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## Untangling product selectivity on clean low index rutile $\text{TiO}_2$ surfaces using first-principles calculations†

Anum Shahid Malik and Lisa A. Fredin  \*

Computational modeling of metal oxide surfaces provides an important tool to help untangle complex spectroscopy and measured catalytic reactivity. There are many material properties that make rational catalytic design challenging, and computational methods provide a way to evaluate possible structural factors, like surface structure, individually. The mechanism of water oxidation or oxygen evolution is well studied on some anatase surfaces and the rutile  $\text{TiO}_2$  (110) surface but has not yet been mapped on other low-index Miller rutile surfaces that are present in most experimental nano-titania catalysts. Here first principles calculations provide new insights into water oxidation mechanisms and reactivity of the most common low-index Miller facets of rutile  $\text{TiO}_2$ . The reactivity of three surfaces, (101), (010), and (001), are explored for the first time and the product selectivity of multistep electron transfer on each surface is compared to the well-studied (110) surface. Density functional theory shows that a peroxy,  $\text{O}^{(\text{P})}$ , intermediate is more favorable for water oxidation on all facets. The  $\cdot\text{OH}$  radical formation is favored on the (001) facet resulting in a high overpotential for oxygen evolution reaction (OER). The (101) and (110) facets have low overpotentials,  $\sim 0.3$  V, and favor two-electron proton-coupled electron transfer to produce  $\text{H}_2\text{O}_2$ . The only facet that prefers direct OER is (001), leading to  $\text{O}_2$  evolution in a four-electron process with an overpotential of 0.53 V. A volcano plot predicts the selectivity and activity of low-index Miller facets of rutile  $\text{TiO}_2$ , revealing the high activity of the peroxy OER mechanism on the (010) facet.

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### 1. Introduction

Photocatalytic water splitting *via* solid-state materials might provide an inexpensive way to generate energy from renewable resources.<sup>1–3</sup> Early active photocatalysts were developed using sacrificial reagents for either  $\text{H}_2$  or  $\text{O}_2$  evolution.<sup>4</sup> However, discovering the ideal material capable of spontaneously achieving the two reactions remains a major challenge. In particular, semiconductor-based photocatalysts with multiple facets allow important properties to be tuned, like light absorption, mobility of charge carriers, and their driving force to the water solution.<sup>5–8</sup> An ideal material will have a large enough band gap to absorb a large amount of sunlight,<sup>9,10</sup> while the valence band maximum (VBM) and conduction band minimum (CBM) must lie energetically below  $\text{O}_2/\text{H}_2\text{O}$  and above  $\text{H}^+/\text{H}_2$  potentials to drive holes for water oxidation and electrons for reducing  $\text{H}^+$ , respectively.<sup>11</sup>

Titanium dioxide ( $\text{TiO}_2$ ) is one of the most used materials in heterogeneous photocatalysis because of its strong stability under different conditions.<sup>12,13</sup> Rutile  $\text{TiO}_2$ 's wide band gap of 3.0 eV, makes it a UV light-responsive material, and the number of different stable facets allow for a range of activity for different reactants.<sup>14,15</sup> The overpotential of multiple water oxidation mechanisms has been investigated on the rutile  $\text{TiO}_2$  (110) surface, which is considered to be the most stable facet.<sup>16–18</sup> Specifically, the amount of energy required to drive each step beyond the equilibrium potential, known as overpotential,<sup>19–22</sup> provides a good metric of surface reactivity. The photo-oxidation of water on defect-free rutile (110) surfaces has been broadly explored,<sup>19,21,23–31</sup> as well as, direct prediction of OER on rutile (110) with subsurface oxygen vacancies,<sup>32–42</sup> multiple surface coverages,<sup>19,29,43,44</sup> and metal nanoclusters<sup>45–50</sup> adsorbed on the surface provides a detailed picture of its reactivity.

In contrast, other terminations of rutile  $\text{TiO}_2$  that are experimentally accessible and have received much less attention. In particular, understanding the photocatalytic activity, especially the effect on yields, rates, or selectivity, of the lower index surfaces has been largely overlooked.<sup>51</sup> Initially, these surfaces were not explored by computational scientists because surface

Department of Chemistry, Lehigh University, Bethlehem, PA 18015, USA.

E-mail: [lafredin@lehigh.edu](mailto:lafredin@lehigh.edu)

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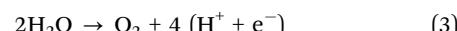
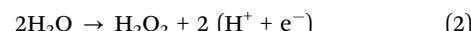
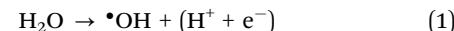
energy calculations show that they are less stable than the (110) surfaces, with stability decreasing  $(100)^{52-54} > (101)^{55-58} > (001)^{58-61}$  which is correlated to the density of undercoordinated surface sites.<sup>18</sup> A recent article that calculated the electronic structures of hydroxylated low-index surfaces of rutile and anatase titanium dioxide, suggested that hydroxyl-bridged surfaces have a lot of potential for photo-electrocatalysis but did not directly assess the catalytic performance of these low-index facets.<sup>62</sup> In the absence of studies identifying the role of each crystal facet in photocatalytic redox reactions, the understanding of photo-oxidation of water by nano-titania is incomplete as only 64% of particle surfaces are (110).<sup>63-65</sup> Thus, computational studies that can separately calculate the properties of each surface are critical to understanding the reactivity of experimental nanostructures.

An important consideration whenever generating models of catalytic surfaces is the stability of those surfaces, especially under catalytic conditions. It is well known that some low-index facets of anatase  $\text{TiO}_2$ , in particular (101),<sup>66</sup> reconstruct significantly. In general, very little surface reconstruction is seen when rutile surfaces are optimized using DFT.<sup>18</sup> However, while rutile is a more stable phase in general, there is experimental evidence for the reconstruction of atomically flat rutile (001) above 750 °C.<sup>67</sup> This is not surprising as stoichiometric (001) has a surface step edge. This edge in the ⟨001⟩ can either be a row of in-plane Ti atoms<sup>68</sup> or in-plane oxygen atoms.<sup>69</sup> Scanning tunneling microscopy has shown that the (001) rutile surfaces synthesized have bright rows on the surface<sup>70</sup> that can be assigned to the surface oxygen rows. When (001) rutile surfaces terminated with in-plane oxygens rather than raised bridging oxygens have been optimized no reconstruction is observed.<sup>23</sup>

A second structural consideration in modeling metal oxide catalysis is atomic vacancies observed in experimental materials.<sup>54-56,71-74</sup> Due to the minimal surface disorder seen in rutile crystals and DFT, most studies of rutile,<sup>75-77</sup> both (110) and other surfaces, focus on oxygen vacancies and surface coverages.<sup>78,79</sup> When adsorbed species are more stable than bare surfaces, this type of surface coverage can be thought of as a surface reconstruction. Typically, the dissociation of species on surfaces in a water environment are adsorbed oxygen species like hydroxyl-bridges.<sup>62</sup> Before computational effort is invested in fully exploring the reactivity of other low-index surfaces of rutile  $\text{TiO}_2$ , a detailed understanding of the complex oxidation of water on each stoichiometric surface is required.

Of the two half-reactions of water splitting, the oxidation step is the most challenging due to the coupling of 4 electron and proton transfers and the creation of an oxygen–oxygen ( $\text{O}_2$ ) bond.<sup>80</sup> One major issue contributing to catalytic inefficiency is side reactions leading to unproductive products or products that directly block active sites. In particular, water oxidation could lead to  $\cdot\text{OH}$  radicals,  $\text{H}_2\text{O}_2$ , or  $\text{O}_2$  evolution electrochemically or photoelectrochemically.<sup>20</sup> These three half-cell reactions that lead to the above-mentioned products depend on the number of electrons transferred, 1, 2, or 4 electrons. The formation energy of  $\cdot\text{OH}$  in the aqueous phase from  $\text{H}_2\text{O}$  (eqn (1)) at pH = 0 is 2.4 V.<sup>81</sup> When  $\Delta G_{\text{OH}^*} > 2.4$  eV, water

oxidation occurs *via* the one-electron process resulting in the formation of unproductive  $\cdot\text{OH}$ . In a two-electron process, the amount of energy required for the production of  $\text{H}_2\text{O}_2$  in the aqueous phase (eqn (2)) is 1.76 V.<sup>82</sup> When  $\Delta G_{\text{OH}^*} < 2.4$  eV and  $\Delta G_{\text{O}^*} > 3.5$  eV at pH = 0,  $\text{H}_2\text{O}_2$  is formed. If  $\Delta G_{\text{OH}^*} < 2.4$  eV and  $\Delta G_{\text{O}^*} < 3.5$  eV at pH = 0, water oxidation would undergo the four-electron process to the desired  $\text{O}_2$  evolution. The required energy for the production of  $\text{O}_2$  in the aqueous phase from  $\text{H}_2\text{O}$  is 1.23 V.<sup>82</sup>



This work uses computational catalytic tools to predict solar-to-chemical energy conversion on the four low-index Miller surfaces of rutile  $\text{TiO}_2$ , (110), (101), (010), and (001) (Fig. S1, ESI†). First-principle calculations can predict the redox potentials of multielectron proton-coupled electron transfer mechanisms on each facet. Unlike experimental reactivity, density functional theory (DFT) allows the mechanism through two distinct reactive intermediates, *i.e.*, dangling  $\text{O}^*$  and surface-bound peroxy  $\text{O}^*$  denoted as  $(\text{O}^{(\text{d})})$  and  $(\text{O}^{(\text{p})})$ , to be examined separately. The structure of each surface and the intermediates and thermodynamic analysis of the free energy for the three possible products, *i.e.*,  $\cdot\text{OH}/\text{H}_2\text{O}_2/\text{O}_2$ , provide insights into the selectivity of these understudied surfaces. This work provides experimentalists with design guidelines for faceted  $\text{TiO}_2$  crystalline nanomaterials that should enhance photocatalytic water oxidation by identifying the most suitable facets for OER and criteria for product selectivity.

## 2. Computational methodology

Spin-polarized density functional theory (DFT) characterized the intermediates for OER activity of the rutile  $\text{TiO}_2$  (001), (101), (110), and (010) surfaces. For the structure determination, the Perdew–Burke–Ernzer (PBE) parameterizations of the exchange and correlation potential in the generalized gradient approximation (GGA)<sup>83</sup> as applied in the Vienna *Ab Initio* Simulation Package (VASP) code was adopted.<sup>84,85</sup> To expand the electronic wave function, and valence configurations of the atoms:  $3s^23p^64s^23d^2$  for Ti's (12 valence electrons),  $2s^22p^4$  for O's (6 valence electrons), and 1s for H (1 valence electron) with PAW potentials to account for the core electrons a plane-wave energy cutoff of 400 eV was applied. The self-consistent DFT energies convergence criterion was  $10^{-4}$  eV with a force on each atom of  $0.01$  eV  $\text{\AA}^{-1}$ . The bulk rutile with tetragonal symmetry of  $\text{TiO}_2$  was cleaved along the (001), (101), (110), and (010) surfaces to form stoichiometric and symmetric slabs. A  $2 \times 2 \times 1$  supercell was used for calculations. The slabs thickness were set to four Ti layers, and the vacuum length was 15  $\text{\AA}$ . The bottom Ti layer was fixed while the other three Ti layers were allowed to relax. The optimized lattice parameters are  $a = 18.41 \text{\AA}$ ,  $b = 9.20 \text{\AA}$ ,  $c = 20.16 \text{\AA}$  and  $\alpha = \beta = 90.00^\circ$ ,  $\gamma = 90.32^\circ$  for (001),  $a = 21.85 \text{\AA}$ ,  $b = 9.18 \text{\AA}$ ,  $c = 23.97 \text{\AA}$ , and  $\alpha = \beta = \gamma = 90.00^\circ$  for (101),

$a = 11.80 \text{ \AA}$ ,  $b = 12.99 \text{ \AA}$ ,  $c = 24.45 \text{ \AA}$ , and  $\alpha = \beta = \gamma = 90.00^\circ$  for (110), and  $a = 11.76 \text{ \AA}$ ,  $b = 9.51 \text{ \AA}$ ,  $c = 31.12 \text{ \AA}$  and  $\alpha = \beta = \gamma = 90.00^\circ$  for (010). After complete optimization of slabs, we chose the Ti metal atom as an active site on the surface and the OER intermediates ( $\text{OH}^*$ ,  $\text{O}^{(\text{d})}$ ,  $\text{O}^{(\text{p})}$ , and  $\text{OOH}^*$ ) were adsorbed at a Ti-O bond length of 2.00  $\text{\AA}$  and again allowed to relax. For sampling the Brillouin zone, a  $\Gamma$ -centered  $3 \times 2 \times 1$   $k$ -point mesh was used based on the Monkhorst-Pack scheme.<sup>86</sup> All reported energetics and electronic density of states were calculated using HSE06.<sup>87</sup> Photoexcitation is accounted for as an initial potential provided by the photoexcited electron in the first reaction step as explained in the scheme for free energy profile calculations for OER given in the ESI.<sup>†</sup>

### 3. Results and discussion

The rutile polymorph of titania is composed of  $\text{TiO}_6$  octahedra, which are arranged to form edge-sharing chains along the [001] direction and are corner-sharing in the (001) plane. The surface orientations determine how these octahedra are cut at each of the four low-index Miller surfaces (110), (101), (010), and (001) (Fig. 1) resulting in a variation of local geometry and coordination number for the stoichiometric surface atoms. On the lowest energy rutile surface, (110) (Fig. 1), half of the Ti atoms are five-coordinated ( ${}^{[5]}_{\text{Ti}}$ , where  ${}^{[n]}_{\text{A}}$  is a  $n$ -coordinated atom of A) and the other half are  ${}^{[6]}_{\text{Ti}}$  along the [001] surface rows, these  ${}^{[6]}_{\text{Ti}}$  have additional bridging surface oxygen atoms ( ${}^{[2]}_{\text{O}}$ ) joining them, completing their octahedral coordination. In contrast, the rutile (010) surface has only  ${}^{[5]}_{\text{Ti}}$  atoms, with surface  ${}^{[2]}_{\text{O}}$  atoms bridging them (Fig. 1). On the (110) surface the bridging Ti-O bonds are perpendicular to the surface plane while on the (010) surface the bridging oxygens are inclined at an angle to the surface ( $61^\circ$  in the relaxed stoichiometric structure). The (101) surface also has only  ${}^{[5]}_{\text{Ti}}$  with bridging  ${}^{[2]}_{\text{O}}$ . However, while on both the (010) and (101)

surfaces the  ${}^{[5]}_{\text{Ti}}$  lie at the center of the base  $\text{TiO}_5$  square pyramids that are slanted from the surface normal. On the (101) surface the ( $-\text{O}-\text{Ti}-\text{O}-\text{Ti}-$ ) chains are zigzagged along the [101] direction, giving the  $\text{TiO}_5$  square pyramids alternating tilts (Fig. 1). When truncated to the (101) surface, the bulk  $\text{TiO}_6$  octahedra form rows where long and short Ti-O bonds have been removed, forming chains of alternating enantiomeric Ti surface sites. The (001) surface exhibits alternating O and Ti rows in the [110] direction, with alternating  ${}^{[6]}_{\text{Ti}}$  and  ${}^{[4]}_{\text{Ti}}$  (Fig. 1). The  ${}^{[6]}_{\text{Ti}}$  surface metal sites occupy the center of  $\text{TiO}_6$  octahedra, whereas the elimination of two oxygen atoms leads to the relaxation of the octahedron to a distorted tetrahedral  ${}^{[4]}_{\text{Ti}}$ . Each (001) surface O atom is bonded to one  ${}^{[4]}_{\text{Ti}}$  and one  ${}^{[6]}_{\text{Ti}}$ . The diverse coordination of Ti and O is known to result in a range of surface energies; (110) < (010) < (101) < (001),<sup>17,38</sup> matching well with the formation energies per atom of each unit cell (Table S8, ESI<sup>†</sup>). The density of states (DoS, Fig. S6, ESI<sup>†</sup>) of each surface show that their valence bands are all composed of O (2p) orbitals and their conduction bands are mostly comprised of Ti (3d) orbitals. In addition, all of the plots showed a shift in the Fermi energy ( $E_f$ ) toward the valence band edge with a typical rutile band gap of  $\sim 3$  eV.

Here we directly measure the effect of surface chemistry on water-splitting catalytic properties. The multistep proton-coupled electron transfer (PCET) processes for one-, two-, and four-electron transfer reactions (eqn (1)–(3)) are considered for each surface. The (110) surface has been well explored<sup>19,21,23–31</sup> and is included here for direct comparison, but all the results are consistent with previous DFT studies on the bare surface. The detailed PCET mechanism is shown in Section 1 of the SI. For both the peroxy and dangling oxygen mechanisms the free energies of  $\text{OH}^*$  and  $\text{O}^*$  were calculated (Table 1). It is striking that the lowest possible energy mechanism on all the facets goes through the surface-bound peroxy  $\text{O}^*$  (Table 1), denoted as  $\text{O}^{(\text{p})}$ . This is important as this mechanism is often overlooked in favor of the similar but less plausible dangling  $\text{O}^*$  intermediate, signified as  $\text{O}^{(\text{d})}$  (Fig. 2). The formation energy of each intermediate adsorbed on the surfaces is within DFT error of the surface formation energy and about  $2 \times s$  ( $\sim -4.5$  eV) more favorable than the dissociation energy of water (5.15 eV).

For  $\text{O}_2$  evolution, the rate-determining step is  ${}^*\text{OH}$  for the (001), (101), and (110) surfaces, whereas, the rate on (010) is determined through the last  $\text{O}_2$  evolution. The surface adsorption of  $\text{OH}^*$  is the first step in OER, and its energy and charge transfer (as determined by a  $\sim 0.41$  to 0.48 e<sup>−</sup> Bader charge, Table S6, ESI<sup>†</sup>) remains the same for all mechanisms. This step is lowest in energy on the (010) surface at 1.04 eV (Fig. 3). Loss of the proton to generate  $\text{O}^*$  is the branching point for the  $\text{O}^{(\text{d})}$  vs.  $\text{O}^{(\text{p})}$  mechanisms (each mechanism is labeled as surface<sup>(intermediate)</sup>). Each mechanism only has one newly adsorbed surface oxygen, however in the peroxy mechanism the  $\text{O}^*$  forms a bond with an existing surface oxygen.  $\text{O}^{(\text{p})}$  formation is more favorable for all facets and is significantly lower in energy on (010) ( $\sim 1$  eV) than all the other surfaces. This is probably due to the charge transfer to the dangling  $\text{O}^{(\text{d})}$  intermediates as compared to the newly adsorbed oxygen in the peroxy  $\text{O}^{(\text{p})}$ .

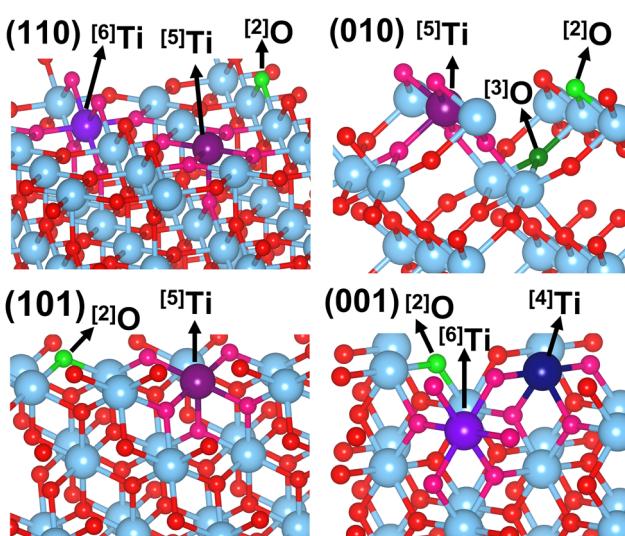
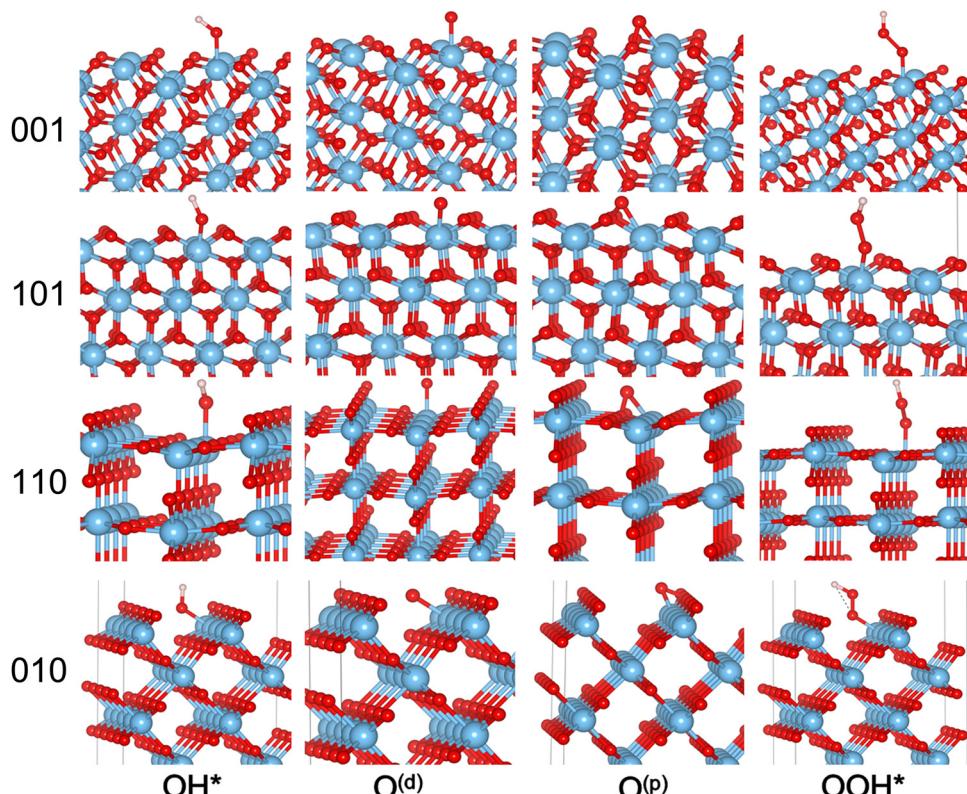


Fig. 1 Rutile (110), (010), (101), and (001) surfaces and surface atom coordination (dark blue  ${}^{[4]}_{\text{Ti}}$ , dark purple  ${}^{[5]}_{\text{Ti}}$ , light purple  ${}^{[6]}_{\text{Ti}}$ , and bright green  ${}^{[2]}_{\text{O}}$ , dark green  ${}^{[3]}_{\text{O}}$ ) on each. Red atoms are O and light blue are Ti.

**Table 1** Free energies relative to the resting state  ${}^*+2\text{H}_2\text{O}$  for  $(\Delta G_{\cdot})$ ,  $\text{OH}^*$  ( $\Delta G_{\text{OH}^*}$ ),  $\text{O}^{(\text{d})}$  ( $\Delta G_{\text{O}^{(\text{d})}}$ ),  $\text{O}^{(\text{p})}$  ( $\Delta G_{\text{O}^{(\text{p})}}$ ),  $\text{OOH}^*$  ( $\Delta G_{\text{OOH}^*}$ ), and  $\text{O}_2$  ( $\Delta G_{\text{O}_2}$ ) and overpotentials  $\eta$  through four-, two- and one-electron ( $\text{O}_2/\text{H}_2\text{O}_2/\text{OH}$  evolution) processes for all surfaces and mechanisms, labeled surface  ${}^{\text{intermediate}}$ . The rate-limiting step for each mechanism is bolded

Mechanism	$\Delta G_{\text{OH}^*}$	$\Delta G_{\text{O}^{(\text{d})}}$	$\Delta G_{\text{O}^{(\text{p})}}$	$\Delta G_{\text{OOH}^*}$	$\Delta G_{\text{O}_2}$	Product	R.D.S	$\eta$ (V) $1\text{e}^-$	$\eta$ (V) $2\text{e}^-$	$\eta$ (V) $4\text{e}^-$
001 <sup>(d)</sup>	2.99	5.19	—	6.02	4.92	$\cdot\text{OH}$	$\text{OH}^*$	1.76	—	—
001 <sup>(p)</sup>	2.99	—	4.72	6.02	4.92	$\cdot\text{OH}$	$\text{OH}^*$	1.76	—	—
101 <sup>(d)</sup>	2.13	4.66	—	5.47	4.92	$\text{H}_2\text{O}_2$	$\text{O}^*$	—	0.77	1.30
101 <sup>(p)</sup>	2.13	—	4.01	5.47	4.92	$\text{H}_2\text{O}_2$	$\text{OH}^*$	—	0.37	0.90
110 <sup>(d)</sup>	1.99	4.55	—	4.48	4.92	$\text{H}_2\text{O}_2$	$\text{O}^*$	—	0.80	1.33
110 <sup>(p)</sup>	1.99	—	3.64	4.48	4.92	$\text{H}_2\text{O}_2$	$\text{OH}^*$	—	0.23	0.76
010 <sup>(d)</sup>	1.04	3.40	—	3.16	4.92	$\text{O}_2$	$\text{O}^*$	—	—	1.13
010 <sup>(p)</sup>	1.04	—	1.76	3.16	4.92	$\text{O}_2$	$\text{O}_2$	—	—	0.53



**Fig. 2** Optimized structures of Rutile (110), (010), (101), and (001) and their four possible OER intermediates.

intermediates, thus lowering the binding energies of the peroxy mechanism. Interestingly, some of the peroxy  $\text{O}^*$  charge seems to be shared with its bonded surface oxygen (Table S6, ESI†) proving that peroxy species is preferable on defect-free  $\text{TiO}_2$  surface which is in good agreement with previous studies.<sup>23,24</sup>

Adsorption of a second OH leading to an  $\text{OOH}^*$  depends on the energy and mechanism of the  $\text{O}^*$  step. The observed charge transfer is  $\sim 0.94$  to  $1.49$  to the  $\text{OOH}^*$  on all surfaces. Interestingly, the dangling mechanism on the (010) and (110) surfaces has a downhill  $\text{OOH}^*$  step. This however isn't enough to make the dangling mechanism more favorable overall. While the step energies for the two mechanisms are very different (Table S3, ESI†), according to Sabatier's principle<sup>88</sup> of reactivity, catalytic

activity is actually a balance between strong and weak interactions between the substrate and the catalyst.

For the  $\cdot\text{OH}$  formation 1-electron process, all of the surfaces have the same overpotential. For the  $\text{H}_2\text{O}_2$  formation 2-electron process,  $110^{(\text{p})}$  has the lowest overpotential of  $0.23$  V, followed by  $101^{(\text{p})}$  at  $0.37$  V with  $\text{OH}^*$  as the rate-limiting step, for both. Four-electron  $\text{O}_2$  evolution through the  $010^{(\text{p})}$  has the least overpotential of  $0.53$  V. Interestingly, among all surfaces (010) showed highest charge transfer from surface to intermediates supporting high photocatalytic activity of this surface.

The product selectivity map<sup>20,21</sup> (Fig. 4) compares the relative free energies of  $\text{OH}^*$  and  $\text{O}^*$  to the reaction equilibrium potentials for  $\text{H}_2\text{O}_2$ ,  $\text{O}_2$ , and  $\cdot\text{OH}$  formation. None of the surfaces predict a different product for the two mechanisms.

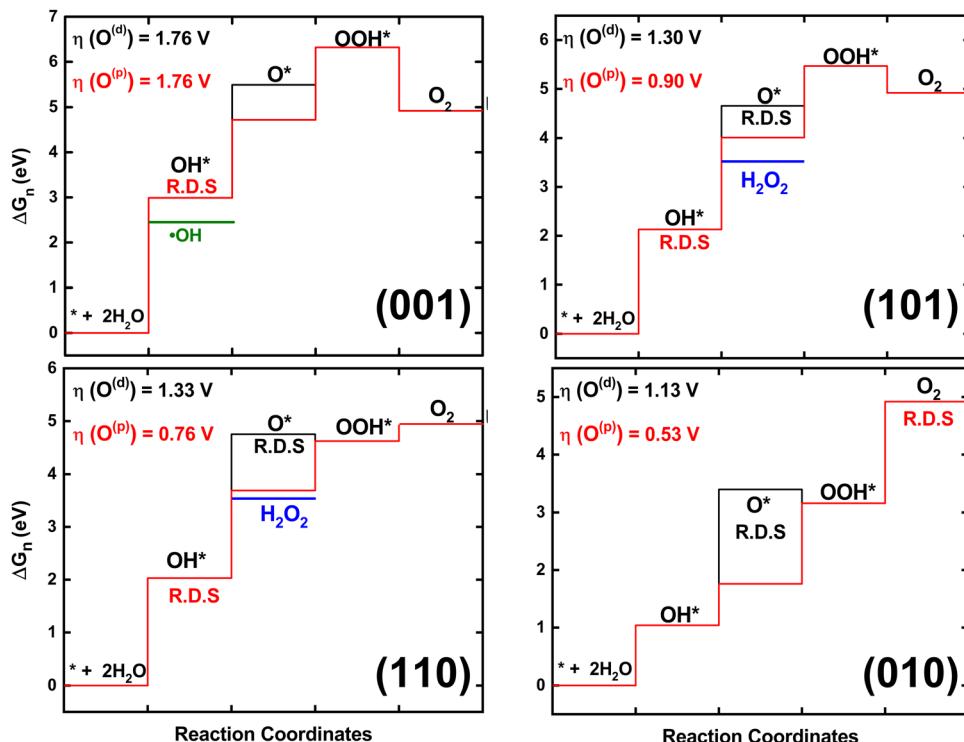


Fig. 3 Free energy profiles and overpotential of OER on stoichiometric (001), (101), (110), and (010) rutile through dangling  $O^{(d)}$  (black) and peroxy  $O^{(p)}$  (red) intermediates under no external potential. The rate-determining step (R.D.S.) is marked and  $H_2O_2$  formation (blue) and  $^*OH$  formation (green) are shown for relevant surfaces.

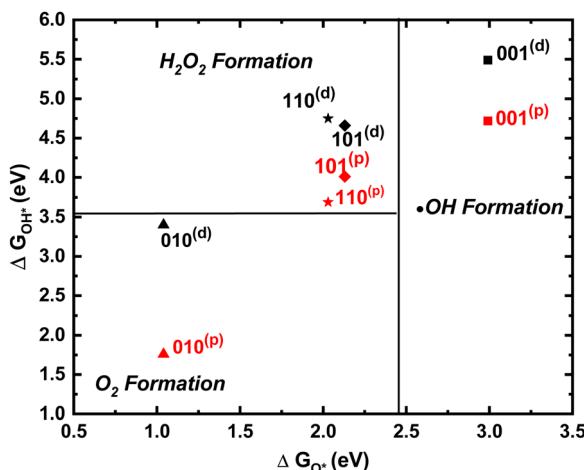


Fig. 4 Phase diagram for product selectivity for rutile (001), (101), (110), and (010) surfaces. Black and red show dangling and peroxy mechanisms, respectively.

Instead,  $^*OH$  formation is favored on (001),  $H_2O_2$  formation for (110) and (101), while only  $O_2$  evolution is preferred for (001). Interestingly, rutile 110<sup>(p)</sup> is adjoining the  $O_2$  evolution boundary, indicating that with very little added energy (110) could evolve  $O_2$ . Importantly, under irradiation, the redox potential of photogenerated holes in the valence band is almost equal to the band gap (over  $\sim 3$  eV) making all three mechanisms ( $1e^-$ ,  $2e^-$ , and  $4e^-$ ) realistic on all these surfaces. Water

oxidation gates most easily on (110) and (101) through the formation of  $H_2O_2$ . On the (001) surface however  $^*OH$  formation likely makes the surface unproductive for  $O_2$  evolution.

Because these reactions occur in the presence of water and involve protons moving at many steps, pH plays a role in the reactivity. In particular, the energy of every step is modulated by pH. By using a pH-dependent reference electrode, the calculated overpotential can directly account for the effect of pH on surface reactivity.<sup>17,21,89–91</sup> While a pH of 14 (pH = 0 in Table 1) alters the binding energies of the reaction intermediates (Table S3, ESI†) and affects the threshold values for the  $1e^-$ ,  $2e^-$ , and  $4e^-$  processes, it does not affect the selectivity and overpotential of OER on each surface.

Volcano plots have been extensively used for the analysis of OER activity of different oxide systems.<sup>92–94</sup>  $\Delta G_{O^*} - \Delta G_{OH^*}$  provides a computational metric of OER activity<sup>95</sup> that can predict the activity of various catalysts. Plotting the negative value of calculated overpotential ( $-\eta$ , activity) as a function of this metric for each of the facets considered here leads to a volcanic relationship (Fig. 5). The top of the volcano shows the best OER activity with the lowest overpotential for 010<sup>(p)</sup>. It is clear in the volcano plot that the overpotential depends strongly on the mechanism for each surface, *i.e.*  $O^{(d)}$  or  $O^{(p)}$ . Among all the facets (001) results in the highest overpotential indicating that this facet is least active for water oxidation. This is in good agreement with previous studies that show (001) is unstable, with high surface energy and experimental reconstruction.<sup>96–98</sup>

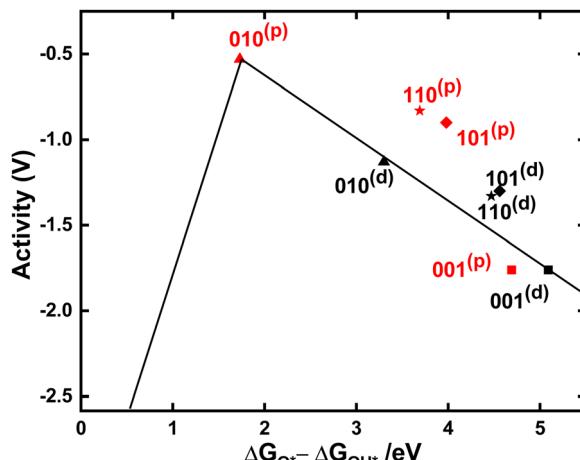


Fig. 5 Volcano plot ( $-\eta$  vs.  $\Delta G_{O^*} - \Delta G_{OH^*}$ ) for the oxygen evolution reaction on low-indexed  $TiO_2$  surfaces explored in this study. The data points are grouped with black color for dangling  $O^{(d)}$  and red color for peroxy  $O^{(p)}$ .

However, these results show clearly that other low-indexed facets, beyond the well-studied (110), should be considered for water oxidation. In particular,  $010^{(p)}$  is more reactive and  $101^{(p)}$  is almost as reactive as than  $110^{(p)}$ .

## 4. Conclusions

This work provides the first direct calculations of water oxidation on low-index rutile  $TiO_2$  facets, (001), (101), and (101), using DFT. This work provides new insights into water oxidation mechanisms and reactivity of various low-index Miller facets of rutile  $TiO_2$ . In particular, water oxidation proceeds through the peroxy intermediate on all of these stoichiometric facets. The (001) facet resulted in high overpotential for OER leading to  $^{\bullet}OH$  radical formation. A two-electron process to produce  $H_2O_2$  is favored on the (101) and (110) facets with fairly low overpotentials,  $\sim 0.3$  V, for OER. The only facet that prefers direct OER is (010), with an overpotential of 0.53 V. These results are supported *via* a volcano plot which predicts the high activity of a peroxy mechanism of OER on the (010) facet. Critically, these results show that facets beyond the well-studied (110) may play a role in measured reactivity and should be explored further to better understand the effect of surface coverage and oxygen vacancies.

## Conflicts of interest

The authors declare that they have no competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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