





Cite this: *Dalton Trans.*, 2023, **52**, 18391

# A Raman spectroscopic and *ab initio* investigation of aqueous boron speciation under alkaline hydrothermal conditions: evidence for the structure and thermodynamic stability of the diborate ion†

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Raman spectra of aqueous sodium borate solutions, with and without excess NaOH, NaCl, and LiCl, have been obtained from perpendicular and parallel polarization measurements acquired using a custom-built sapphire flow cell over the temperature range 25 to 300 °C at 20 MPa. The solvent-corrected reduced isotropic spectra include a large well-defined band at 865 cm<sup>-1</sup> which overlaps with the boric acid B(OH)<sub>3</sub> band at 879 cm<sup>-1</sup>, and becomes increasingly intense at elevated temperatures. This band does not correspond to the spectrum of any other previously reported aqueous polyborate ions, all of which have symmetric stretching bands at frequencies below that of borate, [B(OH)<sub>4</sub>]<sup>-</sup>, at 745 cm<sup>-1</sup>. Based on the classic high-temperature potentiometric titration study by R. E. Mesmer, C. F. Baes and F. H. Sweeton, Acidity measurements at elevated temperatures. VI. Boric acid equilibria, *Inorg. Chem.*, 1972, **11**, 537–543, the new band was postulated to arise from a diborate ion, [B<sub>2</sub>(OH)<sub>7</sub>]<sup>-</sup> or [B<sub>2</sub>O(OH)<sub>5</sub>]<sup>-</sup>. *Ab initio* density functional theory (DFT), together with chemical modelling studies, suggest that it is most likely [B<sub>2</sub>(OH)<sub>7</sub>]<sup>-</sup>. Thermodynamic formation quotients derived from the peak areas showed variations with ionic strength as well as charge-balance discrepancies, which suggest one or more unidentified minor equilibrium species may also be present. The most likely candidate is the divalent diborate species [B<sub>2</sub>O<sub>2</sub>(OH)<sub>4</sub>]<sup>2-</sup> which is also predicted to have a band near 865 cm<sup>-1</sup> and is postulated to be present as a sodium ion pair. These are the first quantitative Raman spectra ever reported for borate-rich solutions under such conditions and provide the first spectroscopic evidence of a diborate species at PWR reactor coolant temperatures.

Received 3rd August 2023,  
Accepted 20th October 2023

DOI: 10.1039/d3dt02514d

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## 1. Introduction

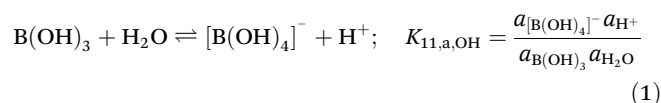
An understanding of boric acid chemistry is essential to the nuclear industry, as boron containing compounds are added to the primary coolant in order to control the neutron flux in high-temperature pressurized water reactors (PWRs). Aqueous boric acid solutions can be highly complex; at least 10 different polyborate species are known to exist in solution depending on the specific conditions. Various spectroscopic techniques such as UV-visible spectroscopy,<sup>1</sup> infrared spectroscopy,<sup>2</sup> Raman spectroscopy,<sup>3–10</sup> X-ray diffraction,<sup>5,11</sup> dielec-

tric relaxation spectroscopy<sup>12</sup> and NMR<sup>13</sup> have previously been used to study aqueous boron species in order to identify different species and deduce their structures. The two principal challenges in studying boron species are the diversity of polyborate species that can co-exist at equilibrium under a wide range of conditions, and the experimental challenges associated with the quantification of these species under hydrothermal conditions.

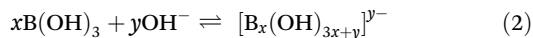
The classical high-temperature potentiometric titration study of polyborate formation constants by Mesmer *et al.*<sup>14</sup> showed that, at temperatures up to 200 °C, the principal reactions are the ionization of boric acid,

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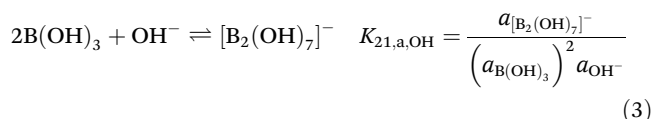
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and the formation of the triborate, tetraborate and/or pentaborate ions by ionization/condensation reactions such as:<sup>15</sup>

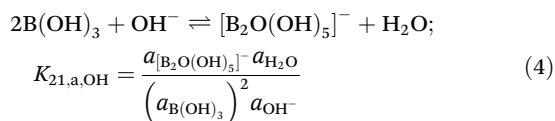


as well as more complicated stoichiometries. Subsequent studies by Raman spectroscopy and other methods noted above, confirmed the stoichiometries to be  $[\text{B}_3\text{O}_3(\text{OH})_4]^-$ ,  $[\text{B}_4\text{O}_5(\text{OH})_4]^{2-}$ , and  $[\text{B}_5\text{O}_6(\text{OH})_4]^-$ , respectively.<sup>6,9</sup>

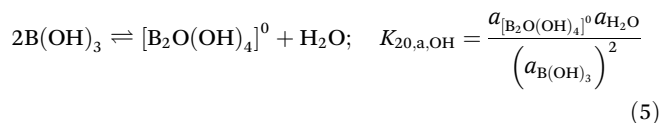
Although no spectra for diborate or metaborate species have been previously reported in aqueous solutions under ambient conditions, these species may be important under the high-temperature, high-pressure conditions encountered in nuclear reactor coolant. The potentiometric titration experiments reported by Mesmer and others<sup>14–16</sup> are able to determine the boron stoichiometry and charge, but not the degree of hydration or structure, of the aqueous species in their speciation models. The diborate species inferred from potentiometric measurements, which is postulated to be either  $[\text{B}_2(\text{OH})_7]^-$  or  $[\text{B}_2\text{O}(\text{OH})_5]^-$ , forms through the reactions:



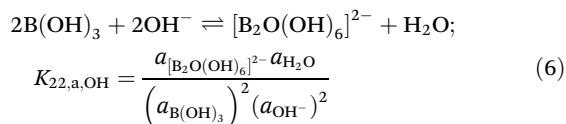
or



Although neutral and divalent diborates may form through condensation reactions, such as:



and



there is no evidence for them in the potentiometric studies reported to date.

The present study reports the reduced isotropic Raman spectra for sodium borate solutions under alkaline conditions at temperatures up to 300 °C at 20 MPa, using a newly designed titanium-alloy flow cell with sapphire windows.<sup>8</sup> The characteristic vibrational frequencies and relative scattering coefficients reported by Applegarth *et al.*<sup>9</sup> were used to calculate the equilibrium concentrations of the polyborate species from the reduced isotropic Raman spectra. The assignment of bands to the diborate species, and the relative intensities of the major peaks in the spectrum of each species, was based on density functional theory (DFT) calculations using Gaussian 03 software at several levels of theory with, and without, the polar-

izable continuum model solvation shell. These experimental results are not consistent with speciation calculations from the two different chemical equilibrium models of interest to the nuclear industry under these conditions, the OLI Analyzer Studio 9.2.1 software<sup>17</sup> and the EPRI MULTEQ software (ChemWorks 4.0, MULTEQ database v. 7.0).<sup>18,19</sup> The speciation results from the Raman measurements were used to calculate new values for the thermodynamic formation quotients of the diborate ion. These are the first quantitative Raman spectra ever reported for borate-rich solutions under hydrothermal conditions and provide the first spectroscopic evidence of a diborate species at PWR reactor coolant temperatures.

## 2. Experimental

### 2.1. Chemical and solution preparation

Boric acid,  $\text{B}(\text{OH})_3$ , (Alfa Aesar, 99.9995%), NaCl (Sigma, 99.5%), LiCl (Sigma-Aldrich, 99+%), and potassium hydrogen phthalate (KHP) (Fisher Scientific, 99.95%), were dried in an oven to constant mass before use. Sodium perchlorate (Alfa Aesar, ACS anhydrous grade, 98–102%) was used without further treatment. Carbonate-free stock solutions of 0.998 mol  $\text{kg}^{-1}$  and 1.023 mol  $\text{kg}^{-1}$  NaOH were prepared by mass from 50% w/w aqueous solution (Alfa Aesar) and standardized by triplicate titrations against KHP.

All borate solutions were prepared by adding a calculated mass of  $\text{B}(\text{OH})_3$  to a 0.998 mol  $\text{kg}^{-1}$  or 1.023 mol  $\text{kg}^{-1}$  NaOH solution to obtain the desired  $\text{B}(\text{OH})_3$  molality in the final solution. Sodium perchlorate (0.1 mol  $\text{kg}^{-1}$ ) was added to all solutions as an internal reference standard. All solutions were prepared by mass to an estimated standard uncertainty of  $\pm 0.5\%$ , using 18.2 M $\Omega$  cm ultrapure water from a Millipore Direct-Q 5 water purification system, and stored in sealed Nalgene bottles until used. For the solutions requiring higher NaOH molalities (buffer ratios  $>1$ ), additional 50% w/w NaOH, whose composition had been quantified during the preparation of the 0.998 mol  $\text{kg}^{-1}$  and 1.023 mol  $\text{kg}^{-1}$  NaOH solutions, was added by mass. These were estimated to have a larger standard uncertainty,  $\pm 2\%$ .

The stoichiometric buffer ratios of these solutions,

$$R_{\text{Buffer}} = m_{\text{NaOH}}^{\text{ST}} / m_{\text{B}(\text{OH})_3}^{\text{ST}} = (m_{\text{NaTotal}} - m_{\text{ClO}_4^-}) / m_{\text{BTotal}} \quad (7)$$

refer to the stoichiometric molality ratio of NaOH to  $\text{B}(\text{OH})_3$  used to make the solutions,  $m_{\text{NaOH}}^{\text{ST}}$  and  $m_{\text{B}(\text{OH})_3}^{\text{ST}}$ . Thus, ( $R_{\text{Buffer}} = 0$ ,  $m_{\text{B}} = 0.80$  mol  $\text{kg}^{-1}$ ) refers to a pure  $\text{B}(\text{OH})_3$  solution with  $m_{\text{B}(\text{OH})_3}^{\text{ST}} = 0.80$  mol  $\text{kg}^{-1}$  and  $m_{\text{NaOH}}^{\text{ST}} = 0.00$  mol  $\text{kg}^{-1}$ , and ( $R_{\text{Buffer}} = 1.0$ ,  $m_{\text{B}} = 1.0$  mol  $\text{kg}^{-1}$ ) refers to an aqueous solution of sodium borate with  $m_{\text{B}(\text{OH})_3}^{\text{ST}} = 1.00$  mol  $\text{kg}^{-1}$  and  $m_{\text{NaOH}}^{\text{ST}} = 1.00$  mol  $\text{kg}^{-1}$ .

In order to determine the effects of ion-pair formation and ionic strength, solutions of  $\text{NaB}(\text{OH})_4$  ( $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 0.320$  mol  $\text{kg}^{-1}$ ) and  $\text{LiB}(\text{OH})_4$  ( $R_{\text{Buffer}} = 1.000$ ,  $m_{\text{B}} = 0.310$  mol  $\text{kg}^{-1}$ ) were prepared using the procedures described above, to which an approximately equimolar excess of NaCl or LiCl was added by mass.



## 2.2. Raman spectroscopy and titanium sapphire flow cell

The reduced isotropic spectra of the borate solutions described above were measured from 25 to 300 °C at 20 MPa using a novel custom-made sapphire flow cell described previously in detail by Sasidharanpillai *et al.*<sup>8</sup> The whole assembly was fitted into a Teflon cell holder in a fixed position on the translation stage of the Raman microscope. Experiments were carried out in constant flow mode at a flow rate of 0.5 ml min<sup>-1</sup>, with temperature controlled to within ±1 °C over the several hours required to make each set of measurements. Constant pressure in the line was maintained using a syringe pump (Teledyne ISCO Inc.) filled with ultrapure water and a backpressure regulator (TESCOM 26-1722-24) located at the end of the flow line. The solutions to be studied were pumped through the cell using a 24 mL sample injection loop on a Rheodyne injector.

Raman spectra were obtained from polarized back-scattering measurements at constant temperature using a custom-made Horiba Jobin Yvon HR800 LabRAM system constructed with a fiber-optic coupled OLYMPUS confocal microprobe, using a 532 nm laser exciting line and a super-long-working-distance achromatic 20× objective lens (SLMPlan, OLYMPUS). Spectra were collected with polarizers set parallel and perpendicular to the polarization of exciting beam such that a baseline-corrected reduced isotropic spectra could be obtained, following the experimental protocol from Sasidharanpillai *et al.*<sup>8</sup>

The solvent-subtracted baseline-corrected spectra for quantitative equilibrium constants were obtained by recording the spectra of the water blanks and solutions, using both polarizations as a series on the same day, with the flow cell in a fixed position under the confocal microscope at constant temperature and pressure. Each Raman spectrum for the parallel (||) and perpendicular (⊥) polarizations was the average of eight runs in order to reduce the background noise. A perchlorate standard solution was injected at the beginning and end of the day's runs, and these spectra varied by <5% during the course of the day, indicating the laser power remained constant during the full set of runs. The temperature thermostating over the course of each day was constant to ±2 °C or better.

Isotropic Raman spectra,  $I_{\text{iso}}(\bar{\nu})$ , were obtained from the parallel (||) and perpendicular (⊥) polarized spectra using previously described methods.<sup>8,9,20</sup> The isotropic water spectrum was subtracted to obtain each solvent-corrected isotropic spectrum  $I_{\text{iso}}(\bar{\nu})$ .<sup>8,9,20</sup> The reduced isotropic spectra,  $R_{\text{iso}}(\bar{\nu})$  was obtained by correcting for the frequency dependence and the Boltzmann distribution.<sup>8,20</sup> An example of the experimental Raman spectra for both solution and water at parallel and perpendicular polarizations, the isotropic spectra of the solution and solvent, and the resulting solvent-corrected isotropic spectrum is shown in ESI (Fig. S1†).

## 2.3. *Ab initio* and DFT calculations

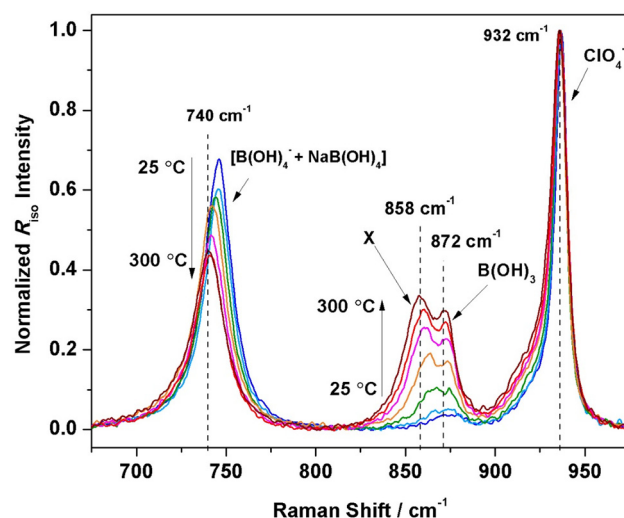
Calculations were performed using Gaussian 03 software, with MP2 calculations carried out using the frozen core approximation. The geometries were optimized using a stepping stone

approach, in which the geometries at the levels HF/6-31G\*, HF/6-31+G\*, HF/6-311+G\*, B3LYP/6-31G\*, B3LYP/6-31+G\*, B3LYP/6-311+G\*, MP2/6-31G\*, MP2/6-31+G\*, and MP2/6-311+G\* were sequentially optimized, and the geometry and molecular orbital reused as an initial guess for the subsequent level. Default optimization specifications were generally used. After each optimization, a frequency calculation was performed at the same level and the resulting Hessian was used in the subsequent optimization. Symmetry-constrained Z-matrix coordinates were used to speed up the optimizations. If imaginary frequencies were found, then the symmetry was lowered along the appropriate irreducible representation and the process was repeated. The Hessian was evaluated at the first geometry (Opt = CalcFC) for the first level in a series in order to aid geometry convergence. Full details of the computational methods are reported elsewhere.<sup>21</sup> The Raman intensities and depolarization ratios were calculated by default for Hartree-Fock calculations; for B3LYP and MP2 calculations, these were done by specifying Freq = Raman. For selected structures, the process was repeated with the conductor-like polarizable-continuum solvation model (SCRF = CPCM). Calculations for the divalent diborate species and the triborate species were done with Gaussian 16.

## 3. Raman spectroscopic results

### 3.1. Reduced isotropic Raman spectra

Fig. 1 displays a plot of the reduced isotropic Raman spectra of an aqueous solution prepared with equal ratios of NaOH and boric acid (Solution 1,  $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 1.019$  mol kg<sup>-1</sup>) for temperatures from 25 °C to 300 °C at 20 MPa. At 25 °C, there are two peaks at 745 cm<sup>-1</sup> and 936 cm<sup>-1</sup>, which correspond to



**Fig. 1** Reduced isotropic Raman spectra,  $R_{\text{iso}}(\bar{\nu})$ , of  $\text{NaB}(\text{OH})_4$  (aq.) at temperatures from 25 to 300 °C and 20 MPa for Solution 1, Run 1 ( $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 1.019$  mol kg<sup>-1</sup>, with 0.0902 mol kg<sup>-1</sup> sodium perchlorate). The spectra are normalized with respect to the perchlorate internal standard peak. The frequencies shown are peak positions at 300 °C.



$[\text{B}(\text{OH})_4]^-$  and the  $[\text{ClO}_4]^-$  internal standard, respectively. At temperatures above 75 °C, two overlapping peaks appear, with maxima at  $\sim 865$  and  $\sim 875$   $\text{cm}^{-1}$ , whose intensities increase as the temperature is increased. The band at  $\sim 875$   $\text{cm}^{-1}$  is clearly the  $\text{B}(\text{OH})_3$  symmetric stretch, however, the lower frequency shoulder at  $\sim 865$   $\text{cm}^{-1}$  does not correspond to any previously reported aqueous borate or polyborate species. The  $\text{B}(\text{OH})_3$  peak and the unknown peak (marked as “Species X”) were not well resolved at lower temperatures, but became better resolved above 150 °C. At higher temperatures, the borate peak intensity decreased, while the intensities of the  $\text{B}(\text{OH})_3$  band and the unknown peak both increased. All peaks shifted to lower energies with increasing temperature.

To confirm that the new species is an equilibrium species at high temperature, reduced isotropic Raman spectra for a solution of ( $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 1.019$  mol  $\text{kg}^{-1}$ , with 0.0902 mol  $\text{kg}^{-1}$  sodium perchlorate) were recorded at 22 °C, then again after heating to 200 °C, and a final time after cooling it back to 22 °C (ESI, Fig. S2†). Both spectra at 22 °C were identical and showed the presence of only the borate and perchlorate peaks, while the spectrum at 200 °C clearly indicated three peaks (borate, unknown species X, and boric acid). This showed that the new species at 865  $\text{cm}^{-1}$  was formed only at high temperatures, and that the reaction is reversible.

The Raman spectra for Solution 1 ( $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 1.019$  mol  $\text{kg}^{-1}$ , and perchlorate standard) were run in dupli-

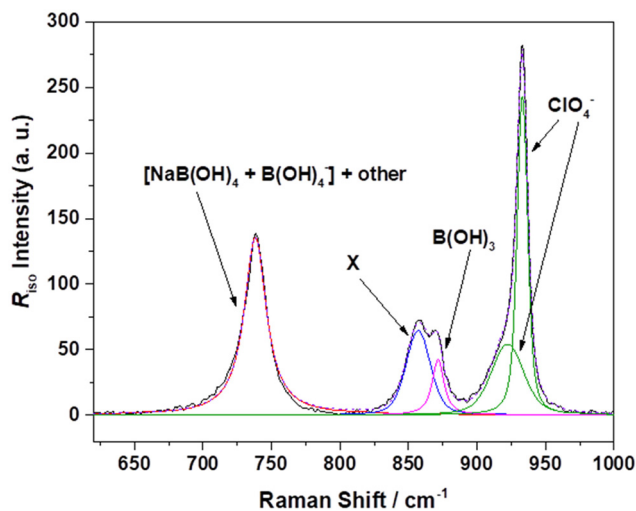
**Table 1** Relative peak areas<sup>a</sup> for the boron and polyborate species with respect to the perchlorate internal standard, calculated from the reduced isotropic Raman spectra of  $\text{NaB}(\text{OH})_4$  at 20 MPa, with and without excess NaOH from 25 to 300 °C

<i>t</i> /°C	745 $\text{cm}^{-1}$ band		865 $\text{cm}^{-1}$ band		875 $\text{cm}^{-1}$ band	
	$\nu/\text{cm}^{-1}$	Area	$\nu/\text{cm}^{-1}$	Area	$\nu/\text{cm}^{-1}$	Area
Solution 1 (Run 1), $R_{\text{Buffer}} = 0.980$ , $m_{\text{B}} = 1.0188$ mol $\text{kg}^{-1}$ , $m_{\text{NaClO}_4} = 0.0902$ mol $\text{kg}^{-1}$						
150	745	$1.126 \pm 0.066$	866	$0.128 \pm 0.009$	875	$0.046 \pm 0.003$
200	742	$1.084 \pm 0.082$	863	$0.225 \pm 0.018$	873	$0.108 \pm 0.009$
250	741	$0.895 \pm 0.034$	862	$0.361 \pm 0.015$	872	$0.170 \pm 0.010$
275	740	$0.787 \pm 0.041$	861	$0.450 \pm 0.024$	872	$0.181 \pm 0.010$
300	740	$0.894 \pm 0.028$	858	$0.469 \pm 0.016$	872	$0.211 \pm 0.007$
Solution 1 (Run 2), $R_{\text{Buffer}} = 0.980$ , $m_{\text{B}} = 1.0188$ mol $\text{kg}^{-1}$ , $m_{\text{NaClO}_4} = 0.0902$ mol $\text{kg}^{-1}$						
150	742	$1.147 \pm 0.073$	866	$0.146 \pm 0.010$	874	$0.054 \pm 0.005$
200	741	$1.038 \pm 0.075$	863	$0.252 \pm 0.020$	873	$0.082 \pm 0.008$
250	740	$0.894 \pm 0.090$	859	$0.382 \pm 0.039$	872	$0.158 \pm 0.016$
Solution 2, $R_{\text{Buffer}} = 0.984$ , $m_{\text{B}} = 1.0391$ mol $\text{kg}^{-1}$ , $m_{\text{NaClO}_4} = 0.0955$ mol $\text{kg}^{-1}$						
150	741	$1.112 \pm 0.037$	866	$0.132 \pm 0.009$	873	$0.043 \pm 0.008$
200	740	$0.958 \pm 0.046$	862	$0.227 \pm 0.013$	872	$0.099 \pm 0.006$
250	739	$0.809 \pm 0.053$	859	$0.342 \pm 0.024$	870	$0.155 \pm 0.011$
Solution 3, $R_{\text{Buffer}} = 1.716$ , $m_{\text{B}} = 0.96404$ mol $\text{kg}^{-1}$ , $m_{\text{NaClO}_4} = 0.0945$ mol $\text{kg}^{-1}$						
150	744	$1.161 \pm 0.033$	864	$0.192 \pm 0.007$	NA	NA
200	743	$1.044 \pm 0.081$	863	$0.260 \pm 0.021$	NA	NA
250	741	$0.930 \pm 0.057$	858	$0.405 \pm 0.026$	NA	NA
Solution 4, $R_{\text{Buffer}} = 3.542$ , $m_{\text{B}} = 0.90062$ mol $\text{kg}^{-1}$ , $m_{\text{NaClO}_4} = 0.0883$ mol $\text{kg}^{-1}$						
150	744	$1.237 \pm 0.043$	865	$0.132 \pm 0.010$	NA	NA
200	743	$0.983 \pm 0.041$	864	$0.246 \pm 0.012$	NA	NA
250	741	$0.901 \pm 0.040$	859	$0.302 \pm 0.017$	NA	NA
Solution 5a, $R_{\text{Buffer}} = 0.980$ , $m_{\text{B}} = 0.32012$ mol $\text{kg}^{-1}$ , $m_{\text{NaClO}_4} = 0.0283$ mol $\text{kg}^{-1}$						
250	740	$0.818 \pm 0.043$	859	$0.434 \pm 0.026$	872	$0.286 \pm 0.016$
Solution 5b, $R_{\text{Buffer}} = 0.980$ , $m_{\text{B}} = 0.32012$ mol $\text{kg}^{-1}$ + 0.301 mol $\text{kg}^{-1}$ NaCl, $m_{\text{NaClO}_4} = 0.0283$ mol $\text{kg}^{-1}$						
250	740	$0.864 \pm 0.061$	859	$0.462 \pm 0.036$	872	$0.252 \pm 0.019$
Solution 6a <sup>b</sup> , $R_{\text{Buffer}} = 1.000$ , $m_{\text{B}} = 0.30980$ mol $\text{kg}^{-1}$ , $m_{\text{NaClO}_4} = 0.0330$ mol $\text{kg}^{-1}$						
250	740	$0.535 \pm 0.029$	859	$0.297 \pm 0.019$	872	$0.229 \pm 0.013$
Solution 6b <sup>b</sup> , $R_{\text{Buffer}} = 0.980$ , $m_{\text{B}} = 0.30980$ mol $\text{kg}^{-1}$ + 0.302 mol $\text{kg}^{-1}$ LiCl, $m_{\text{NaClO}_4} = 0.0330$ mol $\text{kg}^{-1}$						
250	740	$0.658 \pm 0.041$	740	$0.384 \pm 0.029$	740	$0.269 \pm 0.019$

<sup>a</sup> Standard uncertainties,  $\pm$ , were taken to be equal to the relative standard errors of the Voigt function fits to the perchlorate and species bands.

<sup>b</sup>  $\text{LiB}(\text{OH})_4$  solution.





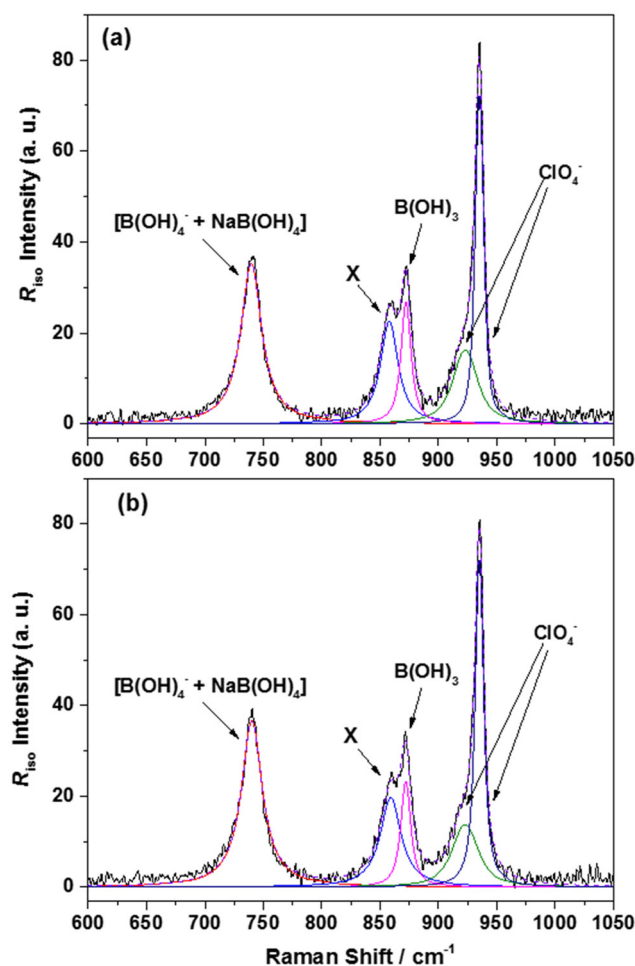
**Fig. 2** Reduced isotropic Raman spectra of  $\text{NaB(OH)}_4$  (aq.),  $R_{\text{iso}}(\bar{\nu})$ , at 250 °C and 20 MPa, showing the fitted Voigt functions used to determine peak positions and peak areas relative to the perchlorate internal standard for Solution 1, Run 1 ( $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 1.019 \text{ mol kg}^{-1}$ ,  $0.0902 \text{ mol kg}^{-1}$  sodium perchlorate). Where "X" is diborate, Fig. 6 is believed to be a more accurate representation of the individual species bands.

cate on a separate day, at 20 MPa and temperatures from 25 to 250 °C, and a second solution with similar composition (Solution 2, Table 1) was also run under the same conditions. Peak fitting to integrate the area under each band was done with a Voigt function using the curve fitting function in Origin Pro 2016 software. The fitting parameters for the position and the Lorentzian and Gaussian widths of the boric acid peak at each temperature were constrained to be same as those reported by Sasidharanpillai *et al.*,<sup>8</sup> for the boric acid peak in a 0.780 molal boric acid solution acquired with the same instrument under similar experimental conditions. As an example, the deconvoluted spectrum of Solution 1 at 250 °C is shown in Fig. 2. The areas were determined as the areas of peaks for species  $i$  relative to the perchlorate internal standard,  $A_i/A_{\text{IS}}$ . Following established practice,<sup>8</sup> the sum of the areas of the two peaks at  $\sim 935 \text{ cm}^{-1}$  and  $\sim 920 \text{ cm}^{-1}$  was used in the calculation of the total area of the perchlorate band. The standard errors in the relative areas for the boron bands were 10% or less. The solutions and initial concentrations run in this study, together with the frequencies and relative peak areas corresponding to each of the deconvoluted Raman bands, are tabulated in Table 1.

We measured Raman spectra at 250 °C using sodium borate solutions in  $\text{D}_2\text{O}$  with isotopically pure  $\text{B(OD)}_3$  and  $\text{NaOD}$ , similar in composition to Solutions 1, 3 and 4, in an attempt to confirm the identification of diborate species. This single set of runs using isotopically pure  $\text{B(OD)}_3$  and  $\text{NaOD}$  consumed about 1000 mL  $\text{D}_2\text{O}$ . Complications arising from the Fermi resonance effects in the spectra for  $\text{B(OD)}_3$  and the shifts in speciation associated with the deuterium isotope effect on its ionization constant proved too difficult to resolve.<sup>22,23</sup> Details are reported in ESI section S2.†

### 3.2. The effect of excess $\text{Na}^+$ and $\text{Li}^+$ cations and possible ion pairing

Previous Raman experiments on boric acid/borate confirmed that Raman spectroscopy cannot distinguish between free borate  $[\text{B(OH)}_4]^-$  and the ion pair  $[\text{NaB(OH)}_4]^0$ , possibly because  $[\text{NaB(OH)}_4]^0$  exists as solvent-separated ion pairs.<sup>9</sup> Reduced isotropic Raman spectra for  $\text{NaB(OH)}_4$  and  $\text{LiB(OH)}_4$  solutions (Solution 5:  $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 0.320$ ; and Solution 6:  $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 0.310 \text{ mol kg}^{-1}$ ; respectively), and the spectra of the same solutions to which an approximately equimolar excess of  $\text{NaCl}$  or  $\text{LiCl}$  had been added, were recorded at 250 °C and 20 MPa. Fig. 3 shows the isotropic spectra and corresponding deconvolution of peaks for Solution 5a ( $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 0.320$ ) and Solution 5b ( $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 0.320$ ,  $m_{\text{NaCl}} = 0.301$ ) at 250 °C and 20 MPa. The similarity in the spectra and corresponding deconvolution for solutions with



**Fig. 3** Reduced isotropic Raman spectra of  $\text{NaB(OH)}_4$ (aq.) with and without  $\text{NaCl(aq.)}$ ,  $R_{\text{iso}}(\bar{\nu})$ , at 250 °C and 20 MPa, showing the fitted Voigt functions used to determine peak positions and peak areas relative to the perchlorate internal standard. (a) Solution 5a:  $R_{\text{Buffer}} 0.980$ ,  $m_{\text{B}} = 0.32012 \text{ mol kg}^{-1}$  with  $0.0283 \text{ mol kg}^{-1}$  sodium perchlorate and (b) Solution 5b:  $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 0.32012 \text{ mol kg}^{-1}$  +  $0.301 \text{ mol kg}^{-1}$   $\text{NaCl}$  with  $0.0283 \text{ mol kg}^{-1}$  sodium perchlorate.



and without excess NaCl/LiCl indicates that the presence and identity of the cation does not affect the concentration of the unknown species, and confirms either that the new band does not result from ion-pair formation, or that there is extensive ion pairing in even the dilute  $\text{NaB}(\text{OH})_4$  and  $\text{LiB}(\text{OH})_4$  solutions. The frequencies and relative peak areas are reported in Table 1.

### 3.3. The effect of excess hydroxide

The Raman spectra of solutions of different  $R_{\text{Buffer}}$  values  $\geq 1$  were recorded at 150, 200 and 250 °C and 20 MPa in order to understand the effect of hydroxide ion on the equilibrium reactions responsible for the newly observed species. The reduced isotropic Raman spectra and peak deconvolution of Solutions 3 ( $R_{\text{Buffer}} = 1.716$ ) and 4 ( $R_{\text{Buffer}} = 3.542$ ) at 250 °C and 20 MPa, are shown in Fig. 4. When the concentration of

hydroxide ion was increased, the boric acid peak became negligible, and only the bands associated with the borate ion and the new species could be observed. The frequencies and peak areas of each band are listed in Table 1. The ratio of the peak areas for the bands at 865  $\text{cm}^{-1}$  and 745  $\text{cm}^{-1}$ ,  $A_{865}/A_{745}$ , increased with temperature, and did not depend strongly on the hydroxide concentration.

## 4. *Ab initio* and DFT computational results

### 4.1. Borates, diborates, and higher polyborates

In a previous study on polyborates by Applegarth *et al.*<sup>9</sup> at 25 and 80 °C, the predicted isotropic Raman spectra of boric acid,  $\text{B}(\text{OH})_3$ ; borate ion,  $[\text{B}(\text{OH})_4]^-$ ; the oxo-bridged diborates  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$  and  $[\text{B}_2\text{O}(\text{OH})_5]^-$ ; the cyclic triborate ion,  $[\text{B}_3\text{O}_3(\text{OH})_4]^-$ ; metaboric acid,  $\text{B}_3\text{O}_3(\text{OH})_3$ ; tetraborate,  $[\text{B}_4\text{O}_5(\text{OH})_4]^{2-}$ ; and the pentaborates  $[\text{B}_5\text{O}_6(\text{OH})_4]^-$  and  $[\text{B}_5\text{O}_6(\text{OH})_6]^{3-}$ , were discussed and compared with experimental results. The frequencies for boric acid, borate, and the higher polyborates were reported by Applegarth *et al.*<sup>9</sup> It was shown that the frequencies of unscaled MP2 and B3LYP low-temperature Raman spectra compared very favorably with experimental results for  $\text{B}(\text{OH})_3$ ,  $[\text{B}(\text{OH})_4]^-$ ,  $[\text{B}_3\text{O}_3(\text{OH})_4]^-$ ,  $[\text{B}_4\text{O}_5(\text{OH})_4]^{2-}$ , and  $[\text{B}_5\text{O}_6(\text{OH})_4]^-$ , suggesting that these were the observed species. There was no experimental evidence from the Raman spectra for the presence of either  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$  or  $[\text{B}_2\text{O}(\text{OH})_5]^-$  at these temperatures, consistent with the recently completed detailed NEA/OECD literature review by the Thermodynamic Database Project.<sup>24</sup> Generally speaking, the MP2 and B3LYP results were found to underestimate the experimental frequencies by up to 35  $\text{cm}^{-1}$  because the effect of the solvent was not explicitly included in these calculations, and this effect increased with the overall charge of the species. Hartree Fock calculations, which were also carried out, were found to overestimate the frequencies by a larger, less predictable amount.

The high-temperature Raman results obtained in this study were used to direct our calculations. These suggest that there is an additional species in equilibrium with  $\text{B}(\text{OH})_3$  and  $[\text{B}(\text{OH})_4]^-$ , which gives rise to a characteristic Raman band at 865  $\text{cm}^{-1}$ , concomitant with dissociation of borate into boric acid. Based on the known spectra of the boric acid/borate solutions at 25 °C,<sup>9</sup> the most likely candidates are the metaborate ion,  $[\text{BO}(\text{OH})_2]^-$ ; one of four diborate species,  $[\text{B}_2\text{O}(\text{OH})_5]^-$ ,  $[\text{B}_2\text{O}_3(\text{OH})_4]^{2-}$ ,  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$  or  $[\text{B}_2(\text{OH})_7]^-$ ; or a higher polyborate species (possibly  $[\text{B}_3\text{O}_3(\text{OH})_5]^{2-}$ ) that is not a significant species at 25 °C. Less likely neutral species that might result from the condensation reactions of boric acid, driven by higher ionic strength or temperature, are  $[\text{B}_2(\text{OH})_6]^0$  and  $[\text{B}_2\text{O}(\text{OH})_4]^0$ .

*Ab initio* computational studies on these species were carried out at several levels of theory, with and without solvation, as discussed in the following section. Selected gas-phase structures were taken from previous studies of Pye *et al.*<sup>21,25</sup> The structures of the diborate species derived from

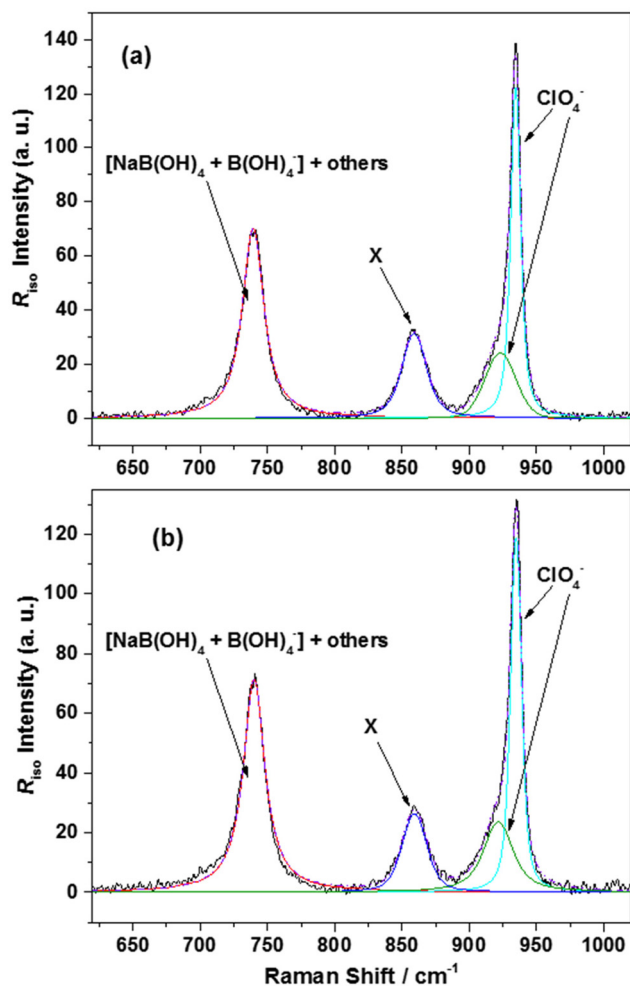


Fig. 4 Reduced isotropic Raman spectra of  $\text{NaB}(\text{OH})_4(\text{aq.})$  with excess  $\text{NaOH}(\text{aq.})$ ,  $R_{\text{Iso}}(\bar{\nu})$ , at 250 °C and 20 MPa, showing the fitted Voigt functions used to determine peak positions and peak areas relative to the perchlorate internal standard. (a) Solution 3:  $R_{\text{Buffer}} = 1.716$ ,  $m_{\text{B}} = 0.96404 \text{ mol kg}^{-1}$ , with  $m_{\text{NaClO}_4} = 0.0945 \text{ mol kg}^{-1}$  sodium perchlorate; (b) Solution 4:  $R_{\text{Buffer}} = 3.542$ ,  $m_{\text{B}} = 0.90062 \text{ mol kg}^{-1}$ , with  $0.0883 \text{ mol kg}^{-1}$  sodium perchlorate.



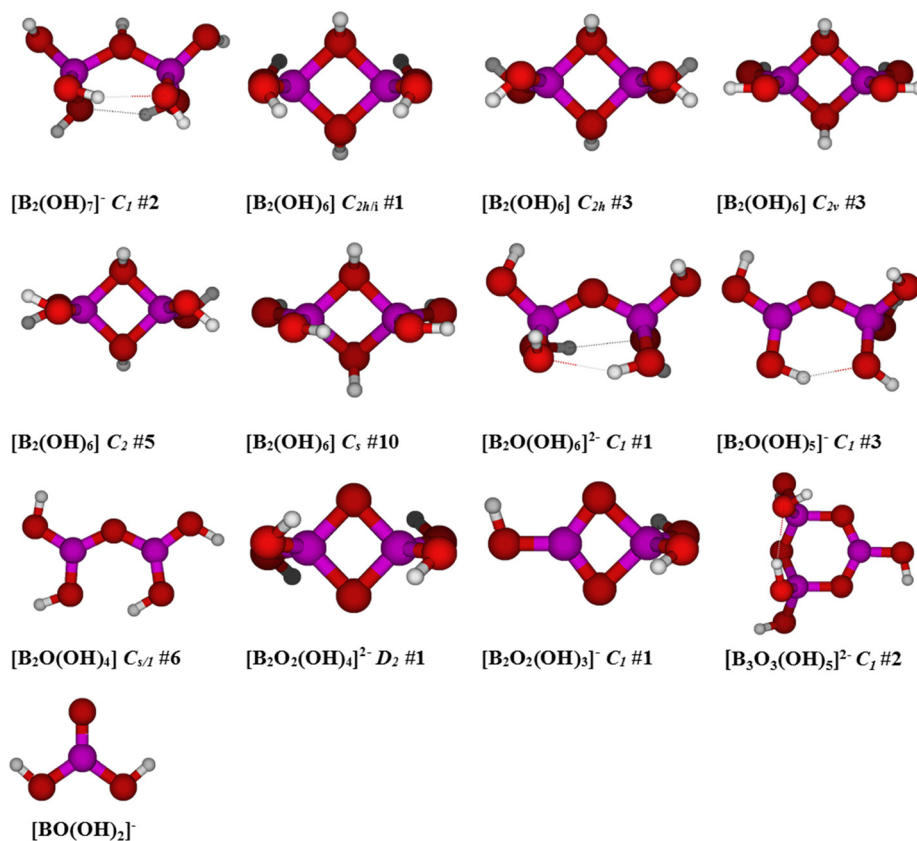


Fig. 5 Calculated structures (using Gaussian 03) of the postulated diborate species considered for the unknown Raman peak at  $865\text{ cm}^{-1}$ , along with their symmetry.

these calculations in this study are shown in Fig. 5. Gas-phase Raman frequency calculations were done for a broader number of potential di/triborate species initially, with results listed in ESI (Table S1†). The Raman frequencies and the corresponding isotropic Raman activities for the ionic di/triborate species in solution phase are tabulated in Table 2.

#### 4.2. Neutral diborate species

**4.2.1. Boric acid dimer,  $[B_2(OH)_6]^0$ .** The possibility of a neutral dimer of boric acid,  $[B_2(OH)_6]^0$ , was explored computationally. Initial attempts to locate a  $C_s$ -symmetric dimer with a single bridging hydroxyl group resulted in dissociation to a hydrogen-bonded boric acid dimer  $[B(OH)_3]_2$ , thus systematic desymmetrization from a high symmetry structure was attempted. Neither of the two  $D_{2h}$  forms are minima, but, unexpectedly, some of the  $C_{2v}$  and  $C_{2h}$  structures were. Some  $C_{2h}$  structures broke two B–O bonds during optimization to give two molecules of boric acid. Furthermore, some additional minima were found, of  $C_2$  and  $C_s$  symmetry. Of all of the potential structures,  $C_{2v}$  #3 was the most stable, however, the calculated isotropic Raman modes corresponding to B–O stretching and/or deformation are too low in frequency. The gas-phase dimerization energy was also calculated to be prohibitively large for any appreciable amount to coexist with boric acid ( $35\text{--}104\text{ kJ mol}^{-1}$ ).

**4.2.2. Oxo-bridged dimer of boric acid,  $[B_2O(OH)_4]^0$ .** The dehydrated oxo-bridged dimer of boric acid,  $[B_2O(OH)_4]^0$ , was also considered. None of the four possible  $C_{2v}$  structures were stable, but the corresponding  $C_2$  structures were, in which the  $BO_3$  subunits have twisted out of the plane of the B–O–B bridge. These  $C_s$  structures formed by rotating hydroxyl groups and containing an internal hydrogen bond, were also stable, with  $C_s$  #6 being the most stable overall; however, the most intense band in the isotropic Raman spectrum was predicted to be too low ( $770\text{--}780\text{ cm}^{-1}$ ) to make this a reasonable possibility.

#### 4.3. Ionic diborate species

**4.3.1. The diborate ion,  $[B_2(OH)_7]^-$ .** The diborate ion identified in the potentiometric study by Mesmer *et al.*<sup>14</sup> was postulated to be  $[B_2(OH)_7]^-$ . The computational methods employed here indicate that neither of the two  $C_{2v}$  forms are minima on the potential energy surface, and the same is true of the two  $C_2$  and four  $C_s$  structures derived from them. In fact, one of the  $C_s$  structures dissociates into boric acid and borate. However, two minimum-energy  $C_1$  structures do exist, of which the second is slightly more stable. This species is predicted to have two intense bands in the isotropic Raman spectrum below  $1000\text{ cm}^{-1}$ , where the higher but less intense band for B3LYP calculations gives a reasonable match to experiment.





**4.3.2. Oxo-bridged diborate ions**  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$ ,  $[\text{B}_2\text{O}(\text{OH})_5]^-$ ,  $[\text{B}_2\text{O}_2(\text{OH})_4]^{2-}$ , and  $[\text{B}_2\text{O}_2(\text{OH})_3]^-$ . Frequency and isotropic Raman activity calculations for oxo-bridged diborate species were performed with same basis set as in the gas phase calculations, using a polarizable continuum model to simulate hydration effects.

The oxo-bridged diborates  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$  and  $[\text{B}_2\text{O}(\text{OH})_5]^-$  were previously considered<sup>9</sup> as candidates for the band at  $773\text{ cm}^{-1}$ , observed as a shoulder on the borate peak at  $745\text{ cm}^{-1}$ .  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$  may exist as an oxo-bridged dimer with one of two  $C_2$  and three  $C_1$  structures lying within  $15\text{ kJ mol}^{-1}$  of each other, having weak bands at  $812\text{--}870\text{ cm}^{-1}$  which appear in the correct region for matching with the experimental band at  $865\text{ cm}^{-1}$ .  $[\text{B}_2\text{O}(\text{OH})_5]^-$  may exist as an oxo/hydroxo doubly bridged dimer, but these forms were not stable and resulted in cleavage of one of the  $\text{B}\text{--}\mu\text{OH}$  bonds upon relaxation of symmetry constraints, giving rise to one of nine possible oxo-bridged  $C_1$  structures.  $[\text{B}_2\text{O}(\text{OH})_5]^-$  is calculated to have weak bands at  $890\text{--}940\text{ cm}^{-1}$  which would be too high in frequency. Additionally, both of these species have an intense band predicted at lower frequencies ( $680\text{--}720\text{ cm}^{-1}$ ), which is not experimentally observed.

Species containing two oxo bridges were also considered.  $[\text{B}_2\text{O}_2(\text{OH})_4]^{2-}$  may exist as one of two possible  $D_{2h}$  structures, neither of which was found to be stable. Desymmetrization can give rise to two  $D_2$ , four  $C_{2h}$ , and one  $C_{2v}$  structures. The  $D_2$  #1 structure is the most stable at all levels, and the  $C_{2h}$  #1 and  $D_2$  #2 structures are stable at some levels. For unstable structures, further desymmetrization give stable structures with  $C_2$ ,  $C_i$ , and  $C_s$  symmetry. The two most intense bands of roughly equal intensity in the isotropic Raman spectrum are predicted at  $570\text{--}580\text{ cm}^{-1}$  and  $830\text{--}850\text{ cm}^{-1}$ , and these are expected to be systematically too low by about  $20\text{ cm}^{-1}$ . The latter band, therefore, is a viable candidate for the experimentally observed band at  $865\text{ cm}^{-1}$ , however, no evidence for the predicted weak band at around  $600\text{ cm}^{-1}$  was observed in the experimental spectrum ( $R_{\text{Buffer}} = 0.980$ ,  $m_{\text{B}} = 1.019\text{ mol kg}^{-1}$ ). It is possible that these peaks would be obscured if  $[\text{B}_3\text{O}_3(\text{OH})_4]^-$  was present, but this does not appear to be the case for solutions of this composition.

The second possible species with two oxo bridges is  $[\text{B}_2\text{O}_2(\text{OH})_3]^-$ , which could exist as one of two  $C_{2v}$  structures, neither of which is a minimum. Desymmetrization to one of two possible  $C_2$  or four possible  $C_s$  structures also did not result in minima. Two  $C_1$  structures exist, the first of which is the most stable, however, the calculations predict the existence of several intense bands in the  $500\text{--}1000\text{ cm}^{-1}$  range and none of these are a satisfactory match to experiment. In addition, of the two bands that bracket the experimental value, it is the remaining two which would have the greatest intensity.

#### 4.4. Ionic triborate species

**4.4.1. The triborate ion,  $[\text{B}_3\text{O}_3(\text{OH})_5]^{2-}$ .** The cyclic divalent triborate ion was also examined. Neither of the two  $C_s$  forms were stable, and converted to the corresponding  $C_1$  forms. Several intense isotropic bands in the range  $500\text{--}800\text{ cm}^{-1}$  were noted. Most of the lower frequency bands correspond to

HOB bending. It is unlikely that these would be observed in practice because the coupling with water librations in the first solvation shell would broaden the bands. No band at around  $865\text{ cm}^{-1}$  was observed; however, a band predicted at  $\sim 730\text{ cm}^{-1}$ , which would be obscured under the experimentally observed borate peak at  $745\text{ cm}^{-1}$ , may be a contributing factor to the apparent charge-balance discrepancy, noted below.

#### 4.5. Solvent effects: CPCM calculations

Candidates for the unknown species were therefore reduced to  $[\text{B}_2(\text{OH})_7]^-$ ,  $[\text{B}_2\text{O}(\text{OH})_5]^-$ ,  $[\text{B}_2\text{O}_2(\text{OH})_4]^{2-}$ ,  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$  and  $[\text{BO}(\text{OH})_2]^-$  based on the frequencies from different levels of gas phase calculations together with polarizable continuum model calculations. The reduced Raman isotropic frequencies and their corresponding Raman activities for the three diborate species and metaboric acid, using HF/6-31G\*, HF/6-31+G\*, HF/6-311+G\*, B3LYP/6-31G\*, B3LYP/6-31+G\*, B3LYP/6-311+G\*, MP2/6-31G\*, MP2/6-31+G\*, and MP2/6-311+G\* with a polarizable continuum model, are summarized in Table 2. The Raman activities (intensities) correspond to the unpolarised spectra. Only those expected to give significant intensity in the isotropic spectra (depolarization ratio significantly less than 0.75) are listed. In the discussions below, computational frequencies for comparison with experiment were taken from the MP2/6-311+G\* results in Table 2.

The  $[\text{B}_2\text{O}(\text{OH})_5]^-$  species is calculated to have two bands, one in the range  $700\text{--}750\text{ cm}^{-1}$  and the other in the range  $910\text{--}975\text{ cm}^{-1}$ , depending upon the level of theory and basis set (Table 2). The  $[\text{B}_2(\text{OH})_7]^-$  species also was also calculated to have two strong bands, with a peak in the range  $690\text{--}740\text{ cm}^{-1}$  and another in the range  $830\text{--}890\text{ cm}^{-1}$ . The divalent species  $[\text{B}_2\text{O}_2(\text{OH})_4]^{2-}$  is predicted to have a very strong band in the region  $830$  to  $850\text{ cm}^{-1}$ , which may correspond to the experimental band at  $865\text{ cm}^{-1}$ , but the absence of a weak band near  $600\text{ cm}^{-1}$  appears to rule it out. The other divalent species,  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$ , was found to have only one strong calculated band centered in the region  $700\text{--}740\text{ cm}^{-1}$ , and therefore cannot be the source of the experimental band at  $865\text{ cm}^{-1}$ . Although the computational results for mononuclear metaborate  $[\text{BO}(\text{OH})_2]^-$  do yield a very strong band at  $888\text{ cm}^{-1}$ , the very strong bands predicted to be at  $\sim 1050\text{ cm}^{-1}$  and  $1450\text{ cm}^{-1}$  are completely absent in the experimental spectra.

## 5. Chemical equilibrium modelling

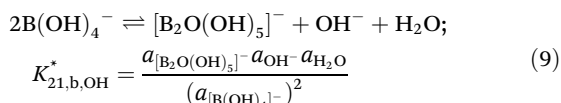
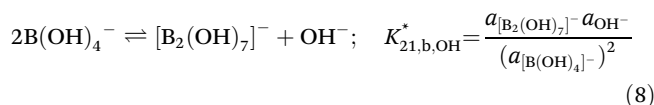
### 5.1. Modelling considerations

**5.1.1. Choice of potential diborate species for further modelling.** The Raman spectra predictions from the MP2/6-311+G\* computational results presented above, yielded four ionic species with very strong bands in the range of interest, ( $865 \pm 80$ )  $\text{cm}^{-1}$ . The diborates  $[\text{B}_2(\text{OH})_7]^-$  and  $[\text{B}_2\text{O}(\text{OH})_5]^-$  were predicted to have bands at  $848\text{ cm}^{-1}$  and  $925\text{ cm}^{-1}$ , respectively. In addition, they are predicted to have strong bands at  $719\text{ cm}^{-1}$  and  $728\text{ cm}^{-1}$ , respectively, which may underlie the

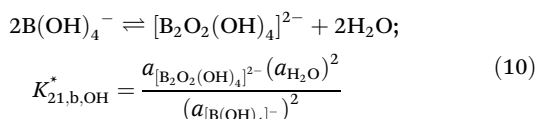


borate band at 745 cm<sup>-1</sup>. The divalent species [B<sub>2</sub>O<sub>2</sub>(OH)<sub>4</sub>]<sup>2-</sup> was considered less likely to be the major species contributing to the experimental band at 865 cm<sup>-1</sup>, because of the absence of a weak band near 600 cm<sup>-1</sup> and charge balance considerations described below. Although the metaborate ion [BO(OH)<sub>2</sub>]<sup>-</sup> shows a very strong computational band at 835 cm<sup>-1</sup>, it was ruled out by the absence of strong and very strong bands at 1049 cm<sup>-1</sup> and 1451 cm<sup>-1</sup> in the experimental spectra.

The classic potentiometric study by Mesmer *et al.*<sup>14</sup> identified a singly-charged diborate ion as a statistically significant species from 50 to 200 °C. As a result, it seems likely that the new species is one or both of the diborates [B<sub>2</sub>(OH)<sub>7</sub>]<sup>-</sup> and [B<sub>2</sub>O(OH)<sub>5</sub>]<sup>-</sup>, with [B<sub>2</sub>O<sub>2</sub>(OH)<sub>4</sub>]<sup>2-</sup> possibly also present as an equilibrium species at temperatures above 200 °C. Thus, the relevant diborate reactions to be considered in developing a chemical equilibrium model are:



and, possibly,



Here, the asterisk notation,  $Q_{21,\text{b,OH}}^*$ , indicates cumulative formation of the diborate from B(OH)<sub>4</sub><sup>-</sup> rather than B(OH)<sub>3</sub>. Eqn (8) to (10) are expressed as formation reactions from borate rather than boric acid because the equilibrium molalities of B(OH)<sub>3</sub> are negligible at the hydroxide concentrations used in Solutions 4 and 5.

The modelling approach adopted here was based on boron mass balance. Speciation calculations were carried out using the experimental peak areas of the three bands, the boron mass balance, and the known scattering coefficients of B(OH)<sub>3</sub> and [B(OH)<sub>4</sub>]<sup>-</sup>,<sup>8,9</sup> from the expression:

$$m_i = \left( \frac{S_{\text{IS}}}{S_i} \right) \cdot \left( \frac{A_i}{A_{\text{IS}}} \right) \cdot m_{\text{IS}} \quad (11)$$

Here,  $m_i$  and  $m_{\text{IS}}$  are the molalities of the species  $i$  and the perchlorate internal standard, IS, respectively;  $S_i/S_{\text{IS}}$  is the relative scattering coefficient for species  $i$  with respect to the internal standard;  $A_i$  and  $A_{\text{IS}}$  are the peak areas of species  $i$ , and the internal standard, respectively. The values for the relative scattering coefficients  $S_i/S_{\text{IS}}$  for B(OH)<sub>3</sub> and [B(OH)<sub>4</sub>]<sup>-</sup> were taken from Applegarth *et al.*<sup>9</sup> and Sasidharanpillai *et al.*<sup>8</sup> Although both monovalent species [B<sub>2</sub>(OH)<sub>7</sub>]<sup>-</sup> and [B<sub>2</sub>O(OH)<sub>5</sub>]<sup>-</sup> are predicted to have two strong bands in the frequency range relevant to this study, [B<sub>2</sub>(OH)<sub>7</sub>]<sup>-</sup> was selected because Gaussian

calculations typically under-predict, rather than over-predict the experimental vibrational frequency.<sup>23</sup> The divalent species with [B<sub>2</sub>O<sub>2</sub>(OH)<sub>4</sub>]<sup>2-</sup> was also included in the chemical equilibrium modelling as a less likely candidate species.

**5.1.2. Identifying the “best” diborate chemical model.** To carry out the speciation analysis, the reduced isotropic spectrum of the diborate species was assumed to consist of the strong band at 865 cm<sup>-1</sup>, and a second band underlying the borate peak at 745 cm<sup>-1</sup>, with relative intensities (relative scattering coefficients) of  $S_{\text{B}_2,745}/S_{\text{B}_2,865}$ , where  $S_{\text{B}_2,745}/S_{\text{B}_2,865}$  is defined as the scattering coefficient ratio of diborate peaks at 745 cm<sup>-1</sup> and 865 cm<sup>-1</sup>. Trial values of  $S_{\text{B}_2,745}/S_{\text{B}_2,865}$  were then used to estimate the contribution of [B<sub>2</sub>(OH)<sub>7</sub>]<sup>-</sup> to the total area of the peak at 745 cm<sup>-1</sup> using eqn (12), and to the peak area of borate using eqn (13):

$$A_{\text{B}_2,745} = \frac{S_{\text{B}_2,745}}{S_{\text{B}_2,865}} \cdot A_{\text{B}_2,865} \quad (12)$$

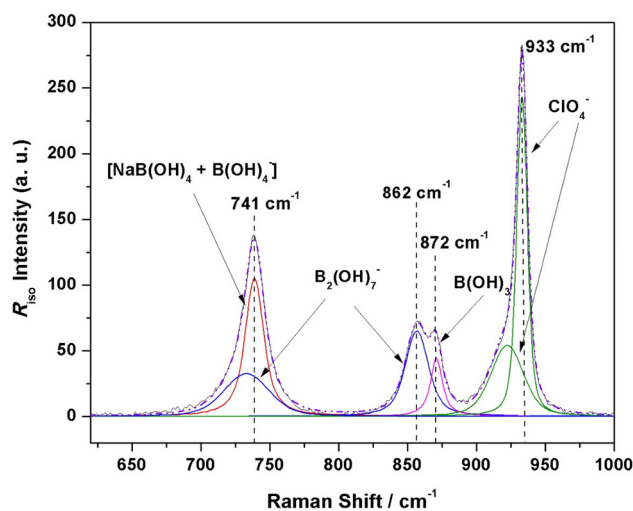
$$A_{\text{Borate},745} = A_{\text{total},745} - A_{\text{B}_2,745} \quad (13)$$

where  $A_{\text{B}_2,745}$ ,  $A_{\text{Borate},745}$  and  $A_{\text{total},745}$  are the areas corresponding to diborate at 745 cm<sup>-1</sup>, borate at 745 cm<sup>-1</sup> and total area of the peak at 745 cm<sup>-1</sup>, respectively. Three choices for the scattering coefficient of the diborate band at 745 cm<sup>-1</sup>, relative to the band at 865 cm<sup>-1</sup> were considered:  $S_{\text{B}_2,745}/S_{\text{B}_2,865} = 0$  (Model 1);  $S_{\text{B}_2,745}/S_{\text{B}_2,865} = 0.95$  (Model 2); and  $S_{\text{B}_2,745}/S_{\text{B}_2,865} = 1.5$  (Model 3). Model 1 is applicable to diborate species postulated to have no band at 745 cm<sup>-1</sup>, corresponding exclusively to band “X” in Fig. 2. Models 2 and 3 were based on the MP2/6-311+G\* computational values of  $S_{\text{B}_2,745}/S_{\text{B}_2,865}$  for [B<sub>2</sub>(OH)<sub>7</sub>]<sup>-</sup> and [B<sub>2</sub>O(OH)<sub>5</sub>]<sup>-</sup>, respectively, in Table 2. Although computational Raman scattering intensities are known to be quite unreliable,<sup>21,25</sup> the calculated relative Raman intensities of two bands within the same molecule are expected to be more accurate.

Models 1 and 3 proved to be not consistent with the physico-chemical constraints. For Model 1, the experimental scattering coefficient of the 865 cm<sup>-1</sup> band relative to that of the perchlorate internal standard  $S_{\text{B}_2,865}/S_{\text{IS}}$  was found to increase by about 300% from 150 °C to 300 °C, and had significant discrepancies in the charge balance of Solutions 1 and 2 of +10% at 150 °C, rising to +20% at 300 °C. Model 3 had an almost constant scattering coefficient, but a negligible concentration of [B(OH)<sub>4</sub>]<sup>-</sup> at 300 °C, which contradicts the results of previous studies by Mesmer *et al.*,<sup>14</sup> Wang *et al.*<sup>17</sup> and Palmer *et al.*<sup>26</sup>

Model 2 yielded scattering coefficients that were independent of concentration and temperature above 150 °C,  $S_{\text{B}_2,865}/S_{\text{IS}} = 0.107 \pm 0.015$ . The charge balances had small systematic discrepancies. For Solutions 1 and 2 it was too positive (~15% at 150 °C rising to ~30% above 200 °C), and for Solutions 5 and 6 at 250 °C it was similarly elevated (~+12% after the effect of the excess NaCl and LiCl was subtracted) (ESI, Table S2†). Varying the relative scattering coefficient of the diborate bands by ±10% did not significantly change the internal consistency of the treatment. Representative fits for





**Fig. 6** Reduced isotropic Raman spectra of  $\text{NaB(OH)}_4(\text{aq.})$ ,  $R_{\text{Iso}}(\bar{\nu})$ , at 250 °C and 20 MPa from Fig. 2, indicating the calculated hypothetical contributions to the 745  $\text{cm}^{-1}$  band from  $[\text{B(OH)}_4]^-$  and  $[\text{B}_2(\text{OH})_7]^-$  corresponding to a relative scattering factor for the diborate ion bands of  $S_{\text{B}_2,745}/S_{\text{B}_2,865} = 0.95$ , as predicted by the DFT calculations.

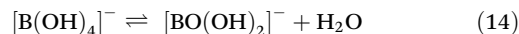
the reduced isotropic Raman spectra using Model 2 for  $\text{Na}(\text{BOH})_4(\text{aq.})$ ,  $R_{\text{Iso}}(\bar{\nu})$ , at 250 °C and 20 MPa are shown in Fig. 6. The calculated equilibrium molalities and diborate scattering coefficients using Model 2 are tabulated in Table 3.

These results provide strong evidence for the presence of a new species that is a diborate ion, with bands in the 745 region and at 865  $\text{cm}^{-1}$ ,  $S_{\text{B}_2,745}/S_{\text{B}_2,865} = 0.95 \pm 0.10$ . The analysis above suggests that the new species is very probably  $[\text{B}_2(\text{OH})_7]^-$ . A factor analysis of the Raman spectra at 250 °C was performed, using the singular value decomposition 'svds' function on Matlab R2021b. Although the data set was limited and mathematically underdetermined, there were four statistically significant factors. In addition to the peaks at 739.4  $\text{cm}^{-1}$  (borate) and 874.0  $\text{cm}^{-1}$  (boric acid), there were also major peaks identified at 737.5  $\text{cm}^{-1}$  and 863.7  $\text{cm}^{-1}$ , and minor peaks at 746.9  $\text{cm}^{-1}$ , 754.5  $\text{cm}^{-1}$ , 853.3  $\text{cm}^{-1}$ , and 866.0  $\text{cm}^{-1}$ , at 250 °C, supporting the model with a new species having a Raman peak around  $\sim 750$  and 865  $\text{cm}^{-1}$ .

The charge-balance discrepancy and the factor analysis of the high temperature Raman data, suggest that another anionic boron species may be present as a minor equilibrium species, possibly  $[\text{B}_2\text{O}_2(\text{OH})_4]^{2-}$ . Adding a contribution from the minor divalent species to the band at 865  $\text{cm}^{-1}$  did not lead to an improved model. The possibility that  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$  might have been present was addressed by adding a divalent anionic species to the 745  $\text{cm}^{-1}$  band in the models noted above and varying the relative scattering coefficients of both diborate species. However, it was not possible to achieve fully temperature-independent scattering coefficients and charge balance.

Additional evidence that the 865  $\text{cm}^{-1}$  band is not due to  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$  or  $[\text{BO}(\text{OH})_2]^-$  is provided by the effect of hydroxide on the reduced isotropic Raman spectra at 250 °C. As can

be seen in Reactions 8 and 9, hydroxide participates directly in the formation of these two diborate ions from borate. However, the divalent diborate species  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$  and metaborate form by condensation reactions which are not pH dependent, as described in Reaction 14 and by:



It is clear from the stoichiometry of these reactions that the equilibria to form monovalent  $[\text{B}_2(\text{OH})_7]^-$  and/or its condensed product  $[\text{B}_2\text{O}(\text{OH})_5]^-$  are affected by changes in the concentration of  $\text{OH}^-$ , whereas the formation of  $[\text{B}_2\text{O}(\text{OH})_6]^{2-}$  and/or  $[\text{BO}(\text{OH})_2]^-$  are not. The constant values for the relative scattering factors in Table 3, calculated from the relative peak areas of the 745  $\text{cm}^{-1}$  and 865  $\text{cm}^{-1}$  bands for Solutions 3 and 4 using Model 2, support the conclusion that  $[\text{B}_2(\text{OH})_7]^-$  and/or  $[\text{B}_2\text{O}(\text{OH})_5]^-$  are the equilibrium diborate species. This is consistent with the potentiometric studies reported by Mesmer *et al.*<sup>14</sup> who identified the presence of a singly charged diborate species in sodium borate solutions at higher temperature, and postulated the existence of the  $[\text{B}_2(\text{OH})_7]^-$  species. The consistent value obtained for the scattering factors at other temperatures over the range 200 to 300 °C,  $S_{[\text{B}_2(\text{OH})_7]^-}^f \approx 0.107 \pm 0.015$ , despite changes in pH associated with changes in the boric acid ionization constant further supports this conclusion.

Based on the evidence presented above, our analysis was based on the premise that  $[\text{B}_2(\text{OH})_7]^-$  is the major equilibrium diborate species, and that polyborate formation quotients could be determined using the concentrations from Model 2.

## 5.2. Equilibrium chemical speciation and diborate formation quotients

The equilibrium quotient for  $[\text{B}_2(\text{OH})_7]^-$  diborate formation from the borate ion, according to reaction (8), was calculated from the expression:

$$Q_{21,\text{b,OH}}^* = \frac{m_{[\text{B}_2(\text{OH})_7]^-} \cdot m_{\text{OH}^-}}{(m_{\text{B(OH)}_4^-})^2} \quad (15)$$

using the experimental molalities of the species calculated from Model 2. Here, the asterisk notation,  $Q_{21,\text{b,OH}}^*$ , indicates cumulative formation of the diborate from  $\text{B(OH)}_4^-$  rather than  $\text{B(OH)}_3$ .

The experimental molalities of each species and resulting formation quotients for  $\text{B}_2(\text{OH})_7^-$  are tabulated in Table 3. For Solutions 3 and 4, the molalities of the hydroxide ions required for these calculations were calculated from charge and mass balance. For all other solutions, which had buffer ratios  $R_{\text{Buffer}} \approx 1$ , the hydroxide molalities were derived from the experimental borate and boric acid molalities, and the expression for the ionization constant of boric acid reported by Palmer *et al.*,<sup>26</sup> as described in our previous study.<sup>8</sup>

The diborate formation quotients from Table 3 for Solutions 1 and 2 ( $\text{NaBOH}_4(\text{aq.})$ ,  $R_{\text{Buffer}} = 1$ ,  $m = 1 \text{ mol kg}^{-1}$ ) are plotted as a function of temperature in Fig. 7, where they are compared to the equilibrium constants reported by



**Table 3** Experimental solvent densities, equilibrium molalities for boron species and hydroxide, the relative scattering coefficient,  $S_{B_2,865}^r = (S_{[B_2(OH)_7]^-}/S_{[ClO_4]^-})$  and the resulting formation constants  $Q_{21,b,OH}^*$  for diborate at  $p = 20$  MPa. The relative scattering coefficients for the diborate bands 745 and 865  $cm^{-1}$  were taken to be  $S_{B_2,745}/S_{B_2,865} = 0.95 \pm 0.10$  (Model 2)<sup>a</sup>

$t/^\circ C$	$\rho_w/kg\ m^{-3}$	$m_{B(OH)_3}$	$m_{[B(OH)_4]^-}$	$m_{[B_2(OH)_7]^-}$	$m_{(OH)^-}$	$S_{[B_2(OH)_7]^-}^r$	$I/mol\ kg^{-1}$	$\log Q_{21,b,OH}^*$ Exp.	$\log Q_{21,b,OH}^*$ Wang <i>et al.</i> <sup>17</sup>	$\log K_{21,b,OH}^*$ Palmer <sup>24</sup>
Solution 1 (Run 1), $R_{Buffer} = 0.980$ , $m_B = 1.0188\ mol\ kg^{-1}$										
150	927.69	18.6 ± 1.4	616 ± 43	192 ± 21	47.65	(0.060 ± 0.008)	1.017	-1.618	-3.233	-2.512
200	877.97	44.0 ± 3.7	534 ± 53	220 ± 26	49.56	0.092 ± 0.013	0.991	-1.416	-3.002	-2.107
250	816.09	69.1 ± 4.0	339 ± 24	305 ± 12	41.04	0.106 ± 0.006	0.932	-0.962	-2.880	-1.878
275	778.71	73.4 ± 4.1	220 ± 29	363 ± 15	32.50	0.112 ± 0.007	0.897	-0.615	-2.860	-1.791
300	734.71	85.9 ± 3.2	275 ± 20	329 ± 10	42.25	0.129 ± 0.006	0.912	-0.736	-2.866	-1.691
Solution 1 (Run 2), $R_{Buffer} = 0.980$ , $m_B = 1.0188\ mol\ kg^{-1}$										
150	927.69	22.1 ± 1.9	619 ± 47	189 ± 23	40.33	(0.070 ± 0.010)	1.013	-1.700	-3.233	-2.512
200	877.97	33.2 ± 3.3	490 ± 49	248 ± 24	60.27	0.092 ± 0.011	0.988	-1.206	-3.002	-2.107
250	816.09	64.3 ± 6.7	326 ± 61	314 ± 31	42.47	0.109 ± 0.016	0.930	-0.900	-2.880	-1.878
Solution 2, $R_{Buffer} = 0.984$ , $m_B = 1.0391\ mol\ kg^{-1}$										
150	927.69	18.5 ± 3.5	648 ± 28	186 ± 14	50.20	(0.067 ± 0.007)	1.049	-1.652	-3.243	-2.512
200	877.97	42.4 ± 2.8	482 ± 32	257 ± 16	46.32	0.084 ± 0.007	1.000	-1.290	-3.014	-2.107
250	816.09	66.9 ± 4.8	315 ± 38	329 ± 19	39.40	0.099 ± 0.009	0.949	-0.883	-2.891	-1.878
Solution 3, $R_{Buffer} = 1.716$ , $m_B = 0.96404\ mol\ kg^{-1}$										
150	927.69	0.95 ± 0.15	629 ± 25	167 ± 13	857.6	(0.109 ± 0.009)	1.832	-0.440	-3.426	-2.512
200	877.97	2.23 ± 0.64	513 ± 55	225 ± 27	915.8	0.109 ± 0.016	1.862	-0.104	-3.237	-2.107
250	816.09	3.20 ± 0.68	350 ± 41	305 ± 20	996.9	0.126 ± 0.012	1.902	0.397	-3.111	-1.878
Solution 4, $R_{Buffer} = 3.542$ , $m_B = 0.90062\ mol\ kg^{-1}$										
150	927.69	0.35 ± 0.09	668 ± 30	116 ± 15	2406	(0.100 ± 0.015)	3.336	-0.377	-3.767	-2.512
200	877.97	0.95 ± 0.14	450 ± 27	225 ± 14	2515	0.097 ± 0.007	3.391	0.461	-3.606	-2.107
250	816.09	2.64 ± 0.39	368 ± 27	265 ± 14	2555	0.101 ± 0.008	3.411	0.964	-3.431	-1.878
Solution 5a, $R_{Buffer} = 0.980$ , $m_B = 0.32012\ mol\ kg^{-1}$										
250	816.09	36.5 ± 2.0	78.1 ± 9.7	103 ± 5.0	19.51	120 ± 0.009	0.285	-0.483	-2.152	-1.878
Solution 5b, $R_{Buffer} = 0.980$ , $m_B = 0.32012\ mol\ kg^{-1} + 0.301\ mol\ kg^{-1}\ NaCl$										
250	816.09	32.1 ± 2.5	82.0 ± 13.7	103 ± 7.0	21.97	0.127 ± 0.013	0.590	-0.472	-2.681	-1.878
Solution 6a, <sup>b</sup> $R_{Buffer} = 0.980$ , $m_B = 0.30980\ mol\ kg^{-1}$										
250	816.09	34.1 ± 2.0	56.8 ± 7.9	109 ± 4.1	15.22	0.090 ± 0.007	0.279	-0.287	-2.520	-1.878
Solution 6b, <sup>b</sup> $R_{Buffer} = 0.980$ , $m_B = 0.30980\ mol\ kg^{-1} + 0.302\ mol\ kg^{-1}\ LiCl$										
250	816.09	40.1 ± 2.8	66.0 ± 11.3	102 ± 5.8	14.18	0.124 ± 0.012	0.581	-0.479	-3.024	-1.878

<sup>a</sup> Uncertainties are propagated standard errors from the fitted Voight functions. Values in parentheses have scattering coefficients beyond the 90% confidence limit of the mean,  $S_{B_2,865}^r = 0.107 \pm 0.015$ , and were considered to have systematic errors.  $\log Q_{21,b,OH}^*$ , from Wang *et al.*<sup>17</sup> were calculated for similar  $R_{buffer}$  using OLI Studio but for the formation of  $B_2O(OH)_5^-$ .  $\log K_{21,b,OH}^*$ , from Palmer were calculated from  $\log K_{11}$  and  $\log K_{12}$  expressions in Ref. 24. <sup>b</sup>  $LiB(OH)_4$  solution.

Ferguson *et al.*<sup>27</sup> and Palmer *et al.*<sup>26</sup> Van't Hoff fits to the experimental formation quotients at ionic strength  $I = 1\ mol\ kg^{-1}$  from this work (Solutions 1 and 2) and from Mesmer *et al.*<sup>14</sup> yield the expressions:

$$\log Q_{21,b,OH}^*(T, I = 1\ mol\ kg^{-1}) = (-1673 \pm 171) + (2.28 \pm 0.35)/T \quad (16)$$

and

$$\log Q_{21,b,OH}^*(T, I = 1\ mol\ kg^{-1}) = (-2182 \pm 153) + (2.42 \pm 0.35)/T \quad (17)$$

respectively. The experimental values of  $\log Q_{21,b,OH}^*$  from this study are systematically higher than Mesmer's potentiometric

values at the same ionic strength. The difference decreases with increasing temperature.

The formation quotients from this Raman study are in very good agreement with those from the conductivity measurements by Ferguson *et al.*,<sup>27</sup> despite the fact that these are very different methods with different assumptions and approximations. We note that these Raman and conductivity measurements were all carried out on  $NaB(OH)_4$  solutions at molalities from  $0.2\ mol\ kg^{-1}$  to  $1\ mol\ kg^{-1}$ , with or without excess NaOH, in which diborate is a major species. The potentiometric measurements by Mesmer *et al.* were carried in  $1\ mol\ kg^{-1}$  KCl solutions with boron concentrations from  $0.03$  to  $0.5\ mol\ kg^{-1}$ , at equilibrium hydroxide concentrations below  $0.01\ mol\ kg^{-1}$ , in which diborate was a minor species. This raises the possi-



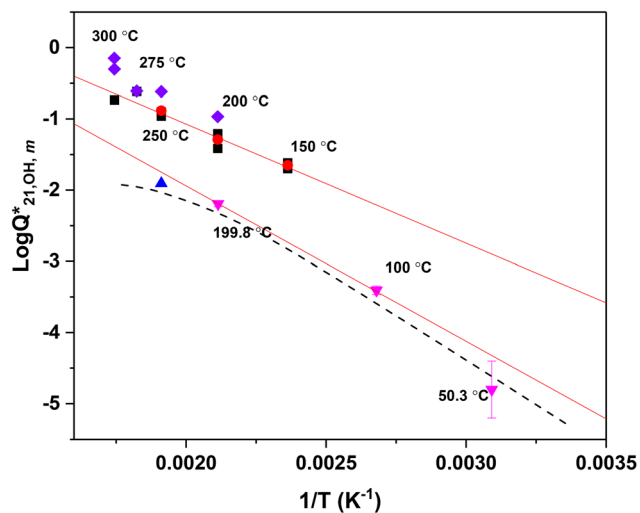


Fig. 7 Plot of  $\log Q_{21,b,OH}^*$  as a function of temperature ( $1/T$ ) at  $p = 20$  MPa from this work and at  $p_{sat}$  from Mesmer's experimental data.<sup>14</sup> The filled black squares (■) and filled red circles (●) represent the experimental  $\log Q_{21,b,OH}^*$  for Solutions 1 and 2, respectively. The pink triangles (▼) are Mesmer's experimental data<sup>14</sup> at 50, 100, and 200 °C. The blue triangle (▲) is the extrapolated value at 250 °C from Mesmer's data by Palmer *et al.*<sup>26</sup> The red lines are the van't Hoff fits to the experimental data from this work and from Mesmer *et al.* at  $l = 1 \text{ mol kg}^{-1}$ , eqn (16) and (17). The purple diamonds (◆) represent the formation constants from conductivity experiments.<sup>26</sup>

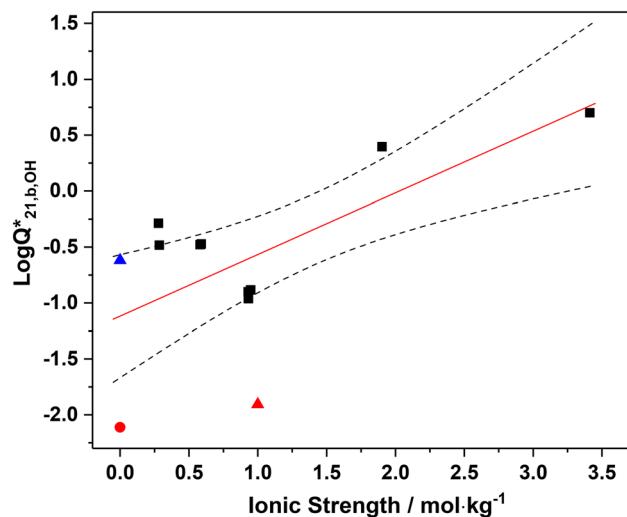


Fig. 8 Plot of  $\log Q_{21,b,OH}^*$  as a function of ionic strength at 250 °C at  $p = 20$  MPa. The black squares (■) are the experimental values from this work. The blue triangle (▲) represents the value from conductivity experiments by Ferguson *et al.*<sup>27</sup> The red triangle (▲) and circle (●) are Mesmer's value of  $\log Q_{21,b,OH}^*$  at  $l = 1 \text{ mol kg}^{-1}$  and  $l = 0$ , extrapolated to 250 °C by Palmer *et al.*<sup>26</sup> The red line is the weighted linear fit to the Raman data, given by eqn (20). The 90% confidence limits for the linear model are shown by the dashed black curves.

bility that a second species, possibly a sodium ion pair, is contributing to the formation constants reported as  $Q_{21,b,OH}^*$  in Table 3 and Fig. 7.

### 5.3. Diborate formation constants

The equilibrium constant for diborate formation,  $K_{21,b,OH}^*$ , is given by the expression:

$$K_{21,b,OH}^* = Q_{21,b,OH}^* \times Q_{\gamma,21,b,OH}^* \quad (18)$$

where the terms

$$Q_{21,b,OH}^* = \frac{m_{[B_2(OH)_7]^-} \cdot m_{OH^-}}{(m_{B(OH)_4^-})^2} \quad \text{and} \quad Q_{\gamma,21,b,OH}^* = \frac{\gamma_{[B_2(OH)_7]^-} \cdot \gamma_{OH^-}}{(\gamma_{B(OH)_4^-})^2} \quad (19)$$

are the formation quotient and activity coefficient quotient, respectively. The composition-dependence of the experimental formation quotients at 250 °C is plotted as a function of the ionic strength in Fig. 8, along with extrapolated values from Mesmer and Palmer *et al.*,<sup>26</sup> and the experimental value from Ferguson *et al.*<sup>27</sup> The plot also shows the results of fitting these values with linear regression, using weighting factors proportional to the total boron concentration of each solution, to yield the expression:

$$\log Q_{\gamma,21,b,OH}^* = \log K_{21,b,OH}^* - aI \quad (20)$$

Where  $\log K_{21,b,OH}^* = -1.20 \pm 0.229$  and  $a = 0.639 \pm 0.134$ . The uncertainties are standard errors.

For consistency with our previous Raman study on the formation constants of triborate,<sup>8</sup> an attempt was made to model the activity coefficient quotient using the same treatment, which is based on the expressions developed by Palmer *et al.*<sup>26</sup> A simple treatment was also used in which the activity coefficients were assumed to depend only on ionic charge, so that:

$$\gamma_{[B_2(OH)_7]^-} = \gamma_{[B(OH)_4]^-} = \gamma_{OH^-} \quad (21)$$

and

$$K_{\gamma,21,b,OH}^* = Q_{\gamma,21,b,OH}^* \quad (22)$$

Neither model predicted the steep ionic-strength dependence of  $\log Q_{21,b,OH}^*$  shown in Fig. 8.

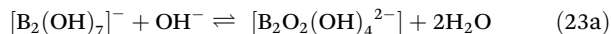
## 6. Discussion

### 6.1. Composition dependence of $Q_{21,b,OH}^*$ and evidence for a second diborate species

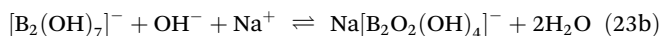
As noted in section 5.2, the formation quotients from this Raman study are in very good agreement with those from the conductivity measurements by Ferguson *et al.*,<sup>27</sup> yet are systematically larger than the potentiometric results reported by Mesmer *et al.*, which were measured in KCl solutions at lower pH. The composition-dependent equilibrium constants plotted in Fig. 8 are consistent with these trends and since the magnitude of  $\log K$  increases with the molalities of  $Na^+$  and  $OH^-$ . Noting that the effect of hydroxide on the equilibrium



between  $[\text{B}_2(\text{OH})_7]^-$  and  $[\text{B}_2\text{O}_2(\text{OH})_4]^{2-}$  is governed by a reaction that directly involves hydroxide,



we speculate that this may be evidence for the presence of  $[\text{B}_2\text{O}_2(\text{OH})_4]^{2-}$ , in the form of a contact ion pair.



The band assignments used to derive the formation quotients reported in Table 3 are based on the computationally predicted vibrational frequencies listed in Table 2 and the assumption that no polyborate species other than  $[\text{B}_2(\text{OH})_7]^-$  and/or  $[\text{B}_2\text{O}(\text{OH})_5]^-$  contributes to the intensity of the  $865\text{ cm}^{-1}$  band. While the computational spectrum of  $[\text{B}_2\text{O}_2(\text{OH})_4]^{2-}$  also showed an intense band near  $865\text{ cm}^{-1}$ , it was rejected on the grounds that no weak band near  $600\text{ cm}^{-1}$  was observed in the experimental spectra. This objection may not be valid in the case of the  $[\text{B}_2\text{O}_2(\text{OH})_4]^{2-}$  contact ion pair. With reference to the structure in Fig. 5, the predicted band near  $865\text{ cm}^{-1}$  is essentially the symmetric B–O(H) stretch, while the band near  $600\text{ cm}^{-1}$  primarily due to the in-plane  $\text{B}_2\text{O}_2$  deformation, with some coupling to the BOH bending mode. The formation of a contact ion-pair with  $\text{Na}^+$  at the ring site would be expected to shift the  $600\text{ cm}^{-1}$  band to higher frequencies and to reduce its intensity.

## 6.2. Uncertainties in the diborate formation quotients

The formation quotients for  $[\text{B}_2(\text{OH})_7]^-$  from this work, plotted in Fig. 7 and 8, show a much larger experimental scatter than has been observed in similar studies using the same methods.<sup>8,9</sup> The uncertainties arise, in part, from the possible contribution of  $\text{Na}[\text{B}_2\text{O}_2(\text{OH})_4]^-$  to the  $865\text{ cm}^{-1}$  band, and in the need to resolve the relative contributions of the diborate species and  $[\text{B}(\text{OH})_4]^-$  to the band at  $745\text{ cm}^{-1}$ . The interpretation is complicated further by the inability of Raman spectroscopy to distinguish between the free borate ion,  $[\text{B}(\text{OH})_4]^-$  and the sodium borate ion-pair,  $[\text{NaB}(\text{OH})_4]^{0,9,12}$ . Calculations based on the ion-pair formation constants reported by Arcis *et al.*<sup>28</sup> suggest that the majority of the aqueous borate species at these concentrations may in fact be solvent-separated ion pairs. As a result, the bands at  $745$  and  $865\text{ cm}^{-1}$  may also include contributions from sodium ion pairs with diborate,  $[\text{NaB}_2(\text{OH})_7]^{0,}$  which presents a similar hydroxyl-rich surface to the surrounding hydration shell. Accurate measurements over a much wider range of solution compositions and the full temperature range would be needed to resolve these issues.

## 6.3. Impact on chemical speciation models for aqueous boron

The complex aqueous speciation chemistry of boron is of critical interest to the nuclear industry, and is relevant to a number of other sectors including geology/geochemistry, natural waters, and various chemical and industrial processes. In the nuclear industry, two major software packages are used for modeling chemical speciation in reactor coolant. These are

based on different chemical equilibrium models and independent critically evaluated thermodynamic data.<sup>26,29</sup> The Electric Power Research Institute's (EPRI) chemical modelling software, MULTEQ, which is distributed as part of ChemWorks Tools (v.7.0), makes use of a "model species" activity coefficient treatment, the Meissner equation,<sup>30</sup> and is most accurate at ionic strengths below  $1\text{ mol kg}^{-1}$ . The OLI Analyzer Studio 9.2.1 software (OLI Systems Inc.), is based on standard-state properties from the Helgeson–Kirkham–Flowers (HKF) equation<sup>31,32</sup> and the mixed-solvent electrolyte (MSE) model for excess properties from Anderko *et al.*<sup>33</sup> MULTEQ and OLI have adopted different chemical formulations for the diborate ion. MULTEQ defines the diborate ion as  $[\text{B}_2(\text{OH})_7]^-$ , while OLI Studio defines diborate as the condensed species  $[\text{B}_2\text{O}(\text{OH})_5]^-$ . It is also important to note that MULTEQ uses the equation reported by Marshall and Franck<sup>34</sup> for the ionization constant of water,  $K_w$ , while OLI uses the expression derived for the HKF model.<sup>31,32</sup> The critically-evaluated values for speciation, phase equilibria, and other thermodynamic properties of boron-containing systems in the OLI Analyzer Studio 9.2.1 have been reported by Wang *et al.*<sup>17</sup>

A revision to the databases of both MULTEQ and OLI Studio to include the new diborate formation quotients from this study, should include the results from our earlier work on the formation constants for the triborate ion.<sup>8</sup> The spectra reported for the more acidic boric acid/borate solutions in the triborate study, impose an upper limit on the formation constant of  $[\text{B}_2(\text{OH})_7]^-$  because the presence of diborate as an equilibrium species at concentrations above the detection limit of  $0.1\text{ mol kg}^{-1}$  would have been observable as a weak band at  $865\text{ cm}^{-1}$  when, in fact, no such bands were seen. This upper limit is more consistent with the formation constant reported by Palmer, than with the results in Table 3 and Fig. 7, consistent with presence of a second diborate species as discussed above.

The implication of these results for model database development are twofold. First, the experimental results demonstrate that the  $[\text{B}_2(\text{OH})_7]^-$  ion is a significant species that may form under 'hideout'-type conditions in nuclear power reactors, and in hydroxide-rich borate solutions at elevated temperatures in other chemical and industrial processes. Second, the divalent ion  $[\text{B}_2\text{O}_2(\text{OH})_4]^{2-}$  may also be present as an ion pair with alkali metal ions and may also affect boron hideout chemistry. Finally, as noted above, the Raman spectra of borate solutions in our recent triborate publication show that these diborate species are not expected to present at high enough concentrations to significantly affect the bulk primary coolant chemistry in PWR nuclear reactors.

## 7. Conclusions

The presence of a previously unreported equilibrium aqueous boron species has been identified by Raman spectroscopy in  $\sim 1\text{ mol kg}^{-1}$   $\text{NaB}(\text{OH})_4$  solutions at temperatures from  $150$  to  $300\text{ }^\circ\text{C}$  and  $20\text{ MPa}$ . The most plausible polyborate species



structures were examined computationally, as well as by observing the effects of excess  $\text{Li}^+$ ,  $\text{Na}^+$ , and  $\text{OH}^-$  ions on the experimental Raman spectra. The experimental results, together with the computational frequency predictions, indicate that the most likely candidate for the boron species are  $[\text{B}_2(\text{OH})_7]^-$  and/or  $[\text{B}_2\text{O}(\text{OH})_5]^-$ , which is consistent with Mesmer's potentiometric studies.<sup>14</sup> The DFT-predicted frequencies suggest that  $[\text{B}_2(\text{OH})_7]^-$  is the more likely candidate for the major species. The Raman scattering coefficients, equilibrium concentrations, and formation constants were calculated from three different modelling approaches based on peak area and mass balance. The models had charge-balance discrepancies for solutions in which hydroxide concentrations were calculated using the boric acid ionization constants and activity coefficient model reported by Palmer *et al.*,<sup>26</sup> however, Model 2 yielded constant scattering coefficients within the experimental uncertainties, while other models did not. As a result of this finding and of the DFT-predicted vibrational spectra, the formation quotients for  $[\text{B}_2(\text{OH})_7]^-$ ,  $Q_{21,\text{b,OH}}^*$ , calculated from the equilibrium concentrations determined using Model 2 are most consistent with the computational and Raman results.

The formation quotients for  $[\text{B}_2(\text{OH})_7]^-$ ,  $Q_{21,\text{b,OH}}^*$  from both models showed inconsistencies that varied with temperature and composition. These may be due to the presence of another equilibrium species at temperatures above  $\sim 150$  °C, and/or a strong activity coefficient effect that is not well represented by the models used in this study. If present, the most likely candidate for a second unknown species is the divalent diborate ion pair,  $\text{Na}[\text{B}_2\text{O}_2(\text{OH})_4]^-$ . The detection limits observed for the Raman spectra of boric-acid rich solutions at these temperatures<sup>8,9</sup> place an upper limit on the standard-state formation constants of  $[\text{B}_2(\text{OH})_7]^-$  at all the temperatures studied.

## Author contributions

Swaroop Sasidharanpillai: data curation, formal analysis, investigation, methodology, validation, writing – original draft, writing – review & editing. Jenny S. Cox: data curation, investigation, methodology, formal analysis, validation, writing – original draft, writing – review & editing. Cory C. Pye: investigation, formal analysis, methodology, writing – original draft. Peter R. Tremaine: conceptualization, formal analysis, methodology, project administration, supervision, validation, visualization, funding acquisition, writing – original draft, writing – review & editing, resources.

## Conflicts of interest

There are no conflicts of interest to declare.

## Acknowledgements

This research was supported by the Electric Power Research Institute (EPRI Project 10006135) and by the Natural Science

and Engineering Research Council of Canada (NSERC) Discovery Grant RGPIN-2017-05894. The authors thank OLI Systems Inc. (Edison, N.Y.) for donating their software package OLI Analyzer Studio 9.2.1 to the Hydrothermal Chemistry Laboratory at the University of Guelph. Dr Peiming Wang and Dr Andrzej Anderko (OLI) provided help and advice with the database and software, and insightful input to the diborate ion-pair discussions. We are grateful to Mr Case Gielen (Chemistry and Physics Machine Shop) who constructed the titanium flow cell, and Mr Ian Renaud (Chemistry Electronics Shop) who constructed the temperature controller. The authors also express their gratitude to Dr Daniel Wells (EPRI) for providing technical advice, many fruitful discussions, and steadfast support on this project. We are also grateful to Dr Shirley Dickinson and Dr Hugues Arcis (National Nuclear Laboratory, UK) and Dr Jane Ferguson (St Mary's University, NS) for many suggestions and technical discussions related to polyborate thermodynamics. Dr Matt Wolf provided input on earlier versions of the manuscript. The authors thank ACEnet for computational resources. We also thank the reviewers for insightful comments on the original manuscript and for suggesting the  $\text{D}_2\text{O}$  experiments, both of which led to worthwhile improvements in the final paper.

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