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A hydro-thermophoretic trap for microparticles near a gold-coated substrate†

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Optical tweezers have revolutionised micromanipulation from physics and biology to material science. However, the high laser power involved in optical trapping can damage biological samples. In this context, indirect trapping of microparticles and objects using fluid flow fields has assumed great importance. It has recently been shown that cells and particles can be turned in the pitch sense by opto-plasmonic heating of a gold surface constituting one side of a sample chamber. We extend that work to place two such hotspots in close proximity to each other to form a very unique configuration of flow fields forming an effective quasi-three-dimensional 'trap', assisted by thermophoresis. This is effectively a harmonic trap confining particles in all three dimensions without relying on other factors to confine the particles close to the surface. We use this to show indirect trapping of different types of upconverting particles and cells, and also show that we can approach a trap stiffness of 40 fN μm^{-1} indicating a weak confinement regime without relying on feedback.

I. Introduction

The manipulation of micrometer-sized particles, particularly their high-precision positioning and confinement, remains an active area of research with many applications in physics, biology and materials sciences. Examples of the strategies utilised to confine microparticles are optical,[1–5] magnetic,[6–8] electrokinetic,[9,10] acoustic,[11] thermophoretic,[12] and thermo-capillary.[13] However, some of these techniques are limited by the necessity of special material properties of the confined objects or the environment. To overcome this limitation, hydro-dynamic trapping has been successfully utilized, and is becoming particularly attractive for the life sciences, but the optical control remains limited. Current hydrodynamic trapping strategies can be categorized into contact-based methods,[14,15] where dissolved particles are immobilized against either walls, wells, posts or other obstacles by fluid flow, and non-contact based methods, where particles can be confined in stagnation-point flows,[16,17] microvortices[18] or microeddies.[19]

Even though current hydrodynamic trapping methods pose reduced constraints on the material properties of the confined particle,[20] high-precision manipulation of particles requires the use of extremely precise and stable microfluidic pumps and accessories. Moreover, these methods cannot be used to generate flows locally in closed chambers, being global, typically ranging between pumps and outlets rendering the spatial resolution of such techniques much lower than many optical technologies. Active feedback-based techniques have also been used to confine locally, for example with thermo-viscous flows.[16,17] However, such methods can only confine microparticles in two-dimensions.

In this paper, we present a new method to create a quasi three-dimensional (3D) trap for microparticles from the combined effects of thermophoresis[21–23] and hydrodynamics (thermo-plasmonic flows[24–26] generated by two heated spots on a gold-coated substrate). The hotspots are heated by illumination with infra-red lasers, which induce thermoplasmonic convection currents. When two such hotspots are placed close to each other, the advection of a particle by thermoplasmonic flow confines it near the substrate and along the line joining the hotspots. See Fig. 1 for a schematic and Section 3.3 for a detailed description. The confinement along the line joining the traps is by opposing thermophoretic forces due to each hotspot. These two effects combine to form a quasi-3D hydro-thermophoretic trap. We show that this trap can confine upconverting particles of various sizes and *Dictyostelium* cells in quasi-3D. We also find that these particles continue to rotate in the out-of-plane sense, thereby implying that these are not resting on the substrate. We can move the set of hotspots which then moves the trap and relocates the confined particle. We also show that we can control the location of the confinement along

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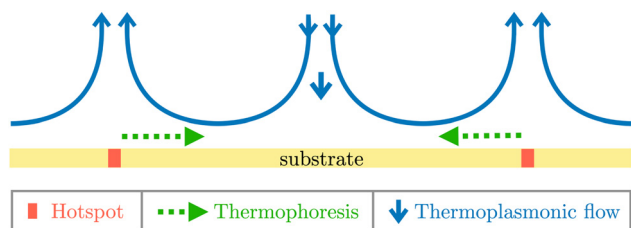[b] Department of Physics, IIT Madras, Chennai 600036, India. E-mail: rsingh@iitm.ac.in

Fig. 1 Schematic diagram for the mechanism of quasi-3D trapping of microparticles through the combined effects of thermophoresis and thermoplasmonic flows. Both are ensued by laser heating a gold-coated substrate. See text.

Fig. 2 FESEM images of upconverting particles with diagonal lengths (a) 5 μm, (b) 3 μm, (c) 1.5 μm and (d) 500 nm.

the line joining the two hotspots by tuning the power of the two lasers. This hydro-thermophoretic trap confines in full three dimensions without relying on any global fluid flows through microfluidic pumps, *etc.* Our strategy is different from that employed in some thermophoretic trapping schemes,[23,27–31] which have much thinner sample chambers, and the actual confinement is only two-dimensional.

The thermoplasmonic flow that develops as a consequence of heating of a gold substrate, as shown in Fig. 1, is well-known.[24–26,32] It can also be envisaged that these flows generate a saddle point in the middle of two such hotspots. However, we show how to obtain a three-dimensional stable fixed point with assistance from thermophoresis and thermoplasmonic flows. Such an indirect quasi-3D confinement has never been observed before. We describe this in detail below.

The organization of the rest of the paper is as follows. In Section 2, we describe the experimental set-up used to create a quasi-3D trap for microparticles. Section 3 contains details of our experimental and theoretical results. This section also rationalizes the mechanism for quasi-3D trapping upconverting particles of various sizes and *Dictyostelium* cells. We conclude in Section 4 by summarising our results and suggesting directions for future work (Fig. 2).

II. Experimental system

The experiments were carried out using an optical tweezers setup (OTKB/M, Thorlabs, USA) in an inverted-microscope configuration, as shown in Fig. 3. The objective lens is a 100×, oil-immersion type with 1.3 Numerical Aperture (N.A.) from Olympus while the condenser is E plan 10× with 0.25 N.A. (air-immersion) from Nikon. A diode laser with a wavelength of 1064 nm (Lasever, 1.5 W maximum power) and a butterfly laser with a wavelength of 975 nm (Thorlabs, USA, 300 mW maximum power) were employed for the experiments. The power readings were made at the sample chamber in the experiment by using a power meter (PM100D, Thorlabs). The lasers are directed into the sample chamber through the Dichroic Mirror 1, after passing *via* a polarizing beam splitter. An LED is used to illuminate the sample chamber through Dichroic mirror 2 and eventually the visible light is collected by a CMOS camera through dichroic mirror 2 (Thorlabs, USA). The sample is prepared by dispersing the particles or cells in water, 20 μl of which is
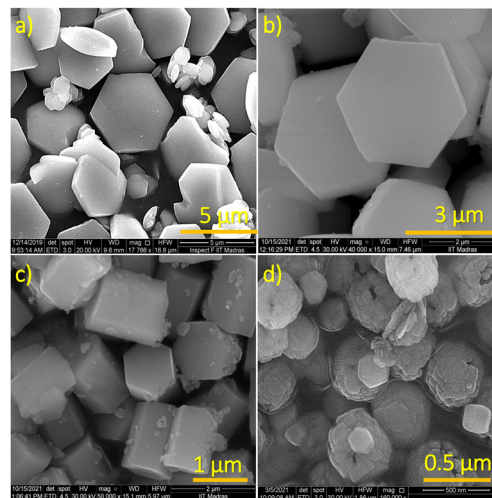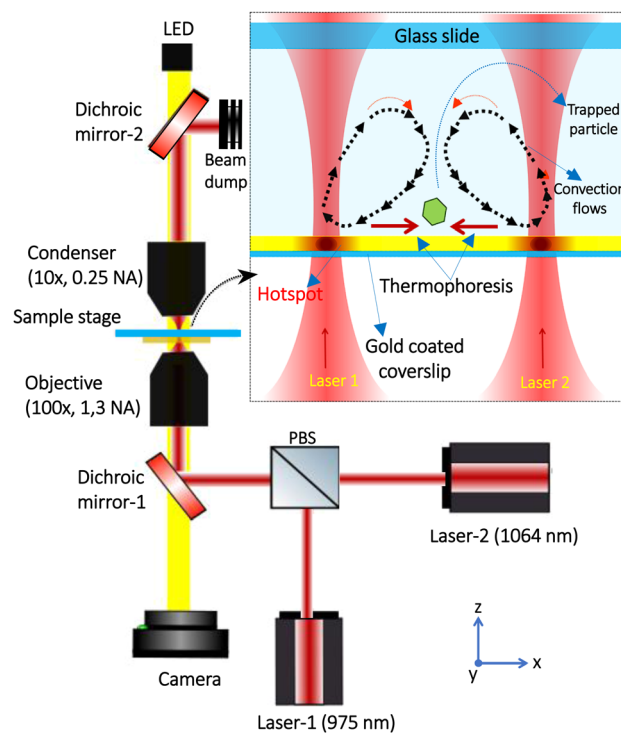

Fig. 3 The above figure represents the schematic diagram of the experiment. The extended view of the sample chamber shows the three dimensional confinement of a hexagonal shaped particle at an equilibrium position due to the thermal convection currents. The thermal currents are generated by focusing two laser beams (with wavelengths 975 nm and 1064 nm) at optimum powers on a gold-coated surface, with a separation between the beam spots of 15 μm.

transferred to the sample chamber using a micro-pipette. The sample chamber consists of a glass slide of size 75 mm × 25 mm × 1.1 mm (Blue star, number 1 size, English glass), on the top of which, the sample is mounted with a gold-coated glass coverslip

(Blue star, number 1 size, English glass). A thin film of gold having a thickness of 30 μm is coated on the glass coverslip of thickness 170 μm. The whole system is then inverted and put on the sample stage (Thorlabs Nanomax 300 – piezoelectric stage) so that the gold layer comes in direct contact with the sample, as shown in Fig. 3.

A. Preparation of gold coating

For making the gold film layer, the glass substrate was cleansed in an ultrasonic bath with acetone, IPA, and de-ionized water for 5 minutes each, and dried with nitrogen. To improve the adhesion of the gold, 5 nm of chromium was first evaporated onto the substrate at a rate of 0.05 nm s^{-1}, followed by 30 nm gold evaporation at 0.1 nm s^{-1}. A quartz crystal monitor was used to check the thickness of the deposition while the pressure in the evaporation chamber was maintained at 1 nbar throughout the process.

B. Preparation of upconverting particles

The upconverting particles used in the experiment are all prepared by the basic hydrothermal method. Preparation of 5 μm particles is already reported in ref. 33. The particles with diagonal lengths 3 μm, 1.5 μm and 500 nm are iron co-doped upconverting particles.[34]

In order to prepare the hexagonal particles with diagonal length of 3 μm (NaYF$_4$:Er,Tb, 15 at% of Fe), 0.126 M yttrium nitrate (Y(NO$_3$)$_3$, 63 at% of Y) and 0.3 M of sodium citrate (Na$_3$C$_6$H$_5$O$_7$) were mixed with 14 ml of water and stirred vigorously for 15 minutes. To this solution, 40 mM ytterbium nitrate (Yb(NO$_3$)$_3$, 20 at% of Yb), 4 mM erbium nitrate (Er(NO$_3$)$_3$, 2 at% of Er) and 30 mM ferric nitrate (Fe(NO$_3$)$_3$, 15 at% Fe) in 21 ml of water were added, resulting in a milky white solution. This solution is then turned into transparent by adding 0.5 M of Sodium Fluoride (NaF) in 67 ml water. Magnetic stirring is continued for 1 hour. The transparent solution is then transferred into a 200 ml autoclave (Teflon lined) and sealed tightly. This is then heated in a muffle furnace at 200 °C for 12 hours. After allowing to cool down to room temperature, this solution is then washed with water and ethanol four times and dried at 100 °C. The sample in powdery form is obtained after the drying process.

The particles of diagonal length 1.5 μm (NaYF$_4$:Er,Tb, 30 at% of Fe) were also prepared by the same protocol, except with optimisations in the concentrations of Ferric Nitrate and Yttrium Nitrate to 0.06 M and 0.096 M, respectively.

C. Preparation of *Dictyostelium* cells

The *Dictyostelium* cells (wild type D. Discoideum AX2) were prepared by inoculating the spores in 90 mm tissue culture plates containing axenic HL5 growth medium (HLG01XX – Formedium, Norfolk, UK, pH 6.4) supplemented with penicillin (100 units per ml) and streptomycin sulphate (100 mg ml^{-1}). The cultures were then incubated at 22 °C until semi-confluent plates were obtained. The mid-log cells were collected in ice cold KK2 buffer (2.2 g l^{-1} KH$_2$PO$_4$ and 0.7 g l^{-1} K$_2$HPO$_4$, pH 6.4), washed twice and stored on ice for further experiments.

D. Estimation of temperature at the hotspots

The temperature measurements at the hotspots on gold are carried out by high-sensitivity upconversion luminescence thermometry.[35–39] Here, we exploit the temperature dependent fluorescence properties of the upconversion particles when excited with NIR radiation (975 nm in our case). We use NaYF$_4$:Er^{3+},Yb^{3+} upconversion particles as contactless nano-thermometers. These particles are well-known for their broad working-temperature range[38] (298–393 K) coupled with a decent sensitivity. The particles exhibit the characteristic transitions in Er ions as $^2H_{11/2} \rightarrow {}^4I_{15/2}$ (517–527 nm, green), $^4S_{3/2} \rightarrow {}^4I_{15/2}$ (535–560 nm, green), and $^4F_{9/2} \rightarrow {}^4I_{15/2}$ (640–680 nm, red) prominent fluorescence bands.[37] Such an upconversion particle is illuminated with a laser of wavelength 975 nm just below the gold surface, as shown in Fig. 4(a), and the emission from the particle in the back-scattered direction is collected using a spectrometer (Research India).

Since the particle is held close to the gold surface, the area on which the laser falls serves as the hotspot in this configuration. The localized surface plasmonic heating on the gold substrate caused by the laser irradiation significantly increases the temperature of its surroundings which in turn induces the convection flows. This temperature change is being sensed by
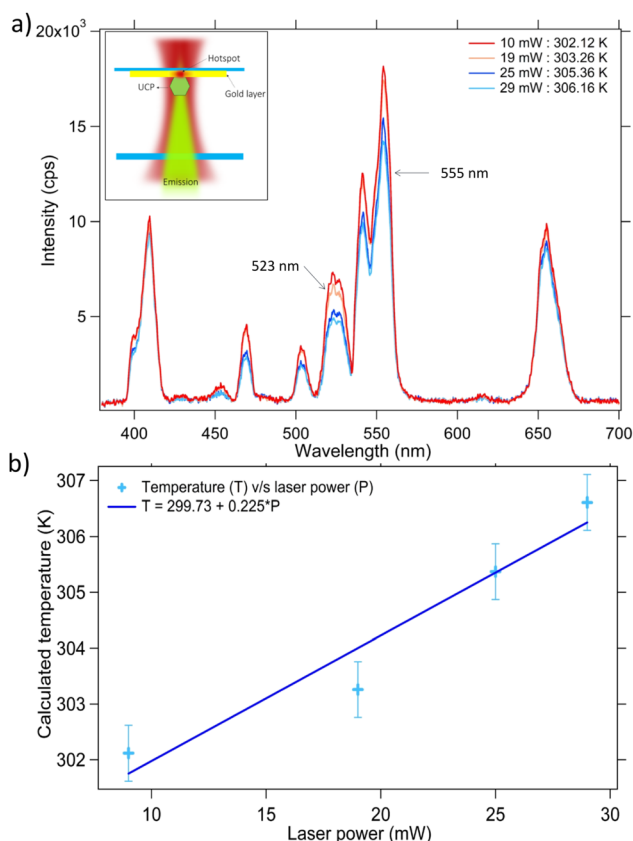

Fig. 4 (a) The emission spectra of the particle just below the gold layer at different laser powers. (b) The linear relationship between incident power and the calculated temperature. The laser powers are measured at the sample plane.

the particle in its emission spectra, as shown in Fig. 4(a). We exploit the strong temperature dependence of spectral lines centered at 523 nm and 555 nm for the approximate estimation of the local temperature. The fluorescence intensity ratio (FIR) of the particle is given by,[36]

$$\mathrm{FIR}(\varDelta) = \frac{I_{555}}{I_{523}} = A\mathrm{e}^{\frac{\delta E}{k_B T}} \qquad (1)$$

ehere I, A, δE, k_B, and T represent the intensities of the spectral lines, preexponential constant, energy gap between the two transitions, Boltzmann constant and absolute temperature, respectively. The emission spectra of the particle at room temperature ($T = 298$ K) is taken as the reference from which A can be reduced (0.152). As the temperature of the system is raised using laser power, the spectral intensities (I_{555}, I_{523}) fall down, which increases the FIR ($T_0 \rightarrow T_1 \Rightarrow \varDelta_0 \rightarrow \varDelta_1$). Then, the increased temperature at the hotspot is given by,[37]

$$\frac{1}{T_1} = \frac{1}{T_0} - \frac{k_B}{\delta E}\ln\left(\frac{\varDelta_1}{\varDelta_0}\right) \qquad (2)$$

and the sensitivity of the thermometer can be determined using,

$$\delta S_r = \frac{\delta \mathrm{FIR}}{\delta T} \times 100\% \qquad (3)$$

The temperature sensitivity of NaYF$_4$:Er^{3+},Yb^{3+} particles that we used is calculated to be 4.97% K^{-1}. The temperature at the hotspot at any incident laser power can be found from the linear relationship between them, as shown in Fig. 4(b).

E. The experiment

The laser beams (namely, laser-1 (975 nm) and laser-2 (1064 nm)) are focused on this gold film at optimum powers to generate the two hotspots (H1 and H2, respectively). The hotspots are displaced in the x-direction by a separation of 14 μm to create the hydro-thermophoretic trap for a hexagonal shaped upconverting particle of diagonal length 5 μm. The laser power at both the hotspots is optimised until the particle gets confined at the middle region. The separation between the hotspots is reduced to 9 μm and 6 μm to trap smaller hexagonal shaped upconverting particles having diagonal lengths of 3 μm and 1.5 μm, respectively. The powers of both lasers were adjusted simultaneously to observe the dynamics of the particles in the generated hydro-thermophoretic trap. Furthermore, the hotspots H1 and H2 are moved 20 μm apart to trap *Dictyostelium* cells and the subsequent spores. We use the MTrack plug-in of ImageJ software to determine the position of the centroid of the trapped particle as a function of time.

III. Results and discussion

In this section, we describe our main experimental and theoretical results.

A. Quasi-3D trapping upconverting particles

We find that particles and cells having different structural morphologies and sizes get confined three dimensionally at an equilibrium position between the two hotspots. A hexagonal shaped upconverting particle of diagonal length 5 μm is trapped at a distance of 6 μm from each hotspot, as shown in Fig. 5(a). The powers of the laser beams at hotspots H1 and H2 were recorded to be 9 mW and 8.7 mW, respectively, and the estimated temperature at each hotspot is 302.6 K ($\Delta T = 4.6$ K).

The particle is spatially confined in all three dimensions but also observed to be executing different out-of-plane rotations, namely roll[34] and pitch[40–43] due to the thermoplasmonic fluid
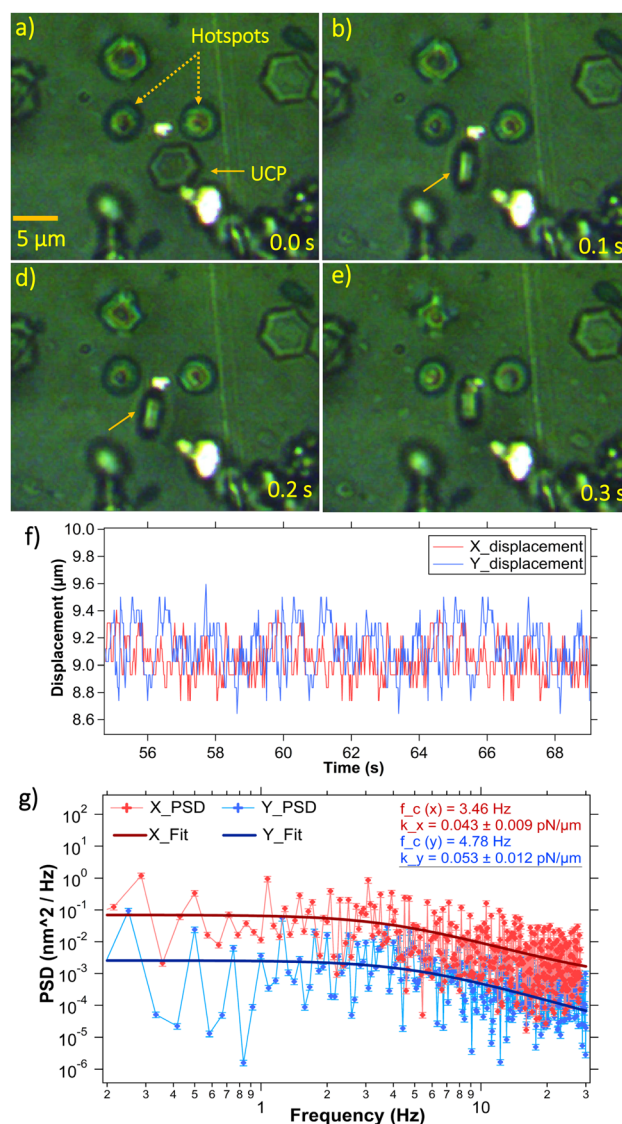

Fig. 5   (a)−(e) A hexagonal shaped upconverting particle (UCP) of diagonal length 5 μm getting trapped between the convection currents generated by the hotspots on gold. (f) x and y displacement time series of the trapped particle. (g) The power spectral densities of the trapped particle obtained from (f), fitted with Lorentzian curves. The trap stiffness along the x and y directions is calculated to be $k_x = 43 \pm 9$ fN μm^{-1} and $k_y = 53 \pm 12$ fN μm^{-1}, respectively.

flow. It is not exactly clear why the particle executes this rotation but it could arise from minor differences in fluid velocities in the local neighborhood of the equilibrium location. We use the M-track plug-in of ImageJ software to generate the x and y – displacement time series, as shown in Fig. 5(f).

The power spectrum obtained from the same time-series is fitted with a Lorentzian curve and calibrated.[44] The trap-stiffnesses are calculated in both the x and y directions (see Fig. 5(g)). Hence, it is observable that our indirect hydro-thermophoretic trap behaves remarkably similar to a conventional harmonic optical trap,[45] without relying on particle's refractive index and size.

We also trap 3 μm and 1.5 μm sized hexagonal shaped upconverting particles to test the applicability of our trap on smaller particles. Both 3 μm and 1.5 μm sized particles get confined in three dimensions, between the hotspots, as shown in Fig. 6(a) and 8(a), respectively. We observe that a 3 μm sized trapped particle follows the trap when we displace the set of hotspots on the gold substrate at a speed of 2.2 μm s^{-1} in the x-direction as well as at 1.8 μm s^{-1} in the y-direction (see Fig. 6(b)–(f)). The laser powers were set to be 11 mW and 10 mW at hotspots H1 and H2 respectively. And from Fig. 4(b), the estimated temperature at the hotspots is 303.6 K ($\Delta T = 5.6$ K). The yellow arrows marked in the figures are taken as references to illustrate the effect.

The centroid position of the trapped particle is then tracked to generate a displacement time series. The spatial distributions of the particle in the x and y directions obtained from the time series are fitted with a Gaussian curve, as shown in Fig. 6(g)–(h). The trap stiffness is calculated from the same Gaussian fit (Fig. 6(h)).

B. Tunability of the center of the quasi-3D trap

We also observe that a 1.5 μm sized confined particle follows the same trap properties. In order to illustrate the effect of confinement by the set of hotspots, we turn off one of the lasers. The particle displaces close to the on hotspot when we turn off the other laser, as shown in Fig. 8(b), (c) and (e), (f). It can be seen that the particle executes pitch rotational motion near individual hotspots H1 and H2 as already reported (Fig. 7).[46] It is brought back to the initial hydro-thermophoretic trap by turning the laser (laser-1) at the hotspot (H1) on, as shown in Fig. 8(d).

We then direct our attention to the spatial tunability of the hydro-thermophoretic trap along the line joining the hotspots. We trap a 3 μm particle and a cluster of 500 nm sized upconverting particles, as shown in Fig. 9(a). We observe that the trapped particles move towards the hotspot H1, when the laser power at the hotspot H2 is increased from 6 mW to 9 mW, that is, from $T = 300.2$ K to 302.6 K (see Fig. 9(b) and (c)). These regain their initial positions when the power is brought back to 6 mW after a finite time interval. The trapped particles also show a similar response in the opposite direction when the laser power at hotspot H1 is increased, keeping the power at H2 constant or when the laser power at H2 is reduced further to 1 mW.
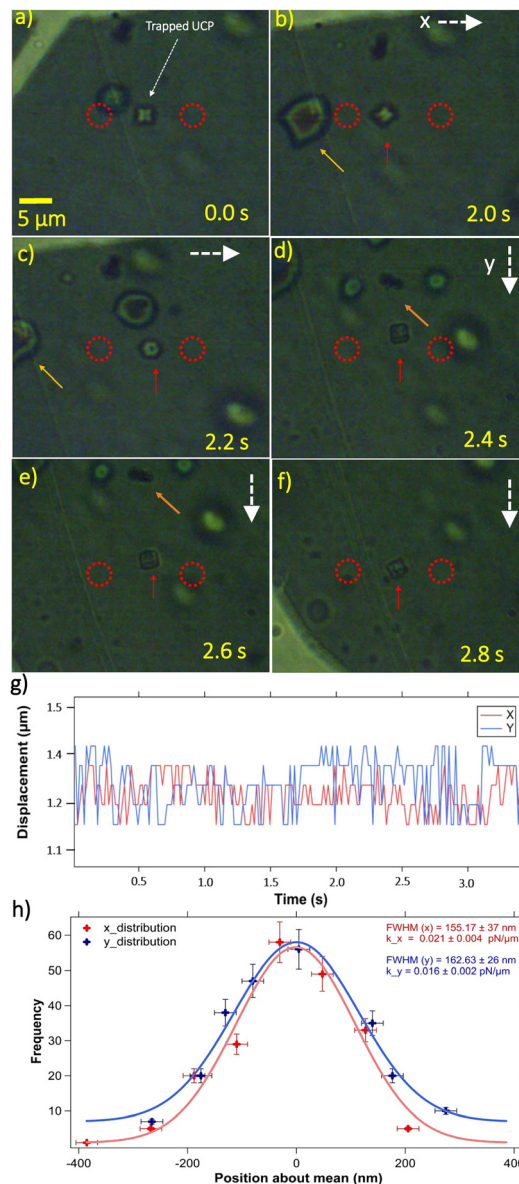

Fig. 6 (a) A UCP of diagonal length 3.2 μm confined between two hotspots on gold. The red-dashed circles in the figures represent the positions of the hotspots. (b)–(f) The particle follows the same hydro-thermophoretic trap when the stage is moved. The arrow mark on the top shows the direction in which the sample stage is moved. In (g) the x and y displacement time series of the trapped particle is shown. (h) This figure shows the calibrated histogram of the x and y-displacement time series (g). The trap stiffness is calculated to be $k_x = 21 \pm 2$ fN μm^{-1} and $k_y = 16 \pm 4$ fN μm^{-1}.

C. Mechanism of hydro-thermophoretic trapping

We now present the theory describing the formation of a quasi-3D hydro-thermophoretic trap for microparticles. We show that it is possible to trap microparticles through a combination of thermophoresis and hydrodynamics (thermoplasmonic fluid flows). Both these effects are caused by the laser heating of the gold-coated substrate, as we describe below. We first describe the ''hydro'' part of the mechanism by studying the thermoplasmonic fluid flows.
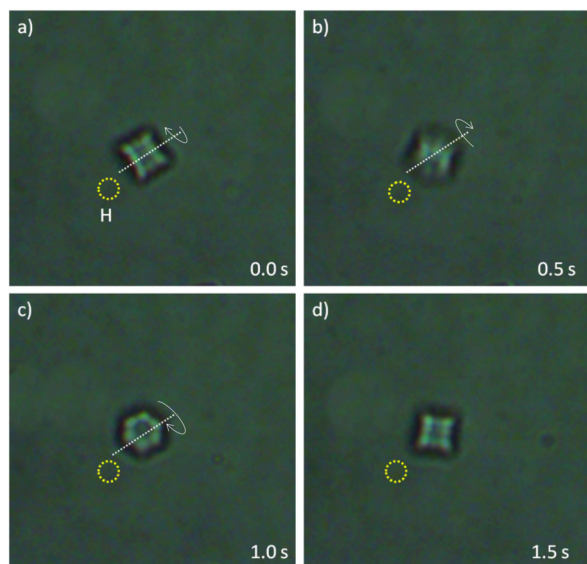
Fig. 7 A hexagonal shaped upconversion particle executing the out-of-plane rotations, caused by the convection flows near a laser hotspot on gold. The dashed line indicates the axis with respect to which the particle is rotating.

1. Thermoplasmonic flows. We now study the fluid flows produced by plasmonic heating of the gold substrate through laser radiations (see Fig. 3 for a schematic diagram of the system). The fluid flow $\boldsymbol{v}(\boldsymbol{r})$, at a point $\boldsymbol{r}$ in the bulk, satisfies the Stokes equation.[47]

$$-\nabla p + \eta \nabla^2 \boldsymbol{v} + \boldsymbol{f}_{\mathrm{T}} = 0 \qquad (4)$$

where p is the fluid pressure, η is the viscosity and $\boldsymbol{f}_{\mathrm{T}}$ is the force density in the fluid due to the plasmonic heating of the gold substrate. The fluid is incompressible $\nabla \cdot \boldsymbol{v} = 0$. In addition, the fluid flow vanishes at the plane walls of the experimental chamber.

$$\boldsymbol{v} = 0 \text{ at the walls.} \qquad (5)$$

The fluid flow is driven by the plasmonic heating of the gold substrate through laser radiations of source densities q_i.[24–26,32] We need to obtain the force density in the fluid to obtain the fluid flow from the solution of the above equations. The force density $\boldsymbol{f}_{\mathrm{T}} = \alpha \delta T \hat{z} = \alpha(T - T_0)\hat{z}$ in the fluid is obtained from the Boussinesq approximation for buoyancy-driven natural convection[24,48,49] Here $\alpha = \rho \beta g$ is a material dependent constant, while ρ is fluid density, β is the thermal expansion coefficient, g is the acceleration due to gravity, T_0 is the temperature of the undisturbed fluid and $\hat{z}$ is the unit vector along the z-direction, away from the surface. The force density driving the fluid flow depends on the temperature profile. The temperature field, at any point on the substrate, is given by the solution of the following equation[25,32]

$$\rho_{\mathrm{s}} c_{\mathrm{P}} \frac{\partial T}{\partial t} + \boldsymbol{\nabla} \cdot (\kappa \boldsymbol{\nabla} T) = -(q_1 + q_2). \qquad (6)$$

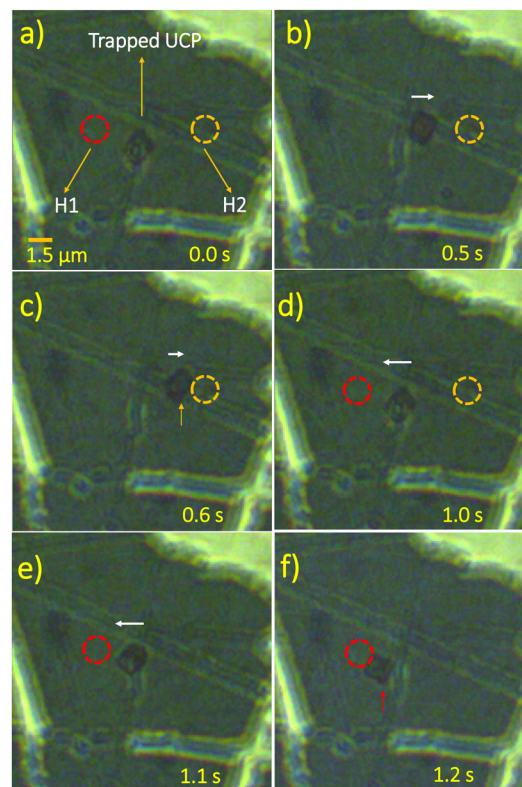**Fig. 8** Response of a cuboid shaped upconverting particle of face diagonal length 1.5 μM to the convection currents generated by each hotspot. In (a), the particle is confined at the hydro-thermophoretic trap. H1 and H2 represent the hotspots on the gold surface generated by the lasers (laser-1 (975 nm) and laser-2 (1064 nm)). Figures (b and c) show the movement of the same particle towards the conventional optical trap of a 1064 nm laser when the left hotspot (H1) is turned off. In (d), the particle is brought back to the hydro-thermophoretic trap by turning the hotspot H1 on. Figures (e and f) show the movement of the particle towards the optical trap created by the 975 nm laser when the hotspot H2 is turned off. Rotations of the particle are also observed when it reaches the individual optical trap due to the convection currents (c and f).

Here c_{P} is the heat capacity of the substrate, κ is the thermal conductivity, ρ_{s} is its density, while q_1 and q_2 are the heat source density which serve as a source term for the computation of the temperature field $T(\boldsymbol{r})$. The total heat powers generated on the hotspot from the two lasers are Q_1 and Q_2, where $Q_i = \int q(\boldsymbol{r})\mathrm{d}\boldsymbol{r}$. The temperature and heat flux are continuous at the gold-coated substrate. There is a reduction of mass density around the gold-coated substrate because of heating by the laser, which yields the upward convection of the fluid driven by the force density $\boldsymbol{f}_{\mathrm{T}}$, defined above. In the following, we obtain an expression for the temperature field and present a numerical computation of the flow field in the system.

2. Thermophoresis away from hotspots. A microparticle can self-propel in the presence of a thermal gradient due to thermophoresis,[21] even in the absence of any external force acting on it. The thermophoretic velocity of a particle is given as,[21,50,51]

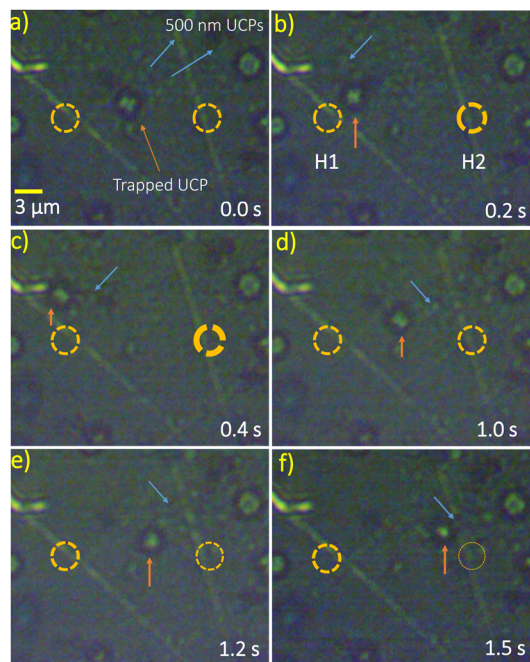$$\boldsymbol{v}_{\mathrm{T}} = -D_{\mathrm{T}} \boldsymbol{\nabla} T, \qquad (7)$$

Fig. 9 Tunability of the position the trap with the laser power. In (a), a hexagonal UCP of diagonal length 3 μm (red arrow) and a cluster of spherical UCPs with diameter 500 nm (blue arrows) are trapped. H1 and H2 are the hotspots created by the two lasers (laser-1 and laser-2, respectively). The power of laser-2 (1064 nm) is gradually increased from an initial value of 6 mW to 9 mW and 15 mW, the new positions of the trap and hence the particles are shown in (b) and (c), respectively. The particles come back to the initial positions when the laser power is brought back to 6 mW as shown in (d). In (e) and (f) the trap position is moved towards the hotspot H2 by decreasing the power of laser-2 from 6 mW to 1 mW.
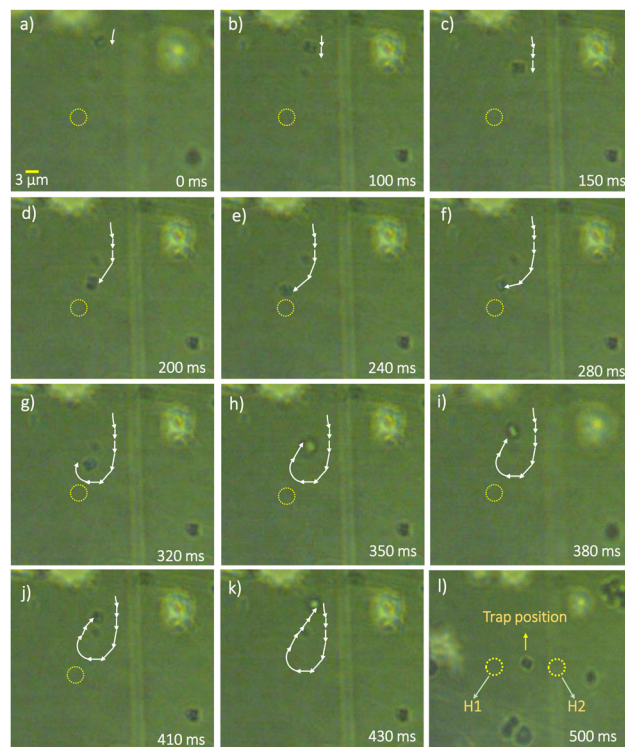

Fig. 10 The strong planar convection flows that are being followed by a 3 μm sized particle near to the laser hotspot. The particle comes to the trap position when the laser powers are matched as shown in (l). The position of the particle is tracked and shown in Fig. 11(c).

where D_T is the thermophoretic mobility.[21] For our experimental system, the thermophoretic velocity v_T is away from the hotspot. This is because the Soret coefficient $S_T = D_T/\mathcal{D}$ is positive in our system, where $\mathcal{D}$ is the diffusion constant. See Fig. 1 for a schematic diagram. Such thermophoretic motion of microparticles away from a hotspot was used in ref. 29 to create a two-dimensional trap on a gold substrate using a rotating temperature field. This was achieved by laser heating on the circumference of a circle. The sample chamber was very thin and ensured confinement in the third direction. In the following, we explain the mechanism to create a quasi-3D trap using the thermophoretic motion from two fixed lasers and thermoplasmonic flows created by them.

To proceed further, we need to obtain an explicit form of the temperature field $T(\boldsymbol{r}, t)$ at a point $\boldsymbol{r}$ in the bulk fluid. The explicit form of the temperature field will then be used in eqn (7) to obtain the thermophoretic velocity of a particle along the line joining the hotspots. A balance of thermophoretic velocities from the two hotspots gives the location of the center of the trap. The plasmonic excitation from laser heating gets thermalized at a time-scale of milliseconds, and thus, the temperature follows the laser field almost instantaneously. The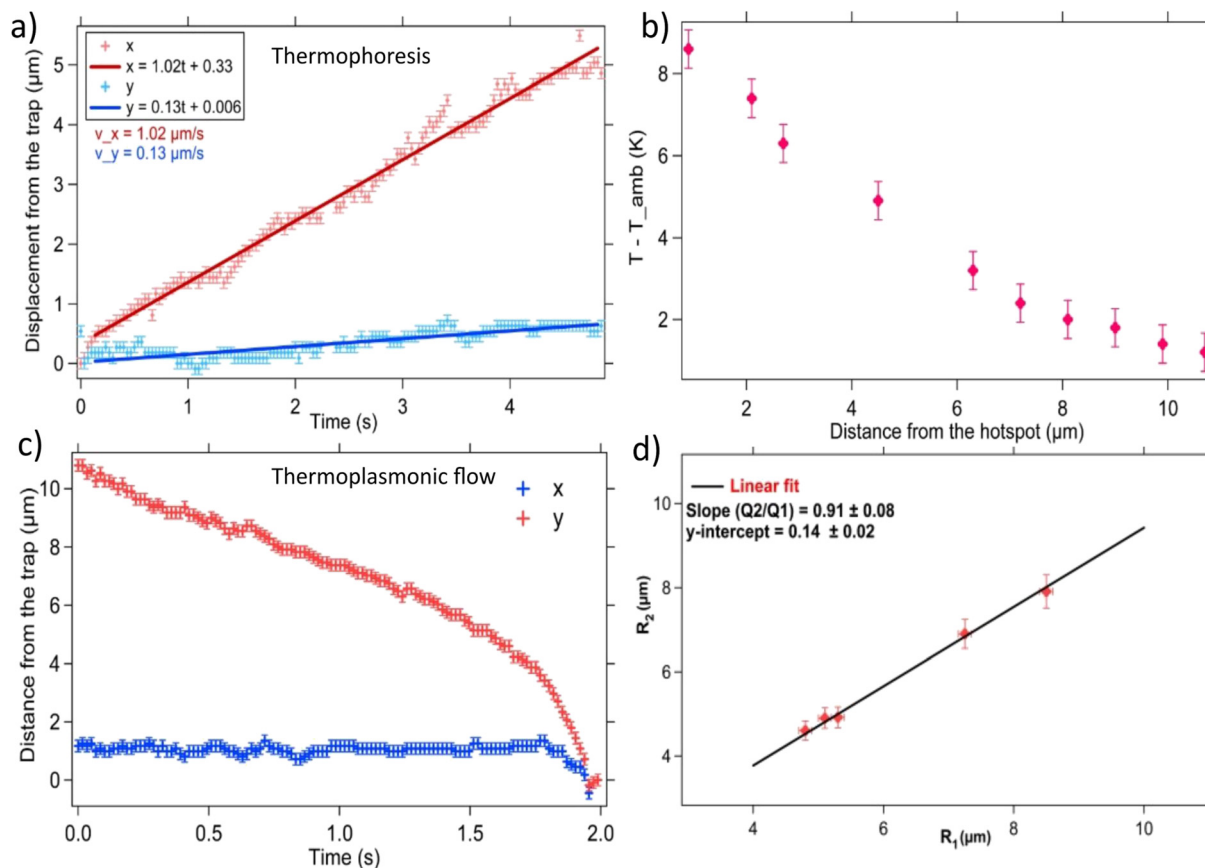 leading order instantaneous and isotropic form of the temperature field at a point $\boldsymbol{r}$, due to heating of the two hotspots, is given as

$$T(\boldsymbol{r}, t) = T_0 + \frac{Q_1}{4\pi\kappa|\boldsymbol{r} - \boldsymbol{r}_1|} + \frac{Q_2}{4\pi\kappa|\boldsymbol{r} - \boldsymbol{r}_2|}. \tag{8}$$

Here κ is the heat conductivity, Q_i is absorbed power at the ith hotspot, and $\boldsymbol{r}_i$ is the location of the ith hotspot, such that $|\boldsymbol{r} - \boldsymbol{r}_i|$ is the distance of field point $\boldsymbol{r}$ from the center of the ith hotspot. We can now use the above form of the temperature field in eqn (7) to obtain estimates for the thermophoretic velocity of a particle due to each hotspot in our setup.

The thermoplasmonic flow ensures that the particle finds itself along the line joining the hotspots, as described in detail below. A balance of the thermophoretic velocities due to the two hotspots gives the location of the trap center since its magnitude is higher than the fluid velocity along this direction. Here we have used the fact that the thermophoretic velocity of a particle due to the two hotspots is along the line joining the hotspots but in opposite directions (see also Fig. 1). It then follows that the ratio of the distance of the trap center from the location of the two hotspots can be given as

$$R_1 = R_2 \sqrt{\frac{Q_1}{Q_2}}. \tag{9}$$

Here R_1 and R_2, are, respectively, the distance of the centre of the trap from the first and second hotspot. The above

Fig. 11 (a) The thermophoretic migration of a 3 μm sized upconversion particle shown in Fig. 9. The thermophoretic velocities are found to be, $v_x = 1.02 \pm 0.21$ μm s^{-1} and $v_y = 0.13 \pm 0.04$ μm s^{-1}. (b). The temperature sensed by a 3 μm sized upconversion particle as a function of distance from the hotspot is plotted. (c) The displacement–time graph of an upconversion particle which follows the thermoplasmonic fluid flow near the hotspot is shown (see Fig. 10). In (d), the graph plotted between the distances R_1 and R_2 (obtained by varying the laser powers at the hotspots H1 and H2), along with the best linear fit. The slope gives the ratio of the square root of the laser power, $\sqrt{Q_2/Q_1}$ (kept at 0.86 ± 0.09 in experiments). This is in excellent agreement with eqn (9).
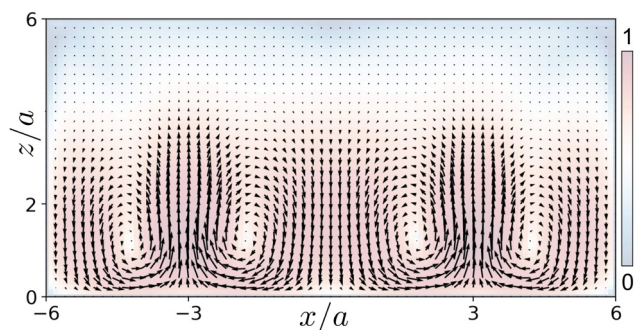

Fig. 12 Vector plot of the thermoplasmonic fluid flow in the xz-plane, overlaid on the color map of flow speed normalised by its maximum, due to laser heating of the gold substrate at $x = \pm 3a$, where a is the size of the particle. See text.

expression is in excellent agreement with the experimental observations of Fig. 11(d).

We now describe the combined effect of thermophoresis and thermoplasmonic flows using the equations given in Section 3.3.1. We consider that the gold-coated surface is in

the xy-plane, such that two hotspots are along the x-axis. We then need to solve for the Stokes equation to obtain the fluid flow. This is done by using the expression for the force density in the fluid defined in Section 3.3.1, such that $\alpha = \rho\beta g$, where $\beta = 10^{-4}$ K^{-1} is the thermal expansion coefficient,[48] while $\rho = 10^3$ kg m^{-3} is the density of the fluid, and $g = 9.8$ m s^{-2} is the acceleration due to gravity. Values for the other relevant parameters are: $T_0 = 298$ K, $c_p = 100$ J kg^{-1} K^{-1}. Using these parameters, the equations are solved using the finite element method to obtain the thermoplasmonic fluid flow. Fig. 11 contains the resulting streamlines of the fluid flow, overlaid on a pseudo color map of the flow speed, in the xz-plane due to the two hotspots along the x-axis on the gold-coated substrate. It can be seen that the heating of the gold substrate by the laser causes temperature gradients, which lead to convection flows away from the heated spot. The corresponding flow in the xy-plane, near the gold-coated surface, has been plotted in Fig. 13. From the two figures, it is clear that the flow will advect any particle in such a way that it will get pushed back to the bottom surface from the bulk due to flow in the z-direction. The flow in the y-direction will also pull the particle along the line
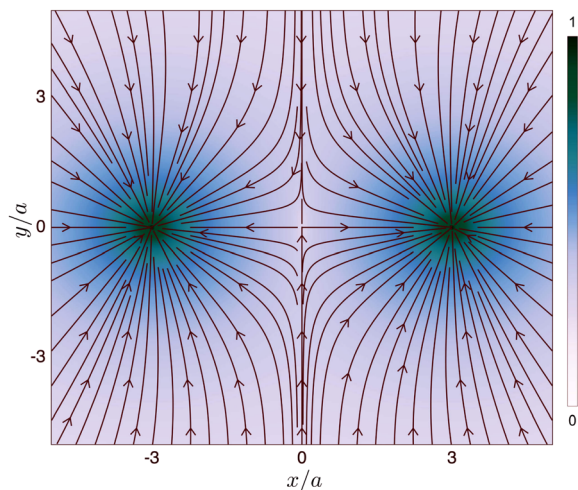
Fig. 13 Streamlines of the thermoplasmonic fluid flow in the xy-plane, overlaid on the color map of flow speed normalised by its maximum, due to laser heating of the gold substrate at $x = \pm 3a$, where a is the size of the particle. See text.

joining the two hotspots along the x-axis. We see in our experiments that particles are trapped along this line. A particle is trapped along the line joining the hotspots due to opposing thermophoretic forces acting on it from the two hotspots (as described above). To summarise, in this section, we have shown that a combination of thermophoretic and thermoplasmonic effects can confine microparticles in quasi-3D. This is the essence of the mechanism shown in the schematic diagram of Fig. 1. The location of the trap center is determined by the
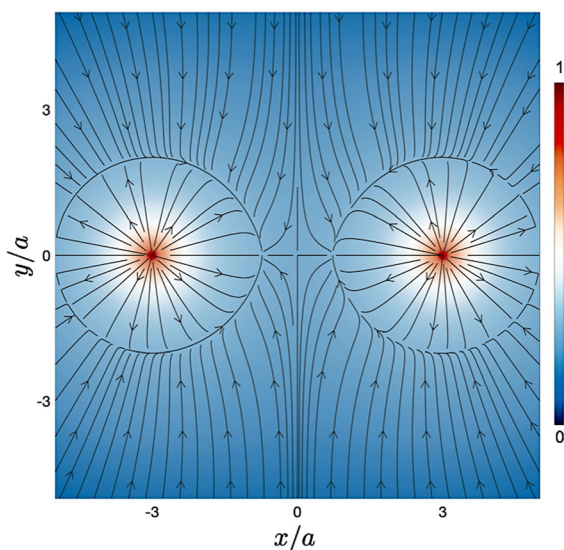

Fig. 14 Vector plot of the velocity field experienced by a particle due to the combined effects of thermophoretic drift as well as advection by the thermoplasmonic fluid flow in the xy-plane, overlaid on the color map of flow speed normalised by its maximum, due to laser heating of the gold substrate at $x = \pm 3a$, where a is the size of the particle. The dynamics along the x-direction are dominated by thermophoresis away from the hotspot, while the dynamics in the y- and z-directions are controlled by the fluid flow (see Fig. 12).

competition between opposing thermophoretic forces in the plane of the substrate (see eqn (9)). We note that our comparison for the numerically computed fluid flow and dynamics observed in the experiments is only qualitative. A detailed quantitative comparison of the theoretical fluid flow and experimentally measured velocity of particles will be presented in a future work (Fig. 14).

D. Quasi-3D trapping of biological samples

Next, we focus our attention onto trapping biological samples. We find that a 10 μm sized *Dictyostelium* cell also gets confined for 1 minute, as shown in Fig. 15(a). To trap the cell, we have
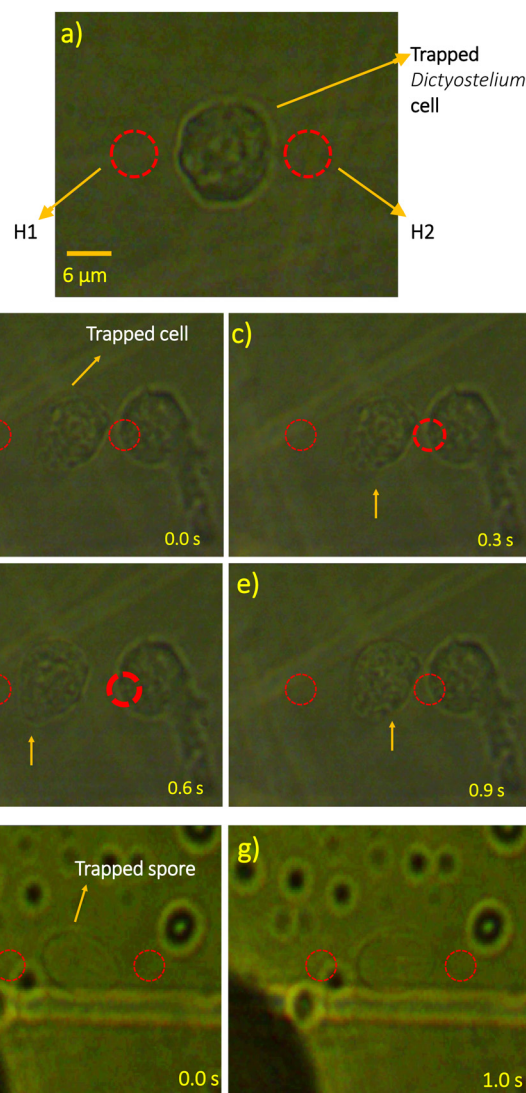

Fig. 15 Confinement of *Dictyostelium* cells and their spores at the hydro-thermophoretic trap. (a) A single cell is trapped between the hotspots H1 and H2. The trapped *Dictyostelium* cell is displaced towards the hotspot H1 as shown in (b) and (c), when the laser power at hotspot H2 is increased from 16 mW to 25 mW. In (d), the cell is brought back to the initial position by reducing the laser power at H2 to 16 mW. Figures (e) and (f) show that a spore of *Dictyostelium* is trapped at the thermoplasmonic trap for a long time.

used higher laser powers at the hotspots, 35 mW at H1 and 29 mW at H2 ($\Delta T \approx 6.9$ K). We also find that the trap does not cause any damage to the trapped living cell over experimental timescales (this is because the change in temperature at the location of the confined *Dictyostelium* cell is only about 1 °C, as shown in Fig. 11(b)) which extends the applications of our system to biological specimens. The observation of the tunability of the trap's position is also performed with the *Dictyostelium* cell (see Fig. 15(b)–(e)). Here, the laser power at hotspot H2 is increased and then decreased to ascertain the positional changes of the cell. Moreover, it is also possible to trap elongated biological structures with a length of 12 μm, such as spores of *Dictyostelium*, in quasi-3D, as shown in Fig. 15(f)–(g).

IV. Conclusions and perspectives

In conclusion, we have developed a novel method that allows for the efficient quasi-three dimensional trapping of microscopic particles and living cells. We have studied the fundamental physics behind this indirect thermoplasmonic trap by exploiting the first principles of fluid mechanics. We find that the quasi-three-dimensional confinement of particles and cells between the hotspots on gold is induced by the combined effects of thermophoresis and thermoplasmonic fluid flow. The trap that we generated is well in agreement with a fundamental harmonic trap by observation, and the forces are in the order of 50 fN for a displacement of 1 μm. The size regime of the trappable particles is determined by the laser powers and the horizontal separation between them on gold. However, we have trapped particles with sizes varying from 500 nm to 5 μm and cells having a size more than 10 μm. We observe that the indirect hydro-thermophoretic trap causes considerably less damage to the living cells (the change in temperature at the location of the confined *Dictyostelium* cell is only about 1 °C, see Fig. 11(b), and thus, no damage occurs over experimental timescales) as compared to an optical trap, while allowing us to apply forces in the order of pico newtons to the trapped particle. The control over the thermophoretic velocities of the particles with the laser powers enables us to achieve the precise positioning of the trapped particle. Moreover, in this way, controlled roll out-of-plane rotation of the particle can also be performed. Exciting future directions include studying dynamics of synthetic and biological microparticles, which cannot be trapped using conventional methods, utilizing the hydro-thermophoretic trap introduced here.

Conflicts of interest

There are no conflicts of interest to declare.

Acknowledgements

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