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Interactions between conducting surfaces in salt solutions†

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In this work, we simulate interactions between two perfectly conducting surfaces, immersed in a salt solution. We demonstrate that these forces are quantitatively different from those between (equally charged) non-conducting surfaces. There is, for instance, a significant repulsion between net neutral surfaces. On the other hand, there are also qualitative similarities, with behaviours found with non-conducting surfaces. For instance, there is a non-monotonic dependence of the free energy barrier height, on the salt concentration, and the minimum essentially coincides with a flat profile of the apparent surface charge density (*i.e.* the effective net surface charge density, some distance away from the surface, when accounting for ion neutralization), outside the so-called Stern layer. These conditions can be described as “perfect surface charge neutralization”. Despite observed quantitative differences, we demonstrate that it might be possible to mimic a dispersion containing charged colloidal metal particles by a simpler model system with charged non-conducting particles, using modified particle–ion interactions.

1 Introduction

Interactions between particles and charged surfaces in aqueous salt solutions are important and ubiquitous in many areas of soft matter. They have been thoroughly investigated over decades and their theory is also well-established.^{1–16} If the particle surfaces are weakly charged, or if the salt is monovalent, these interactions can usually be approximated by the celebrated DLVO theory.^{17,18} At high electrostatic coupling strengths, *e.g.*, in the presence of multivalent ions, numerous theoretical and experimental studies have illustrated that a simple Poisson–Boltzmann (PB) treatment, even at the non-linear level, may lead to predicted behaviours that are qualitatively wrong. The origin of this failure is the mean-field approximation upon which the PB theory is based. This amounts to a neglect of ion correlations, which are significant in the presence of strong electrostatic interactions. Of particular importance is the correlation between similarly charged ions, whereby “Coulomb holes” are effectively created, *i.e.*, a volume around ions, from which other like-charged species are excluded.

Ion correlations manifest themselves in various ways, and important phenomena that find their source in these mechanisms

(and will not be captured by a PB treatment) include: overcharging (charge reversal) whereby multivalent counterions overcompensate the bare surface charge;¹⁹ attraction between like-charged particles,^{3,4,9} and repulsion between particles of opposite surface charge.^{11,20} These phenomena are related. It is well-established that ion correlations, when sufficiently strong, will generate a short-ranged attraction between like-charged surfaces. At larger separations, however, the same correlations will lead to a long-ranged double-layer repulsion, between effectively overcharged surfaces, for a high enough concentration of the multivalent salt. Below some threshold concentration, overcharging is absent and a double-layer repulsion at long range still results, but is due to the incomplete screening of the bare surface charges. Thus, at some intermediate critical concentration value, there is a “perfect surface neutralization” point, whereby the long-range repulsive barrier is negligible.^{12–16,21–24} Experimentally, this manifests itself as a specific salt concentration where the charged particle dispersion has minimal stability. The neutralization point can also be experimentally identified through a vanishing electrophoretic mobility. These observations, and their underlying causes, have been theoretically confirmed both *via* simulations as well as more approximate treatments.

The situation is less obvious when the particles are *metallic*, or otherwise conducting.^{1,25} In this case, the strong surface polarization will induce secondary effective interactions between particles, which is a scenario considerably more difficult to treat theoretically. Despite some progress that has been made on these systems,^{26–29} questions regarding the phenomena described above (for non-conducting particles),

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remain to be validated for the conducting case. For example, it is still unclear whether a threshold salt concentration exists, above which charge reversal takes place and, if it does, how strongly does the surface conduction affect its value. Furthermore, it would also be of interest to devise simplified approaches, wherein the computationally costly effects of surface polarization can be approximately taken into account. This would be especially useful when dealing with dispersions containing colloidal conducting particles, wherein multiple image interactions are exceptionally difficult to handle.

In this work, we will simulate the interaction between two perfectly conducting planar surfaces and investigate the role played by multivalent ions in determining a point of surface neutralization (or charge reversal). We also introduce a simple effective model that mimics the conducting case by mapping it onto a model of a charged non-conducting particle with an additional (suitably chosen) particle-ion interaction.

2 Model and methods

The salt solution is described by a soft-sphere version of the so-called primitive model, wherein the aqueous solvent only exerts its influence *via* the dielectric constant, $\epsilon_r = 78.3$. The temperature is set to 298 K, whereby the Bjerrum length becomes about 7.16 Å. For the major part of this work, we will focus on 3:1 salts. However, for completeness, we will also include a study of a 4:1 salt. The ions are modelled as softly repulsive spheres, carrying a central charge. This soft repulsion, u_r , between two ions separated by r has the form,

$$\beta u_r = \left(\frac{d}{r}\right)^{12} \quad (1)$$

where $d = 4$ Å, and β is the inverse thermal energy. This essentially amounts to an implicit assumption of the ions being well solvated, *i.e.* there are no net (excess) van der Waals attractions between the ions.[‡] The simulated system is composed of the salt solution confined between two flat, perfectly conducting surfaces with infinite extension in the (x, y) plane. These surfaces are located at $z = 0$, and $z = h$. A hard wall repulsion ensures that the z -coordinate of the centre of every ion is confined so that, $d/2 \leq z \leq h - d/2$. Each surface also defines a plane of dielectric discontinuity. The simulated ions are confined to a unit cell C_0 , which, further constrains the ions so that their x - and y -coordinates satisfy, $|x| \leq L/2$ and $|y| \leq L/2$. Periodic boundary conditions are applied along the (x, y) directions, which is modelled *via* an infinite number of replicas of C_0 parallel to the confining electrodes. The salt solution in C_0 is generally not electroneutral. However, total electroneutrality is guaranteed *via* the image charges generated by the two conducting surfaces, which are reflected ad infinitum in the two surfaces. More specifically, the image charges are an infinite number of reflected replicas of C_0 in the two

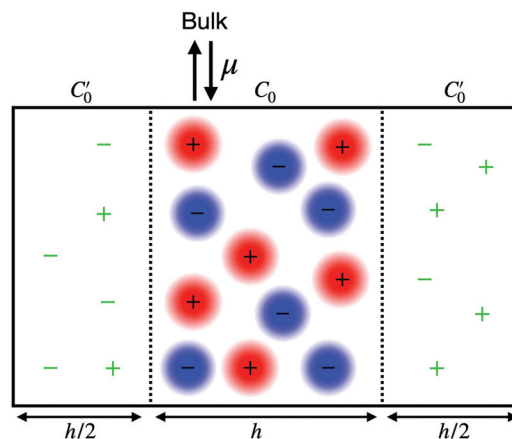


Fig. 1 An illustration of the unit cell. For reasons of notational simplicity, only monovalent ions, and image ions, are depicted. However, in our simulations, the cations were multivalent, with multivalent image charges. Note that the surface charge density is a fluctuating quantity, and bulk exchange is handled by single ion insertion, and deletion, steps.

subspaces $z > h$ and $z < 0$, whereby each reflection at a surface plane leads to the ions taking on an opposite charge.³⁰ These infinite images and the periodic replicas along the (x, y) direction, defines the complete simulated ensemble.

As described in previous work,³¹ and also illustrated in Fig. 1, a symmetric electroneutral “super-cell”, $C = C_0 + C'_0$, can be defined, consisting of the central cell C_0 , together with the nearest halves, C'_0 , of the adjacent reflected (image) cells. An infinite 3-dimensional array of replicas of C reproduces the ensemble described above. An advantage of our current unit cell C definition, is that its dipole moment is zero. Placing C'_0 fully to the left, or to the right, of C_0 will lead to a spurious electric field of the unit cell (even at zero applied voltage), which needs to be accounted for.^{32–34} Thus the ensemble can be straightforwardly treated using 3-D Ewald methods. One of the consequences of our construction is that the total Ewald energy, U_C , of the ions in C is equal to twice the energy of the ions in C_0 . That is,

$$U_{C_0}(\mathbf{r}^n) = \frac{1}{2} U_C(\mathbf{r}^n) \quad (2)$$

which follows from simple symmetry arguments. Here, (\mathbf{r}^n) , represents the configuration of ions in C_0 . We also note that, even though C contains twice as many particles as C_0 , only n are independent, which means the total energy of the particles in C is a function of (\mathbf{r}^n) . This method was dubbed the “Image Ewald” method (IE).³¹

In order to establish proper surface interactions, across a range of different separations (h), we need to ensure that the confined fluid is in equilibrium with an appropriate bulk solution. This is achieved *via* Grand Canonical (Metropolis) Monte Carlo (GCMC) simulations. As we have also demonstrated recently,³¹ it is possible to use individual ion chemical potentials μ_{ind} , and perform separate GCMC steps for each species. We can define the *mean* chemical potential as,

[‡] Similar arguments have led to the standard coarse-grained treatment of repulsive (often hard-sphere) interactions between monomers in a “good solvent” polymer solution model.



$\mu_{\text{salt}} = \sum_{i=1}^{N_{\text{sp}}} \nu_i \mu_{\text{ind}}(Z_i)$, where N_{sp} is the number of species with different valencies Z_i . The coefficients, ν_i satisfy, $\sum_{i=1}^{N_{\text{sp}}} \nu_i Z_i = 0$ and $\sum_{i=1}^{N_{\text{sp}}} \nu_i = 1$. The individual ion chemical potentials in the bulk salt solution, can then be formally written as,

$$\mu_{\text{ind}}(Z_i) = \mu_{\text{salt}} - Z_i e \Psi_{\text{ref}} \quad (3)$$

where Ψ_{ref} measures the asymmetry of the electrolyte model. For a symmetric ($Z:Z$) electrolyte $\Psi_{\text{ref}} = 0$, but it is non-zero for the asymmetric salts ($3:1$ and $4:1$) investigated in this work.

In our simulations the value of Ψ is not known *a priori*. Instead we introduce a so-called bias potential, Ψ_{bias} , that discriminates between anions and cations so that the individual ion chemical potentials become,

$$\mu_{\text{eff}}(Z_i) = \mu_{\text{salt}} - Z_i e \Psi_{\text{bias}} \quad (4)$$

These effective chemical potentials are used in the Grand Canonical Boltzmann weights for insertion/deletion moves of the individual ions. The difference $\Psi_{\text{bias}} - \Psi_{\text{ref}}$ is the Donnan potential, which is due to the charge distribution at the interface between the bulk and the confined electrolyte. In our system the Donnan potential is equal to the surface potential. Thus, our simulations are carried out at constant surface potential. In an experimental setup, using an atomic force microscope, or a surface force apparatus, with potentiometric regulation, the Donnan potential would correspond to the applied voltage.

For a non-zero Donnan potential the simulation box C_0 will not be electroneutral. However, the repeated supercell, C , is ensured to be electroneutral by the completely correlated image charges. While the surface potential is fixed, the instantaneous surface charge density, σ_s , (determined by the image charges) will fluctuate around some average value $\langle \sigma_s \rangle$. It should be noted that this average value will vary with the surface separation. We will denote its limiting value, at large separations by σ_s^{single} .

To complete our analysis we introduce some other definitions and calculation protocols. The “apparent” surface charge density, $\sigma_{\text{app}}(z)$, is defined as,

$$\sigma_{\text{app}}(z) = \sigma_s + e \int_0^z (Z_c \rho_c(z') - Z_a \rho_a(z')) dz' \quad (5)$$

where $\rho_c(z)$ and $\rho_a(z)$ denote the average cation and anion densities (with valencies Z_c and Z_a respectively). The integrand is thus the average charge density at z' and electroneutrality and symmetry causes $\sigma_{\text{app}}(z)$ to vanish at the mid-plane. The normal force acting between the electrodes can be calculated from the free energy change associated with a small shift of the surface separation, from h to $h - \delta h$. The procedure is detailed in the ESI.† In all our calculations, we used $\delta h = 0.001 \text{ \AA}$.

In our simple approach, the electrode polarization is treated *via* image charges, which represents the response of the surfaces to thermal fluctuations of the ions. At long-range these ion-induced thermal fluctuations of the surfaces lead to an

algebraically decaying repulsive contribution to the normal pressure. There is another contribution to the pressure, that is neglected in our model, due to correlated thermal fluctuations of the bare surfaces (and underlying solvent). This gives rise to an attractive zero frequency van der Waals pressure, $P_{\text{vdW}}(0)$, that should be added to the measured normal pressure, and exactly cancels the repulsive ion-induced contribution at long-range. This pressure contribution is analytic^{26,27} and has the following form,

$$\beta P_{\text{vdW}}(0) = -\frac{\zeta(3)}{8\pi h^3} \quad (6)$$

where $\zeta(n)$ is the Riemann zeta function. Upon addition of this term, the resulting total normal pressure, denoted by, P_N , displays a non-algebraic, salt-screened long-ranged behaviour. The exact match between $-P_{\text{vdW}}(0)$ and the simulated (uncorrected) normal pressure at long range, has been demonstrated and scrutinized in an earlier work on 1:1 salt solutions.²⁹ By adding $P_{\text{vdW}}(0)$ to our simulated pressures, we ensure that our results provide “pure Coulomb” contributions, to which suitably estimated vdW interactions (for instance *via* a metal–water–metal Hamaker constant) may be subsequently added, in the spirit of DLVO theory. As mentioned above, the procedure to evaluate P_N is described in the ESI.† The net pressure, P_{net} can be estimated by subtracting the value at the largest simulated separation, h_{max} , *i.e.* $P_{\text{net}}(h) = P_N(h) - P_N(h_{\text{max}})$. That is, we assume h_{max} is suitably large so that the fluid is essentially bulk-like near the mid-plane. Finally, the net interaction free energy per unit area, $\Delta g_s(h)$, is found by integrating (we used a cubic spline) the net pressure, $\Delta g_s(h) = -\int_{\infty}^h P_{\text{net}}(h') dh'$

3 Results

We will start by investigating the response of surface forces to a change of Ψ_{bias} , which in turn leads to different surface charge densities. Given that our intent in this work is to establish possible relations between apparent surface charge density profiles and free energy barriers, we will focus on long-range behaviours. Correlations between the trivalent cations will always cause a strong attraction at short range, which are indeed observed in our simulations. However, this behaviour is not the focus of this work, so in most cases we will concentrate on that part of the interaction at and beyond the free energy barriers.

A 4 mM salt solution at various surface charges σ_s^{single}

With the salt chemical potential adjusted such that the bulk concentration is about 4 mM, we obtain the surface interactions, at various bias potentials (and therefore different σ_s^{single}), as shown in Fig. 2(a). There are a few remarkable observations. First, we note that even for net neutral surfaces, there is a significant double-layer repulsion, in stark contrast to standard DLVO theory. Moreover, the repulsion varies in a non-monotonic manner with the applied potential, *i.e.*, with σ_s^{single} . If we start with a surface that is net neutral at large



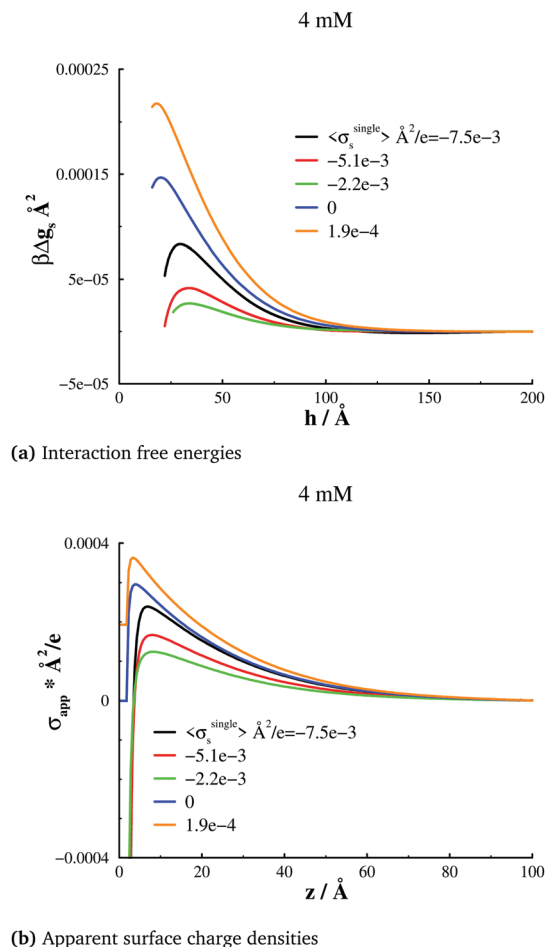


Fig. 2 Interaction free energies per unit area, and apparent surface charge density profiles, at a salt concentration of 4 mM. Results are provided for a range of applied bias potentials, Ψ_{bias} , and thus a range of (large separation) average surface charge densities, σ_s^{single} . (a) Interaction free energies per unit area, $g_s(h)$. (b) Apparent surface charge densities, $\sigma_s^{\text{app}}(z)$, at a "large" separation, $h = 200 \text{ \AA}$.

separations, the barrier becomes larger for a slight positive surface charge density ($\sigma_s^{\text{single}} = 0.00019 e$), but is initially weaker if the surfaces are made negative ($\sigma_s^{\text{single}} = -0.0022 e \text{ \AA}^{-2}$, and $\sigma_s^{\text{single}} = -0.0051 e \text{ \AA}^{-2}$). Even $\sigma_s^{\text{single}} = -0.0075 e \text{ \AA}^{-2}$ is insufficient to generate a repulsion as strong as for neutral surfaces, although the difference is diminished nevertheless. The apparent surface charge density profiles, evaluated at a large separation, displays exactly the same qualitative behaviour as the surface interactions. This is illustrated in Fig. 2(b). A comparison between the graphs in Fig. 2(a) and (b) also reveals that the systems wherein the maximum of the apparent surface charge density is located near the surface, correspond to surface force barriers which also occur at short separations. Already at this stage, our results imply a close relationship between $\sigma_s^{\text{app}}(z)$ and the position and magnitude of the repulsive barrier in P_{net} . We report further evidence for this below.

As already mentioned, this work focuses on the long-ranged part of the interactions, but it should be noted that we do indeed establish ion-correlation attractions at short range, for all investigated cases, as expected in the presence of highly

valent counterions. With a 1 : 1 salt, this regime would vanish, and we would obtain monotonically repulsive interactions. Such systems have been explored in an earlier work,²⁹ using simulations as well as an image charge adjusted version of Poisson–Boltzmann theory. While successful for 1 : 1 salt solutions, such a mean-field ansatz would fail for our systems, containing multivalent counterions, since an account for ion correlations is required to even qualitatively capture the presence of an attractive regime.

A given bias potential will generate some average surface charge density at large separations, as indicated in the legends of Fig. 2. However, these averages will vary as the surfaces are brought closer together, which in turn might influence the interaction free energy. Our simulation data suggest that this effect indeed exists, but also that its relevance sometimes is small. In Fig. 3, we plot how the average surface charge density changes with separation, i.e. $\langle \sigma_s(h) \rangle - \langle \sigma_s^{\text{single}} \rangle$. We note that in the cases where $\langle \sigma_s^{\text{single}} \rangle$ is negative, the average surface charge density becomes less negative at short separations, but the relative change is quite modest. When the isolated surfaces are neutral, or weakly positive, on the other hand, the net change is negative, and in these cases the effect appears strong enough to be significant.

A 22 mM salt solution at various surface charges σ_s^{single}

Let us now examine the responses at a higher bulk salt concentration of 22 mM. We summarize our results in Fig. 4. The behaviours are qualitatively similar to those we found at 4 mM, although the effects of a decreased electrostatic screening length are apparent. Again, we note how the free energy barrier responds in a non-monotonic manner to an incremental increase of the applied bias potential, starting from a low value. This behaviour is analogous for the maximum degree of overcharging at an isolated surface. At an intermediate bias potential, for which $\sigma_s^{\text{single}} = -0.005 e \text{ \AA}^{-2}$, we find the weakest barrier, and also the smallest degree of overcharging. The range of the barriers are also qualitatively reflected by the surface distance at which the maximum overcharging occurs.

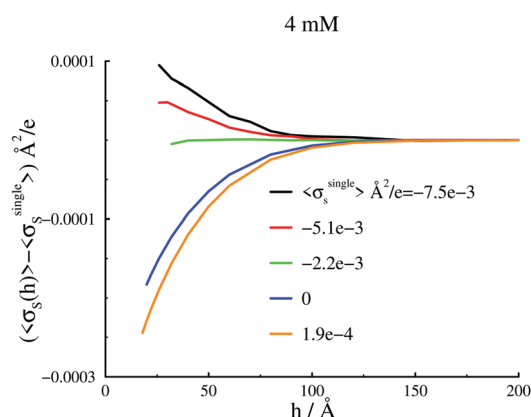
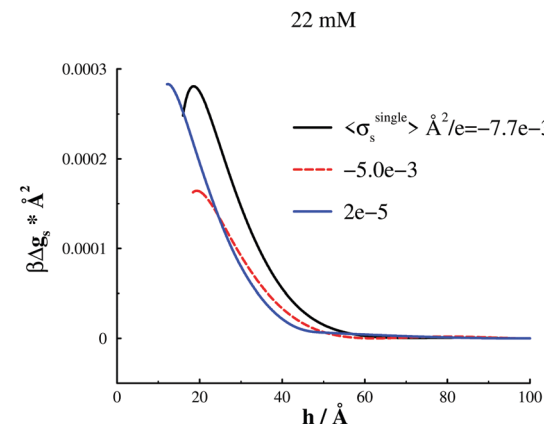
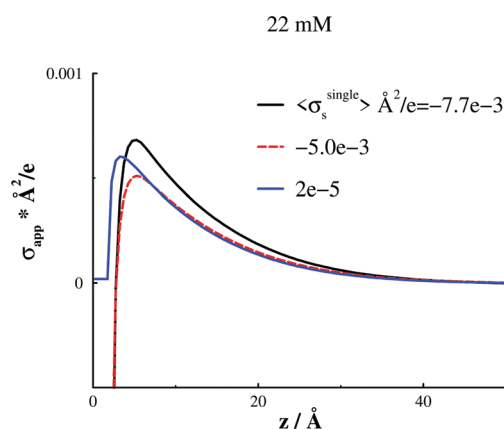


Fig. 3 Separation dependence of the net average surface charge density, $\langle \sigma_s(h) \rangle - \langle \sigma_s^{\text{single}} \rangle$, for various applied bias potentials, Ψ_{bias} .





(a) Interaction free energies

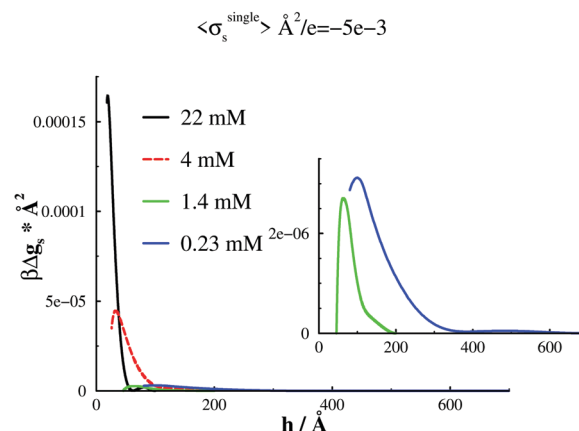


(b) Apparent surface charge densities

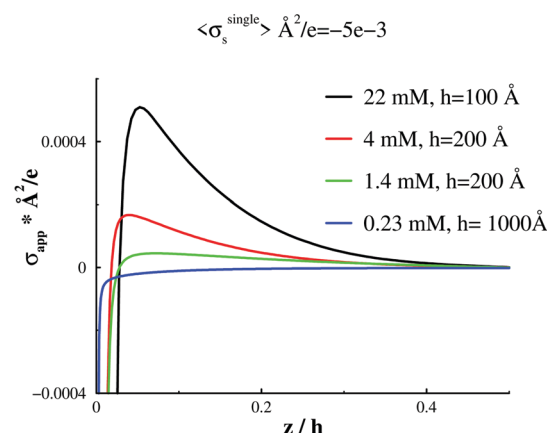
Fig. 4 Analogous results as those reported in Fig. 2, but at a salt concentration of 22 mM, and a “large” separation $h = 100 \text{ Å}$. (a) Interaction free energies per unit area, $g_s(h)$. (b) Apparent surface charge densities, $\sigma_s^{\text{app}}(z)$, at a “large” separation, $h = 100 \text{ Å}$.

$\sigma_s^{\text{single}} \approx -0.005 \text{ e } \text{Å}^{-2}$: salt concentration dependence

In this section, we will investigate surface forces, at a constant limiting surface charge density $\sigma_s^{\text{single}} \approx -0.005 \text{ e } \text{Å}^{-2}$, but for different bulk salt concentrations. In order to facilitate such a comparison, we must first adjust Ψ_{bias} , for each chosen concentration (chemical potential), at a large surface separation. In Fig. 5(b), we note that overcharging vanishes at a sufficiently low concentration, and that there is a threshold concentration, of about 1.4 mM, at which $\sigma_{\text{app}}(z)$ is essentially flat, outside the primary adsorption layer (or “Stern layer”). Below this threshold concentration, $\sigma_{\text{app}}(z)$ has a positive slope beyond the Stern layer, and above the threshold, the slope is negative. If we compare with Fig. 5(a), we see that close to the threshold concentration, the free energy barrier has almost vanished. The barriers are stronger at higher as well as lower salt concentrations, and, as expected, they are more long-ranged in the latter case. Thus, there is a non-monotonic dependence of the barrier height on the salt concentration with the minimum coinciding with a flat $\sigma_{\text{app}}(z)$ profile (outside the Stern layer). These observations indicate a condition that can be described



(a) Interaction free energies



(b) Apparent surface charge density

Fig. 5 Interaction free energies per unit area, and apparent surface charge density profiles, for surfaces with $\langle \sigma_s \rangle \approx -0.005 \text{ e } \text{Å}^{-2}$ (for large separations), at various salt concentrations. (a) Interaction free energies per unit area, $g_s(h)$. (b) Apparent surface charge densities, $\sigma_s^{\text{app}}(z)$. Notice that the x coordinate is reduced by some “large” separation, h , which is different at different salt concentrations, as indicated in the legend.

as “perfect surface charge neutralization”. As stated in the Introduction, similar behaviour has been observed also for non-conducting surfaces, experimentally,^{13,35,36} as well as theoretically.^{21–24} At long range, there will be a double-layer repulsion between surfaces that are effectively negative, or positive, depending on whether the surfaces are overcharged, or “undercharged”. However, at the threshold concentration (about 1.4 mM in our case), the effective surface charge is close to zero, which essentially eliminates the double-layer repulsion. As mentioned, these observations have already been established for non-conducting surfaces, but this is, to the best of our knowledge, the first report of similar findings for conducting surfaces. Given the extra adsorption of multivalent ions that such surfaces generate, the threshold concentration will be lower than for non-conducting surfaces.²⁴

A simple adsorption model with non-conducting charged surfaces

Let us summarize our findings thus far. The slope and range of $\sigma_{\text{app}}(z)$, outside the Stern layer at a single surface, carries



information about the range and strength of the free energy barrier, when two such surfaces interact. This observation might help us to more simply identify the predominate mechanisms in at least two ways. Firstly, we note that a single simple canonical simulation of an isolated surface can provide useful information about how two such surfaces will interact – without having to conduct expensive grand canonical surface force calculations across a range of different surface separations. Secondly, the apparent relevance of the $\sigma_{\text{app}}(z)$ profile at long range, suggests the possibility of a simplified approach, where the expensive treatment of image charges can be avoided. Here we will explore such a model, by replacing the image charge treatment by using an attractive, short-ranged adsorption potential, $w(z)$, between ions and the surfaces. We will furthermore report interactions between conducting, and non-conducting surfaces in a 1.1 mM 4:1 salt solution, where the surface charge density at large separations is $\langle \sigma_s^{\text{single}} \rangle \approx -0.01 \text{ e } \text{\AA}^{-2}$. This will allow further scrutiny of our suggested simplified approach, with an added adsorption potential to mimic effects from image charges.

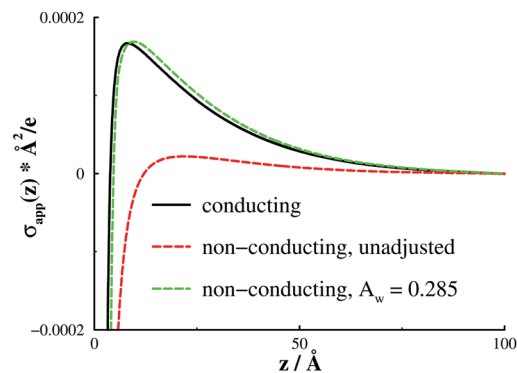
We expect an attraction between an ion and a conducting surface, with a strength proportional to Z_i^2 , from the self-image charge of an ion of valency Z_i . However, this attraction will be screened as the ion moves away from the interface, so assuming it to be short-ranged, we shall model it as a linear function. With these considerations in mind, we propose the following adsorption potential, as an alternative to the image charge approach used above,

$$\beta w_i(z) = -A_w Z_i^2 \left(1 - \frac{z - d/2}{d} \right), d/2 \leq z \leq 3d/2 \quad (7)$$

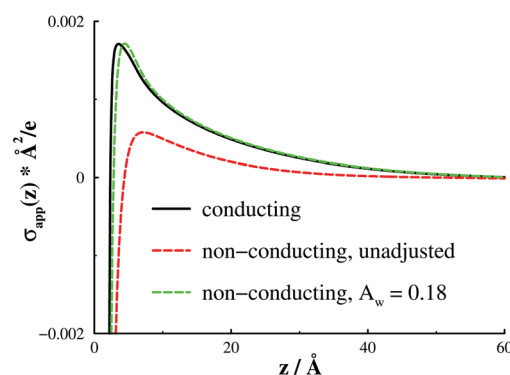
where w_i is zero above the upper limit ($3d/2$), and A_w is a positive fitted parameter. We assume this interaction acts at both surfaces. The result of fitting A_w is summarized by the apparent surface charge densities shown in Fig. 6. We note that for the 3:1 salt, $A_w = 0.285$ leads to an apparent surface charge density profile that resembles the corresponding one established with conducting (but otherwise inset) surfaces. A similar observation holds for a 4:1 salt, with $A_w = 0.18$.

In Fig. 7 we show the resulting normal pressures, P_N , compared with those for both conducting and non-conducting surfaces. We see that interactions between conducting surfaces can be successfully captured by the surface adsorption model, without using explicit dielectric boundaries. We should also point out that, for non-conducting surfaces, one cannot apply the IE simulation method.

Instead, we utilized an external mean electrostatic potential, which was calculated from previously simulated ion density profiles, to account for long-ranged interactions external to the simulated volume.^{37,38} Furthermore, in the addition and deletion moves of the GCMC simulations an overall electroneutral group of ions were either added, or removed, from the simulation cell. The pressure component normal to the surfaces, P_N , was, for non-conducting surfaces, obtained by calculating the average z -projection of all forces per unit area, acting across the mid plane of the slit. Despite these differences in simulation



(a) 4 mM 3:1 salt, $\langle \sigma_s \rangle^{\text{single}} \approx -0.005 \text{ e } \text{\AA}^{-2}$



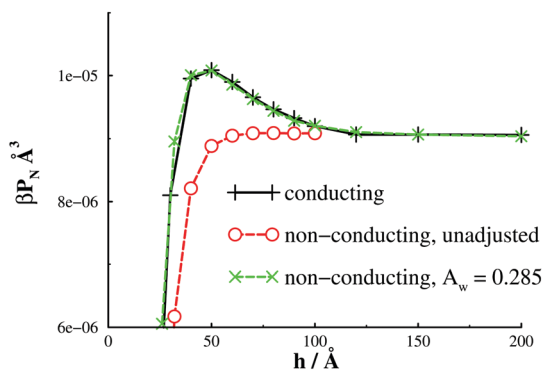
(b) 1 mM 4:1 salt, $\langle \sigma_s \rangle^{\text{single}} \approx -0.01 \text{ e } \text{\AA}^{-2}$

Fig. 6 Apparent surface charge densities, $\sigma_s^{\text{app}}(z)$, at conducting and non-conducting walls. (a) A 4 mM 3:1 salt, and $\langle \sigma_s^{\text{single}} \rangle \approx -0.005 \text{ e } \text{\AA}^{-2}$. (b) A 1 mM 4:1 salt, and $\langle \sigma_s^{\text{single}} \rangle \approx -0.01 \text{ e } \text{\AA}^{-2}$. The red dashed curves display results for non-conducting surfaces, as obtained without any non-electrostatic adsorption potential. By adjusting A_w (see eqn (7)) with the data for conducting surfaces as target (black curves), we arrived at the green dashed curves. This was achieved for $A_w = 0.285$ (3:1 salt, graph (a)), and $A_w = 0.18$ (4:1 salt, graph (b)), respectively.

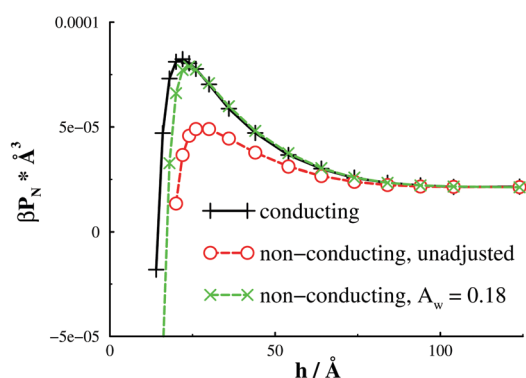
methodology, the limiting normal pressure at large separations (the bulk pressure) is identical, within some small amount of noise. This is an important check that confirms that long-ranged interactions are satisfactorily predicted, and that the simulated pressures are correctly evaluated.

Finally, in Fig. 8, we report the corresponding net interaction free energies, per unit area. The agreement between interactions obtained with adsorption-adjusted models, and those from a full image charge treatment, is not perfect, but nevertheless encouraging. The apparently successful application of the fitted (single-particle) potential suggests that image effects are dominated by the short-ranged adsorption of the counterions. While the simulations presented here are against flat surfaces, they may be of some relevance to conducting spherical colloidal particles where the radius is large. Dispersions of such particles will be dominated by pair interactions between the colloids, and it is possible that the Derjaguin approximation can also be brought to bear to take account of curvature. This gives some hope that simulations of a colloidal





(a) 4 mM 3:1 salt, $\langle \sigma_s \rangle^{single} \approx -0.005 \text{ e}/\text{\AA}^2$.



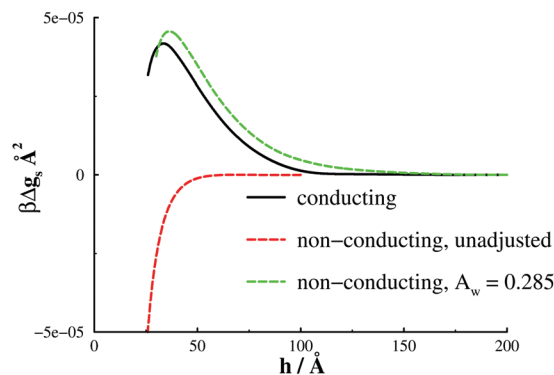
(b) 1 mM 4:1 salt, $\langle \sigma_s \rangle^{single} \approx -0.01 \text{ e}/\text{\AA}^2$.

Fig. 7 Slit normal pressures, P_N , for the systems described in Fig. 5. Results are shown for conducting and non-conducting surfaces that carry a similar average surface charge density, but are otherwise inset, as well as for a non-conducting surface that has a non-electrostatic ion affinity. The latter affinity was adjusted so as to generate an apparent surface charge density profile that, at large separations, resemble the corresponding profile at a non-conducting (inset) surface, as shown in Fig. 5. This procedure emanated in the A_w values that are reported in the legends of the graphs.

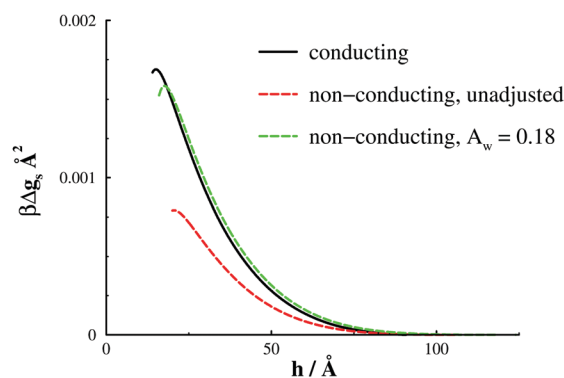
dispersion might be approximated by a model where multiple image charges are replaced by a similar ion adsorption potential. Of course, one would need to fit the adsorption potential using a separate single particle pre-simulation, by matching integrated charge density profiles ($\sigma_s^{app}(r)$), but this would still amount to very large computational savings for a many-particle simulation.

4 Conclusions

This simulation study has focused on the accurate determination of electrolyte properties confined by conducting surfaces and in electro-chemical equilibrium with a fixed bulk solution. We have shown that a surface neutralization threshold concentration is observed in these systems, similar to that seen in non-conducting surfaces. This has significance in many experimental systems, where the charged particles are either metallic or semi-metallic, or else have mobile charges on their surfaces.



(a) 4 mM 3:1 salt, $\langle \sigma_s \rangle^{single} \approx -0.005 \text{ e}/\text{\AA}^2$.



(b) 1 mM 4:1 salt, $\langle \sigma_s \rangle^{single} \approx -0.005 \text{ e}/\text{\AA}^2$.

Fig. 8 Interaction free energies, g_s , for the systems described in Fig. 5.

In addition to this, we have uncovered very strong repulsive barriers to particle association even for ostensibly uncharged particles. This effect is primarily due to the adsorption of multivalent charged species at the electrode surfaces due to strong self-image interactions. This adsorption can also promote surface overcharging. The forced desorption of these ions as the surfaces approach can lead to surface-surface repulsion, though the full story can be complex, as we have also seen that the close approach of apparently neutral surfaces can increase multivalent ion adsorption (and the magnitude of the surface charge) at least at intermediate separations. Finally, we have explored the possibility of mapping these conducting systems to one of non-conducting charged surfaces with an additional adsorption potential. Fitting this short-ranged potential to the effective surface charge gives rise to very similar surface interactions. Though the success of such a potential for spherical colloid particles is purely conjecture at this stage, evidence would suggest that this approach holds some promise for facilitating calculations on conducting particles, by way of a much simpler model.

Conflicts of interest

There are no conflicts to declare.



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