Theoretical study on the stability, ferroelectricity and photocatalytic properties of CaBiO$_3$

Xiang-Fu Xu,$^a$ Li-Fang Chen,$^a$ Hua-Kai Xu,$^a$ Guo-Xia Lai,$^a$ Su-Mei Hu,$^a$ Hong Ji,$^a$ Jia-Jun Tang,$^b$ Xing-Yuan Chen$^d$$^*$ and Wei-Ling Zhu$^a$$^*$

Materials with high ferroelectric polarization strength and sufficient absorption of visible light have unique advantages in photocatalysis. Based on the results of structure search, phonon frequency, and elasticity coefficient calculations, CaBiO$_3$ has a stable R3 polar structure. First-principles calculations indicate that R3-CaBiO$_3$ is a potentially efficient ferroelectric visible-light photocatalytic material for hydrogen production. CaBiO$_3$ under slight strain can maintain high ferroelectric polarization strength, strong visible light absorption capacity and small effective mass. CaBiO$_3$ under tensile strain has potentially ferroelectric photogeneration of hydrogen with a band edge position that crosses the redox potential of water. These results can expand the application of Bi-based materials in photocatalytic hydrogen production.

1. Introductions

Perovskite oxides exhibit a wide range of ferroelectric, piezoelectric, and thermoelectric characteristics as well as electro-optical effects, which makes them a focus in the photovoltaic and photocatalysis fields.$^{1-3}$ Ferroelectric materials display spontaneous polarization due to the offset of positive and negative charge centers, providing a new prospect for photovoltaic device design by promoting the separation of photoexcited carriers.$^4$ In addition, the internal electric field of ferroelectric polarization also enhances inhibition of the recombination of electrons and holes.$^5$ Ferroelectric materials can also serve as new candidates for photocatalysis, similar to the P-N junction mechanisms, which significantly impact surface photochemistry.$^6$ The non-polluting hydrogen energy generated by photocatalysis is one of the mainstays of future energy development.$^7$ The spontaneous polarization of ferroelectrics can provide a strong internal electric field for the photocatalytic water separation process, which are beneficial for photocatalytic hydrogen production.$^8$ Bismuth-based semiconductors have attracted extensive attention for their excellent photocatalytic performance under visible light due to Bi ions' unique 6s and 6p orbitals.$^9,10$ First-principle calculation results show that CaBiO$_3$ has a potentially stable R3 ferroelectric structure,$^{11,13}$ an excellent visible light-absorbing material with a bandgap of about 1.8 eV.$^{11}$ Rokesh et al. synthesized CaBiO$_3$ through glycine-complexation (GC) and ion-exchange (IE) methods and found that it can generate highly reactive photocatalytic free radicals to degrade pollutants.$^{13}$ For semiconductor materials to meet the conditions of photocatalytic hydrogen production, the bandgap must be larger than the standard Gibbs free energy change for the decomposition of water into H$_2$ and O$_2$, while the band edge position must extend across the redox potential of water.$^{14}$ The CaBiO$_3$ crystal structure search is processed using the evolutionary algorithm implemented in the USPEX code$^{15-17}$ in this paper. The stability of CaBiO$_3$ is further verified by phonon frequencies and elasticity coefficients. Our calculation results show that CaBiO$_3$ under tensile conditions has excellent potential as a new ferroelectric photocatalytic semiconductor material for hydrogen production.

2. Calculation method

The stable structure of CaBiO$_3$ is searched by USPEX code with 20 atoms. The initial structure of the first generation is set as 300, and that of the second generation is 50. The convergence standard remains unchanged for the 10th generation. Variables of 50% genetic, 20% random, 20% soaring, and 10% lattice mutation were set in the calculation. As shown in Table 1, the stable structure space group number of CaBiO$_3$ is 146 (R3 space group), which consistent with earlier theories and experimental reports.$^{11-13}$ The calculated CaBiO$_3$ structure by USPEX software is transformed into a conventional cell structure as shown in Fig. 1. The calculated lattice parameters a and c of CaBiO$_3$ are 5.88 Å and 15.47 Å respectively, which is closed to the early reports in the literature (a = 5.81 Å, c = 15.22 Å).[14] The electronic structure, elastic properties, and photoelectric properties of R3 space group CaBiO$_3$ are calculated using first-principles software packaged in VASP.$^{19}$ The PAW pseudopotential method is used to describe the interaction between electrons and nuclei, and the exchange-correlation functional between electrons is
treated by Perdew–Burke–Ernzerhof (PBE) functional. The cutoff energy was taken at 520 eV, and the Monkhorst–Pack $k$-point sampling was given as 0.03 Å$^{-1}$ in the calculation. The energy and force convergence criteria are set as $10^{-6}$ eV and $10^{-2}$ eV Å$^{-1}$, respectively. The bandgap and absorption spectra of CaBiO$_3$ are calculated by Modified Becke–Johnson (MBJ) exchange potential since PBE functional usually underestimates the bandgap of the material. Parameter C in the MBJ functional was set as 1.7, and the bandgap result calculated was close to the earlier hybrid HSE functional (Heyd–Scuseria–Ernzerhof) report result. The strain is introduced by changing the lattice parameters of $a$ and $b$ to relax the $c$ lattice parameter, indicating the introduction of 2% tensile strain. The calculated lattice parameters $a$ and $c$ of CaBiO$_3$ under 2% tensile strain become 6.00 Å and 15.14 Å respectively. Lattice parameters $a$ and $b$ are reduced by 2% to relax lattice parameter $c$, representing the introduction of 2% compressive strain. The calculated lattice parameters $a$ and $c$ of CaBiO$_3$ under 2% compressive strain become 5.76 Å and 15.87 Å respectively. T-CaBiO$_3$ represents the introduction of tensile strain in CaBiO$_3$, while C-CaBiO$_3$ represents the introduction of compressive strain in CaBiO$_3$.

### 3. Stability analysis

The search results for USPEX suggest that CaBiO$_3$ with R3 space group is a potentially stable structure. The elastic properties and phonon frequencies of CaBiO$_3$ with R3 space group are calculated to verify the stability furtherly. CaBiO$_3$ with R3 space group has seven independent elastic coefficients. The

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Fig. 1 The structure and lattice parameters of pristine R3-CaBiO$_3$ and R3-CaBiO$_3$ under strain.
independent elastic coefficients must satisfy the following inequalities group (1) to achieve mechanical stability.\(^2\)

\[
\begin{align*}
C_{11} &> |C_{12}| \\
C_{13}^2 &< 0.5 \times C_{33} (C_{11} \times C_{12}) \\
C_{14}^2 + C_{15}^2 &< 0.5 \times C_{44} \times (C_{11} - C_{12}) \\
C_{44} &> 0
\end{align*}
\]

The calculated elastic coefficients are shown in Table 2, which meet all the requirements of the inequality group for mechanical stability. \(2 \times 2 \times 2\) supercell contained 80 atoms have been used to calculate the phonon frequency of pristine \(\text{CaBiO}_3\) and \(\text{CaBiO}_3\) under strain conditions. The calculated phonon frequency of pristine \(\text{CaBiO}_3\) with the \(R3\) space group in Fig. 2 shows that there is no imaginary frequency in the whole Brillouin region, indicating that it is a potentially metastable structure. \(\text{CaBiO}_3\) under compressive or tensile strain conditions can still maintain stability due to the calculated elastic coefficients and phonon frequency results in Table 2 and Fig. 2. The elastic coefficients and phonon frequency of \(\text{CaBiO}_3\) under compressive strain condition become larger since the shorter bond lengths of \(\text{Ca–O}\) and \(\text{Bi–O}\) in the Fig. 3 could lead to the increased atomic interactions. Conversely, the tensile strain effect causes the bond length of \(\text{CaBiO}_3\) to be larger for reducing the atomic interactions, which leading to the lower elastic coefficients and phonon frequencies.

![Fig. 2](image1.png) The calculated phonon frequencies.

![Fig. 3](image2.png) The bond length differences (\(Δ\)) of Bi–O (left) and Ca–O (right) relative to pristine \(\text{CaBiO}_3\) under strain.

![Fig. 4](image3.png) The (a) calculated energy and (b) ferroelectric polarization strength with the movement of atoms. \(λ\) is the atom displacement interpolation between ferroelectric (1) and paraelectric states (0) states.

<table>
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<th>Ca (Å)</th>
<th>Bi (Å)</th>
<th>O (Å)</th>
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<td>(\text{CaBiO}_3)</td>
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<td>0.43</td>
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<td>T-(\text{CaBiO}_3)</td>
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4. Calculated ferroelectric properties

The ferroelectric properties of the $R3$-CaBiO$_3$ polarized structure are calculated by the modern polarization theory of the Berry Phase method,$^{23,24}$ and $R3$ is chosen as the centrosymmetric phase. The calculation results are shown in Fig. 4, and $\lambda$ is the linear interpolation scale value between the polarized and centrosymmetric phase structures. $R3$-CaBiO$_3$ forms a noticeable

Fig. 5  The calculated energy band structure and density of states.
double potential well curve with atomic movement, and the position of the potential well represents the ferroelectric polarized phase. The calculated ferroelectric polarization strength is 59.63 με cm⁻², which is close to the value of 56 με cm⁻² reported in the earlier literature, and close to the ferroelectric polarization strength of conventional ferroelectric oxide R3c ZnSnO₃.\(^{25,26}\)

Next, we consider the effect of strain on the ferroelectric properties of R3CaBiO₃. R3CaBiO₃ under the presence of a slight strain, can still maintain ferroelectric polarization strength larger than 50 με cm⁻² as well. The ferroelectric driving mechanism of R3CaBiO₃ is similar to that of the R3c structures BiFeO₃ and ZnSnO₃, which is mainly determined by the action of the A-site ions (Ca, Bi or Zn) and O ions.\(^{27,28}\) The offset of Ca ions increases from 0.40 Å to 0.34 Å under 2% tenseile strain in Table 3, which reduces the ferroelectric polarization strength. The offset of Ca ions increases to 0.46 Å under compressive strain, which improves the ferroelectric polarization strength. Ca ion at A site of CaBiO₃ under strain conditions has the most direct effect on the ferroelectric properties of the system.

5. Discussions on photocatalytic properties

The optical properties of materials are closely related to the band structure. As shown in Fig. 5, the calculated energy band structure of CaBiO₃ is an indirect bandgap. Although an indirect bandgap is not an optimal function for light absorption, it could reduce the probability of photoelectron-hole radiation recombination. The calculated band gap of the pristine CaBiO₃ is 1.58 eV by MBJ functional, which is consistent with the value reported by HSE functional in the literature.\(^{14}\) The optical absorption properties of the material are closely related to the bandgap of the material itself. In order to further understand the absorption of visible light, we also calculated the optical absorption spectrum. The relation between the optical absorption coefficient \(\alpha(\omega)\) of CaBiO₃ and the real \(\varepsilon\) and the imaginary \(\varepsilon\) of the dielectric function is shown below eqn (2).

\[
\alpha(\omega) = \frac{2\omega}{c} \left( \frac{\sqrt{\varepsilon_r^2(\omega) + \varepsilon_i^2(\omega)} - \varepsilon_i^2(\omega)}{2} \right)^{\frac{1}{2}}
\]

\(\omega\) is the circular photon frequency, and \(c\) is the speed of light. The pristine CaBiO₃ begins to absorb visible light when the incident photon energy is close to 1.6 eV and forms the prominent absorption peak (about 2.2 eV) in Fig. 6, indicating that it has a strong visible light absorption capacity. The slight red shift appears in the absorption coefficient of CaBiO₃ under tensile strain due to the longer bond length and lower band gap, while the opposite reaction occurs in the compressive strain condition.

The band edge of CaBiO₃ was calculated according to the following empirical formula\(^{29}\) to explore the photocatalytic hydrogen production ability of CaBiO₃,

\[
E_{VBM} = \chi - 0.5E_g + E_0
\]

where \(E_g\) is the bandgap, \(\chi\) is the mean electronegativity, and \(E_0\) is the frame of reference as a scale factor concerning the normal hydrogen electrode (NHE) of the vacuum. As shown in Fig. 7, the CBM band edge position of pristine CaBiO₃ is close to the reduction potential of \(\text{H}^+/\text{H}_2\), while the band edge position of VBM is lower than the oxidation potential of \(\text{O}_2/\text{H}_2\), showing a potential photocatalytic hydrogen production capacity. The empirical formula above was also used for the band edge positions of photocatalytic materials TiO₂, NaBiO₃, and KBiO₃.\(^{10-12}\) Their band edge positions all cross the redox potential of water and satisfy the condition of decomposition water to produce hydrogen. The calculated density of the state of CaBiO₃ shows that the conduction band and valence band are mainly composed of O-2p and Bi-6s orbitals, which is similar to other Bi-based photocatalytic materials.\(^{13}\) The effective mass of the electron in CaBiO₃ under strain conditions is also relatively small, which is close to NaBiO₃ \((0.4 m_0)\) and KBiO₃ \((0.8 m_0)\), as shown in Table 4, suggesting that the photogenerated carriers
of CaBiO$_3$ could be easy to separate. The higher transfer rate of photogenerated carriers and lower recombination rate could be produced due to the larger $D$ value. $D$ is defined as the ratio of the hole effective mass to the electron effective mass. The $D$ values of CaBiO$_3$ at a slight strain in Table 4 range from 2.5 to 2.8, which is slightly larger than that of the conventional photocatalytic ferroelectric material BaTiO$_3$ ($D = 2.44$) calculated by the MBJ functional. 16,17 Meanwhile, the large ferroelectric strength and strong visible light absorption of CaBiO$_3$ will further contribute to the improvement of photocatalytic performance. The band edge positions of T-CaBiO$_3$ and C-CaBiO$_3$ are corrected by the 1 s core energy level of Bi atoms in pristine CaBiO$_3$. As shown in Fig. 7, the CBM band edge position of CaBiO$_3$ under tensile strain moves up and becomes higher than the hydrogen reduction potential, which could be favorable to hydrogen production. The CBM band edge of C-CaBiO$_3$ moved down and was lower than hydrogen reduction potential, which reduced hydrogen production efficiency. CaBiO$_3$ under tensile strain can still maintain high ferroelectric polarization strength and strong visible light absorption ability, further promoting photocatalytic hydrogen production.

6. Conclusion

The USPEX software was used to explore the CaBiO$_3$ structure in this paper. The results show that the stable structure of CaBiO$_3$ is the $R3$ space group configuration. The phonon frequencies and elasticity coefficients calculations also indicate that $R3$-CaBiO$_3$ satisfies the stability condition. The ferroelectric polarization of $R3$-CaBiO$_3$ is mainly generated by the shift of the symmetry center of Ca-O ions. The shift of Ca ions significantly affects the ferroelectric polarization of $R3$-CaBiO$_3$ under strain conditions. The offset of Ca ions decreases under tensile strain with reduced ferroelectric polarization strength, while the opposite case is in the compressive strain condition. $R3$-CaBiO$_3$ can preserve the high ferroelectric polarization strength and visible light absorption capacity under the slight strain. The band edge position of CaBiO$_3$ under tensile strain can cross the redox potential of water and maintain a small electron-effective mass with the large ratio of hole and electron masses, which is favorable for photocatalytic hydrogen production. CaBiO$_3$ is a potential ferroelectric photocatalytic material for hydrogen production under visible light.

Conflicts of interest

The authors declared that they have no conflicts of interest to this work. We declare that we do not have any commercial or associative interest that represents a conflict of interest in connection with the work submitted.

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References


