Lithium-ion distribution and motion in two-dimensional covalent organic frameworks: the example of TAPB-PDA COF†

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Two-dimensional covalent organic frameworks (2D COFs) are promising as solid-state electrolytes due to their high structural stability, lack of glass transition temperature, and molecular versatility. For more rational molecular and system design toward better ionic conduction in COFs, a detailed understanding of the ion distributions, ionic motions, and interactions among different species is needed. Achieving this goal requires insights at the molecular level, where computer simulations can be a powerful tool. However, efficient protocols that can model lithium-ion trajectories in COFs over long times are still to be explored, which are needed for the reliable consideration of Li⁺ motions as well as for the development of high-throughput molecular screening strategies for accelerated materials discovery. Here, we apply molecular dynamics simulations with electronic continuum correction to study lithium-ion distributions and motions in 2D COFs. The efficient force fields have allowed us to model trajectories over hundreds of nanoseconds and the consideration of experimentally relevant lithium loading. The imine-linked TAPB-PDA COF, which has become a model system in COF-related studies, is taken here as an example. LiClO₄ is used to provide Li⁺, and the role of propylene carbonate is studied. Our analysis provides a comprehensive understanding of the distributions and motions of lithium ions and anions. It was found that LiClO₄ tends to form clusters that attach to the walls of COF pores that limit ionic motions. The addition of propylene carbonate molecules helps the dispersion of Li⁺ in the COF pores for increased mobility. These results highlight the role of microscopic interactions between different components and point to potential optimization directions for higher ionic conductivity engineering of 2D COFs.

1. Introduction

The fast development of electric vehicles and grid-scale energy storage systems demands post lithium-ion batteries (LIBs) with high energy and power density. All-solid-state Li batteries are particularly attractive as they have superior energy density compared to commercial lithium-ion batteries due to the high theoretical specific capacity of lithium metal of 3860 mA h g⁻¹ (in comparison to 374 mA h g⁻¹ for the commercial graphite anode). To obtain Li metal batteries with high performances, it is essential to develop solid electrolytes (SEs) with high Li⁺ conductivities and stability. One of the most promising SEs discovered in recent years is two-dimensional covalent organic frameworks (2D COFs). They are a type of highly versatile, porous material with atomically precise, nanometer-sized pores and can be integrated with designed functional groups for electron conduction and ion transport. As SEs, stacked 2D COFs form open channels for ion transport, and the lack of a glass transition temperature makes them ideal for working in a wide temperature range. However, the Li⁺ conductivities of pristine COFs often do not exceed the order of 10⁻² S cm⁻¹ at room temperature, compared to 10⁻¹ S cm⁻¹ of liquid organic electrolytes. These low ion conductivities have largely limited their applications as SEs. Ultimately improving COFs for their successful application in Li metal batteries requires a thorough understanding of the ion transport mechanism as well as the molecular structures and interactions in these COF-based systems, which, unfortunately, remains largely unclear. For example, it is known that lithium ions do not occupy the entire available space in the COF framework. Instead, these COFs often have a lithium loading from 0.2 to 4% with ions...
of the structural features of 2D COF systems of tens of nm and at tens of ns.\cite{28,29} Here, we apply molecular dynamics simulations to investigate lithium-ion transport in imine-linked COFs using TAPB-PDA COF as an example, which has become a model system in COF-related studies\cite{30-32} and the force field parameters of which have been well established.\cite{33,34} The electronic continuum correction (ECC) allows taking into account implicitly the polarization effect within the efficient force fields.\cite{35,36} Different amounts of propylene carbonate were considered to understand its impact on Li\(^+\) distribution and motion. The efficient simulations have allowed us to model systems with experimentally relevant Li loading and PC ratios for trajectories up to 200 ns. The simulations revealed the molecular interactions among Li\(^+\), anions, COFs, and PC molecules. It was found that LiClO\(_4\) tends to form clusters inside the COF pores, which leads to noncontinuous Li\(^+\) transport pathways and localized ionic motion. The addition of PC molecules leads to more uniform distributions of lithium ions and makes it easier for them to move across the pores. The result is more continuous transport pathways and improved ionic conductivities.

2. Methodologies

TAPB-PDA COF has eclipsed stacking with a layer distance of 3.5 Å.\cite{31} Here, we consider multi-layer TAPB-PDA COF sheets in a co-facial configuration, and a 2 × 2 × 20 supercell is constructed. Fig. 1 shows the top and side views of the supercell, which has 240 terephthalaldehyde (PDA) units and 160 1,3,5-tris(4-aminophenyl)benzene (TAPB) units. This structure is mixed with 240 LiClO\(_4\) (one per PDA unit), corresponding to a lithium loading of 1.6 wt% and similar to the values used experimentally.\cite{8,11,16} Different PC amounts that correspond to 10 wt%, 20 wt%, and 40 wt% in the final system were then added. The initial mixture structure was constructed using the PACKMOL package,\cite{37} where LiClO\(_4\) (and PC molecules) were randomly distributed in the available space in the COF framework. The chemical structures of TAPB-PDA COF and PC can be found in Fig. S1 in the ESL.\(^\dagger\)

Here, we utilize the all-atom optimized potentials for liquid simulations (OPLS-AA).\cite{38} This force field has been shown to reproduce well the results of 2D COFs, including the TAPB-PDA COF at the density functional theory level in our previous works, in cases without external forces and at moderate applied stress.\cite{33,34,39} The OPLS parameters of ClO\(_4\) were taken from the work of Acevedo and co-workers.\cite{40} The atomic partial charges of ClO\(_4\) and PC were calculated using the ChelpG scheme\cite{41} at the oB97Xd/6-31G(d,p) level\cite{42} for consistency with the parameters of TAPB-PDA COF.\cite{33}

Electronic continuum correction allows for the reasonable description of charged particles by implicitly taking the electronic polarization effect while using the efficient classical force fields.\cite{15,16} ECC has been successfully applied in studying chemistry- and biology-related problems, and recently, electrolytes for lithium-sulfur batteries.\cite{36} The core idea of ECC is that

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the corrected partial charge writes as: $q^ECC_i = \frac{q_i}{\sqrt{\varepsilon_{el}}}$

(1)

where $\varepsilon_{el}$ is the high-frequency dielectric constant of the medium. In most relevant cases, $\varepsilon_{el}$ is close to 2. In our simulations, the partial charges for lithium ions and all atoms in ClO$_4^-$ were scaled by 0.7. Our benchmarks show that the OPLS force field with this correction leads to a diffusion coefficient of lithium ions in propylene carbonate of $1.6 \times 10^{-6}$ cm$^2$ s$^{-1}$ (see Fig. S2 in the ESI†), which is within the experimental range of $1.2 \times 10^{-6}$–$2.6 \times 10^{-6}$ cm$^2$ s$^{-1}$. All MD simulations were performed using the GROMACS (2021.5) package. The smooth particle–mesh Ewald (PME) method was used for electrostatic interactions. The time step is 1 fs. The systems were brought to 298 K over 5 ns and simulated for 200 ns in total. The last 100 ns-trajectory was used for analysis. Velocity rescaling and Nose–Hoover thermostats were used for equilibrium and production simulations, respectively. For each system, snapshots of the structures were saved every 0.1 ns. The coordinates of COFs, Li$^+$, ClO$_4^-$, and PC molecules were then extracted and used for further analysis.

The mean square displacement (MSD) of lithium ions is expressed as:

$$\text{MSD}(t) = \frac{1}{N} \sum_{i=1}^{N} [r_i(t) - r_i(0)]^2$$

Fig. 1 (a) Top and (b) side view of the modeled $2 \times 2 \times 20$ TAPB-PDA COF supercell. $a = b = 7.4$ nm, $c = 7.0$ nm, $\alpha = \beta = 90^\circ$, $\gamma = 120^\circ$. $a$ and $c$ are aligned with the $x$ and $z$ directions, respectively.

Fig. 2 (a) Top and (b) side view of the snapshot at 200 ns for TAPB-PDA COF mixed with LiClO$_4$. (c) A tilted view of the same structure with representative local structures of Li$^+$, ClO$_4^-$, and COF. Red spheres represent Li$^+$. Green spheres and rods represent ClO$_4^-$. "View Article Online"

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where \( N \) is the total number of lithium ions, and \( r_i(t) \) is the coordinate of lithium ion \( i \) at time \( t \). Since we are mainly considering lithium-ion transport through the pores (in the \( z \)-direction), it is useful to use the one-dimensional version of eqn (2):

\[
\text{MSD}_{1D}(t) = \frac{1}{N} \sum_{i=1}^{N} [r_{z,i}(t) - r_{z,i}(0)]^2
\]

where \( r_{z,i} \) is the coordinate of lithium ion \( i \) in the \( z \)-direction. The self-diffusion coefficient is then calculated as:\textsuperscript{49}

\[
D_{1D} = \frac{1}{2} \lim_{t \to \infty} \frac{\text{MSD}_{1D}(t)}{t}
\]

where \( t \) is time. The conductivity of lithium ions can be obtained based on the following relationship:\textsuperscript{50}

\[
\sigma_{\text{Li}^+} = \frac{e^2 c_{\text{Li}^+} D_{1D}}{k_B T} = \frac{1}{2} \frac{e^2 c_{\text{Li}^+}}{k_B T} \lim_{t \to \infty} \frac{\text{MSD}_{1D}(t)}{t}
\]

where \( e \) is the elementary charge, \( k_B \) is the Boltzmann constant, \( T \) is temperature, and \( c_{\text{Li}^+} \) is the concentration of \( \text{Li}^+ \).

### 3. Results and discussion

The simulations show that \( \text{LiClO}_4 \) forms clusters of a few nanometers, as illustrated in Fig. 2. The strong electrostatic interactions between ions \( \text{Li}^+ \) and \( \text{ClO}_4^- \) bind them closely...
together. These clusters interact with the COF via van der Waals forces and are attached to the walls of the COF pores. We note that the LiClO₄ clusters do not penetrate the COF layers. As suggested in the radial distribution function \( g(r) \) in Fig. 3(a), ClO₄⁻ forms shells around Li⁺ with a typical center-of-mass distance of 3.4 Å. As for the corresponding atoms, Li⁺ forms short contacts with the oxygen atoms in ClO₄⁻ with a strong peak at 2.1 Å (Fig. 3(b)), which agrees well with the value of ~2.0 Å from \textit{ab initio} molecular dynamics simulations.²⁷ From Fig. 3(a) and (c), it can also be seen that the closest Li⁺–Li⁺ distance ranges from 3 Å to 7 Å, and a second ClO₄⁻ shell from the center Li⁺ forms at ~6–8 Å. Overall, these data suggest that lithium ions are closely bound to the ClO₄⁻ counterion inside the LiClO₄ clusters. The strong peaks of the radial distribution functions in Fig. 3(a)–(c) at short distances and declining trends at long distances are consistent with the nanometer size of the LiClO₄ clusters. The radial distribution function in Fig. 3(d) suggests a contact around 2.2 Å between Li⁺ and the nitrogen atoms in the imine linkage of the TAPB-PDA COF. Interestingly, the interaction between LiClO₄ and TAPB-PDA COF induces structural deformation of the COF and leads to increased degrees of layer mismatch (also see Fig. S3 and S4 in the ESI†). As Fig. 2(b) shows, the pore walls sink in the opposite direction of the attached LiClO₄ cluster.

Adding PC leads to more significant monomer unit displacement (Fig. S4, ESI†) and more loosely bound cations and anions. Fig. 4 Snapshots at 200 ns for TAPB-PDA COF mixed with LiClO₄ with (a) 10 wt%, (b) 20 wt% and (c) 40 wt% PC. Red spheres, green rods and cyan lines represent Li⁺, ClO₄⁻ and PC molecules, respectively.
anions inside the TAPB-PDA COF. With increasing PC ratio, the peaks in the radial distribution functions in Fig. 3(a)–(c) get weaker at short ranges, which suggests increased distances among Li\(^+\) and between Li\(^+\) and ClO\(_4^-\). As Fig. 4 demonstrates, Li\(^+\) and ClO\(_4^-\) are well dispersed in the space where the PC molecules occupy, unlike in Fig. 2 where LiClO\(_4\) forms localized clusters. At higher PC ratios, the Li\(^+\)–N peak in Fig. 3(d) also decreases, which suggests that more Li\(^+\) are located away from the walls of the COF pores. On the other hand, the locations of the strongest peaks in Fig. 3(a)–(d) remain similar to those in the case without PC. This suggests that the local configurations of Li\(^+\) that is still in contact with ClO\(_4^-\) and TAPB-PDA COF could remain similar. Li\(^+\) interacts mainly with the oxygen atoms in PC, particularly the one that forms a double bond to C. This is demonstrated by the strong peak at 2.1 Å in the radial distribution function of Li\(^+\) and O=C in Fig. 3(e). Furthermore, our data suggest that Li\(^+\) tends to coordinate to PC in a side configuration instead of a top configuration, as shown in Fig. 5(a). The reason is as follows: a dominating top configuration would result in one prominent peak in the radial distribution function of Li\(^+\) and O–R (PC), whereas most Li\(^+\) coordinating in a side configuration leads to two prominent peaks as shown in Fig. 3(f). Representative structures of ClO\(_4^-\) and PC-coordinated lithium ions are shown in Fig. 5(b) and (c).

The formation of LiClO\(_4\) clusters in the absence of PC leads to localized distributions of the anions and cations in the TAPB-PDA COF. Indeed, as Fig. 6(a) illustrates, Li\(^+\) and ClO\(_4^-\) only occupy a portion of the available space in TAPB-PDA COF in a non-continuous manner. Since Li\(^+\) and ClO\(_4^-\) are closely bound, their occupations are largely overlapped. On the other hand, the distribution of PC molecules is more uniform, which suggests that they are more mobile than Li\(^+\) and ClO\(_4^-\) and spread more easily into the TAPB-PDA COF pores. In addition, Li\(^+\) and ClO\(_4^-\) are primarily distributed inside the PC region and form a good mixture, as shown in Fig. 6(b) and (c). As a result, the Li\(^+\) and ClO\(_4^-\) distributions become more uniform and continuous pathways form, suggesting easier motion inside the COF pores.

The fact that LiClO\(_4\) does not distribute uniformly in the COF pores and the absence of continuous lithium transport pathways can be detrimental to lithium-ion transport. The above discussions show that lithium ions are limited to their clusters or the PC region when present. As a result, when lithium ions approach the boundaries of LiClO\(_4\) clusters (or the PC region), their motion may be slowed. To confirm this speculation, we quantify the ionic motion by calculating the MSD in the z-direction according to eqn (3) (we note that ion transport across the channel walls to an adjacent pore is unlikely since ions are not observed in between the COF sheets). As shown in Fig. 7(a), the increase of MSD of Li\(^+\) with time slows down at longer distances, which agrees with the above speculation. A few other observations include: the mean square deviations of Li\(^+\) and ClO\(_4^-\) are of similar strength, suggesting similar moving speeds; PC molecules are more mobile than Li\(^+\) and ClO\(_4^-\); increasing the amount of PC leads to larger MSDs for both Li\(^+\) and ClO\(_4^-\), which demonstrates increased ionic motions.

The MSDs, while deviating from linearity over long time scales, can be used to shed light on the Li\(^+\) conductivities. For the system without PC, \(\sigma_{\text{Li}^+}\) is roughly estimated to be 1.4 \(\times\) 10\(^{-5}\) S cm\(^{-1}\) (\(D_{\text{Li}^+} = 3.0 \times 10^{-9}\) cm\(^2\) s\(^{-1}\)), while for the 40 wt% PC system it increases to 7.4 \(\times\) 10\(^{-5}\) S cm\(^{-1}\) (\(D_{\text{Li}^+} = 1.6 \times 10^{-8}\) cm\(^2\) s\(^{-1}\)). These values are on similar orders to the reported experimental ionic conductivities of COFs.\(^{12,25}\) The addition of PC molecules leads to increased ionic conductivity, highlighting its beneficial effect on promoting the motion of lithium ions in TAPB-PDA COF.

Since the motion of Li\(^+\) is largely limited to the LiClO\(_4\) clusters or the PC regions, it is likely that the movement of lithium ions over long distances inside the COF pores could proceed with the help of migration of the LiClO\(_4\) clusters or the PC regions. To further improve the ionic conductivity of COFs,
efforts need to be taken to increase the tendency of mixing between the ionic species and COFs and suppress the appearance of ion clusters, which might benefit from mimicking the role of PC molecules in the molecular structure design. The molecular-level engineering of microscopic ion-COF configurations could be key to realizing high-performance, all-solid-state electrolytes.

4. Conclusions

In summary, molecular dynamics simulations with electronic continuum correction were applied to study lithium-ion distribution and motion in the imine-linked TAPB-PDA COF. The efficient force fields enable us to model trajectories as long as 200 ns with experimentally relevant Li loading and propylene carbonate amounts.

LiClO$_4$ tends to form clusters and attach to the walls of the pores of TAPB-PDA COF. Li$^+$ ions coordinate with the oxygen atoms in ClO$_4^-$ and the nitrogen atoms in the imine linkage, with typical distances of 2.1 Å and 2.2 Å, respectively. The PC molecules blend into the LiClO$_4$ clusters and expand the space that Li$^+$ can occupy in the TAPB-PDA COF framework. Lithium ions are found to coordinate with the oxygen atoms in PC in a side configuration, with coordination lengths ranging from 2.0 Å to 2.2 Å.

The location of Li$^+$ is primarily restricted to the LiClO$_4$ clusters, and the formation of continuous transporting pathways is difficult. In comparison to the ionic species, PC molecules are more mobile. Adding PC leads to a more uniform distribution of Li$^+$ and makes it easier for lithium ions to spread in the pores of the COFs. This helps the formation of continuous ion transport pathways and easier ionic motion inside COFs.

The simulation protocols established here demonstrate efficient modeling of Li-ion motions in COF-based systems, thus being beneficial to the further development of high-throughput molecular screening methods for accelerated...
materials discovery. Overall, these results indicate that, in order to further improve the ionic conductivities of COFs, molecular design and engineering can target suppressing the appearance of ion clusters and promoting the formation of continuous ion transport pathways. Such strategies may benefit from mimicking the role of PC molecules as revealed here.

Conflicts of interest
There are no conflicts to declare.

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