

## PAPER

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## Computational assessment of the potential of cross-catalytic coprecipitating systems for the bottom-up design of nanocomposites†

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The production of nanocomposites is often economically and environmentally costly. Silica-witherite biomorphs, known for producing a wealth of life-like shapes, are nanocomposites entirely formed through self-organization processes. Behind these precipitates are two precipitation reactions that catalyze each other. Using a simple computational approach, we show here that this type of chemical system – defined here as Cross-Catalytic Coprecipitating Systems (CCCSs) – is of great interest to material design. Provided that cross-catalytic effects are sufficient to overcome the precipitation thresholds for each phase, all CCCSs can be expected to self-organize into nanocomposite materials through a one-pot, one-step synthesis protocol. Symmetry-breaking events generating various complex, ordered textures are predicted in CCCSs involving crystalline phases. While high levels of stochasticity lead to a loss of ordering, coprecipitation is found to be robust to diffusion or advection in the solution. This model shows that a couple of chemical reactions can generate a range of complex textures – with possibly distinct physical/chemical properties. Cross-catalytic coprecipitating systems consequently represent a promising avenue for producing nanocomposites with complex textures at reduced economic and environmental costs.

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## Introduction

Every year, new types of nanocomposites are designed in various fields of technology.<sup>1–11</sup> Because of their enhanced capabilities, they can help to solve critical technological challenges, among which the production of electricity from light<sup>6</sup> or heat,<sup>3</sup> energy storage<sup>1,4,5</sup> and pollution treatment<sup>2,8</sup> are some prominent examples. However, a general issue is that the production of these materials is complicated, energy-consuming and costly. This represents a hindrance for scaling up production.

One approach generally adopted to produce nanomaterials with reduced economic and environmental costs, the bottom-up synthesis approach, relies on harnessing the self-organization capabilities of certain chemical systems.<sup>12–14</sup> Inorganic nanoparticles, for example, can spontaneously co-orient to form the so-called mesocrystals.<sup>15,16</sup> It was also found experimentally that reaction-diffusion processes occurring

during the synthesis of organic membranes or during crystal growth can generate Turing-like patterns at the nanoscale.<sup>17,18</sup> Yet, the self-organization of different phases into a nanocomposite appears more difficult than the self-organization of a single type of nanoparticle. It usually requires separate steps and specialized devices.<sup>3,7</sup> Apart from some recent notable exceptions, such as the preparation of binary mesocrystals<sup>19</sup> and ternary metallic heterojunctions,<sup>20</sup> for most nanocomposites, the synthesis of the constituent phases and their assembly into the desired material are separate. The one-pot, one-step self-organization of molecular reactants into the final material remains a critical challenge.

Incidentally, a chemical system studied for several decades can represent a formidable inspiration in this regard: silica-witherite biomorphs.<sup>21</sup> They are self-organized nanocomposites of crystalline witherite and amorphous silica that are well known for the diverse, life-like morphologies they display.<sup>22–24</sup> It has been demonstrated that the complex morphogenetic mechanisms underlying biomorph growth are primarily due to the interplay between the precipitation of both phases (Fig. 1-A).<sup>25–27</sup> Witherite precipitation under alkaline conditions locally decreases pH. This pH drop increases the saturation of silica and triggers its precipitation. Silica precipitation, in turn, leads to a local increase of pH and an increase of the saturation of witherite. Consequently, the precipitation of each phase, owing to pH changes, favors the precipitation of the other phase, leading to a complex cyclic coprecipitation (Fig. 1-A).

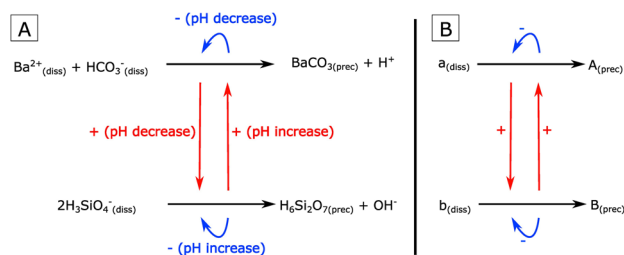
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**Fig. 1** (A) Schematic drawing of the cyclic coprecipitation underlying silica-witherite biomorph growth.<sup>25–27</sup> (B) Schematic drawing of the general principle of a cross-catalyzed coprecipitating system. One dissolved species ( $a_{(\text{diss})}$ ) precipitates to form a condensed phase ( $A_{(\text{prec})}$ ). A second dissolved species ( $b_{(\text{diss})}$ ) precipitates to form a distinct condensed phase ( $B_{(\text{prec})}$ ). Cross-catalysis between the two reactions is depicted by red arrows. Self-inhibition of each reaction is depicted by blue arrows. Modalities of enhancement and inhibition may vary depending on the actual system.

Silica-carbonate biomorphs thus demonstrate the possibility for two distinct inorganic phases to organize into a complex 3D nanocomposite *while they precipitate*, due to the interaction between both precipitation reactions. Research suggests that the control of environmental parameters such as pH or temperature grants a fine control on the precipitated textures.<sup>28,29</sup> Silica-witherite biomorphs could thus reveal highly useful for the design of new optical devices or microcarriers.<sup>30–32</sup>

In general, we define here this type of system as a Cross-Catalytic Coprecipitating System (abbreviated in the following as CCCS). CCCSs consist in two parallel precipitation reactions, forming two distinct condensed phases, that catalyze each other (Fig. 1-B). This definition is very general, since there are no constraints on the nature of the phases precipitated – they may be organic or inorganic, crystalline or amorphous – and no constraints on the modalities of cross-catalysis. CCCSs may consequently involve different types of chemical species and exist in various contexts.

In this study, we tested the general capabilities of CCCSs for material design using a numerical model. Among the different computational approaches that have been developed for modelling nucleation and growth processes (see *e.g.* the work of L. Gránásy and coworkers<sup>33,34</sup>), it was decided to use a simple, two-dimensional model inspired by cellular automata<sup>35,36</sup> that focuses on the core of the process of cross-catalyzed coprecipitation. An overview of the model is given in the Experimental section of this paper. The code is given in the ESI.†

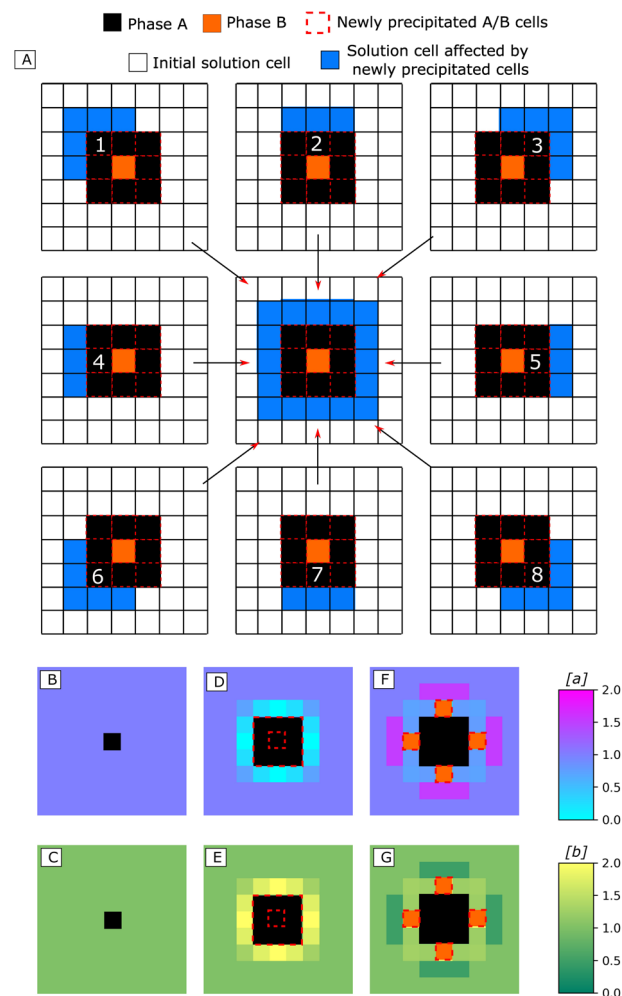
## Experimental

The principle of the model revolves around three major elements:

(1) Two parallel reactions of precipitation –  $a_{(\text{diss})} \rightarrow A_{(\text{prec})}$  and  $b_{(\text{diss})} \rightarrow B_{(\text{prec})}$  – exist. Precipitation is constrained in a square crystallographic lattice.  $a_{(\text{diss})}$ ,  $A_{(\text{prec})}$ ,  $b_{(\text{diss})}$  and  $B_{(\text{prec})}$  are respectively abbreviated to  $a$ ,  $b$ ,  $A$  and  $B$  in the following.

(2) The precipitation of phases A or B occurs when the concentration in  $a$  or  $b$  (resp. noted  $[a]$  and  $[b]$ ) reaches a certain

threshold  $T$ .<sup>37–40</sup> To model nucleation energy barriers, two thresholds were introduced for each phase, one for growth ( $T_{a,g}$  and  $T_{b,g}$ ) and one, higher, for nucleation ( $T_{a,n}$  and  $T_{b,n}$ ).



**Fig. 2** Illustration of the model. (A) Illustration of the effect of one round of precipitation on the surrounding solution cells. The effects of each newly precipitated cell of phase A (numbered from 1 to 8 and depicted in black with red dashed frames) are isolated visually here on the eight graphs at the periphery. The effect of precipitation on  $[a]$  and  $[b]$  is split between the solution cells surrounding the newly precipitated cell (represented in blue). The concentration  $[a]$  (resp.  $[b]$ ) in each of the blue cells is decreased (resp. increased) by  $O_a/5$  around precipitating cells no 1, 3, 6 and 8, and by  $O_a/3$  around precipitating cells no 2, 4, 5 and 7. The influences of each single precipitating cell are added in the center graph. They generate a gradient in the solution, located along the sides of the growing precipitate. The influence of precipitation on local chemistry consequently depends on the geometry of the preexisting precipitate. (B to G) Description of the initial phase of the growth for a given set of conditions. The simulation starts with a nucleus of phase A. In B, D, and F, the evolution of  $[a]$  in the solution cells is pictured. In C, E, and G,  $[b]$  in the solution cells is shown. In D and E, A precipitates all around the nucleus (black cells with the red dashed frame). Growth of phase A generates a gradient of  $[a]$  and  $[b]$  in the surrounding solution. Under these conditions, the threshold of  $[b]$  for B to nucleate ( $T_{b,n}$ ) is reached only in the middle of the faces (F and G). The subsequent precipitation of B (orange cells with the dashed red frame) further complexifies the geometry of  $[a]$  and  $[b]$  around the growing precipitate.

(3) The precipitation of one phase increases locally the saturation levels for the other phase and decreases locally the saturation levels for this phase – this is depicted in Fig. 2-A. The intensity of these cross-catalysis and self-inhibition effects is represented by parameters  $O_a$  and  $O_b$ . The precipitation of phase A releases a quantity  $O_a$  of b and consumes a quantity  $O_a$  of a in the solution cells surrounding the newly precipitated cell. The precipitation of phase B releases (respectively consumes) an amount  $O_b$  of a (respectively b) in the solution cells surrounding the newly precipitated cell.  $O_a$  and  $O_b$  values are correlated to the amplitude of concentration oscillations in the solution cells.

In this model, the focus is given to cross-catalysis, and it is assumed that no further interactions between the four chemical species  $a_{(diss)}$ ,  $A_{(prec)}$ ,  $b_{(diss)}$  and  $B_{(prec)}$  exist. It must be noted however that variable supplementary interactions between these species may exist in a real system (for example, both precipitated species may react together). Depending on their nature, such interactions could significantly alter precipitation and should be taken into account in relevant systems.

## Results and discussion

Starting from a single nucleus of phase A, simulations were run using various values for growth thresholds ( $T_{a,g}$  and  $T_{b,g}$ <sup>37–40</sup>) and for the amplitude of cross-catalysis effects ( $O_a$  and  $O_b$ ). The results show that depending on these parameters, cross-catalytic systems may display several behaviors drastically different from each other, referred to here as Regimes 0 to 5, and shown in Fig. 3-A. Maintained coprecipitation, the desired target for the one-pot/one-step synthesis of nanocomposites, corresponds to Regime 5. We also note that under certain conditions, due to the self-inhibition, single-phase porous precipitates can be obtained (Regime 4). While we do not discuss them further in this work, which is focused on nanocomposites, those porous precipitates can be of high interest to the engineering of molecular sieves.<sup>41–43</sup>

The results indicate that a system of two reactions, although it behaves in a cross-catalytic manner, may never produce nanocomposites if it does not fulfill supplementary conditions. The domain of the parameter space where Regime 5 was observed in the simulations can be seen in Fig. 3-B (yellow) for two different couples of values for growth thresholds  $T_{a,g}$  and  $T_{b,g}$ . In order to observe maintained coprecipitation, the chemical oscillations due to A and B precipitation ( $O_a$  and  $O_b$ ) must be sufficient so that both growth thresholds  $T_{a,g}$  and  $T_{b,g}$  are overcome – *i.e.*, cross-catalysis is effective for both reactions. Regime 5 is consequently observed only above minimal values of  $O_a$  and  $O_b$ ; these minimal values increase when  $T_{a,g}$  or  $T_{b,g}$  values are increased (Fig. 3-B).

One could intuitively predict that in Regime 5, coprecipitation would always result in both phases precipitating alternatively, layer by layer. Interestingly, due to the underlying lattice constraining precipitation, this is not the case. Indeed, the local concentration changes in the solution around the growing precipitate are smaller on the corners than on the sides (see Fig. 2-A for a graphical explanation of this effect). Due to this

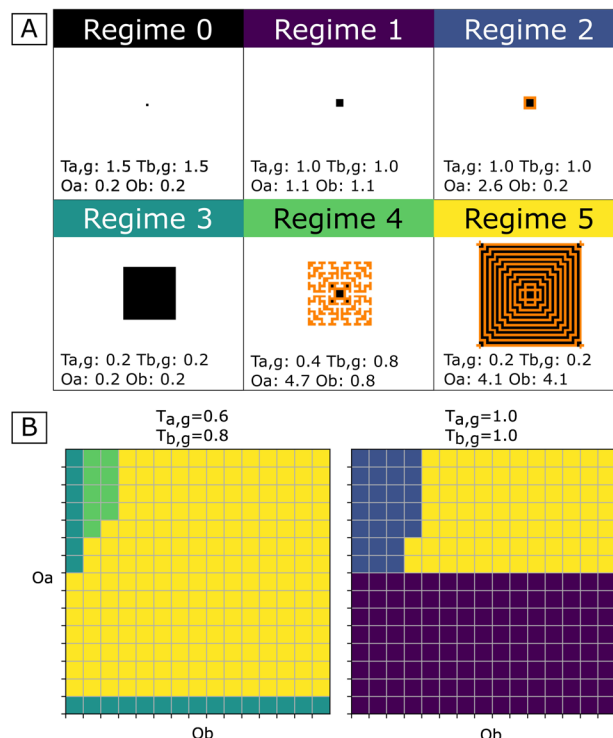
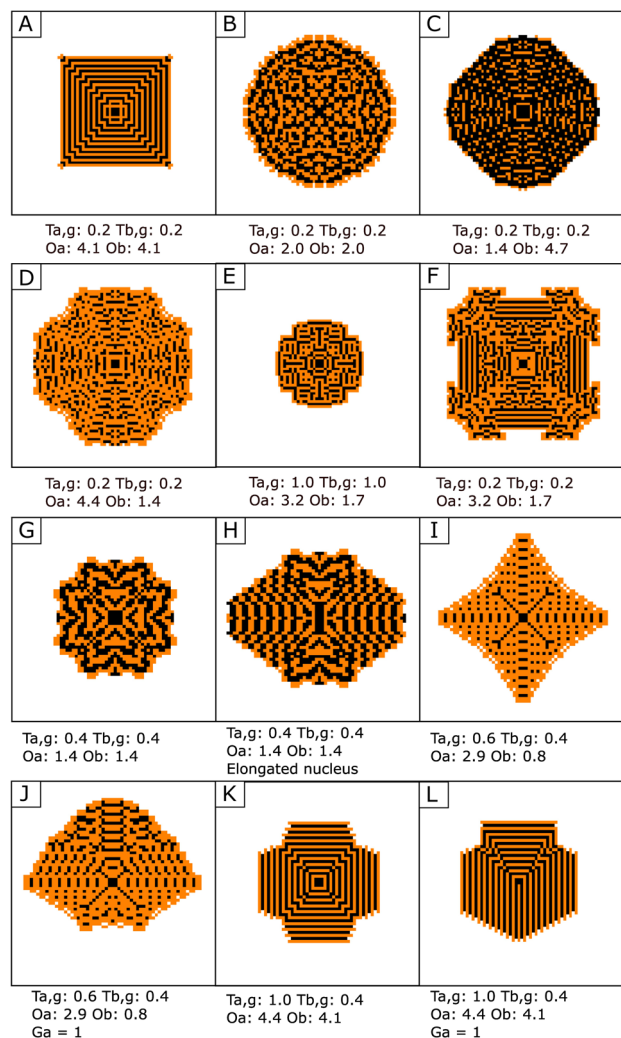


Fig. 3 (A) Main growth regimes of CCCSs. For each regime, one example precipitate is shown with its corresponding parameters (see the corresponding videos in the ESI†). Phase A depicted in black and phase B in orange. All simulations initiated with a single cell of phase A as the nucleus, initial [a] and [b] of 1, and nucleation thresholds  $T_{a,n} = T_{b,n} = 2$ . The simulations last ten timesteps, with different combinations of conditions of values for the growth thresholds  $T_{a,g}$  and  $T_{b,g}$  and intensities of cross-catalysis effects  $O_a$  and  $O_b$ . In Regime 0, growth does not occur (initial [a] and [b] are lower than  $T_{a,g}$  and  $T_{b,n}$  respectively). Regime 1: growth arrested after one timestep of A precipitation, due to complete self-inhibition. Regime 2: concomitant growth of both phases is arrested after a few timesteps. Regime 3: continuous growth of one phase. Regime 4: growth of porous single-phase precipitates due to partial self-inhibition. Regime 5: concomitant, continuous growth of both phases. (B) Illustration of the dependency of observed regimes on parameters  $T_{a,g}$ ,  $O_a$  and  $O_b$  for a single cell of phase A as the nucleus.  $O_a$  and  $O_b$  range from 0.2 to 4.7. The color chart corresponds to the color of regimes shown in panel A.

‘corner effect’, saturation levels may reach the precipitation thresholds only in some of the solution cells surrounding the precipitate (Fig. 2-D and E). If this occurs, it represents a symmetry-breaking event that increases the geometric complexity of the obtained precipitate and creates new gradients of concentration in the surrounding solution (Fig. 2-F and G). Those gradients can then reverberate into other symmetry-breaking events. This result suggests more generally that, provided at least one of the precipitated phases in a CCCS follows a crystallographic lattice, symmetry-breaking events can occur and nanocomposites with complex textures are formed.

In composite materials obtained using a CCCS, geometry is not controlled by crystal facet energy – as is the case in many classical crystalline systems<sup>44</sup> – but by spatial heterogeneities in concentrations in the solution surrounding the precipitate. The history of symmetry-breaking events, and therefore the texture





**Fig. 4** Examples of textures from Regime 5 obtained after ten time-steps, with nucleation thresholds of  $T_{a,n} = T_{b,n} = 2$ . See the corresponding videos in the ESI.† Phase A depicted in black and phase B in orange. Only a small subset of observed diversity is shown. The parameters used for obtaining each precipitate are written below. (A and B) Effect of a decrease of both  $O_a$  and  $O_b$ . (C and D) Effect of a change of the relative values of  $O_a$  and  $O_b$ . (E and F) Effect of an increase of both  $T_{a,g}$  and  $T_{b,g}$ . (G and H) Effect of a change of the nucleus symmetry – here, rectangle (H) instead of square (G). See also Fig. S3.† (I to L) Effect of a gradient of concentration in the solution. (I and K) No gradient. (J and L) The same conditions, but with a gradient of  $[a]$ , ranging from 0.5 to 1.5 from the bottom to the top of the simulation space. See also Fig. S4.†

and shape of the precipitate, is thus highly sensitive to the values of the precipitation thresholds and the amplitude of chemical oscillations. With this simple model, by varying these parameters, it was found that a very large variety of nanocomposite materials may be obtained in a CCCS. A glimpse of the diversity obtained after ten timesteps from a single cell nucleus of phase A and for different combinations of  $T_{a,g}$ ,  $T_{b,g}$ ,  $O_a$  and  $O_b$  is shown in Fig. 4A–F.

For constant values of  $T_{a,g}$  and  $T_{b,g}$ , high values for both  $O_a$  and  $O_b$  lead logically to more complete rounds of precipitation of A and B at each timestep, and the obtained textures are close

to a simple layer-by-layer precipitation (Fig. 4-A). Lower values for  $O_a$  and/or  $O_b$  are correlated to increased occurrences of symmetry-breaking events and an increased complexity in the obtained textures (Fig. 4-B). A higher chemical oscillation for one phase –  $\alpha$  – than for the other phase –  $\beta$  – favors a larger volume of phase  $\beta$  in the precipitate, since smaller volumes of  $\alpha$  precipitated are necessary to reach thresholds for  $\beta$  precipitation. Therefore, the ratio  $O_a/O_b$  is negatively correlated with the ratio of A volume precipitated to B volume precipitated – see Fig. 4-C and D and S1.† As can be expected, for constant values of chemical oscillation  $O_a$  and  $O_b$ , an increase in growth thresholds  $T_{a,g}$  and  $T_{b,g}$  overall slows down precipitation, and precipitates obtained after the same number of time steps are smaller – see Fig. 4-E and F and S2.†

Another factor controlling growth is the morphology and nature of the seed. While using a different seed appears to have a rather limited influence on simple textures (Fig. S3-B and C†), it can drastically alter the precipitation history of more complex textures (Fig. S3-D–F†). Noticeably, a change of the symmetry of the seed may be reverberated and modify the symmetry of the obtained precipitates (Fig. 4-G,H and S3-D†).

The spatial gradients of concentration also have an effect, by introducing an axis of polarity in the precipitates (Fig. 4-I–L and S4†). The spatial gradients of concentrations can lead consequently to a supplementary degree of morphologic and textural complexity in the obtained nanocomposite.

Studying self-assembly processes from the nano- to the micro-scale is a notorious technical challenge.<sup>45,46</sup> Experiments were not undertaken in this study, that instead focuses on finding general conditions for obtaining nanocomposites with complex textures. Regarding the silica-witherite biomorphs system described in Introduction of this article, the pH-mediated cross-catalysis mechanism has been demonstrated using pH-sensitive dyes,<sup>25,27</sup> but the internal texture of these nanocomposites has revealed difficult to characterize at the nanometer scale. Yet, the textures reported in this study of CCCSs can be compared to patterns observed in natural and experimental crystalline materials (Fig. 5). The growth of single crystals can lead to the formation of ordered compositional patterns. Let us mention the cases of oscillatory zoning correlated with cyclic compositional changes (Fig. 5-A),<sup>47–49</sup> or the zoning in experimentally grown “dyed” crystals, generally due to the incorporation of light-absorbing molecules in preferential growth sectors (Fig. 5-B–D).<sup>50–52</sup> Precipitation may also create ordered patterns at the scale of several crystals. Prominent examples are wave-like compositional patterns referred to generally as “Liesegang rings” (Fig. 5-E) or the orientational patterns formed during spherulitic growth (Fig. 5-F) – very common phenomena that occur in a number of natural and experimental settings.<sup>17,53–57</sup> Processes behind these patterns are disparate and arguably quite different from CCCSs. However, they confirm that ordered compositional patterns may frequently form during the growth of crystalline materials.

There are two important factors that may prevent coprecipitation and/or ordering in CCCSs and that need to be discussed. The first is molecular diffusion in the solution. Diffusion around growing precipitates leads in principle to





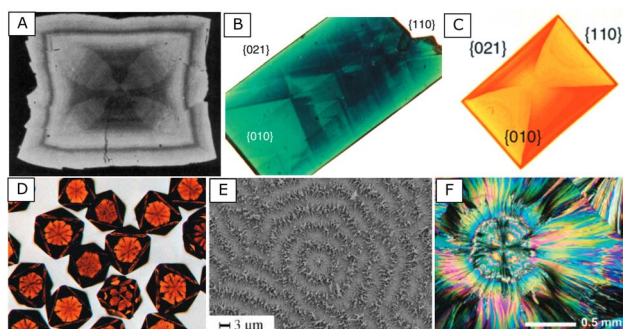


Fig. 5 Examples of compositional (A to E) or orientational (F) ordering that may occur during the growth of single (A to D) or multiple (E and F) crystals and reported in previous works. (A) (Br,Sr)SO<sub>4</sub> solid solution crystal (ref. 46). Darkness in the crystal is correlated to the relative proportions of Sr and Ba. (B) Phthalic acid crystal grown in the presence of methyl green dye (ref. 47). (C) Phthalic acid crystal grown in the presence of Nile red dye (ref. 49). (D) AgBr crystals grown in the presence of Maskasky dye (ref. 48). (E) Concentric rings formed by self-organization of BaCO<sub>3</sub> crystals during their growth (ref. 17). (F) Spherulitic growth and orientational pattern observed during the crystallization of hippuric acid at 80 °C (ref. 50).

a dilution of the cross-catalytic effect in the solution. To test the effect of diffusion, simulations were run where the diffusion of a and b molecules in the solution was modelled, following Fick's Law:

$$\vec{F}_i = D \nabla[i]$$

with  $\vec{F}_i$  the flux of molecules  $i$ ,  $\nabla[i]$  the gradient of concentration of molecule  $i$ , and  $D$  a diffusion constant. The results indicate that the coprecipitation behavior in the CCCS is robust to diffusion (Fig S5,† first three columns). It is only for very high  $D$  values ( $D = 0.3$ ) that coprecipitation was consistently lost (Fig. S5,† last column). The complexity of precipitated textures however tends to be reduced for  $D$  values of 0.1 and higher (Fig. S5,† third column). These findings are consistent with previous observations made on silica-witherite biomorphs. In this system, nanocomposites were obtained even when the solution was stirred mechanically up to 350 rpm (ref. 58) – note that, similarly to molecular diffusion, mechanical stirring creates a dilution of the cross-catalytic chemical effect in the vicinity of the growing biomorph.

The second factor that may prevent ordering in the CCCS is stochasticity. The model used here is purely deterministic, with “hard” thresholds determining whether precipitation occurs or not. However, some amount of randomness may exist in the CCCS. In the case of silica-witherite biomorphs, for example, silica precipitation is related to its polymerization in solution, which follows stochastic rules.<sup>59</sup> Random fluctuations in the space and time of the reactant's concentration may also exist,<sup>60</sup> and impurities can be randomly integrated during synthesis processes.<sup>61</sup> To account for those phenomena and test the effect on the obtained textures, a batch of simulations was run where the hard thresholds were replaced by soft thresholds – *i.e.*, the probability that precipitation occurs  $P$  depends on saturation  $s$ ,

following a sigmoidal law centered on the precipitation threshold  $T$ :

$$P = 1/(1 - L \cdot \exp(T - s))$$

with  $L$ , a curvature parameter, correlated to the steepness of the sigmoidal curve and inversely correlated to the amount of randomness (Fig. S6†).

The results show that for  $L$  values of  $10^5$ , the ordering obtained with a purely deterministic behavior is not altered (Fig. S7,† first column). When  $L$  is decreased to 100, the ordering is significantly altered (Fig. S7,† second column). Higher amounts of randomness, with an  $L$  value of 10, lead to complete obliteration of any ordering (Fig. S7,† third column).

In order to make use of the potential of the CCCS for nanocomposite synthesis in the future, a first step will be to look for couples of precipitation reactions that can interact in a cross-catalytic manner and involve at least the precipitation of one crystalline phase. The challenge is that this interaction may be straightforward – *e.g.* if the product of one reaction is the reactant of the other, or more indirect – as is the case for example in silica-witherite nanocomposites. It could be envisioned to look for such interactions using network analysis on large databases of chemical reactions.

Screening experiments should then be conducted on the systems previously found in order to search for CCCS behavior. In coprecipitation experiments, chelators could be used with various concentrations in order to modify effective precipitation thresholds  $T_{a,g}$  and  $T_{b,g}$ . Increased viscosity of the mother solution could also be tested (provided that the medium remains inert), since it could slow down diffusion and increase effective  $O_a/O_b$ . A rigorous confrontation of the model with experimental results would ideally require to (1) image ongoing precipitation at the nanometre scale and (2) analyze the evolution of local solution properties around the precipitates. However, this is technically very difficult.<sup>45,46</sup> While liquid cell TEM is a promising tool to image nanoscale precipitation mechanisms, it is still a relatively young technique that has not yet been applied in this context. The measurement of solution properties at the nanoscale remains a technical challenge.<sup>25,62</sup> Consequently, as of now, it may be easier to evaluate potential CCCSs through the characterization of final precipitates.

Promising precipitates will present a high anisotropy that could be evidenced using X-ray diffraction. The texture (as well as physical and chemical properties) of these precipitates should be carefully investigated using *e.g.* transmission electron microscopy. In order to verify that the system indeed is a CCCS, one should assess how changes in precipitation thresholds, the amplitude of cross-catalysis, and the nucleus shape affect the obtained precipitate, and compare it with the general observations made in Fig. 4.

Alternatively, first principles simulations, already used in the context of precipitation reactions,<sup>63</sup> could in the future lead to a fine prediction of the behavior of potential CCCSs. This could circumvent some experimental difficulties and give information about cross-catalysis parameters  $O_a$  and  $O_b$  – parameters otherwise difficult to assess experimentally.



As a supplementary note, the mechanical stability of materials obtained through coprecipitation can be a concern in some cases.<sup>64</sup> Although this particular problem was not considered here, the assessment of the material stability outside of the solvent should be conducted on experimentally obtained precipitates.

## Conclusions

Depending on the type of behavior wanted for a specific CCCS, this study shows that several requirements exist:

(1) In order to obtain a nanocomposite through maintained coprecipitation, the cross-catalysis effects ( $O_a$  and  $O_b$ ) must be sufficient to overcome successively the precipitation thresholds of A and B ( $T_a$ ,  $T_b$ ).

(2) In order to obtain ordered nanocomposites, besides the previous requirement, the degree of randomness must be moderate ( $L > 100$ ).

(3) In order to obtain nanocomposites displaying complex textures due to symmetry-breaking events, besides previous requirements, it is required that at least one of the phases A or B follows a crystallographic lattice (see Fig. 2).

Although this model is simple, it captures the most general and critical behaviors that may be expected in cross-catalytic coprecipitating systems and illustrates their important potential. These systems are able to produce various nanocomposites with a highly complex texture through a single-pot, single-step process. While precipitation was constrained in a square crystallographic lattice in this model, phases precipitated may be either crystalline or amorphous; they also could be organic or inorganic. Besides, if precipitation thresholds and the amplitude of chemical oscillations are adjustable, a single couple of chemical reactions can produce several types of materials, potentially displaying distinct physical/chemical properties. Such systems are therefore most promising for reducing the economic and environmental costs of nanocomposite production. We hope that this study will trigger new experimental studies looking for the patterns anticipated by our computational approach.

## Author contributions

J. R.: conceptualization, methodology, software, validation, writing – original draft, writing – review and editing, and visualization. B. M.: conceptualization and writing – review and editing. H. C.: conceptualization, writing – review and editing, and supervision. J. M. G. R.: conceptualization, writing – review and editing, supervision, and funding acquisition.

## Conflicts of interest

There are no conflicts to declare.

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