numerical study that incorporated both natural convection and forced convection phenomena within the flow channel of PV/T systems. A comparative analysis was performed to examine temperature variations in PV/T systems using different types of nanofluids—water, Fe<sub>3</sub>O<sub>4</sub>–water, and SiO<sub>2</sub>–water. Utilizing nanomaterials as primary fluids in water has been suggested as a more efficient alternative compared to using water alone.

SiO<sub>2</sub> and water have demonstrated enhanced cooling capabilities and improved electrical performance in solar cells. Rejeb *et al.*<sup>23</sup> investigated a PV/T system composed of tube and

sheet using four different combinations of nanofluids: Al<sub>2</sub>O<sub>3</sub>, Cu, water, and ethylene glycol. Their experiment incorporated data from three distinct cities: Mashhad, Lyon, and Monastir. The researchers concluded that nanofluids with water as the base were more efficient for electricity generation compared to those with glycol as the base. Khanjari *et al.*<sup>24</sup> analyzed a PV/T system for both energy and exergy considerations using water-based nanofluids. The numerical investigation revealed that Ag/water nanofluids outperformed Al<sub>2</sub>O<sub>3</sub>/water nanofluids, leading to improved energy and exergy efficiencies. They also noted that the overall energy and exergy efficiency increased with a higher concentration of nanoparticles in the base fluids but decreased with increasing velocity in the channel.

Xu and Kleinstreuer<sup>25</sup> examined a high photovoltaic thermal system using water-based nanofluids for cooling purposes. They found that increasing nanoparticle concentration improved the electrical efficiency of PV/T systems while minimizing entropy generation. Additionally, they suggested that lowering the inlet temperature would result in an increase in electricity output. Elmir *et al.*<sup>26</sup> conducted a numerical simulation of a PV/T system with varying alumina Al<sub>2</sub>O<sub>3</sub> concentrations in water, ranging from 0% to 10%. The PV/T system comprised a silicon layer and was exposed to sunlight at a 30-degree angle. Their findings indicated a 27% increase in heat transfer rate when the volume fraction of alumina was fixed at 10% and the Reynolds number was set to 5.

An investigation was carried out by Naidu *et al.*<sup>27</sup> using the finite element method to explore different types of meshing elements for solving the three-dimensional Darcy–Brinkmann equation. This test revealed that meshing elements of quartic order provide better accuracy. Finally, it was suggested that this method can be easily employed for irregular shapes. A study was conducted by Devi and Nagaraja,<sup>28</sup> applying high-order triangular meshing alongside the finite element method to enhance the performance of wind turbine blades in the 4-digit series. The governing equations were solved numerically. Performance and increased energy production were tested with varying attack angles and non-dimensional Reynolds numbers. The results provide valuable suggestions for optimizing blade shapes to achieve improved performance, even in icing and morphing conditions. Another study was discovered<sup>29</sup> that focused on the application of nanofluids. In this study, the Darcy equation and Fourier's law of heat conduction were employed to investigate heat transfer characteristics, including conduction, convection, and radiation, within a porous fin featuring an exponential profile. The governing equations were converted into non-dimensional forms using non-dimensional terms. The study deduced that introducing porosity to the fin and utilizing the exponential profile effectively increased the rate of heat transfer. Furthermore, the use of nanomaterials enhanced heat transfer beyond what was initially expected. A curved surface was analyzed with the application of Casson-based nanoliquid, considering the effects of porosity and thermal radiation.<sup>30</sup> The ordinary differential equations (ODEs) used to obtain the numerical solution for the actual problem resulted from a non-dimensional formulation. It was observed that increasing the curvature of the surface increased velocity but decreased



temperature. Furthermore, it was demonstrated that improving thermal radiation increased both temperature and the Hartmann number. These findings may be applied to enhance the performance of heat exchangers and devices intended for cooling purposes. Many of the literature can be viewed<sup>31–37</sup> that contains the application of nanomaterials in the applied engineering.

After reviewing the existing literature on photovoltaic thermal systems and the use of nanofluids to enhance heat transfer rates for various applications, including photovoltaic thermal systems, this article aims to improve the electrical performance of a PV/T (photovoltaic/thermal) system. This improvement is achieved by introducing hybrid nanofluids, created by mixing titanium oxide and silver nanoparticles in water. The configuration of this PV/T system is kept simple, consisting of a flow channel containing a rotating circular cylinder, an absorber to increase the heat gain from solar radiation, and polycrystalline silicon, a well-known component for electricity generation. To simulate this approach, incompressible Navier–Stokes and energy equations are employed in COMSOL multiphysics to obtain numerical solutions for velocity field components, pressure, and temperature. To enhance the PV/T system's performance, we conducted trials varying parameters such as Reynolds number, volume fraction, and the rotational velocity of the cylinder. The first section of this article outlines the problem formulation, including the construction of the photovoltaic thermal system, geometrical measurements of the PV/T system, thermophysical properties of both the cell construction and hybrid nanofluids, and the governing partial differential equations. In the subsequent part of this article, we verify the numerical results against available correlations and conduct a mesh-independent study to ensure precision and minimize errors in the numerical work. The results discussion section presents velocity, pressure, and temperature data against the increasing values of the selected parameters. Following this, we assess the efficiency of the PV/T system, which is the central focus of this article. Finally, the conclusion section summarizes the key findings and contributions of the study.

## 2. Problem formulation

In this study, we will analyze a photovoltaic thermal system composed of three distinct components: polycrystalline silicon, copper as an absorber, and a flow channel that incorporates a metallic cylinder (see Fig. 1). Due to the channel's symmetry along the  $z$ -axis, we model the problem in two dimensions. Consider a cylinder with a radius ( $R$ ) fitted at the center of the channel, which is rotated along the  $y$ -direction with a velocity  $\omega$ . We define an aspect ratio of 0.15, representing the ratio between the channel's height and the cylinder's radius. Our study aims to investigate the influence of forced convection on a mixture of nanoparticles, including titanium oxide and silver, dispersed in a water-based fluid. This mixture is introduced into the flow channel through the left entrance with an initial velocity ( $u_{in}$ ), which varies based on the Reynolds number ( $Re$ ). The nanoparticles blend is introduced at a constant temperature ( $T_{in} = 50^\circ\text{C}$ ) into the fluid system. At the right exit of the channel, a zero pressure condition is imposed, while all other walls are considered to have no-slip boundary conditions, as shown in Fig. 1. Solar radiation falls on the system, undergoing a bifurcation, with one part harnessed for electrical energy generation and the other part transmitted through the system to raise its temperature. Our primary objective is to enhance the performance of PV/T systems by actively cooling them using hybrid nanofluids. This cooling process will lower the temperature, optimizing electrical energy production. Table 1 summarizes the construction of the PV/T system.

In this numerical investigation, we will focus on pure conduction within the top two layers of the PV/T system, consisting of silicon and a copper absorber. To examine this phenomenon, it is crucial to determine the thermophysical characteristics of these two solid materials, which are presented in Table 2. Our primary objective is to reduce the temperature of the PV/T system since an increase in its temperature can adversely affect electricity generation levels. By concentrating on temperature reduction within the PV/T system, we aim to optimize and enhance its electrical output. It is well-known that increasing the fluid velocity can lead to temperature reduction. In this computational simulation of photovoltaic/thermal (PV/T) systems, our

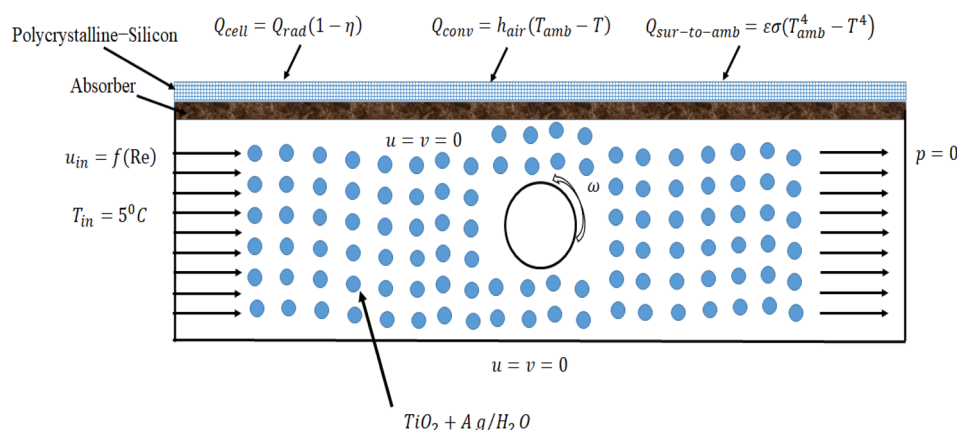


Fig. 1 Construction of photovoltaic thermal system (PV/T) with boundary conditions for finite element investigation.



Table 1 Parameter to construct the observed channel of PV/T system

Symbols	Values	Description
$H_{in}$	20 [mm]	Inlet height
$H_{out}$	$H_2$	Outlet height
$L_{cell}$	100 [mm]	Length of channel
$H_{absorber}$	1 [mm]	Height of the absorber
$H_{silicon}$	1 [mm]	Height of the silicon panel
$A$	$L_{cell}H_{in} - \pi R^2$ [mm <sup>2</sup> ]	Flow channel's area
$P$	$2L_{cell} + 2H_{in} + 2\pi R$ [mm]	Perimeter of the flow channel
$d_h$	$4 \times A/P$ [mm]	Hydraulic diameter of the flow channel
$A_r$	0.15	Aspect ratio from cylinder's radius to the channel's height
$R$	$aH_{in}$ [mm]	Radius of the cylinder
$\omega$	0.01, 0.05, 0.09, 0.1, 0.2 [m s <sup>-1</sup> ]	Velocity of cylinder

Table 2 Material properties of PV/T<sup>38</sup>

Symbols	Values	Description
$(c_p)_{abs}$	386 [J kg <sup>-1</sup> K <sup>-1</sup> ]	Specific heat at constant pressure for absorber (copper)
$\rho_{abs}$	8900 [kg m <sup>-3</sup> ]	Density of copper
$(\kappa_t)_{abs}$	398 [W m <sup>-1</sup> K <sup>-1</sup> ]	Thermal conductivity of copper
$\rho_{sili}$	2330 [kg m <sup>-3</sup> ]	Density of silicon
$(c_p)_{sili}$	716 [J kg <sup>-1</sup> K <sup>-1</sup> ]	Heat capacity of silicon
$(\kappa_t)_{sili}$	157 [W m <sup>-1</sup> K <sup>-1</sup> ]	Thermal conductivity of silicon
$\beta$	0.003 [1/K]	Temperature coefficient
$E$	0.9	Emissivity
$\eta_{ref}$	0.2	Reference efficiency of cell
$A_c$	$L_{cell}H_{silicon}$	Area of one cell

goal is to improve electrical efficiency by increasing the Reynolds number and elevating the circular cylinder's velocity. This study aims to provide valuable insights for optimizing PV/T performance. As a result, the numerical investigation will span Reynolds numbers ranging from 100 to 1000, with an increase in the number of rotations from 0.01 to 0.2 m s<sup>-1</sup>.

To reduce the temperature of the PV/T system, we will conduct experiments within the flow channel using a coolant, such as nanofluids. This numerical modeling study aims to analyze the behavior of the flow channel under forced convection, employing a hybrid mixture composed of titanium oxide (TiO<sub>2</sub>) and silver (Ag) with water as the base fluid. To implement the model of this hybrid mixture through the governing partial differential equations, we require the thermophysical properties of the materials, as summarized in Table 3. It's noteworthy that the thermal conductivity of silver exceeds that of titanium oxide. Therefore, we will use a titanium oxide volume fraction that is twice as large as that of silver. The numerical analysis will involve varying the silver volume fraction within the range of 0.01 to 0.2 to examine its effects. After establishing five values for each of the Reynolds number, volume fraction, and the cylinder's speed, we will develop 125 different models and simulations for the current study.

### 2.1. Constitutive partial differential equations

We will implement a finite element procedure using the commercial software COMSOL 6.0. Since our investigation involves three different domains, with pure conduction occurring in the top two layers of the channel, handled by energy equations

in two dimensions. The temperature distribution in these top two layers is a result of solar radiation. Three distinct heat flux conditions will be applied to the top two layers of the silicon cell, as illustrated in Fig. 1. In the two-dimensional flow channel, we will analyze a combined convection and conduction problem using the heat equation and the incompressible Navier–Stokes equations. Let “ $V$ ” represent the velocity field in two dimensions, with “ $V_x$ ” and “ $V_y$ ” as its components along the  $x$  and  $y$ -axes, respectively. The governing partial differential equations for the incompressible Navier–Stokes and energy equations can be written as follows:

$$\frac{\partial V_x}{\partial x} = -\frac{\partial V_y}{\partial y} \quad (1)$$

$$V_x \frac{\partial V_x}{\partial x} + V_y \frac{\partial V_x}{\partial y} + \frac{1}{\rho_{nf}} \frac{\partial p}{\partial x} = \mu_{hnf} \left( \frac{\partial^2 V_x}{\partial x^2} + \frac{\partial^2 V_x}{\partial y^2} \right) \quad (2)$$

$$V_x \frac{\partial V_y}{\partial x} + V_y \frac{\partial V_y}{\partial y} + \frac{1}{\rho_{nf}} \frac{\partial p}{\partial y} = \mu_{hnf} \left( \frac{\partial^2 V_y}{\partial x^2} + \frac{\partial^2 V_y}{\partial y^2} \right) \quad (3)$$

$$V_x \frac{\partial T}{\partial x} + V_y \frac{\partial T}{\partial y} = \alpha_{hnf} \left( \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right) \quad (4)$$

### 2.2. Further calculation formulas

After getting the numerical results, the mean temperature of the domain will be computed as eqn (7), the heat transfer coefficient will be computed by (6) and the average Nusselt number



Table 3 Properties of nanofluids to carry the convection process<sup>39</sup>

Description	Symbols	Values
Density of TiO <sub>2</sub>	$\rho_{np1}$	4250 [kg m <sup>-3</sup> ]
Density of (Ag)	$\rho_{np2}$	10.5 [kg m <sup>-3</sup> ]
Total density of nanoparticles	$\rho_{np}$	$\frac{\phi_1 \rho_{np1} + \phi_2 \rho_{np2}}{\phi_1 + \phi_2}$
Specific heat at constant pressure of titanium oxide	$C_{pnp1}$	686.2 [J kg <sup>-1</sup> K <sup>-1</sup> ]
Specific heat at constant pressure of silver	$C_{pnp2}$	235 [J kg <sup>-1</sup> K <sup>-1</sup> ]
Over all specific heat at constant pressure of nanoparticles	$C_{pnp}$	$\frac{\phi_1 \rho_{np1} C_{pnp1} + \phi_2 \rho_{np2} C_{pnp2}}{\rho_{np}}$
Volume fraction of (Ag)	$\phi_2$	0.01, 0.05, 0.09, 0.1, 0.2
Volume fraction of TiO <sub>2</sub>	$\phi_1$	$2\phi_2$
Total volume fraction of nanoparticles in the base fluid	$\phi$	$\phi_1 + \phi_2$
Thermal conductivity of TiO <sub>2</sub>	$\kappa_{np1}$	8.952 [W mK <sup>-1</sup> ]
Thermal cond. Of silver (Ag)	$\kappa_{np2}$	429 [W mK <sup>-1</sup> ]
Overall thermal conductivity	$\kappa_{np}$	$\frac{\phi_1 \kappa_{np1} + \phi_2 \kappa_{np2}}{\phi}$
Density of water	$\rho_{bf}$	998 [kg m <sup>-3</sup> ]
Total density of nanofluids	$\rho_{hnf}$	$\rho_{bf}(1 - \phi) + \phi \rho_{np}$
Specific heat at constant pressure of water	$C_{pbf}$	4182 [J kg <sup>-1</sup> K <sup>-1</sup> ]
Total specific heat of the nanofluids at the constant pressure	$C_{phnf}$	$\frac{\rho_{bf}(1 - \phi) C_{pbf} + \rho_{np}(1 - \phi) C_{pnp}}{\phi}$
Thermal conductivity of water	$\kappa_{bf}$	0.597 [W mK <sup>-1</sup> ]
Total thermal conductivity of hybrid mixture	$\kappa_{hnf}$	$\left( \frac{\kappa_{np} + 2\kappa_{bf} + 2(\kappa_{np} - \kappa_{bf})\phi}{\kappa_{np} + 2\kappa_{bf} - 2(\kappa_{np} - \kappa_{bf})\phi} \right) \kappa_{bf}$
Water viscosity	$\mu_{bf}$	0.000998 [Pas]
Viscosity of nanofluid	$\mu_{hnf}$	$\frac{\mu_{bf}}{(1 - \phi)^{2.5}}$
Reynolds number	Re	100
Inlet velocity	$u_{in}$	$\frac{\text{Re} \mu_{hnf}}{\rho_{hnf} D_h}$
Inlet temperature	$T_{in}$	5 °C
Heat flux	$Q_{rad}$	1000 [W m <sup>-2</sup> ]
Reference temperature	$T_{ref}$	25 °C
Ambient	$T_{amb}$	45 °C

will be computed by (5). Eqn (9) demonstrates the efficiency of the cell in terms of percentage, with respect to the reference efficiency measured at the reference temperature  $T_{ref}$ . Eqn (14) is presenting the total heat flux appeared for the cell. Where  $Q_{sur-to-amb}$  is presenting the radiation from surface to surroundings of the medium. In Sindh, Pakistan region the ambient temperature is mostly 45 °C in month of June–July, therefore, we are examining the efficiency of this PV/T according to Sindh, Pakistan region.

Average Nusselt number:

$$Nu = \frac{hD_h}{\kappa_{hnf}} \quad (5)$$

Heat transfer coefficient:

$$h = \frac{-k_{hnf} T_x}{T - T_b} \quad (6)$$

Bulk temperature:

$$T_b = \frac{\int_0^{H_t} V_x T dx}{\int_0^{H_t} V_x dx} \quad (7)$$

Prandtl number:

$$Pr = \frac{\mu_{hnf} C_{phnf}}{\kappa_{hnf}} \quad (8)$$

Percentage change in the cell efficiency:

$$\eta_{\%} = 100 \times \frac{\eta_{cell} - \eta_{ref}}{\eta_{ref}} \quad (9)$$

where

$$\eta_{cell} = \eta_{ref}[1 - \beta(T_{cell} - T_{ref})] \quad (10)$$

Nusselt number by Kimura *et al.*:<sup>40</sup>

$$Nu_K = 1.62 \left( \text{Re} \text{Pr} \frac{D_h}{L} \right)^{1/3} \quad (11)$$

Nusselt Number by Gryta *et al.*:<sup>41</sup>

$$Nu_G = 0.298 \text{Re}^{0.646} \text{Pr}^{0.316} \quad (12)$$

Nusselt number by Pak and Cho<sup>42</sup>





$$\text{Nu}_{\text{P\&C}} = 0.021\text{Re}^{0.8}\text{Pr}^{0.5} \quad (13)$$

$$Q_{\text{abs}} = Q_{\text{cell}} - (Q_{\text{sur-to-rad}} + Q_{\text{con}}) \quad (14)$$

Here,

The heat source in the domain:

$$Q_{\text{cell}} = Q_{\text{sun}}(1 - \eta) \quad (15)$$

Heat reflected surrounding:

$$Q_{\text{rad}} = \varepsilon\sigma(T_{\text{cell}}^4 - T_{\text{amb}}^4) \quad (16)$$

Heat transferred to the PV-panel by surroundings:

$$Q_{\text{conv}} = h(T_{\text{amb}}^4 - T^4) \quad (17)$$

### COMSOL working procedure

COSMOL Multiphysics software provides a general Java-based code to solve the governing equations for relevant phenomena, yielding numerical solutions. Additionally, it offers robust graphics for post-processing. The software comprises the following general steps applicable to various problem types. While it is user-friendly, it does require a thorough study to identify the appropriate interfaces and boundary conditions for the specific problem.

Step 1: Begin by configuring the parameters necessary for constructing the channel's geometry and defining the material properties required for the domain of the channel. Additionally, when incorporating the flow of nanomaterials, establish the parameters essential for implementing the nanofluids model

Step 2: Configure the model's geometry using the parameters provided in step 1

Step 3: Identify the materials within the designated domain. Utilize the specified material properties as exemplified here; at the top of PV/T, polycrystalline silicon is affixed. In this domain, apply the material properties of silicon by selecting the material button accessible in the model builder window

Step 4: Identify and apply the boundary conditions along each domain. In this context, we are conducting parallel computations for both the Navier–Stokes equation and the energy equation. Both equations will be solved concurrently, and it is essential to impose the appropriate conditions for fluid flow and heat transfer

Step 5: Determine the optimal number of elements required to achieve precise results with minimal error. It is advisable to conduct a comparative analysis of the numerical results against existing literature to validate the accuracy of your simulations

Step 6: Execute the program by selecting specific parameters to assess the influence of the variables of interest

Step 7: Perform post-processing on the obtained numerical simulation results

### 3. Validation and accuracy with meshing process

Fig. 2 illustrates that the current geometry under observation is meshed with irregular triangular elements to obtain

a numerical solution. Achieving a high degree of numerical accuracy is a crucial aspect of the numerical procedure. To address this, a mesh independence study is conducted, involving the use of different numbers of elements for meshing the geometry to obtain numerical results for specific variables of interest. COMSOL 6.0 automatically assesses the geometry's complexity and generates a dense mesh in regions where obtaining a solution is typical. In our geometry, a high-density mesh is particularly needed around the cylinder and in the multiple domains. We conducted experiments using various element counts, ranging from 1000 to 100 000. Subsequently, we calculated average values for velocity magnitude, temperature, and pressure at the outlet of the channel (refer to Fig. 3). The improvement in the average velocity field is evident in Fig. 3(a) when the number of elements is increased. We found that achieving mesh independence requires having more than 20 000 elements. In Fig. 3(b) and (c), we observe that achieving mesh independence for temperature and pressure requires using a number of elements exceeding 15 000. However, to ensure higher accuracy, we conducted 125 simulations employing approximately 61 450 elements and achieved a residual of  $10^{-6}$ .

We are now presenting Table 4, which offers a comprehensive comparison of the average Nusselt number throughout the flow channel. The average Nusselt number at the channel outlet is determined in this study by applying eqn (5)–(7) and utilizing experimentally validated correlations (11)–(13) from the existing literature. Based on the data presented in Table 4, it is clear that the findings of this study align well with the existing correlations.

#### 3.1. Error analysis

Finally, an error analysis is done for the continuity equation attached in the Fig. 4. It can be noticed that increasing the length of the channel the error in computing the continuity equation is increased. This is because at the middle of the channel below which the error is calculated due increasing in the turbulence reason the error is slightly occur. However, observed for all other values of  $x$  away from the cylinder we can see that no turbulence in the region a best result to compute the continuity equation is given by the algorithm. Therefore, we recommend to create a dense mesh near the wake of the cylinder.

### 4. Results and discussion

This article presents a numerical study of a photovoltaic thermal system that incorporates the transport of hybrid nanofluids. These nanofluids consist of titanium oxide and silver nanoparticles, with water as the base fluid. The PV/T system has a simple construction, comprising only a polycrystalline silicon layer on top, copper as an absorber below the silicon layer, and a flow channel that includes a moving cylinder with a speed denoted as  $\omega$ . Our primary objective in this study is to reduce the cell temperature to enhance its electrical efficiency. Therefore, we are conducting a parametric study



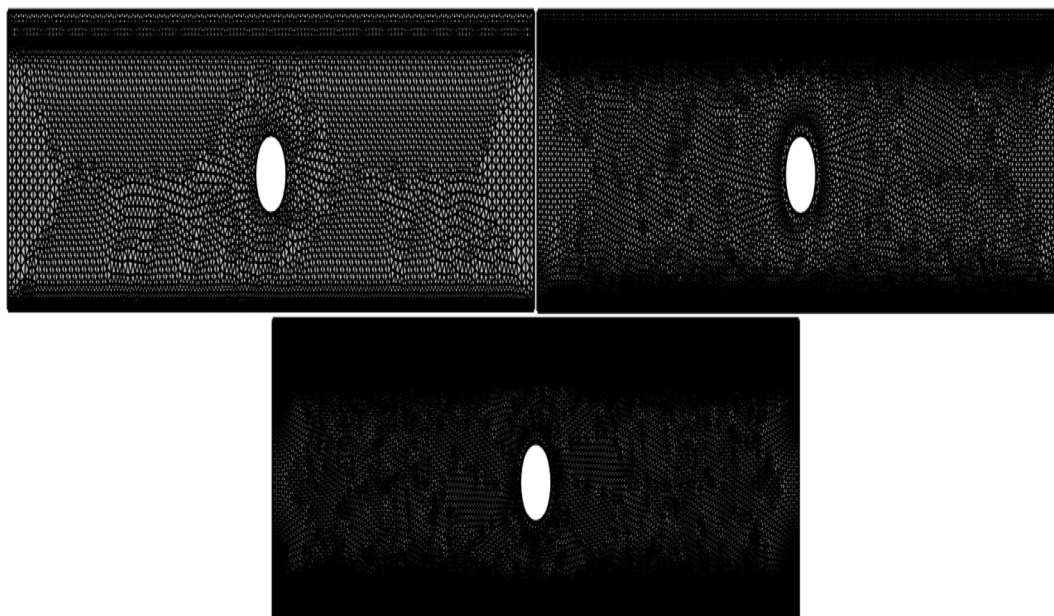


Fig. 2 Three step meshing procedure of photovoltaic thermal system from fine mesh to finest mesh with irregular triangular elements.

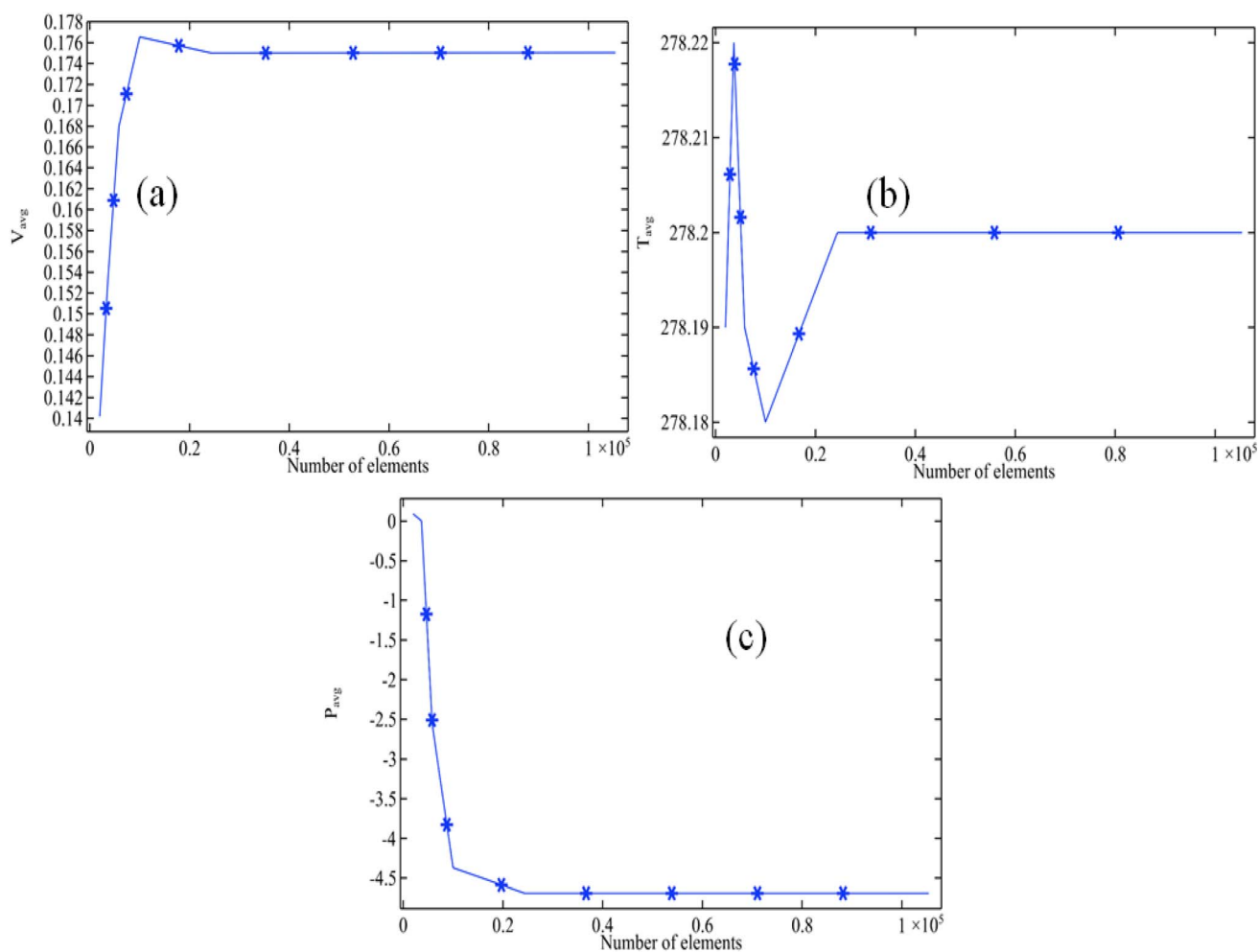
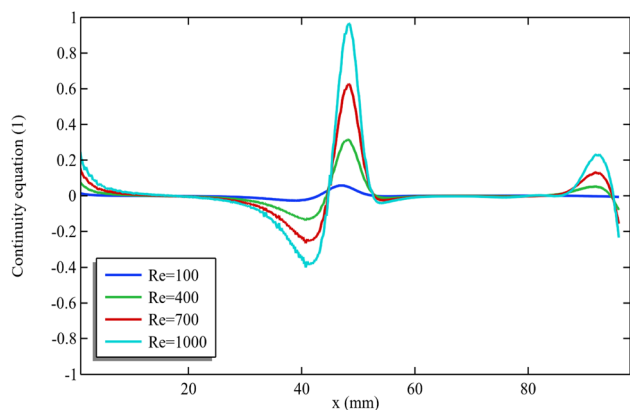


Fig. 3 Mesh independent outcomes when  $Re = 1000$ ,  $w = 0.2$  and  $\phi_2 = 0.2$  (a) velocity magnitude at the outlet (b) average temperature at the outlet (c) average pressure at the outlet.



**Table 4** Comparison of average Nusselt with the present work to the available correlations for laminar

Re	$\phi_2$	$\omega$	$Nu_K$	$Nu_G$	$Nu_p$	$Nu_{\text{present}}$
100	0.01	0.01	6.2224	6.903	2.1076	5.0777
100	0.05	0.01	6.2224	6.903	1.8009	4.9754
100	0.09	0.01	6.2224	6.903	1.6082	4.9112
100	0.1	0.01	6.2224	6.903	1.5726	4.8993
100	0.2	0.01	6.2224	6.903	1.4126	4.846
300	0.01	0.01	8.9742	14.036	5.0755	9.3621
300	0.05	0.01	8.9742	14.036	4.337	9.1159
300	0.09	0.01	8.9742	14.036	3.8729	8.9612
300	0.1	0.01	8.9742	14.036	3.7871	8.9326
300	0.2	0.01	8.9742	14.036	3.402	8.8042
500	0.01	0.01	10.64	19.524	7.6376	12.601
500	0.05	0.01	10.64	19.524	6.5263	12.23
500	0.09	0.01	10.64	19.524	5.8279	11.997
500	0.1	0.01	10.64	19.524	5.6988	11.954
500	0.2	0.01	10.64	19.524	5.1193	11.761
800	0.01	0.01	12.445	26.451	11.124	16.673
800	0.05	0.01	12.445	26.451	9.5053	16.134
800	0.09	0.01	12.445	26.451	8.4881	15.794
800	0.1	0.01	12.445	26.451	8.3	15.732
800	0.2	0.01	12.445	26.451	7.456	15.45
1000	0.01	0.01	13.406	30.552	13.298	19.085
1000	0.05	0.01	13.406	30.552	11.363	18.44
1000	0.09	0.01	13.406	30.552	10.147	18.035
1000	0.1	0.01	13.406	30.552	9.9222	17.96
1000	0.2	0.01	13.406	30.552	8.9132	17.624

**Fig. 4** Error analysis for the continuity equation near the base of the rectangular channel when  $\phi_1 = \phi_2 = 0.001$  and  $\omega = 0.01$ .

involving Reynolds number, the volume fraction of silver (half of titanium oxide), and the speed of the rotating cylinder. In the results discussion, we present numerical results for velocity patterns, pressure, temperature, and electrical efficiency percentage, calculated using formula (9).

#### 4.1. Velocity field and pressure distribution in the flow channel

The streamline pattern of the velocity field is depicted in Fig. 5. It is evident that the rotation of the cylinder has a notable impact on the flow pattern of the material. Fig. 5 is generated by fixing  $Re = 1000$  and  $\omega = 0.01$ . In Fig. 5(a), with a significance level of 0.05,

the presence of a vortex along the circular cylinder is apparent, indicating fluid recirculation. Additionally, three more vortices are observed at the lower corner of the channel's end. Fig. 5 illustrates that the maximum velocity of the hybrid nanofluids, due to rotation, appears below the cylinder. Notably, as the velocity of the cylinder increases from 0.05 to 0.1 (see Fig. 5(a–c)), the size of the vortex along the cylinder and other vortices also increases. However, when  $\omega = 0.2$  is observed (see Fig. 5(d)), the vortex along the cylinder and other vortices at the corner's end appear smaller. This is because the fluid is compressed due to the additional rotational power applied to the cylinder.

Due to the rotation of the cylinder, angular momentum is generated in the surrounding area, resulting in the production of primary and secondary vortices. Primarily, when the fluid interacts with the boundary, vortex formation occurs. This is because the cylinder is continuously rotating, so when the fluid collides with it from below, the fluid accelerates, leading to a higher observed cylinder speed in the downward direction. It has also been observed that when the cylinder's speed is  $0.2 \text{ m s}^{-1}$ , the vortices begin to decrease in size. This effect may be attributed to the fact that as the rotational speed increases significantly, the fluid becomes compressed, potentially causing a reduction in the size of the vortex.

Surface plots and contour presentation of pressure is described though Fig. 6 for  $Re = 100$  and  $\phi_2 = 0.01$  and by altering the  $\omega = 0.05$ – $0.2$ . In this presentation for each case, we can see that the minimum pressure is existed along the recirculating cylinder and pressure isobars are clearly showing or indicating the recirculation of cylinder. For pressure, we can see that when  $\omega = 0.05$  only two vortices are created one is along the cylinder and other is above the cylinder. However, for the other cases, pressure is created three vortices of pressure contours. It can be seen that increasing the rotation of cylinder is creating a negative pressure inside the cylinder which is indicating most of the fluid is attracting by that region.

The appearance of vortices in response to pressure is a result of the interaction between the cylinder's surface and the fluid. Additionally, in Fig. 6(d), a negative pressure is observed, indicating that the fluid moving forward will be drawn toward this region.

#### 4.2. Temperature against the chosen parameters

In Fig. 7(a), the maximum temperature is measured along the cell against the increasing Reynolds number (100–1000) for all volume fraction (0.01–0.2) of the silver and discussed only two cases of speed of rotation of cylinder (0.01 and 0.2). When the volume fraction of silver remains constant and the cylinder rotation speed increases, it is observed that the maximum temperature decreases with an increase in the Reynolds number range of 100–1000. In Fig. 7(b), when the rotation of cylinder is fixed at  $\omega = 0.01$ , the highest temperature of the cell is moderately reducing with increasing the  $Re$ . However, when the rotation of cylinder is fixed at  $\omega = 0.2$ , then temperature of cell is decreasing quickly for moderate Reynolds number from (100–300). In this case, we found that the maximum temperature is decreasing from 298 K to 279.





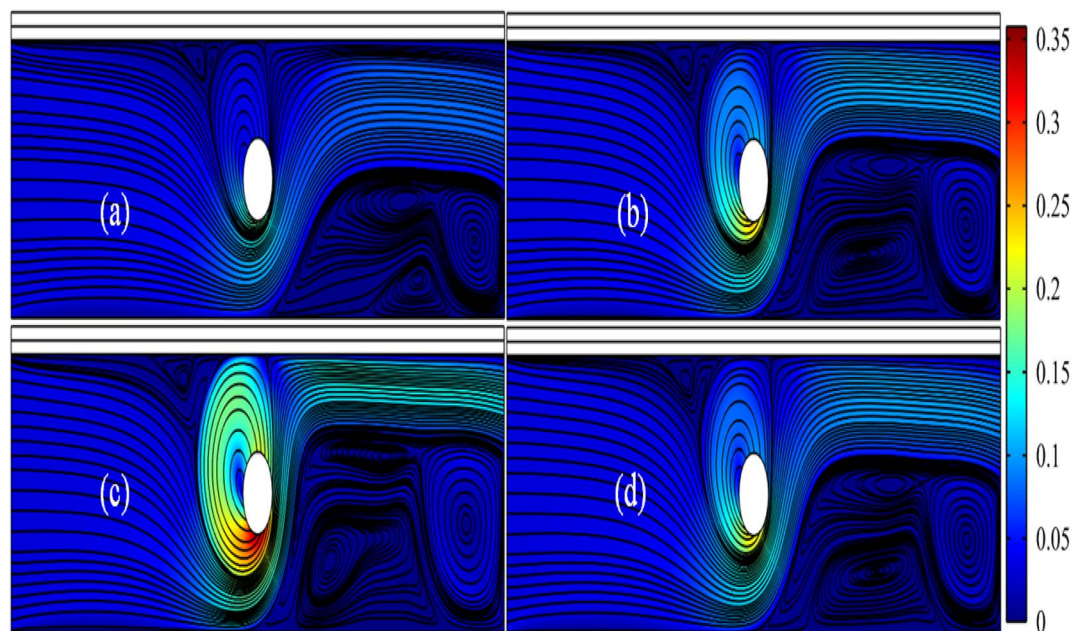


Fig. 5 Velocity surface plots and the streamlines presentation in the flow channel of photovoltaic thermal system when  $Re = 1000$ ,  $\phi_2 = 0.01$  (a)  $\omega = 0.05 \text{ m s}^{-1}$  (b)  $\omega = 0.01 \text{ m s}^{-1}$  (c)  $\omega = 0.1 \text{ m s}^{-1}$  and (d)  $\omega = 0.2 \text{ m s}^{-1}$ .

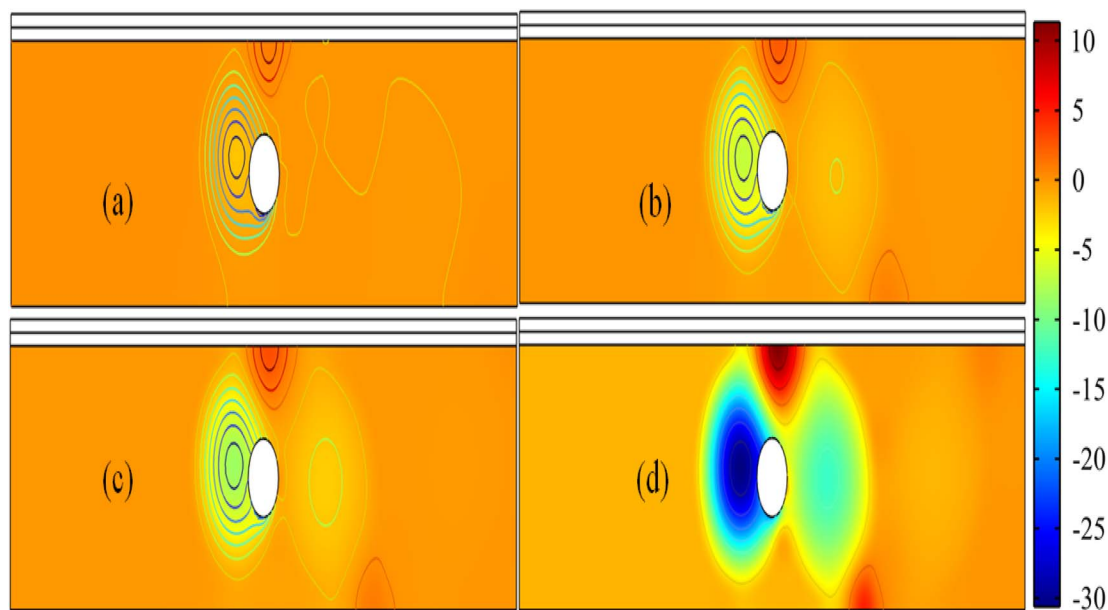


Fig. 6 Surface plots and the pressure contours presentation in the flow channel of photovoltaic thermal system when  $Re = 100$ ,  $\phi_2 = 0.01$  (a)  $\omega = 0.05 \text{ m s}^{-1}$  (b)  $\omega = 0.01 \text{ m s}^{-1}$  (c)  $\omega = 0.1 \text{ m s}^{-1}$  and (d)  $\omega = 0.2 \text{ m s}^{-1}$ .

An increase in the Reynolds number results in an increased flow rate in the channel, indicating that more nanofluids enter the channel per unit of time. This increase in flow rate subsequently leads to a decrease in the maximum temperature. It can be anticipated that increasing the cylinder's rotation speed will further enhance the flow rate in the channel, consequently causing a more pronounced reduction in temperature.

In Fig. 8, the graph illustrates the relationship between the maximum temperature of a cell and two variables: the volume fraction of silver and the rotational speed of the cylinder. The data shown is for two Reynolds numbers,  $Re = 100$  and  $Re = 1000$ . The results indicate that when  $Re = 100$ , increasing the volume fraction of silver leads to a decrease in the maximum cell temperature, while keeping the rotation rate constant. The maximum cell temperature can be achieved minimum with



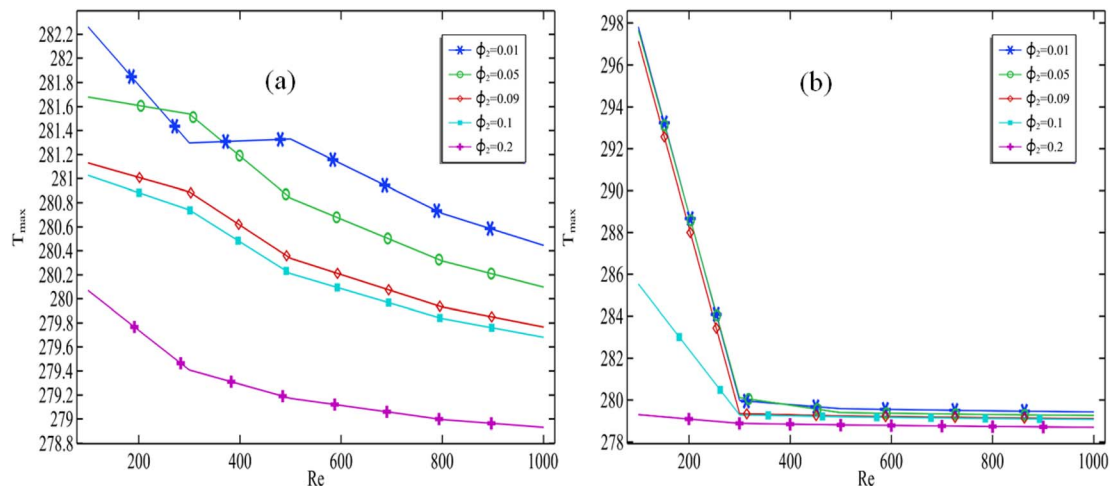


Fig. 7 Maximum cell temperature against  $Re$  with altering the volume fraction of silver when (a)  $\omega = 0.01$  and (b)  $\omega = 0.2$ .

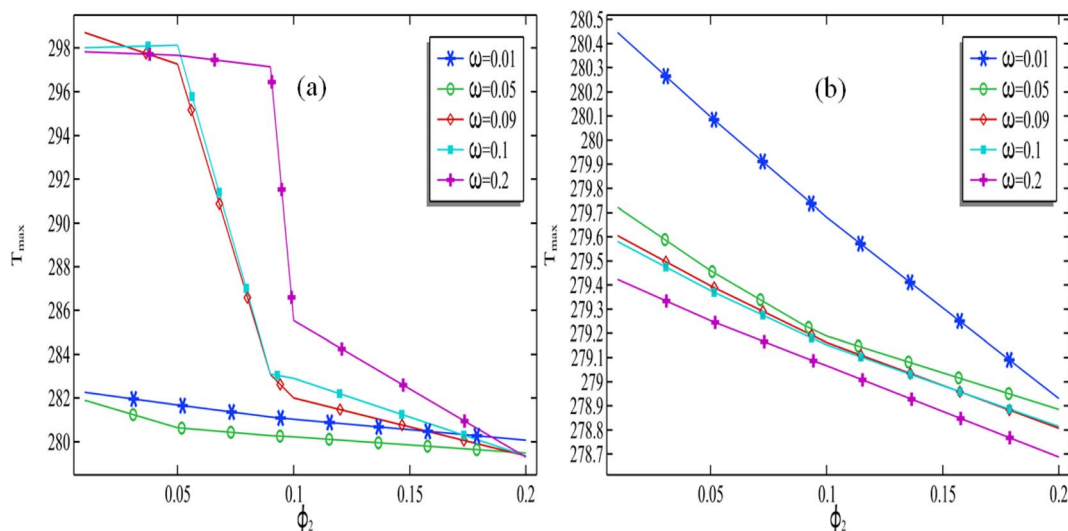


Fig. 8 Maximum cell temperature against volume fraction of silver with altering the cylinder rotation when (a)  $Re = 100$  and (b)  $Re = 1000$ .

raising the silver when  $Re = 100$  and the cylinder rotation must be kept at  $\omega = 0.05$  see Fig. 8(a). In Fig. 8(b), it can be understood that the maximum temperature against the volume fraction of the silver fraction is decreasing for each fixed rotation when  $Re = 1000$ . At this graph, we *ca.* understand when the  $Re = 1000$ , the maximum cell temperature can be maintained minimum when  $\omega = 0.2$ . From this discussion, it can be concluded that to reduce the temperature of the cell high Reynolds number must be played with high speed of the cylinder. Based on the analysis of specific cases, it can be inferred that as the volume fraction of cell increases, there is a consistent decrease in the maximum temperature reached by the cell.

As mentioned earlier, it is expected that nanofluids will act as coolants. Therefore, it can be observed that increasing the concentration of nanomaterials enhances the thermal conductivity of the resulting fluid, contributing to a decrease in temperature. Additionally, it has already been explained that an

increase in the Reynolds number supports an increase in the flow rate, which in turn leads to a more significant temperature reduction, as illustrated in Fig. 8(b).

A graphical representation, in Fig. 9, has been generated to evaluate the highest recorded temperature within the cell. This measurement is obtained by varying the rotational speed of the cylinder while keeping the silver volume constant and increasing the  $Re$ . It is evident that as the number of rotations of the cylinder increases while keeping the Reynolds number and volume fraction of the cylinder constant, there is a decrease in the maximum temperature of the cell. However, there is one exception observed in Fig. 9(a) where the Reynolds number is 100 and the volume fraction is 0.01. It can be seen that increasing the Reynolds number when rotation of cylinder is varied, put a negative impact in maximum temperature of the cell. In Fig. 9(b), the silver content remains constant at a volume fraction of  $\phi_2 = 0.2$ , it is obvious that with taking enhancement



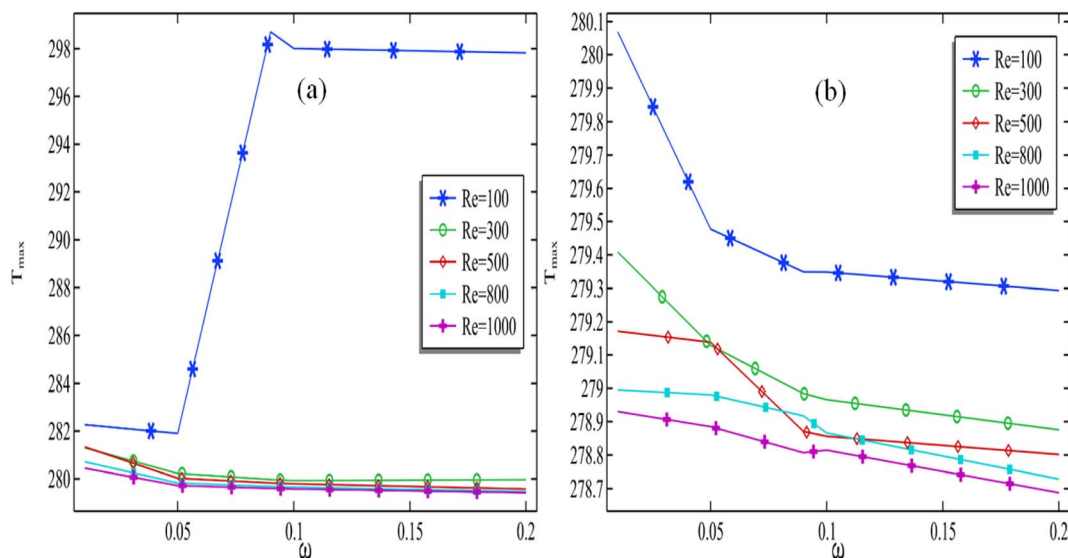


Fig. 9 Maximum cell temperature against rotation of cylinder with altering Reynolds number when (a)  $\phi_2 = 0.01$  and (b)  $\phi_2 = 0.2$ .

to the speed of the cylinder as well as the Reynolds number, the optimized cell temperature can be declined sufficiently.

This demonstrates that when the incoming fluid's speed is significantly lower than the rotation of the cylinder, it effectively circulates the fluid around the cylinder without expelling it from the channel. Consequently, for moderate Reynolds numbers, such as  $Re = 1000$ , the maximum temperature is found to increase. However, for all other cases, the maximum temperature decreases with an increase in the rotation of the cylinder. Increasing the cylinder's rotation consistently contributes to temperature reduction, particularly for higher Reynolds numbers.

#### 4.3. The percentage of cell efficiency *via* the reference efficiency

In this section, our focus is on determining the percentage of cell efficiency in relation to the reference efficiency, which is mathematically defined in eqn (9). In the previous section we have measured the temperature (max) along the cell by altering the selected parameters  $Re$ ,  $\phi_2$  and  $\omega$ .

In Fig. 10(a), The efficiency of the cell, decreases as we move along the channel from the inlet to the outlet. This decline in efficiency can be attributed to the reference efficiency. The graphs presented in this study were generated using a fixed silver volume fraction of 0.2, with  $\omega = 0.2$ . We observe initially, the cell efficiency is declined from starting of the length to the end of the length. As, we set the rotating cylinder at the middle of the channel, when hybrid fluid passed through the position the cell efficiency is further improved. It is very clear from Fig. 10(a), improving the Reynolds number the cell efficiency is improved further. It can be seen that by applying the present model of photovoltaic cell with the transport of hybrid nano-fluids, the maximum cell efficiency due to the reference efficiency can be achieved up to 5.93. Moreover, fixing the cylinder at the middle of the flow channel produced the contraction

region for the material at the middle of the channel which is the reason of improvement of the cell efficiency.

Fig. 10(b) presents a graph illustrating the relationship between cell efficiency (expressed as a percentage) and cell length, while increasing the volume fraction of silver, at a Reynolds number of 1000 and with a constant value of  $\omega = 0.2$ . The cell efficiency% is declined first from the initial length of the channel but due to the presence of the cylinder at the middle the cell efficiency is further improving along the length of the channel for each case of fixed volume fraction of the silver. The enhancement of cell efficiency in terms of cell length is observed when increasing the concentration of silver nano-particles in the base fluid. The maximum cell efficiency is observed at the end of the cell for a moderate volume fraction of silver. However, for a higher volume fraction, the maximum efficiency percentage due to reference efficiency is found at the channel. By progressively increasing the volume fraction within the range of 0.01–0.2, the efficiency of the cell, expressed as a percentage, is observed to improve from 5.68% to 5.93% at the channel. It is evident, based on Fig. 10(b), that positioning the cylinder at the center of the channel consistently enhances the overall efficiency of the cell.

In Fig. 10(c), the graphic representation illustrates a noticeable decrease in cell efficiency percentage as we move along the length of the channel, regardless of the cylinder's rotation speed. Although, a clear pattern of for the cell efficiency cannot be deducted from here against the rotational speed of the cylinder because when the rotational speed  $\omega = 0.01$ , the cell efficiency% is moderate as we compared the greater values of rotational speed of cylinder at the middle of the flow channel. When we set the rotational speed of the cylinder to  $\omega = 0.2$ , it becomes evident that the cell efficiency at the middle of the channel improves. Moreover, it is observed that when  $\omega = 0.01$ , the cell efficiency reaches its maximum at the channel's inlet and decreases towards the outlet. Conversely, when  $\omega = 0.2$ , this



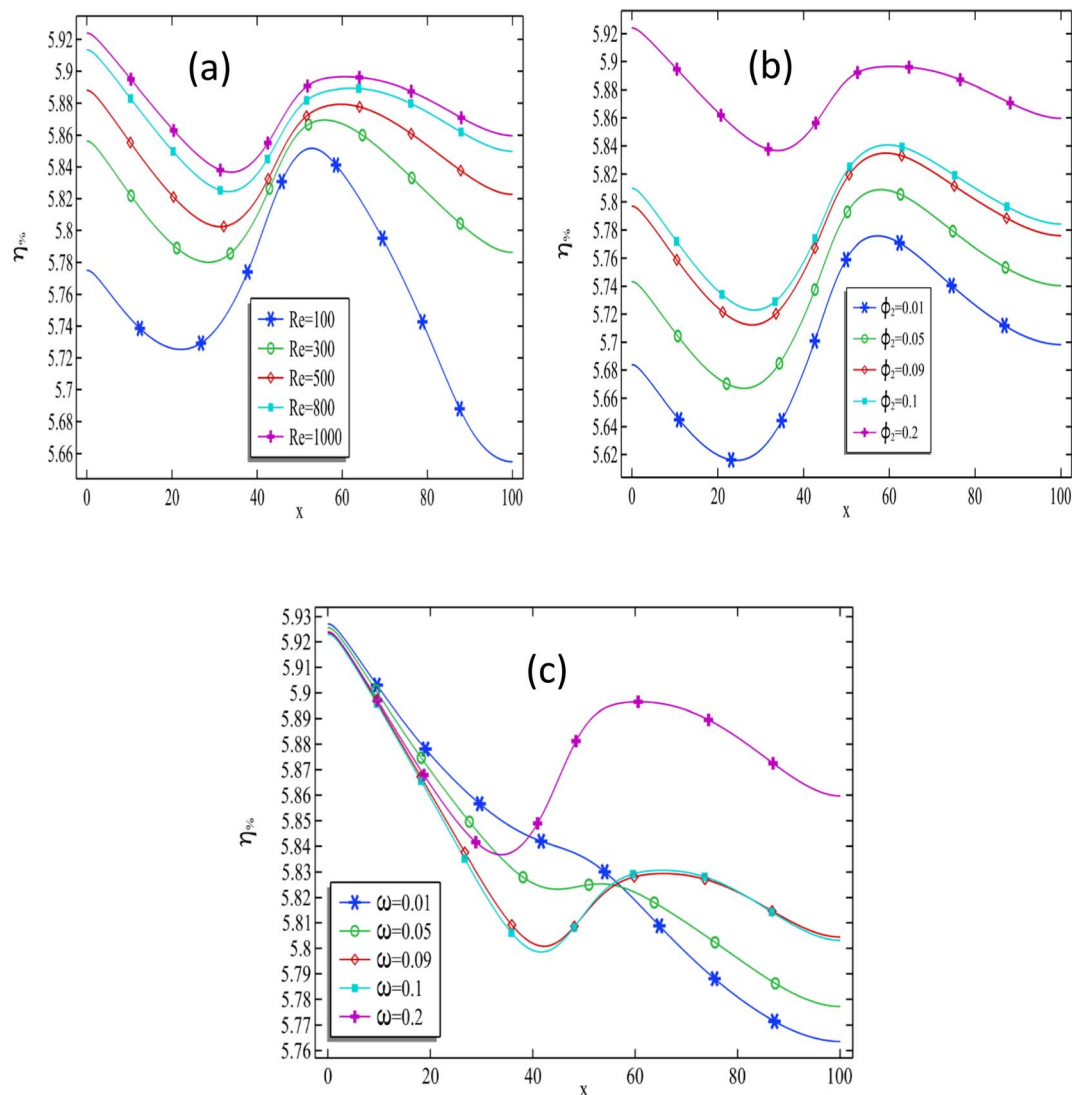


Fig. 10 The cell efficiency% against the length of the cell for (a) all particulars Reynolds numbers (b) all particulars volume fraction of silver (c) all particulars rotation of the cylinder.

pattern is reversed. Hence, based on these findings, it can be concluded that increasing the rotational speed of the cylinder consistently leads to a higher cell efficiency for the cylinder.

Impacts of Reynolds number, volume fraction and cylinder's rotation is almost clear on the temperature. In return we also know that decreasing in the cell temperature implies increase in the cell efficiency. Therefore the results above can be expected according to impact.

## 5. Conclusions

In this current numerical study, we conducted an examination of a two-dimensional photovoltaic thermal system that incorporates three distinct domains, each featuring a rotating cylinder positioned at the center of the channel. While various configurations of PV/T systems are available for numerical investigation, our simulation focuses on a 2D PV/T system consisting of polycrystalline silicon, copper, and a flow

channel. These thermal systems are designed to generate electricity through solar radiation, but their efficiency decreases as the solar cell temperature rises. To control the temperature, a coolant such as nanofluids is circulated through the flow channel of this system to maintain the cell's temperature. Therefore, we are investigating the PV/T cell by using a hybrid mixture of  $\text{TiO}_2$  and silver, with water as the base, while maintaining the volume fraction of  $\text{TiO}_2$  twice that of silver. The parametric study involves varying the Reynolds number from 100 to 1000, adjusting the volume fraction of silver from 0.01 to 0.2, and changing the rotational speed of the cylinder from 0.01 to 0.2  $\text{m s}^{-1}$ . We have successfully resolved the problem at hand using Python coding within the COMSOL 6.0 software platform, considering the governing Navier equations and the energy equation. The following concluding points are provided below:

- Due to rotation of the circular cylinder, a vortex along the cylinder and three other vortices are appeared at the corner of





the exit which is down in the channel. The size of these four vortices is increased from 0.01–0.1 m s<sup>-1</sup> of speed of cylinder and then reduced.

- It was found that due to recirculation of the cylinder the maximum speed of the mixture and the minimum pressure can only be deducted along the cylinder.

- The temperature of the cell decreases with increasing Reynolds number and volume fraction of silver. It was noticed that the maximum temperature of the cell is decreased along the rotation of the cylinder when the range of the Reynolds number is keeping higher.

- When Reynolds number is kept constant at Re = 100, it was observed that the minimum value of the maximum cell temperature occurs when the value of omega is 0.05. The same case exists for Re = 1000 when omega = 0.2.

- The cell efficiency% due to reference efficiency is declined along the length of the channel but attaching a rotating cylinder at the middle of the channel is improving further as it was shown though graphs.

- The cell efficiency along the length of the channel is always improved by increasing the Reynolds number from 100 to 1000. The maximum cell efficiency was found when Re = 1000, phi2 = 0.2 and omega = 0.2 m s<sup>-1</sup> and it was found 5.93% cell efficiency was achieved due to reference efficiency.

- Increasing the volume fraction of silver always enhances cell efficiency. This improvement can only be achieved through cylinder rotation when Reynolds numbers are maintained at high levels or by keeping the inlet velocity high.

## 6. Future recommendations

In this current article, we have developed a formulation to investigate and enhance the performance of a photovoltaic thermal system with the simplest construction. We recommend that the problem can be extended further by considering different configurations, such as using a glazing pipe and glass cover. Initially, a single rotated cylinder was placed in the middle of the channel; however, the problem could be further extended by introducing two circles in the middle of the channel. These circles could be attached at 25% and 75% of the channel's length. The investigation of enhancing the performance of the PV/T system was conducted using laminar flow and the passage of nanoparticles. To expand upon this work, the extension of turbulence flow and the application of the ternary nanofluid model could be considered.

## Conflicts of interest

There are no conflicts to declare.

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