Charge delocalization and aromaticity of doubly reduced double-walled carbon nanohoops†

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Cycloparaphenylenes (CPPs) exhibit selective host capabilities, featuring the ability to incorporate smaller CPPs to form double-walled host–guest complexes. Moreover, CPPs can also be stabilized by global aromaticity under twofold oxidation or reduction, involving electronic conjugation along with the overall structural backbone. Herein we explore the structural modifications, bonding, electron delocalization and magnetic properties of doubly reduced double-walled CPP complexes with DFT methods, in the isolated and aggregate \([n + 5]\text{CPP} \supseteq [n]\text{CPP}^2\) \((n = 5–8)\) species. Our results show that the hosts undergo structural, bonding and delocalization deformations towards quinoidal configurations and exhibit global long-ranged shielding cones similar to global aromatic free dianionic CPPs, accounting for charge delocalization on the outer nanohoops, whereas the guests preserve local aromatic benzenoid configurations, resulting in global and local aromatic circuits within the host–guest aggregate. This observation suggests that in multi-layered related species electronic delocalization will be retained at the outer structural surface. The aromaticity of the hosts is manifested in the strong upfield shifts of the guests’ \(^1\text{H}-\text{NMR}\) signals. Hence, CPP complexes can be extended to doubly reduced species stabilized by global host aromaticity expanding our understanding of doubled-walled nanotubes at the nanoscale regime.

Introduction

Macroyclic aromatic carbon structures with curved \(\pi\)-surfaces exhibit exceptional structural and electronic properties with flourishing applications in nanomaterials, organic–electronic devices and supramolecular chemistry. \(^1\)–\(^9\) Among such structures, cycloparaphenylenes (CPPs), also called nanohoops, are a unique class of polyyclic aromatic hydrocarbons (PAHs) consisting of para-connected benzene rings forming an in-plane macroyclic \(\pi\) system. They can be conceived as the smallest unit of armchair carbon nanotubes (CNTs), embodying the prospect for “bottom-up” organic synthesis of such single-walled nanomaterials. \(^10\)–\(^13\) Due to the pioneering work of Jasti, \(^14\)–\(^17\) Itami \(^11\)–\(^13\), \(^18\), \(^19\) and Yamago \(^20\)–\(^23\) groups, among others, \(^24\), \(^25\) over the last decade, the selective synthesis of numerous \([n]\text{CPPs}\) on a gram-scale is now attainable, allowing for further exploration of their chemistry.

One of the remarkable properties of \([n]\text{CPPs}\) is the large interior space of the radial \(\pi\)-system which is capable of selectively binding smaller \(\pi\)-structures stabilized by \(\pi-\pi\) interactions, establishing them as exemplary hosts with adjustable selectivity according to the number of benzene rings. Thus, numerous host–guest complexes with \([n]\text{CPPs}\) serving as hosts have been experimentally characterized or theoretically predicted in recent years incorporating fullerences, \(^16\), \(^26\)–\(^33\) planar and curved PAHs \(^34\)–\(^36\) or even smaller CPPs \(^37\), \(^38\) as guests. The latter, termed “Russian doll” \(^39\) or “Planetary orbit” \(^40\) complexes, can be conceived as the shortest double-walled carbon nanotubes (DWCNTs). \(^37\) Initially they were theoretically investigated by Fomine \(^39\) and Bachrach \(^40\) who predicted that \([n]\text{CPPs}\) can be selectively bound by \([n + 5]\text{CPPs}\), forming \([n + 5]\text{CPP} \supseteq [n]\text{CPP}\) complexes, experimentally confirmed in 2017 by Yamago with NMR spectroscopy for \(n = 5–8\) and \(^10\), \(^37\) while Wang et al. recently prepared the \([12]\text{CPP} \supseteq [6]\text{CPP}\) complex, \(^38\) enabling the investigation of DWCNTs at the molecular level.

\([n]\text{CPPs}\) display a local aromatic character of each benzene ring and they can be described as a collection of Clar’s \(\pi\)-sextets, \(^41\) while the whole macrocycles can be regarded as non-aromatic benzenoid structures. \(^42\)–\(^46\) However, upon two-fold oxidation \(^17\)–\(^50\) or reduction \(^51\)–\(^53\) the \([n]\text{CPPs}\) turn on global in-plane macrocyclic aromaticity adopting a quinoidal structural configuration. Thus, the doubly charged species are able to sustain global macrocyclic diatropic currents under the effect of a perpendicular external magnetic field. \(^32\) In turn,
the π currents produce a globally induced magnetic field which is manifested with global long-ranged shielding cones providing reasonable interpretation of the 1H-NMR chemical shift variations in the aromatic macrocycles, as well as in host–guest aggregates. Hence, charged nCPPs stabilized by global aromaticity are of special interest in redox chemistry, with promising potential applications in organic electronic devices, energy storage materials and supramolecular chemistry, paving the way for novel host–guest complexes with unique selective guest binding capabilities.

Herein we set out to explore doubly reduced double-walled nanohoop complexes [n + 5]CPP | [n]CPP\(^{2–}\) (n = 5–8) by means of density functional theory (DFT) focusing on geometrical deformation, bonding, electron delocalization, induced magnetic fields and 1H-NMR chemical shifts, in order to investigate the charge delocalization and aromaticity of these complexes, as well as to provide useful information for experimental characterization. We show that the charge is exclusively delocalized on the hosts enabling a global aromatic character of the outer nanohoops, resulting in strong upfield chemical shifts of the strongly shielded guests, which tend to preserve their local benzenoid structures. The variations in host aromaticity affect the 1H-NMR chemical shifts of the inner guests, which are strongly shifted upfield.

Computational methods

Geometry optimizations were performed using Gaussian\(^6^0\) employing Grimme’s standalone pure functional B97D3 with D3BJ dispersion corrections, along with the all-electron triple-ζ basis set with one polarization function (def2TZVP). B97D3 was chosen because it has been shown that it performs with very good agreement to CCSD(T) or other hybrid functionals for nonbonded π–π interactions of polycyclic hydrocarbons and CPP complexes, providing accurate results with reduced computational cost. The stability of the wavefunctions of charged complexes was tested using stable = opt keyword. All structures were verified as local minima on the potential energy surface by analytical frequencies calculations which yielded real vibrational frequencies. Molecular orbitals’ energy levels were recalculated with the oB97XD\(^{6^7}\) functional with the same basis set, because pure DFT functionals underestimate the HOMO–LUMO gaps, whereas hybrid functionals provide more accurate predictions.

Chemical shielding calculations were performed with the ADF2019\(^6^9,7^0\) program. NICS calculations at the centers of the complexes were computed at the PBE/TZ2P level. 1H-NMR chemical shifts were calculated using the hybrid PBE0 functional\(^7^1\) and triple-ζ Slater basis set with one polarization function TZP, using benzene as the reference (\(\delta_{\text{benzene}} = 7.36 \text{ ppm}\))\(^7^2\) according to the formula:

\[
\delta_{\text{calc}} = \sigma_{\text{benzene}} - \sigma_{\text{calc}} + \delta_{\text{benzene}}
\]

The induced magnetic field was derived from chemical shielding tensor calculations within the GIAO formalism according to the formula:

\[
B_{ij}^{\text{ind}} = \sigma_{ij}^{\text{GIAO}} B_{ij}^{\text{ext}} (i, j = x, y, z).
\]

The chemical shieldings were calculated in square grids of points with edges of 17.5 Å and step size 0.5 Å employing the Perdew–Burke–Ernzerhof (PBE) functional\(^7^3\) with the double-ζ stater basis set with one polarization function (DZP). Dissection of the 2D induced magnetic field to π and σ + cores, as well as host–guest π-contributions were achieved with the natural chemical shielding (NCS) approach\(^7^5\) using the NBO6.0 program,\(^7^6\) taking into consideration the contributions of the respective localized natural bond orbitals (NBO) with a distinct π or σ character. Moreover, CMO analysis of the induced magnetic field was performed at the same level, taking into consideration the magnetic response of frontier canonical orbitals. Still, the calculation and dissection of \(\mu^{\text{ind}}\) in 3D is computationally rigorous for large systems and alternatively the pseudo–π approach has been employed for the 3D visualization of the π response by representing the π orbitals with the corresponding σ orbitals of a hydrogen molecular model with the geometry of the carbon skeleton.\(^7^7–7^9\) Additional calculations of the total full electron 3D magnetic response were carried out with Gaussian at the PBE/SVP level and mapped visualizations on VDW surfaces were made with the VMD program.\(^8^0\) Input preparation, output processing, NBO and CMO dissection and 2D/3D visualization of the induced magnetic field were performed with our custom PyMAF program.\(^8^1\)

Mayer bond orders\(^8^2,8^3\) and 6-center Delocalization Index\(^8^4\) (MCI) were calculated with the Multiwfn program.\(^8^5\) MCI was calculated with the oB97XD functional adopting the pseudo–π approach\(^8^6,8^7\) within the fuzzy-atom space (FAS) partitioning, using modified parameters to minimize errors in the atomic overlap matrix.

Results and discussion

Geometrical characteristics and local electron delocalization

The optimized structures of [n + 5]CPP | [n]CPP\(^q\) (n = 5–8, q = 0, 2+, 2–) complexes are presented in Fig. 1 and Fig. S1 (ESI). All dianionic ground state complexes were found to have stable closed-shell restricted wavefunctions. On the other hand, the ground states of the dicaticionic complexes were found to be open-shell triplet states. A characteristic structural feature of such complexes is the inclination angle between the host and the guest. According to the literature, when the inclination angle is zero (0°) adopting a parallel orientation between the host and the guest, the complex is termed “Russian doll”, whereas for non-zero inclination angles the complex is termed “Planetary orbit”.\(^3^7,3^9,4^0\) The inclination angles are estimated from the fitted planes of host and guest ipso carbons, as described by Bachrach.\(^4^0\) Our calculations detected three stable configurations for neutral [10]CPP | [5]CPP with inclination angles of 0°, 14.5° and 50.8°, where the Russian-doll configuration is the global minimum, as it was found to be more stable by 3.3 kcal mol\(^\text{–1}\) and 1.9 kcal mol\(^\text{–1}\) with respect to the planetary orbit configurations respectively. For the dianion [10]CPP | [5]CPP\(^2–\) only a planetary orbit configuration was
located with an inclination angle of 13.8°. For the neutral higher complexes \((n = 6, 7, \text{ and } 8)\) only planetary orbit configurations were located, where the inclination angles computed at the B97D3/def2TZVP level of theory \((32.7°, 26.4° \text{ and } 23.2° \text{ for } n = 6, 7, \text{ and } 8 \text{ respectively})\) are in good agreement with those reported by Bachrach\(^{40}\) at the CPCM(THF)/oB97X-D/6-31G(d) level. For the dianions with \(n = 7\) and \(8\) both Russian-doll and planetary orbit configurations were found with the former being more stable by \(0.36 \text{ kcal mol}^{-1}\) and \(1.61 \text{ kcal mol}^{-1}\) for \(n = 7\) and \(8\) respectively. For the dications with \(n = 6, 7\) and \(8\) only planetary orbit configurations were located with similar small inclination angles \((10.5°, 10.3° \text{ and } 10.8° \text{ for } n = 6, 7, \text{ and } 8 \text{ respectively})\), whereas for \(n = 5\) a Russian-doll configuration was located.

The characteristic geometric modification of global aromatic doubly charged \([n]\text{CPPs}\) \((q = 2+, 2−)\) is a shift towards the quinoidal structure compared to the local aromatic benzenoid structure of the neutral counterparts (Fig. 2a), primarily expressed with the shortening of \(C_{\text{ipso}}−C_{\text{ipso}}\) bonds and secondary with the shortening of \(C_{\text{ortho}}−C_{\text{ortho}}\) bonds, as well as the elongation of \(C_{\text{ipso}}−C_{\text{ortho}}\) bonds. The trend of \(C_{\text{ipso}}−C_{\text{ipso}}\) modification with regard to the nanohoop size and the charge of both free and complexed \([n]\text{CPPs}\) is presented in Fig. 2b, while the optimized averaged C–C bond lengths are given in Table S1 (ESI\(^†\)). For free \([n]\text{CPPs}\) both the dianions and the dications undergo the same shortening of \(C_{\text{ipso}}−C_{\text{ipso}}\) bond lengths characteristic of quinoidal configuration, which decreases as the size of the nanohoop increases, from \(0.05 \text{ Å} \text{ (} n = 5 \text{)}\) to \(0.01 \text{ Å} \text{ (} n = 13 \text{)}\). Upon neutral complex formation, the C–C bond lengths of both the hosts and the guests remain essentially unchanged compared to free neutral molecules. However, variations are expected and observed for the doubly charged complexes. The guests in the dianions \((n = 5−8)\) retain very similar bond lengths with the neutral complexes. In contrast, the hosts in the dianions \((n = 10−13)\) undergo the same shortening with the quinoidal free dianions. On the other hand, in the dications the \(C_{\text{ipso}}−C_{\text{ipso}}\) lengths of both the guests and the hosts are shortened halfway towards the quinoidal free dications.

To obtain more insight into the bonding characteristics we computed the Mayer Bond Orders (MBO) given in Table S3 (ESI\(^†\)), while the trend of \(C_{\text{ipso}}−C_{\text{ipso}}\) bonds is presented in Fig. 2d. The MBOs of \(C_{\text{ipso}}−C_{\text{ipso}}\) of neutral free molecules vary in the range of \(1.00 \pm 0.02\) and slightly decrease with increasing size, whereas for the charged molecules the MBO values are distinctly higher by an average value of \(\sim 0.10\) and decrease...
more sharply with increasing size. The MBO values of neutral complexes, as well as the guests of dianionic complexes are very close to the corresponding free molecules, denoting the persistence of the benzenoid character. However, the guests of dicaticionic complexes present higher MBO values than their neutral and dianionic counterparts. In contrast, the hosts of both dicaticionic and dianionic complexes display similar MBOs with the free dianions, denoting a shift towards quinoidal structures.

Another characteristic structural modification of the doubly charged \([n]\text{CPP}\) species, is the decrement of the dihedral angles between adjacent phenylenes, compared to the neutral counterparts, tending toward a vertical orientation with respect to the macrocycle plane.\(^{51}\) The trends and values of the averaged optimized dihedral angles are presented in Fig. 2b and Table S2 (ESI†) respectively. Concerning the neutral complexes, both hosts and guests display a similar small decrement of an averaged \(4^\circ\) in their dihedral angles compared to the corresponding free \([n]\text{CPP}\), except for the guest \([5]\text{CPP}\) which displays a negligible angle in the Russian-doll configuration (0.5°) which increases to 11.9° in the planetary orbit configuration. The guests of the dianions display a very small decrement in the dihedral angles compared to the guests of the neutral complexes \((\Delta = 1.8^\circ, 4.5^\circ \text{ and } 1.6^\circ \text{ for planetary orbit } n = 6, 7 \text{ and } 8 \text{ respectively}), \Delta = 1.5^\circ \text{ and } 0.1^\circ \text{ for Russian-dolls with } n = 7 \text{ and } 8, \text{ respectively})\), while in the dications the decrement is more pronounced \((\Delta = 12.0^\circ, 13.2^\circ \text{ and } 7.9^\circ \text{ for } n = 6, 7 \text{ and } 8 \text{ respectively})\). In contrast, the hosts are much more affected by the double charge, leading to similar dihedrals in the dianions and the dications compared to the corresponding free charged \([n]\text{CPP}\).

The preceding analysis of geometrical and bonding characteristics reveals a quinoidal character for the hosts of the doubly reduced complexes suggesting a global aromatic character, whereas the guests retain their benzenoid structures implying the persistence of local aromaticity. On the other hand, in the triplet state dications both the hosts and the guests are geometrically affected to a lesser degree towards a quinoidal character. Hereafter we will focus on the closed-shell dianionic species, since investigation of the open-shell aromaticity of nanohoops requires a specialized approach\(^{89}\) which is out of the scope of the current paper.

It has been shown by geometric, magnetic and electron delocalization criteria that local aromaticity decreases in the presence of global aromaticity in CPPs.\(^{45}\) To evaluate the variations of electron delocalization and local aromaticity we calculated the Multicenter Delocalization Index (MCI) for the six-membered rings. The MCI values for all rings are given in Table S4 (ESI†) and the trends are presented in Fig. 2e. It is evident that electron delocalization of phenylene rings remains unaffected upon neutral complex formation and is invariant to the macrocycle size. On the other hand, global aromatic free dianions display substantially reduced delocalization of phenylenes, which increases with macrocycle size. The trends of the MCI for the hosts and guests of the dianionic complexes are very similar to those of the \(C_{ipso} - C_{ipso}\) lengths. For the guests the MCI values are in the range of neutral counterparts. In contrast the hosts display MCI values very close to the free dianions. Hence the guests of the dianions preserve the local aromatic character of neutral counterparts, whereas the hosts adopt the reduced local aromatic character of global aromatic free dianions.

Finally, the planetary orbit and Russian doll configurations for \(n = 7\) and 8 display similar or identical values concerning structural, bonding and delocalization indices, denoting that the configuration of the complexes does not affect the aromaticity of the system.

**Induced magnetic fields of \([5]\text{CPP}\) and \([10]\text{CPP}\) \((q = 0, 2 –)\)**

When an aromatic ring, such as benzene, is placed inside a uniform magnetic field with the ring plane oriented perpendicular to the field (tilt angle \(0^\circ\)), then the delocalized \(\pi\) electrons induce a clockwise ring current, which subsequently induces a secondary magnetic field forming a long-ranged shielding cone above and below the ring, complemented by a weaker torus-shaped deshielding zone outside the ring plane. This out-of-plane response can be visualized as 3D isosurfaces or 2D maps of the \(z\) component of the induced magnetic field \(B^\text{ind}_z\), which is equivalent to NICS\(_{zz}\).\(^{90,91}\) As the tilt angle increases to a final parallel orientation of the ring (tilt angle \(90^\circ\)), the in-plane response \((B^\text{ind}_x \text{ or } B^\text{ind}_y)\) forms a short-ranged shielding area surrounding the ring, while the weak paratropic zone always remains outside the ring.\(^{45,58}\) Furthermore, the isotropic response \(B^\text{ind}_{iso}\), which is equivalent to iso-chemical shielding surfaces (ICSS),\(^{92}\) accounts for the averaged orientation to the external field due to molecular tumbling and can be directly related to \(^1\)H-NMR experiments. However, in curved hydrocarbons the \(\sigma\) electrons can contribute significantly to the shielding\(^{93}\) and therefore only the \(\pi\) contributions must be considered to evaluate the aromatic character of such systems. Hereafter we explore the \(\pi\) magnetic response of free neutral and doubly reduced \([5]\text{CPP}\) and \([10]\text{CPP}\) molecules and extend our investigation to \([10]\text{CPP} \supseteq [5]\text{CPP}\) and higher complexes.

The magnetic response of the \(\pi\) system of \([10]\text{CPP}\) in terms of the induced magnetic field \(B^\text{ind}_{z(\text{iso})}\) \((i = \text{iso}, z, x)\) is shown in Fig. 3 and it is depicted with isosurfaces calculated with the pseudo-\(\pi\) model and as 2D maps derived with all electron calculations and dissected to \(\pi\) contributions employing NBO analysis. The isotropic response \(B^\text{ind}_{z(\text{iso})}\) (Fig. 3a) displays local shielding areas depicted with a blue color surrounding each phenylene ring, representing the local aromatic character and can be inspected by inspecting the out-of-plane response and the in-plane response \(B^\text{ind}_{z(x)}\). The out-of-plane response \(B^\text{ind}_{z(x)}\) (Fig. 3b) displays local short-ranged shielding areas in the vicinity of each phenylene ring, because the external field is parallel to the rings,\(^{58}\) while a weak paratropic area, depicted with yellow in the 2D map, is observed inside the macrocycle (NICS\(_{zz} = 4.55 \text{ ppm}\)) as a result of the cumulative effect of weak local paratropic contributions of each ring. The in-plane response \(B^\text{ind}_{x(x)}\) (Fig. 3c) displays local long-ranged shielding cones at the phenylene rings that are oriented perpendicular to the applied field (tilt angle \(0^\circ\)), while the shielding cones are...
contracted as the tilt angle increases and the rings become parallel to the applied field. For the dianion [10]CPP−, the in-plane response of $B_{\text{ind}}^{\text{N(2)}}$ (Fig. 3f) has identical shape with the neutral and slightly contracted extension, indicating that the local aromatic character of each ring under a parallel orientation of the external field is preserved regardless of the charge state. However, the out-of-plane component $B_{\text{ind}}^{\text{z}}$ of the macrocycle (NICS$_{zz}$ = −24.2 ppm), representing global macrocyclic aromaticity. As a result, the isotropic response $B_{\text{ind}}^{\text{ISO}}$ (Fig. 3d) is dominated by the out-of-plane component and displays a weaker global shielding cone (NICS$_{\text{iso}}$ = −7.2 ppm).

The same behavior is observed for [5]CPP (Fig. S2, ESI) with local shielding cones on phenylene rings in the neutral state and a global long-ranged shielding cone for the out-of-plane response $B_{\text{ind}}^{\text{z}}$ of the dianion (NICS$_{zz}$ = −31.5 ppm), leading to a global shielding isotropic response (NICS$_{\text{iso}}$ = −7.9 ppm). However, the out-of-plane response $B_{\text{ind}}^{\text{z}}$ of neutral [5]CPP displays a short-ranged global deshielding cone (NICS$_{zz}$ = 23.8 ppm) leading to weak global paratropicity of the isotropic response $B_{\text{ind}}^{\text{ISO}}$ (NICS$_{\text{iso}}$ = 7.9 ppm). Although a global deshielding cone is a characteristic feature of antiaromatic molecules, in this case it is attributed to the cumulative paratropic effect of each ring inside the macrocycle, which is enhanced compared to the corresponding response of [10]CPP due to the small diameter of [5]CPP.

### Induced magnetic fields of [n + 5]CPP–[n]CPP complexes

The out-of-plane response of neutral and doubly reduced complexes [10]CPP–[5] is shown in Fig. 4a and b. The magnetic

![Fig. 3](image-url) Isosurfaces of pseudo-$\pi$ and contour maps of $\pi$ contributions to the isotropic ($B_{\text{ind}}^{\text{ISO}}$), out-of-plane ($B_{\text{ind}}^{\text{z}}$) and in-plane ($B_{\text{ind}}^{\text{x}}$) components of the induced magnetic field of neutral [10]CPP (a–c) and dianion [10]CPP− (d–f). Isosurface isovalue ±5 ppm. Blue: shielding; red: deshielding.

![Fig. 4](image-url) $\pi$ contributions to the out-of-plane component of the induced magnetic field, $B_{\text{ind}}^{\text{z}}$ of [10]CPP–[5]CPP (q = 0, 2−) complexes (a and b) and NBO-dissected contributions of hosts (c and d) and guests (e and f). Isosurface isovalue ±5 ppm. Blue: shielding; red: deshielding.
response of neutral \([10]\text{CPP} \supset [5]\text{CPP}\) (Fig. 4a) displays local shielding cones on phenylene rings and a global paratropic cone inside the guest (NICS\(_{zzz}\) = 35.0 ppm and NICS\(_{nnn}\) = 12.6 ppm) showing that the local aromatic character of the host and the guest is precisely retained, as the magnetic response of the complex is the sum of the magnetic response of neutral \([10]\text{CPP}\) and \([5]\text{CPP}\) (Fig. S4, ESI†). On the other hand, the out-of-plane response of the dianion (Fig. 4b) displays a global long-ranged shielding cone at the host which diminishes and becomes weakly paratropic inside the guest (NICS\(_{zzz}\) = 3.6 ppm). Accordingly, the isotropic response (Fig. S3a and b, ESI†) displays weak but long-ranged global shielding cones at the host and very weak paratropicity inside the guest (NICS\(_{zzz}\) = 2.0 ppm). This behavior clearly suggests that under twofold reduction the host becomes aromatic, while the guest seems to retain its local aromatic character, contributing paratropically at the center of the macrocycle. Otherwise, if the guest was aromatic, then the diatropicity would be greatly enhanced at the vicinity of the inner nanohoop. Hence, the extra charge appears to be delocalized mainly on the host \([10]\text{CPP}\).

The magnetic response of the complex is the cumulative result of host and guest responses. Hence, to gain insight into the origin and the variations in aromaticity, we dissected the total \(\pi\) response of each complex to distinct responses of host and guest macrocycles, by selecting the respective \(\pi\)-NBO (or \(\sigma\)-NBO for the pseudo-\(\pi\) model) contributions to chemical shielding, since each NBO is localized on a specific macrocycle in the complex. The results of NBO host–guest dissection are presented in Fig. 4c–f for the out-of-plane response and in Fig. S3c–f (ESI†) for the isotropic response. Furthermore, we compare the \(B_{n}^{\text{ind}}(0)\) of each macrocycle in the complexes, as well as the total \(\pi\) response, with the \(B_{n}^{\text{ind}}(0)\) of the corresponding free neutral or doubly reduced \([10]\text{CPP}^{2−}\) and neutral \([5]\text{CPP}\), as well as their cumulative result, keeping the geometries of the macrocycles as they have been deformed in the complex (Fig. S3 and S4, ESI†). For the neutral complex the dissected magnetic responses of the host and the guest (Fig. 4c and e) are identical to free neutral \([10]\text{CPP}\) and \([5]\text{CPP}\) respectively, as expected. Accordingly, the total \(\pi\) magnetic response of the neutral complex is identical to the cumulative result of \([5]\text{CPP} + [10]\text{CPP}\) (Fig. S4, ESI†). On the other hand, the host of the dianion (Fig. 4d) induces a strong shielding cone comparable to free \([10]\text{CPP}^{2−}\), sustaining a \(B_{n}^{\text{ind}}(0)\) value of \(−4\) ppm at 10.2 Å above the center, while for the free \([10]\text{CPP}^{2−}\) this diatropicity is found at 11.0 Å. Moreover, the paratropic response of the guest (Fig. 4f) is slightly weaker than free \([5]\text{CPP}\). Accordingly, the total \(\pi\) response of the dianion \([10]\text{CPP} \supset [5]\text{CPP}^{2−}\) is only marginally weaker than the cumulative result of \([5]\text{CPP} + [10]\text{CPP}^{2−}\) (Fig. S5, ESI†).

The preceding analysis of \([10]\text{CPP} \supset [5]\text{CPP}\) showed that the pseudo-\(\pi\) model provides a very accurate qualitative picture of the \(\pi\) magnetic response of the complexes, which is consistent with all-electron calculations of the total \(\pi\) response, as well as with the NBO dissection to host–guest contributions. Hence, we calculated the pseudo-\(\pi\) magnetic response of the higher complexes \([n + 5]\text{CPP} \supset [n]\text{CPP} (n = 6–8)\) and dissected the complex response to host–guest contributions, as shown in Fig. 5. The higher complexes show the same magnetic behavior with \([10]\text{CPP} \supset [5]\text{CPP}, with local shielding cones at the neutral states, and global shielding cones on the hosts of the doubly reduced complexes. The guests of the dianions display local shielding cones on phenylene rings, preserving the local aromatic character.

**CMO analysis**

According to CMO analysis, the variations of the magnetic response can be interpreted by analyzing the contributions of frontier orbitals.\(^{56,57}\) In general, the highest lying orbitals shape the overall magnetic response via paratropic contributions induced from occupied-to-virtual MO rotational excitations, whereas the lower orbitals induce a diatropic response. The excitations obey the selection rules and the magnitude of the paratropic response depends on the energy gap and the overlap of the respective rotated orbitals.\(^{57,94}\) In antiaromatic molecules the HOMO \(\rightarrow\) LUMO rotational excitation is symmetry allowed resulting in the characteristic strong paratropicity, whereas in aromatic molecules these excitations are usually forbidden. In contrast to planar PAHs, \([n]\text{CPPs}\) exhibit increasing HOMO–LUMO gaps with the number of rings, which is also evident in neutral complexes, where the HOMOs are localized on the guest (Fig. S6, ESI†). In the doubly reduced complexes, the electronic structure is modulated such that the HOMOs are localized on the host, leading to a drastic decrease of the
HOMO–LUMO gap, which in contrast to neutral species decreases with increasing size (Fig. 6). The small HOMO–LUMO gaps are compatible with antiaromatic molecules, but in such electronic configurations the strong paratropic response of HOMOs is cancelled due to their nodal structure which forbids the respective HOMO → LUMO rotational excitation by symmetry. Accordingly, in the dianions the major contributing rotational allowed excitation is the HOMO/C0 → LUMO, displaying a weaker magnetic response with regard to the neutral counterparts due to a smaller overlap.

In Fig. 7 the magnetic response of frontier orbitals and the corresponding rotational excitations of [10]CPP ↔ [5]CPP complexes are presented. In neutral [10]CPP ↔ [5]CPP the HOMO and LUMO are localized exclusively on the guest, whereas the HOMO−1 and LUMO+1 are on the host. These orbitals correspond to the HOMO and LUMO of free [5]CPP and [10]CPP respectively and therefore they display similar paratropic magnetic responses. Specifically, a strong global deshielding cone is induced on the guest from HOMO−LUMO excitation (NICS_{zz}^{HOMO−LUMO} ≈ 53 ppm), whereas the HOMO−1 → LUMO+1 excitation induces a global deshielding cone on the host (NICS_{zz}^{HOMO−1 → LUMO+1} ≈ 16 ppm, Fig. 7a). In the doubly reduced complex the HOMO → LUMO excitation is forbidden by symmetry and the dianion presents diminished paratropicity due to a smaller overlap of the remaining allowed excitations. Specifically, in the dianion the HOMO is mainly localized on the host and presents a weak diatropic response, while the HOMO/C0 → LUMO and HOMO−2 → LUMO excitations contribute paratropically by 45 ppm and 3 ppm on the guest and the host respectively, resulting in a strong deshielding cone at the guest and a very weak deshielding cone at the host (Fig. 7b). Consequently, the dianion retains much of the paratropicity in the guest, whereas in the host the paratropic contributions are marginal, resulting in the strong global diatropic response discussed above.

1H-NMR chemical shifts

The varying aromaticity of neutral and dianionic complexes is expected to be manifested in the hydrogen chemical shifts, providing a useful interpretation of the respective 1H-NMR experimental signals in host–guest aggregates. In Fig. 8a and b the isotropic chemical shielding of a full electron kernel is mapped on the VDW surfaces of neutral and doubly reduced [10]CPP ↔ [5]CPP. In the neutral complex the hydrogens of the

HOMO−LUMO gap, which in contrast to neutral species decreases with increasing size (Fig. 6). The small HOMO–LUMO gaps are compatible with antiaromatic molecules, but in such electronic configurations the strong paratropic response of HOMOs is cancelled due to their nodal structure which forbids the respective HOMO → LUMO rotational excitation by symmetry. Accordingly, in the dianions the major contributing rotational allowed excitation is the HOMO−1 → LUMO, displaying a weaker magnetic response with regard to the neutral counterparts due to a smaller overlap.

In Fig. 7 the magnetic response of frontier orbitals and the corresponding rotational excitations of [10]CPP ↔ [5]CPP complexes are presented. In neutral [10]CPP ↔ [5]CPP the HOMO and LUMO are localized exclusively on the guest, whereas the HOMO−1 and LUMO+1 are on the host. These orbitals correspond to the HOMO and LUMO of free [5]CPP and [10]CPP respectively and therefore they display similar paratropic magnetic responses. Specifically, a strong global deshielding cone is induced on the guest from HOMO−LUMO excitation (NICS_{zz}^{HOMO−LUMO} ≈ 53 ppm), whereas the HOMO−1 → LUMO+1 excitation induces a global deshielding cone on the host (NICS_{zz}^{HOMO−1 → LUMO+1} ≈ 16 ppm, Fig. 7a). In the doubly reduced complex the HOMO → LUMO excitation is forbidden by symmetry and the dianion presents diminished paratropicity due to a smaller overlap of the remaining allowed excitations. Specifically, in the dianion the HOMO is mainly localized on the host and presents a weak diatropic response, while the HOMO/C0 → LUMO and HOMO−2 → LUMO excitations contribute paratropically by 45 ppm and 3 ppm on the guest and the host respectively, resulting in a strong deshielding cone at the guest and a very weak deshielding cone at the host (Fig. 7b). Consequently, the dianion retains much of the paratropicity in the guest, whereas in the host the paratropic contributions are marginal, resulting in the strong global diatropic response discussed above.

1H-NMR chemical shifts

The varying aromaticity of neutral and dianionic complexes is expected to be manifested in the hydrogen chemical shifts, providing a useful interpretation of the respective 1H-NMR experimental signals in host–guest aggregates. In Fig. 8a and b the isotropic chemical shielding of a full electron kernel is mapped on the VDW surfaces of neutral and doubly reduced [10]CPP ↔ [5]CPP. In the neutral complex the hydrogens of the

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Fig. 8 Isotopic chemical shielding mapped on 90% VDW surfaces of (a) neutral and (b) dianion [10]CPP ↔ [5]CPP complexes (solid lines) at 0 (green) and 2− (red) charge states. Experimental values (black) taken from ref. 4.
guest are deshielded, due to the deshielding cone of [5]CPP. In contrast, the hydrogens of the guests in the dianion are strongly shielded from the global shielding cone of the hosts.

The trends of the average calculated $^1$H-NMR chemical shifts are depicted in Fig. 2c and their values are given Table S5 (ESI†). The calculated chemical shifts of neutral free $n$CPPs lying in the range 7.4–8.1 ppm are in very good agreement with experimental values$^9$ with an average deviation $\Delta \approx 0.1$ ppm. The calculated shifts of free dianions are substantially upfield shifted by $\sim 3.9$ ppm, ranging from 3.1 ppm to 4.5 ppm. The upfield shift of doubly reduced $[n]$CPPs, owing to their global aromatic character, is in line and somewhat larger than the experimental data ($\sim 5.36$ ppm)$^{51}$.

Upon neutral complex formation the hosts are essentially unaffected ($\Delta < 0.07$ ppm for $n = 10–13$), while the guests are shifted upfield by $\sim 1.2$ ppm, whereas the experimental data of Yamago$^{37}$ showed a marginal upfield shift for the guests ($\Delta \approx 0.1$ ppm). Concerning the doubly reduced complexes, very clear trends of upfield shifting are observed, differentiating the hosts from the guests. In the dianions, the hosts are upfield shifted by $\sim 3.1$ ppm ranging from 3.9 ppm to 4.8 ppm, very close to the free $[n]$CPP$^2$ ($n = 10–13$) counterparts. The aromaticity of the hosts is manifested in the chemical shifts of the guests which are upfield shifted as they are experiencing strong shielding from the host. Indeed, the guests of the dianions are strongly shifted by $\sim 8.5$ ppm taking negative values, ranging from $-3.3$ ppm to $-1.4$ ppm.

**Conclusions**

In summary, the doubly reduced double-walled cycloparaphenylene complexes $[n+5]$CPP $\supseteq [n]$CPP$^2$ ($n = 5–8$) have been investigated with DFT methods and compared to the neutral counterparts as well as with the free $[n]$CPPs focusing on structural, bonding, electron delocalization and magnetic properties, in order to account for their variation in charge delocalization, aromaticity and $^1$H-NMR spectroscopy properties. According to structural deformations, bonding and local electron delocalization variations, the hosts of the dianions adopt the quinoidal configuration of the corresponding global aromatic free $[n]$CPP$^2$, suggesting that the extra electrons are delocalized on the outer nanohoop of the complex enabling a global aromatic character, while the guests preserve the benzoid geometry of the neutral state.

Under the effect of an external magnetic field, the hosts induce a global long-ranged shielding cone, representing a global aromatic character, similar to the corresponding free dianions $[n]$CPP$^2$. Since the magnetic response of the complex is the cumulative effect of both the host and the guest, the NBO dissection of the complex response to host and guest contributions reveals the individual behavior of each nanohoop. Hence in the dianions the hosts retain the global long-ranged shielding cone of the free $[n]$CPPs$^2$ denoting an exclusive delocalization of the extra charge on the outer nanohoop, whereas the guests preserve the local shielding cones of each phenylene ring, denoting the persistence of local aromaticity of neutral free species. The distinctive magnetic behavior of doubly reduced complexes is rationalized by the modulated electronic configuration which forbids strong paratropic contributions from HOMO $\rightarrow$ LUMO excitations and allows excitations from lower orbitals to LUMO, with weaker contributions due to smaller overlaps. Thus, in host–guest “Russian doll” or “Planetary orbit” dianionic species, the global aromatic behavior is retained in the outer structural layer, suggesting that further electronic delocalization in multi-layered related species will be contained at the outer structural surface.

The aromaticity of the hosts is manifested in the $^1$H-NMR chemical shifts of the guests experiencing a strong shielding, which are upfield shifted in the dianions by $\sim 8$ ppm with respect to the free neutral counterparts. These predictions could be helpful for the experimental identification of doubly reduced nanohoop complexes with $^1$H-NMR spectroscopy, extending our understanding of double-walled nanotubes at the nanoscale regime.

Finally, we introduce and propose to aromaticity researchers a new approach for the investigation of complex carbon aggregates by the dissection of the induced magnetic field to individual host and guest $\pi$-contributions using NBO analysis, which can be very accurately and effectively modelled employing the computationally lightweight pseudo-$\pi$ method.

Our group is currently working on an investigation of the properties and aromaticity of open-shell $\pi$-complexes and their complexes.

**Conflicts of interest**

There are no conflicts to declare.

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