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Dynamics study of the post-transition-statebifurcation process of the (HCOOH)H⁺ → $CO + H_3O^+/HCO^+ + H_2O$ dissociation: application of machine-learning techniques†

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The process of protonated formic acid dissociating from the transition state was studied using ringpolymer molecular dynamics (RPMD), classical MD, and quasi-classical trajectory (QCT) simulations. Temperature had a strong influence on the branching fractions for the HCO $^+$ + H₂O and CO + H₃O $^+$ dissociation channels. The RPMD and classical MD simulations showed similar behavior, but the QCT dynamics were significantly different owing to the excess energies in the guasi-classical trajectories. Machine-learning analysis identified several key features in the phase information of the vibrational motions at the transition state. We found that the initial configuration and momentum of a hydrogen atom connected to a carbon atom and the shrinking coordinate of the CO bond at the transition state play a role in the dynamics of HCO⁺ + H₂O production.

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1 Introduction

Proton-transfer reactions are vital in interstellar chemistry, and several charged species, such as H_3^+ , HCO^+ , H_3O^+ , and CH_5^+ , act as efficient proton donors to neutral molecules found in the interstellar medium. 1-8 The cross-sections or reaction rate coefficients for these proton-transfer processes are typically large because of the strong attractive interaction between charged and neutral molecules and the sizable proton affinity values of neutral interstellar species.^{9,10} In many of these proton-transfer reactions, the large excess energy is distributed into the protonated product molecule through the spectator stripping mechanism, where the transfer of a light proton particle occurs at large distances between the reactants, leading to a large initial vibrational energy in the H-X bond (X is a proton-accepting atom). An example is the H_3^+ + HCOOH $\rightarrow H_2$ + (HCOOH) H^+ reaction, $^{6-8,11}$ which is the focus of this study. The large excess energy in the protonated (HCOOH)H⁺ molecule can lead to its subsequent decomposition into two product channels: HCO+ + H2O and CO + H₃O⁺. These product molecules, along with the parent HCOOH

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molecule, have been detected in the interstellar medium, 12 making the corresponding [CO + H₃O⁺]:[HCO⁺ + H₂O] branching fraction an important parameter in astrochemical modeling. Additionally, the decomposition process associated with the unimolecular reaction of the energetic (HCOOH)H+ molecule can lead to a post-transition-state bifurcation (PTSB), where one transition-state (TS) structure results in two different product channels, as found in a previous theoretical study by Uggerud et al.⁸ They calculated the potential energy surface (PES) property using ab initio quantum chemistry and suggested that the initial protonated product takes the HC(OH)2+ structure, which subsequently isomerizes into the $(HCO \cdots H_2O)^+$ type complex via the hydrogen transfer TS. This $(HCO \cdot \cdot \cdot H_2O)^+$ complex can dissociate into both the HCO+ + H2O and CO + H3O+ fragments, but additional molecular rearrangements are required to achieve the latter CO + H_3O^+ fragments. The primary objective of this study is to computationally understand the dynamic mechanism of product branching in the dissociation of the (HCOOH)H+ molecule. As suggested by Uggerud et al.,8 we have investigated the indirect dissociation mechanism of the $(HCO\cdots H_2O)^+$ type complex via the hydrogen transfer TS under the condition which the large excess energy generated by the protonation is redistributed as the internal energy. The energies which are more than the barrier height of the TS have been regarded as the thermal energies in this study. Notice that the proton affinities of the formic acid and H_2 are 742.0 kJ mol⁻¹ (177.3 kcal mol⁻¹) and 4.39 eV (101.3 kcal mol⁻¹), respectively. 13,14 It is expected that there is enough energy to exceed the barrier in the (HCOOH)H+ molecule.

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The TS typically connects one set of reactants with one set of products, resulting in a single reaction pathway as a function of the intrinsic reaction coordinate (IRC). 15,16 However, there are also examples of chemical reactions where a single TS leads to multiple products. 17-20 This phenomenon, known as PTSB, 19,20 occurs due to the bifurcating nature of the post-transition-state reaction pathway on the PES. Notably in such cases, the product branching ratio is controlled by nuclear dynamics, 21,22 although non-dynamical methods for practically estimating branching ratios have been proposed by several groups.²³⁻²⁸ In most of the previous PTSB studies, the product branching ratios were calculated using the well-known classical trajectory method initiated from the structures around the TS. More specifically, the quasi-classical trajectory (QCT) method, where quantized vibrational energies are also treated with a classical mechanics manner, is frequently employed. In fact, in the previous study by Uggerud et al.,8 on-the-fly ab initio QCT calculations were used to estimate the [CO + H₃O⁺]:[HCO⁺ + H₂O] branching fraction although only a small number of trajectories were integrated due to huge computational cost. In addition to this, it is worth mentioning that the QCT calculations frequently show zero-point leakage phenomenon leading to erroneous nuclear dynamics. 29-31 Thus, the accuracy of the QCT scheme used in bifurcation reactions has not yet been fully understood. Motivated by this, we here calculate the branching fractions using three different nuclear dynamics methods including QCT, classical molecular dynamics (MD), and ring-polymer MD (RPMD)³²⁻³⁶ methods to understand the effect of the nuclear dynamics method in branching dynamics. Notice that the RPMD method can approximately describe both nuclear quantum effects and thermal fluctuation. 29,37-53

In order to efficiently apply the above-mentioned three nuclear dynamics methods to the dissociation of (HCOOH)H⁺ into CO + H₃O⁺ or HCO⁺ + H₂O, we here utilize two different machine-learning (ML) computational techniques. One is the Δ -ML method^{54–56} for constructing a global PES. Generally, the electronic structure calculations considering the electronic correlation term for the systems, which have the large number of nuclear degrees of freedom and include heavy atoms, need high computational cost. Δ-ML method has been developed to avoid the expensive calculation cost with maintaining the accuracy of the PES. The low-level calculations such as Hartree-Fock and semiempirical methods are supposed as the fundamental PES, and the several high-level potential energies (and their gradients) are used as the correction term. The differences between the low-level and high-level PESs are utilized as the training data set. Then, the differential potential function Δ is evaluated using machine-learning technique. As will be described below, one can efficiently calculate both the potential energy and gradient values at a given nuclear structure using the PES of the protonated formic acid developed by the Δ -ML method.⁵⁶ Thus, one can integrate a large number of trajectories. The second technique is a supervised ML classification approach, which is used to understand the detailed branching dynamics, i.e., the correlation between the initial conditions and the product branching. The branching fractions can be investigated through the ML

analysis using statistical data such as the Cartesian coordinates and momenta or normal mode phase information at the initial TS region. It should be mentioned that, as the number of nuclear degrees of freedom in the chemical system increases, it can become difficult to identify which initial coordinates or momentum properties are important for the determination of the branching process. The ML classification approach helps us to identify the significant properties that dominate the bifurcation dynamics without relying on human intuition.⁵⁷ Similar ML analysis techniques have been applied to other chemical reaction systems that exhibit PTSB. 58-60 The details of the Δ -ML method, the MD method and those of the supervised ML algorithm are described in Section 2. The results of the dynamics and machine-learning analysis are discussed in Section 3. The conclusion is presented in Section 4.

2 Methodology

2.1 Development of Δ -ML PES

To integrate a statistically convergent number of MD trajectories within a reasonable computational timeframe, it is crucial to develop an accurate PES function. In this work, we have chosen to use the Δ -ML approach. ⁵⁶ This approach describes the final PES as the sum of a low-level PES function and a correction function, which are both functions of nuclear coordinates. In the Δ -ML approach developed by Bowman et al., these two functions are fitted using permutationally invariant polynomials to the results of ab initio calculations. 61,62 In this work, we have chosen to use the semiempirical GFN2-xTB method⁶³⁻⁶⁵ as the low-level PES to avoid the time-consuming PES fitting procedure. The correction term was determined by fitting a dataset consisting of energy differences between the GFN2-xTB and ab initio calculations to a 3rd-order permutationally invariant polynomial function.

The ab initio level chosen in this study is the MP2 method with a 6-31G(d) basis set, as it allows for the qualitative comparison of the present results with those of previous studies by Uggerud et al. 8 In order to develop the PES to describe the (HCOOH)H⁺ dissociation dynamics, a dataset of 192 000 data points was generated by performing on-the-fly MD calculations at the MP2/6-31G(d) level. Subsequently, GFN2-xTB calculations were performed to obtain a dataset for fitting. The root-mean-square error (RMSE) for the fit was 209.9 cm⁻¹. The fitting error for the correction energy is presented in Fig. S1 in the ESI.† All MP2/6-31G(d) level calculations were conducted using the Gaussian09 program package, 66 while the GFN2-xTB calculations were performed using the xtb program (ver. 6.5.1), 65,67 with an electronic temperature of 2500 K to achieve better convergence in the self-consistent charge iteration.⁶⁴

2.2 Three types of the real-time MD simulations

In this study, three types of MD simulations, which are the QCT, classical MD and RPMD, have been performed on the Δ -ML PES. To clarify the (HCOOH)H⁺ dissociation processes, all MD simulations started around the TS. Under the assumption that (HCOOH)H⁺ is thermalized and has the internal energies more than the potential energy at the TS, the energies over the

TS barrier height were considered as the thermal energies. In this work, the temperatures 298, 1000, 2000 and 4000 K, which correspond to the thermal energies 0.6, 2.0, 4.0 and 8.0 kcal mol⁻¹, were employed. For QCT, the initial coordinates and momenta were randomly sampled, considering the zeropoint energy (ZPE) and thermal energy for each normal mode at the TS structure. On the other hand, for the RPMD and classical MD, the initial coordinates and momenta were sampled by path-integral molecular dynamics (PIMD) technique. Then, the real-time RPMD and classical MD simulations from the initial conditions obtained by the PIMD simulation were performed. The details of the QCT, PIMD, RPMD and classical MD are mentioned below.

2.2.1 QCT. To evaluate the dynamics of the protonated formic acid dissociation, QCT simulations were performed using the Born-Oppenheimer molecular dynamics (BOMD) approach. 68 The BOMD method, which is a tool in the Gaussian 09 program package, was used to solve the equations of motion (EOMs) by incorporating a Hessian-based integrator with a fifth-order polynomial fit. The simulations were run for approximately 500 fs, using the GFN2-xTB method with the Δ -ML PES. The initial coordinates and velocities were randomly sampled, considering the ZPE and thermal energy for each normal mode at the TS structure. The velocities for the imaginary frequency mode were sampled according to the statistical Boltzmann distribution, and the initial coordinates of the imaginary mode were always located on the TS.

2.2.2 PIMD. To perform the real-time dynamics simulations, the PIMD simulations (based on the imaginary time path integral theory) were conducted to obtain the phase information of the thermal distribution at temperatures of 298, 1000, 2000, and 4000 K. The thermal phase distribution was used as the initial conditions for real-time dynamics simulations. The PIMD simulations were performed at the TS for each normal mode, including one imaginary mode, among the 12 modes. To maintain the molecular structures around the TS, the vibrational normal mode coordinates were employed instead of Cartesian coordinates.

The PIMD simulations were carried out for a simple onedimensional PES, $V(Q_{\alpha})$, in atomic units, where Q_{α} is the α -th normal mode coordinate for the vibrational frequency at the stationary point. The quantum partition function Z at temperature T in the path integral representation is

$$Z = \lim_{N \to \infty} \left(\frac{\mu N}{2\pi \beta \hbar^2} \right)^{N/2} \int d\mathbf{Q}_{\alpha} \exp(-\beta V_{\text{eff}}(\mathbf{Q}_{\alpha})), \tag{1}$$

where N is the number of beads, $\beta \equiv 1/k_BT$ represents a reciprocal temperature with the Boltzmann constant $k_{\rm B}$, $\hbar = 1$ and $\mu = 1$ (in atomic units) are the reduced Planck constant and the reduced mass for the Q_{α} respectively, and $\mathbf{Q}_{\alpha} = (Q_{\alpha}^{1}, \dots, Q_{\alpha}^{N})^{T}$ is the N-dimensional vector coordinate. The effective potential $V_{\rm eff}$ is given by

$$V_{\text{eff}} = \frac{1}{2}\mu\omega_N^2 \mathbf{Q}_{\alpha}^T \mathbf{A} \mathbf{Q}_{\alpha} + \phi(\mathbf{Q}_{\alpha}), \tag{2}$$

with $\omega_N \equiv \sqrt{N}/\beta\hbar$ being a harmonic chain frequency and **A** being a matrix whose the elements are described as $A_{ii} = 2\delta_{ii}$ –

 $\delta_{i,j+1} - \delta_{i,j-1}$ with the cycle boundary conditions $0 \to N$ and $N+1 \rightarrow 1$. The first term of the right-hand side of eqn (2) represents the harmonic interaction between the adjacent beads. The second term is the bead-averaged physical potential

$$\phi(\mathbf{Q}_{\alpha}) = \frac{1}{N} \sum_{j=1}^{N} V(Q_{\alpha}^{j}), \tag{3}$$

where $V(Q_{\alpha}^{j})$ is the harmonic potential with the α -th vibrational frequency ω_{α} , and

$$V(Q_{\alpha}^{j}) = \frac{1}{2}\omega_{\alpha}^{2}(Q_{\alpha}^{j})^{2}.$$
 (4)

For imaginary frequency mode, where ω_{α}^{2} is negative, the $V(Q_{\alpha}^{j})$ becomes

$$V(Q_{\alpha}^{j}) = \frac{1}{2} f |\omega_{\alpha}^{2}| (Q_{\alpha}^{j})^{2}, \tag{5}$$

with f = 0.1 being the bias factor. In this study, the first term in $V_{\rm eff}$ has been diagonalized in the same manner as in previous studies. 69,70 The diagonalization of the matrix NA is defined by

$$\mathbf{U}^{T}(N\mathbf{A})\mathbf{U} = \Lambda, \tag{6}$$

with the analytical diagonal eigenvalue matrix Λ and the eigenvector U. The eigenvalue matrix elements are represented by

$$\lambda_{2k} = 4N\sin^2\left(\frac{\pi k}{N}\right) (k \neq 0),$$

$$\lambda_{2k+1} = 4N\sin^2\left(\frac{\pi k}{N}\right) \left(k \leq \frac{N-1}{2}\right),$$
(7)

with $\lambda_1 = 0$ and $\lambda_N = 4N$. The eigenvector matrix elements are expressed as

$$U_{j,2k} = \sqrt{\frac{2}{N}} \cos\left(\frac{2\pi jk}{N}\right) (k \neq 0)$$

$$U_{j,2k+1} = \begin{cases} \sqrt{\frac{1}{N}} & (k = 0) \\ \sqrt{\frac{2}{N}} \sin\left(\frac{2\pi jk}{N}\right) & \left(k \leq \frac{N-1}{2}\right). \end{cases}$$
(8)

The coordinate \mathbf{Q}_{α} can be transformed to $\tilde{\mathbf{Q}}_{\alpha}$ using the eigenvector,

$$\tilde{\mathbf{Q}}_{\alpha} = \frac{1}{\sqrt{N}} \mathbf{U}^T \mathbf{Q}_{\alpha}.$$
 (9)

Using the newly defined coordinate $ilde{\mathbf{Q}}_{lpha}$ and its conjugated momentum $\tilde{\mathbf{P}}_{\alpha} = (\tilde{P}_{\alpha}^{1}, \dots, \tilde{P}_{\alpha}^{N})^{T}$, the Hamiltonian H of the classical representation is defined as

$$H(\tilde{\mathbf{Q}}_{\alpha}, \tilde{\mathbf{P}}_{\alpha}) = \frac{1}{2} \tilde{\mathbf{P}}_{\alpha}^{T} \tilde{\boldsymbol{\mu}}^{-1} \tilde{\mathbf{P}}_{\alpha} + \frac{1}{2} \mu \omega_{N}^{2} \tilde{\mathbf{Q}}_{\alpha}^{T} \Lambda \tilde{\mathbf{Q}}_{\alpha} + \phi(\mathbf{Q}_{\alpha}(\tilde{\mathbf{Q}}_{\alpha})), \quad (10)$$

where $\tilde{\mu}$ is a diagonal matrix, whose elements are the fictitious mass for the newly defined phase space $(\tilde{\mathbf{Q}}_{\alpha}, \tilde{\mathbf{P}}_{\alpha})$. The diagonal terms diag($\tilde{\boldsymbol{\mu}}$) = $(\mu, \tilde{\mu}^2, \dots, \tilde{\mu}^N)$ are expressed as

$$\tilde{\mu}^{j=1} = \mu = 1, \ \tilde{\mu}^{j} = \lambda_{j} \mu \ (2 \le j \le N).$$
 (11)

Note that the matrix $\tilde{\mu}$ is constant for any vibrational mode when the number of beads N is the same for all vibrational modes. The canonical equations of motion (EOMs) are then conventionally derived from eqn (10):

$$\dot{\tilde{\mathbf{Q}}}_{\alpha} = \tilde{\boldsymbol{\mu}}^{-1} \tilde{\mathbf{P}}_{\alpha}, \tag{12}$$

$$\dot{\tilde{\mathbf{P}}}_{\alpha} = -\mu \omega_N^2 \Lambda \tilde{\mathbf{Q}}_{\alpha} - \frac{\partial \phi(\mathbf{Q}_{\alpha}(\tilde{\mathbf{Q}}_{\alpha}))}{\partial \tilde{\mathbf{Q}}_{\alpha}}.$$
 (13)

The EOMs were integrated by employing the velocity Verlet algorithm⁷¹ with time step $\Delta t = 0.20$ fs with the Nóse–Hoover chain thermostat^{72–74} for each vibrational mode. The initial phase information $\tilde{\mathbf{Q}}_{\alpha}$ and $\tilde{\mathbf{P}}_{\alpha}$ were randomly chosen. The canonical ensemble was maintained until the expectation value of the internal energy converged – with a total of 11×10^6 steps. Note that the initial coordinates and momenta for the real-time dynamics for RPMD as well as classical MD were picked up from the ones every 1000 steps after the 1×10^6 steps simulations. The number of beads N were set as 32, 10, 6, and 4 for the temperature T = 298, 1000, 2000, and 4000 K. The EOMs were solved individually for all vibrational modes, $\alpha \in (1, \dots, 3n-6)$ (for nonlinear molecule), where n is the number of atoms. The coordinates and their velocities $(\tilde{\mathbf{Q}}_{\alpha}, \tilde{\mathbf{Q}}_{\alpha})$ were transformed to $(\mathbf{Q}_{\alpha}, \tilde{\mathbf{Q}}_{\alpha})$ via the inverse transformation of eqn (9).

Once the phase information for all vibrational modes was gathered, the vibrational normal mode can then be transformed conventionally to Cartesian coordinates and their time derivatives:

$$\vec{q}^j = \stackrel{\longleftrightarrow}{L} \vec{Q}^j, \tag{14}$$

where $\vec{q}^j = (q^j_1, \cdots, q^j_{3n})^T$ and $\vec{Q}^j = (Q^j_1, \cdots, Q^j_{\alpha+6}, \cdots, Q^j_{3n})^T$ are the mass-weighted Cartesian coordinate vector and the normal mode coordinate vector for j-th bead, respectively. Notice that (Q_1, \cdots, Q_6) represents the translational and rotational (not vibrational) modes. \vec{L} is the $3n \times 3n$ unitary matrix used to obtain the vibrational frequency diagonal matrix, Ω , diag $(\Omega) = (\omega_1^2, \cdots, \omega_{\alpha+6}^2, \cdots, \omega_{3n}^2)$. The Cartesian coordinates $\vec{x}^j = (x^j_1, \cdots, x^j_{3n})^T$ and their velocities for j-th bead can eventually be obtained by

$$\Delta \vec{x}^j = \overrightarrow{M}^{-1/2} \vec{q}^j, \tag{15}$$

where $\Delta \vec{x}^j$ is the displacement coordinates:

$$\Delta \vec{x}^j = \vec{x}^j - \vec{x}^e, \tag{16}$$

with \vec{x}^e being the 3n-dimensional Cartesian coordinate vector at the stationary point where is the TS in this study. \vec{M} is the diagonal matrix whose elements m_l correspond to the atomic mass for the l-th Cartesian coordinate. Note that the centroid of beads is written by

$$\vec{x}^{\text{cent}} = \frac{1}{N} \sum_{i=1}^{N} \vec{x}^i. \tag{17}$$

Likewise, their velocities can be obtained based on eqn (14), (15) and (17).

2.2.3 RPMD. The semiclassical real-time MD simulation, referred to as the RPMD method, $^{32-36}$ was carried out at temperature T=298, 1000, 2000, and 4000 K. The RPMD method, which can represent nuclear quantum effects such as ZPE and quantum tunneling, 37,38 has been extensively used. $^{29,39-53}$ In contrast with the Hamiltonian for one-dimensional normal mode of PIMD, the Hamiltonian for RPMD is defined for the $(3n \times N)$ bead)-multidimensional system from Cartesian coordinate representation:

$$H(\vec{\mathbf{X}}, \vec{\mathbf{P}}) = \sum_{l=1}^{3n} \left(\frac{1}{2} \mathbf{P}_l^T \boldsymbol{\mu}_l^{-1} \mathbf{P}_l + \frac{1}{2} m_l \omega_N^2 \mathbf{X}_l^T \Lambda \mathbf{X}_l \right) + \phi(\vec{\mathbf{x}}), \quad (18)$$

where $\mathbf{X}_l = (X_l^1, \dots, X_l^N)^T$ and $\mathbf{P}_l = (P_l^1, \dots, P_l^N)^T$ are the newly defined N-dimensional coordinate and its conjugated momentum vectors, respectively. The \mathbf{X}_l were obtained from the N-dimensional l-th Cartesian coordinate vector $\mathbf{x}_l = (x_1^1, \dots, x_l^N)^T$:

$$\mathbf{X}_l = \frac{1}{\sqrt{N}} \mathbf{U}^T \mathbf{x}_l. \tag{19}$$

 $\vec{\mathbf{X}}$, $\vec{\mathbf{P}}$ and $\vec{\mathbf{x}}$ are the $(3n \times N \text{ bead})$ -dimensional newly defined coordinates $\vec{\mathbf{X}} = (\mathbf{X}_1^T, \cdots, \mathbf{X}_{3n}^T)$, their conjugated momenta $\vec{\mathbf{P}} = (\mathbf{P}_1^T, \cdots, \mathbf{P}_{3n}^T)$, and the Cartesian coordinates $\vec{\mathbf{x}} = (\mathbf{x}_1^T, \cdots, \mathbf{x}_{3n}^T)$, respectively. The fictitious mass matrix for μ_l for $(\mathbf{X}_l, \mathbf{P}_l)$ has the diagonal elements of the atomic mass of the l-th Cartesian coordinate:

$$\mu_l^j = m_l (1 \le j \le N).$$
 (20)

The last term of eqn (18) is the average physical potential:

$$\phi(\vec{\mathbf{x}}) = \frac{1}{N} \sum_{i=1}^{N} V(x_1^i, \dots, x_{3n}^i), \tag{21}$$

where V is the physical potential energy.

The EOMs of eqn (18) were then calculated by the velocity Verlet algorithm⁷¹ with time step $\Delta t = 0.50$ fs for the real-time propagation without the thermostat. The total simulation time was 500 fs, which was the same as that for the classical MD simulation described below. The RPMD and subsequent classical MD simulations for the real-time dynamics were performed using the PIMD program (ver. 2.4.0) developed by Shiga.⁷⁵

2.2.4 Classical MD. Thermalization has been discussed in the PIMD section, and the real-time dynamics has been explained in the RPMD section. In the classical MD simulations, the number of beads N was set to 1. In this case, the Hamiltonian of eqn (10) has been re-expressed for thermalization as

$$H(Q_{\alpha}, P_{\alpha}) = \frac{P_{\alpha}^{2}}{2} + V(Q_{\alpha}). \tag{22}$$

Note that the expectation value of the internal energy for this thermalization lacks the contribution of the ZPE.

The Hamiltonian (without the thermostat) for the real-time dynamics therefore becomes the conventional classical Hamiltonian:

$$H(\vec{x}, \vec{p}) = \sum_{l=1}^{3n} \frac{p_l^2}{2m_l} + V(\vec{x}), \tag{23}$$

where \vec{x} and \vec{p} are the Cartesian coordinates $\vec{x} = (x_1, \dots, x_{3n})^T$ and the conjugated momenta $\vec{p} = (p_1, \dots, p_{3n})^T$, respectively.

2.3 Supervised ML

Supervised ML was performed to analyze the features dictating the branching reaction. In this study, binary classifications of the branching dynamics were carried out based on 108 TS features, including vibrational modes, their velocities, bond distances, bond angles, and dihedral angle. The random forest (RF), K-nearest neighbor (KNN), multi-layer perceptron (MLP), stochastic gradient descent (SGD), support vector machine (SVM), and logistic regression (LogR) algorithms, which are implemented in the Scikit-Learn Python Library, were employed in this study. The lightGBM (LGB) algorithm implemented in Python3 was also carried out. Both of RF and LGB classifiers are decision tree-based algorithms. The RF is the method based on the bagging also known as bootstrap aggregating that is a parallel ensemble learning method, whereas boosting algorithm used in the LGB method is a sequential ensemble learning method. The SelectFromModel method with the RF model of the Scikit-learn library was used to perform feature selection and reduction to half in order to improve the classification accuracy score. The accuracy of each classification model was obtained by performing a 5-fold cross validation on the most relevant 54 TS features. To obtain the accuracy scores with eliminating the dimension influences of each feature,⁵⁷ the data sets were normalized into [0, 1]. An optimized RF (RF Opt) and LGB models were obtained by performing hyperparameter optimization using the GridSearchCV method of the Scikit-learn library in Python3. The data sets were initially split as the training and validation data (75%) and test data (25%), then hyperparameter optimization was performed with 5-fold cross validation in the training and validation data. The parameters which are the number of estimator, criterion, max depth, and max features, were optimized for the RF model. In contrast, the minimum number of data per leaf, the number of leaves, the number of iterations, the coefficients of L1 and L2 regularization, and metric were tuned for the LGB method with gradient boosting decision tree (GBDT). The learning rate was set to 0.05 for the LGB model to avoid overfitting. Eventually the RF Opt and LGB models with best estimators were generated for the training and validation data. Once the high accuracy score for the test data using the RF Opt and LGB models are obtained, we can extract the reliable feature importance of the RF and LGB models. Notice that the gain-based feature importance for LGB model was obtained in this study.

Results and discussion

3.1 Potential energy profile

Fig. 1 illustrates the reaction pathway (represented by a black line) from the reactant (EQ₁), which is the equilibrium protonated formic acid, to the complex intermediate CO···H₃O⁺ (INT₄), and includes key geometries. As previously discussed

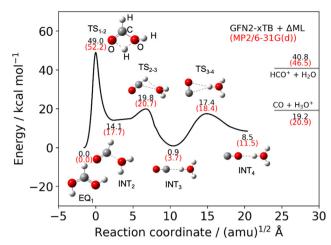


Fig. 1 Potential energy curve calculated using GFN2-xTB method with the Δ -ML approach for the dissociation reactions, illustrating key geometries. The potential energies of the key geometries are compared with MP2/6-31G(d)

in the methodology section, the PES was calculated using the GFN2-xTB approach with correction by the Δ -ML method, with the reactant set at $0.00 \text{ kcal mol}^{-1}$. The potential energy curve is composed of three IRC calculations and is condensed into a single curve. The first TS, denoted as TS1-2, connects EQ1 and INT2 and describes the large energy barrier in the proton/hydrogen transfer reaction between two oxygen atoms. However, it is expected that the reaction can overcome this barrier because the protonated formic acid has large excess energy. 6-8,11 Beyond TS₁₋₂, the potential energies of the remaining intermediates and TSs are lower than the TS₁₋₂ energy. INT₂ and TS₂₋₃ have precursor structures of the HCO⁺ + H₂O product. Then, the protontransfer reaction $OCH^+ \cdots H_2O \rightarrow OC \cdots H_3O^+$ occurs from TS_{2-3} to INT3. The CO molecule rotates between INT3 and INT4 through TS₃₋₄. The potential energies written in black and red correspond to the values obtained from our PES and MP2/6-31G(d) level calculations, respectively. Additionally, the values are compared with results from previous theoretical studies that were calculated using the MP2/6-31G(d) level.8 Our potential profiles are in good agreement with the previous study (see Table S1, ESI†). The quality of the PES is sufficient for performing appropriate MD simulations, as the protonated formic acid has excess energy. In this study, it is not important for the molecule to tunnel through the barrier in the reaction pathway. The potential energy values are listed in Table S1 in the ESI.†

3.2 PIMD sampling

The coordinates and momenta at TS₁₋₂ were sampled on the PES (described by eqn (4) and (5)) by the PIMD technique to perform the RPMD method, which is the real-time dynamics simulation. Fig. S2 and S3 in the ESI,† show the imaginary vibrational frequency mode and the temperature-dependent populations of vibrational states of harmonic oscillators with different wavenumbers $\tilde{\nu}_{\alpha} = \omega_{\alpha}/2\pi c$, where c is the speed of light. The formula of the population is expressed as eqn (A8) in Appendix A. As shown in Fig. S3 (ESI†), higher excitation occurs

as temperature increases and the vibrational frequency is smaller as expected. At 4000 K, for the smallest wavenumber $\tilde{\nu}_2$, the vibrational mode is populated even in the 20-th excited state. In contrast, vibrational excitation over the 4-th excited state rarely occurs for the largest frequency mode $\tilde{\nu}_{12}$, even at 4000 K.

Fig. S4 in the ESI,† illustrates the expectation value of the configuration space for the Q_2 and Q_{12} modes, corresponding to the smallest and largest frequencies, respectively. The results of thermalization by the PIMD and classical procedures are depicted in Fig. S4a-d (ESI†). The black line represents the magnitude of the zero-point vibrational wave function $|\Psi_0|^2$. In the case of the smallest frequency mode shown in Fig. S4a and c (ESI†), the expectation values from both PIMD and classical simulations at temperatures of 1000, 2000 and 4000 K are similar, as the ZPE is smaller than the expectation value of the internal energy $\langle E \rangle$ (as seen in Table S2 in the ESI†); thus, quantum effects are not significant at higher temperatures. At 298 K, the distribution of coordinates is along the line of $|\Psi_0|^2$ in Fig. S4a and c (ESI†). Conversely, in Fig. S4b (ESI†), the expectation values of the configuration space at 298, 1000, and 2000 K obtained using PIMD sampling are distributed along the zero-point vibrational wave function $|\Psi_0|^2$. At 4000 K, the coordinate distribution has a larger tail than $|\Psi_0|^2$. In contrast with PIMD sampling, the distributions at temperatures below 2000 K obtained using classical sampling in Fig. S4d (ESI†) are narrower than $|\Psi_0|^2$ because the configuration space has a classical limit. The distributions at 4000 K shown in Fig. S4b and d (ESI†) are similar, as the internal energy is dominated by $k_{\rm B}T$ rather than ZPE at this temperature.

Table S2 (ESI†) presents the expectation value of the internal energies $\langle E \rangle$ obtained using PIMD sampling and the analytical internal energy $\langle U_{\rm q} \rangle$ for the quantum harmonic oscillator at various temperatures, including the ZPE. It is observed that the energy calculated using PIMD simulations $\langle E \rangle$ for all normal modes at each temperature is in good agreement with the analytical value $\langle U_{\rm q} \rangle$ (as described in eqn (A7) in Appendix A). At 298 K, ZPE dominates the $\langle E \rangle$. As the temperature increases, $k_{\rm B}T$ becomes more dominant over ZPE, particularly for smaller wavenumber $\tilde{\nu}_{\alpha}$. In contrast, Table S3 (ESI†) illustrates the expectation values of the internal energies $\langle E \rangle$ obtained using classical sampling and the analytical values $\langle U_c \rangle$ (as described in eqn (A3) in Appendix A). The $\langle U_c \rangle$ is only temperaturedependent and does not depend on the vibrational frequencies. As a result, the energy $\langle E \rangle$ for the classical procedure for all normal modes is almost the same at each temperature. From these results, it can be concluded that both thermalizations via PIMD and classical procedures are effective.

Branching fraction

Fig. 2 illustrates the branching fraction between $[CO + H_3O^+]$ and [HCO⁺ + H₂O] from QCT, classical MD, and RPMD simulations at various temperatures. The number of trajectories correlated with the branching and the total number of trajectories are listed in Table 1. At 298 K, the CO + H₃O⁺ fragments are dominant in all simulations shown in Fig. 2. As the

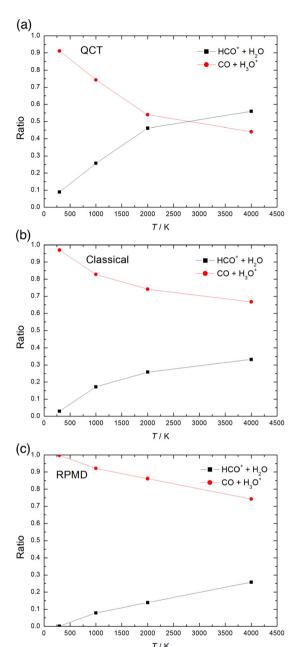


Fig. 2 Branching fraction profiles as a function of temperature for (a) QCT, (b) classical MD, and (c) RPMD. The black and red lines represent the product ratio of the $HCO^+ + H_2O$ and $CO + H_3O^+$, respectively.

temperature increases, the HCO+ + H2O branching fraction increases. The fraction behavior for QCT is significantly different from that of other simulations. The HCO⁺ + H₂O becomes the primary product at 4000 K for QCT, while the main products for classical MD and RPMD simulations remain CO + H₃O⁺. This property is likely influenced by the ZPE leakage, 29-31 which is frequently discussed as the problem for the QCTs^{51-53,60,76,77} which have excessive energies (vibrational quantization energies in classical trajectories). It can be predicted that the ZPE leakage phenomenon substantially influences the branching dynamics. Recently, Tremblay et al. have also shown that the ZPE percentage affects the bifurcation ratio. ⁷⁸ The HCO⁺ + H₂O fragments

Table 1 Number of HCO⁺ + H₂O and CO + H₃O⁺ fragment trajectories, and the total number of trajectories $N_{\rm Traj.}$ at each temperature for QCT, classical MD and RPMD simulations

T/K	$HCO^+ + H_2O$	$CO + H^3O^+$	$N_{ m Traj.}$
QCT			
298	272	2793	3065
1000	531	1535	2066
2000	1016	1188	2204
4000	1249	984	2233
Classical M	ID		
298	83	2693	2776
1000	390	1877	2267
2000	524	1705	2229
4000	572	1147	1719
RPMD			
298	4	2212	2216
1000	201	2359	2560
2000	280	1740	2020
4000	492	1418	1910

for RPMD are slightly less than those for classical MD, but both tendencies are similar. One possible reason of the slight difference at high temperature could be the procedure for solving the EOMs. For RPMD, the EOMs for the each bead were solved then the centroid get influenced by the mean force from the beads. In contrast, the classical MD were time-propagated based on the solution of the EOMs of the classical nuclei. As shown in Fig. S4 (ESI†), the initial configuration distribution at high temperature doesn't really contribute the difference of the branching fractions between the RPMD and classical MD because the configuration distribution at high temperature for both classical MD and RPMD are quite similar. Table 2 shows the comparison the branching fractions from three types of simulations with previous studies. The previous theoretical study⁸ shows that the HCO⁺ + H₂O

Table 2 Branching fractions with the standard deviations of HCO⁺ + H₂O and CO + H₃O⁺ products at each temperature for QCT, classical MD and RPMD simulations compared with previous studies

	Products/%	Products/%	
T/K	HCO ⁺ + H ₂ O	CO + H ₃ O ⁺	
QCT			
298	8.9 ± 0.5	91.1 ± 0.5	
1000	25.7 ± 1.0	74.3 ± 1.0	
2000	46.1 ± 1.1	53.9 ± 1.1	
4000	55.9 ± 1.1	44.1 ± 1.1	
Classical MD			
298	3.0 ± 0.3	97.0 ± 0.3	
1000	17.2 ± 0.8	82.8 ± 0.8	
2000	23.5 ± 0.9	76.5 ± 0.9	
4000	33.3 ± 1.1	66.7 ± 1.1	
RPMD			
298	0.2 ± 0.1	99.8 ± 0.1	
1000	7.9 ± 0.5	92.1 ± 0.5	
2000	13.9 ± 0.8	86.1 ± 0.8	
4000	25.8 ± 1.0	74.2 ± 1.0	
Theo. (ref. 8)			
298	40	60	
1000	60	40	
Exp. (ref. 6)			
298	30	70	
Exp. (ref. 11)			
353	17.8	82.2	

branching fraction increases as temperature increases, which indicates our simulations are qualitatively agreement with the previous one. The product ratios of HCO+ + H2O fragments measured at 298 and 353 K were 30% and 17.8%. 11 Both values are relatively larger than our data for all simulations at 298 K. From the results, it could be tentatively estimated that the direct dissociation process right after the protonation contributes the increasing of the HCO⁺ + H₂O products because our simulations have considered the indirect dissociation process after the excess energy from the proton affinity are thermalized as the internal energy, which is also knows as the intramolecular vibrational redistribution. In the following section, we discuss the crucial initial phase information at TS₁₋₂, which has a huge effect on the bifurcation dynamics, using ML analysis.

Binary classification by the supervised ML algorithms

Fig. 3 illustrates the accuracy scores for the 54 TS features in the binary classification of the CO + H₃O⁺ and HCO⁺ + H₂O dissociation trajectories at 298 K for the classical MD simulations using various classification models. Note that an equal number of CO + H₃O⁺ and HCO⁺ + H₂O dissociation trajectories were included in the data set for the ML analysis. As mentioned above, the data sets were normalized into [0, 1] to adjust the magnitude and to eliminate the dimension effects of each feature. The scores and error bars represent the means and standard deviations for a 5-fold cross validation, respectively. The RF model provided an accuracy of 86.7%, which was improved to 92.9%, using the RF Opt model. The accuracy score of the LGB algorithm was 95.2% which was a best score in the algorithms. Other models such as KNN, MLP, SGD, SVM, and LogR also had excellent performance, with accuracy ranging from 81.3-91.6%.

The relative importance of various 54 TS features to the RF Opt and LGB models, such as the total energy for the initial coordinates and momenta, the velocity between the center of mass of HCO⁺ and H₂O, bond lengths, bond angles, dihedral angles, mass-weighted displacement (MWD), and velocity (MWV) for each normal mode, are shown in Fig. 4a and b. The numbers in parentheses for each feature represent the

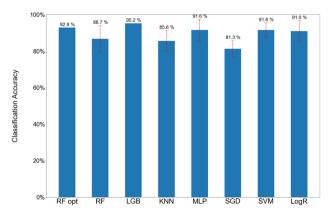


Fig. 3 Accuracy scores in the binary classification for the 298 K classical simulation

numbered atoms: H1, H2, H3, O4, O5, and C6 (see Fig. 5a). Fig. 4 was constructed based on the data set having 83 dissociation trajectories of each CO + H₃O⁺ and HCO⁺ + H₂O dissociation. Note that Fig. S5 and S6 (ESI†) present comparable accuracy scores and feature importance distributions composed from three different subsets of the data which are 60, and 40 of each dissociation channel. This indicates that the number of trajectories was sufficient to generate a reliable result. Both of Fig. 4a and b derived from the RF and LGB models, which have 92.9% and 95.2% accuracy scores, show the similar representative significant features. Notice that these scores are the test scores not training scores, which indicates that the models have avoided overfitting. The angle \angle (H1-O5-O4) is presented as the most important feature. The motion of H1, which possesses the lightest weight among H1, O5, and O4, is important for the bifurcation reaction. In Fig. 4, the importance to the MWDs of modes 6 and 7, and to the MWV of mode 8, also demonstrate the significant features in the classification. The normal mode vectors for modes 6, 7, and 8 (shown in Fig. 5) consist of a considerable H1 motion contribution. The bond distance between O5 and C6, and the velocity between the center of mass of HCO^+ and H_2O , $\vec{\nu}_{HCO^+}\!\!-\!\!\vec{\nu}_{H_2O}$, are also important features in the classification, as shown in Fig. 4. Fig. S7 (ESI†) displays the accuracy scores for the most relevant six features for each algorithm. The high accuracy scores suggest that these six features are important in the binary classification. In this case, most representative features were also the ∠(H1-O5-O4) for both of RF and LGB models. At 4000 K,

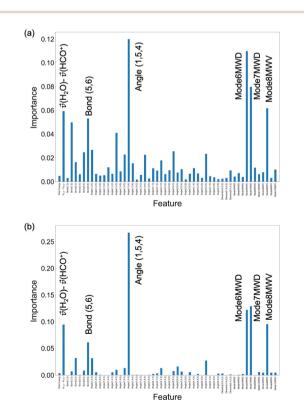


Fig. 4 Importance of 54 TS features with respect to the 298 K classical simulation derived from the (a) RF Opt and (b) LGB models.

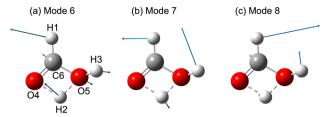


Fig. 5 Normal mode vectors at the TS_{1-2} for (a) mode 6, Q_6 with the atom numbering, (b) mode 7, Q_7 , and (c) mode 8, Q_8

significant features (as seen in Fig. S8 in the ESI†) are not present in the dynamics, indicating that it is difficult to classify the trajectories at this temperature. This suggests that interactions between vibrational modes occur efficiently during the branching process at higher temperatures.

Significant features for the bifurcation reaction

Fig. 6 shows the normalized distribution of the most relevant six features of the CO + H₃O⁺ and HCO⁺ + H₂O dissociation trajectories for the 298 K classical MD simulation. As shown in Fig. 6a, the initial configurations with wider and narrower angles of \angle (H1-O5-O4) contribute to dissociation into HCO⁺ + H_2O and $CO + H_3O^+$, respectively. The large velocity of mode 8, which is correlated with the opening motion of \angle (H1–O5–O4), also represents dissociation into HCO+ + H2O, as shown in Fig. 6b. Fig. 6c and d show that negative displacement of modes 6 and 7 (see Fig. 5) contributes to HCO⁺ + H₂O dissociation. The negative vector directions of modes 6 and 7 are consistent with the positive direction of mode 8. The results suggest that structures of HCO+ that are almost linear play a role in the HCO⁺ + H₂O dissociation process, despite the H1 atom getting close to H₂O. This is a counter-intuitive bifurcation process that can be revealed through ML analysis without human intuition. Fig. 6 shows the normalized distribution as a function of the data set for the most relevant six features of the CO + H₃O⁺ and HCO⁺ + H₂O dissociation trajectories for the 298 K classical MD simulation. In Fig. 6e, the data shows that the initial configuration with a shrinking O5-C6 bond distance is important for the dissociation into the HCO⁺ + H₂O fragment. This suggests that the repulsive potential energy of the O5-C6 bond plays a role in guiding the trajectories toward a higher potential energy than the HCO⁺ + H₂O dissociation channel. Fig. 6f shows the velocity distribution of $\vec{v}_{HCO^+} - \vec{v}_{H_2O}$. Both the $HCO^+ + H_2O$ and CO + H₃O⁺ dissociation have stretching velocities, but the lower stretching velocities dissociate to the HCO⁺ + H₂O instead of the higher velocities. This is also a counter-intuitive branching. The results indicate the large $\vec{v}_{HCO^+} - \vec{v}_{H,O}$ velocity at t = 0 fs is insignificant to the HCO+ + H2O dissociation process. All Fig. 6a-f demonstrate feature overlap, implying that the dissociation dynamics are not dependent only on a single mode.

Conclusion

We investigated the dissociation processes of the (HCOOH)H⁺ molecule from the TS using three types of molecular dynamics

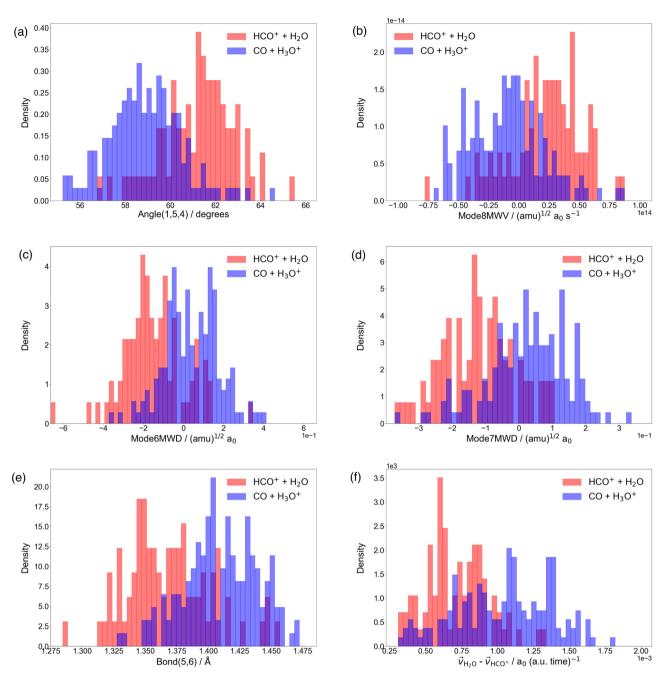


Fig. 6 Normalized distribution for the (a) H1-O5-O4 bond angle, (b) mass-weighted velocity for mode 8, (c) MWD for mode 6, (d) MWD for mode 7, (e) O5-C6 bond distance, and (f) velocity between the center of mass of HCO⁺ and H₂O at the TS₁₋₂. Red and blue bars represent the feature distribution with respect to the $HCO^+ + H_2O$ and $CO + H_3O^+$ dissociation trajectories of the classical MD simulations at 298 K.

simulations: QCT, classical MD, and RPMD at temperatures of 298, 1000, 2000, and 4000 K. The effects of temperature were considered in relation to the large excess energies from the proton affinity of (HCOOH)H⁺. The dissociation into HCO⁺ + H_2O , which has a higher potential energy (40.8 kcal mol⁻¹) than the CO + H₃O⁺ dissociation channel (19.2 kcal mol⁻¹), increases as the temperature increases. We found that the branching fractions of the QCT are significantly different from the fractions obtained in other classical MD and RPMD simulations. The initial coordinates and momenta used in the QCT include

the excess energy necessary to describe the vibrational quantization in classical particles, but this ZPE leakage phenomenon leads to inaccurate branching. The HCO⁺ + H₂O branching fractions obtained from the three types of simulations at 298 K were underestimated the experimental results. It could be provisionally evaluated that the direct dissociation process after the protonation contributes the product ratio. We will perform the development of more accurate PES to obtain a more quantitative branching fraction then report elsewhere the discussion.

Paper PCCP

We used ML analysis to determine which features at the TS strongly contribute to the HCO⁺ + H₂O dissociation. Good results were obtained for the binary classification of the HCO⁺ + H₂O and CO + H₃O⁺ dissociation trajectories using the RF Opt, RF, LGB, KNN, MLP, SGD, SVM, and LogR algorithms in relation to 298 K classical simulations. The feature importance for the classical MD simulations at 298 K was determined by the RF Opt model. We found that the initial configuration of the linear HCO⁺ and O5-C6 shrinking, and the initial velocity of the stretching direction between the center of mass of HCO⁺ and H₂O are significantly important for the HCO+ + H₂O dissociation process. In this study, ML analysis proved vital for identifying bifurcation reaction selectivity from TS features.

Author contributions

TM and TT devised and supervised the project. TT acquired the funding. TM, SI, YH, and TT designed the methodology. TM, SI, YH, and YK performed the calculations. TM, SI, YH, and YK analyzed and visualized the data. TM, SI, YH, and TT verified the methods and the results. TM and TT wrote the original draft and edited and reviewed it.

Conflicts of interest

There are no conflicts to declare.

Appendix A. Canonical ensemble for one-dimensional harmonic oscillator

The one-dimensional classical Hamiltonian for harmonic oscillator of α th mode is expressed as eqn (22):

$$H(Q_{\alpha}, P_{\alpha}) = \frac{P_{\alpha}^{2}}{2} + \frac{1}{2}\omega_{\alpha}^{2}Q_{\alpha}^{2}.$$
 (A1)

The partition function Z_c of a classical representation is defined as

$$Z_{c} = \int \frac{dP_{\alpha}dQ_{\alpha}}{h} \exp\left[-\beta \left(\frac{P_{\alpha}^{2}}{2} + \frac{1}{2}\omega_{\alpha}^{2}Q_{\alpha}^{2}\right)\right]$$

$$= \frac{1}{h} \left(\frac{2\pi}{\beta}\right)^{1/2} \left(\frac{2\pi}{\beta\omega_{\alpha}^{2}}\right)^{1/2}$$

$$= \frac{1}{\beta\hbar\omega_{c}},$$
(A2)

where h is Planck constant with the relation $\hbar = \frac{h}{2\pi}$. The internal energy $\langle U_c \rangle$ therefore becomes

$$\langle U_{c} \rangle = -\frac{\partial}{\partial \beta} \ln Z$$

$$= \frac{1}{\beta}.$$
(A3)

In contrast, the quantum expression of the Hamiltonian is

written as

$$H_{\alpha} = \frac{1}{2} \left(-\hbar^2 \frac{\partial^2}{\partial Q_{\alpha}^2} + \omega_{\alpha}^2 Q_{\alpha}^2 \right). \tag{A4}$$

The well-known energy representation solved by the timeindependent Schrödinger equation is

$$E_{n_{\text{vib}}}^{(\alpha)} = \hbar \omega_{\alpha} \left(n_{\text{vib}} + \frac{1}{2} \right) \quad (n_{\text{vib}} = 0, 1, 2, \cdots), \tag{A5}$$

where $n_{\rm vib}$ is the vibrational quantum number. The partition function Z_q for the quantum harmonic oscillator is represented by

$$Z_{\rm q} = \sum_{n_{\rm vih}=0}^{\infty} {\rm e}^{-\beta E_{n_{\rm vib}}^{(z)}} = \frac{{\rm e}^{-\beta\hbar\omega_z/2}}{1 - {\rm e}^{-\beta\hbar\omega_z}}, \tag{A6}$$

with some linear algebra. The temperature-dependent internal energy $\langle U_{\rm q} \rangle$ for the quantum representation is described as

$$\langle U_{\mathbf{q}} \rangle = -\frac{\partial}{\partial \beta} \ln Z$$

$$= \hbar \omega_{\alpha} \left[\frac{1}{e^{\beta \hbar \omega_{\alpha}} - 1} + \frac{1}{2} \right]. \tag{A7}$$

The internal energy $\langle U_{\rm q} \rangle$ depends on temperature and the vibrational frequency while the energy $\langle U_c \rangle$ is the only temperature-dependent parameter. The probability $P_{\alpha}^{(n_{\text{vib}})}$ of populating the state n_{vib} with energy $E_{n_{\text{vib}}}^{(\alpha)}$ can be represented as

$$P_{\alpha}^{(n_{\text{vib}})} = \frac{\exp\left(-\beta E_{n_{\text{vib}}}^{(\alpha)}\right)}{Z_{\text{q}}}.$$
 (A8)

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Notes and references

- 1 J. L. Neill, A. L. Steber, M. T. Muckle, D. P. Zaleski, V. Lattanzi, S. Spezzano, M. C. McCarthy, A. J. Remijan, D. N. Friedel, S. L. Widicus Weaver and B. H. Pate, J. Phys. Chem. A, 2011, 115, 6472-6480.
- 2 P. Ehrenfreund, L. d'Hendecourt, S. Charnley and R. Ruiterkamp, J. Geophys. Res.: Planets, 2001, 106, 33291-33301.
- 3 D. Smith, P. Spanel and T. J. Millar, Mon. Not. R. Astron. Soc., 1994, **266**, 31-34.
- 4 D. A. Fairley, G. B. I. Scott, C. G. Freeman, R. G. A. R. Maclagan and M. J. McEwan, J. Chem. Soc., Faraday Trans., 1996, 92, 1305-1309.
- 5 M. Ohishi, S.-i Ishikawa, T. Amano, H. Oka, W. M. Irvine, J. E. Dickens, L. M. Ziurys and A. J. Apponi, Astrophys. J., 1996, 471, L61-L64.

6 G. I. Mackay, A. C. Hopkinson and D. K. Bohme, J. Am. Chem. Soc., 1978, 100, 7460-7464.

- 7 G. I. Mackay, S. D. Tanner, A. C. Hopkinson and D. K. Bohme, Can. J. Chem., 1979, 57, 1518-1523.
- 8 O. Sekiguchi, V. Bakken and E. Uggerud, J. Am. Soc. Mass Spectrom., 2004, 15, 982-988.
- 9 S. G. Lias, J. F. Liebman and R. D. Levin, J. Phys. Chem. Ref. Data, 1984, 13, 695-808.
- 10 E. P. L. Hunter and S. G. Lias, J. Phys. Chem. Ref. Data, 1998, 27, 413-656.
- 11 S. E. Sanni, P. A. Alaba, E. Okoro, M. Emetere, B. Oni, O. Agboola and A. O. Ndubuisi, Sustainable Energy Technol. Assess., 2021, 45, 101078.
- 12 E. Herbst, Annu. Rev. Phys. Chem., 1995, 46, 27-53.
- 13 NIST Chemistry Webbook, https://www.nist.gov.
- 14 T. Oka, Chem. Rev., 2013, 113, 8738-8761.
- 15 H. Eyring, J. Chem. Phys., 1935, 3, 107.
- 16 J. L. Bao and D. G. Truhlar, Chem. Soc. Rev., 2017, 46, 7548-7596.
- 17 S. Maeda, Y. Harabuchi, Y. Ono, T. Taketsugu and K. Morokuma, Int. J. Quantum Chem., 2015, 115, 258-269.
- 18 J. Rehbein and B. K. Carpenter, Phys. Chem. Chem. Phys., 2011, 13, 20906-20922.
- 19 D. H. Ess, S. E. Wheeler, R. G. Iafe, L. Xu, N. Çelebi-Ölçüm and K. N. Houk, Angew. Chem., Int. Ed., 2008, 47, 7592-7601.
- 20 S. R. Hare and D. J. Tantillo, Pure Appl. Chem., 2017, 89, 679-698.
- 21 S. Pratihar, X. Ma, Z. Homayoon, G. L. Barnes and W. L. Hase, J. Am. Chem. Soc., 2017, 139, 3570-3590.
- 22 Z. Yang and K. N. Houk, Chem. Eur. J., 2018, 24, 3916-3924.
- 23 Z. Yang, X. Dong, Y. Yu, P. Yu, Y. Li, C. Jamieson and K. N. Houk, J. Am. Chem. Soc., 2018, 140, 3061-3067.
- 24 B. K. Carpenter, Annu. Rev. Phys. Chem., 2005, 56, 57-89.
- 25 T. H. Peterson and B. K. Carpenter, J. Am. Chem. Soc., 1992, 114, 766-767.
- 26 J. Zheng, E. Papajak and D. G. Truhlar, J. Am. Chem. Soc., 2009, 131, 15754-15760.
- 27 S. Lee and J. M. Goodman, J. Am. Chem. Soc., 2020, 142, 9210-9219.
- 28 S. Lee and J. M. Goodman, Org. Biomol. Chem., 2021, 19, 3940-3947.
- 29 N. Bulut, A. Aguado, C. Sanz-Sanz and O. Roncero, J. Phys. Chem. A, 2019, 123, 8766-8775.
- 30 S. Habershon and D. E. Manolopoulos, J. Chem. Phys., 2009, 131, 244518.
- 31 G. Czakó, A. L. Kaledin and J. M. Bowman, J. Chem. Phys., 2010, 132, 164103.
- 32 I. R. Craig and D. E. Manolopoulos, J. Chem. Phys., 2004, **121**, 3368-3373.
- 33 I. R. Craig and D. E. Manolopoulos, J. Chem. Phys., 2005, 122, 084106.
- 34 I. R. Craig and D. E. Manolopoulos, J. Chem. Phys., 2005, **123**, 034102.
- 35 T. F. Miller III and D. E. Manolopoulos, J. Chem. Phys., 2005, 123, 154504.

- 36 S. Habershon, D. E. Manolopoulos, T. E. Markland and T. F. Miller III, Annu. Rev. Phys. Chem., 2013, 64, 387-413.
- 37 R. Pérez De Tudela, F. J. Aoiz, Y. V. Suleimanov and D. E. Manolopoulos, J. Phys. Chem. Lett., 2012, 3, 493-497.
- 38 R. Pérez De Tudela, Y. V. Suleimanov, J. O. Richardson, V. Sáez Rábanos, W. H. Green and F. J. Aoiz, J. Phys. Chem. Lett., 2014, 5, 4219-4224.
- 39 Y. V. Suleimanov, R. Collepardo-Guevara D. E. Manolopoulos, J. Chem. Phys., 2011, 134, 044131.
- 40 Y. V. Suleimanov, J. Phys. Chem. C, 2012, 116, 11141-11153.
- 41 Y. V. Suleimanov, R. Pérez De Tudela, P. G. Jambrina, J. F. Castillo, V. Sáez-Rábanos, D. E. Manolopoulos and F. J. Aoiz, Phys. Chem. Chem. Phys., 2013, 15, 3655-3665.
- 42 Y. V. Suleimanov, W. J. Kong, H. Guo and W. H. Green, J. Chem. Phys., 2014, 141, 244103.
- 43 Y. V. Suleimanov, F. J. Aoiz and H. Guo, J. Phys. Chem. A, 2016, 120, 8488-8502.
- 44 J. W. Allen, W. H. Green, Y. Li, H. Guo and Y. V. Suleimanov, J. Chem. Phys., 2013, 138, 221103.
- 45 J. Espinosa-Garcia, A. Fernandez-Ramos, Y. V. Suleimanov and J. C. Corchado, J. Phys. Chem. A, 2014, 118, 554-560.
- 46 K. M. Hickson, J. C. Loison, H. Guo and Y. V. Suleimanov, J. Phys. Chem. Lett., 2015, 6, 4194-4199.
- 47 Y. Li, Y. V. Suleimanov and H. Guo, J. Phys. Chem. Lett., 2014, 5, 700-705.
- 48 E. Gonzalez-Lavado, J. C. Corchado, Y. V. Suleimanov, W. H. Green and J. Espinosa-Garcia, J. Phys. Chem. A, 2014, 118, 3243-3252.
- 49 P. del Mazo-Sevillano, A. Aguado, E. Jiménez, Y. V. Suleimanov and O. Roncero, J. Phys. Chem. Lett., 2019, 10, 1900-1907.
- 50 P. del Mazo-Sevillano, A. Aguado and O. Roncero, J. Chem. Phys., 2021, 154, 094305.
- 51 K. Saito, Y. Hashimoto and T. Takayanagi, J. Phys. Chem. A, 2021, 125, 10750-10756.
- 52 H. Suzuki, T. Otomo, K. Ogino, Y. Hashimoto and T. Takayanagi, ACS Earth Space Chem., 2022, 6, 1390-1396.
- 53 T. Murakami, R. Iida, Y. Hashimoto, Y. Takahashi, S. Takahashi and T. Takayanagi, J. Phys. Chem. A, 2022, 126, 9244-9258.
- 54 R. Ramakrishnan, P. O. Dral and M. Rupp, J. Chem. Theory Comput., 2015, 11, 2087-2096.
- 55 P. O. Dral, A. Owens, A. Dral and G. Csányi, J. Chem. Phys., 2020, 152, 204110.
- 56 A. Nandi, C. Qu, P. L. Houston, R. Conte and J. M. Bowman, J. Chem. Phys., 2021, 154, 051102.
- 57 S. Du, X. Wang, R. Wang, L. Lu, Y. Luo, G. You and S. Wu, Phys. Chem. Chem. Phys., 2022, 24, 13399-13410.
- 58 N. Rollins, S. L. Pugh, S. M. Maley, B. O. Grant, R. S. Hamilton, M. S. Teynor, R. Carlsen, J. R. Jenkins and D. H. Ess, J. Phys. Chem. A, 2020, 124, 4813-4826.
- 59 S. M. Maley, J. Melville, S. Yu, M. S. Teynor, R. Carlsen, C. Hargis, R. S. Hamilton, B. O. Grant and D. H. Ess, Phys. Chem. Chem. Phys., 2021, 23, 12309-12320.
- 60 J. Melville, C. Hargis, M. T. Davenport, R. S. Hamilton and D. H. Ess, J. Phys. Org. Chem., 2022, 35, e4405.

Paper

61 Z. Xie and J. M. Bowman, J. Chem. Theory Comput., 2010, 6,

- 26-34.
- 62 A. Nandi, C. Qu and J. M. Bowman, J. Chem. Theory Comput., 2019, 15, 2826-2835.
- 63 S. Grimme, C. Bannwarth and P. Shushkov, J. Chem. Theory Comput., 2017, 13, 1989-2009.
- 64 C. Bannwarth, S. Ehlert and S. Grimme, J. Chem. Theory Comput., 2019, 15, 1652-1671.
- 65 C. Bannwarth, E. Caldeweyher, S. Ehlert, A. Hansen, P. Pracht, J. Seibert, S. Spicher and S. Grimme, Wiley Interdiscip. Rev.: Comput. Mol. Sci., 2021, 11, e1493.
- 66 M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, J. A. Montgomery, Jr, T. Vreven, K. N. Kudin, J. C. Burant, J. M. Millam, S. S. Iyengar, J. Tomasi, V. Barone, B. Mennucci, M. Cossi, G. Scalmani, N. Rega, G. A. Petersson, H. Nakatsuji, M. Hada, M. Ehara, K. Toyota, R. Fukuda, J. Hasegawa, M. Ishida, T. Nakajima, Y. Honda, O. Kitao, H. Nakai, M. Klene, X. Li, J. E. Knox, H. P. Hratchian, J. B. Cross, Bakken, C. Adamo, J. Jaramillo, R. Gomperts, R. E. Stratmann, O. Yazyev, A. J. Austin, R. Cammi, C. Pomelli, J. W. Ochterski, P. Y. Ayala, K. Morokuma, G. A. Voth, P. Salvador, J. J. Dannenberg, V. G. Zakrzewski, S. Dapprich, A. D. Daniels, M. C. Strain, O. Farkas, K. Malick, A. D. Rabuck, K. Raghavachari,

J. B. Foresman, J. V. Ortiz, Q. Cui, A. G. Baboul,

Clifford, J. Cioslowski, B. B. Stefanov, G. Liu,

- A. Liashenko, P. Piskorz, I. Komaromi, R. L. Martin, D. J. Fox, T. Keith, M. A. Al-Laham, C. Y. Peng, A. Nanayakkara, M. Challacombe, P. M. W. Gill, B. Johnson, W. Chen, M. W. Wong, C. Gonzalez and J. A. Pople, Gaussian 09, Gaussian, Inc., Wallingford, CT, 2009.
- 67 Semiempirical Extended Tight-Binding Program Package xtb Ver. 6.5.1, https://github.com/grimme-lab/xtb.
- 68 J. M. Millam, V. Bakken, W. Chen, W. L. Hase and H. B. Schlegel, J. Chem. Phys., 1999, 111, 3800-3805.
- 69 A. Witt, S. D. Ivanov, M. Shiga, H. Forbert and D. Marx, J. Chem. Phys., 2009, 130, 194510.
- 70 M. Shiga, J. Comput. Chem., 2022, 43, 1864-1879.
- 71 W. C. Swope, H. C. Andersen, P. H. Berens and K. R. Willson, J. Chem. Phys., 1982, 76, 637-649.
- 72 S. Nosé, Mol. Phys., 1984, 52, 255-268.
- 73 W. G. Hoover, Phys. Rev. A: At., Mol., Opt. Phys., 1985, 31, 1695-1697.
- 74 G. J. Martyna, M. L. Klein and M. Tuckerman, J. Chem. Phys., 1992, 97, 2635-2643.
- 75 M. Shiga, PIMD Ver. 2.4.0, https://ccse.jaea.go.jp/software/ PIMD/index.en.html, 2020.
- 76 L. Bonnet, Int. Rev. Phys. Chem., 2013, 32, 171-228.
- 77 C. Doubleday, M. Boguslav, C. Howell, S. D. Korotkin and D. Shaked, J. Am. Chem. Soc., 2016, 138, 7476-7479.
- 78 M. T. Tremblay and Z. J. Yang, J. Phys. Org. Chem., 2022, 35, e4322.