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Role of imine isomerization in the stereocontrol of the Staudinger reaction between ketenes and imines*

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Computational-experimental analysis has allowed determining that the stereochemistry of the Staudinger reaction between ketenes and imines is strongly associated with the nature of the imine, which affects the two steps of the reaction. The first step, namely the nucleophilic attack of the sp²-hybridized nitrogen atom of the imine on the sp-hybridized carbon atom of the ketene, is affected by the energetically accessible in situ isomerization patterns of the imine. The second step consists of a conrotatory electrocyclization of the zwitterionic intermediate formed in the previous step. This latter pericyclic step depends on the inward/ outward torquoelectronic effects generated by the substituents of the imine. The impact of these factors on the stereochemistry of this reaction has been analyzed kinetically by numerical methods. The results of these simulations are compatible with the experimental results and support these conclusions.

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Introduction

Since its discovery in 1907 (ref. 1) the Staudinger reaction between ketenes and imines has been one of the most useful methods for the convergent and stereocontrolled synthesis of βlactams² and other valuable compounds³ of biological interest. The versatility of this important reaction is increased by using ketene precursors such as acyl chlorides⁴ or diazo ketones⁵ (Scheme 1). Aside from its practical interest, this reaction is also important from the mechanistic standpoint. As Tidwell⁶ has written, "cycloaddition has remained as the most distinctive, useful and intellectually challenging aspect of ketene

chemistry". In particular, the Staudinger reaction between ketenes and imines constitutes an example of a low energy [2 +2] thermal cycloaddition, a process for which the least motion supra-supra approach is symmetry forbidden.⁷ Actually, in this process the reactants can avoid the orbital symmetry allowed but geometrically demanding $[\pi_2 s + \pi_2 a]$ thermal pathway by means of a stepwise mechanism.8 Thus, the commonly accepted mechanism of the Staudinger reaction involves a sequential formation of the N1-C2 and C3-C4 covalent bonds of the β -lactam ring, according to the reaction path shown in Scheme 1.9

The first step of the reaction consists of a nucleophilic attack of the imine nitrogen on the sp-hybridized carbon atom of the ketene to form, via transition structure TS1, a zwitterionic intermediate denoted as INT in Scheme 1. From this intermediate, the cycloadduct is formed by a conrotatory ring closure associated with transition structure TS2 that can be viewed as an intramolecular Mannich-type reaction of the enolate moiety on the electrophilic iminium part (Scheme 1).8a



Scheme 1 The general mechanism of the Staudinger reaction between ketenes and imines. The possible substituents at the different positions are not shown.

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However, it is important to note that the intramolecular nature of this second step and the contributions of the frontier orbitals of the intermediate **INT** result in a conrotatory motion in the resulting transition structure **TS2**. Therefore, this latter step of the reaction is subjected to tor-quoelectronic effects.¹⁰

A major issue of this reaction is the variable stereocontrol achieved depending upon the nature of the substituents or the reaction conditions.¹¹ In 2006, a systematic experimental study on the stereochemistry of the Staudinger reaction was reported by Xu and coworkers.¹² In this important work, formation of *trans*-cycloadducts was rationalized in terms of rotation about the N1–C4 bond in the corresponding intermediates. This mechanism was also postulated by some of us to understand the formation of *trans*-4-alkoxy- β -lactams in the Staudinger reaction between ketenes and imidates.¹³ In subsequent papers, Xu *et al.* explored this mechanism experimentally in photochemical¹⁴ and computationally in thermal Staudinger (2 + 2)-cycloadditions.¹⁶

It was reported that the reaction of imines derived from polycyclic aromatic amines and aryloxy ketenes yields exclusively the corresponding *trans*-cycloadducts instead of the *cis*-cycloadducts usually found in the reaction between alkoxyketenes and imines derived from substituted anilines.¹⁷ A computational study¹⁸ was performed on these reactions showing that the kinetic distribution in the *cis* : *trans* ratio of the corresponding β -lactams can be understood in terms of the initial E/Z isomerization of the starting imines.

Within this context, the aim of the present work is to extend previous experimental-computational studies to different substituents at the three possible positions of the β -lactam ring in order to assess the general character of the previously proposed mechanism by searching computationally all the possible intermediates and transition structures. As relevant case studies we selected ketenes 1a,b and imines 2ad (Scheme 2). These reagents possess different geometric and electronic features that can shed some light on the factors that determine the stereochemical outcome of this important, but still challenging, reaction. In this work, we confirm the complex nature of the Staudinger reaction in terms of the relevance of the E/Z isomerization of the starting imine, which competes with a similar isomerization in the zwitterionic intermediates. Ultimately, the origins of the cis/trans selectivity of these reactions can be connected with the imine E/Zisomerization.



Scheme 2 Ketenes and imines included in the present study. The corresponding (2 + 2) β -lactam cycloadducts 3 are indicated in Scheme 3.

Results and discussion

We first studied the reaction between methoxy- or acetoxyacetyl ketene (**1a,b** respectively) and (*E*)-*N*-2-naphthyl imine **2a**, (*E*)-*N*-mesityl imine **2b** and aryliminoindolones **2c,d**. These ketenes were generated *in situ* from the corresponding methoxyacetyl and acetoxyacetyl chlorides, **1**′**a** and **1**′**b**, respectively (Scheme 3). Different reaction conditions were considered. Given the stepwise nature of the reaction mechanism and the presence of zwitterionic intermediates, dichloromethane at $-78 \text{ }^{\circ}\text{C} \rightarrow \text{rt}$ (method A) or at room temperature (method B), as well as less polar toluene (method C) were tested. Concerning the order of addition of the reagents, two different protocols were



Scheme 3 Staudinger reactions between ketenes 1a,b (generated from the corresponding acyl chlorides 1'a,b) and Schiff bases 2a–d under different conditions. X-ray diffraction structures of *cis*- and *trans*-3bc are also given.

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considered: the "imine-first" sequence (method a) and the "acyl chloride-first" protocol (method b). The combination of these reaction conditions should provide information about the *in situ* generation of the ketene and its reaction with the corresponding imine. The reaction conditions and observed stereochemical outcomes of these reactions are gathered in Scheme 3.

As far as (E)-N-2-naphthyl imine 2a is concerned, the reaction yields a 3:1 racemic cis- and trans-3aa mixture of isolated diastereoisomers under the A-b protocol. This result complements the trans-preference previously observed in the reaction between methoxyketene 1a and (E)-N-1-naphthyl phenyl imine.18 In addition, the reaction of acetoxyacetyl ketene 1b and (E)-N-mesityl imine 2b in refluxing toluene under the "iminefirst" protocol yields exclusively trans-3bb. In the case of the reaction of acetoxyacetyl ketene 1b and aryliminoindolone 2c, the proportion of cis-trans-products strongly depends on the solvent and reaction temperature used. In that case, *cis*-3bc is the observed major product (1.3:1) when the reaction is carried out at low temperature. Moreover, an increase in the reaction temperature favors the formation of trans-3bc (1:3.9). The stereochemistry of racemic cis- and trans-3bc were confirmed by X-ray diffraction analysis.19 Isatine-derived imine 2d yielded complex reaction mixtures upon reaction with methoxyacetyl chloride under different reaction conditions listed in Scheme 3 as A-b. The corresponding 2-azetidinones could be detected in these reaction mixtures as by-products. Being aware that the amide indolone may interfere with the Staudinger reaction by consuming acid chloride and forming species that may compete with the 2-azetidinone formation, we carried out the reaction of imine 2d with an excess (2.2 equivalents per equivalent of imine) of acid chloride. Under these conditions, excellent yields of the corresponding 2-azetidinones having the isatine amide nitrogen acylated were isolated as 1:1 cis-trans mixtures in both cases (Scheme 3). Thus, under the A-b protocol, equimolar ratios of both cis- and trans-3ad.bd cycloadducts were obtained, confirming the low stereocontrol of these Staudinger reactions leading to 4-spiro- β -lactams. Interestingly, an increase of the proportion of the *trans*-β-lactam 3bc was observed when toluene was used as solvent (C-a conditions, Scheme 3), instead of more polar dichloromethane (B-a conditions).

To understand the origins of this stereocontrol, we have performed DFT calculations on the $1a + 2a \rightarrow 3aa$, $1b + 2b \rightarrow$ 3bb and $1b + 2c \rightarrow 3bc$ reactions at the M06-2X(PCM)/def2-TZVPP level of theory. We have explored the potential energy surfaces associated with all the possible intermediates and transition structures of Staudinger reactions between imines 2a-c and ketenes 1a,b leading to cis- and trans-cycloadducts 3aa,bb,bc. The shape of the scans thus obtained projected on two reaction coordinates related to the pertinent internuclear distances and dihedral angles can be appreciated in Fig. 1A, together with the definition of the kinetic constants corresponding to each elementary step (Fig. 1B). This general picture shows that the stereochemical outcome depends not only on the two steps of the (2 + 2) reaction but also on the E/Z isomerisation of the starting imine 2 or zwitterionic intermediate INT via transition structures TS1 and TSR, respectively. Therefore, a detailed analysis of each elementary step is required.



Fig. 1 (A) General reaction paths for the Staudinger reactions between ketenes **1a**,**b** and imines **2a**,**b**,**c** to yield *cis*- and *trans*- β -lactams **3aa**,**bb**,**bc**. The reaction coordinates correspond to the formation of the N1–C2 and C3–C4 bonds as well as modifications of the indicated dihedral angles. (B) Definition of the kinetic constants associated with each elementary step.

The E/Z isomerization of imines has been studied both experimentally²⁰ and computationally.²¹ According to these studies, at least three mechanisms have been proposed (Scheme 4). The first one consists of a rotation about the $C(sp^2)$ =N(sp^2) imine moiety. The second and third mechanisms involve inversion of configuration at the nitrogen atom, with a C=*N*-aryl bond angle of *ca*. 180 deg. In the second case, this inversion takes place with a concomitant rotation of the aryl group (perpendicular inversion), whereas in the third case this inversion occurs with no rotation of the N-aryl group (planar inversion).

In N-benzylideneanilines, the experimental E/Z isomerization barriers range from *ca.* 14 kcal mol^{-1} for electron withdrawing groups to *ca.* 19 kcal mol^{-1} for electron releasing groups such as dimethylamino or methyl groups.^{21a} Similar studies on imines stemming from ketones showed E/Z isomerization activation energies of ca. 15 kcal mol⁻¹.^{21b,c} Hammett plots of these experimental data suggest different mechanisms depending upon the nature of the substituents. In general, the inversion pathways are predominant. In the case of electronreleasing substituents at the N-aryl moiety, the planar mechanism is the less energetic one, whereas electron-withdrawing substituents at the same position promote perpendicular geometries in the corresponding transition structures.²² These data indicate that, in a given Staudinger reaction, the energy barrier associated with E/Z isomerization of the starting imine can compete with the activation energies of the two-step



Scheme 4 Rotation and inversion mechanisms for (E)/(Z) isomerization of imines

mechanism, in particular with the first step leading to the formation of the C-N bond of INT intermediates. Therefore, the computational studies discussed below will start with this E/Zisomerization step.

We started our study by analyzing the isomerization of imine (E)-2a in dichloromethane and at 195.15 K (-78 °C, Aconditions). The geometry of the transition structure TSia and the relative energies of the two isomers as well as the activation energy for the isomerization reaction are shown in Fig. 2A. According to our results, since the C4-N1-C5 bond angle of TSia is ca. 180 deg., the isomerization mechanism for this imine consists of an inversion of the starting imine. In addition, the β naphthyl group in TSia is perpendicular to the C6-C4-N1 plane, thus indicating an aza-allenyl structure for this saddle point (Fig. 2B).

This cumulene structure is stabilized with respect to Nphenyl imines by delocalization of the negative charge along the N-aryl system of TSia (Fig. 2B). This delocalization can be appreciated by inspection of the bond index of the N1-C5 pair (Fig. 2A). Therefore, the isomerization mechanism corresponds to the inversion-perpendicular mode shown in Scheme 4. The calculated activation energy for the isomerization of (E)-2a is ca. 1.3 kcal mol⁻¹ higher than the *N*-1- α -naphthyl counterpart.¹⁶ As expected, the (Z)-isomer of 2a is calculated to be ca. 4.9 kcal mol⁻¹ less stable than its (*E*)-isomer.

In the case of N-mesityl imine 2b, our calculations show that the presence of the three methyl groups results in a reduction of the isomerization barrier of ca. 2 kcal mol⁻¹ compared to its unmethylated counterpart.¹⁶ As in the (E)/(Z) transformation of



Fig. 2 (A) Optimized structure of transition structure TSia, associated with the isomerisation of imine 2a (M06-2X(PCM)/def2-TZVPP level of theory). Relative Gibbs energies, in kcal mol⁻¹, computed at 195.15 K (A-conditions, see Scheme 3) are also given. Bond distances and angles are in Å and deg., respectively. Numbers in parentheses correspond to the calculated bond orders. (B) Several polar resonance forms corresponding to TSia emphasizing its aza-allenyl structure.



Fig. 3 Optimized structure of transition structure TSib, associated with the isomerization of imine 2b (M06-2X(PCM)/def2-TZVPP level of theory). Relative Gibbs energies, in kcal mol⁻¹, computed at 195.15 K (A-conditions, see Scheme 3) and at 298.15 K (in brackets) are also given. Bond distances and angles are in Å and deg., respectively. Numbers in parentheses correspond to the calculated bond orders.

imine **2a**, the isomerization mechanism consists of an inversion-perpendicular pathway (*vide supra*).

The isomerization pattern of imine 2c is slightly different (Fig. 4A). According to our calculations, TSic exhibits C_s symmetry and therefore the isomerization takes place via inplane inversion with no rotation about the N-PMP bond. Analysis of the Wiberg bond indices and the Kohn-Sham MOs are compatible with Valence Bond (VB) resonance forms shown in Fig. 4B (see ESI[†] for further information). The aromaticity of the indole moiety in TSic determines the relatively large contribution of different polar forms in which the simultaneous azaallenic delocalization pattern observed in TSia is not essential. This situation permits to keep the C_s symmetry and leads to a relatively low activation energy compared to the one associated with the isomerization of N-aryl imine 2b. In addition, the energy gap between both isomers is of 1 kcal mol⁻¹ at 298 K (Fig. 4A). Our calculations show that the isomerization process of 2c is feasible via an inversion-planar geometry of the corresponding transition state, a mechanism favored in ketimines with electron-releasing groups at the N-aryl substituent.²² This rapidly cis/trans interconversion at room temperature was found to be characteristic of 3-arylimino-2-indolones. Further analysis under benzene reflux conditions (348.15 K, close to Cconditions) show a reduction of about 0.4 kcal mol^{-1} on the



Fig. 4 (A) Optimized geometry of TSic and relative Gibbs free energies (M06-2X(PCM)/def2-TZVPP level of theory). Gibbs corrections computed at 298.15 K (room temperature, dichloromethane, B-conditions) and 384.15 K, (refluxing toluene, C-conditions, in brackets) in kcal mol⁻¹, are also given. Bond distances and angles are in Å and deg., respectively. Numbers in parentheses correspond to the calculated bond orders. (B) Several polar resonance forms corresponding to TSic compatible with its C_s symmetry.

computed activation barriers, thus favoring the equilibration of both isomers. Moreover, at this temperature, the energy difference between (E)-/(Z)-imines decreases. Remarkably, ¹H-NMR experiments on E/Z mixtures of imine **2c** at different temperatures showed fast exchange between the methyl groups signals at 373 K and 393 K (for *N*-methyl and methoxy moieties, respectively). These temperature values correspond to a Gibbs activation energy of *ca*. 19.1–19.6 kcal mol⁻¹ (see ESI† for further details), in nice agreement with the theoretical value, thus showing the reliability of the computational study.

We next examined the transition structures, reaction intermediates and products corresponding to the reaction between methoxyketene **1a** and both isomers of imine **2a**.

The relative energies and geometries of the transition structures are gathered in Fig. 5. Our calculations indicate that (E)-2a is less nucleophilic than its (Z)-isomer. Thus, the calculated nucleophilic values ω^{-} with respect to **1a** are 1.58 and 1.85 meV, respectively (see eqn (8) in the Computational methods section). However, the activation energy for the formation of (E)-**INTaa** *via* (*E*)-**TS1aa** is 0.4 kcal mol⁻¹ lower than that associated with formation of (Z)-INTaa. Both saddle points TS1aa correspond to noncoplanar attacks (see the corresponding ω_{4123} values in Fig. 5) of the imine nitrogen on the sp-hybridized carbon atom of methoxyketene 1a. It is noteworthy that the activation barriers for the formation of N1-C2 bonds in both intermediates are lower than those computed for the isomerization steps between (E)- and (Z)-2a. In particular, the activation free energy associated with formation of (E)-INTaa from (E)-2a and **1a** is 7.5 kcal mol^{-1} lower than that corresponding to the conversion of (E)-2a into (Z)-2a (Fig. 2 and 5). In addition, (Z)-**INTaa** is only 0.6 kcal mol⁻¹ more stable than (*E*)-**INTaa** because of the lower steric crowding associated with the phenyl group at C4.

Conrotatory cyclization of (E)-INTaa to yield cis-3aa has an activation barrier of 5.7 kcal mol⁻¹, a process much faster than isomerization to yield (Z)-INTaa via TSRaa (Fig. 5). The energy barrier associated with this latter isomerization is higher than that calculated for the isomerization of the starting imine. In the former case, the iminium moiety cannot isomerize via the inversion (perpendicular) mechanism and rotation about the C=N(+), more costly in terms of energy, is the only possibility. Therefore, this isomerization postulated for other Staudinger reactions, is not competitive in this specific case. The $[\pi_4 c]$ electrocyclization of (Z)-INTaa has a lower activation barrier compared to its (E)-counterpart. These results agree with the torquoselectivity effects that operate in both saddle points. Thus, in cis-TS2aa the electron-releasing group methoxy group is outward with respect to the C3…C4 bond in formation, whereas the electron-releasing group 4-phenyl is inward. Therefore, despite having a methoxy group placed in a favored position, this latter orientation is not favored according to the torquoselectivity theory. In contrast, in trans-TS2aa both substituents occupy outward positions, which results in a less energetic saddle point. Actually, the activation barrier associated with the conrotation of (E)-INTaa via cis-TS2aa is calculated to be 2.5 kcal mol⁻¹ higher in energy than that associated with conrotation of (Z)-INTaa via trans-TS2aa. As far as the relative



Fig. 5 Fully optimized transition structures (M06-2X(PCM)/def2-TZVPP level of theory) associated with formation of β -lactams **3aa** from methoxyketene **1a** and imine **2a**. Bond distances, angles and dihedral angles (as defined in Fig. 1, in absolute values) are given in Å and deg., respectively. Numbers on the arrows are the relative Gibbs energies, in kcal mol⁻¹ and at 195.15 K (dichloromethane, Aconditions).

energies of both β -lactam cycloadducts are concerned, *trans*-**3aa** is calculated to be only 0.3 kcal mol⁻¹ more stable than its *cis*-congener.

The reaction between acetoxyketene 1b and imine 2b in both its (*Z*)- and (*E*)-forms was also analysed. The relative energies and the geometries of the relevant transition structures are gathered in Fig. 6.

In this case, the activation barrier associated with the N1–C2 bond formation of (*Z*)-**2b** is 1.5 kcal mol⁻¹ (A-conditions) or 1.4 kcal mol⁻¹ (B-conditions) lower than that of its (*E*) counterpart. This is in agreement with the higher computed nucleophilicity ω^- of (*Z*)-**2b** compared to (*E*)-**2b** (1.4 and 6.1 10⁻¹ meV, respectively, see eqn (8) in the Computational methods section). This is a consequence of the presence of the methyl groups in *ortho*-CMe position, which leads to a rotation about the C6–C4– C5–CMe dihedral angle thus avoiding the expected planar disposition observed in most *N*-aromatic imines. The final effect is the enhancement of the occupation of the imine lone pair.

Remarkably, in this case the activation barrier associated with the conrotatory step is higher than the one associated with the first step, in contrast with the previous example. Thus, the high steric clash makes the barrier to rise up to 13.0 kcal mol⁻¹ for *cis*-**TS2bb** and 8.9 kcal mol⁻¹ for *trans*-**TS2bb**. This latter relative lower energy is also in agreement with the 3-out/4-out torquoelectronic effect operating in trans-TS2bb. Our calculations show that *trans*-3bb is about 2 kcal mol⁻¹ more stable than cis-3bb. In addition, our results indicate that, once the first step of the Staudinger reaction has started, the reaction paths leading to both cycloadducts are independent to each other, since pathways connecting (E)-INTbb and (Z)-INTbb via TSRbb are of much higher energy (Fig. 6). Also in this case, rotation about the C=N(+) bond in **INTbb** has an activation energy of *ca*. 36 kcal mol^{-1} , a value that cannot compete with the activation energies associated with conrotatory electrocyclizations leading to cis- and trans-β-lactams 3bb. Therefore, also in this case, formation of trans-3bb via isomerization of zwitterionic



Fig. 6 Fully optimized transition structures (M06-2X(PCM)/def2-TZVPP level of theory) associated with formation of β -lactams **3bb** from acetoxyketene **1b** and imine **2b**. Bond distances, angles and dihedral angles (as defined in Fig. 1, in absolute values) are given in Å and deg., respectively. Numbers on the arrows are the relative Gibbs energies, in kcal mol⁻¹ at 195.15 K (dichloromethane, A-conditions) and at 298.15 K (dichloromethane, B-conditions, in brackets).



Fig. 7 Fully optimized transition structures (M06-2X(PCM)/def2-TZVPP level of theory) associated with formation of β -lactams **3bc** from acetoxyketene **1b** and imine **2c**. Bond distances, angles and dihedral angles (as defined in Fig. 1, in absolute values) are given in Å and deg., respectively. Numbers on the arrows are the relative Gibbs energies, in kcal mol⁻¹ and at 298.15 K (dichloromethane, B-conditions) and at 384.15 K, (refluxing toluene, C-conditions, in brackets).

intermediate (*E*)-**INTbb** to its congener (*Z*)-**INTbb** cannot proceed under A- and B-conditions.

Finally, we examined the reaction between acetoxyketene 1b and imine 2c in both (*Z*)- and (*E*)-forms. The relative energies and the geometries of the relevant transition structures are gathered in Fig. 7.

The computed nucleophilicity ω^- of both isomers of imine **2c** are 0.74 and 7.91 meV for (*E*)-**2c** and (*Z*)-**2c** respectively. Similarly, acetoxyketene **1b** is more electrophilic than its methoxy analogue **1a**. The computed ω^+ for these ketenes are 41.3 and 45.2 meV, respectively. It is remarkable that in this case the activation energy at 298.15 K, associated with formation of the N1-C2 bond, is lower than the barrier corresponding

to the imine isomerization step (see Fig. 4 and 7). Moreover, at the same temperature both (*E*)-**TS1bc** and (*Z*)-**TS1bc** are reached through a similar activation barrier. In this case, the second step of the reaction, namely the formation of the C3–C4 bond *via* a conrotatory electrocyclization presents lower energetic barriers than the initial step. Saddle point *cis*-**TS2bc** is calculated to be associated with a lower free energy barrier with respect to *trans*-**TS2bc**. This is not surprising since in the former conrotatory saddle point the electron-withdrawing amidic C==O moiety occupies the 4-inward position, whereas the electron-releasing phenyl moiety is in an also favored 4-outward disposition. Surprisingly, the activation barrier of the first step increases at higher temperatures (C-conditions), pointing out

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the relevance of the entropic term in these particular N1–C2 bond formation reactions. In this reaction, the Gibbs energy of transition state **TSRbc**, associated with rotation about the N1– C2 bond, corresponded to a significantly lower activation energy associated with the conversion of (*E*)-**INTbc** into (*Z*)-**INTbc**. However, this latter activation energy is much larger than the activation energies associated with conrotatory transition structures **TS2bc**. Therefore, also in this reaction formation of β lactam *trans*-**3bc** is not predicted to proceed *via* isomerization of zwitterionic intermediates. Once again, *trans*-**3bc** is calculated to be 1.2 or 2 kcal mol⁻¹ thermodynamically more stable than its *cis*-analogue at 298.15 K (B-conditions) or 384.15 K (Cconditions), respectively.

The computational analysis of these three reactions provide a general picture that involves four aspects: (i) the isomerization of the imine; (ii) the activation energy associated with the formation of the C–N bond; (iii) the relative stability and interconversion of the zwitterionic intermediates; and (iv) the activation energy associated with the formation of the C(3)-C(4)bond. The relative weights of these events can determine the stereochemical outcome of each reaction. Table 1 compiles the most relevant computational data associated with these calculations.

We generated the kinetic profiles for $1a + 2a \rightarrow 3aa$, $1b + 2b \rightarrow 3bb$ and $1b + 2c \rightarrow 3bc$ as we did in the reaction between ketene 1a and the *N*-(1-napthalen-yl) congener of imine 2a.¹⁶ We performed our simulations assuming that formation of β -lactams 3aa, bb, bc from the corresponding zwitterionic intermediates **INT** is irreversible. Therefore, the formation of *cis*- and *trans*-cycloadducts 3 can be described by means of eqn (1) and (2):

$$\frac{\mathrm{d}[trans-3]}{\mathrm{d}t} = k_2^t[(Z)-\mathrm{INT}] \tag{1}$$

Table 1 Summary of the most relevant computational data^{*a*} shown in Fig. 2–7. L and S descriptors denote large and small substituents, respectively

Reaction	$\underline{1a+2a \rightarrow 3aa}$	$\begin{array}{c} \mathbf{1b} + \mathbf{2b} \rightarrow \\ \mathbf{3bb} \end{array}$		$\begin{array}{c} \mathbf{1b} + \mathbf{2c} \rightarrow \\ \mathbf{3bc} \end{array}$	
Rxn conditions ^b	А	Α	В	В	С
$\Delta G_{\rm a}({\rm TSi})$	19.4	17.7	17.8	17.9	17.5
$\Delta G_{\rm rel}[(Z)-2 - (E)-2]$	4.9	2.7	2.9	1.0	0.4
$\Delta G_{\rm a}[(E)$ -TS1]	11.9	9.6	10.1	15.1	19.6
$\Delta G_{\rm a}[(Z)$ -TS1]	12.3	8.1	8.7	15.1	18.4
$\Delta G_{\rm rel}[(E)$ -INT – (Z)-INT]	-0.6	-1.4	-1.5	0.0	-1.1
$\Delta G_{\rm a}(\mathbf{TSR})$	22.6	36.1	36.7	9.9	7.6
$\Delta G_{\rm a}(cis$ -TS2)	5.7	13.0	12.9	0.2	0.1
$\Delta G_{\rm a}(trans-{\rm TS2})$	3.2	8.9	8.6	3.9	1.9
$\Delta G_{\rm rxn}(cis-3)$	-33.9	-26.7	-30.6	-28.8	-32.8
$\Delta G_{\rm rxn}(trans-3)$	-34.2	-67.8	-28.2	-69.0	-30.2

^{*a*} Activation (ΔG_a), relative (ΔG_{rel}) and reaction (ΔG_{rxn}) free energies calculated at the M06-2X(PCM)/def2-TZVPP level of theory, given in kcal mol⁻¹. ^{*b*} Temperatures and solvents for conditions A–C are given in Scheme 3.

$$\frac{\mathrm{d}[cis-\mathbf{3}]}{\mathrm{d}t} = k_2^c[(E)-\mathbf{INT}] \tag{2}$$

The evolution of intermediates and reactants is described by eqn (3):

$$-\frac{\mathrm{d}}{\mathrm{d}t}A = KA \tag{3}$$

where A represents reactants and reaction intermediates in the form

$$A = \begin{pmatrix} [(E)-2] \\ [(Z)-2] \\ [(E)-\mathbf{INT}] \\ [(Z)-\mathbf{INT}] \end{pmatrix}$$
(4)

and *K* is the interaction matrix that includes the kinetic constants associated with the different elementary steps:

$$K = \begin{pmatrix} k_i + k_1^E[1] & -k_{-i} & -k_{-1}^E & 0 \\ -k_i & k_{-i} + k_1^Z[1] & 0 & k_{-1}^Z \\ -k_1^E[1] & 0 & k_{-1}^E + k_R + k_2^c & -k_{-R} \\ 0 & -k_1^Z[1] & k_R & k_{-1}^Z + k_{-R} + k_2^t \end{pmatrix}$$
(5)

The meaning of the different kinetic constants is outlined in Fig. 1B. These kinetic constants were calculated from the relative energies reported in Table 1 (see also Fig. 2–7) and using the Eyring equation:

$$k_i = \frac{k_{\rm B}T}{h} \exp\left(-\frac{\Delta G_i^{\neq}}{RT}\right) \tag{6}$$

Numerical integration of eqn (1)-(6) led to the time profiles shown in Fig. 8 (the values for these constants can be found in the ESI[†]). The simulated kinetic profiles associated with the formation of 3aa from 1a and 2a show the preferential formation of cis-3aa under A-conditions (Fig. 8A). This result can be explained in terms of the lower activation barrier associated with the N1-C2 bond formation compared to that associated with the isomerization of the imine 2a (11.9 kcal mol⁻¹ vs. 19.4 kcal mol^{-1} respectively, Fig. 2 and 5). Therefore, the starting imine (E)-2a would react with methoxyketene 1a to form (E)-INTaa instead of isomerizing to form (Z)-2a. Moreover, the barrier associated with the second step is lower than the isomerization of this intermediate, thus forming β-lactam cis-3aa as the major stereoisomer, in good agreement with the experimental results. In the case of imine 2b, our simulations show a strong dependence on the reaction conditions. At low temperature (195.15 K, A-conditions, Fig. 8B), the imine isomerization takes place slowly. Therefore, despite the ring closure of (E)-INTbb is about 4 kcal mol⁻¹ higher in energy than the ring closure of (Z)-INTbb, a noticeable amount of cis-3bb is formed. At 298.15 K, despite there is no significant difference between the computed imine isomerization activation barriers, the kinetics are one order of magnitude faster. Therefore, initial



Fig. 8 Simulated stereochemical outcomes associated with the reaction between ketenes **1a**,**b** and imines **2a**,**b**,**c** to yield β -lactams (A) *cis*- and *trans*-**3a**; (B and C) *cis*- and *trans*-**3bb**; (D and E) *cis*- and *trans*-**3bc**. The distributions of isomers at different temperatures and in the presence of different solvents were obtained from eqn (6)–(11).

isomerization of 2b is observed prior to the N1-C2 bond formation step. In this case, the energy difference between the ring closure activation barriers promoted the exclusive formation of trans-2bb. As far as arylaminoindolone 2c is involved, the simulated kinetic profile is strongly dependent of the reaction temperature. At room temperature (B-conditions), preferential formation of *cis*-3bc is predicted by our simulations (Fig. 8D) whilst at 384.15 K (C-conditions) trans-3bb is the major one (Fig. 8E). This trend towards trans-selectivity at higher temperatures was previously observed by Xu et al.23 In the former case, the free energy difference between the initial step corresponding to the formation of the N1–C2 bond is of *ca.* 2 kcal mol^{-1} , which determines the preferential formation of (E)-INTbc compared to (Z)-INTbc (Fig. 7). Moreover, in the case of (E)-INTbc the activation barrier associated with the second step is lower than the one associated with the N1-C2 bond-breaking step leading to the reactants or the isomerization process. This means that the initial equilibrated mixture of imines 2c

would react with acetoxyketene **2b** to form preferentially (*E*)-**INTbc**. This latter intermediate would finally evolve to the kinetically favoured product *cis*-**3bc**. On the other hand, at 384.15 K there is a difference in free energy of only 0.4 kcal mol⁻¹ between both imines.

In addition, the difference in the activation barrier associated with the reaction of (E)-/(Z)-2c with ketene 1b is of 0 kcal mol^{-1} (B-conditions) or 1.2 kcal mol^{-1} (C-conditions). The energetic difference between the ring closure activation barrier and the decomposition of the intermediates towards the reactants is *ca.* 1 kcal mol⁻¹ higher in the case of (*Z*)-**INTbc**. Chemical intuition would suggest the preferential formation of cis-3bc in a less complicated mechanistic scenario. However, due to the exponential nature of the relationship between the kinetic constants and the computed free activation barriers, slightly higher differences in activation barriers do not necessarily implies higher differences in the kinetic constants. In fact, our simulation shows the preferential formation of the most stable β -lactam *trans*-**3bc** under C-conditions (Fig. 8E), in qualitative agreement with the experimental findings (vide supra). This result also suggests that a nonpolar solvent such as toluene under refluxing conditions transfers the stereocontrol to the formation of the polar zwitterionic intermediate. It is noteworthy that, in the three cases studied in this work, (E)/(Z)isomerization of intermediates INT has no effect on the respective stereochemical outcomes. Actually, removal of these isomerization processes in the A-matrix of eqn (5) by making k_R $= k_{-R} = 0$ yields kinetic profiles identical to those gathered in Fig. 8. However, since the magnitude of the activation energies associated with this isomerization process can vary significantly in magnitude, its relevance in other Staudinger reactions cannot be ruled out.

In summary, our computed kinetic profiles are in qualitative agreement with the observed experimental outcomes, pointing out the complex nature of the reaction mechanism of the Staudinger reaction between ketenes and imines, despite its formal simplicity.

Conclusions

Results above show that the Staudinger reaction is extremely sensitive to multiple factors. In principle, initial (E)/(Z)-imine isomerization in N-polyaromatic imines is difficult and the reaction leads mainly to reaction mixtures in which cis-β-lactams predominate. For these substrates, the stereochemistry of the final four-membered ring is determined by the initial formation of the corresponding zwitterions, and hence from the ratio of (E)/(Z) imines. Isatine-derived imines yield reaction mixtures in which the corresponding trans-2-azetidinone predominates under refluxing toluene conditions. The second step of the reaction, namely the formation of the C3-C4 bond via a conrotatory electrocyclization presents lower energetic barriers than the initial nucleophilic attack of the imine to the ketene. The corresponding trans-β-lactam is exclusively obtained from the imine derived from the bulkier 2,4,6-trimethylaniline and benzaldehyde, 2b. The presence of bulkier substituents in the initial imine can hamper the second step,

Moreover, the decomposition of these intermediates increases its relevance at higher reaction temperatures, thus yielding the thermodynamically more stable *trans*- β -lactam. It is remarkable that, in all the studied cases, the isomerization of the zwitterionic intermediates has no relevance on the stereochemical outcome of the reaction. This isomerization step has been claimed several times as the responsible for obtaining of cis-trans mixtures in the reaction of acid chlorides and imines in the presence of tertiary amines.

It is also noteworthy that all the conrotatory electrocyclic transition structures associated with the second step of the reaction follow the inward/outward torquoelectronic model developed by Houk. However, other factors can determine the observed stereocontrol of the reaction.

To sum up, depending upon the nature of the imine, three different situations may determine the selectivity of the Staudinger reaction: the ability of isomerization of the imine, the formation of the intermediate zwitterions, which is related to the nucleophilicity of the imine and, finally, the inward/ outward disposition of the substituents in the conrotatory cyclisation of the zwitterionic intermediates to yield irreversibly the corresponding β-lactams. In the mechanistic model by Xu et al.12 the isomerization of the zwitterionic intermediates determines the stereochemical outcome. The present study extends this model by including the isomerization of the starting imine, which can be determinant in some cases, such as those reported in the present study.

Experimental methods

General methods for the preparation of β-lactams 3

Method A-a. To a solution of imine 2 (1.79 mmol) and Et₃N (1.97 mmol) in 15 mL of anhydrous CH₂Cl₂ purged with argon and cooled to -78 °C, a solution of acyl chloride (1.79 mmol) in 5 mL of CH₂Cl₂ was dropwise added. The mixture was allowed to reach rt overnight. The crude mixture was washed with saturated NaHCO₃ (3.0 mL) and brine (3.0 mL). The combined organic layers were dried over anh. Na₂SO₄ and the solvent evaporated in vacuo. The crude mixtures were purified by SiO₂ chromatography (EtOAc/Hex mixtures).

Method A-b. A solution of Et₃N (0.27 mmol) in 0.5 mL of CH₂Cl₂ was dropwise added via syringe to a solution of the corresponding acid chloride (0.25 mmol) purged with argon and cooled to -78 °C. The reaction mixture was kept stirring for 20 min at this temperature and a solution of imine 2 (0.22 mmol) in 0.5 mL of CH₂Cl₂ was then dropwise added. The mixture was allowed to reach at rt overnight. The crude mixtures were then diluted with 5.0 mL of CH₂Cl₂, washed with saturated NaHCO₃ (3.0 mL) and brine (3.0 mL). The organic layer was dried over anh. Na₂SO₄ and the solvents evaporated in vacuo. The crude mixtures were purified by SiO₂ chromatography (EtOAc/Hex mixtures). For imine 2d the ratio imine : acid chloride : TEA was 1 : 2.2 : 2.6.

Method B-a. To a solution of imine 2 (1.79 mmol) and Et₃N (1.97 mmol) in 15 mL of anhydrous CH₂Cl₂ purged with argon at rt, a solution of acyl chloride (1.79 mmol) in 5 mL of CH₂Cl₂ was dropwise added. The resulting mixture was stirred at rt for the corresponding time. The crude mixtures were then diluted with 5.0 mL of CH_2Cl_2 , washed with saturated NaHCO₃ (3.0 mL) and brine (3.0 mL). The organic layers dried over anh. Na₂SO₄ and the solvents evaporated in vacuo. The crude mixtures were purified by SiO₂ chromatography (EtOAc/Hex mixtures).

Method C-a. To a solution of imine 2 (1.79 mmol) and Et₃N (1.97 mmol) in 15 mL of anhydrous toluene purged with argon, a solution of acyl chloride (1.79 mmol) in 5 mL of anhydrous toluene was dropwise added. The resulting mixture was refluxed for 3 hours. The crude mixtures were then diluted with 5.0 mL of toluene, washed with saturated NaHCO₃ (3.0 mL) and brine (3.0 mL). The combined organic layers were dried over anh. Na₂SO₄ and the solvent evaporated *in vacuo*. The crude mixtures were purified by SiO₂ chromatography (EtOAc/Hex mixtures).

3-Methoxy-1-(naphthalen-1-yl)-4-phenylazetidin-2-one, 3aa Methoxyacetyl chloride (98.0 mg, 0.90 mmol), imine 2a (183.0 mg, 0.79 mmol) and Et₃N (98.2 mg, 0.972 mmol) were reacted following Method A-b. After quenching the reaction, a crude mixture with a 3:1 cis/trans ratio was obtained and purified by SiO₂ chromatography (Hex/EtOAc 4 : 1) to obtain cis-3aa (125 mg, 0.41 mmol, 52%) and trans-3aa (45 mg, 0.15 mmol, 19%) as white solids.

cis-3aa: mp: 156-157 °C. ¹H NMR (CDCl₃, 300 MHz): δ 7.75 (d, J = 9.1 Hz, 2H), 7.71–7.59 (m, 3H), 7.51–7.31 (m, 7H), 5.35 (d, J = 4.9 Hz, 1H), 4.90 (d, J = 4.9 Hz, 1H), 3.24 (s, 3H). ¹³C NMR (CDCl₃, 75 MHz): δ 164.4, 134.6, 133.4, 133.1, 130.5, 129.1, 128.7, 128.6, 127.9, 127.7, 127.4, 126.6, 125.1, 117.4, 114.1, 84.7, 61.8, 58.4. IR (CH₂Cl₂) $\nu = 1746 \text{ cm}^{-1}$. HRMS (ESI) m/z calc. for $C_{20}H_{17}NO_2 [M]^+$: 303.1259, found 303.1268.

trans-3aa: mp: 192–193 °C. ¹H NMR (CDCl₃, 300 MHz): δ 7.75 (d, J = 9.6 Hz, 2H), 7.68 (d, J = 7.5 Hz, 1H), 7.63-7.55 (m, 2H),7.49–7.32 (m, 7H), 5.06 (d, J = 1.8 Hz, 1H), 4.49 (d, J = 1.8 Hz, 1H), 3.63 (s, 3H). ¹³C NMR (CDCl₃, 75 MHz): δ 164.3, 136.3, 134.6, 133.4, 130.5, 129.3, 129.2, 128.7, 127.7, 127.4, 126.6, 125.9, 125.2, 117.5, 114.3, 91.2, 63.4, 58.3. IR $(CH_2Cl_2) \nu =$ 1769 cm⁻¹. HRMS (ESI) m/z calc. for C₂₀H₁₇NO₂ [M]⁺: 303.1259, found 303.1323.

1-Mesityl-2-oxo-4-phenylazetidin-3-yl acetate, 3bb. Acetoxvacetyl chloride (244.3 mg, 1.79 mmol), imine 2b (400.0 mg, 1.79 mmol) and Et₃N (200 mg, 1.97 mmol) were reacted following Method A-a. After quenching the reaction, only trans-3bb was observed by NMR in the reaction crude. Pure trans-3bb (272 mg, 47%) was obtained after purification by SiO₂ chromatography (Hex/EtOAc 4:1) as a white solid.

trans-3bb: mp: 128–129 °C. ¹H NMR (CDCl₃, 300 MHz): δ 7.31 (s, 5H), 6.82 (s, 2H), 5.84 (d, J = 2.0 Hz, 1H), 5.18 (d, J = 2.0 Hz, 1H), 2.49–2.17 (bs, 6H), 2.23 (s, 3H), 2.22 (s, 3H). ¹³C NMR (CDCl₃, 75 MHz): δ : 169.7, 163.0, 137.9, 135.0, 129.5, 129.3, 128.9, 128.8, 127.0, 79.8, 66.2, 20.8, 20.6, 19.3. IR $(CH_2Cl_2) \nu =$ 1758 cm⁻¹. HRMS (ESI) m/z calc. for C₂₀H₂₁NO₃ [M]⁺: 323.1521, found 323.1519.

1-(4-Methoxyphenyl)-1'-methyl-2',4-dioxospiro[azetidine-2,3'indol-ine]-3-yl acetate, **3bc**. Following Method B-a from acetoxyacetyl chloride (33.7 mg, 0.25 mmol), imine **2c** (66.5 mg, 0.25 mmol) and Et₃N (28.3 mg, 0.28 mmol), a crude mixture (80.0 mg, 0.22 mmol, 87%) with a 1.3 : 1 *cis/trans* ratio was obtained. Following Method C-a from acetoxy-acetyl chloride (33.7 mg, 0.25 mmol), imine **2c** (66.5 mg, 0.25 mmol) and Et₃N (28.3 mg, 0.28 mmol), a crude mixture (75 mg, 0.20 mmol, 82%) with a 1 : 3.9 *cis/trans* ratio was obtained. Purification by SiO₂ chromatography (Hex–EtOAc 1.5 : 1) of the reaction crudes allowed the obtention of pure *cis*-**3bc** and *trans*-**3bc** as white solids.

cis-**3bc**: mp: 197–198 °C. ¹H NMR(CDCl₃, 300 MHz): δ 7.45 (td, *J* = 7.8, 1.3 Hz, 1H), 7.33 (dd, *J* = 7.4, 1.2 Hz, 1H), 7.14 (td, *J* = 7.6, 1.0 Hz, 1H), 7.03–6.97 (m, 1H), 7.02 (d, *J* = 9.0 Hz, 2H), 6.73 (d, *J* = 9.0 Hz, 2H), 5.63 (s, 1H), 3.72 (s, 3H), 3.29 (s, 3H), 2.14 (s, 3H). ¹³C NMR (CDCl₃, 75 MHz): δ 170.1, 170.0, 160.1, 157.0, 143.5, 131.0, 129.2, 123.5, 123.3, 123.2, 119.1, 114.5, 109.1, 82.6, 66.7, 55.4, 26.8, 20.3. IR (CH₂Cl₂) ν = 1770, 1725 cm⁻¹. HRMS (ESI) *m*/*z* calc. for C₂₀H₁₈N₂O₅ [M]⁺: 366.1216, found 366.12128.

trans-**3bc**: mp: 173–174 °C. ¹H NMR (CDCl₃, 300 MHz): δ 7.43 (t, J = 7.8 Hz, 1H), 7.34 (d, J = 7.1 Hz, 1H), 7.09 (t, J = 7.6 Hz, 1H), 7.02 (d, J = 9.0 Hz, 2H), 6.96 (d, J = 7.8 Hz, 1H), 6.73 (d, J = 9.0 Hz, 2H), 5.74 (s, 1H), 3.70 (s, 3H), 3.33 (s, 3H), 1.86 (s, 3H). ¹³C NMR (CDCl₃, 75 MHz): δ 171.8, 168.9, 160.2, 157.0, 144.5, 131.2, 129.2, 125.2, 122.8, 120.4, 118.9, 114.5, 109.1, 80.3, 66.4, 55.3, 26.8, 19.9. IR (CH₂Cl₂) $\nu = 1761, 1723$ cm⁻¹. HRMS (ESI) *m*/*z* calc. for C₂₀H₁₈N₂O₅ [M]⁺: 366.1216, found 366.1224.

3-Methoxy-1'-(2-methoxyacetyl)-1-(4-methoxy-phenyl)spiro[azetidine-2,3'-indoline]-2',4-dione, **3ad**. Methoxyacetyl chloride (189.0 mg, 1.74 mmol), Et₃N (208.0 mg, 2.05 mmol) and imine **2d** (0.200 g, 0.79 mmol) were reacted following Method A-b. After quenching the reaction, a crude mixture with a 1 : 1 *cis/ trans* ratio was obtained and purified by SiO₂ chromatography (Hex/EtOAc 7 : 3) to obtain *cis*-**3ad** (88.0 mg, 0.22 mmol, 28%) and *trans*-**3ad** (75.0 mg, 0.19 mmol, 24%) as white solids.

cis-3ad: mp: 169–171 °C. ¹H NMR (CDCl₃, 300 MHz): δ 8.43 (d, J = 8.2 Hz, 1H), 7.58–7.46 (m, 1H), 7.41–7.26 (m, 2H), 7.02 (d, J = 9.0 Hz, 2H), 6.76 (d, J = 9.0 Hz, 2H), 4.83 (s, 1H), 4.76 (d, J = 6.6 Hz, 2H), 3.73 (s, 3H), 3.56 (s, 3H), 3.50 (s, 3H). ¹³C NMR (CDCl₃, 75 MHz): δ 171.8, 170.5, 162.3, 157.1, 138.9, 131.3, 128.8, 126.4, 123.8, 122.9, 119.1, 117.4, 114.6, 94.1, 73.7, 68.1, 60.0, 59.6, 55.4. IR (CH₂Cl₂) $\nu = 1769$, 1727 cm⁻¹. HRMS (ESI) m/z calc. for C₂₁H₂₀N₂O₆ [M]⁺: 396.1321, found 397.1319.

trans-3ad: mp: 139–140 °C. ¹H NMR (CDCl₃, 300 MHz): δ 8.42 (d, J = 8.0 Hz, 1H), 7.62–7.47 (m, 2H), 7.36–7.33 (m, 1H), 7.00 (d, J = 9.0 Hz, 2H), 6.75 (d, J = 9.0 Hz, 2H), 4.82 (s, 1H), 4.74 (s, 2H), 3.72 (s, 3H), 3.57 (s, 3H), 3.14 (s, 3H). ¹³C NMR (CDCl₃, 75 MHz): δ 174.3, 170.5, 161.7, 157.2, 139.5, 131.4, 129.0, 126.1, 126.1, 121.0, 119.0, 116.9, 114.7, 90.7, 73.8, 67.2, 59.6, 59.3, 55.4. IR (CH₂Cl₂) $\nu = 1756$ cm⁻¹. HRMS (ESI) *m*/*z* calc. for C₂₁H₂₀N₂O₆ [M]⁺: 397.1321, found 397.1323.

2-(3-Acetoxy-1-(4-methoxyphenyl)-2',4-dioxospiro[azetidine-2,3'indoline]-1'-yl)-2-oxoethyl acetate, **3bd**. Acetoxyacetyl chloride (357.6 mg, 2.62 mmol), Et_3N (313 mg, 3.09 mmol) and imine **2d** (0.300 g, 1.19 mmol) were reacted following Method A-b. After quenching the reaction, a crude mixture with a 1:1 *cis/trans* ratio was obtained and purified by SiO₂ chromatography (Hex/ EtOAc 7:3) to obtain *cis*-**3bd** (0.135 g, 0.30 mmol, 25%). *trans*-**3bd** could not be isolated pure.

cis-**3bd**: mp: 170–172 °C. ¹H NMR (CDCl₃, 300 MHz): δ 8.32 (d, J = 8.2 Hz, 1H), 7.49 (t, J = 7.8 Hz, 1H), 7.40 (d, J = 7.6 Hz, 1H), 7.30 (d, J = 8.2 Hz, 1H), 7.01 (d, J = 8.9 Hz, 1H), 6.75 (d, J = 8.9 Hz, 1H), 5.58 (s, 1H), 5.32 (d, J = 17.2 Hz, 1H), 5.08 (d, J = 17.2 Hz, 1H), 3.70 (s, 3H), 2.21 (s, 3H), 2.14 (s, 3H). ¹³C NMR (CDCl₃, 75 MHz): δ 171.8, 170.2, 170.1, 167.0, 159.4, 157.3, 139.0, 131.5, 128.4, 126.5, 123.0, 119.1, 117.2, 114.7, 83.9, 67.0, 64.1, 55.3, 20.3, 20.0. IR (CH₂Cl₂) ν = 1767, 1729 cm⁻¹. HRMS (ESI) m/z calc. for C₂₃H₂₀N₂O₈ [M]⁺: 452.1220, found 452.1231.

Computational methods

All the calculations reported in this paper have been performed within density functional theory.²⁴ The different stationary points were optimized using the highly parameterized M06-2X functional,²⁵ that has been demonstrated to be well suited for the treatment of nonbonding interactions and dispersion forces, which can be relevant in densely substituted interacting systems.²⁶ The standard def2-TZVPP basis sets²⁷ as implemented in the GAUSSIAN 16 (ref. 28) suite of programs has been used. In the optimization and characterization of **TSR** saddle points, open-shell structures were considered in order to describe the possible diradical character of these stationary points associated with rotation about the C=N(+) bond.

Wiberg indices²⁹ B_i were evaluated using the natural bond orbital (NBO) method.³⁰ Zero-point vibrational energy (ZPVE) and Gibbs free energy corrections (TCGFE) were computed at the M06-2X(PCM)/def2-TZVPP level. All the thermodynamic magnitudes were calculated by using thermal corrections computed at 195 K, 298 K or 384 K. Activation Gibbs free energies (ΔG) and reaction Gibbs free energies (ΔG) were computed at the same level considering the initial reagents for the first addition step, and intermediates directly connected to the transition structure for the sing closure step and were corrected in order to consider solvated standard states (see ESI⁺). This approximate methodology for the evaluation of temperature corrections is based on equations derived from noninteracting particles systems that may introduce some errors in the case of low-lying electronic excited states systems. However, we assume that in our particular scenario these errors are similar in all stationary points and have scarce influence in the computed energetic profiles.

Assfeld *et al.*³¹ have shown that inclusion of solvent effects is necessary to reproduce correctly the reaction profile of the Staudinger reaction using *ab initio* methods. We have introduced the solvent effects in our DFT calculations by means of the Polarizable Continuum Model (PCM).³² In all the cases included in this study, the solvents considered were dichloromethane ($\varepsilon = 8.9$) and toluene ($\varepsilon = 2.27$), the ones used in the experimental study. The kinetic treatment of the computed activation Gibbs free energies was performed by means of the FACSIMILE program.³³

$$\omega^+ = \frac{\mu^2}{2\eta} \tag{7}$$

where μ and η are the chemical potential and hardness of the species under study, respectively. Similarly, the nucleophilicity indexes of imines **2** with respect to electrophilic ketenes **1** were calculated using the following conceptually related expression:³⁵

$$\omega_{2 \to 1}^{-} = \frac{1}{2} \frac{(\mu_2 - \mu_1)^2}{(\eta_2 + \eta_1)^2} \eta_2 \tag{8}$$

The chemical potentials and hardnesses of ketenes 1 were calculated within the following approximations:^{26α}

$$\mu_1 = -\frac{I_1 + A_1}{2} \approx \frac{\varepsilon_{\text{HOMO}(1)} - \varepsilon_{\text{LUMO}(1)}}{2} \tag{9}$$

$$\eta_1 = I_1 - A_1 \approx \varepsilon_{\text{LUMO}(1)} - \varepsilon_{\text{HOMO}(1)}$$
(10)

In these latter equations, *I* and *A* stand for the ionization potential and electron affinity and $\varepsilon_{\text{HOMO}}$ and $\varepsilon_{\text{LUMO}}$ are the orbital energies of the corresponding frontier orbitals. In the case of imines 2, since the nucleophilic attacks involve the MOs n_{N} associated with the nitrogen lone pairs, eqn (3) and (4) were adapted accordingly:

$$\mu_2 \approx \frac{\varepsilon_{n_{\rm N}(2)} - \varepsilon_{\rm LUMO(2)}}{2} \tag{11}$$

$$\eta_2 \approx \varepsilon_{\text{LUMO}(2)} - \varepsilon_{n_N(2)}$$
 (12)

Author contributions

F. P. C.: conceptualization, formal analysis, funding acquisition, methodology, project administration, supervision, visualization, resources, writing – original draft. A. de C.: investigation (computational and experimental results), methodology, software, data curation, validation, supervision, visualization. M. A. S.: conceptualization, formal analysis, funding acquisition, methodology, project administration, supervision, validation, resources, writing – review & editing. L. C.: investigation (experimental results), data curation. J. M.: investigation (experimental results). B. K. B.: conceptualization, funding acquisition, project administration, supervision, resources. D. B.: investigation (experimental results).

Conflicts of interest

There are no conflicts to declare.

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