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Layered post-transition-metal dichalcogenide SnGe₂N₄ as a promising photoelectric material: a DFT study

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First-principles calculations were performed to study a novel layered SnGe₂N₄ compound, which was found to be dynamically and thermally stable in the 2H phase, with the space group $P\bar{6}m2$ and lattice constant $a = 3.143$ Å. Due to its hexagonal structure, SnGe₂N₄ exhibits isotropic mechanical properties on the x - y plane, where the Young's modulus is 335.49 N m⁻¹ and the Poisson's ratio is 0.862. The layered 2H SnGe₂N₄ is a semiconductor with a direct band gap of 1.832 eV, allowing the absorption of infrared and visible light at a rate of about 10^4 cm⁻¹. The DOS is characterized by multiple high peaks in the valence and conduction bands, making it possible for this semiconductor to absorb light in the ultraviolet region with an even higher rate of 10^5 cm⁻¹. The band structure, with a strongly concave downward conduction band and rather flat valence band, leads to a high electron mobility of 1061.66 cm² V⁻¹ s⁻¹, which is substantially greater than the hole mobility of 28.35 cm² V⁻¹ s⁻¹. This difference in mobility is favorable for electron-hole separation. These advantages make layered 2H SnGe₂N₄ a very promising photoelectric material. Furthermore, the electronic structure of 2H SnGe₂N₄ responds well to strain and an external electric field due to the specificity of the p - d hybridization, which predominantly constructs the valence bands. As a result, strain and external electric fields can efficiently tune the band gap value of 2H SnGe₂N₄, where compressive strain widens the band gap, meanwhile tensile strain and external electric fields cause band gap reduction. In particular, the band gap is decreased by about 0.25 eV when the electric field strength increases by 0.1 V Å⁻¹, making a semiconductor-metal transition possible for the layered SnGe₂N₄.

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1 Introduction

Nowadays, the quick development of modern technology delivers wonderful solutions to human life while also causing excessive energy consumption, natural resource depletion, and severe pollution. As a result, new devices must be more powerful and energy-efficient, with advanced materials at the heart of the solution. Two-dimensional (2D) materials have been widely considered as promising candidates for this task due to a wide range of excellent features, including good thermal conductivity, tunable band gaps, high charge carrier mobility, surface activity, electronic anisotropy, and ultrahigh specific surface area.¹⁻⁸ As a result, several two-dimensional structures, including MoS₂/SiC heterostructures, PdSeO₃ monolayers, COFs, AgBiP₂Se₆ monolayers, phosphorene nanoribbons, and

carbon-doped BN nanosheets, have been demonstrated to be ideal for solar energy conversion and photocatalysis.⁹⁻¹⁴ Other 2D materials, such as MoS₂, hexagonal-BN, WSe₂-MoS₂, MoSe₂, WSe₂, and hybrid 2D material heterostructures, are also very promising for the next generation of transistors,¹⁵⁻²⁰ allowing for the miniaturization and integration of nano-electronic devices.

Despite extensive theoretical research, most 2D materials are difficult to produce experimentally. As a result of Hong's successful exfoliation of MoSi₂N₄ monolayers,²¹ a series of investigations on the novel 2D material family with the formula MX₂Y₄ (M = transition metal, X = Ge or Si, and Y = As, P, or N) has been performed, in which the MY₂ in the 2H phase is sandwiched between two buckled honeycomb XY layers.²² On the one hand, most M₂Y₄ monolayers have the same advantageous properties, such as high charge carrier mobility and good tensile strength. On the other hand, the ability to modify the 2H-MY₂ and XY layers in the sandwiched structure of MX₂Y₄ results in a wide range of excellent properties. MoSi₂N₄ and WSi₂N₄ monolayers, for example, are excellent candidates for optoelectronic and photovoltaic applications^{21,23} due to their high visible light absorption, good charge carrier mobility, and suitable band structure. Likewise, the intrinsic piezoelectric

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monolayers CrSi_2N_4 , VSi_2P_4 , and VSi_2N_4 are very promising for spintronic devices.^{23,24} Furthermore, numerical studies²⁵ show that monolayer and bilayer MoSi_2Z_4 ($\text{Z} = \text{P}, \text{As}$) exhibit outstanding structural stability, isotropic mechanical characteristics, a low bandgap, good carrier mobilities, exceptional optical absorption, superior photon responsivity, and external quantum efficiency.

While most d-block metals are theoretically predicted to form MoSi_2N_4 -like structures,^{23,26,27} analogous formations containing post-transition metals (p-block metals) have not yet been investigated. It is worth noting that the majority of p-block elements have been demonstrated to form stable 2D phases with lattice structures similar to that of graphene.²⁸ The post-transition metal Sn, in particular, has been shown to exist in a buckled hexagonal structure with mechanical stability and high photothermal activity.^{29–31} Furthermore, Sn monolayers can combine with other 2D materials like boron nitride and graphene to form multi-plane structures similar to MoSi_2N_4 -like monolayers.^{32,33} To extend the search for new 2D materials, the post-transition metal Sn was designed to replace Mo in the SnGe_2N_4 monolayer, the characteristics of which were investigated in this paper using first-principles calculations. Also explored are the impacts of strain and external electric fields on the characteristics of layered SnGe_2N_4 .

2 Methodology

The layered SnGe_2N_4 lattice structure was built in the 2H phase with the space group $P6m2$, because MoSi_2N_4 was experimentally discovered to crystallize in the 2H phase,²¹ and most of the compounds in the MoSi_2N_4 family have also been confirmed theoretically to be more stable in the 2H phase than in the 1T phase.^{23,34–37} Taking into account the atomic radii of the constituent atoms Mo, Si, and N, the initial lattice parameters were established to be $a = b = 3.143 \text{ \AA}$, and $c = 30 \text{ \AA}$ to avoid interaction between monolayers due to the periodicity. The equilibrium structure of SnGe_2N_4 was obtained by relaxing the present atomic model using the generalized gradient approximation specified by Perdew–Burke–Ernzerhof (PBE)³⁸ and implemented in the Vienna *ab initio* simulation package (VASP).³⁹ The semi-empirical function DFT-D3⁴⁰ was also used to account for the weak van der Waals interactions between the H– SnN_2 and GeN planes. The pseudopotentials, which were used to represent the interaction between particles, including ions and valence electrons of the N- $2s^2 2p^3$, Sn- $4d^{10} 5s^2 5p^2$ and Ge- $3d^{10} 4s^2 4p^2$ orbitals, were constructed using the projected augmented wave (PAW) approach,⁴¹ where the scale relativistic effects were included. All cell periodic functions were expanded using a plane wave basic set with a cut off energy of 500 eV and a Gaussian smearing parameter of 0.05. The self-consistent calculations were carried out until the difference in total energies was less than 1 meV, the force acting on ions smaller than 0.01 eV \AA^{-1} , and the electron energy less than 10^{-4} eV . It is worth noting that a $15 \times 15 \times 1 k$ -point mesh was employed for both structural optimization and calculating the system's characteristics. Furthermore, the PBE + SOC method was used to include the spin–orbit interaction, and the hybrid function

described by Heyd–Scuseria–Ernzerhof (HSE06)⁴² was used to improve the system's band gap. A $4 \times 4 \times 1$ supercell was constructed to calculate the phonon dispersion of 2H SnGe_2N_4 , where the PHONOPY package and finite displacement method as implemented in VASP⁴³ were used.

3 Stability and elastic properties

The optimized hexagonal structure of 2H SnGe_2N_4 , as shown in Fig. 1(a), is characterized by lattice parameters $a = b = 3.143 \text{ \AA}$, which are close to the lattice constants of $\text{CrGe}_2\text{N}_4 = 2.98 \text{ \AA}$, $\text{MoGe}_2\text{N}_4 = 3.04 \text{ \AA}$, and $\text{WGe}_2\text{N}_4 = 3.04 \text{ \AA}$.²³ Like other compounds in the 2D MoSi_2N_4 family,^{44,45} the layered SnGe_2N_4 is constructed by a 2H– SnN_2 monolayer vertically stacked between two buckled hexagonal GeN layers such that each Sn atom bonds with six Ge atoms, forming a trigonal prism. The lengths of the Sn–N and Ge–N bonds are 2.2 \AA and 1.9 \AA , respectively. These bond lengths are about 7% larger than the corresponding values of the spinel SnGe_2N_4 , which were calculated by the LDA method in a previous study by Ching *et al.*⁴⁶ It is worth noting that the bond lengths of layered SnGe_2N_4 were computed using the PBE approach; nonetheless, the LDA and PBE methods reveal bond lengths that differ just slightly.⁴⁷ Therefore, the bonding nature of 2H SnGe_2N_4 is expected to be more covalent than the one in spinel SnGe_2N_4 . This assumption is confirmed by the fact that the Sn–N and Ge–N bond lengths in 2H SnGe_2N_4 are longer than the sum of the corresponding constituent ionic radii of Sn, Ge, and N, which are 1.32 \AA , 1.14 \AA , and 0.54 \AA , respectively.⁴⁸ The electron localization function (ELF) of layered SnGe_2N_4 on the (1 1 0) cross-section is depicted in Fig. 1(b), where fully localized (1.0) and delocalized (0.5) electrons are denoted by red and green areas, respectively, while the blue region (0.0) denotes very low electron density. The red zone is largely focused on the N atoms, indicating that electrons are strongly localized around these atoms. Meanwhile, a considerable spread of delocalized electrons can be seen in the green areas connecting the N atoms to Sn atoms or Ge atoms. As a result, the layered SnGe_2N_4 exhibits covalent bonding properties.

Because no previous research has indicated the existence of 2H SnGe_2N_4 , its stability must be examined. The phonon dispersion along the highly symmetric path Γ –M–K– Γ in the Brillouin zone was conducted to estimate the dynamical stability of 2H SnGe_2N_4 . As illustrated in Fig. 1(e), all 21 phonon branches (corresponding to 7 atoms in a unit cell) are positive, demonstrating the dynamic stability of 2H SnGe_2N_4 . The acoustic branches are characterized by gradual slopes, indicating a moderate group velocity, elastic modulus and median melting point of 2H SnGe_2N_4 . It is expected that heat transferred by the acoustic branches is not interrupted by the optical branches due to the existence of a frequency gap between the two types of phonon branches. The thermal stability was estimated by heating the 2H SnGe_2N_4 to 300 K for 6 ps using *ab initio* molecular dynamics (AIMD). The total energy of the 2H SnGe_2N_4 does not vary drastically over the temperature fluctuation for 6 ps, as illustrated in Fig. 1(c and d), suggesting the thermal stability of this structure. The energy–time graph in



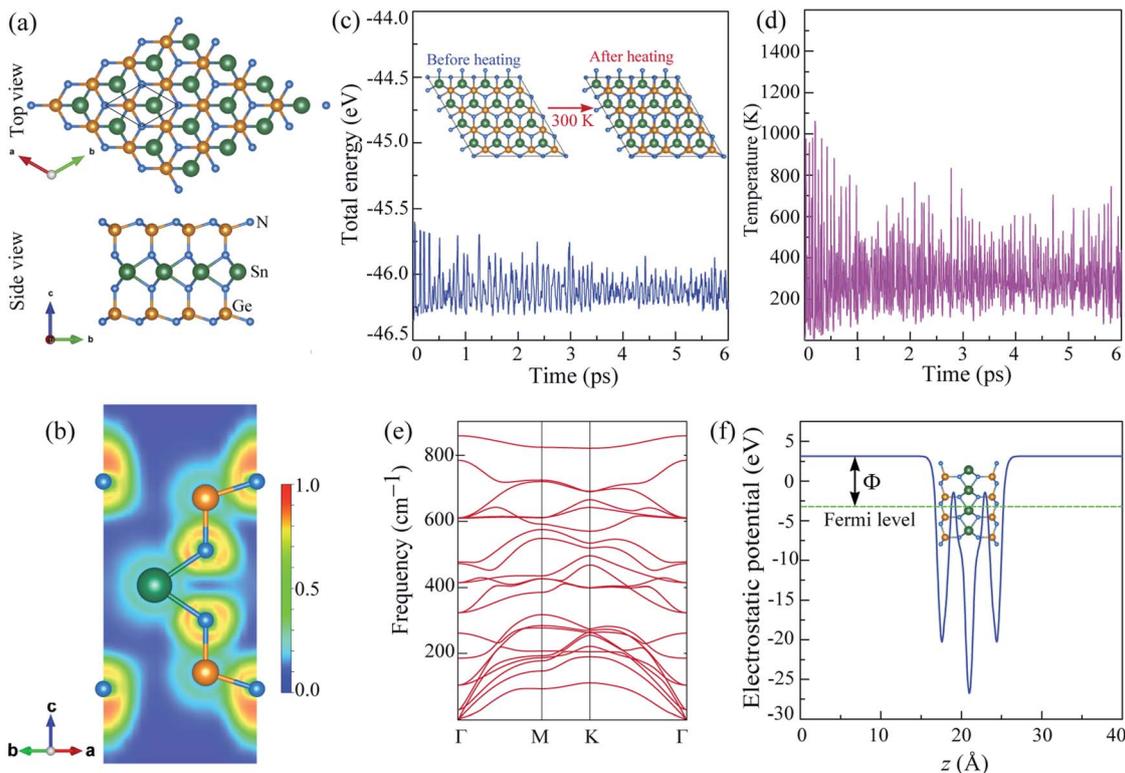


Fig. 1 (a) Top and side views, (b) electron localization function (ELF) of optimized 2H SnGe₂N₄. Time-dependence of (c) total energy and (d) temperature in 2H SnGe₂N₄ at 300 K, (e) phonon dispersion, and (f) work function, depending on the distance along the z-axis, of 2H SnGe₂N₄.

Fig. 1(c) also shows certain local minima owing to modest structural perturbations that swiftly recover to the equilibrium 2H SnGe₂N₄ structure.

To analyze the mechanical strength of 2H SnGe₂N₄, strain was applied to the compound to measure the Young's modulus $Y(\theta)$ and Poisson's ratio $\nu(\theta)$, where θ is the in-plane angle between the lattice vector and the direction of the strain. The elastic constants C_{11} , C_{12} and C_{66} were calculated to determine $Y(\theta)$ and $\nu(\theta)$ as follows:⁴⁹

$$Y(\theta) = \frac{C_{11}C_{22} - C_{12}^2}{C_{11}\sin^4(\theta) + \alpha\sin^2(\theta)\cos^2(\theta) + C_{22}\cos^4(\theta)}, \quad (1)$$

$$\nu(\theta) = \frac{C_{12}\sin^4(\theta) - \beta\sin^2(\theta)\cos^2(\theta) + C_{12}\cos^4(\theta)}{C_{11}\sin^4(\theta) + \alpha\sin^2(\theta)\cos^2(\theta) + C_{22}\cos^4(\theta)}, \quad (2)$$

where $\alpha = (C_{11}C_{22} - C_{12}^2)/C_{66} - 2C_{12}$ and $\beta = C_{11} + C_{22} - (C_{11}C_{22} - C_{12}^2)/C_{66}$.

As shown in Fig. 2, the symmetric circles of the Young's modulus and Poisson's ratio suggest isotropic mechanical characteristics of SnGe₂N₄ in the x-y plane. As the Young's modulus represents the slope of the stress-strain curve, the layered SnGe₂N₄ with a Young's modulus of 335.49 N m⁻¹, as presented in Table 1, is expected to be more brittle than MoSi₂As₄ and MoSi₂P₄, whose Young's moduli are about 118–138 N m⁻¹.²⁵ At the same time, it is more ductile than other materials in the same family, such as MoSi₂N₄ and WSi₂N₄, whose Young's modulus is 500–600 N m⁻¹.^{37,50} Meanwhile, the

Poisson's ratio of 0.286 implies that 2H SnGe₂N₄ expands perpendicularly to the strain direction.

Aside from light absorption, another significant property of photoelectric materials is their work function.^{51–53} The work function is the amount of energy required to release an electron from the surface of a substance and transfer it to vacuum. As a result, the difference between the vacuum electrostatic potential and the Fermi level is equivalent to this energy.⁵⁴ The predicted work function Φ of 2H SnGe₂N₄ is 6.216 eV, as shown in Fig. 1(f), which is comparable to the work functions of layered transition metal dichalcogenides (ZrSe₂, HfSe₂, NbSe₂, 1T-TaS₂, 2H-TaS₂, MoS₂, MoSe₂, SnS₂ and SnSe₂), which range from 5 to 7.4 eV.⁵⁵ The work function of roughly 4.08 to 4.95 eV of spinel ferrites and MXenes is promising for applications in catalysis, renewable energy, and optoelectronics.^{56,57} Furthermore, with a work function of around 6–7 eV, HfS₂, GaS is a promising

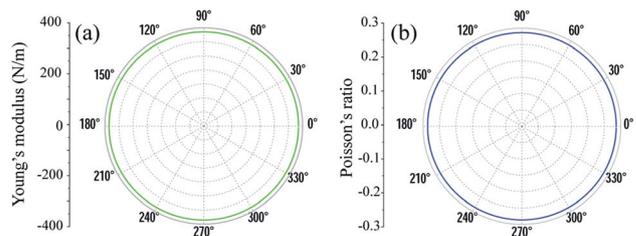


Fig. 2 Dependence of (a) Young's modulus $Y(\theta)$ and (b) Poisson's ratio $\nu(\theta)$ on the in-plane angle θ calculated for 2H SnGe₂N₄.



Table 1 Lattice structure a , bond lengths $d_{\text{Sn-N}}$ and $d_{\text{Ge-N}}$ in angstrom (Å), band gap E_g in eV calculated by PBE, PBE + SOC and HSE06 approaches, elastic constants C_{11} , C_{12} and C_{66} , and Young modulus Y_{2D} in N m^{-1} , and Poisson's ratio ν of optimized 2H SnGe_2N_4

| a | $d_{\text{Sn-N}}$ | $d_{\text{Ge-N}}$ | Δh | E_g^{PBE} | $E_g^{\text{PBE+SOC}}$ | E_g^{HSE06} | C_{11} | C_{12} | C_{66} | Y_{2D} | ν |
|-------|-------------------|-------------------|------------|--------------------|------------------------|----------------------|----------|----------|----------|----------|-------|
| 3.143 | 2.203 | 1.908 | 7.443 | 0.934 | 0.932 | 1.832 | 365.417 | 104.569 | 130.424 | 335.493 | 0.286 |

material for photoelectric applications.^{58,59} Therefore, 2H SnGe_2N_4 with a reduced work function and higher light absorption should be an excellent choice for photoelectric applications.

4 Electronic properties of 2H SnGe_2N_4

The band structure of 2H SnGe_2N_4 was computed using the PBE, PBE + SOC and HSE06 approaches along the symmetric Γ -M-K path of the 2H crystalline phase. The results are shown in Fig. 3, where the maximum of the valence band has been relocated to the Fermi level. The high discrepancy in band gap values, as seen in Table 1, is due to different calculating methods. Due to the loose treatment of the correlative effect, the underestimating of the band gap is a well-known issue of the GGA (PBE) method.³⁸ PBE calculations yield a band gap of 0.934 eV for 2H SnGe_2N_4 . The SOC parameter was included in the PBE + SOC calculations to account for the spin-orbit coupling effect.

The band gap calculated by PBE + SOC almost does not change, as shown in Fig. 3(b), because the quantum number L of p-block elements (Sn, Ge, and N) is not significant in comparison to f-block elements, where the relativistic influence is considerably stronger. However, there is still some interaction between the electrostatic field of the positively charged nucleus and the magnetic dipole of the electron, resulting in a higher density of lower valence bands, as illustrated in Fig. 3(b) and observed by PBE + SOC calculations. Aside from the SOC effect, the interaction of strongly correlated electrons from the d-orbitals of Sn and Ge atoms, as calculated using the HSE06 method,⁴² must also be considered. As a result, the over-delocalization of valence bands induced by the PBE method⁶⁰ is

reduced, resulting in a greater gap between the conduction and valence bands. As seen in Fig. 3(c), the HSE06 band gap has increased to about double that of the PBE band gaps. The weighted band structures in Fig. 4 show the considerable influence of the d-orbital interaction on the band structure of SnGe_2N_4 .

As shown in Fig. 3(d) and 4, the valence band maxima (VBM) are primarily made up of d-orbitals of Sn and Ge atoms. As a result, changes in these bands have a considerable impact on the whole system's band gap. Furthermore, this impact is extended to lower valence bands *via* substantial hybridization of N-p, Sn-d, and Ge-d orbitals, resulting in valence band extension compared to the PBE band structures. Meanwhile, the conduction band minima (CBM) are mainly constructed by the s-orbitals of Sn, Ge, and N atoms, and minor contribution from the p-orbitals of N atoms. The 1.8 eV band gap of 2H SnGe_2N_4 is larger than the ones, which were calculated by the PBE approach, of other MoSi_2N_4 monolayers, such as CrGe_2N_4 , MoGe_2N_4 and WGe_2N_4 , which are in the range of 1.27–1.51 eV.²³ The 2H SnGe_2N_4 , on the other hand, can absorb more visible and infrared light than MoSi_2N_4 and WSi_2N_4 monolayers (HSE band gaps are 2.23–2.57 eV).²³

5 Photoelectric properties and charge carrier mobility of 2H SnGe_2N_4

The band structure of 2H SnGe_2N_4 , calculated by the HSE06 approach, is characterized by an appropriate band gap for absorbing infrared and visible wavelengths, which constitute the majority of solar energy. Furthermore, the lowest conduction bands are very concave downward, as shown in Fig. 4, indicating high electron mobility. The mobility of holes, on the other hand, is expected to be low due to the relatively flat

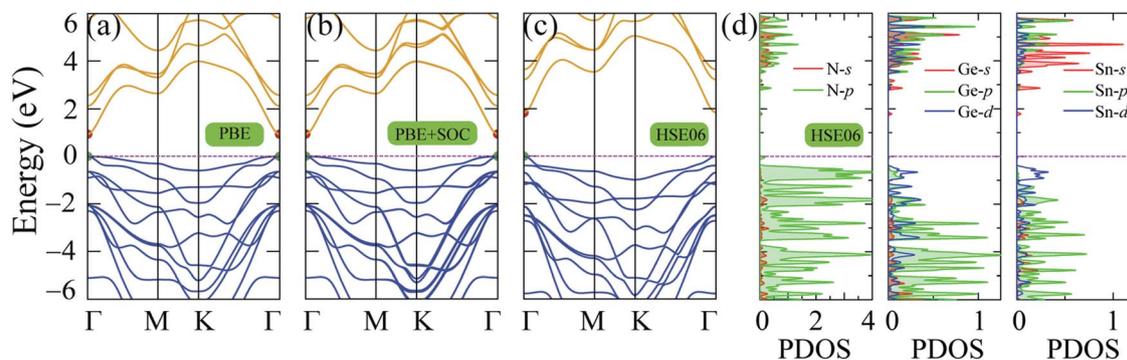


Fig. 3 Band structure of 2H SnGe_2N_4 obtained by (a) PBE, (b) PBE + SOC and (c) HSE06 methods; (d) partial density of states of SnGe_2N_4 calculated by HSE06 method.



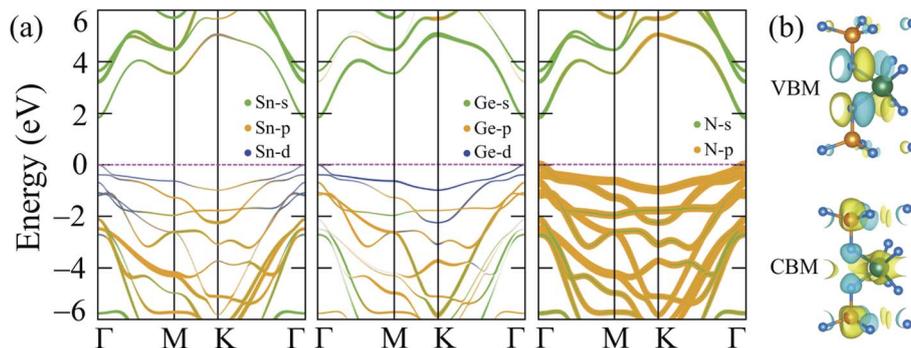


Fig. 4 (a) Weighted band structures and (b) isosurfaces of the VBM and CBM charge densities of 2H SnGe₂N₄.

valence bands. As a result, 2H SnGe₂N₄ is predicted to be a good photoelectric material whose optical properties should be investigated. The light absorption ability of 2H SnGe₂N₄ is investigated using the absorption rate $\alpha(\omega)$, which was computed using the dielectric function $\epsilon(\omega)$ matrix values⁶¹ and is shown in Fig. 5. The imaginary part of the dielectric function was calculated by applying the Bethe–Salpeter equation (BSE) on top of the G_0W_0 method,^{62,63} which takes into consideration the interactions between electrons and between electrons and holes. The imaginary part of the dielectric function $\text{Im}(\epsilon)$ arises from the transition of electrons from occupied bands to unoccupied bands when stimulated by photons of appropriate energy, as seen in Fig. 3(d). As a result, the spectrum of $\text{Im}(\epsilon)$ is comparable to the spectrum of $\alpha(\omega)$.

The absorption rate of 2H SnGe₂N₄ in the ultraviolet region is around 10^5 cm^{-1} , with the highest peak near 4 eV. According to Fig. 3(d), this peak corresponds to the electron transition from the highest valence bands near -1 eV, which are dominated by N-p, Ge-d, and Sn-d orbitals, to the lowest conduction

bands near 2 eV and 3 eV, which are dominated by N-p/s, Ge-s, and Sn-s orbitals. The absorption rate $\alpha(\omega)$ reaches its maximum peaks in the visible range at 1.96 eV and 2.68 eV, with intensities of around 10^4 . These peaks are caused by electron transitions from N-p orbitals in the valence bands to N-s/p, Ge-s, and Sn-s orbitals in the conduction bands. In general, the layered SnGe₂N₄ shares some common optical characteristics with 2H WGe₂N₄, WSi₂N₄, MoGe₂N₄, SnSi₂N₄ and MoSi₂N₄,^{23,36} where the absorption rate is as high as around 10^4 in the infrared and visible ranges, and it increases to 10^5 at higher energy levels of the ultraviolet range.

The charge carrier mobility was calculated by applying the deformation potential theory.^{64,65} For the 2D structures, the charge carrier mobility is denoted as μ_{2D} and the elastic modulus as C_{2D} . The value of μ_{2D} is expressed via C_{2D} , effective mass m^* and the deformation energy constant E_d (defined based on Fig. 6(b)) as follows:

$$\mu_{2D} = \frac{e\hbar^3 C_{2D}}{k_B T m^* \bar{m} E_d^2}, \quad (3)$$

where

$$\frac{1}{m^*} = \frac{1}{\hbar^2} \left| \frac{\partial^2 E(k)}{\partial k^2} \right|, \quad (4)$$

$$C_{2D} = \frac{1}{\Omega_0} \frac{\partial^2 E}{\partial \epsilon_{\text{uni}}^2}, \quad (5)$$

$$E_d = \frac{\Delta E_{\text{edge}}}{\epsilon_{\text{uni}}}. \quad (6)$$

The formulas (3)–(6) use the reduced Planck constant \hbar , elementary charge e , unit cell volume Ω and the Boltzmann constant k_B . The total energy E and uniaxial strain ϵ_{uni} were taken from energy–strain graph in Fig. 6(a).

The calculated transport parameters of 2H SnGe₂N₄ in Table 2 demonstrate the direction-independent effective masses of both holes and electrons, which can be explained by the isotropy of 2H SnGe₂N₄'s hexagonal honeycomb structure. Formula (4) illustrates an inverse relationship between effective mass and the differentiation of band edge curves. As a result, the electron's low

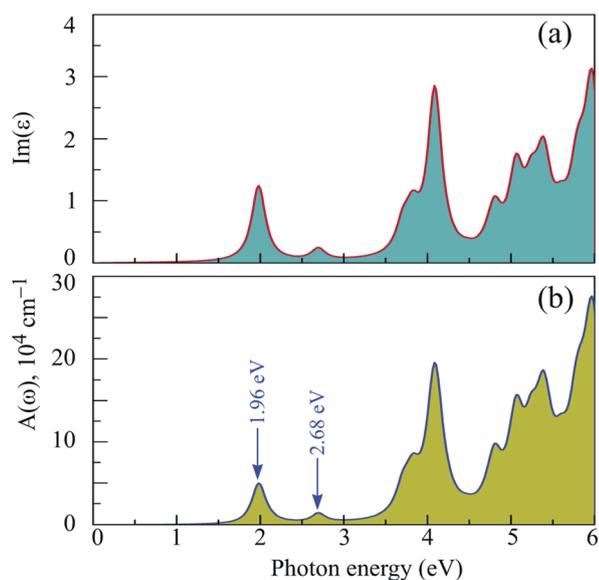


Fig. 5 (a) Imaginary dielectric constant ϵ and (b) absorption rate as a function of frequency ω .



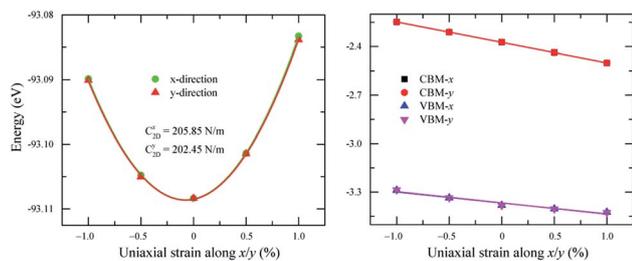


Fig. 6 Dependence of (a) total energy and (b) band edge alignment on x and y uniaxial strains.

Table 2 Calculated elastic moduli C_{2D} , effective mass m^* , deformation energy constants E_d , and charge carrier mobilities μ_{2D} of 2H SnGe₂N₄

| | | C_{2D} (N m ⁻¹) | m^* (m_0) | E_d (eV) | μ_{2D} (cm ² V ⁻¹ s ⁻¹) |
|----------|---|-------------------------------|-----------------|------------|---|
| Electron | x | 205.85 | 0.16 | -12.62 | 1061.66 |
| | y | 202.45 | 0.16 | -12.62 | 1044.08 |
| Hole | x | 205.85 | -1.69 | -6.84 | 28.35 |
| | y | 202.45 | -1.69 | -6.99 | 26.69 |

effective mass ($-1.69m_0$) agrees well with the very concave conduction bands in Fig. 3. The increased effective mass of a hole, on the other hand, is the result of flat valence bands. As a result, the mobility of the electrons is substantially greater than that of the holes. These findings contradict those of 2D MoSi₂N₄, where the hole mobility is greater than the electron mobility²¹ due to more concave valence bands than conduction bands.⁶⁶ The mobility of charge carriers in the x and y directions is approximately the same as in the SnSi₂N₄ compound.³⁶ The 2H SnGe₂N₄'s electron mobility of 1061.66 cm² V⁻¹ s⁻¹ is much higher than the one of MoS₂.⁶⁷ In comparison with MX₂N₄ monolayers (M = Mo, W; X = Si, Ge),²³ whose electron mobilities are in the range of 200–690 cm² V⁻¹ s⁻¹ and hole mobilities are in the range of 1100–2490 cm² V⁻¹ s⁻¹, the layered SnGe₂N₄ possesses higher electron mobility and lower hole mobility, which are about 1061.66 cm² V⁻¹ s⁻¹ and 28.35 cm² V⁻¹ s⁻¹, respectively.

6 Effect of strain and external electric fields on the electronic structure of 2H SnGe₂N₄

Strain is well known to effectively modify the band structures of many 2D materials^{68,69} due to the fact that the Hamiltonian function of the 2D structure is greatly affected by the decrease of its symmetry.⁷⁰ As shown in Fig. 3, the HSE06 band gap is larger than the PBE band gap, however both band structures share very similar patterns. The PBE method describes the electronic structures well with low computational cost. Therefore, the PBE methods are suitable for investigating the band gap variation of 2H SnGe₂N₄ due to strain and external electric field; the results are presented in Fig. 7, where the applied strain ranges from -10% to 10%, and the external electric field varies from -0.5 to 0.5 V Å⁻¹.

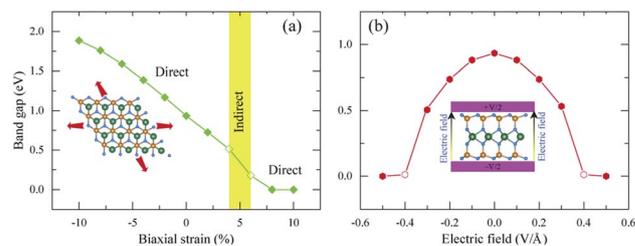


Fig. 7 The effect of (a) biaxial strain and (b) an external electric field on the band gap of 2H SnGe₂N₄.

The band gap of 2H SnGe₂N₄ grows almost linearly as the compressive strain reaches -10%, whereas tensile strain causes the band gap to decrease at the same slope down to zero at a strain of 7%. It is necessary to note that the PBE method underestimates the band gap values;^{71,72} the difference in band gap values obtained by PBE and HSE06, as shown in Table 1, is about 0.9 eV. However, the rates of decrease of the band gap, shown in Fig. 7, are about 0.1 eV every 1% of tensile strain and 0.25 eV every 0.1 V Å⁻¹. Therefore, it is expected that the layered SnGe₂N₄ semiconductor will change into a metal under a higher rate of tensile strain or higher electric strength. External electric fields, both negative and positive, cause a decrease in the band gap of 2H SnGe₂N₄. The external electric fields cause the reduction of SnGe₂N₄'s band gap, as shown in Fig. 7(b) as a quadratic function of the electric strength. The variation of the band structure was estimated and is shown in Fig. 8 and 9 to obtain some insight into the behavior of the band gap of 2H SnGe₂N₄ under external variables.

As seen in Fig. 8, compressive strain primarily impacts the highest valence bands located at -2 to 0 eV. These valence bands are generated *via* the hybridization of s- and p-orbitals from N atoms and d-orbitals from Ge and Sn atoms, as seen in Fig. 4. According to the perturbation theory,⁷³ the p- and d-states repel each other, and the interaction of d-states from neighboring atoms is similarly repulsive.^{74,75} Because the three atoms Sn, Ge and N come closer to each other under compressive pressures, the higher valence bands tend to be

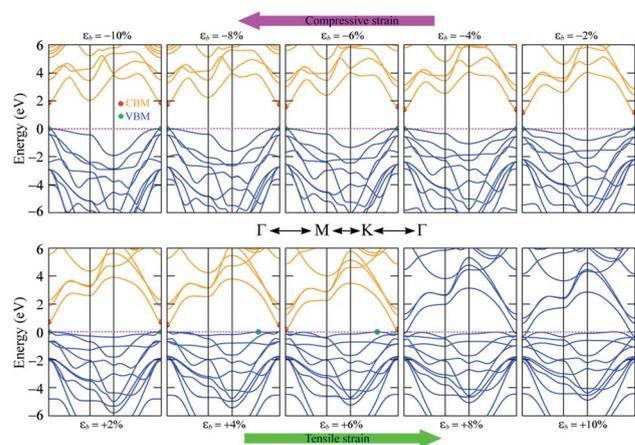


Fig. 8 Band structure variation of 2H SnGe₂N₄ under biaxial strain ϵ (b).



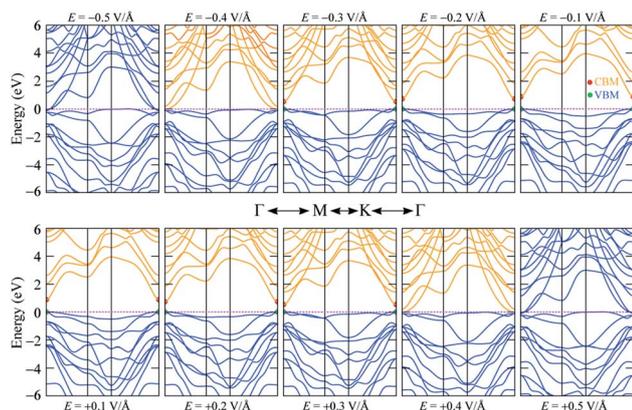


Fig. 9 Band structure variation of 2H SnGe₂N₄ under an external electric field E .

forced down, as illustrated in Fig. 8, resulting in a wider band gap of 2H SnGe₂N₄. Tensile strains have the opposite effect, causing the repulsion between orbitals to decrease, resulting in orbital overlap and narrowing the band gap.

The effect of external electric fields on the band gap of 2H SnGe₂N₄, as depicted in Fig. 9, originates from another mechanism where there is not structural deformation and the crystal field theory (CFT)^{76,77} plays an important role. The static external electric fields will mostly break the degeneracy of d and f orbitals. In the case of 2H SnGe₂N₄, the d orbitals from Ge and Sn atoms contribute a significant part to the highest valence bands. Therefore, when the degeneracy of these states is lifted by electric fields, the valence bands become flatter. As a result, the band gap of 2H SnGe₂N₄ is effectively and uniquely reduced by electric fields regardless of their sign.

In general, both strain and external electric field have notable effects on the band gap value of 2H SnGe₂N₄. Based on the fast and steady decrease of SnGe₂N₄'s band gap under tensile strains and external electric fields, a semiconductor-metal transition is expected to happen for layered SnGe₂N₄. In particular, tensile strains from 4–6% change the band gap nature from direct into indirect.

7 Conclusion

For the first time, the particular properties of layered SnGe₂N₄ were investigated using the PBE, PBE + SOC, and HSE06 methods. The layered SnGe₂N₄ was theoretically predicted to crystallize in a hexagonal structure with the space group $P\bar{6}m2$. The present compound's dynamic and thermal stabilities were confirmed using phonon dispersion estimates and AIMD modeling, respectively. Furthermore, 2H SnGe₂N₄ is mechanically stable, with the Young's modulus (335.493 N m^{-1}) and Poisson's ratio (0.286) indicating that it is tougher than other layered materials in the same structural group, such as MoSi₂N₄, WSi₂N₄, and MoSi₂N₄.

The layered SnGe₂N₄ has a direct band gap of around 1.89 eV and highly concave downward conduction bands that are mostly made up of s-orbitals of the three elements. The fact that

the highest valence bands are mostly produced by the hybridization of d-orbitals from Ge, Sn, and N atoms plays a significant role in the electrical, optical, and transport capabilities. The narrow band gaps and many peaks in the valence and conduction bands of 2H SnGe₂N₄ allow it to absorb light strongly in the infrared, visible, and even ultraviolet regions. This advantage, together with the extremely high electron mobility and a work function of roughly 6 eV, makes 2H SnGe₂N₄ a very promising photoelectric material. Because of its unique electronic structure, 2H SnGe₂N₄ actively responds to strain and external electric fields, leading to a noticeable change in the band gap values, and a possible transition between the semiconductor and metallic natures of layered SnGe₂N₄.

Conflicts of interest

There are no conflicts to declare.

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