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# A combined experimental and molecular simulation study on stress generation phenomena during the Ziegler–Natta polyethylene catalyst fragmentation process†

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The morphology of particles obtained under different pre-polymerization conditions has been connected to the stress generation mechanism at the polymer/catalyst interface. A combination of experimental characterization techniques and atomistic molecular dynamics simulations allowed a systematic investigation of experimental conditions leading to a certain particle morphology, and hence to a final polymer with specific features. Atomistic models of nascent polymer phases in contact with magnesium dichloride surfaces have been developed and validated. Using these detailed models, in the framework of McKenna's hypothesis, the pressure increase due to the polymerization reaction has been calculated under different conditions and is in good agreement with experimental scenarios. This molecular scale knowledge and the proposed investigation strategy would allow the pre-polymerization conditions to be better defined and the properties of the nascent polymer to be tuned, ensuring proper operability along the whole polymer production process.

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## Introduction

Polyolefins (PO) have contributed to shaping the modern world. Being very versatile, they are used in a wide range of applications and their demand is still expected to increase in volume and applications in the next few decades, imposing an urgent need for sustainable production processes and for improving end-of-life management.<sup>1,2</sup>

The target of all polyolefin manufacturing businesses is to design a process to promote polymer chain growth. For industrial applications, polyethylene (PE) can be produced with both free coordination catalysts (*i.e.*, low pressure PO production technologies) and radical initiators (*i.e.*, high pressure PO production technologies). Coordination catalysts have the huge advantage of fine

control of the polymer molecular microstructure leading to the production of polyolefins with a wide range of properties unimaginable before their discovery. The reason for the success of modern industrial polymerization processes is largely due to the evolution of catalyst technologies and to their achieved level of sophistication towards producing multi-modal grades. Academic and industrial olefin catalytic processes have been developed and implemented since the original discoveries of Ziegler and Natta,<sup>3</sup> and Hogan and Banks (Phillips catalysts).<sup>4</sup> Nowadays, huge volume plants are run in a very cost competitive way. Still, there is margin to optimize production processes and make them more efficient and sustainable, for example in terms of energy efficiency, smooth and controlled operations and optimal product design.<sup>5–10</sup>

Most low pressure olefin polymerization processes utilize heterogeneous catalysts in multi-stage reactor configurations consisting of two- or three-phase reactors connected in series. An optimal process design must take into account different aspects influencing the final properties of the produced polymer. As an example, the mass and heat transfer phenomena occurring during the process may affect the polymerization rate and the polymer molecular microstructure. The evolution of the catalyst (synthesized using MgCl<sub>2</sub> or silica to impregnate a variable quantity of active sites) internal morphology on polymer particle growth during the early stage of polymerization is another striking example. Indeed, the way the nascent polymer induces the fragmentation of the catalyst particles determines the internal and external morphological properties of the polymer particles which in turn, affect the operability of

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the plant, its productivity, and the final polymer properties.<sup>4</sup> All these phenomena mentioned above take place during the dynamic operation of the polymerization reactor, while all aspects controlling those phenomena have a significant impact on both economic and environmental costs. A standard industrial catalytic polymerization process is schematized below (Scheme 1).

In a typical catalytic olefin polymerization process the catalyst is continuously fed to the reactor train together with the addition of a co-catalyst, monomer, comonomer, diluent, and chain transfer agents. The pre-polymerization process involves injecting the catalyst into a slurry reactor that usually operates under relatively mild conditions.<sup>1</sup> In this step, 10–100 grams of polymer per gram of catalyst is produced. Then, the pre-polymerized powder (prepolymer) is injected into the main reactor. The purpose of the pre-polymerization is to improve the control of catalyst particle morphology and obtain an appropriate size of the catalyst particle as well as nascent polymer for the injection into the main reactor train. This is needed since the process conditions in the main reactor are such that the local reaction rates are quite high, and “virgin” catalyst particles would not maintain their integrity without pre-polymerization. In other words, the pre-polymerization step allows just enough polymer to be generated, which means that the catalyst particles fragment but not so much and not too quickly that they disintegrate. For simplicity, we will refer to the term “particle” as the catalyst particle plus a small fraction of polymer which is produced in the pre-polymerization step and can trigger the fragmentation of catalyst particles. It has to be noted that smooth initial fragmentation of the catalyst particle contributes to lessening of the internal heat and mass transfer limitations.<sup>11</sup>

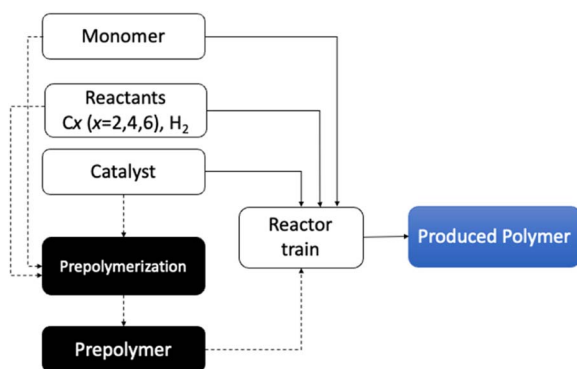
The reaction taking place in the main reactor train is the chain propagation, in the sense of the addition of new monomer (or comonomer) building blocks in the polymeric chain initiated at the catalyst active sites. Hydrogen is added into the reactor to control the molecular weight distribution (MWD), since it acts as the transfer agent causing the break of the developed chain and controlling the length of the produced polymer. Comonomer addition, apart from the apparent increase of its content of the developed polymer, further

reduces the crystallization potential of the nascent polymer, increases the possibility of diffusion of the monomer and comonomer within the catalyst particle, and affects the solubility behaviour of the monomer too (co-solubility effect).<sup>12–16</sup> Usually, a monomer/diluent recycle step precedes the storage of the product.

It is well known that the particle morphology controls the rate at which the reactive species reach the active sites and, hence, the molecular properties of the produced polymer like MWD, the copolymer composition distribution (CCD) and the concentration of the polymer branches. It is worth noting that poor particle morphology (defined, *e.g.*, by shape, bulk density, roughness) would lead to risks of agglomeration, sheeting and chunking phenomena, which largely affect the reactor's operability. Optimal control of particle morphology is directly related to: (i) the growth rate of the catalyst particles during the process. (ii) The selection of the pre-polymerization and polymerization conditions such as the temperature, pressure and the component composition in the reactor.<sup>8,17–19</sup> (iii) How the nascent polymer accumulates in the catalyst particles during the polymerization reaction leading to the particle fragmentation. Based on the above considerations, it is clear that the fragmentation phenomena are pivotal in the particle morphology evolution. A deep understanding of that phenomena would lead to further optimization of the process.<sup>5–10</sup> Indeed, even smaller variation of the properties of the fragmented particles in the early stages of polymerisation can be amplified during the successive polymerization steps and lead to very different morphologies. In practice, control of the initial fragmentation in the plants is mainly handled based on experience and best practices. Besides temperature, monomer and diluent, the particle morphology is adjusted by adding hydrogen (known to improve the flowability) and comonomers, *e.g.* 1-butene or 1-hexene (known to improve productivity, and at the same time decreasing the polymer crystallinity till the point to lead to particle stickiness).

Generally speaking, fragmentation can be seen as the first step of the polymerization process where the accumulated polymer causes the rupture of the local catalyst support material.<sup>11</sup> More specifically, the accumulation of mechanical stresses on the walls of the pores of the catalyst particles causes the fragmentation (see Scheme 2). The mechanism of particle break-up and the evolution of the internal morphology are the result of a trade-off between the rate of polymerization (rate of stress generation), the structural arrangement of the catalyst particle (distribution and structure of the pores) and the polymer properties at the point of stress. As an example, the  $\text{MgCl}_2$  support used in the Ziegler–Natta catalysts has been shown to be more friable compared to the silica support,<sup>20–23</sup> resulting in a faster fragmentation process.

From the experimental point-of-view, it is rather difficult to track the early stages of fragmentation. Recently, a combination of X-Ray ptychography and fluorescence nano-tomography has been used to get a 3D-spatial resolution of titanium atoms (Ziegler–Natta catalyst family) involved in the early stage of olefin polymerization.<sup>24</sup> The authors revealed a coexistence of different mechanisms, involving the core of the particle and the



Scheme 1 Industrial flow-chart process of a typical fourth-generation plant for polyethylene polymerization.



diffusion of monomers thought it, which contribute to the fragmentation process.<sup>25</sup>

To the best of our knowledge, a description at the molecular level (~10 nm, the typical length-scale of atomistic modelling) and a fundamental understanding of the interfacial phenomena controlling the early stage of fragmentation is still missing from the scientific literature of heterogeneous catalysis.

As for microscopic modelling, most of the molecular mechanics and quantum chemical studies in the field of Ziegler–Natta catalysis focus on the nature and properties of Ti-species: active site formation and the energetic pathways of the polymerization reaction,<sup>26–34</sup> and understanding of the role of Lewis bases in the support morphology and active site polymerization behaviour, as well as in the MgCl<sub>2</sub> surface morphology.<sup>35,36</sup> On the other hand, macroscopic modelling approaches focus on the selection of the operation conditions of reactors to perform optimization studies.<sup>5,17–19,37–44</sup> There are two examples of this class of modeling approaches: Polymer Flow (PF) models are a typical example of modeling aimed to predict the final polymer properties like MWD, CCD and reaction rate;<sup>8,45</sup> morphology models (MF) based on experimental information, like porometer data,<sup>17–19</sup> are used to describe how the fragmentation takes place during the polymerization reaction.<sup>17,40,41,45,46</sup> However, though they can well describe the fragmentation mechanism, they are not predictive “*a priori*”

because experimental morphology information is needed at different stages of the process. Moreover, a connection between microscopic atomic and macroscopic modeling approaches is still missing. A full integration of these two classes of approaches is amenable, because this would be a powerful tool to gain a fundamental understanding of the phenomena involved in the polymerization process.

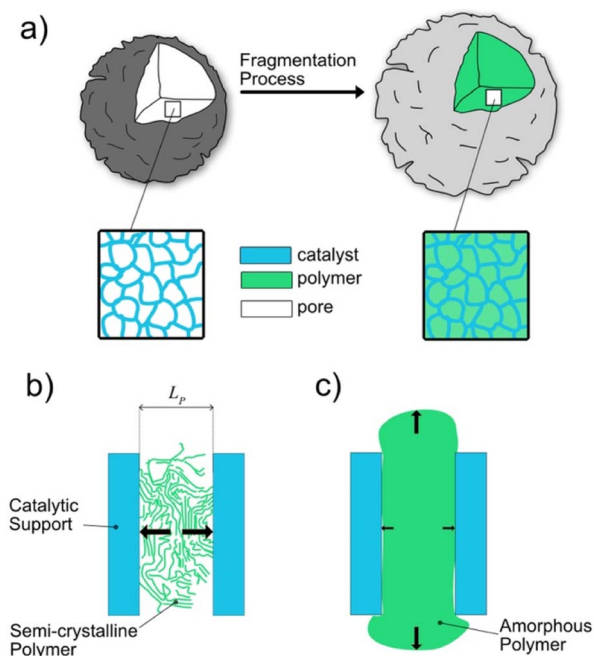
Herein, we provide an unprecedented contribution to the field by linking the morphologies of particles obtained under different conditions to the stress generation mechanism at the polymer/catalyst wall interface by combining experimental characterization and atomistic molecular dynamics (MD) simulations. The paper is organized as follows: in the Results section, a systematic investigation of experimental conditions leading to a certain particle morphology, and hence to a final polymer with specific characteristics, is discussed. The modelling strategy, purposely designed to investigate the stress generation at the atomic level, is then reported and discussed. Effect of crystallinity of PE and then of additives on the stress generation is evaluated through MD simulations and compared with experiments. Finally, in the Conclusion section the main results are summarized. Both, experimental and computational methods are briefly reported in the Experimental method section.

## Results

### Polymer particle morphologies produced under different conditions

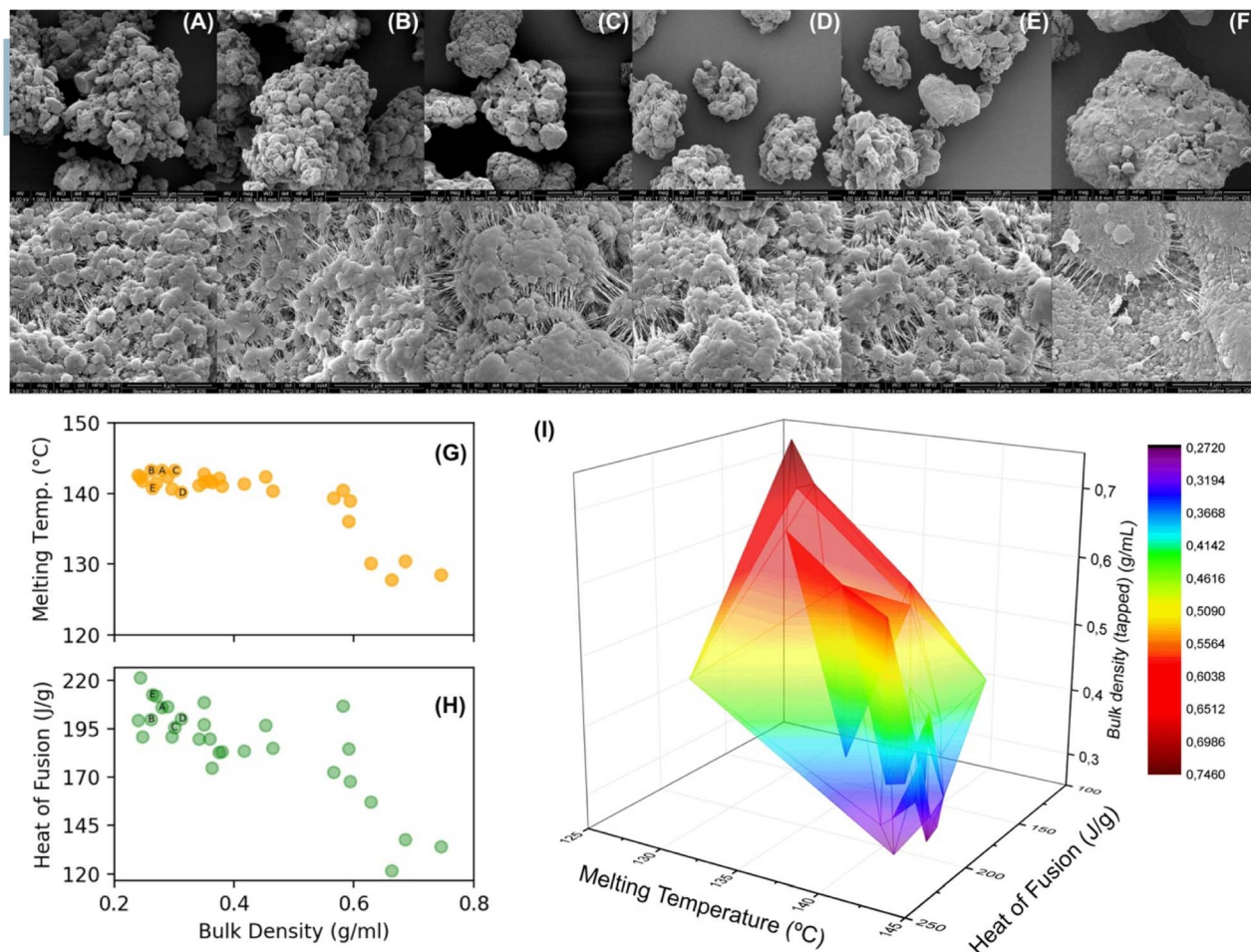
Since the particle morphology is a direct consequence of the fragmentation pattern,<sup>8,11,47,48</sup> we have experimentally investigated the morphologies obtained under a relatively broad range of conditions. In Fig. 1 a series of SEM images are shown for PE samples produced with a MgCl<sub>2</sub> supported catalyst at different temperatures (from 313 K to 353 K), or with different compositions (samples B and C: at the same temperature 323 K and different monomer (C<sub>2</sub>) concentrations; sample D: at 323 K with H<sub>2</sub>; sample F: at 343 K with comonomer (C<sub>6</sub>)). SEM images show minor but important differences between all morphologies. For instance, the samples A and E, at 313 and 353 K respectively, show significant differences in the surface roughness. While for the samples A–C the differences in terms of roughness are minor, sample F exhibits a smoother surface, and samples D and E are comparable. An empirical correlation between the particle morphology and the nascent polymer properties can be gained by linking the bulk density with the heat of fusion and the melting temperature of the nascent polymer (collected by DSC during the first heating scan).

In Fig. 1H–I, a dataset of melting temperature, heat of fusion and bulk density is reported. From this figure it is clear that high heats of fusion and melting temperatures correspond to a low bulk density indicating a high degree of crystallinity of the nascent polymer. Keeping constant the temperature of polymerization, the addition of a third component, like H<sub>2</sub>, or a higher C<sub>2</sub> concentration, alters the physical state of the produced polymer. This effect can be seen by comparing the samples B and D (see the samples labelled with B and D in the panels G and H of Fig. 1). Both are produced at 323 K, with the



**Scheme 2** (a) Schematic representation of the fragmentation process. On the left a particle with no active polymerization reaction is shown. When the polymerization takes place, from the catalyst surface, the polymer starts to fill the pore more and more. The stress is accumulated up to fragmentation (particle on the right). Limiting scenarios for the catalytic support fragmentation proposed by McKenna: (b) crystalline polymer cannot flow out of pores and large stress is accumulated on the walls (black arrows). (c) Amorphous polymer flowing out (most of the stress is released laterally, black arrows). A bi-dimensional finite pore is considered for simplicity.<sup>11</sup>





**Fig. 1** SEM images of polyethylene samples (panels A–F) produced under different temperature conditions (A: 313 K, B and C: 323 K, D: 323 K and H<sub>2</sub>, E: 353 K, F: 343 K and C<sub>6</sub>), and/or with different compositions (B and C: different C<sub>2</sub> concentrations; D: with H<sub>2</sub>). Top: 1000 $\times$ ; bottom: 300 00 $\times$ ). Melting temperature (G) and heat of fusion (H) of the produced polymer as a function of the bulk density. The DSC technique has been used to measure the melting temperature and heat of fusion of the polymer (first heating scan). (I) 3D plot correlating the bulk density and both the properties of the polymer produced, heat of fusion (crystallinity degree of PE) and melting temperature (lamella dimension).

difference that sample B contains only C<sub>2</sub>, and sample D is produced in the presence of H<sub>2</sub>.

In particular, the addition of hydrogen reduces the lamellar length leading to a polymer with a lower melting temperature and higher bulk density. More in general, a low melting temperature leads to a high bulk density. The reported empirical correlations agree with the two extreme scenarios proposed by McKenna.<sup>11</sup> In his hypothesis the particle morphology is controlled by the physical state of the nascent polymer.

In Scheme 2, a representation of the fragmentation process is provided. Cartoons showing particles before and after the polymerization reaction are compared in Scheme 2a. While in Scheme 2b and c, both scenarios hypothesized by McKenna for the stress generation mechanism are depicted. Depending on experimental conditions, the nascent polymer can be in the semicrystalline or amorphous state. In the first case, local mechanical stress starts to accumulate quickly on catalyst walls since when the nascent polymer just covers the pore dimension  $L_p$  (see Scheme 2b). Due to the rigidity of crystal domains the accumulated stress is not released, causing a rapid fragmentation of the catalyst walls with

a consequential lowering of the bulk density. This scenario is compatible with a polymer morphology reported in Fig. 1A in which the nascent polymer has a high overall crystallinity. In contrast, if the polymer is in the amorphous state, or possesses a low crystallinity, the stress is released by the polymer squeezing out from the pore (Scheme 2c and panel E of Fig. 1).

### Molecular dynamics simulations

The MD technique is used to study PE semi-crystalline or amorphous phases in contact with the MgCl<sub>2</sub> surface (the inert crystalline support of the Ziegler–Natta catalyst). The adopted detailed atomistic models allow the chemical structures of species, the composition, and physical states of the systems (semicrystalline or amorphous, temperature conditions, presence of additives, *etc.*) to be connected to their thermodynamic properties. We designed two systems representing the extreme scenarios discussed above. We aimed to study the phenomena occurring at the interface between the MgCl<sub>2</sub> surface and amorphous or semi-crystalline phases of PE.



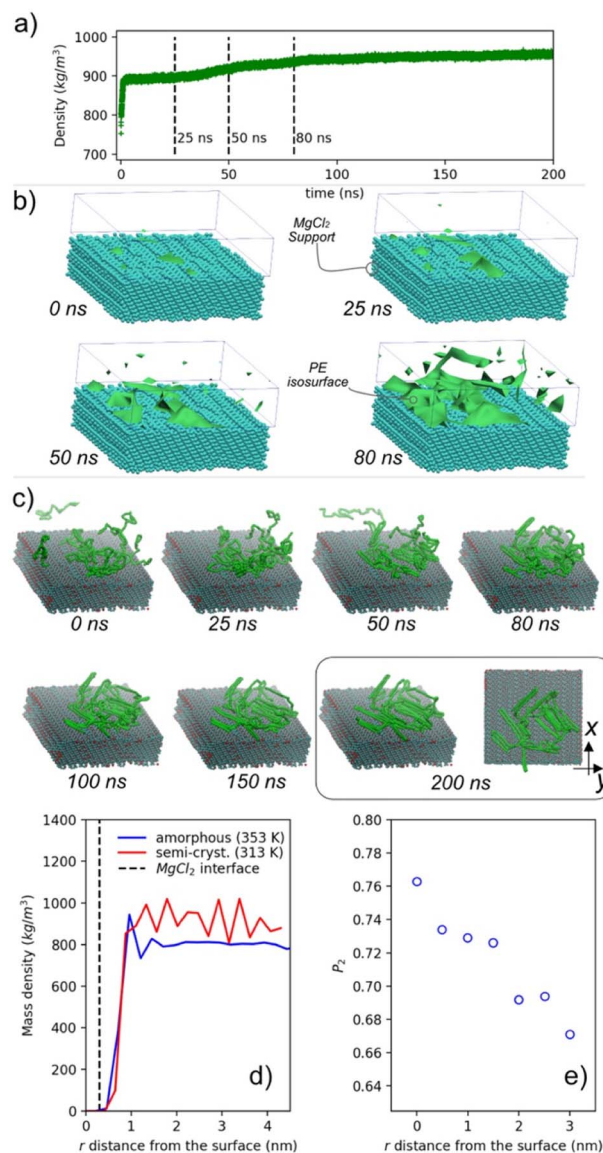
### Crystallization of PE at the interface with MgCl<sub>2</sub>: structural properties and crystalline domain stability

The crystalline phase of PE is obtained by using the TraPPE-UA (transferable potentials for phase equilibria, united atom) force-field, developed by Siepmann<sup>49</sup> and parameterized to match the equilibrium properties of linear and branched alkanes and for different properties relevant to the present study. In addition to the PE model, an atomistic model of an MgCl<sub>2</sub> crystal surface is employed. A detailed description of the models and of their validations are reported in the Method and ESI sections.<sup>†</sup> In the following, we report MD simulations of PE/MgCl<sub>2</sub> interfaces and interphases of systems composed of 111 PE chains in contact with the surface (110) of MgCl<sub>2</sub>.

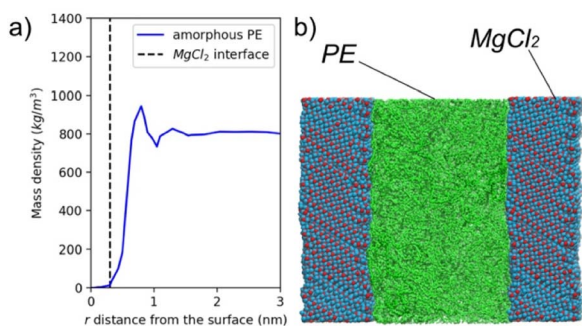
The amorphous PE, simulated at 500 K, shows a significant structuration at the interface with MgCl<sub>2</sub>, due to the presence of a solid surface (Fig. 2a). In particular, the PE mass density profile averaged by collecting atomic positions shows a maximum value at  $\sim 0.6$  nm from the surface, corresponding to an increase of 20% of mass density with respect to the bulk value of  $780 \text{ kg m}^{-3}$ . The highest peak is at a distance roughly equal to the close contact distance between PE atoms and the crystalline surface (*i.e.* sum of the van der Waals radii of the CH<sub>2</sub> group and Mg and Cl atoms, see the ESI<sup>†</sup> for the model parameters). After some further structuring (an oscillation weaker than the previous first peak), at a distance beyond 1.5 nm, the density attains an average almost constant value equal to the bulk one. Similar density profiles were observed in several computational studies on confined systems by investigating the polymer/solid interfaces with either atomistic<sup>50–52</sup> or coarse-grained models.<sup>53,54</sup> The behavior of density of a liquid phase confined between walls is mainly determined by the entropic effect, moreover net attractive interactions between the liquid phase and the wall can contribute to its enhancement.<sup>55</sup>

Fig. 3a shows the mass density temporal evolution of PE during the quenching procedure (from 500 to 280 K). It can be observed that after  $\sim 25$  ns of induction time, there is a sudden increase of the density, which reaches, at the end, a plateau of about  $946 \text{ kg m}^{-3}$ . The observed trend is typical of a first order liquid–solid transition. In the time interval 25–100 ns, density

fluctuations promote the nucleation and the growth of crystal domains. A more detailed picture of crystalline domain formation can be gained by having a look at the sequence of density isosurfaces shown in Fig. 3b. The reported isosurfaces,



**Fig. 3** (a) Temporal variation of PE mass density, for the system PE in contact with a crystalline slab of MgCl<sub>2</sub>, during the first 100 ns of the fast quenching procedure. (b) Density isosurfaces of PE (in green) at different stages of simulation. The MgCl<sub>2</sub> bead support is reported together with the isosurfaces. (c) Snapshot sequence of selected chains. Selected chains belong to spatial regions with a mass density 1.3 times larger than the average density of the last configuration. (d) Mass density profiles of amorphous (blue line) and semi-crystalline (red line) phases of PE in contact with a crystalline slab of MgCl<sub>2</sub> (black discontinuous line). Profiles in panels (d) and (e) are calculated in the direction normal to the MgCl<sub>2</sub> surface and time averaged over the last 50 ns of NPT production runs. (e) Orientational order parameter  $P_2$  as a function of the distance  $r$  from the surface. The final configuration has a degree of crystallinity of  $\sim 68\%$ , like those obtained from the homogeneous melt using the same quenching procedure (see the ESI<sup>†</sup> for further details).



**Fig. 2** (a) Mass density profile calculated for a system composed of PE chains in contact with the (110) surface of a crystalline slab of MgCl<sub>2</sub> at a  $T = 500$  K. (b) Next to the plot, a snapshot representing the equilibrium state is reported. The PE polymer chains are in green, while the magnesium and chlorine atoms are in red and cyan, respectively.



computed at different times of crystalline domain formation, represent spatial regions where the PE density is 1.3 times larger than the average density of the last semicrystalline configuration. The presence of a source of heterogeneities, in our case the interface with the  $\text{MgCl}_2$  surface, induces the crystallization of PE. This is a well-known effect used in many technological applications.<sup>56–60</sup> We observe a typical case of heterogeneous nucleation in which regions with higher probability of nucleation (higher PE density) are found at the  $\text{MgCl}_2$  surface, see the isosurfaces at 25, 50 and 80 ns in Fig. 3b. The effect of unidimensional confinement in the crystallization process has been computationally studied, *via* MD or MC (Monte Carlo), for a variety of polymers and substrates.<sup>61–67</sup> In particular, Frenkel *et al.* investigated the structure and free energy landscape of a semiflexible lattice polymer during the crystallization occurring in the presence of an interface.<sup>61</sup> More recently, Yamamoto has shown that even the fast crystallization obtained in computer modelling can reproduce morphologies and lamellae orientation in agreement with those experimentally observed from ultrafast undercooling of a PE melt.<sup>64</sup> Rutledge and co-workers deeply studied the crystallization of PE under several conditions,<sup>68–72</sup> focusing on the nucleation at the crystalline/melt interface.<sup>73</sup>

The typical lamellar morphology starts to appear after about 10 ns, reaching in  $\sim 200$  ns a well-defined structuration. A snapshot sequence of PE crystalline domain formation is shown in Fig. S13.† Lateral and top views of the snapshot at 200 ns show a disordered orientation of the lamellae with respect to the  $\text{MgCl}_2$  surface. In Fig. 3c, the conformations assumed by a selection of representative PE chains, in contact with the  $\text{MgCl}_2$  surface, are reported at different stages of the crystallization. At the starting time ( $t = 0$  ns), chain segments in contact with the  $\text{MgCl}_2$  surface start to order themselves forming a crystalline stem (nucleus). Then, the addition/formation of further crystalline stems leads to a growth of the initial nucleus (see the snapshot sequence at 25, 50, 80 and 200 ns in Fig. 3c). In experiments, it has been observed that a confined environment contributes to modifying the growth and crystal orientation.<sup>59</sup> In particular, the crystal domain orientation depends on both the polymer film thickness and polymer/substrate interactions.<sup>74,75</sup> A thin film of the order of 100 nm shows a preferential parallel orientation of lamellae with respect to the substrate, while ultrathin films,  $<100$  nm but higher than the average random coil chain size can induce both edge-on (perpendicular) or flat-on (parallel) orientation of the lamellae with respect to the substrate. In a quasi-two dimensional ultrathin film, where the thickness approaches the average size of random coil chains, the observed crystalline morphologies have low orientation, resembling seaweed and dendrites.<sup>76,77</sup> Typical examples are reported for PET,<sup>78</sup> PEO<sup>75</sup> and PE.<sup>79</sup> In our simulated systems we found, in agreement with experimental observations, both parallel and perpendicular orientations of lamellar domains.

The stability and structural properties of both systems have been tested at 353 and 313 K, respectively. In Fig. 3d, the mass density profiles of amorphous and semi-crystalline PE in contact with  $\text{MgCl}_2$  are reported. The profiles unveil the

different polymer structuration at the interface. Specifically, the semi-crystalline phase of PE exhibits a series of regularly spaced peaks showing long range order typical of a semicrystalline phase. Conversely, for the amorphous PE only a short distance order (up to  $\sim 2$  nm from the interface) is preserved. The relatively long-order structuration of semi-crystalline PE is further confirmed by the orientational order parameter ( $P_2$ ) calculated as a function of the distance from the  $\text{MgCl}_2$  surface, Fig. 3e. see Section 1.3 of ESI† for the definition of  $P_2$ . The highest  $P_2$  value ( $\sim 0.76$ ) is found at the highest density peak. However, the  $P_2$  is considerably high ( $\sim 0.66$ ) even at  $\sim 3$  nm from the surface. We expect that the different mobilities of the amorphous and crystalline phases, which affects the stress accumulation mechanism, is a physical behaviour that can be represented by atomistic simulations.

### Molecular view of the stress generation mechanism

Molecular simulations, beside structural properties, give access to the thermodynamics of the simulated systems. The pressure  $P$  can be directly calculated from MD simulations by the virial theorem of Clausius (eqn (1)), where the virial is defined as the product of the particle position vectors and forces acting on them (eqn (2)):

$$PV = Nk_B T + \langle W \rangle \quad (1)$$

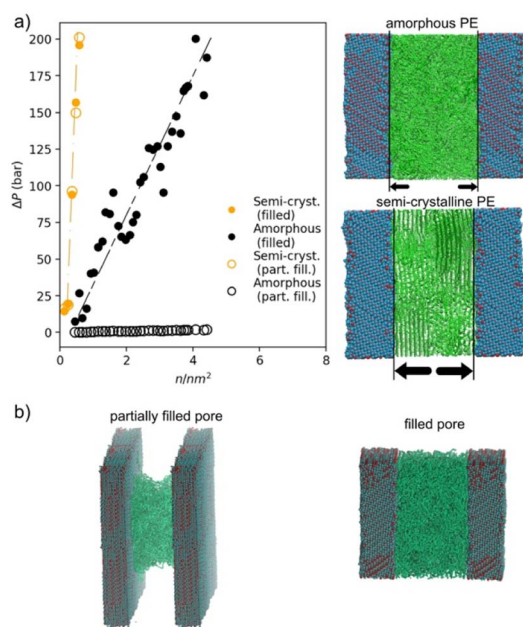
$$W = \frac{1}{3} \sum_i^N \mathbf{r}_i \mathbf{f}_i \quad (2)$$

where  $Nk_B T$  is the ideal term coming from the kinetic energy of the particles and  $W$  is the excess term coming from specific interactions among the simulated particles (in eqn (2),  $\mathbf{r}_i$  is the position of atom  $i$ , and  $\mathbf{f}_i$  is the force acting on atom  $i$  exerted by all other atoms bonded and non-bonded forces contributing as scalar product to the virial). From the definition of the kinetic energy and of the virial it is also possible to calculate separately the pressure tensor term along specific directions. In the following, the pressure component perpendicular to the wall/polymer interface is considered. MD simulations of the flowing amorphous phase and non-flowing semicrystalline phase in contact with  $\text{MgCl}_2$  have been performed to register the pressure increase as a consequence of the increment of inserted monomers per unit area (see Scheme 2b and c). In particular, the effect of the increment of monomer number is obtained by reducing the volume of the box by gradually shrinking the box length in the direction perpendicular to the  $\text{MgCl}_2$  surface, while the other two lengths parallel to the surface are unchanged. Then, the pressure increase defined as the difference between actual pressure and the one calculated at equilibrium density ( $\Delta P$ , see definition and more details in Section 1.4 of ESI†) is recorded as a function of the number of inserted monomers per unit area as reported in Fig. 4a. A first set of simulations is performed to model the two limiting scenarios of McKenna in which different flowabilities of totally amorphous or semicrystalline phases determine the stress release or its accumulation, respectively. In the case of amorphous phase models, chains can freely flow out of the pore (Fig. 4b) which



corresponds to a very flat behavior of pressure increase (unfilled black circles in Fig. 4a). In contrast, for the semicrystalline case (open orange circles, Fig. 4a), small increases of the inserted monomers ( $\sim 0.5 \text{ n nm}^{-2}$ ) cause large  $\Delta P$  increases. Indeed, the almost incompressible crystal domains prohibit the flow of the polymer, generating stress accumulation perpendicularly to the surface. A significant difference was found between the amorphous and semicrystalline phases. These simulation results confirm the hypothesis of McKenna indicating that in the semicrystalline case a quick stress accumulation can cause a fast particle fragmentation (experimentally trackable with a lower bulk density of the particle). We can consider an additional situation studying the  $\Delta P$  behavior in the case of “filled pores”. The “filled pores” can be modelled by changing the periodic boundary condition (PBC) treatment (see Fig. 4b). For the semicrystalline case we observe the same  $\Delta P$  increase as for the partially filled pore, orange circle in Fig. 4a. This means that, as expected, the non-flowability of the semicrystalline phase is the dominant factor causing the  $\Delta P$  increase. For the amorphous phase we observe a higher  $\Delta P$  rise in the case of the filled pore rather than the partially filled pore (black circles in Fig. 4a). However, the  $\Delta P$  increase is for both cases of amorphous PE lower than that those of the semicrystalline phase.

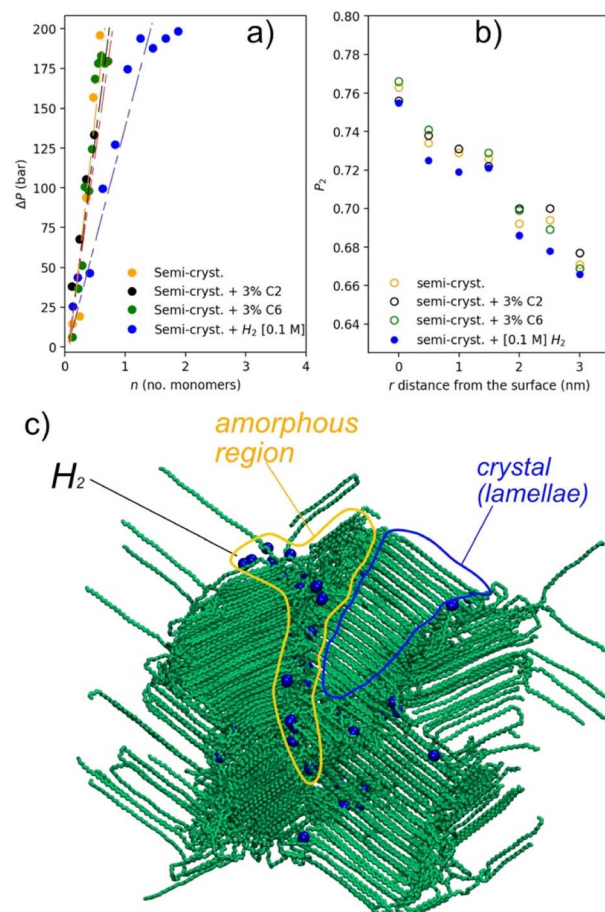
Because the PE is industrially produced in the presence of additives, we investigated how a load of low MW molecules (including  $\text{H}_2$ ,  $\text{C}_2$  and  $\text{C}_6$ ) alters the  $\Delta P$  response in the case of



**Fig. 4** (a) Pressure increases ( $\Delta P$ ) of amorphous and semi-crystalline PE in contact with the  $\text{MgCl}_2$  110 surface as a function of the number of inserted monomers number per unit area. On the left side of the same panel, a scheme illustrating the interfaces at which the pressure increase is generated is reported.  $\Delta P$  is calculated as the difference between the pressure after insertion of a monomer and the equilibrium pressure (1 bar) in the absence of monomer insertion. (b) Snapshots illustrating the partially filled (left side) and filled pore (right side), in the filled pore models the periodicity of the simulation box is set to avoid any polymer vacuum interface (the polymer atoms on the upper side interact with those on the lower side).

a semi-crystalline PE (see Fig. 5). The amorphous case is not considered since the  $\Delta P$  increment is very low (Fig. 4a, open black circles).

This is a crucial aspect to explore since the final properties of the produced polymer are controlled in the industrial processes by regulating the load of reactants.<sup>4</sup> The MD simulations revealed a significant difference between the behavior of PE with a load of  $[0.1 \text{ M}] \text{ H}_2$  and all the remaining samples (with 3% w/w of  $\text{C}_2$  and with 3% w/w of  $\text{C}_6$ ). Only in the case of hydrogen load, the increase of pressure is slower than that in the semi-crystalline case (see blue points in Fig. 5a). Conversely, for the other simulated systems the pressure increase is almost unchanged by addition of  $\text{C}_2$  or  $\text{C}_6$ . It is well expected that the increase of the  $\text{C}_2$  concentration will lead to an increase of the catalyst activity. However, the morphology and the crystallinity of the nascent polymers are comparable, as can be seen by comparing samples 1 and 2 in Table S3,<sup>†</sup> and panels B and C of Fig. 1. Even if the polymer chains are growing at a much faster rate, the fragmentation pattern is practically unchanged (similar bulk densities, high surface roughness, leading to no particle



**Fig. 5** (a)  $\Delta P$  increases for: semi-crystalline pure system (orange points), with a load of  $[0.1 \text{ M}] \text{ H}_2$  (blue points), with a load of 3% of  $\text{C}_2$  (black points) and with a load of  $\text{C}_6$  3% (green points). (b)  $P_2$  order parameter calculated in the direction normal to the  $\text{MgCl}_2$  surface. (c) Snapshot of semi-crystalline PE in contact with  $\text{MgCl}_2$  with a load of  $0.1 \text{ M}$  of  $\text{H}_2$ . Amorphous and crystal domains are identified by a contour to highlight the different distributions of hydrogen atoms in the polymer matrix.



flowability). This behavior is well predicted by our simulation results, showing a negligible difference in the  $\Delta P$  increase when  $C_2$  is added to the PE bulk (Fig. 5a).

In contrast, if a tiny amount of  $H_2$  is added, namely a few ppm, the influence on the morphology is immediately observed (higher bulk density and the powder flows) resulting in enhanced reactor operability and acceptable flowability. By adding  $H_2$  it is well known that the molecular weight of the polymer chains will be shifted to lower chain lengths, while the polymerization rate should not be considerably affected.<sup>80</sup> Consequently, it is further expected that the lower MW would affect crystallization behaviour; however, this is not applicable to the nascent polymer (the increase of crystallinity due to the lower MW will be seen only after melting and re-crystallization). Under the selected polymerization conditions ( $T = 323$  K), the chains start crystallizing before being terminated. In the presence of  $H_2$  the nascent polymer exhibits less long-range order, *i.e.* shorter lamellae, than the polymer produced only with  $C_2$ , as indicated by the lower melting temperature ( $T_{m1}$  first melting point) when comparing samples 2 and 3 in Table S3 of ESI.† A similar trend is also found from MD simulations. In fact, the  $P_2$  order parameter, calculated as a function of the distance from the interface with the support wall, indicates a lower  $P_2$  value for the system loaded with hydrogen (Fig. 5b). Simulation results suggested that  $H_2$  acts as a plasticizer, thus partially increasing the polymer mobility and the possibility of stress release. At the molecular level, the hydrogen molecules, mainly located in the amorphous regions of the semicrystalline model (see the snapshots in Fig. 5c), contribute to enhancing the mobility of the amorphous regions. In practice the hydrogen molecules increase the free volume between polymer chains letting them move and rotate more freely. The increase of the bulk density is a consequence of the improved chain mobility, leading to more efficient expansion/filling of the available pore volume and a smoother increase of stress on the support walls. Interestingly, simulation indicates that the same plasticizing effect is not found in the presence of a comonomer. Indeed, although by adding a comonomer ( $C_6$  or  $C_4$ ) there is again a reduction of the MW and of the crystallinity (this time both in the nascent and in the recrystallized polymer) and the particle morphology improves (see Fig. 1F), only a minor change of the pressure behaviour is calculated. The higher amount of amorphous phase produced when the comonomer is present, indicated by the lower  $\Delta H_1$ , for example when comparing samples 2 and 4 in Table S3 of ESI,† is contributing to the higher bulk density. The effect is noticeable already at very low comonomer concentration values. At higher concentrations, when incorporation of defects inhibits more the *in situ* crystallization, much higher bulk densities can be achieved (Fig. 1H) because of the high content of amorphous phase. *Vice versa*, by dosing only  $H_2$ , a crystalline material is always produced, and the bulk density will be lower.

## Conclusions

A systematic study, connecting the morphology of particles obtained under different polymerization conditions and the possible different stress generation mechanisms at the PE/MgCl<sub>2</sub> support interface, has been presented. In particular,

experimental characterization of the particles in terms of microscopy, heat of fusion, melting temperature and bulk density of the polymer produced under different pre-polymerization conditions has been compared with pressure increases perpendicular to the PE/MgCl<sub>2</sub> interface calculated by atomistic MD under the same conditions.

Two limiting scenarios, corresponding to the McKenna hypothesis, in which different flowabilities of totally amorphous or semicrystalline PE phases have been considered. In the case of amorphous PE phases, very flat behaviors of pressure increases have been calculated. In contrast, for all considered models, in the presence of semicrystalline PE phases, a steep behavior of pressure increase as a function of inserted monomers has been registered. Crystallinity of the nascent PE phase is confirmed as a dominant factor in the stress mechanism generation.

Atomistic MD simulations allowed a straightforward extension to models where additives are present. In particular, a load of low MW molecules such as  $H_2$ ,  $C_2$  and  $C_6$  has been considered for the simulation of stress behavior for both semicrystalline and amorphous PE phases. Interestingly, in agreement with experiments, hydrogen molecules alter the  $\Delta P$  response in the case of a semi-crystalline PE, while, in the same case,  $C_2$  and  $C_6$  do not alter the stress behavior. These results open the possibility, employing the proposed models, of a systematic investigation and rational design of reactants composition. More in general, the proposed approach, focused on a length-scale ( $\sim 10$  nm) intermediate between microscopic and macroscopic modelling of the polymerization process, can open the way to a fruitful bridging of modelling, experiments, and product design.

## Experimental methods

### SEM/EDS

Prepolymerised catalyst samples are analysed using a FEI Quanta 200F Scanning Electron Microscope (SEM) equipped with an Energy Dispersive Spectrometer (EDS). In this method, the pre-polymerised catalyst particles are cut with a microtome blade and attached to a sample holder with a carbon conductive adhesive. The cut specimens are sputter coated with Pd/Au in a Polaron sputter coater to make them conductive.

### Bulk density

For the bulk density measurement a 100 mL cylinder is placed on the balance and tared. Afterwards the cylinder is positioned concentric under the funnel. The funnel is closed by turning the fastener plate. Then the granules or powder is filled quickly in the closed funnel. After the filling the fastener plate is opened. The overrun of the sample above the upper edge of the cylinder is wiped off in a 45° angle with a straight-sharp-edged corner. The cylinder filled with the sample is reweighed to calculate the weight. This determination is performed two times. Resulting weight [ $g \ 100 \text{ mL}^{-1}$ ]  $\times 10 =$  bulk density [ $\text{kg m}^{-3}$ ]. The result is given as the arithmetic mean of the double determination.



## DSC

A TA Instruments Q2000 Differential Scanning Calorimeter calibrated with indium, zinc, and tin and operating under 50 mL min<sup>-1</sup> of nitrogen flow was used. The employed thermal program consisted of a first heating step from 0 to 453 K, followed by a cooling step and a second heating scan from 0 to 423 K. The heating/cooling rate was always 10 K min<sup>-1</sup>. The DSC trace was integrated from 303 K to the end of the melting peak to evaluate the melting enthalpy.

## Computational methods and details

TraPPE-UA has been demonstrated to better reproduce, against experiments, the mass density, thermal expansion coefficient, gyration radius of PE chains, diffusion coefficient, and the early stage of crystallization of an entangled PE without the use of a pre-oriented amorphous melt,<sup>81,82</sup> needed in the case of the PYS force-field.<sup>71</sup> We choose a PE chain of C<sub>150</sub>H<sub>300</sub> (from now C<sub>150</sub>) since it is long enough to display chains folded (lamellae) in the crystal domains.<sup>83</sup> In Section 1 of ESI,† a description and a validation (where needed) of all models used in this paper are reported. In the same section, a procedure to build a stable crystal slab of (110) cut of MgCl<sub>2</sub>, considered in the current literature as the most representative surface for the polymerization reaction,<sup>84,85</sup> is reported. Moreover, since we are going to perform simulations under conditions close to experimental ones, the thermal stability of the crystal slab is also checked (see Section 1.5 of ESI†). The initial well equilibrated PE bulk configuration has been obtained, using the hybrid particle-field approach,<sup>86,87</sup> by following the procedure reported by De Nicola *et al.*,<sup>88,89</sup> and using the OCCAM MD package.<sup>90</sup>

## Conflicts of interest

There are no conflicts to declare.

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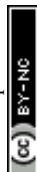
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