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Cr-doped Al_2O_3 -YAG binary and Al_2O_3 -YAG- ZrO_2 ternary eutectic materials crystallized by the micro pulling down technique and their characterization

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Cr-doped Al_2O_3 -YAG and Al_2O_3 -YAG- ZrO_2 eutectic ceramics rods of 3 mm in diameter were solidified from the melt by a micro-pulling down (μ -PD) technique. The Cr dopant affects the microstructure, morphology, and lattice parameters of the as-grown eutectics. As a function of the dopant, the coloration, morphology, microstructure, and luminescence were investigated. Whatever the Cr-dopant concentration, mainly two phases (Al_2O_3 -YAG) in the case of the binary system and three phases (Al_2O_3 -YAG- ZrO_2) in the case of the ternary system were observed. The Chinese script microstructure and colony boundaries are observed in ternary eutectics. Al_2O_3 and YAG phases show faceted morphologies, but for the ZrO_2 phase, growth tends to a weakly faceted manner and forms rods or lamellae. The hydrostatic stress of binary eutectics is less than that of ternary eutectics with same Cr dopant concentration due to the distribution of ZrO_2 particles in the microstructure affected by residual stresses. The spectroscopic properties of the Cr-doped binary and ternary eutectic show that Cr^{3+} ions exist in both Al_2O_3 and YAG phases in octahedral sites.

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1. Introduction

Color eutectic ceramic materials have aroused great attention in the innovation applications of light-emitting diodes (LEDs), watch pointers, and jewelry decoration; it is required to be produced in higher quantities with better economic attributes.^{1–4} The colored (red, blue, yellow, *etc.*) ceramics can be used in jewelry and luxury items and can substitute some specific crystals such as ruby.

The eutectic ceramic materials offer technical characteristics in the quality of hard material and not only scratch resistance, biocompatibility, insensitivity to any chemical attack, resistance to friction and abrasion but also aesthetic advantages intended for dressing applications.^{5–7} The Al_2O_3 -YAG binary and Al_2O_3 -YAG- ZrO_2 ternary systems^{8–11} are among the eutectic ceramic materials that are identified to be the most important composite materials due to directional and rapid solidification from the melt.^{12,13} The high melting temperature >1500 °C allows them to work

stably in an oxidizing environment due to inherent chemical-physical properties.¹⁴ They present excellent mechanical properties that are heavily dependent on the microstructure, morphology, and crystallographic orientations^{15,16} and are considered potential engineering materials. It is evident that controlling the uniform microstructure of the eutectic ceramics in the binary or ternary systems is related to the directional solidification behavior that depends on the solidification methods and specific composition in the equilibrium diagram.^{17–21}

Chromium oxides can be used in ceramics because they are characterized by a large variety of colors. Therefore, chromium is an element of choice for obtaining colored minerals since it colors many compounds in red, purple, or green. It is, in most cases, in the form of Cr^{3+} in octahedral symmetry. Chromium is a transition metal of electronic configuration $\text{Cr}^0 [\text{Ar}] 4s^2 3d^4$, which gives it a wide variety of possible degrees of oxidation from 0 to +6.²² However, oxidation states +3 and +6 are the most commonly encountered in minerals and glasses. Cr^{3+} gives rise to many colors; it is mainly found in octahedral geometry in minerals and is notably not only responsible for the green color of the emerald and red color of ruby but can also give purple as in stichtite.^{23,24} The presence of Cr^{3+} in a more or less distorted octahedral geometry results in the presence of two main absorption bands in the visible range of its optical spectrum.

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The observed energy shifts of the absorption bands of Cr^{3+} between the different minerals explain different colorations since the transmission window in the visible range is modified with these displacements. By the analysis of ruby and the emerald, Vauquelin *et al.*²⁵ discovered that chromium is responsible for the respective red and green colors of these two minerals.

The synthesis of colored eutectic ceramic compounds is not well controlled. For example, despite all efforts, it has never before been possible to produce eutectic ceramics bright red color used for jewelry and watch pivot. The aim of this paper is, in particular, to propose red colored Cr-doped Al_2O_3 -YAG and Al_2O_3 -YAG- ZrO_2 eutectic ceramic materials solidified by the micro-pulling down (μ -PD) technique, allowing significant expansion of the range of possible colors in the production of colored eutectic ceramic materials.

2. Experimental procedure

2.1 Crystal growth conditions

The starting materials were made from commercial high-purity (>99.99%), Cr_2O_3 , Al_2O_3 , Y_2O_3 and ZrO_2 powders. The powders were mixed in agate mortar at eutectic proportion according to the binary (80 mol% Al_2O_3 /20 mol% Y_2O_3) and the ternary (65 mol% Al_2O_3 /16 mol% Y_2O_3 /19 mol% ZrO_2) eutectic composition. The detailed compositions of different prepared materials and references are shown in Table 1. The mixture was sintered at 1500 °C for 24 h in an air atmosphere. Eutectic ceramic rods were solidified from the melt using the micro-pulling down technique presented in previous work.^{11,13,15,21} An iridium crucible is used, and it is tapped in its lower part with a capillary die of 3 mm in diameter. The crucible is enclosed in a chamber swept with an oxygen-free argon stream and is charged with eutectic ceramic raw materials. The crucible is brought to a temperature of 1750 °C \pm 2 °C using a high frequency generator operating at 11 kHz and having a continuous power output of 25 kW. When a pendant drop forms at the bottom of the capillary channel (Fig. 1), it is connected with a rod of eutectic ceramic of selected composition with a diameter of 2 mm to serve as the seed. When the drops weld to the seed, the seed is pulled down at a rate of 0.3 mm min^{-1} . A CCD camera was used to take inset a live picture through a small circular window (Fig. 1). High-purity flowing argon was used to prevent oxidation of the iridium crucible and after heater crucible support.

Table 1 The different compositions used for melt solidification

Binary eutectic (Al_2O_3 (80%)/ Y_2O_3 (20%))				
Sample (reference)	Cr BE1	Cr BE2	Cr BE3	Cr BE4
Dopant	1.9 at%	1.5 at%	0.7 at%	0.4 at%
Ternary eutectic (Al_2O_3 (65%)/ Y_2O_3 (16%)/ ZrO_2 (19%))				
Sample (reference)	Cr TE1	Cr TE2	Cr TE3	Cr TE4
Dopant	1.9 at%	1.5 at%	0.7 at%	0.4 at%

2.2 Characterization methods

2.2.1. XRD phase analysis and scanning electron microscopy. Room-temperature X-ray diffraction patterns were obtained using a Bruker D8 advanced diffractometer with $\text{Cu-K}\alpha_1$ and $\text{Cu-K}\alpha_2$ X-rays ($\lambda = 0.15406$ and 0.15444 nm). The diffraction diagram is scanned over a 2θ range from 15° to 70° in steps of 0.02° with a counting time of 1 s per step and continuous rotation (20 rpm) for measurement. In order to investigate the formation and evolution of microstructures, the eutectic samples were cut and polished along the longitudinal and transversal, and the pieces of about 2 to 10 mm in length were embedded in organic resin. SEM observations of the polished samples were performed with a Phenom desktop scanning electron microscope (SEM) at 5 kV.

2.2.2. Spectroscopic characterizations. The fluorescence lines of ruby single crystals are used to evaluate the residual stresses in the solidified rods and the displacement of the fluorescence line of chromium (Cr^{3+}) is measured. A 473 nm laser wavelength has been used as an excitation source and focused on the surface of the polished samples through a 50× Olympus MIR plan objective with 0.25 NA in order to cover a larger sample area. For each sample, 121 points of measurement are taken on different areas of the polished transversal and longitudinal section. All the measured spectra are fitted using a Gaussian profile in order to determine the exact peak positions of Cr^{3+} fluorescence lines.

The emission spectra were registered at room (RT) and liquid nitrogen temperatures by exciting the crystals with an EKSPLA NT342B tunable OPO (Optical Parametric Oscillator) pumped by a pulsed and frequency-tripled Nd:YAG laser delivering 7 ns laser pulses. Emission signals were dispersed and detected in the visible range with the aid of a SHAMROCK 350 monochromator equipped with both 300 line per mm and 1200 line per mm gratings, and an ANDOR ICCD gated detector. The high temperature measurements were performed using a LINKAM SCIENTIFIC cell DSC600 with an analogous photo-luminescence set-up.

The fluorescence decay measurements were performed by using the same laser excitation sources and a Jobin-Yvon HRS1 monochromator and by analyzing the signals with the help of R928 AsGa (RESEARCH Inc.) photomultiplier tubes coupled with a Wave Runner 64Xi LECROY digital scope, for the visible and NIR spectral ranges, respectively. The excitation spectra of Cr-doped Al_2O_3 -YAG (binary system) and Al_2O_3 -YAG- ZrO_2 (ternary system) eutectics in the range from 285 to 680 nm are recorded at room temperature with the help of an EDINBURGH Instruments FS5 spectrofluorimeter.

3. Result and discussion

3.1 Eutectic solidification and phase's characterization

As a function of the composition, the Cr doped binary (Al_2O_3 -YAG) and ternary (Al_2O_3 -YAG- ZrO_2) eutectic ceramic rods solidified from the melt are shown in Fig. 2. They were crystallized under the stationary stable regime. Except for the



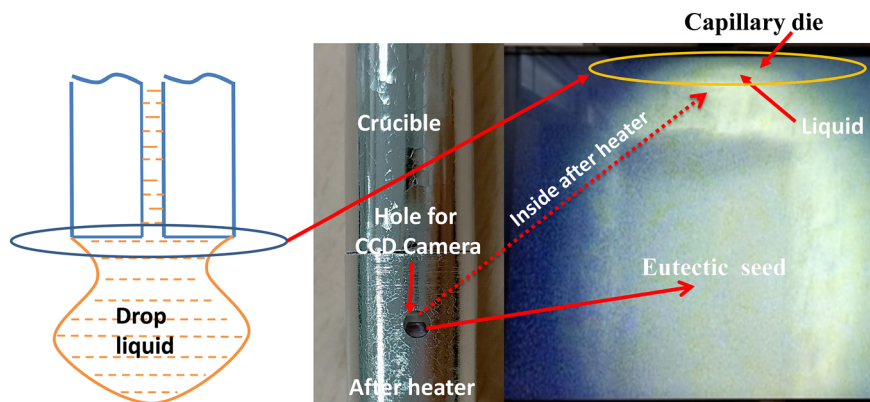


Fig. 1 Schematic illustration of the drop at the bottom of the capillary die (left), CCD camera vision of the growth initiation through the crucible and after heater (right).

CrTE4 (0.4% Cr) sample, the Cr doped eutectic ceramic rods have a stable diameter of 3 mm. Whatever the system (binary or ternary), the red color contrast increases with increasing Cr concentration. The variation in color coordinates (x , y) as presented in the CIE-1931 chromaticity diagram (Fig. 3) shows that various red colors can be obtained by varying Cr concentration in the eutectic ceramics. The ceramics eutectics rods corresponding to high Cr concentration (1.9% Cr) have a strong red color close to the blood color. The surface of the samples is smooth without any visible macroscopic defects such as cracks or bubbles. Fig. 4a and b show the XRD diagram of the eutectic ceramics as a function of Cr concentration for the binary and the ternary systems. The grinding of the material makes it possible to overcome the phenomena of texturing and distortion of cells due to the internal stresses of the material at room temperature. The YAG is identified as the majority phase in both systems. In the case of the Cr-doped Al_2O_3 -YAG binary system, only Al_2O_3

and YAG phases are observed. Additional cubic ZrO_2 phase was crystallized in the case of the Cr-doped Al_2O_3 -YAG- ZrO_2 ternary system. We did not register the presence of YAlO_3 perovskite phase or inclusions belonging to the Al_2O_3 , Y_2O_3 , and Cr_2O_3 oxides, indicating that Cr ion doping did not create impurity phases or induce significant changes in the structure architecture. Table 2 presents the lattice parameters as a function of the Cr concentration. In the case of the YAG phase, whatever the system (binary or ternary), we registered a slight increase in the lattice parameter (a). The YAG has a garnet structure with Y^{3+} occupying a dodecahedral site and Al^{3+} ions occupying octahedral and tetrahedral sites, respectively.²⁶ The cells containing eight groups form $\text{Y}_3\text{Al}_2\text{-Al}_3\text{O}_{12}(\text{X}_3\text{Y}_2\text{Z}_3\text{O}_{12})$. The X, Y, and Z sites cations respectively occupy positions 24c, 16a, and 24d, and the anions are located at the positions 96 h. The chromium (located on the Y sites) is, therefore, at oxidation state 3 and has a punctual

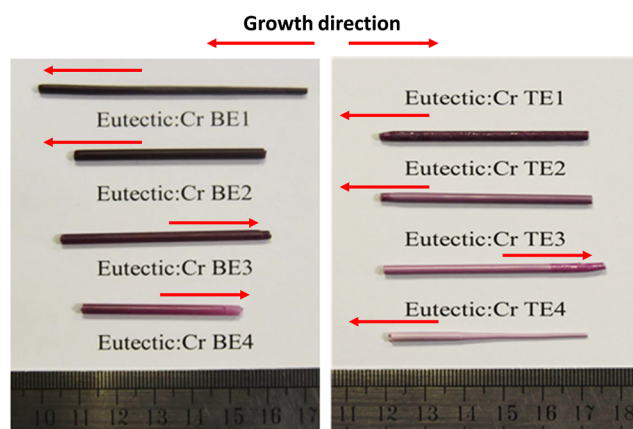


Fig. 2 Cr-doped eutectic ceramics solidified from the melt by μ -PD (pulling rate 0.3 mm min^{-1}). CrBE1: Al_2O_3 -YAG binary (Cr = 1.9 at%). CrBE2: Al_2O_3 -YAG binary (Cr = 1.5 at%). CrBE3: Al_2O_3 -YAG binary (Cr = 0.7 at%). CrBE4: Al_2O_3 -YAG binary (Cr = 0.4 at%). CrTE1: Al_2O_3 -YAG- ZrO_2 ternary (Cr = 1.9 at%). CrTE2: Al_2O_3 -YAG- ZrO_2 ternary (Cr = 1.5 at%). CrTE3: Al_2O_3 -YAG- ZrO_2 ternary (Cr = 0.7 at%). CrTE4: Al_2O_3 -YAG- ZrO_2 ternary (Cr = 0.4 at%).

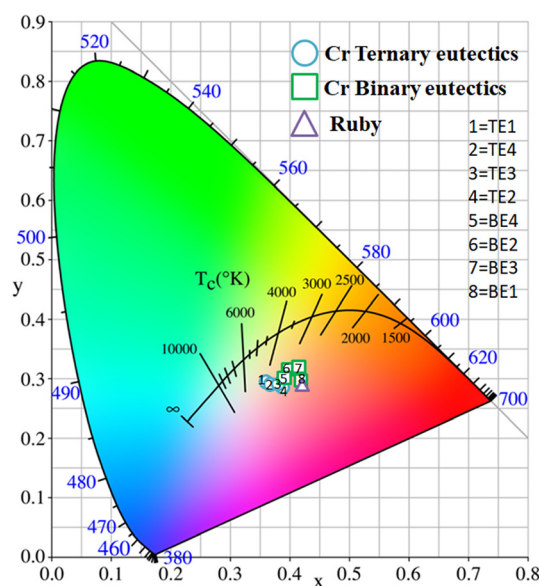


Fig. 3 CIE-1931 chromaticity diagram as a function of Cr concentration in the binary and the ternary eutectics.



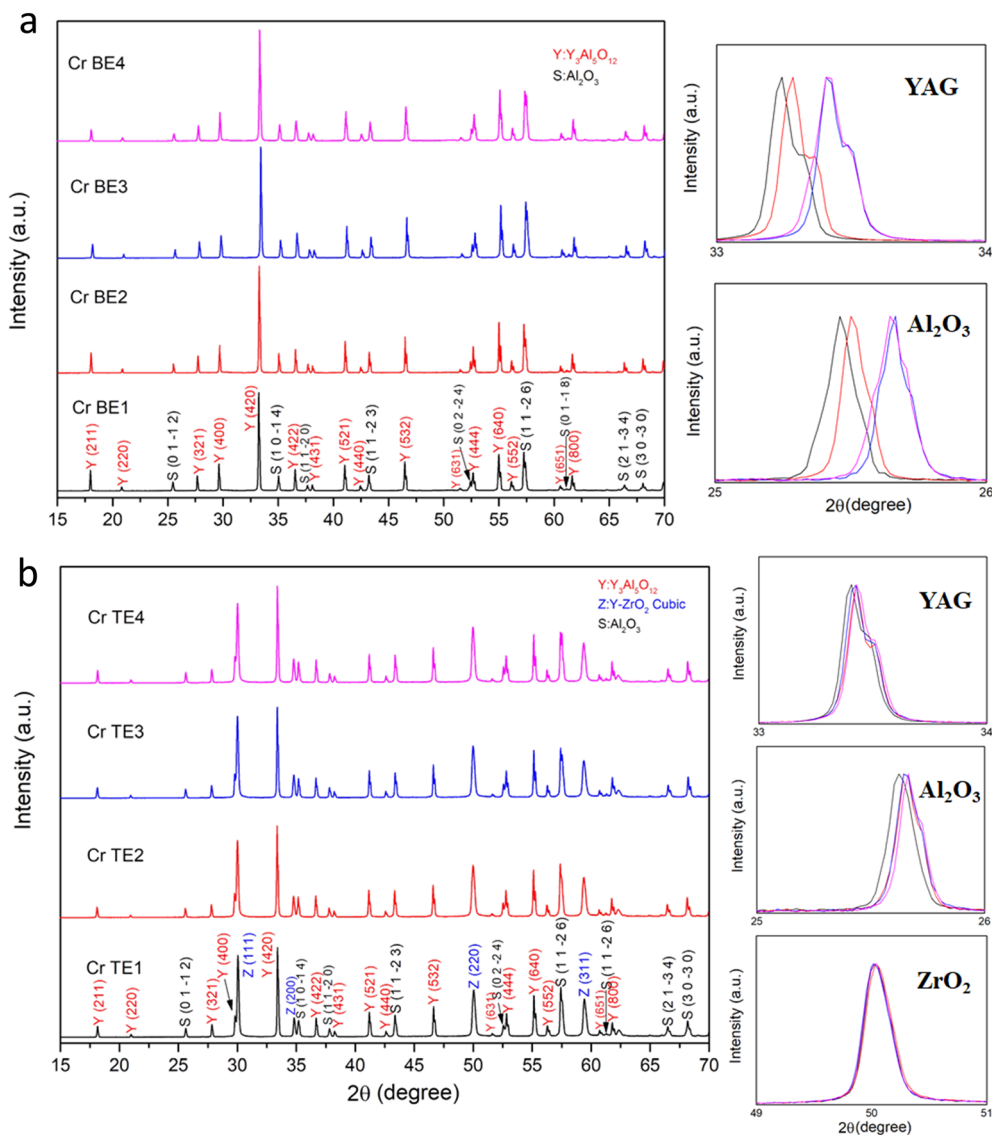


Fig. 4 X-ray diffraction evolution as a function of Cr dopant concentration, (a) Al_2O_3 –YAG binary system and (b) Al_2O_3 –YAG– ZrO_2 ternary system.

symmetry 3^- or C_{3i} in Schönflies notation. The Cr^{3+} substitutes Al^{3+} in a small trigonally distorted octahedral site with C_j symmetry.²⁷ The structure of Al_2O_3 is the same as that of Cr_2O_3 . These two compounds form a complete solid solution, $\text{Al}_{2-x}\text{Cr}_x\text{O}_3$, by substitution of aluminum by

chromium in the octahedral site. The solid solution changes color with the chromium concentration. The introduction of a few tens of ppm of chromium replacing aluminum produces a characteristic pink color. The color intensifies with increasing chromium concentration, and as soon as the latter exceeds a few 0.7 at% for both binary and ternary systems, the compounds acquire a strong red component. The color change of compounds is mainly due to changes in the parameter of the crystal field Δ_0 .^{28,29} Chromium dopant involved in the coloration is essentially in the form of Cr^{3+} in more or less distorted octahedral symmetry. In addition, the broad absorption band peaking at 560 nm in the visible range is increasing with the Cr concentration, then for the highest Cr concentration, the absorption at the edge of this band for wavelength higher than 600 nm is also increasing, giving the sample a deep red color. Both binary and ternary eutectic ceramic rods contained the Cr-doped $\alpha\text{-Al}_2\text{O}_3$ phase belonging to the solid solution $\text{Al}_{2-x}\text{Cr}_x\text{O}_3$. Whatever the Cr

Table 2 Lattice parameters of Cr doped Al_2O_3 –YAG/ Al_2O_3 –YAG– ZrO_2 as a function of the dopant concentration

	Al_2O_3 $R\bar{3}c$ (Å)	$\text{Y}_3\text{Al}_5\text{O}_{12}$ $Ia\bar{3}d$ (Å)	ZrO_2 $Fm\bar{3}m$ (Å)
PDF files	$a = 4.7585, c = 12.9906$	$a = 12.0020$	
Cr BE1	$a = 4.7648, c = 13.0074$	$a = 12.0139$	
Cr BE2	$a = 4.7624, c = 12.9999$	$a = 12.0110$	
Cr BE3	$a = 4.7624, c = 13.0017$	$a = 12.0130$	
Cr BE4	$a = 4.7608, c = 12.9935$	$a = 12.0094$	
Cr TE1	$a = 4.7650, c = 13.0072$	$a = 12.0123$	$a = 5.1605$
Cr TE2	$a = 4.7642, c = 13.0037$	$a = 12.0135$	$a = 5.1619$
Cr TE3	$a = 4.7611, c = 12.9957$	$a = 12.0093$	$a = 5.1625$
Cr TE4	$a = 4.7602, c = 12.9955$	$a = 12.0084$	$a = 5.1628$



concentration and the systems, all the solidified eutectic ceramics showed an increasing a and c -lattices parameters in the Cr-doped α - Al_2O_3 phase. This is principally due to the difference in the Cr^{3+} (61.5 pm) size, which is considerably greater than the size of Al^{3+} (53.3 pm).³⁰ The peaks characteristics of $\text{Al}_{2-x}\text{Cr}_x\text{O}_3$ are therefore progressively shifted towards the lowest values of 2θ with Cr content (Fig. 4). In the case of the Cr-doped Al_2O_3 -YAG-ZrO₂ system, we have not observed a variation of lattice parameter a in ZrO₂ phase. But the X-ray peaks of the cubic zirconia phase were shifted slightly because some amount of Y₂O₃ was dissolved. On the basis of qualitative results under EDS, some amount of Y₂O₃ was contained in the ZrO₂ phase.

Fig. 5 and 6 show the SEM images of the transverse and the longitudinal sections cut from the Cr-doped Al_2O_3 -YAG binary and Al_2O_3 -YAG-ZrO₂ ternary eutectic ceramic rods. The precise knowledge of the solidification conditions,

namely solidification rate and initial composition, makes it possible to study the influence of these different parameters on the morphology. The addition of Cr in the binary Al_2O_3 -YAG system does not strongly affect the architecture morphology of this system.

Unlike the ternary system, the binary eutectic presents a homogeneous microstructure for all the Cr concentrations.

It is composed of two phases distinguished by their different shapes and colors; the black regions correspond to the α - Al_2O_3 phase and the grey regions correspond to YAG ($\text{Y}_3\text{Al}_5\text{O}_{12}$) phase. The Al_2O_3 is the matrix and the YAG phases are disconnected on transverse sections to the solidification direction. The shape and size of the YAG phase are irregular. The longitudinal sections (Fig. 6) show that the microstructure is irregular lamellar and corresponds to the Chinese script microstructure. The lamellae are elongated along the solidification direction. The YAG size increases

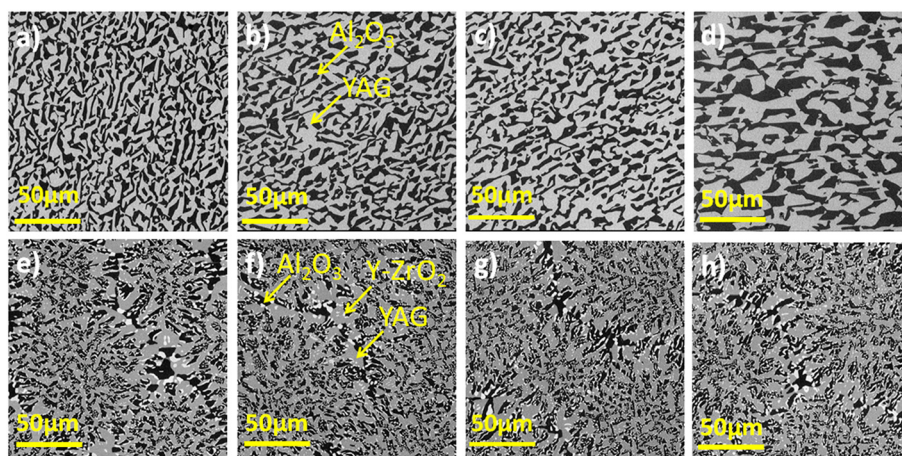


Fig. 5 Transversal microstructure evolution as a function of concentration. (a) Binary eutectic Cr 0.4 at%, (b) binary eutectic Cr 0.7 at%, (c) binary eutectic Cr 1.5 at%, (d) binary eutectic Cr 1.9 at%, (e) ternary eutectic Cr 0.4 at%, (f) ternary eutectic Cr 0.7 at%, (g) ternary eutectic Cr 1.5 at%, (h) ternary eutectic Cr 1.9 at%.

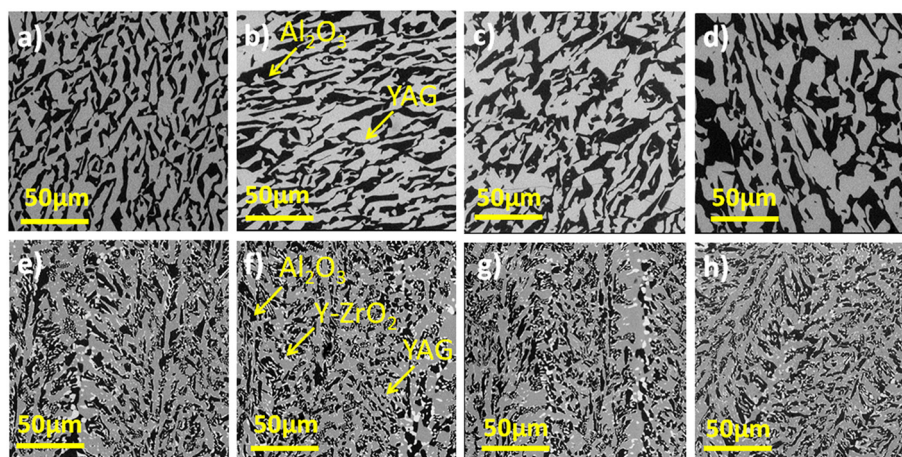


Fig. 6 Longitudinal microstructure evolution as a function of concentration. (a) Binary eutectic Cr 0.4 at%, (b) binary eutectic Cr 0.7 at%, (c) binary eutectic Cr 1.5 at%, (d) binary eutectic Cr 1.9 at%, (e) ternary eutectic Cr 0.4 at%, (f) ternary eutectic Cr 0.7 at%, (g) ternary eutectic Cr 1.5 at%, (h) ternary eutectic Cr 1.9 at%.



with increasing Cr concentration and reaches a maximum average of around 40 μm for 1.9 at% Cr (Fig. 6d). The coarsening as a function of Cr concentration is quite homogeneous and the microstructure remained unchanged. In the binary system, the dimension, homogeneity, and morphology of the microstructure are modified by varying the Cr concentration. A high Cr concentration promotes the contribution of diffusion, leading to an increase in the size of the microstructure. Increasing the Cr concentration is similar to decreasing the pulling rate in the Al_2O_3 –YAG system.²⁶ The microstructure corresponding to the lower Cr concentration (0.4 at%) is much finer. In eutectic solidified with low Cr concentration and smaller phase sizes, the diffusion was enhanced. A significant coarsening of the fine microstructure is registered. It seems that the coarsening process is Cr^{3+} diffusion through $\text{Y}_3\text{Al}_5\text{O}_{12}$ and Al_2O_3 .

For the Cr-doped Al_2O_3 –YAG– ZrO_2 system, the microstructure is composed of three phases, Al_2O_3 , YAG, and ZrO_2 . The main phases are YAG and alumina, which respectively have volume fractions of 42 vol% and 40 vol% (Fig. 6). The zirconia phase is distributed mainly at

the interface of the alumina and YAG phases or in the alumina phase with 1–5 μm . Intragranular ZrO_2 with a very small (0.1–0.8 μm) size surrounded the YAG phase. The longitudinal sections of the solidified samples show a “broken” or irregular lamellar microstructure. The lamellae are elongated along the solidification direction. In the ternary system, as a function of Cr concentration from 0.4 to 1.9 at%, we did not register an increase of YAG grains and magnification of the microstructure as observed in the Al_2O_3 –YAG binary system. The microstructure of the ternary system is finer and with more curved interfaces than that of the Cr-doped Al_2O_3 –YAG eutectic system solidified at the same rate. Whatever the Cr concentration (0.4–1.9 at%), the homogeneous character disappears, giving way to a colonies apparition but the microstructures are interconnected. Both YAG and ZrO_2 phases in the Cr-doped ternary eutectics showed a different morphology than in their respective Al_2O_3 -based binary eutectic systems,^{31–33} but Cr addition does not affect the shape of ZrO_2 particle, and the script size of the YAG phase was found to be uniform for each cross-

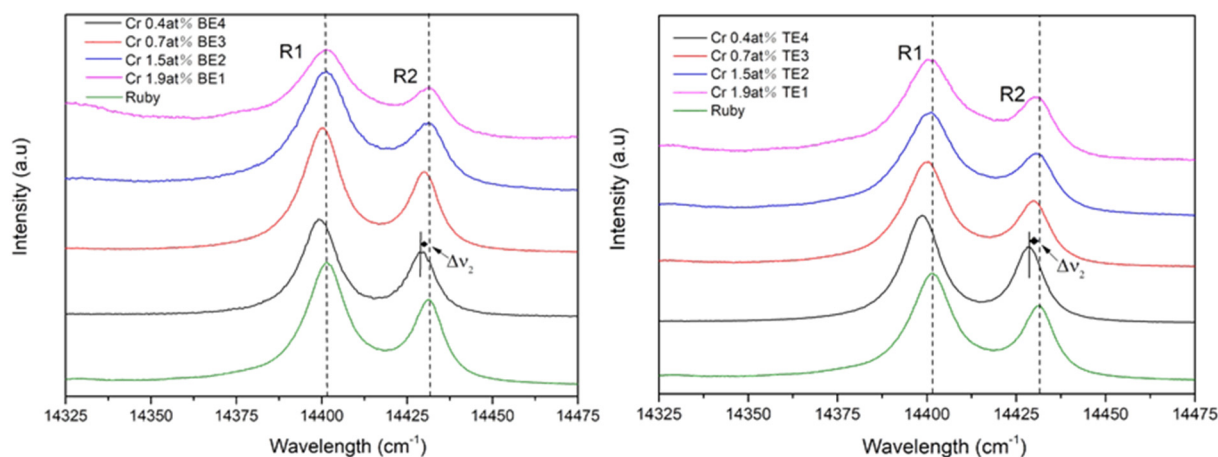


Fig. 7 Ruby fluorescence (R1 and R2 bands) excited with a 473 nm laser in transversal sections of the eutectics as a function of concentration.

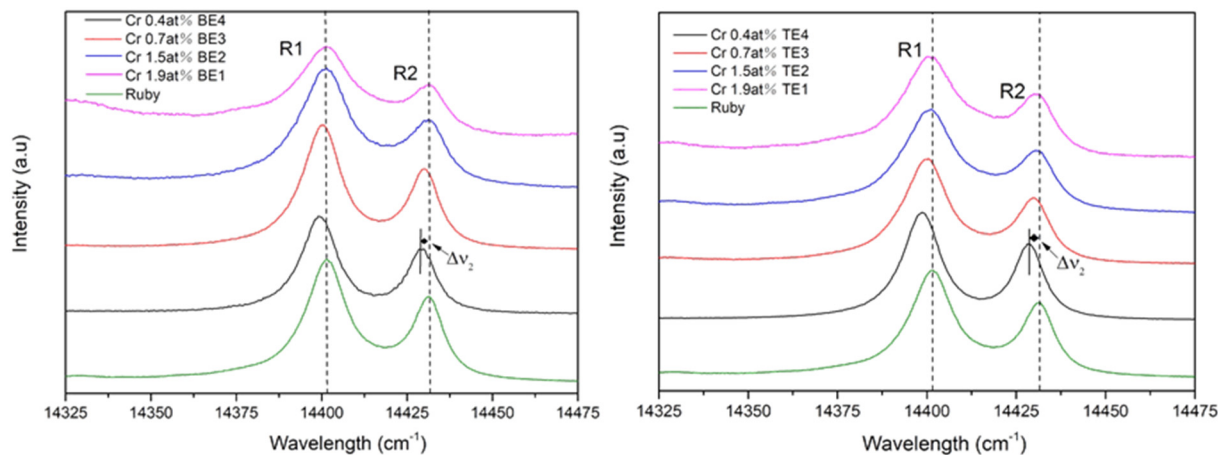


Fig. 8 Ruby fluorescence (R1 and R2 bands) excited with a 473 nm laser in longitudinal sections of the eutectics as a function of concentration.



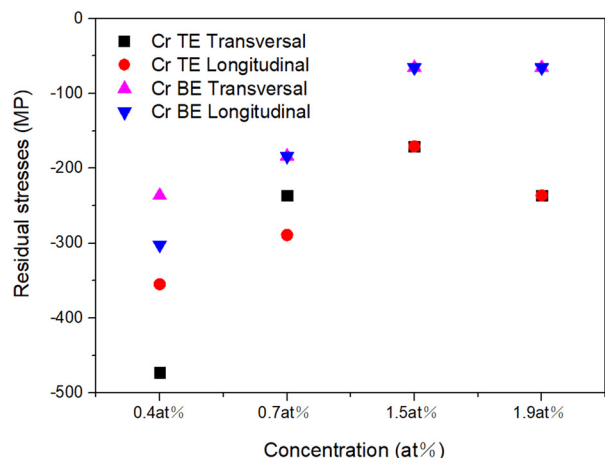


Fig. 9 Variation of the residual stresses (transversal and longitudinal sections) as a function of concentration according to Cr-doped binary and ternary eutectics.

section investigated. The SEM observations show that the Cr doping in the ternary system leads, in our case, to an excess of YAG (in grey) marked by the formation of large

primary crystals. The Al_2O_3 phase (black) is also slightly in excess compared to the garnet phase (grey).

3.2 Residual stress

The thermal elastic residual stresses of eutectics in the solidification process is caused by different thermal expansion mismatches between the $\alpha\text{-Al}_2\text{O}_3$, YAG, and $\text{ZrO}_2\text{:Y}$ phase.^{26,34} The fluorescence of ruby single crystal is taken as a reference to measure the residual stresses due to the electronic Cr^{3+} levels characterized by R1 and R2 luminescence lines; in most instances, the R2-line shift could be used to calculate approximate values of the hydrostatic stress σ_h , the relation follows:^{35,36}

$$\Delta\nu_2 = 7.61\sigma_h,$$

where $\Delta\nu_2$ refers to the peak shift of the R2-line (expressed in units of cm^{-1}) and σ_h presents the hydrostatic stress given in units of GPa. Fig. 7 and 8 show the fluorescence spectra of Cr^{3+} present in the alumina phase of Cr-doped $\text{Al}_2\text{O}_3\text{-YAG}/\text{Al}_2\text{O}_3\text{-YAG-ZrO}_2$ solidified eutectic. The evolution

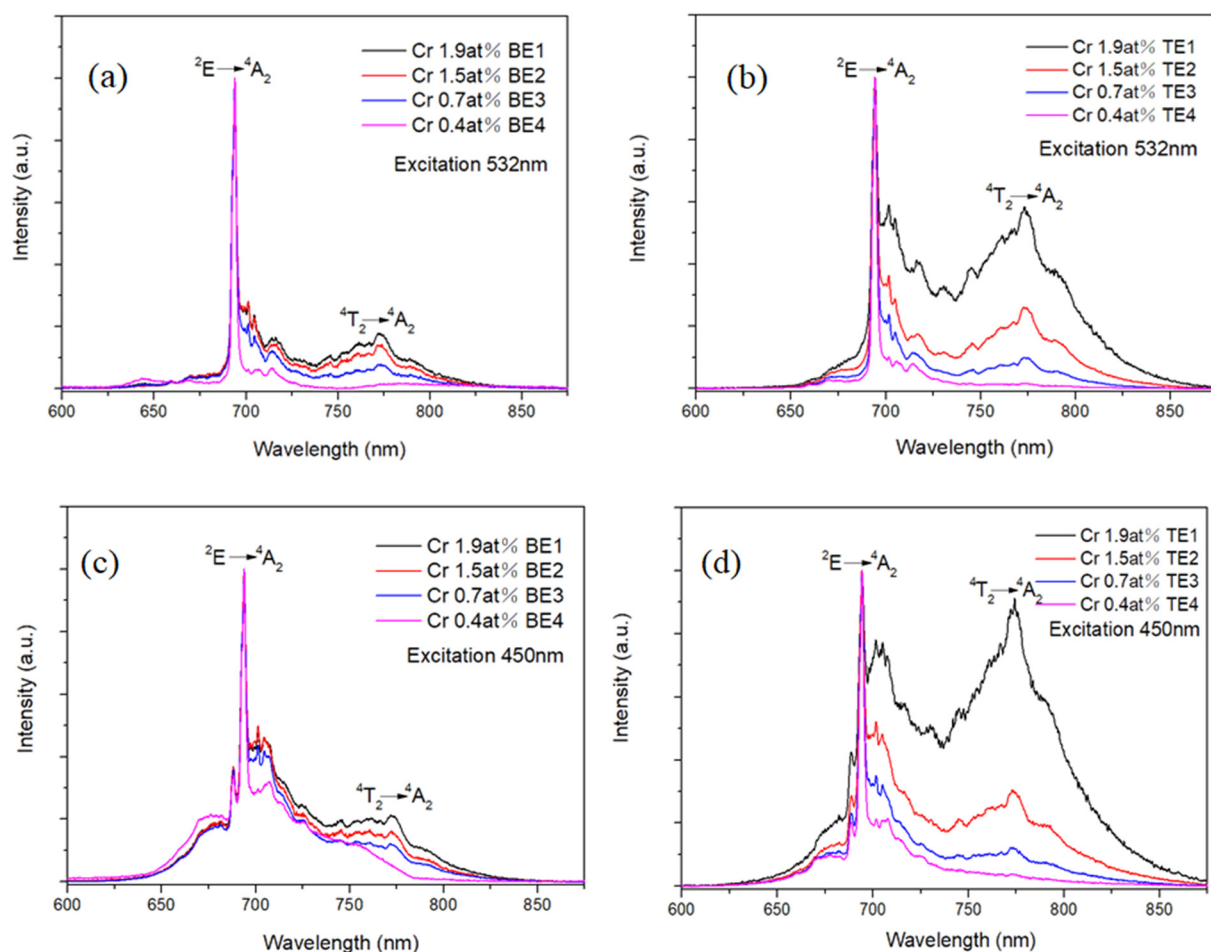


Fig. 10 The room temperature (300 K) emission spectra of eutectics (a) Cr-doped binary eutectics under excitation at 532 nm. (b) Cr-doped ternary eutectics under excitation at 532 nm. (c) Cr-doped binary eutectics under excitation at 450 nm. (d) Cr-doped ternary eutectics under excitation at 450 nm.



of the average hydrostatic stress measured on the transversal and longitudinal section of the samples is shown in Fig. 7 and 8; the negative values of the hydrostatic stress indicate that the alumina phase is under compression, which is observed in references.^{7,37} Whatever the transversal and longitudinal microstructure, the hydrostatic stress of binary eutectics is less than that of ternary eutectics with the same doped concentration due to the distribution of ZrO_2 particles in the microstructure affected by the residual stresses. The higher concentration of Cr-doped eutectic of Chinese script morphology is less compressed than that of at lower concentration. In a word, the variation of the residual stresses of Cr doped Al_2O_3 -YAG/ Al_2O_3 -YAG- ZrO_2 solidified eutectics, which not only depends on the cooling rate and time but also affected by the dopant and the concentration (Fig. 9).

3.3 Emission and excitation spectra

The room temperature (300 K) emission spectra of Cr-doped Al_2O_3 -YAG/ Al_2O_3 -YAG- ZrO_2 eutectics in the wavelength range of 600–900 nm recorded under green (532 nm) and blue excitation light (450 nm) are shown in Fig. 10. Under the green excitation, Cr-doped Al_2O_3 is clearly identified.³⁸ The

sharp line centered at 694 nm corresponds to the forbidden spin transitions from ^2E to $^4\text{A}_2$ level, referred to as R-line, and the broad band centered at 774 nm is due to the phonon-assisted $^4\text{T}_2$ to ground state $^4\text{A}_2$. This last transition was mostly observed when Cr-doped Al_2O_3 was higher than 0.5 at%. Indeed, the relative intensity of the broad band centered at 774 nm is increasing with the concentrations.³⁸ This effect is magnified in Cr-doped ternary eutectics. Moreover, under the blue excitation, an additional sharp line around 688 nm appears, attributed to the $^2\text{E} \rightarrow ^4\text{A}_2$ transition of the Cr-doped YAG phase.³⁹

The low temperature (77 K) emission spectra of Cr-doped binary and ternary eutectics in the wavelength range of 680–850 nm were also recorded under excitation at 532 and 450 nm as shown in Fig. 11. The broad emission band with peaks at 774 nm is observed due to $^4\text{T}_2 \rightarrow ^4\text{A}_2$ transition, in good agreement with R. C. Powell *et al.*⁴⁰ At low temperatures, the $^4\text{T}_2$ emission band is more structured but remains as large as at RT, however, the effect of decreasing temperature strongly affects the structure of the spectra in the 690–710 nm range; splitting of the Cr: Al_2O_3 R lines and magnification of the doublet is observed in its edge around 700 nm.

In order to analyse the rich luminescence spectrum in this range, the emission covering the spectral range from 680 nm

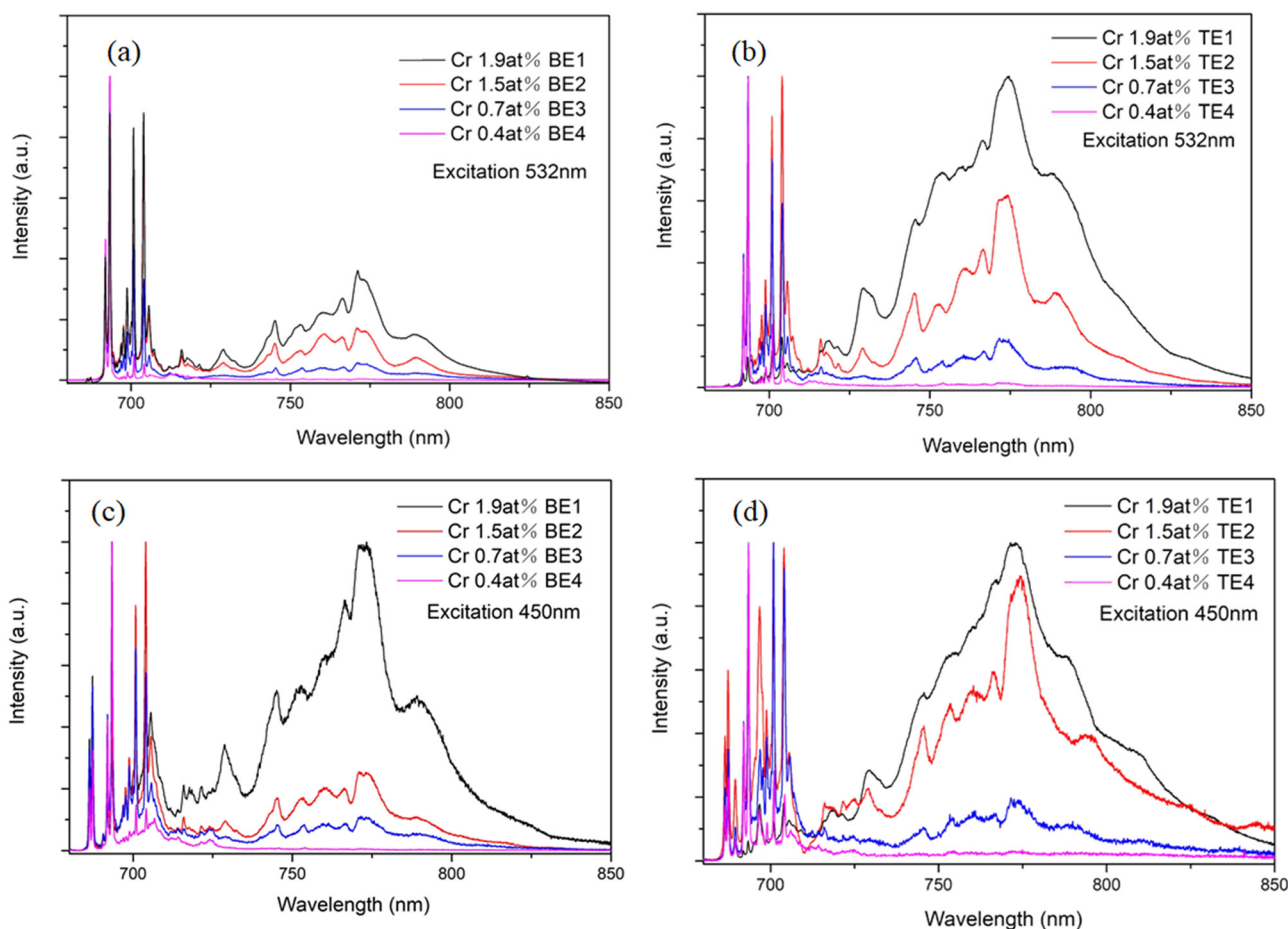


Fig. 11 The low temperature (77 K) emission spectrum of eutectics (a) Cr-doped binary eutectics under excitation at 532 nm. (b) Cr-doped ternary eutectics under excitation at 532 nm. (c) Cr-doped binary eutectics under excitation at 450 nm. (d) Cr-doped ternary eutectics under excitation at 450 nm.



to 710 nm is shown Fig. 12. Under green excitation at 532 nm, the first sharp lines lying at 693.4 nm and 692.0 nm are assigned to R1 $\bar{E} \rightarrow {}^4A_2$ and R2 $\bar{A} \rightarrow {}^4A_2$ lines, respectively, due to the spin-orbit coupling and then, the splitting of the radiative transition ${}^2E \rightarrow {}^4A_2$ in Cr^{3+} ions in octahedral crystal field.^{41,42} Whereas the second doublet of sharp lines at 704.0 nm and 700.9 nm corresponds to Cr^{3+} - Cr^{3+} pair lines, which

are designated as N1 and N2 in Al_2O_3 , respectively.⁴⁰ The ratio between the N and R-line intensity slightly increases in the ternary eutectics.

In addition, under blue excitation (450 nm), a third doublet of sharp lines appears at 686.3 nm and 687.3 nm, corresponding to the splitting of the Cr R line in YAG. The relative intensity of N lines and R lines increases with the Cr

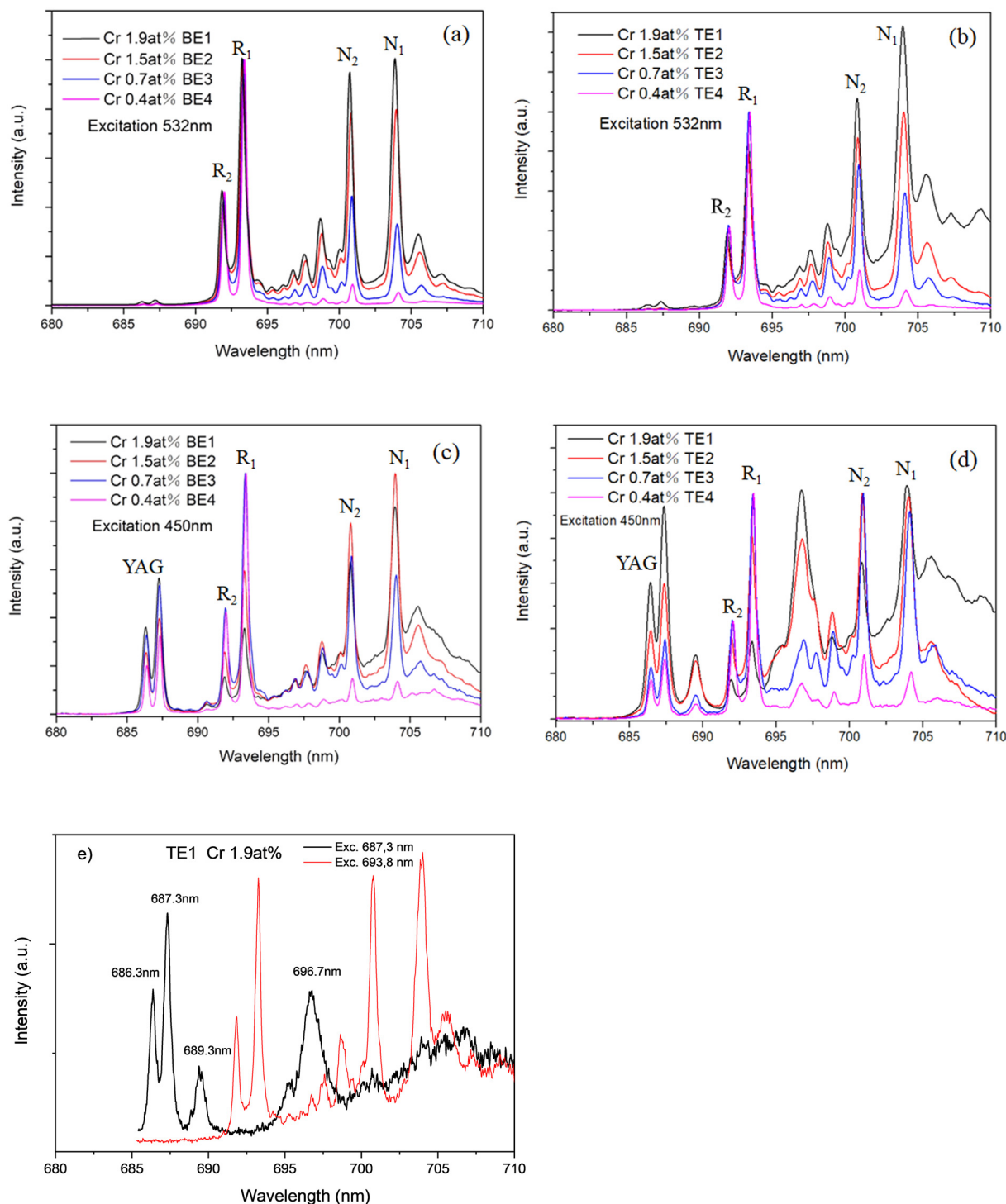


Fig. 12 The low temperature (77 K) emission spectrum of eutectics ranges from 680 nm to 710 nm under excitation at 532 nm a) and b); 450 nm c) and d) and selective excitations at 694.2 and 687.3 nm e).



concentration, as expected. Under 532 nm excitation, no difference between ternary and binary eutectic emission spectra is observed, whereas, under 450 nm excitation, at least two additional lines appear at 689.5 nm and 696.7 nm in the ternary compound coming from Cr-doped YAG phase. Indeed, under selective excitation in the 685–700 nm range, these additional lines only appear when excited in the two 687.3 and 686.0 nm Cr-YAG R lines.

The high temperature emission spectra of eutectics from 315 to 673 K are shown in Fig. 13. Under 532 nm excitation of the Cr in the alumina phase when the temperature is increasing, the 4T_2 level becomes more and more thermally populated, and then the intensity of the broadband increases relatively to the line (694 nm) corresponding to the $^2E \rightarrow ^4A_2$ emission. Under the excitation of 450 nm, the line at 688 nm, $^2E \rightarrow ^4A_2$ of Cr in YAG-phase, rapidly disappears (at already 100 °C). Indeed when the temperature increases, both $^4A_2 \rightarrow ^4T_2$ and $^4A_2 \rightarrow ^4T_1$ absorption or excitation bands, shown in Fig. 14, become much broader, and then, at 450 nm, the excitation of Cr in the alumina phase is enhanced. This result points out that the high temperature measurements corroborate that the

majority of Cr^{3+} ions entered favorably in the Al_2O_3 phase than in the YAG phase. This behavior is observed in both ternary and binary eutectics.

The room temperature excitation spectra of Cr-doped Al_2O_3 -YAG (binary system) and Al_2O_3 -YAG- ZrO_2 (ternary system) eutectics in the range from 285 to 680 nm are shown in Fig. 14. The excitation spectrum consists of two broad bands assigned to the $^4A_2 \rightarrow ^4T_1$ (Y-band) as well as $^4A_2 \rightarrow ^4T_2$ (U-band) spin-allowed transitions.⁴³ By monitoring the emission at 694 nm of Cr in the Al_2O_3 phase, the excitation bands are centered around 400 nm and 560 nm, while by monitoring the emission at 688 nm of Cr in the YAG phase, these bands are both red-shifted and centered around 450 nm and 610 nm, respectively. In addition, sharp excitation bands centered around 660 nm correspond to transitions from the 4A_2 ground state to 2T_1 level above 2E . In Fig. 14c, the asymmetrical shape of the excitation band is due to the overlap of the high energy part of the $^4T_2 \rightarrow ^4A_2$ emission transition of Cr in the Al_2O_3 phase; then it is not possible to select only the Cr luminescence in the YAG phase, this observation being more noticeable in Fig. 11d in the case of the ternary eutectics.

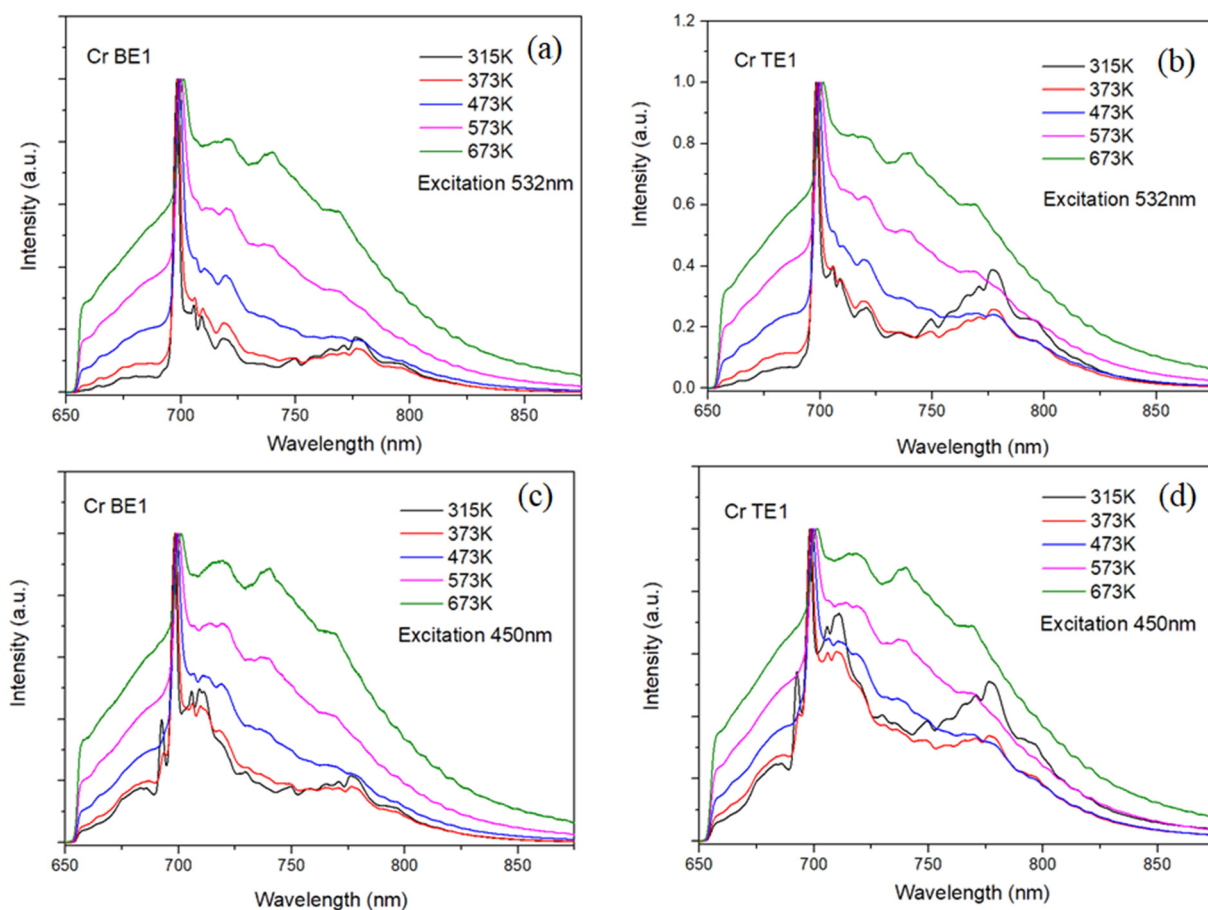


Fig. 13 High temperature emission spectrum, using a long-pass filter at 650 nm, of eutectics from 373 to 673 K (a) Cr-doped binary eutectic under excitation at 532 nm. (b) Cr-doped ternary eutectic under excitation at 532 nm. (c) Cr-doped binary eutectic under excitation at 450 nm. (d) Cr-doped ternary eutectic under excitation at 450 nm.



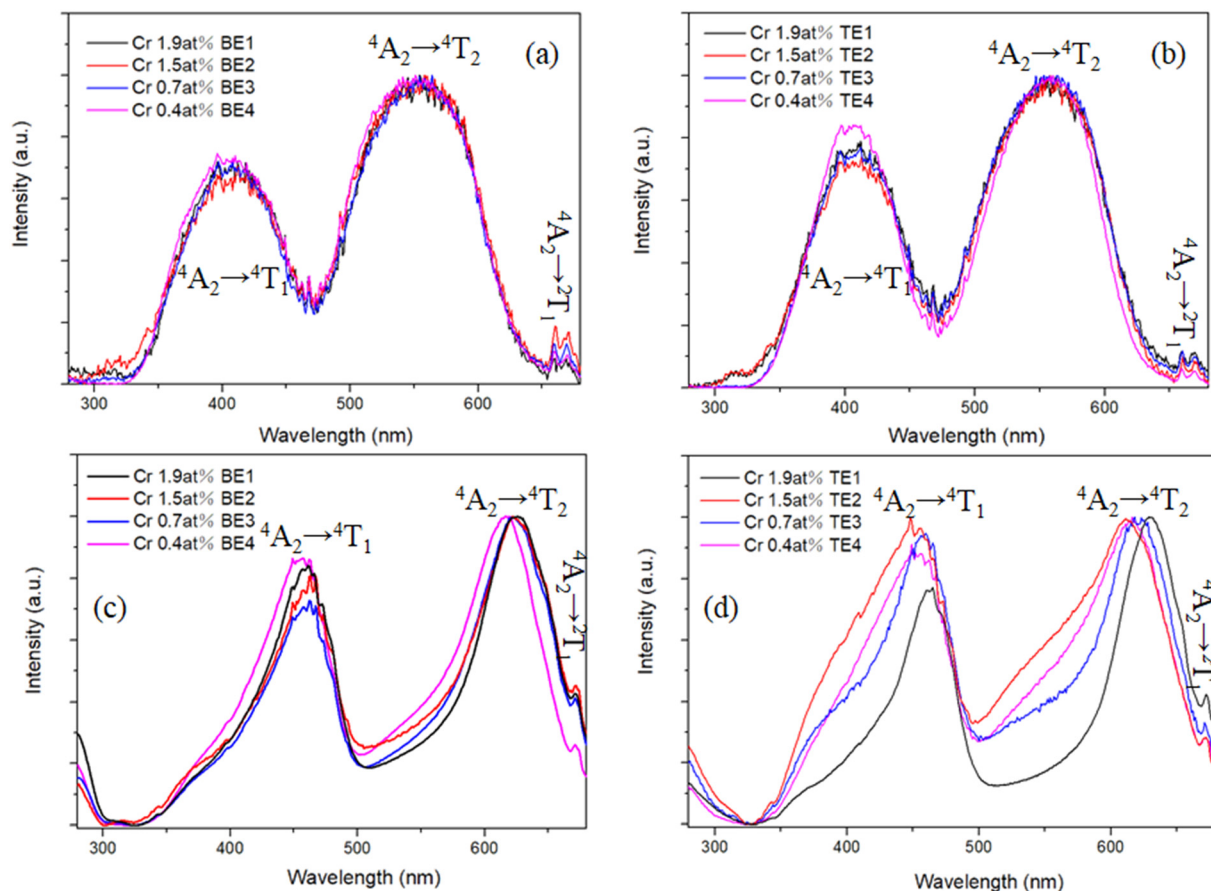


Fig. 14 Excitation spectrum of eutectics at room temperature (a) Cr-doped binary eutectics by monitoring the emission at 694 nm. (b) Cr-doped ternary eutectics by monitoring the emission at 694 nm. (c) Cr-doped binary eutectics by monitoring the emission at 688 nm. (d) Cr-doped ternary eutectics by monitoring the emission at 688 nm.

3.4 Fluorescence decay times

The fluorescence decay curves of the chromium luminescence as a function of the Cr concentration were recorded under 532 and 450 nm excitation at 300 K and 77 K, and the lifetime constants are gathered in Tables 3 and 4, respectively. As the decay curves become non-exponential for the two highest concentrations, as shown in Fig. 15, we calculated the integrated lifetime. As expected, at RT, the long lifetimes of the Cr^{3+} R-line ${}^2\text{E} \rightarrow {}^4\text{A}_2$ spin forbidden transition at 694.3 nm in the Al_2O_3 phase decreases from 3.84 ms to 0.94 ms when the concentration increases from 0.4 to 1.9 at% Cr-doped for the binary eutectics. The concentration quenching effect is more pronounced in Cr-doped ternary, with the lifetime being as short as 0.21 ms for 1.9 Cr at%. This behavior is also noticeable when comparing luminescence decays of the broad band centered at 774.3 nm in the binary and ternary systems. For this wavelength, the decay curves are particularly non-exponential due to the competition of the relaxation process from the excited level to the emitting ${}^4\text{T}_2$ level and the partial thermal equilibrium with the ${}^2\text{E}$ levels. However, this thermal coupling being less efficient at a low temperature

(77 K), it is observed that the values of decay times of the ${}^4\text{T}_2 \rightarrow {}^4\text{A}_2$ allowed transition measured at 773.0 nm becomes shorter than at 300 K. Finally, the decay time of Cr-doped binary eutectics is in good agreement with Cr^{3+} : Al_2O_3 powder,³⁸ and ruby bulk crystals⁴⁰ especially considering the lifetime of about 1 ms for 2 at% of the Cr–Cr pair emission of the N-lines measured at 704 nm under 532 nm at low temperature. It is interesting to note that the lifetime of the emission of Cr pairs is much shorter in the ternary 0.3 ms than in the binary eutectics 0.8 ms.

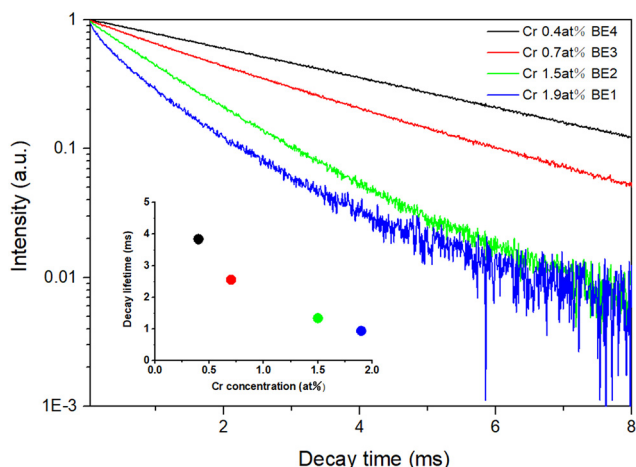
Table 3 The decay times (in ms) of various emissions under 450 nm and 532 nm excitation at 77 K

Sample	Excitation 532 nm		Excitation 450 nm
	694.3 nm	774.3 nm	688.7 nm
Cr BE1	0.94	0.55	1.30
Cr BE2	1.34	1.24	0.95
Cr BE3	2.56	1.60	1.63
Cr BE4	3.84	—	1.78
Cr TE1	0.21	0.09	0.33
Cr TE2	0.63	0.97	0.64
Cr TE3	1.29	0.92	1.33
Cr TE4	3.30	1.08	1.77



Table 4 The decay times (in ms) of various emissions under 450 nm and 532 nm excitation at 77 K

Sample	Excitation 532 nm			Excitation 450 nm
	694.3 nm	704.0 nm	773.0 nm	687.3 nm
Cr BE1	0.74	0.81	0.61	4.80
Cr BE2	0.56	0.81	0.72	3.10
Cr BE3	2.10	1.87	1.08	6.27
Cr BE4	6.13	4.37	0.97	7.28
Cr TE1	0.30	0.26	0.30	1.67
Cr TE2	0.19	0.28	0.54	2.04
Cr TE3	0.77	0.80	0.62	5.54
Cr TE4	3.92	3.81	1.34	6.21

**Fig. 15** Fluorescence decay curves of the 694.3 nm emission under 532 nm excitation in Cr-doped binary eutectics at RT.

Considering the luminescence decay time of the Cr-doped YAG phase at 687.3 nm recorded under 450 nm excitation, the lifetime at 77 K binary eutectic is measured to be about 7.28 ms for 0.4 at% Cr-doped, which is slightly smaller than the 8.8 ms measured in 0.05% at 7 K (ref. 39 and 44) but is slightly longer than that measured here in the Al_2O_3 phase in the same sample. It can be explained by a lower intermediate ligand crystal field strength $D_q/B_p < 2.1$ in YAG^{45} than in Al_2O_3 ($D_q/B > 2.33$),⁴⁶ while the Cr^{3+} octahedral sites are slightly distorted²⁷ in YAG. At room temperature, the lifetime of 1.77 ms in both binary and ternary eutectics is in total agreement with the value given by Bray *et al.*^{39,45} From Tables 2 and 3, one can note that the temperature quenching effect is stronger for the YAG phase than in the ruby-phase while the phonon energy cutoff is rather the same, 865 cm^{-1} and 910 cm^{-1} ,⁴⁷ respectively. In the contrary, the concentration quenching is larger in Al_2O_3 than in the YAG phase; the lifetime decreases ten times between the highest and the lowest concentration at 77 K in Al_2O_3 and only three times in YAG. It suggests that the concentration of Cr in the YAG phase should be lower than in Al_2O_3 -phase due to a lower segregation coefficient in YAG. Finally, as for Cr in the Al_2O_3 phase, the decay becomes also shorter in the ternary compound for Cr in the YAG phase, possibly because of the

higher Cr concentration in ternary eutectics as already suggested from the analysis of the emission spectra or by the decay curves of the N-line emission of pairs. Finally, the dynamics of the new emission lines at 689 and 696 nm are the same as the Cr luminescence in the YAG phase.

4. Conclusion

In this work, Cr-doped Al_2O_3 -YAG binary and Al_2O_3 -YAG- ZrO_2 ternary systems of eutectic ceramics were solidified from the melt by using the μ -PD technique. The coloration, morphology, microstructure, residual stress, and luminescence have been investigated. As a function of Cr-dopant concentration and the binary or ternary system, the relationship between the microstructure and the optical properties, and as a result, solidified eutectic ceramics with optimized microstructures have been elaborated. The Cr-doped eutectics present a red color. Whatever the dopant concentration, mainly two phases (Al_2O_3 -YAG) in the binary system and three phases (Al_2O_3 -YAG- ZrO_2) in the ternary system are observed. The Chinese script microstructure, colonies and colony boundaries are observed in ternary eutectics. From the different sizes of YAG grains, the microstructure formation of binary eutectics depends on the chromium dopant concentration. Moreover, Al_2O_3 and YAG phases show faceted morphologies, but for the ZrO_2 phase, growth tends to a weakly faceted manner and forms rods or lamellae. Whatever the Cr dopant concentration, the hydrostatic stress of the binary eutectics is less than that of ternary eutectics.

The spectroscopic properties of the Cr-doped eutectic clearly show that Cr^{3+} ions enter Al_2O_3 and YAG phases in octahedral sites. The increase in the intensity of the $^4\text{T}_2 \rightarrow ^4\text{A}_2$ emission band relative to the $^2\text{E} \rightarrow ^4\text{A}_2$ lines, on the one hand, and the intensity ratio between the N-lines and R-lines recorded at 77 K, on the other hand, shows that the Cr concentration in Al_2O_3 phase should be higher in the ternary eutectic than in the binary eutectic. The analysis of the emission lifetime in both compounds corroborates this observation: the luminescence quenching by concentration is emphasised in the ternary eutectics. Furthermore, the concentration of Cr in the YAG phase is smaller than in the Al_2O_3 phase. Finally, new lines, which are coupled to the YAG phase, appear at low temperatures in the highest concentrated ternary eutectics.

Finally, the luminescence and spectroscopy of the doped Al_2O_3 -YAG and Al_2O_3 -YAG- ZrO_2 systems are still in the early stages in comparison with chemical and mechanical properties, and research efforts in this field are still very recent. However, from the literature, it can be observed that the combination of the oxide eutectic compositions for optics has not yet been explored completely, and we are probably still in the early stages of research in this field.

Conflicts of interest

There are no conflicts to declare.



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