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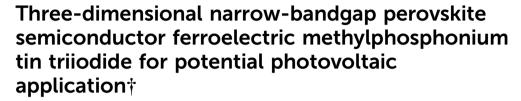


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A novel A-site three-dimensional organic-inorganic halide perovskites (3D OIHP) ferroelectric, methylphosphonium tin triiodide (MPSnI<sub>3</sub>), featuring a narrow bandgap of 1.43 eV, was synthesized. The integration of ferroelectricity with initially moderate efficiency (2.23%) may afford a promising platform to investigate the ferroelectric photovoltaic effect in organic-inorganic halide perovskite solar cells.

The superior performance of methylammonium lead iodide (MAPbI<sub>3</sub>) in photovoltaic applications is a milestone achievement in perovskite chemistry. It has provoked booming research on organic-inorganic halide perovskites (OIHPs).<sup>1,2</sup> OIHP structures containing organic cations and inorganic frameworks combine the merits of easy processability of solutions, lightweight, highly structural tunability, and additional functionalities.3-5 These features render OIHPs prominent performance in light-emitting diodes, solar cells, optoelectronic detectors, and ferroelectric devices.<sup>6,7</sup> Three-dimensional (3D) ABX<sub>3</sub> OIHPs (A = organic cations, B = metal, X = halogen), in which A-cations occupy the voids between BX6 octahedra (most notably (MA or FA)(Pb or Sn)(I or Br)3 where FA is formamidinium), are considered "superstar materials" in optoelectronics and photovoltaics.8 During the past decade, the power conversion efficiency (PCE) of MAPbI<sub>3</sub>-based perovskite solar cells (PSCs) has improved from 3.8% to >25%. 9-11 More recently, Zhan and colleagues converted α-FAPbI<sub>3</sub> films into PSCs with an efficiency of > 23%, <sup>12</sup> comparable with that of commercialized crystalline silicon and GaAs solar cells. Besides the appropriate bandgaps ( $\sim 1.5$  eV) close to the optimal bandgap ( $\sim 1.34 \text{ eV}$ ), <sup>10,12</sup> the high photovoltaic performance of MAPbI<sub>3</sub> is deemed to be associated to its polar nature and ferroelectric polarization at room temperature. 13-15

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Ferroelectric materials with intrinsic spontaneous polarization in photovoltaic devices contribute significantly to formation of a strong local built-in field to facilitate effective separation of electron-hole pairs that are similar to the p-n junctions in conventional solar cells. 16,17 Hence, a ferroelectric photovoltaic effect has long been expected to be a preferable choice for conversion of solar energy. However, the low absorption coefficient and wide bandgap in conventional ferroelectric materials (e.g., BTO, PZT, and LiNbO<sub>3</sub>) are unacceptable in photovoltaic research. 18 Therefore, ferroelectric materials with a narrow bandgap are very important for high-efficiency photovoltaic devices. BiFeO3 has a small bandgap and can absorb many photons, but large leakage currents caused by ineluctable Fe2+ and oxygen vacancies seriously affect ferroelectric polarization. 17,19,20 In OIHPs, Pb-based PSCs have toxic effects on the body and environment. In the past few years, the most promising Sn-based OIHPs have been investigated intensively for applications of solar cells, but they must be lead-free and realize comparable visible-light absorption. Unfortunately, their photovoltaic performances are far from those of leadbased devices. 21-32 FA(Pb or Sn)(I or Br)3 and MAPbBr3 crystallize in centrosymmetric space groups at room temperature and fail to meet the polar symmetry for ferroelectrics. 33-35 In recent years, extensive research has been conducted to extend the family of functional OIHPs, 4,36 whereas the development of new photovoltaic OIHPs has stalled because of the difficulties in stabilizing the parent 3D structural motif. Subjected to the Goldschmidt tolerance factor t (0.8 < t < 1), 3D BX<sub>3</sub><sup>-</sup> cubic frameworks can accommodate only a few small cations, MA, and FA to support a photoactive black perovskite phase. 37,38 At this stage of their development, construction of 3D OIHP ferroelectrics with new A-site cations seems an incredible challenge.

Phosphonium-based molecules are promising as A-site cations because the P atom and N atom (which belong to the same group in the Periodic Table) have similar covalent characteristics. Thus, phosphonium cations and ammonium cations can enable materials to have similar structures and functions, whereas their differences in atomic radius, mass, electron structure, and bond

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length may elicit interesting variables in physical and chemical properties. Based on theoretical calculations of the tolerance factor rule, the methylphosphonium (MP+) cation has been predicted to be available to fill a 3D cage, thereby meeting the demand for the formation of a stable 3D OIHP structure.<sup>39</sup> Very recently, we synthesized a 3D perovskite molecular ferroelectric MPSnBr<sub>3</sub>. At the experimental level we showed (for the first time) that MP<sup>+</sup> can serve as a stable A-site cation in OIHPs. 40 Moreover, in 1999, Mitzi et al. demonstrated the conducting property of tin iodide frameworks. 41,42 In view of those observations, we synthesized a new 3D lead-free OIHP: methylphosphonium tin iodide (MPSnI<sub>3</sub>). It features a narrow bandgap (1.43 eV), which is close to the optimal bandgap ( $\sim 1.34$  eV), thereby making it a competitive candidate for photovoltaic and optoelectronic applications. MPSnI<sub>3</sub> is also a multiaxial ferroelectric with a Curie temperature  $(T_c)$  of 298 K. These attributes may boost the photoelectric performance of MPSnI3-based solar cells. Compared with MPSnBr<sub>3</sub>, substituting bromine for iodine: (i) heralded a new structure; (ii) resulted in a black perovskite phase with a narrower bandgap; (iii) broke through the long-term limitation of A-site 3D iodide perovskite species. We believe our discoveries afford a promising platform to investigate the ferroelectric photovoltaic effect in OIHP solar cells and other optoelectronic applications.

We prepared crystals of MPSnI<sub>3</sub> in a hydroiodic acid solution of equimolar SnI2 and MPI (Fig. S1-S3, ESI†). Single-crystal structure studies revealed that MPSnI3 adopted a 3D ABX3 OIHP structure (A =  $MP^+$ , B =  $Sn^{2+}$ , and X =  $I^-$ ), in which organic  $MP^+$ cations were located in 3D-framework cavities surrounded by SnI<sub>6</sub> octahedra, isostructural to the 3D MASnI<sub>3</sub> (Fig. 1). The crystal structure of MPI adopted a monoclinic space group P2<sub>1</sub>/m (Fig. S4 and Table S1, ESI†).

At 273 K, MPSnI<sub>3</sub> crystallized in polar space group Pba2 (point group = mm2) (Table S1, ESI†). This corresponded to the low-temperature ferroelectric phase (LFP). In the LFP, the MP<sup>+</sup> cations located on 2-fold symmetry axes in the lattice and thus showed 2-fold orientational disorder (Fig. 1a and c). The SnI<sub>6</sub>

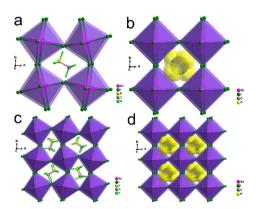


Fig. 1 Basic structures for MPSnI<sub>3</sub> at (a) 273 K, and (b) 313 K, respectively. The P atom and C atom of the MP cation are disordered over the two possible positions. Only one distribution is illustrated for clarity. Packing view of the structures for MPSnI<sub>3</sub> at (c) 273 K, and (d) 313 K, respectively. H atoms of the organic cations in HPP were not modeled because of total disorder, and thus not shown in (b) or (d).

octahedron was distorted, showing short (average of 3.057(5) Å) and long (average of 3.306(5) Å) Sn-I interatomic distances, and an angle of Sn-I-Sn between 158.9° and 178.0° (Fig. S5a and Table S2, ESI†). At 313 K (high-temperature paraelectric phase (HPP)), the crystal structure of MPSnI<sub>3</sub> was refined to the noncentrosymmetric cubic space group  $P\bar{4}3m$  (point group  $\bar{4}3m$ ) (Table S1, ESI†) based on the significant piezoelectric signal response by piezoresponse force microscopy (PFM) (Fig. S6, ESI†). Also, MP cations were modelled to be highly disordered spheres to satisfy the cubic symmetry (Fig. 1b and d). The SnI<sub>6</sub> octahedron also changed to a regular octahedron with only one type of Sn-I interatomic distance of 3.1732(1) Å, and the Sn-I-Sn angle became 180.0° (Fig. S5b and Table S2, ESI†). Therefore, the ferroelectric phase transition from LFP to HPP was associated with the order-disorder transition of MP+ cations and deformation of the [SnI<sub>3</sub>] framework. According to the Aizu rule, this phase transition in MPSnI<sub>3</sub> should be ferroelectric with Aizu notion 43mFmm2.43

Differential scanning calorimetry (DSC) was undertaken to detect the phase transition. During heating, an endothermic peak around 298 K revealed a phase transition for MPSnI<sub>3</sub>, which was higher by 25 K than that for MASnI<sub>3</sub> (Fig. 2a). We confirmed the phase transition by the temperature-dependent second-harmonic generation (SHG) response (Fig. 2b). MPSnI<sub>3</sub> exhibited clear SHG signals in the ferroelectric phase. The SHG intensity of MPSnI<sub>3</sub> had a marked change in  $T_c$ , indicating the appearance of significant symmetry breakage and in accordance with the transition of non-centrosymmetric mm2 and  $\bar{4}3m$  crystallographic symmetry in ferroelectric and paraelectric phases. However, a change in SHG signal was not observed before or after the phase transition temperature ( $T_c = 273 \text{ K}$ ) for MASnI<sub>3</sub>. We also confirmed the phase transition of MPSnI<sub>3</sub> by the dielectric anomaly around  $T_c$  in the temperature-dependent dielectric real part  $(\varepsilon')$  (Fig. 2c). The huge variation of  $\varepsilon'$  around  $T_{\rm c}$  revealed the ferroelectric-to-paraelectric phase transition for

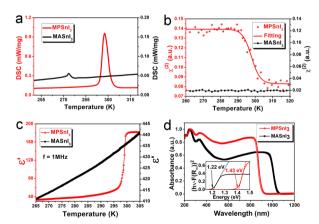


Fig. 2 (a) DSC measurements revealed a structural phase transition at around  $T_{\rm c}$  = 298 K (MPSnI<sub>3</sub>) and  $T_{\rm c}$  = 273 K (MASnI<sub>3</sub>). (b) Second-order nonlinear optical coefficient  $\chi^{(2)}$  as a function of temperature. (c) Temperature dependence of the real part ( $\epsilon'$ ) of the complex dielectric constant at 1 MHz. (d) Ultraviolet-visible absorption spectra for MPSnI<sub>3</sub> and MASnI<sub>3</sub>. The inset shows the Tauc plot.

MPSnI<sub>3</sub>. The Curie-Weiss law is not applicable in such an

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inappropriate ferroelectric compound.<sup>7</sup> The behavior of dielectric permittivity around  $T_c$  can be explained by a fitted model based on the Landau-Ginzburg theory (Fig. S7, ESI†).

The optical property of a MPSnI<sub>3</sub> crystal was investigated by solid-state UV-vis diffuse reflectance spectroscopy at room temperature. The UV-vis absorbance spectrum displayed intense absorption at a band-edge onset of 900 nm (Fig. 2d). The feature of a direct bandgap semiconductor could be concluded (Fig. 2d, insert). From the Tauc plot, the measured optical bandgap for the direct transition was 1.43 eV, which is slightly higher than that for the 3D analogue: MASnI<sub>3</sub> (1.22 eV).

To characterize the ferroelectricity of MPSnI<sub>3</sub>, we employed PFM to enable non-destructive visualization and control of ferroelectric domains on single crystals at 288 K. The cleardomain phase contrast and domain wall are shown in Fig. S3a and S3b (ESI†). The domain structure did not overlap with the topography (Fig. S8, ESI†). For MPSnI<sub>3</sub>, 180° and non-180° domains could coexist on a single crystal, thereby demonstrating the multiaxial nature (Fig. S9, ESI†).

These stable polarizations in the domains could also be switchable under an external electric field. Fig. 3c and d display the well-defined hysteresis loops and typical butterfly-shaped curves for the vertical phase and amplitude signals versus DC bias, respectively, which confirmed the switchable polarization of MPSnI<sub>3</sub>. We also undertook PFM tip poling experiments to observe domain switching directly. Switched domain patterns could be written on a single crystal of MPSnI<sub>3</sub> under application of opposite voltages, which provided solid evidence for ferroelectric polarization switching (Fig. S10, ESI†).44,45

We calculated the hypothetical molecular rotation of MA and MP in the inorganic SnI<sub>3</sub><sup>-</sup> framework, respectively (Fig. S11, ESI†). The state with the lowest energy emerged at 45° and 135° (Fig. 4a), so the molecule was most stable in the face-center direction, in accordance with the measured crystal structure. Compared with MA cations, the energy barrier of MP

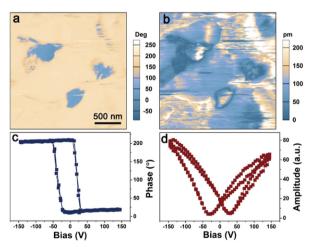


Fig. 3 Vertical PFM phase (a) and amplitude (b) images on the crystal surface of MPSnI<sub>3</sub> at 288 K. Vertical PFM phase (c) and amplitude (d) signals versus the tip bias at a selected location.

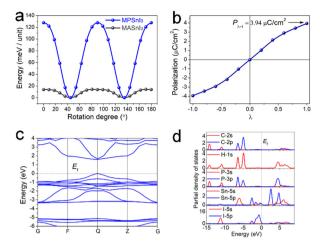


Fig. 4 (a) Rotational energy barrier of MP and MA cations in the inorganic Snl<sub>3</sub><sup>-</sup> framework. (b) Evolution path of polarization with structural distortion of MPSnI<sub>3</sub>. (c) The energy-band structure of a MPSnI<sub>3</sub> crystal shows a direct bandgap of 1.58 eV. (d) The partial density of states (PDOS) of a MPSnI<sub>3</sub> crystal.

rotation was much higher, suggesting a higher ferroelectric phase-transition temperature. Such a high barrier for rotational energy of MPSnI<sub>3</sub> may originate from a heavier molecular mass and larger molecular volume.

To gain deep insight into ferroelectric polarization reversal, density functional theory (DFT) calculations were carried out to evaluate the origin of polarization. 46,47 Based on the modern theory of polarization, 48,49 a dynamic path between two ferroelectric states is constructed according to the crystal structure acquired from single-crystal X-ray diffraction.

Considering the rotational and displacive motion of MP cations in the anionic SnI<sub>3</sub><sup>-</sup> framework, the other states were obtained from the matrix transformation of the coordinates. The variation of polarization versus the dynamic path is displayed in Fig. 4b, from which the ferroelectric polarization with 3.94  $\mu$ C cm<sup>-2</sup> could be extracted from two equivalent ferroelectric configurations ( $\lambda = \pm 1$ ). During ferroelectric switching ( $-1 < \lambda < 1$ ), the polarization value changed smoothly, and turned to zero at  $\lambda = 0$ , suggesting a reference phase with zero polarization.

We also calculated the band structure to obtain deep insight into the electronic structure of MPSnI<sub>3</sub> (Fig. 4c). The conduction band (CB) minimum and valence band (VB) maximum were localized at the same k-vector in the Brillouin zone, so MPSnI<sub>3</sub> was a direct bandgap semiconductor, in good agreement with experimental phenomena. The calculated bandgap was 1.58 eV, close to the experimental value of 1.43 eV. Furthermore, bands can be assigned according to the partial density of states (PDOS), as plotted in Fig. 4d. From PDOS, the bands at the top of the VB originated from the nonbonding states of I-5p, and those at the CB bottom were mainly from the unoccupied Sn-5p orbitals. Clearly, the bandgap of the material was determined by the inorganic {SnI<sub>3</sub>}<sup>-</sup> framework.

We conducted preliminary device fabrication to test the photovoltaic performance of MPSnI3 with a device structure of ITO/ PEDOT:PSS/perovskite/C60/BCP/Ag (Fig. S12-S17 and Table S3, ESI†). Benefiting from outstanding ferroelectric and semiconductor Communication ChemComm

properties, the manufactured MPSnI<sub>3</sub>-based solar-cell device showed initial photoelectric performance, and achieved a moderate PCE of

In summary, we reported a new 3D lead-free OIHP ferroelectric semiconductor of MPSnI<sub>3</sub> that showed clear ferroelectricity with a  $T_c$  of 298 K and a narrow bandgap of 1.43 eV. MPSnI<sub>3</sub> was a multiaxial ferroelectric with the Aizu notion of 43mFmm2, and the ferroelectric domains and polarization switching confirmed its ferroelectricity. The considerable initial energy conversion efficiency, combined with easy processing of solutions, suggests that MPSnI<sub>3</sub> has great potential for photovoltaic, photoelectric, and ferroelectric applications.

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## Conflicts of interest

There are no conflicts to declare.

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