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First-principles examination of two-dimensional Janus quintuple-layer atomic structures $X\text{CrSiN}_2$ ($X = \text{S, Se, and Te}$)

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In this work, we propose novel two-dimensional Janus $X\text{CrSiN}_2$ ($X = \text{S, Se, and Te}$) single-layers and comprehensively investigate their crystal structure, electronic properties, and carrier mobility by using a first-principles method. These configurations are the combination of the CrSi_2N_4 material and a transition metal dichalcogenide. The $X\text{-Cr-SiN}_2$ single-layers are constructed by replacing the N-Si-N atomic layer on one side with chalcogen atoms (S, Se, or Te). The structural characteristics, mechanical or thermal stabilities, and electronic properties are investigated adequately. All three examined configurations are energetically stable and are all small-bandgap semiconductors (<1 eV). Since the mirror symmetry is broken in the Janus material, there exists a remarkable built-in electric field and intrinsic dipole moment. Therefore, the spin-orbit interaction is considered intensively. However, it is observed that the spin-orbit coupling has insignificant effects on the electronic properties of $X\text{CrSiN}_2$ ($X = \text{S, Se, and Te}$). Moreover, an external electric field and strain are applied to evaluate the adjustment of the electronic features of the three structures. The transport properties of the proposed configurations are calculated and analyzed systematically, indicating the highly directional isotropy. Our results suggest that the proposed Janus $X\text{CrSiN}_2$ could be potential candidates for various applications, especially in nanoscale electronic devices.

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1 Introduction

Two-dimensional (2D) materials have attracted interest in not only theoretical but also experimental studies due to their unique physicochemical characteristics. The distinct properties compared to the corresponding bulk phases make 2D materials become potential candidates for tremendous applications such as energy conversion, spintronics,^{1–4} piezoelectric materials,⁵ photocatalysts,⁶ or supercapacitors,⁷ etc. Currently, there are considerable types of 2D materials studied widely, including graphene,^{8,9} transition metal dichalcogenides,^{10–12} post-transition metal monochalcogenides,^{13–15} stanene,¹⁶ or germanene.¹⁷

Currently, Janus single-layers are notably interested as a promising candidate for new 2D nanostructures.^{18–21} Janus materials possess asymmetric structures due to the lacking of vertical symmetry, leading to many new electronic and

photocatalytic properties. Most of the synthesized or proposed Janus structures recently are based on binary or ternary TMDs. Since septuple-atomic-layer MoSi_2N_4 was successfully synthesized²² via chemical vapor deposition, these materials have been studied extensively. The MoSi_2N_4 single-layer exhibited indirect semiconducting behavior and excellent ambient stability. Recently, Gao and co-workers proposed different nanodevices based on the MoSi_2P_4 monolayer, including p-i-n junction field-effect transistors, p-n junction diodes, and photoelectric transistors.²³ In our previous work,²⁴ we proposed and theoretically investigated the five-atomic-layer Janus SMoSiN_2 single-layers that could be obtained from MoSi_2N_4 through the substitutions of S atoms for N-Si-N atoms on one side. The Janus SMoSiN_2 single-layer exhibits a direct-bandgap semiconducting characteristic. Interestingly, our obtained result indicates that the introduction of S atoms to replace the N-Si-N atoms on one side of the MoSi_2N_4 single-layer results in an enhancement of the energy bandgap value and causes the indirect-direct bandgap transition in the considered semiconductor. Then, brand-new heterostructures of the MoSi_2N_2 single-layer were proposed as potential configurations in various applications. Following that research subjects, in the current work, our group proposes the asymmetric atomic structures $X\text{CrSiN}_2$ ($X = \text{S, Se, Te}$) that are constructed from CrSi_2N_4 by substituting N-Si-N atoms by chalcogen atoms (S,

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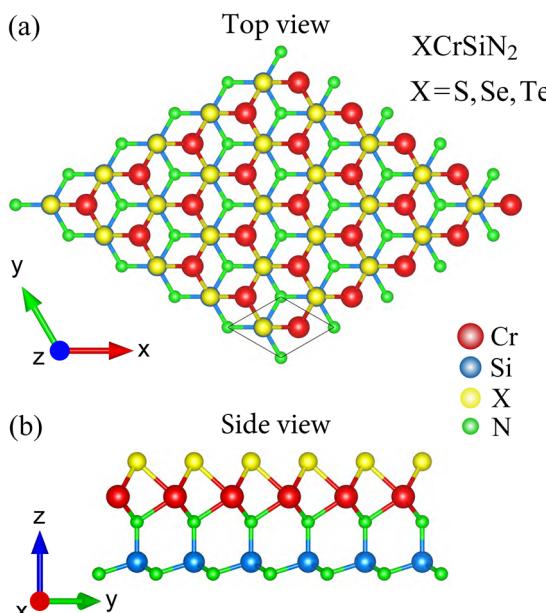


Fig. 1 Top (a) and side (b) views of the crystal structure of XCrSiN_2 ($\text{X} = \text{S, Se, Te}$) single-layers.

Se, and Te). They can be regarded as a 2D Janus material with mirror symmetry breaking resulting in several extraordinary properties.

In this work, we first optimize the crystal structures of three proposed Janus single-layers XCrSiN_2 ($\text{X} = \text{S, Se, Te}$) and verify their mechanical and thermal stabilities by performing the first-principles calculations of phonon dispersion and *ab initio* molecular dynamics (AIMD) calculations. Importantly, the electronic properties are investigated and strictly analyzed through the band structures and weighted band structures of all three configurations. Additionally, we investigate how the electronic states of XCrSiN_2 single-layers are affected by extrinsic factors, such as mechanical strain and external field. Since the mirror symmetry is broken, resulting in a significant difference in electronegativity of the $\text{N}-\text{Si}-\text{N}$ atomic layer and chalcogen atoms, it is expected that the carrier mobilities, hence the generation/combination of electron–hole pairs, are influenced. Therefore, besides structural and electronic properties, in this work, we also discover electronic transport characteristics.

2 Computational method

The simulations in the present work were carried out by using the density functional method (DFT) as implemented by the

Quantum Espresso code.²⁵ We used the generalized gradient approximation (GGA) of Perdew–Burke–Ernzerhof (PBE)²⁶ to consider the exchange–correlation functionals. The first Brillouin zone was sampled by $(15 \times 15 \times 1)$ k -point grid using the Monkhorst–Pack model.²⁷ The cutoff energy for plane waves was set at 50 Ry. The convergence threshold for energy and forces was adopted to be 10^{-6} eV and 10^{-3} eV \AA^{-1} , respectively. Besides, we also used the semiempirical DFT-D3 approach²⁸ to treat the weak van der Waals forces in the examined layered materials. The vertical vacuum distance of 20 \AA was inserted to reduce interactions that may exist between periodic images. The AIMD simulations with the NVT ensemble²⁹ were performed within 8 ps (time step of 1 fs) to test the thermodynamic stability. We used a $6 \times 6 \times 1$ supercell for the AIMD simulations. The deformation potential theory by Bardeen and Shockley was used to evaluate the carrier mobility in the studied single-layers.³⁰

3 Calculated results and discussion

3.1 Crystal lattice

The crystal structures of XCrSiN_2 ($\text{X} = \text{S, Se, Te}$) single-layers belong to the space group $P3m1$ (point group C_{3v}). The optimized crystal structures of the XCrSiN_2 ($\text{X} = \text{S, Se, Te}$) configurations are presented in Fig. 1, where the stacking order of atomic layers is $\text{X}-\text{Cr}-\text{N}-\text{Si}-\text{N}$. The largest lattice constant is found for TeCrSiN_2 of 2.99 \AA , followed by those of TeCrSiN_2 (2.91 \AA) and SCRsiN_2 (2.87 \AA). The cation–cation bond lengths and the thicknesses of the single-layers are also evaluated and listed in Table 1. Similarly, those values are found to decrease in the order of TeCrSiN_2 , SeCrSiN_2 , and SCRsiN_2 single-layers. The discrepancies in the obtained lattice constants, bond lengths, and thicknesses are attributed to the dissimilarity of the ionic radii of Se, Te, and S ions. The obtained lattice constant of XCrSiN_2 is higher than that of CrSi_2N_4 (2.84 \AA).³¹

By calculating and then analyzing the cohesive energy E_{coh} , the chemical bond strength is examined to confirm the structural stability of these suggested Janus structures. The cohesive energy can be calculated from the following expression

$$E_{\text{c}} = \frac{E_{\text{tot}} - (N_{\text{Cr}}E_{\text{Cr}} + N_{\text{Si}}E_{\text{Si}} + N_{\text{N}}E_{\text{N}} + N_{\text{X}}E_{\text{X}})}{N_{\text{Cr}} + N_{\text{Si}} + N_{\text{N}} + N_{\text{X}}}, \quad (1)$$

where E_{Cr} , E_{Si} , E_{N} , E_{X} are the single-atom energies of Cr, Si, N, and X, respectively; E_{tot} is the total energy of the XCrSiN_2 single-layer; and N_{Cr} , N_{Si} , N_{N} , and N_{X} are the atom number of Cr, Si, N, and X in the unit cell, respectively. The negative value indicates that the structure is stable. Hence, all of the three proposed Janus XCrSiN_2 ($\text{X} = \text{S, Se, Te}$) single-layers are energetically stable with the cohesive energies of -7.93 , -7.71 , and -7.38 eV

Table 1 Lattice constant a (\AA), chemical bond length d (\AA), thickness h (\AA), cohesive energy E_{c} (eV per atom), elastic constants C_{ij} (N m^{-1}), Young's modulus Y_{2D} (N m^{-1}), and Poisson's ratio ν . N(b) and N(m) refer to the N atom located at the bottom and in the middle of the single layer

	a	$d_{\text{Cr-X}}$	$d_{\text{Cr-N}}$	$d_{\text{Si-N(b)}}$	$d_{\text{Si-N(m)}}$	h	E_{c}	C_{11}	C_{12}	C_{66}	Y_{2D}	ν
SCRsiN_2	2.87	2.26	1.99	1.74	1.74	4.90	-7.93	326.66	90.62	118.02	301.52	0.277
SeCrSiN_2	2.91	2.39	2.00	1.76	1.74	5.02	-7.71	316.75	85.19	115.78	293.84	0.269
TeCrSiN_2	2.99	2.59	2.01	1.79	1.75	5.18	-7.38	307.02	84.56	111.23	283.73	0.275



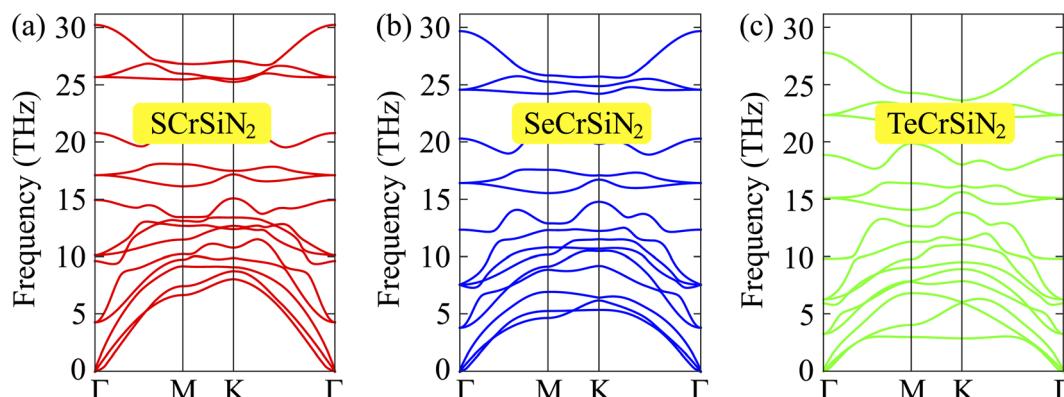


Fig. 2 Phonon dispersions of (a) SCrSiN_2 , (b) SeCrSiN_2 , and (c) TeCrSiN_2 single-layers.

per atom for SCrSiN_2 , SeCrSiN_2 , and TeCrSiN_2 , respectively. The most stable structure is found for SCrSiN_2 that can be expected from the above calculated optimized structure.

Moreover, accurate phonon calculations along the high symmetry line Γ -M-K- Γ are performed to investigate the dynamic stability of the three XCrSiN_2 configurations. It is observed from Fig. 2 that there are fifteen vibrational branches (three acoustic and twelve optical modes) since there are five atoms in the primitive cell. In case the negative frequencies are available, there are no restoring forces against the atom displacement. The absence of the soft phonon modes of XCrSiN_2 indicates the dynamic stability of these structures. No gap can be observed between the acoustic and optical branches demonstrating a quite high scattering process rate, *i.e.* the lattice thermal conductivity is relatively low. Besides, we also investigated the thermal stability of XCrSiN_2 ($\text{X} = \text{S, Se, Te}$) structures by means of AIMD simulations at 300 K as presented in Fig. 3. It can be seen that the total potential energies in all three structures fluctuated insignificantly, about 0.3 eV, and were almost unchanged during the whole simulation. Hence, the vibration of constituent atoms is slight and only around the equilibrium positions, so that the chemical bonds remain robust.

Next, the mechanical stability of Janus structures is investigated by calculating and analyzing the elastic constants in accordance with mechanical stability conditions suggested by Born and Huang.³² In general, for 2D materials, it is necessary to test four independent elastic constants, namely C_{11} , C_{22} , C_{12} , and C_{66} (in Voigt notation). As shown in Fig. 1a, the considered material has a hexagonal structure resulting in $C_{11} = C_{22}$. Consequently, the three following elastic constants are calculated, C_{11} , C_{12} and C_{66} , in which C_{66} is related to C_{11} and C_{12} by the equation $C_{66} = (C_{11} - C_{12})/2$. The obtained results C_{ij} are tabulated in Table 1. It is found that all the elastic constants C_{ij} decrease as the chalcogen element's atomic size increases. In more detail, C_{11} is ranging from 326.66 to 307.02 N m⁻¹, C_{12} is ranging from 90.62 to 84.56 N m⁻¹ and C_{66} is ranging from 118.02 to 111.23 N m⁻¹ in the order of S, Se, and Te chalcogens. The elastic constants of current Janus structures XCrSiN_2 meet Born–Huang's criteria for the hexagonal lattice as $C_{11} > 0$, $C_{11} >$

C_{12} , and $C_{66} > 0$,³³ indicating their structures to be mechanically stable.

The mechanical features are also characterized by Young's modulus and Poisson's ratio, which can be calculated from C_{ij} .

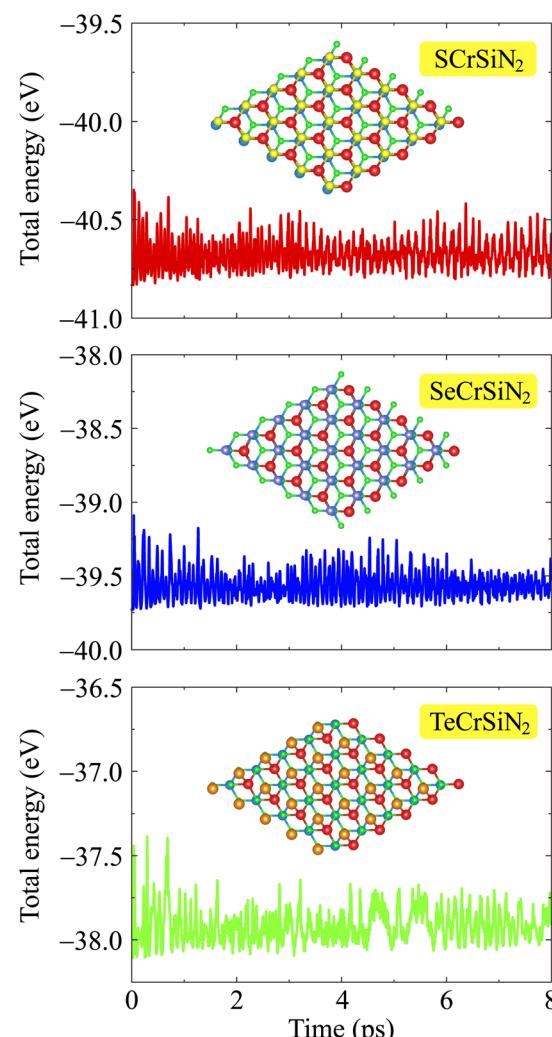


Fig. 3 AIMD calculations for the variations of the total energies to time of XCrSiN_2 single-layers at 300 K. Insets are the crystal structures of the corresponding single layers at the end of the AIMD test.



The direction-dependent 2D Young's modulus (in-plane stiffness) $Y_{2D}(\theta)$ and Poisson's ratio $\nu(\theta)$ can be defined as^{34,35}

$$Y_{2D}(\theta) = \frac{C_{11}C_{22} - C_{12}^2}{C_{11}\sin^4\theta + C_{22}\cos^4\theta - (2C_{12} - A)\sin^2\varphi\cos^2\theta}, \quad (2)$$

$$\nu(\theta) = \frac{C_{12}(\sin^4\theta + \cos^4\theta) - (C_{11} + C_{22} - A)\sin^2\theta\cos^2\theta}{C_{11}\sin^4\theta + C_{22}\cos^4\theta - (2C_{12} - A)\sin^2\theta\cos^2\theta}, \quad (3)$$

where $A = (C_{11}C_{22} - C_{12}^2)/C_{66}$ and θ is the angle relative to the armchair direction. In Fig. 4, we show the polar diagrams of $Y_{2D}(\theta)$ and $\nu(\theta)$ of XCrSiN_2 . The angle-dependent $Y_{2D}(\theta)$ and $\nu(\theta)$ profiles in all three structures display perfect circles. Hence, the Janus XCrSiN_2 single-layers possess isotropic elastic properties. The values of Young's modulus and Poisson's ratio are listed in Table 1. Young's modulus has a similar trend to the elastic constants C_{ij} , *i.e.*, it decreases with increasing atomic radius X . This means that, under the in-plane external force, SCrSiN_2 is the easiest one to be deformed, followed by SeCrSiN_2 and TeCrSiN_2 single-layers. In comparison to the Cr-Se and Cr-S bonds, the Cr-Te bonds are the longest and most deformable, and these findings are in good agreement with the study discussed above. On the other hand, Poisson's ratio $\nu(\theta)$ appears differently: the highest value of $\nu(\theta)$ is found for the SCrSiN_2 single-layer, followed by that of the TeCrSiN_2 single-layer, then that of the SeCrSiN_2 single-layer. However, the discrepancy in Poisson's ratio is insignificant. Moreover, the Poisson's ratio values are calculated to be positive indicating the trend of

contraction (expansion) in the perpendicular direction when there is a tensile (compressive) strain in a certain direction. The Poisson's ratio values are small (ranging from 0.269 to 0.277), indicating all of these single layers are brittle ($\nu < 0.31$).³⁶

3.2 Electronic properties

Along with verifying the structural and dynamic stability, the electronic properties are taken into account by evaluating the band structures. In this work, both PBE and PBE + SOC functionals are utilized in order to examine precisely the energy gaps and other electronic properties of the XCrSiN_2 ($\text{X} = \text{S}, \text{Se}, \text{Te}$) single-layers. The obtained band structures are presented in

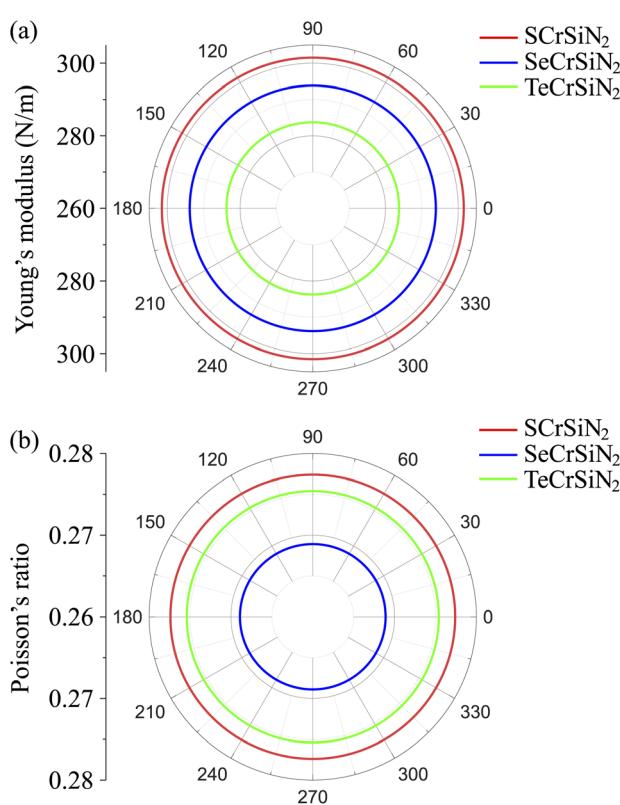


Fig. 4 Polar diagrams for (a) Young's modulus and (b) Poisson's ratio of XCrSiN_2 .

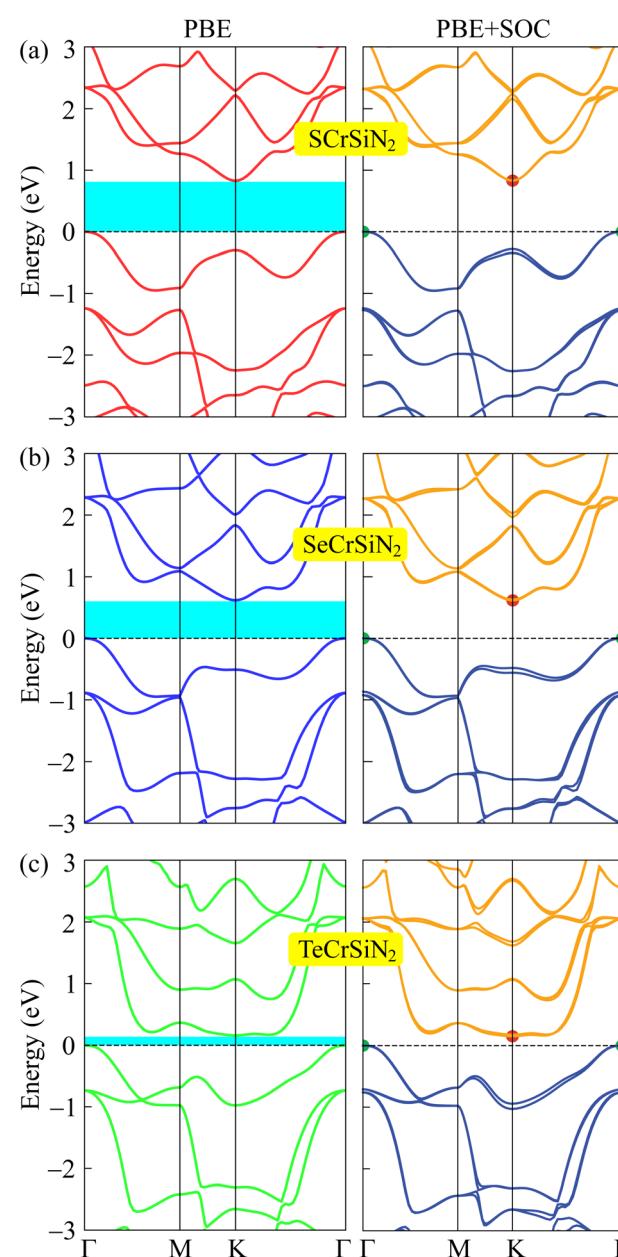


Fig. 5 Calculated band structures of (a) SCrSiN_2 , (b) SeCrSiN_2 , and (c) TeCrSiN_2 single-layers by using the PBE and PBE + SOC methods. The Fermi level is set at 0 eV.



Table 2 The PBE and PBE + SOC bandgaps E_g , vacuum level difference $\Delta\Phi$, work functions Φ on X and N surfaces of $X\text{CrSiN}_2$ single-layers. All parameters are in the units of eV

	E_g^{PBE}	$E_g^{\text{PBE+SOC}}$	$\Delta\Phi$	Φ_N	Φ_X
SCrSiN_2	0.83	0.83	0.26	5.52	5.26
SeCrSiN_2	0.62	0.61	1.07	5.38	4.31
TeCrSiN_2	0.16	0.15	1.91	5.09	3.18

Fig. 5 and the energy bandgaps are reported in Table 2. It is calculated that the PBE bandgaps of SCrSiN_2 , SeCrSiN_2 , and TeCrSiN_2 monolayers are 0.83, 0.62, and 0.16 eV, respectively. The indirect bandgap of XCrSiN_2 is comparable with that of CrSi_2N_4 (0.49 eV). It is obvious that the band structures have the same profiles and the bandgaps calculated using PBE and PBE + SOC functionals are similar. This suggests that for these current

structures, the SOC effect could be neglected to reduce computational cost without any significant difference.

From Fig. 5, we can observe that XCrSiN_2 single-layers exhibit small-bandgap semiconductor characteristics with the bandgaps decreasing as the atomic size of chalcogen X increases (S, Se, and Te). All three configurations are indirect semiconductors because the CBM and VBM are located at K and Γ points, respectively. Besides, the PBE-weighted bands of XCrSiN_2 are illustrated in Fig. 6 in order to investigate the contribution of each orbital to the electronic energy bands. It can be observed that the weighted band structures of the three configurations are quite similar. The main contribution to the CBM in XCrSiN_2 single-layers is the hybridization of the d-orbital of Cr with the p-orbital of S in SCrSiN_2 , and with the d-orbital of Se and Te in SeCrSiN_2 and TeCrSiN_2 , respectively. However, the VBM of XCrSiN_2 is contributed by the hybridization of the d-orbital of Cr with the p-orbital of N mainly, and

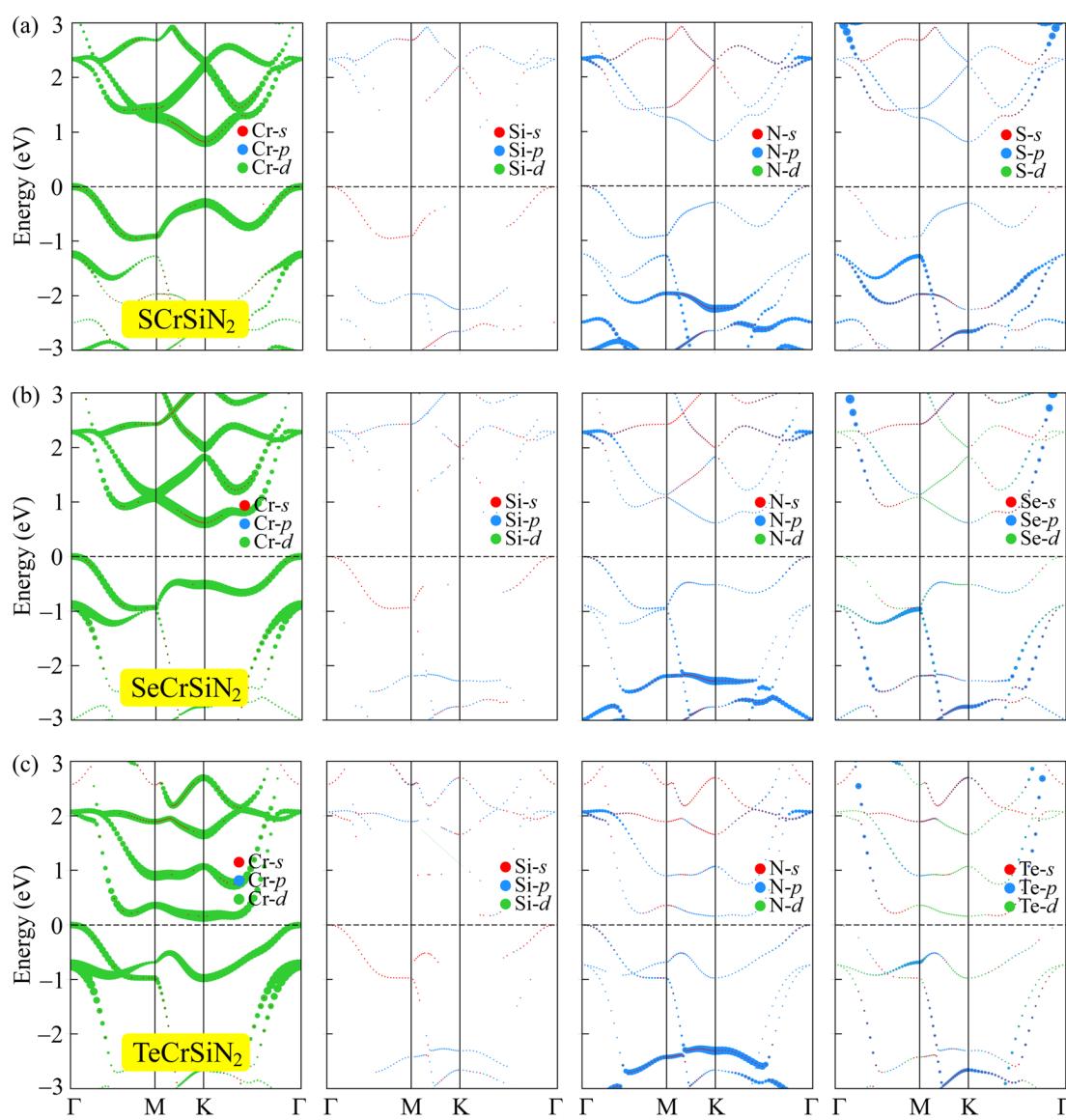
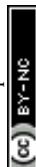


Fig. 6 The PBE weighted bands of (a) SCrSiN_2 , (b) SeCrSiN_2 , and (c) TeCrSiN_2 single-layers.



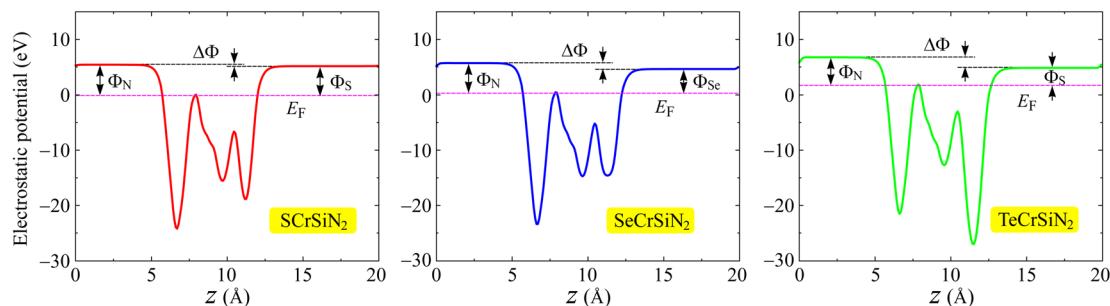


Fig. 7 Electrostatic potentials with the dipole corrections of $X\text{CrSiN}_2$ single-layers. The horizontal dashed line indicates the Fermi level.

partly with the p-orbital/d-orbital of the X atom. The Janus $X\text{CrSiN}_2$ structures may inhibit the undesirable recombination of photoexcited electron–hole pairs due to their small energy bandgap and different atomic contributions in the CBM and VBM.

Furthermore, we calculate the work function Φ , another important feature of electrons. By calculating the electrostatic potential of the vacuum (Φ_{vac}) and of the Fermi level (Φ_{F}), the work function Φ can be defined as $\Phi = \Phi_{\text{vac}} - \Phi_{\text{F}}$. From Table 2, the Φ_{N} and Φ_{X} of the three structures are not much different,

implying that electrons have a comparable ability to escape from surfaces of the $X\text{CrSiN}_2$ single-layers. Because Janus structures lack vertical mirror symmetry, inherent electric dipoles are introduced, which leads to a discrepancy in the vacuum level on the two surfaces along the z -direction, which can be characterized by $\Delta\Phi$. Fig. 5 presents the planar electrostatic potentials of the $X\text{CrSiN}_2$ single-layers where the dipole correction is included.³⁷ The highest vacuum level difference between two different surfaces ($\Delta\Phi$) is found for SCrSiN_2 (0.26 eV), followed by that of TeCrSiN_2 (1.91 eV). The smallest work

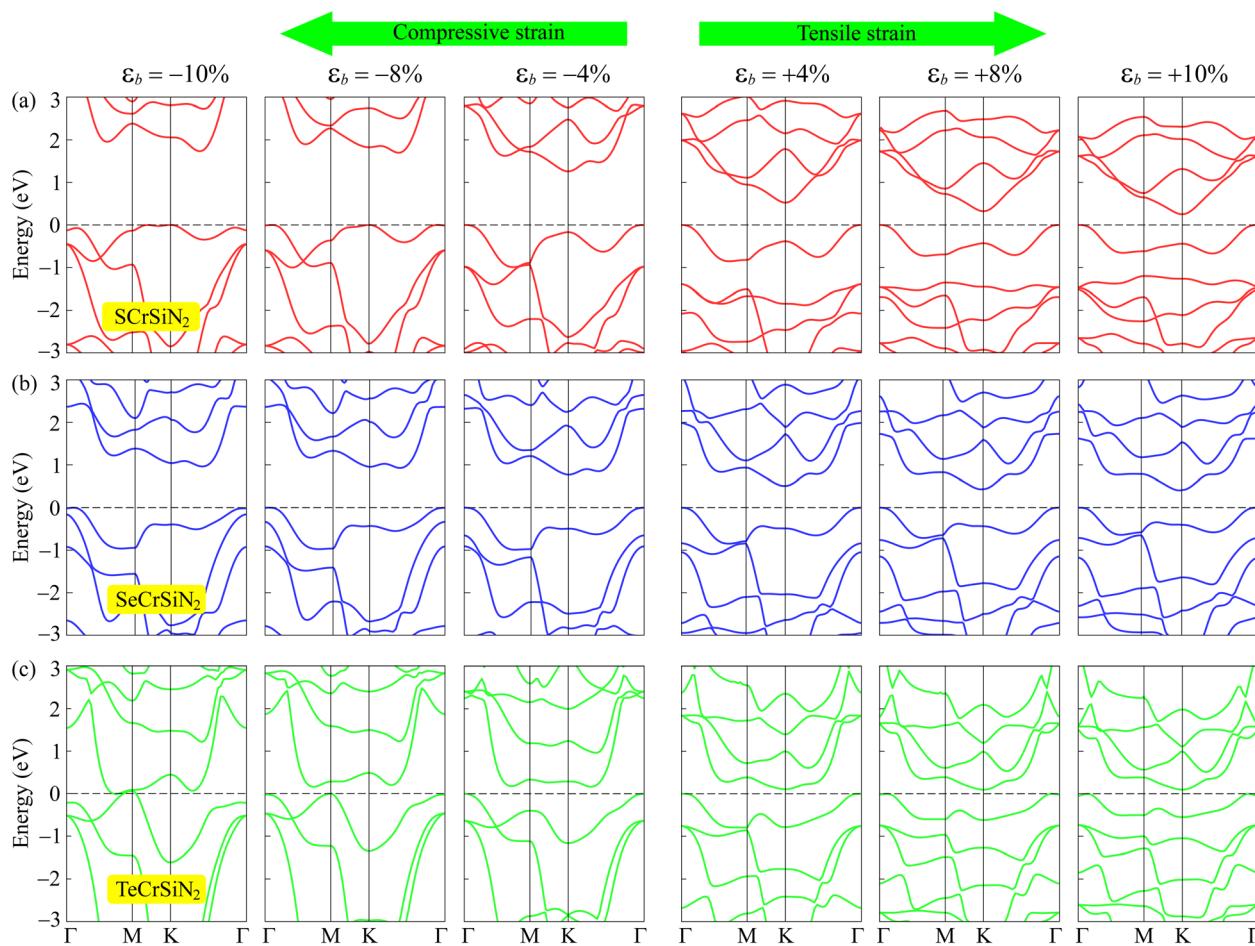


Fig. 8 Band structures of (a) SCrSiN_2 , (b) SeCrSiN_2 , and (c) TeCrSiN_2 under the biaxial strains ε_b .



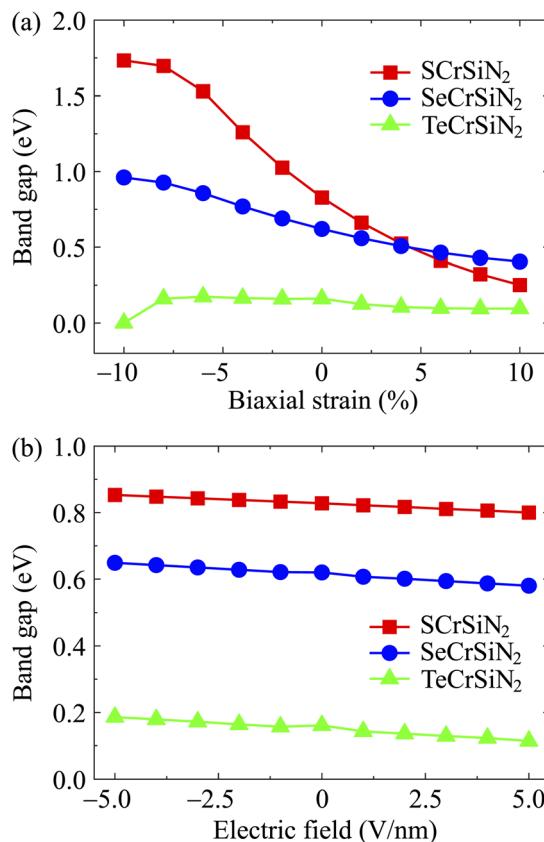


Fig. 9 Bandgaps of XCrSiN₂ as functions of the biaxial strain (a) and external electric field (b).

function is found for SeCrSiN₂ (1.07 eV), demonstrating that the electrons can escape more easily from the surface of SeCrSiN₂ than other structures. These obtained work functions are explained by the slight electronegativity difference between the N and X constituents on the two surfaces (Fig. 7).

It is important to examine the diverse structures under various settings because, as has been reported, the physical properties, particularly the electrical characteristics, of 2D materials are easily modulated by external conditions. Among several approaches, such as doping, heterostructures, *etc.*, strain engineering is one of the simplest but most powerful ways to modulate the electronic structures of 2D nanomaterials. The biaxial strain is defined as $\epsilon_b = (a - a_0)/a_0$, where a and a_0 are the length of the distorted and undistorted computed cells,

respectively. In the current study, we apply a strain of from 0 to $\pm 10\%$, in which compressive strain is represented by the negative sign and tensile strain by the positive sign. Previous studies^{38–42} indicated that the strain could result in a phase transition in 2D structures. In order to evaluate the modification of the electronic states of XCrSiN₂, we applied the volumetric expansion to the unit cell of the current three structures and the tuning of electronic properties by strain ϵ_b is considered. From Fig. 8, it can be observed that the band structures of all three single-layers are altered as the biaxial strains were changed, where the notable change is found to be near the Fermi levels. Fig. 9a depicts the dependence of energy bandgap on the biaxial strain. When the compressive strain increases, the energy bandgaps of both S_{Cr}SiN₂ and SeCrSiN₂ increase, up to about 1.7 and 1.0 eV, respectively. However, for TeCrSiN₂, the energy bandgap is almost unchanged when the compressive strain is lower than 10%; and as $\epsilon_b = -10\%$, the energy bandgap is nearly zero, *i.e.*, there is a transition from a small-bandgap to zero-bandgap semiconductor in TeCrSiN₂. When there is tensile strain, the energy bandgap of S_{Cr}SiN₂ is rapidly decreased (about 0.2 eV as $\epsilon_b = 10\%$); that of SeCrSiN₂ is reduced as well (about 0.5 eV as $\epsilon_b = 10\%$), and that of TeCrSiN₂ is insignificantly changed.

For further investigating the alternative electronic structures under different conditions, besides volumetric strain, an external electric field is next employed to control the electronic structure of examined single-layers. In our modeling, an external electric field is set perpendicular to the 2D plane of materials. The electric field intensity is from -5 V nm^{-1} to $+5 \text{ V nm}^{-1}$. The positive (negative) electric fields indicate that the direction is along (opposite to) the positive z-axis. The obtained calculations for energy bandgaps are plotted in Fig. 9b. It can be seen that bandgaps of all three single layers are hardly changed when the electric field is introduced. These results are derived from the band structure calculations (not shown here) in which there is a weak dependence of the band structure on the electric field.

3.3 Carrier mobility

The carrier mobilities and transport characteristics of XCrSiN₂ are explored in the final section to examine the migration and separation mechanisms. The suitability of a material for use in electrical devices is mostly determined by the mobility of carriers, especially electrons. It is well-known that there are many efficient ways to calculate carrier mobility, such as

Table 3 Effective mass of carrier m^* (m_0), 2D elastic modulus C_{2D} (N m^{-1}), DP constant E_d (eV), and carrier mobility μ ($\text{cm}^2 \text{ V}^{-1} \text{ s}^{-1}$) along the examined directions x and y of XCrSiN₂. m_0 is the free electron mass

		m_x^* (m_0)	m_y^* (m_0)	C_{2D}^x (N m^{-1})	C_{2D}^y (N m^{-1})	E_d^x (eV)	E_d^y (eV)	μ_x ($\text{cm}^2 \text{ V}^{-1} \text{ s}^{-1}$)	μ_y ($\text{cm}^2 \text{ V}^{-1} \text{ s}^{-1}$)
Electron	S _{Cr} SiN ₂	1.08	1.16	420.84	420.99	-10.49	-10.49	67.01	62.80
	SeCrSiN ₂	1.53	1.59	403.19	403.54	-10.04	-10.04	35.62	34.44
	TeCrSiN ₂	5.36	4.78	385.82	386.14	-9.79	-9.79	3.15	3.53
Hole	S _{Cr} SiN ₂	2.98	2.86	420.84	420.99	-5.94	-5.96	29.16	30.36
	SeCrSiN ₂	3.21	3.03	403.19	403.54	-6.77	-6.77	18.74	19.83
	TeCrSiN ₂	3.14	2.92	385.82	386.14	-8.66	-8.66	11.49	12.41

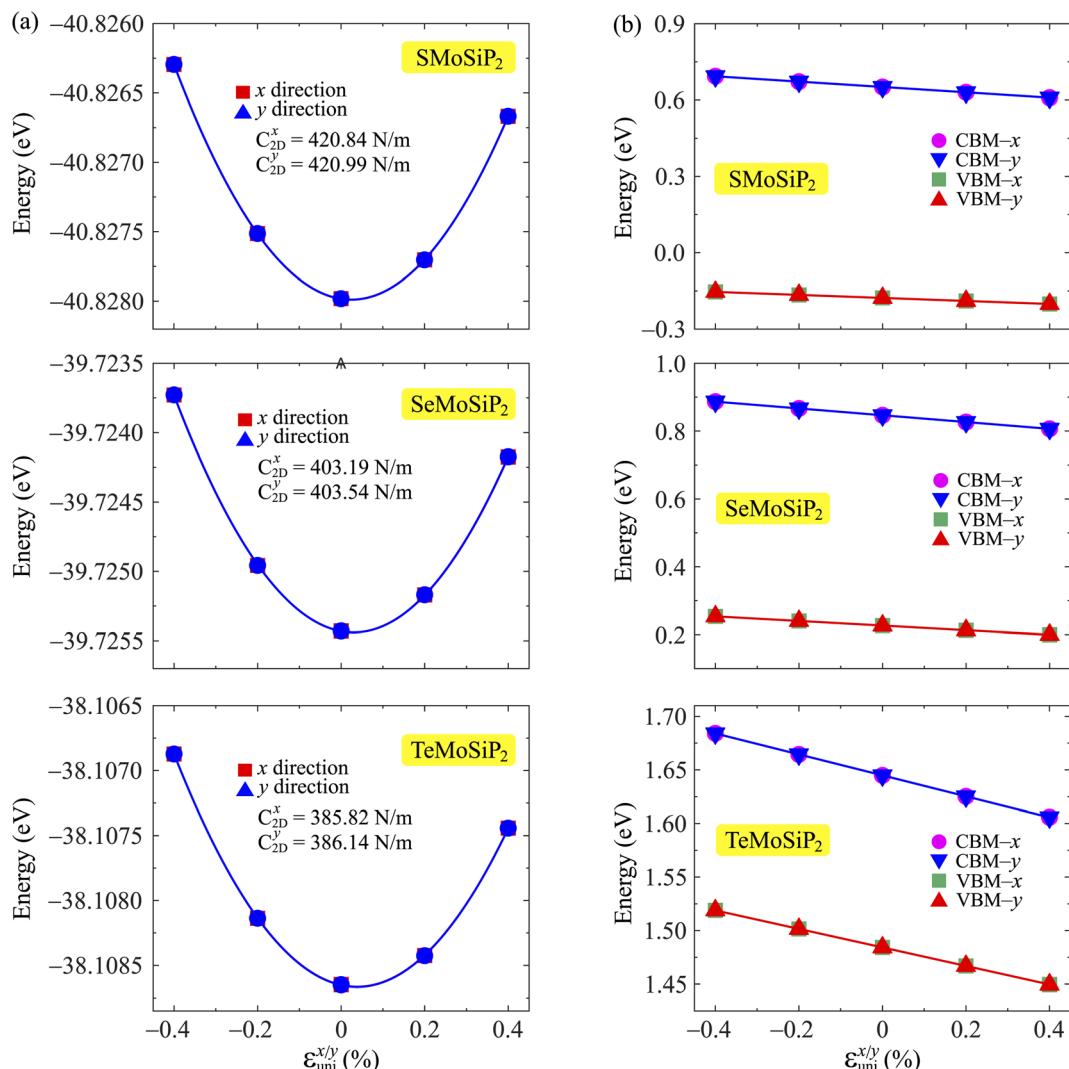


Fig. 10 The uniaxial strain-dependence $\epsilon_{\text{uni}}^{x/y}$ of the total energies (a) and energies at the band edges (b) of XCrSiN₂ single-layers. Fitted data are shown by the solid line.

deformation potential approximation³⁰ and Boltzmann transport theory.⁴³ It should be emphasized that electron-phonon coupling (EPC) is significant in influencing the physical characteristics of materials, particularly thermoelectric properties and thermal conductivity.^{44,45} In the present work, we only use the deformation potential (DP) approximation to evaluate the mobility of carriers. In the DP theory, the carrier mobility for 2D materials μ_{2D} is given by:⁴⁶

$$\mu_{2D} = \frac{e\hbar^3 C_{2D}}{k_B T m^* \bar{m} E_d^2}, \quad (4)$$

where C_{2D} denotes the elastic modulus, E_d is the DP constant, k_B stands for the Boltzmann constant, e refers to the elementary charge, and \hbar refers to the reduced Planck constant. m^* is the effective mass and $\bar{m} = \sqrt{m_x^* m_y^*}$ refers to the average effective mass. The DP constant E_d and elastic modulus C_{2D} are obtained by calculating the band edges and total energy, respectively, with respect to the uniaxial strain. The m^* of the carriers is

calculated based on the dispersion of the CBM and VBM. The more dispersive area, the smaller the effective mass. In this study, the temperature T is set to be 300 K. All of the calculated values of effective mass, elastic modulus, DP constant, and mobility of carriers along the x and y directions are tabulated in Table 3.

The small uniaxial strain ϵ_{uni} (from -0.4 to $+0.4\%$) is used to estimate the changing of total energy and the band edge positions. Fig. 10 illustrates the dependence of the total energies and the energies at the band edges on uniaxial strain ϵ_{uni} . From Fig. 10a, the total energies are found to alter insignificantly when the small uniaxial strain ϵ_{uni} is applied in the x - or y -direction and has similar values in both directions. As for the elastic modulus, the highest value C_{2D} is found for SMoSiN₂, followed by that of SeMoSiN₂, then of TeMoSiN₂. It can be seen that for each structure, the elastic modulus C_{2D}^x and C_{2D}^y are nearly equal; in other words, the elastic modulus is essentially independent of the directions of uniaxial strains. However, it

can be observed from Fig. 10b that the band edge positions of XMoSIN_2 are almost the same along the directions of uniaxial strains. The deformation potential constants E_d listed in Table 3 indicate that for both electron and hole carriers, E_d is quite isotropic with the two in-plane transport directions. Consequently, the carrier mobilities are expected to be directional isotropy with the x and y transport directions.

Concerning directional isotropy, electron and hole mobilities for the x direction and y direction are similar. The electron mobilities in SCrSiN_2 and SeCrSiN_2 are much higher [67.01 (62.08) and 35.62 (34.44) $\text{cm}^2 \text{V}^{-1} \text{s}^{-1}$ along the x –(y) direction] than that in TeCrSiN_2 [3.15 (3.53) $\text{cm}^2 \text{V}^{-1} \text{s}^{-1}$ along the x –(y) direction]. As for hole mobilities, in both directions, higher values are found for the holes in the VBM of SCrSiN_2 and SeCrSiN_2 , followed by that of TeCrSiN_2 . These obtained mobilities demonstrate that the electrons and holes in SCrSiN_2 are all fast carriers with the highest migration abilities among the carriers in the three materials. Moreover, it is worth noting that in SCrSiN_2 and SeCrSiN_2 structures, the mobilities of electrons are greater than those of holes. However, in SeCrSiN_2 structures, it can be seen that the hole mobilities are higher compared to electron mobilities. This is mainly due to the differences of structural and chemical structures, specifically, the differences of dispersion profiles in the CBM and VBM in XCrSiN_2 single-layers as shown in Fig. 5 and 6; hence, the effective mass of electrons and holes is affected.

4 Conclusive remarks

In the current work, we explored the stabilities of the crystal structure, electronic properties, and transport features of the new quintuple XCrSiN_2 single-layers. The results show that the proposed Janus single-layers are energetically and thermally stable that reveal the potential to fabricate experimentally. All three structures exhibit semiconducting behavior with small indirect bandgaps. When biaxial strain is applied, the electronic structures of the Janus XCrSiN_2 single-layers are modulated significantly, especially, at $\varepsilon_b = -10\%$, and those of SCrSiN_2 single-layers are transmitted from the semiconductor to metal. Meanwhile, it is found that these proposed structures show weak dependence of their electronic bands on the electric field. The mobilities of electrons and holes are calculated indicating the highly directional isotropy due to the similarity in the effective masses. The mobility of electrons is higher than that of holes in SCrSiN_2 and SeCrSiN_2 . The calculated results for mobility are found to be opposite for the TeCrSiN_2 case. Our proposed Janus quintuple XCrSiN_2 single-layers are promising 2D materials in the future with various applications.

Conflicts of interest

There are no conflicts of interest to declare.

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