REVIEW

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Solution NMR methods for structural and thermodynamic investigation of nanoparticle adsorption equilibria

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Characterization of dynamic processes occurring at the nanoparticle (NP) surface is crucial for developing new and more efficient NP catalysts and materials. Thus, a vast amount of research has been dedicated to developing techniques to characterize sorption equilibria. Over recent years, solution NMR spectroscopy has emerged as a preferred tool for investigating ligand–NP interactions. Indeed, due to its ability to probe exchange dynamics over a wide range of timescales with atomic resolution, solution NMR can provide structural, kinetic, and thermodynamic information on sorption equilibria involving multiple adsorbed species and intermediate states. In this contribution, we review solution NMR methods for characterizing ligand–NP interactions, and provide examples of practical applications using these methods as standalone techniques. In addition, we illustrate how the integrated analysis of several NMR datasets was employed to elucidate the role played by support–substrate interactions in mediating the phenol hydrogenation reaction catalyzed by ceria-supported Pd nanoparticles.

Introduction

Nanoparticle (NP) catalysts have found many applications in numerous fields such as energy,[1,2] petrochemical,[3,4] and medicine,[5,6] due to their high surface-area-to-volume ratio and size-dependent properties that make them highly efficient and tunable catalysts. Since sorption equilibria play an essential role in determining the efficiency and selectivity of NP catalysis, many analytical techniques have been utilized to characterize ligand–NP surface interactions, including ultraviolet-visible (UV/Vis) spectroscopy,[7-10] fluorescence,[11,12] vibrational spectroscopy,[11-13] and isothermal titration calorimetry (ITC).[14] However, the outcomes of these analytical methods are generally dependent on the specific system under investigation and experimental conditions. In recent years, solution NMR spectroscopy has emerged as a preferred tool to investigate the interaction between the substrate and the NP surface. Indeed, due to its ability to probe dynamic processes occurring over a wide range of timescales (ps to hours), NMR spectroscopy is applicable to a broad range of NP–ligand pairs. In addition, the ability of NMR to provide data with atomic resolution allows a comprehensive characterization of the NP–substrate interaction, returning structural, kinetic, and thermodynamic information on the sorption equilibrium.

This contribution gives a brief overview of non-NMR techniques to investigate small molecule–NP interactions and the types of information these approaches can provide. In addition, we review solution NMR methods commonly employed in the characterization of small molecule–NP interactions, and we provide examples of their applications to various ligand–NP systems. Finally, we discuss how the combined analysis of multiple solution NMR methods was used to characterize the contribution of substrate–support interactions toward the hydrogenation of phenolic compounds catalyzed by ceria-supported palladium (Pd/CeO$_2$) NPs.

Langmuir's theory

Experimental data on ligand–NP interactions are commonly analyzed within the framework of Langmuir's theory.[15-17] The Langmuir model relies on four primary assumptions: (i) the adsorbent surface is homogeneous, (ii) each binding site can only hold one adsorbent molecule (*i.e.* monolayer coverage), (iii) adsorbed molecules do not interact with one another, and (iv) the adsorption process is reversible. Although modified models that address the limitations introduced by such assumptions were proposed,[18-21] the original Langmuir isotherm model is, so far, the most common approach for modelling sorption equilibria.

The interaction between a ligand (L) and a vacant binding site on the surface (S) to form an adsorbed species (LS) can be represented in the form of a chemical equation:

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$$\mathrm{L} + \mathrm{S} \underset{k_{\mathrm{des}}}{\overset{k_{\mathrm{ads}}}{\rightleftharpoons}} \mathrm{LS} \qquad (1)$$

where k_{ads} and k_{des} are the rate constants for adsorption and desorption, respectively. However, while for a typical equilibrium process, the equilibrium constant (K_{eq}) is derived as the ratio between the concentrations of products and reactants (*i.e.* $K_{\mathrm{eq}} = \frac{[\mathrm{LS}]}{[\mathrm{L}][\mathrm{S}]}$ for eqn (1)), for a surface sorption equilibrium in the Langmuir model, the concentration of binding sites is generally unknown and has to be part of the equation. The fraction of surface binding sites occupied by ligands is defined as the surface coverage (θ):

$$\theta = \frac{g_{\mathrm{LS}}}{g_{\mathrm{max}}} \qquad (2)$$

where g_{LS} is the grams of adsorbed ligand per gram of adsorbent and g_{max} is the maximum adsorption capacity (in grams) that corresponds to the monolayer formation in the specific ligand–NP system under investigation. Therefore, the fraction of vacant sites will be expressed as $1 - \theta$.

In the original gas-phase Langmuir model, rates of adsorption (r_{ads}) and desorption (r_{des}) are derived by means of the ligand pressure (p) and the surface coverage θ ($r_{\mathrm{ads}} = k_{\mathrm{ads}}p(1 - \theta)$ and $r_{\mathrm{des}} = k_{\mathrm{des}}\theta$, respectively). However, when applied to the liquid phase systems, the ligand amount is quantified in terms of molar concentration. Taking this and the fact that at equilibrium $r_{\mathrm{ads}} = r_{\mathrm{des}}$ into account, the Langmuir isotherm model is generally represented in one of the two forms shown below:[17]

$$\theta = \frac{KC_{\mathrm{L}}}{1 + KC_{\mathrm{L}}} \qquad (3a)$$

$$q_{\mathrm{LS}} = \frac{q_{\mathrm{max}}KC_{\mathrm{L}}}{1 + KC_{\mathrm{L}}} \qquad (3b)$$

where C_{L} and q_{LS} are the concentrations of desorbed and adsorbed ligand at equilibrium, respectively, q_{max} is the maximum adsorption capacity (in mol L^{-1}), and K is the Langmuir equilibrium constant that corresponds to the inverse of the equilibrium concentration of free ligand when half of the available adsorption sites are occupied (Fig. 1). Therefore, like any equilibrium constant of an association process, the higher the value of K, the stronger the ligand–NP interaction.

In an ideal adsorption study, q_{LS} and C_{L} are measured at increasing ligand concentrations, and the experimental isotherm resulting from plotting q_{LS} *versus* C_{L} is modelled using eqn (3b) to obtain q_{max} and K (Fig. 1). Although powerful in providing information on the number of adsorption sites (q_{max}) and strength of the NP–ligand interaction (K), the latter approach suffers from several experimental limitations. Indeed, accurate modelling of q_{max} and K can only be obtained if a range of ligand concentrations can be spanned so that q_{LS} is measured at C_{L} values that are much smaller and much larger than K^{-1}. In the case where the range $C_{\mathrm{L}} \ll K^{-1}$ cannot be sampled (*i.e.* the analytical technique used to measure q_{LS} and/or C_{L} is not sensitive enough), the experimental isotherm will grow too steeply nearby $C_{\mathrm{L}} \sim K^{-1}$ to obtain an accurate estimate for the Langmuir constant (red and orange curves in Fig. 1). On the
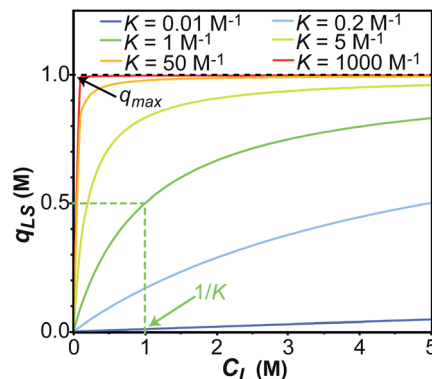

Fig. 1 Simulation of the concentration of surface adsorbed ligand (q_{LS}) *versus* concentration of free ligand (C_{L}) obtained using the Langmuir isotherm model (eqn (3)). Simulations were performed for Langmuir constants (K) of 0.01 (blue), 0.2 (light blue), 1 (green), 5 (yellow), 50 (orange), and 1000 (red) M^{-1}. The maximum surface coverage (q_{max}) was set to 1 M (black dashed line). Half occupancy of the NP surface is obtained at $C_{\mathrm{L}} = 1/K$ (shown with a green dashed line for the $K = 1$ M^{-1} simulation).

other hand, if conditions at which $C_{\mathrm{L}} \gg K^{-1}$ cannot be analyzed (*i.e.* the ligand and/or NP aggregate at a high concentration of small molecule), the experimental isotherm never reaches saturation (*i.e.* $q_{\mathrm{LS}} \sim q_{\mathrm{max}}$) and q_{max} cannot be accurately determined by modelling the experimental data (light blue and dark blue curves in Fig. 1). If the size and morphology of the investigated NP are known, the latter limitation can be circumvented by estimating q_{max} as the highest theoretical ligand density in a monolayer on the NP surface. Oftentimes, the value of K obtained by modelling adsorption data with eqn (3a) and (3b) is treated as a conventional equilibrium constant and used for the estimation of the free energy of adsorption (ΔG_{ads}) by means of the following relationship:

$$\Delta G_{\mathrm{ads}} = -RT \ln K \qquad (4)$$

where T is the temperature and R is the universal gas constant. In such cases, care must be taken to the fact that the Langmuir equilibrium constant obtained by fitting experimental adsorption data is usually not dimensionless.[22] A recent publication reviews the topic in further details and summarizes mathematical approaches to transform the Langmuir constant into a dimensionless standard equilibrium constant compatible with eqn (4).[23]

In addition to providing estimates for thermodynamic parameters, the Langmuir model can be expanded for the investigation of adsorption kinetics. Generally, adsorption of ligands to NPs is described using either a pseudo-first-order (eqn (5))[24] or a pseudo-second-order (eqn (6))[25] kinetic model:

$$\theta(t) = A(1 - e^{-k_{\mathrm{obs}}t}) \qquad (5)$$

$$q_t = \frac{q_{\mathrm{LS}}^2 k_{\mathrm{obs}} t}{1 + k_{\mathrm{obs}} q_{\mathrm{LS}} t} \qquad (6)$$

In these models, A is an empirical constant that depends on the actual values of k_{ads} and k_{des}, k_{obs} is the observed rate

constant of the corresponding pseudo-first or pseudo-second kinetic process, and q_t is the adsorbed amount of the ligand at each time point measurement. In many cases, experimental limitations require the introduction of a time delay factor (t_0) that compensates for the time gap between the addition of ligands to the system and the collection of the data. As a result, the pseudo-first-order kinetic model is more often represented by the following equation:[26,27]

$$\theta(t - t_0) = A(1 - e^{-k_{obs}(t-t_0)}) \tag{7}$$

Depending on the analytical method employed to investigate the adsorption kinetics, eqn (5)–(7) are often modified to accommodate substitution of θ with a directly measured observable.[27]

For processes that follow pseudo-first-order kinetics, an accurate determination of k_{ads} and k_{des} can be obtained if k_{obs} is determined at several concentrations of ligands ($L = C_L + q_{LS}$). Since the rate constants are connected by the linear function $k_{obs} = k_{ads}C_L + k_{des}$, the slope of the experimental k_{obs} over C_L plot provides the value of k_{ads} while the intercept with the y-axis yields k_{des}. Knowledge of the adsorption and desorption rate constants can be used to calculate the Langmuir equilibrium constant by means of the following equation:[23]

$$K = \frac{k_{ads}}{k_{des}} \tag{8}$$

Of note, the latter approach to the determination of K does not require estimation of q_{max} and is, therefore, the preferred method to obtain the Langmuir equilibrium constant for weak ligand–NP interactions.[26] However, it should be noted that eqn (8) only applies to sorption equilibria based on elementary reactions. In the case of more complex equilibria involving one or more intermediate states, the ratio of the rate constants in eqn (8) would not provide an accurate estimate of K.[23]

Overview of analytical methods for characterizing sorption equilibria

Spectroscopic analytical techniques such as UV/Vis, IR, Raman, and fluorescence are the most developed methods for studying the binding of small molecules to NP surfaces, and a large number of studies are available in the literature that use these methods to obtain a qualitative description of binding as well as the necessary parameters for quantifying adsorption *via* the Langmuir theory. In addition, a variety of other analytical methods (*i.e.* X-ray,[28,29] microscopy,[30,31] SS-NMR,[32–36] *etc.*) have been sparsely applied to specific NP–ligand systems, but they have not found a general application for the characterization of sorption dynamics.

Ultraviolet-visible (UV/Vis) spectroscopy

UV/Vis is a sensitive and cost-effective spectroscopic method for the detection and characterization of diverse analytes, ranging from small molecules[7–10] to large biopolymers.[11,12] The UV/Vis adsorption wavelength of an analyte is highly sensitive to the immediate environment, and thus, different UV/Vis absorption maxima are expected for an adsorbed ligand and for the same molecule in the bulk solution. Due to this potential ability to differentiate among adsorbed and desorbed species, UV/Vis spectroscopy has been often used as a standalone technique for detecting ligand–NP adducts and, in some instances, to obtain structural and thermodynamic information on the interaction. However, the low resolution of UV/Vis spectra exposes a major drawback of this technique that often requires separation of the desorbed and adsorbed species *via* precipitation or filtration procedures for quantitative analysis. This sample preparation step hampers the characterization of weak ligand–NP interactions by UV/Vis spectroscopy.

Systems that involve the adsorption of proteins onto NPs are generally excessively complex for conventional UV/Vis and are normally characterized by Surface Plasmon Resonance (SPR).[12] Formation of the NP–ligand conjugate results in a shifted and broadened adsorption spectrum. Since these changes are related to the concentration of bound species, SPR could yield quantitative binding parameters. Although this method is applicable to nearly any type of ligand, it is restricted to metal NPs capable of producing SPR spectra.

Quantitative analysis of binding. The most common approach to quantitative analysis of small molecule–NP systems by UV/Vis involves exposing a standard ligand solution of known concentration (L) to a known amount of NPs and monitoring the changes in the concentration of free (C_L) and surface adsorbed (q_{LS}) ligand over time. Although C_L and q_{LS} could be in principle determined directly by observing the UV/Vis signals of the free and bound small molecule, respectively, the intrinsic low-resolution of UV/Vis spectroscopy hampers a direct quantification of the two species from a single spectrum. Therefore, C_L is often determined from UV/Vis spectra measured on samples in which the adsorbed species is filtered or precipitated out of solution. The q_{LS} value can be derived indirectly by subtracting C_L from L, and the obtained data can be fit using the Langmuir adsorption model (eqn (5)–(8)) to yield the kinetics and thermodynamics of sorption. Employment of UV/Vis spectroscopy in this manner was reported for a few protein–NP and small molecule–NP systems, where the equilibrium association constant[37–41] or a range of kinetic and thermodynamic parameters[9,10,40–47] were determined.

In applications examining adsorption on noble metal NPs (generally gold), UV/Vis spectroscopy can be conveniently complemented by SPR.[48] In this hybrid method, C_L is obtained by UV/Vis as described above, while q_{LS} is measured directly by observing the changes in the SPR spectrum of the NP caused by ligand binding.

The recent interest in DNA-based nanotechnologies ignited further development in the UV/Vis-based methods for quantifying NP adsorption. In particular, a novel quantitative colorimetric approach was introduced to assess the binding strength of DNA bases and nucleosides to silver[39] and gold[38] NPs. The approach relies on following colorimetric changes induced by aggregation of NPs upon ligand binding. As it was shown that the NP aggregation rate is directly correlated to the

concentration of adsorbed ligand, C_L and q_{LS} can be obtained by the colorimetric assay.

Qualitative analysis of binding. Interpretation of UV/Vis spectral changes can also provide valuable non-quantitative information about ligand binding. Indeed, a change in peak position in the spectrum of a ligand upon the addition of NP can indicate the occurrence of ligand–NP interaction. In addition, analysis of these spectral changes in comparison to known references could return structural insight into the mode of interaction. For example, de Haan *et al.* found that the changes in the UV/Vis spectrum of alizarin in the presence of ZnO NPs are consistent with the absorbance spectrum observed for deprotonated alizarin, suggesting that alizarin binds to ZnO NPs in its deprotonated form.[8]

Fluorescence

Fluorescence spectroscopy and its variations, such as Fluorescence Correlation Spectroscopy (FCS), are convenient techniques for investigating adsorption processes due to their high intrinsic sensitivity and their ability to provide input experimental data for the Langmuir isotherm model. The fluorescence of ligands is highly sensitive to quenching by the formation of NP–ligand conjugates. Therefore, analysis of the changes in fluorescence spectra (*i.e.* intensity, broadening, a shift in emission maxima) provides qualitative, and in some cases quantitative, insight into sorption processes.

Although fluorescence was used to study the adsorption of proteins and small fluorescent molecules (dyes) onto NPs,[11,12] the need for the ligand or the NP to be either naturally fluorescent or to carry a covalently attached fluorescent label has limited its broader applicability to the study of sorption equilibria. In addition, if NPs are not removed from the solution (by filtration or centrifugation) before the fluorescence measurement is taken, they have the potential to induce inner filter and light scattering effects that complicate the analysis of the data.[49,50]

Quantitative analysis of binding. Three main fluorescence-based approaches to derive quantitative information for NP–ligand systems were described for inherently fluorescent small molecules and proteins. The Fluorescence Quenching Titration (FQT) method exploits the ability of NPs to quench the fluoresce of bound ligands. Therefore, the solution of a fluorescent ligand is titrated with NP to achieve complete quenching of the signal. Plotting the normalized fluorescence intensity over concentration of NP yields a nonlinear decay that is modelled to provide the estimated binding constant.[51] This methodology found wide application in examining both protein–NP[12] and small molecule–NP[52] interactions. In addition to estimation of binding constants, the fluorescence quenching method could serve as a tool for examining the accessible surface area. For example, the Molecular Probe Adsorption (MPA) method demonstrated the convenience of fluorescence spectroscopy for estimating the available adsorption surface in NPs containing a corona phase.[53]

The Fluorescence Correlation Spectroscopy (FCS) method provides several advantages over FQT. FCS relies on measuring variations of fluorescence produced by species that diffuse through a part of a sample that is actively monitored by a laser beam. This technique is highly sensitive and can detect exceptionally low concentrations of fluorophores, as low as nM. In addition, it does not suffer from complications that arise when measurements are performed with NPs present in the solution. Since the fluorescence of the free ligands can be measured independently from the molecules bound to NPs, the primary outcome of FCS is C_L, while q_{LS} is derived mathematically based on the measured concentration of the desorbed ligand. A well-illustrated example that studied the adsorption of fluorescent compounds rhodamine 6G and calcein on colloidal silica and alumina NPs showed the applicability of FCS to small molecule–NP systems.[54]

Finally, if the ligand and the NP of interest are not intrinsically fluorescent, a competition assay can be applied to characterize NP adsorption. This method is based on exposing the NP loaded with a surface-adsorbed fluorescent molecule to a solution of the non-fluorescent ligand. The release of the fluorescent probe from the NP surface is then monitored to determine the concentration of the non-fluorescent ligand that is adsorbed on the NP surface. The approach was demonstrated using fluorescently labeled oligonucleotides bound to gold NPs through an alkanethiol linker and mercaptoethanol as a displacing agent.[55]

Qualitative analysis of binding. Qualitative analysis of fluorescence spectra was utilized to examine surface characteristics of ligand–NP systems such as charge density,[56] functional group density,[57] dielectric constants,[57] and interfacial pH.[58] Despite the very high sensitivity of fluorescence-based techniques and their ability to provide *in situ* measurements allowing for characterization of dynamic adsorption processes, the inherent challenges (among them the requirement for the fluorescently active ligands and a complicated experimental setup) dramatically limited the extent of studies of small molecules–NP binding thus far.

Vibrational spectroscopy

Interpretation of changes in the vibrational spectra of molecules upon adsorption on a surface was shown to be a highly versatile and convenient approach to yield experimental data necessary for qualitative and quantitative analysis of surface sorption. The two primary vibrational spectroscopy techniques are Fourier-Transform Infrared (FTIR) and Raman spectroscopies. The relative simplicity of sample preparation and data collection resulted in an extensive utilization of these methods for investigating sorption equilibria.

Fourier-transform infrared (FTIR) spectroscopy

The use of FTIR to characterize ligand–NP interactions relies on the ability of IR spectroscopy to detect the establishment of new functionalities in the sample (*i.e.* a ligand–NP bond) or the spectral perturbation of an IR-active functional group within the ligand or NP upon binding.[11–13] Although the high complexity of FTIR spectra has limited their application to the characterization of small molecule–NP interactions,[59–66] the more recent introduction of Attenuated Total Reflectance Fourier Transform

Infrared (ATR-FTIR)[13,67–75] and Surface-Enhanced Infrared Absorption (SEIRA)[13,76–79] has expanded the use of IR-based methods to ligand–NP systems of higher complexity.

Quantitative analysis of binding. Qualitative assessment of capping layers and functionalization at the NP surface is the primary outcome of IR-based techniques. Nonetheless, a carefully designed experiment that includes the necessary standard calibrations could provide a quantitative description of surface coverage as well as the thermodynamic and kinetic parameters of sorption.[67] In the most common quantitative application, the time-dependent intensity change in the ATR-FTIR peaks corresponding to the adsorbed ligand is used to asses time-dependent changes in concentrations of the bound species and obtain the adsorption and desorption rate constants. This approach works best for slow adsorption processes that reach equilibrium at a slow enough rate to allow for data collection at multiple time points (typically minutes to hours), and was successfully applied to investigate the binding of small molecules on TiO_2,[80–87] iron (oxyhydr)oxides,[88] hematite,[89,90] Pt/Al_2O_3,[91] and CeO_2 NPs.[92] In some of these studies, the adsorption and kinetic data were used to derive the Langmuir equilibrium constant using eqn (8).[83–85,92]

Qualitative analysis of binding. Two-dimensional infrared spectroscopy (2D-IR)[93,94] provides a high-resolution picture of the IR-active functionality in the investigated sample and has been utilized in several qualitative investigations of surface adsorption. For example, 2D-IR spectroscopy allowed the characterization of the structure and mobility of the capping layer comprised of amide and carboxylate-containing ligands on gold NPs.[95] In another application, Bian *et al.* demonstrated the ability of multiple-mode multi-dimensional IR to obtain a complete picture of the conformations sampled by 4-mercaptophenol bound to gold NPs.[96] 2D-IR was also employed to study the conformations sampled by the tripeptide glutathione (used a capping layer) on the surface of silver NPs[97,98] and their dependency on the NP size.[97] In another example, 2D-IR was used to detect the Pt–H bond formed upon H_2 activation on Pt[99] and the aggregation of a complex organometallic dye on the surface of TiO_2 NPs.[100]

Raman spectroscopy

One of the main advantages of Raman over IR spectroscopy for the analysis of sorption equilibria is its ability to perform measurements in aqueous environments since water does not interfere with Raman spectra. However, its lower sensitivity has hampered a broader application of the technique. The more recently introduced Surface-Enhanced Raman Scattering (SERS)[101–103] overcomes the low sensitivity limitation of conventional Raman spectroscopy and, under certain circumstances, could even provide single-molecule resolution.[104–108] The number of reported studies that employ SERS to examine surface processes has been rising in the last few years, and we expect the utilization of this technique to study NP adsorption will be much broader in the near future.

Quantitative analysis of binding. There is no standard methodology for the utilization of Raman-based techniques to quantify sorption processes on NPs. However, several recent illustrations include carefully designed experimental protocols capable of providing quantitative data for the chemisorption of small molecules. Similar to the ATR-FTIR technique mentioned above, change in intensity for well-observed SERS bands of ligands interacting with NP can be plotted as a function of time and fit to a Langmuir adsorption model to result k_{obs} for the interaction, as was illustrated by adsorption of 4-aminothiophenol and 2-thio-5-nitrobenzoic acid on gold NPs.[27] One of the most comprehensive examples of SERS application to the ligand–NP system was illustrated by a very detailed investigation of the influence of surface curvature of nanotextured gold NPs on the binding of thiolated ligands.[109] In this study, a wide range of structural, kinetic, and thermodynamic data were obtained using plasmon-enhanced Raman scattering. A robust methodology for determining ligand packing density and concentrations of bound and free substrates by SERS relies on utilizing isotopically labeled versions of the ligands as internal standards. Under this protocol, SERS can deliver the equilibrium constant by fitting the experimental data with the Langmuir adsorption model.[110,111] However, the requirement for the labeled substrates has significantly limited the broader application of this method. A newly introduced approach called "Hot Spot"-Normalized Surface-Enhanced Raman Scattering (HSNSERS) not only eliminates the need for additional internal standards by utilizing surface-enhanced elastic scattering for calibration purposes but also allows for real-time observation of ligand exchange process *in situ*.[112] Application of the HSNSERS technique was initially demonstrated by examining the interaction between several chloroanilines and gold NPs.[112] A few additional studies expanded the utilization of this methodology.[113,114]

Qualitative analysis of binding. SERS has found widespread application in qualitative analysis of ligand–NP interactions, providing important information on the binding mode of ligands on the NP surface.[45,46,48,111,115–137] However, this technique nearly always has to be accompanied by other supporting methods, either theoretical (*i.e.* DFT, surface selection rules)[127–131] or experimental (*i.e.* XPS, FTIR, UV/Vis),[118,127] to aid in the interpretation of the results.

Isothermal titration calorimetry (ITC)

Isothermal Titration Calorimetry (ITC) is a versatile technique for examining thermodynamic and, in some cases, kinetic parameters on molecular interactions.[138–140] The ability of ITC to directly measure ΔH of binding makes it stand out from the rest of the available methods. ITC data collection is performed by measuring the heat adsorbed or released when small aliquots of ligand solution are injected into a sample containing the NP receptor, and binding takes place. Fitting the titration curve (heat over ligand/receptor molar ratio) delivers a complete set of thermodynamic (ΔH, ΔS, and ΔG) and stoichiometric parameters of binding.

Quantitative analysis of binding. ITC has been extensively utilized to study biomacromolecular interactions[141] and, more recently, extended to the examination of other types of ligand-

receptor systems. In particular, ITC was used to quantify the affinity of ligands towards the NP surface and guide the rational design of NP receptors with regulated binding strength towards specific targets.[142,143] In the drug-delivery field, ITC derived data are used to quantify the loading of active pharmaceutical ingredients on NP delivery vehicles.[144] In addition, ITC was reportedly used to characterize the thermodynamics of a few other ligand–NP systems.[52,145,146]

Qualitative analysis of binding. Although quantitative analysis of binding is seen as the main strength of the ITC technique, a quick qualitative assessment of relative affinity trends could be performed on a series of compounds without the need for theoretical modelling of the experimental data. For example, using ITC data recorded for several DNA bases and their peptide analogs in the presence of gold NPs, Gourishankar *et al.* determined relative binding affinities of the ligands toward gold NPs.[147]

Despite the ability of ITC to yield near-complete thermodynamic characterization of binding, its broader application to the small molecule–NP system has been hampered due to experimental challenges and complexities involved in data processing. Among these, relatively long experimental times, interference from the aggregation of the investigated substrates and NPs, significant complications in assessing very weak and very strong bindings ($K < 10^3 \text{ M}^{-1}$ and $K > 10^8 \text{ M}^{-1}$, respectively), and the requirement to account for every contribution to heat in the studied system are generally considered the principal challenges of the ITC technique.

Solution NMR methods for characterizing sorption equilibria

NMR signals originate from low-energy transitions that relax slowly compared to other spectroscopic methods (ms–s). Although this property dooms NMR to the rank of a poorly-sensitive technique, it also provides NMR with several advantages over other analytical methods. Indeed, the low relaxation rate of its signals makes NMR a high-resolution method capable of returning different spectroscopic peaks for the different atoms composing the analyte under investigation. In addition, the fact that NMR excited states are long-lived allows extensive spectroscopic manipulations of the NMR signals that resulted in the creation of an unmatched portfolio of NMR experiments able to characterize dynamic processes occurring on timescales ranging from picoseconds to hours. This ability to probe with atomic-resolution dynamic interactions occurring on a large range of timescales makes NMR an ideal method for studying sorption equilibria that involve multiple adsorbed and intermediate states.

In this section, we review solution NMR methods for the investigation of surface adsorption. Before diving into specific NMR experiments, we will introduce the concept of chemical exchange as applied to solution NMR. Due to their large molecular size, NPs exhibit a large transverse relaxation rate (R_2). Because of the large R_2, NMR signals of NPs are broadened out beyond the detection level of conventional solution NMR

spectroscopy (discussed in detail below). For this reason, the study of surface adsorption by direct investigation of NPs themselves using solution NMR techniques is often impossible, and solid-state NMR techniques are more often applied to this end.[32,148,149] However, in the presence of a chemical exchange equilibrium between a free NMR-visible state and a NP-bound NMR-invisible state, several solution NMR experiments (reviewed below) can be used to imprint information on the structure and dynamics of NP surface-bound species into the spectrum of the free ligand. Therefore, the concept of chemical exchange is crucial for solution NMR studies of surface adsorption.

Chemical exchange in NMR

A process that involves a nucleus exchanging between different chemical environments is called a chemical exchange. In the context of this review, the binding of a small molecule to a NP surface is an example of chemical exchange. The chemical exchange induces changes in the NMR spectrum, and the appearance of the spectrum depends on the timescale in which the exchange occurs.[150–153] There are three main timescales associated with NMR when describing chemical exchange: slow, intermediate, and fast. Each exchange regime can be defined in terms of a chemical shift difference ($\Delta\omega$), relaxation rates of the exchanging species, and exchange rate constant (k_{ex}). In this review, we will use a two-state exchange model to illustrate how exchange affects the NMR spectrum and will refer to this model to simulate data (Fig. 2).

Consider a two-state model where a molecule is in an exchange between state A and state B:

$$\text{A} \underset{k_{-1}}{\overset{k_1}{\rightleftharpoons}} \text{B} \tag{9}$$

The two states are assumed to have different chemical shifts (*i.e.*, $\Delta\omega \neq 0$). k_1 and k_{-1} are the forward and reverse first-order rate constants for the equilibrium (corresponding to k_{ads} and k_{des} in eqn (1), respectively), and $k_{ex} = k_1 + k_{-1}$.[150–153] For simplicity, we will first consider a two-state model where the two exchanging species have similar longitudinal (R_1) and transverse (R_2) relaxation rates ($R_1^A \sim R_1^B$ and $R_2^A \sim R_2^B$, respectively) such as in equilibria describing a conformational change. It is important to note that this is not the case for the small molecule–NP system, which will be discussed later. Fig. 2a illustrates the effect of the exchange on the NMR spectrum of a molecule containing a single NMR-active nucleus. In the fast exchange regime ($\Delta\omega \ll k_{ex}$), a single peak at the population-averaged chemical shift is observed. The observed relaxation rates will also be population-weighted:

$$R_1^{obs} = p_A R_1^A + p_B R_1^B \tag{10}$$

$$R_2^{obs} = p_A R_2^A + p_B R_2^B \tag{11}$$

where R_1^{obs} and R_2^{obs} are the observed longitudinal and transverse relaxation rates, respectively (note that one single peak is detected in the fast exchange regime), and p_A and p_B are the
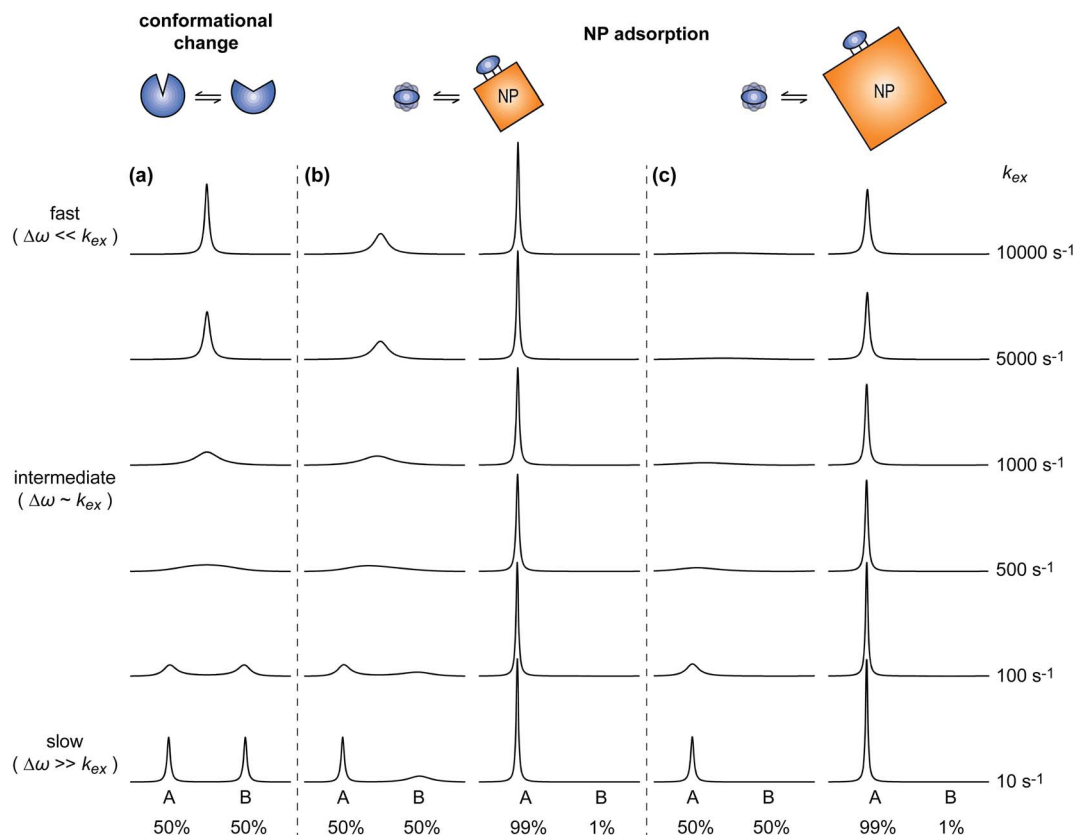
Fig. 2 Simulated NMR spectra illustrating the effect on the NMR lineshape of chemical exchange between two states, A and B, over a range of exchange timescales (0 to 10 000 s^{-1}, bottom to top). In (a), states A and B have an equal population ($p_A = p_B = 0.5$) and transverse relaxation rates ($R_2^A = R_2^B = 10$ s^{-1}). In (b), $R_2^A = 10$ s^{-1} and $R_2^B = 100$ s^{-1} to simulate a sorption equilibrium in which a small molecule adsorbs on a small NP. In the left panel, the populations of desorbed (state A) and adsorbed (state B) species are considered equal ($p_A = p_B = 0.5$). In the right panel, the equilibrium is skewed toward state A ($p_A = 0.99$ and $p_B = 0.01$). In (c), $R_2^A = 10$ s^{-1} and $R_2^B = 1000$ s^{-1} to simulate a sorption equilibrium in which a small molecule adsorbs on a large NP. In the left panel, the populations of desorbed (state A) and adsorbed (state B) species are considered equal ($p_A = p_B = 0.5$). In the right panel, the equilibrium is skewed toward state A ($p_A = 0.99$ and $p_B = 0.01$). In all simulations, the chemical shift difference between states A and B ($\Delta\omega$) is 600 rad s^{-1}. Note that the larger is R_2^B and the more apparent is the effect of the small molecule–NP interaction on the NMR spectra of the ligand. Therefore, the larger is the NP size and the higher is the sensitivity of solution NMR in detecting and characterizing sorption.

fractional populations of states A and B, respectively. On the contrary, in the slow exchange regime ($\Delta\omega \gg k_{ex}$), two peaks are observed, one at the chemical shift of state A and the other at the chemical shift of state B, each relaxing at its own relaxation rates. When the conditions for fast or slow exchange do not apply (*i.e.* $\Delta\omega \sim k_{ex}$), the system is considered to be in the intermediate exchange regime, and the R_2^{obs} is enhanced by the exchange contribution, R_{ex}:

$$\left.\begin{array}{l} R_1^{obs} = p_A R_1^A + p_B R_1^B \\ R_2^{obs} = p_A R_2^A + p_B R_2^B + R_{ex} \end{array}\right\} \quad \text{if } \Delta\omega < k_{ex} \quad (12)$$

$$\left.\begin{array}{l} R_1^{obs,A} = R_1^A \\ R_2^{obs,A} = R_2^A + R_{ex} \end{array}\right\} \quad \text{if } \Delta\omega > k_{ex} \quad (13)$$

where $R_1^{obs,A}$ and $R_2^{obs,A}$ are the R_1^{obs} and R_2^{obs}, respectively, for the NMR peak of species A in the slow-intermediate exchange regime.

The appearance of the NMR spectrum is chiefly dependent on R_2^{obs}, as the linewidth (peak width at half height measured in Hz) of each NMR signal ($\Delta\nu_{1/2}$) is given by:

$$\Delta\nu_{1/2} = \frac{R_2^{obs}}{\pi} \quad (14)$$

Therefore, the increase in R_2^{obs} caused by R_{ex} results in broadening of the detected signal and consequential reduction in intensity (note that the integral of the NMR signal is not affected by the exchange and, therefore, a larger linewidth is associated with a lower peak height). As shown in Fig. 2a, starting from the slow exchange regime and increasing k_{ex}, the two peaks will gradually broaden as a result of the exchange. When $\Delta\omega \sim k_{ex}$ the peaks will coalesce into one single NMR signal that is highly broadened by the chemical exchange. Further increase in k_{ex} will shift the system to the fast exchange regime with a consequent increase in resolution and peak intensity.

We will now consider a two-state model where a molecule is in equilibrium between the free and NP-bound states. Since the two states under chemical exchange differ considerably in molecular size, the dependency of the NMR relaxation rates

from the molecular rotational tumbling needs to be taken into account when discussing the effect of the exchange on the measured NMR spectra. As shown in Fig. 3, the R_1 reaches a maximum when the rate of rotational tumbling ($1/\tau_C$, where τ_C is the rotational correlation time) is on the same order as the Larmor frequency of the observed nucleus. Although this condition depends on the nucleus under investigation (i.e. ^{1}H and ^{13}C have different Larmor frequencies) and on the static field of the spectrometer, the fact that R_1 is small for very small and very large molecules makes $R_1^A \sim R_1^B$ in the majority of the small molecule–NP systems (Fig. 3). On the other hand, the R_2 always increases by increasing τ_C (Fig. 3), and $R_2^A \ll R_2^B$ for small molecule–NP sorption equilibria. The large R_2^B often results in line broadening beyond detection level and, as a result, the NP-bound state becomes invisible by NMR (see Fig. 2b and c). However, despite its invisibility, the surface-bound state can affect the relaxation rate and chemical shift of the NMR-visible free molecule via chemical exchange (Fig. 2b and c), and a number of NMR experiments were developed to use the perturbation of the NMR signals of the NMR-visible state to obtain information on the NP-bound species.

Fig. 2b and c show how the chemical exchange between two states with a large difference in R_2 affects the NMR spectra at different timescales. In the fast exchange regime, a single peak is observed with population-weighted chemical shift and relaxation rates (eqn (10) and (11)). However, since the transverse relaxation data measured in the presence of NP are often analyzed in comparison to the R_2 of the free state, the following equation is more commonly used:

$$R_2^{obs} = R_2^A + R_{llb} \tag{15}$$

where the lifetime line broadening (R_{llb}) describes the increase in the observed transverse relaxation of state A caused by the

exchange with a state with a higher R_2. In the intermediate exchange regime, eqn (12) and (13) still apply for R_1. On the other hand, the R_2 of the NMR-visible peak is given by:

$$R_2^{obs,A} = R_2^A + R_{ex} + R_{llb} \tag{16}$$

It is important to note that while R_{llb} is caused by the exchange between states with a large difference in R_2, R_{ex} is due to the exchange between states with different chemical shifts. Therefore, R_{llb} occurs even for exchange processes with $\Delta\omega = 0$. In the slow exchange regime, when the transverse relaxation rate of the NMR-invisible state is faster than dissociation from the bound to the free state (i.e. $R_2^B > k_{-1}$), the observed R_2 is increased by the apparent rate of the forward reaction (i.e. $R_{llb} = k_1$):[154]

$$R_2^{obs,A} = R_2^A + k_1 \tag{17}$$

This is because any binding event results in an irreversible loss of magnetization as the signal is completely relaxed before the small molecule returns to the NMR-visible free state. When this limiting condition does not apply, $R_{llb} < k_1$ (see below).

In summary, the theoretical considerations discussed in this section indicate that although NP-bound species are not observed directly by solution NMR, the contrast between the fast R_2 of the bound state and the slow R_2 of the free state can be utilized to imprint information about the NP-bound state onto the spectrum of the NMR-visible free state. Given that the R_2 of the visible state is affected differently depending on the timescale of the free-bound equilibrium, the types of solution NMR methods one can use to characterize NP adsorption are also dependent on the timescale in which the exchange occurs. In the following sections, we discuss solution NMR methods for characterizing small molecule–NP interactions at different exchange regimes.

Preparation of stable NMR samples containing nanoparticles

Solution NMR methods to investigate sorption equilibria rely on the direct observation of the ligand–NP adduct (in the case the investigated complex is small enough to be directly detected in a NMR experiment) or on the indirect observation of the NMR-invisible ligand–NP interaction on the spectra of the NMR-visible free ligand (see above). In either case, to obtain accurate and reproducible data, it is important that the ligand and the NP remain homogeneously suspended within the sample throughout the experiment. For soluble NPs, no special procedure is required to prepare NMR samples since the ligand-to-surface ratio will stay consistent throughout the sample and will not change over time. On the contrary, insoluble NPs quickly sediment in solution, changing the concentration of ligand–NP adduct within the NMR active volume over time. Therefore, establishing a generally applicable sample preparation method that results in homogeneously dispersed stable suspensions of insoluble NPs was a crucial step toward increasing the applicability of solution NMR methods to the characterization of sorption equilibria. The method consists in preparing the NMR samples in a gel matrix that prevents NP
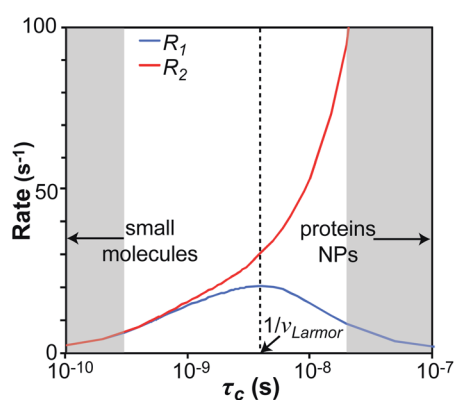

Fig. 3 Simulation of ^{13}C relaxation rates as a function of correlation time at 800 MHz. Simulations were performed for a C–H spin system of fixed bond length (1.09 Å) using eqn (51) and (52). The longitudinal relaxation rate (R_1) increases as τ_C increases, reaches a maximum when the rate of rotational tumbling matches that of Larmor frequency (i.e. when $\tau_C = 1/\nu_{Larmor}$), and decreases as the tumbling rate becomes slower than Larmor frequency (blue curve). The transverse relaxation rate (R_2) increases as τ_C increases (red curve). Transparent gray boxes highlight the ranges of τ_C expected for small molecules (left) or proteins and NPs (right).

sedimentation.[155,156] Such gel matrix should (i) undergo rapid gelation (which allows stabilization of a homogeneous suspension of NPs), (ii) not interfere with the ligand–NP interaction of interest, and (iii) have a minimal fingerprint in the NMR spectrum used for characterizing the ligand–NP system. A library of small molecule gelators that satisfy these requirements was recently developed to stabilize NP suspensions in a number of NMR-friendly aqueous[155] and organic solvents.[156]

When discussing sample preparation protocols, it is also important to mention that indirect detection of the NMR-invisible ligand–NP adduct on the spectra of the NMR-visible free ligand is usually performed on samples in which the sorption equilibrium is highly skewed toward the free state ($p_A \geq 90\%$). Indeed, the large R_2 of the NP-bound state results in line broadening of the NMR signals of the free state even when $p_B \lesssim 1\%$ (note that the exact detection limit depends on R_2^B, with higher R_2^B's resulting in higher sensitivity), and a $p_B > 10\%$ often results in a complete loss of signal (Fig. 2b and c).

Analysis of chemical shift changes (CSCs)

The NMR chemical shift is very sensitive to the local chemical environment of the nucleus. Therefore, chemical shifts are very sensitive reporters of intermolecular interactions. In a conventional CSC experiment, the NMR-visible interaction partner (*i.e.* the ligand) is kept at a constant concentration, while the NMR-invisible component of the interaction (*i.e.* the NP) is titrated into the solution, and the chemical shift change is monitored as a function of the titrant concentration. Fig. 4 illustrates how the NMR spectrum of a small molecule ligand changes upon the titration experiment within the fast, intermediate, and slow exchange regimes. To construct the spectra in Fig. 4, a simple two-state binding model was assumed. Analysis of this figure reveals that no chemical shift change is detected for processes occurring on the slow exchange regime since separate peaks are observed for the free and bound states with changes in peak intensities (discussed below) as the NP is titrated into the ligand (Fig. 4e). At the slow-intermediate exchange regime, a low population of the bound state ($\leq 20\%$) results in a small CSC, while a high population of the bound state ($\geq 50\%$) causes extreme line broadening due to R_{ex}. These effects make monitoring the changes in chemical shift challenging for systems with binding kinetics in the slow-intermediate regime (Fig. 4b–d). Analysis of chemical shift change works best for weak binding interactions that occur on a fast timescale. In the latter case, the observed chemical shift (δ_{obs}) is a weighted average of the free and bound states chemical shifts (δ_A and δ_B, respectively):

$$\delta_{obs} = \delta_A p_A + \delta_B p_B \tag{18}$$

The CSC is measured in reference to the chemical shift of the free state, as described by the following equation:

$$\text{CSC} = \delta_{obs} - \delta_A = (\delta_A p_A + \delta_B p_B) - \delta_A \tag{19}$$

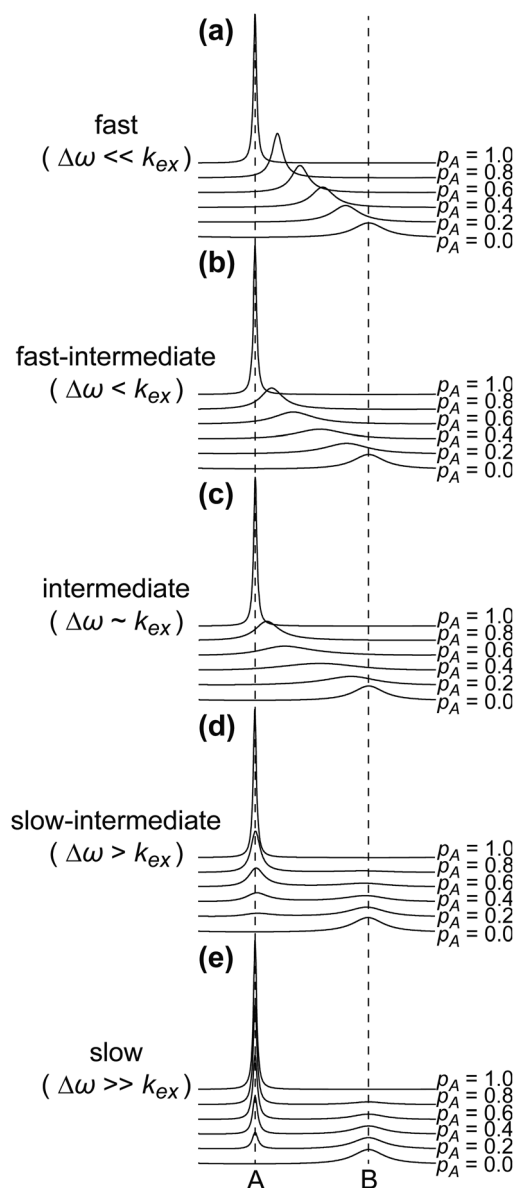Given that $p_A + p_B = 1$, a rearrangement of eqn (19) gives:

Fig. 4 Simulated NMR spectra showing the effect of varying the population of state A (p_A) in a two-state sorption equilibrium occurring on the (a) fast exchange regime ($k_{ex} = 10^4 \text{ s}^{-1}$), (b) fast-intermediate exchange regime ($k_{ex} = 10^3 \text{ s}^{-1}$), (c) intermediate exchange regime ($k_{ex} = 600 \text{ s}^{-1}$), (d) slow-intermediate exchange regime ($k_{ex} = 10^2 \text{ s}^{-1}$), and (e) slow exchange regime ($k_{ex} = 10 \text{ s}^{-1}$). In all simulations, $R_2^A = 10 \text{ s}^{-1}$, $R_2^B = 100 \text{ s}^{-1}$, and $\Delta\omega = 600 \text{ rad s}^{-1}$. The vertical dashed lines indicate the chemical shifts of states A and B.

$$p_B = \frac{\text{CSC}}{(\delta_B - \delta_A)} \tag{20}$$

Although the ability of the CSC analysis to return the concentration of bound ligand makes these experiments a potential input for the Langmuir isotherm modelling (*e.g.*, $p_B \sim \theta$ in eqn (3a)), CSC experiments are associated with several practical problems that hamper their widespread use in quantitative studies of sorption. Indeed, as p_B approaches 1, the

NMR signal may become invisible due to the large R_2 of the bound state. Moreover, since most NPs are sparingly soluble, obtaining near saturation of binding (required for accurate modelling of the Langmuir isotherm – see above) can be challenging, especially for the weak ligand–NP interactions that can be analyzed quantitatively by CSC. As an alternative, one can titrate the ligand into a fixed concentration of NP. In this case, the population of the bound state will decrease as the ligand is titrated in, eventually reaching close to 0 for concentrations of ligand much higher than K. However, it should be noted that the latter approach still suffers from the low sensitivity at low ligand concentrations (when most of the ligand is in the NMR-invisible bound state) and cannot be applied to ligands that oligomerize or precipitate at a concentration higher than K.

Despite all the challenges of CSC, analysis of the NP-induced changes in chemical shifts can still be used to characterize the functionalities involved in the interaction and the binding mode. For example, Calzolai *et al.* determined the location of the interaction site between the ubiquitin and gold NP by analyzing CSCs.[157] They observed that the chemical shifts of only specific residues of ubiquitin changed upon the addition of gold NPs, revealing that the interaction is specific. Similarly, the binding sites for C_{60} fullerene in proteins were identified using CSC analysis.[158,159] Also, by monitoring the interaction between L-lysine and water-soluble ruthenium NPs by CSC analysis, Martinez-Prieto *et al.* revealed that the binding orientation of L-lysine on the NP surface is relevant to the deuteration reaction catalyzed by the NP.[160]

In some cases, the study of surface adsorption on a metal surface using CSC can be hindered by the extreme broadening and peak shift caused by the Knight-shift effect.[161,162] One way to overcome this disadvantage is to have a spacer atom between the observed nucleus of the adsorbed species and the metal surface. For example, using oxygen as the spacer atom, Tedsree *et al.* investigated the chemisorption of formic acid on various metal colloid catalysts and found that the ^{13}C chemical shift values of the adsorbates were directly correlated to the chemisorption strength.[163]

Peak intensity

The NMR signal intensity (intended as the integral of the NMR peak) is related to the number of nuclei resonating at a given chemical shift. Therefore, the intensity of an NMR signal can be used to determine the concentration of a species in the analyzed sample. If a ligand undergoes chemical exchange between the free and NP-bound states on the slow timescale, separate peaks are observed for the adsorbed and desorbed species with intensities that are proportional to the populations of each state (Fig. 2 and 4). Due to its large R_2, the signal of the bound state is line broadened and often invisible in the NMR spectrum. However, the signal for the desorbed ligand is NMR-visible and with an intensity that is proportional to its population in solution. Therefore, in the slow exchange limit, if a sample of a ligand is titrated with known amounts of NP, the decrease in signal intensity can be used to experimentally quantify C_L and q_{LS} (Fig. 4) and model the interaction with the Langmuir theory

(eqn (3a)). For example, Wang *et al.* determined the binding capacity of various proteins to gold NPs by monitoring the decrease in the intensity of the free protein signal at different NP concentrations.[164] In another example, Wang *et al.* showed that by using a 1D half-filter experiment, one could investigate the competitive binding of multiple proteins, each labeled with different isotopes, to gold NPs.[165] Xu *et al.* used a similar approach to investigate the competitive adsorption of two different proteins, GB3 and ubiquitin, and two GB3 variants differing by only one residue to gold NPs.[166] In this study, the authors developed an external referencing system using ^{15}N labeled tryptophan to facilitate the accurate conversion of signal intensity into the concentration of free ligand.

When using the change in signal intensity of the desorbed state in quantitative analysis of sorption equilibria, it is advisable to measure signal intensities by peak integration algorithms rather than by peak height. Indeed, when a ligand is in equilibrium between free and NP-bound state in the slow exchange regime ($\Delta\omega \gg k_{ex}$), if $R_2^B > k_{-1}$, the R_2 of the desorbed state is increased by k_1 (eqn (17)) with a consequential reduction of peak height due to line broadening. In addition, in the more common case of intermediate-slow exchange between desorbed and adsorbed species ($\Delta\omega > k_{ex}$), additional line broadening is caused by the exchange contribution to R_2. As R_{ex} is maximum when the exchanging species are equally populated (*i.e.* $p_B \sim$ 0.5) and is minimum at $p_B \sim 0$ or 1, the presence of an intermediate-slow exchange results in additional modulations of peak height that are not linearly dependent on the concentration of desorbed and adsorbed species (Fig. 4).

Diffusion ordered spectroscopy (DOSY)

DOSY is a useful NMR technique to measure the diffusion coefficients (D) of molecules.[167] The most basic DOSY pulse sequence is shown in Fig. 5.[168] A 90° pulse is applied to excite the nuclear spins, followed by the first gradient, which labels the spins with a phase change that depends on their positions in the NMR tube. A 180° pulse is then applied to invert the sign of the phase change, and a second gradient is applied to refocus the signal. When a sample molecule diffuses during the delay period (shown as Δ in Fig. 5), its NMR signals will not be completely refocused by the second gradient, resulting in reduced NMR signal intensity. Therefore, free small molecules that diffuse fast in the sample will experience greater signal attenuation than the NP-bound molecules that diffuse slowly due to the large size of the NP.

The intensity change from DOSY experiments can be quantitatively described by the Stejskal–Tanner equation:[169]

$$I = I_0 \, e^{-D\gamma^2 G^2 \delta^2 \left(\Delta - \frac{\delta}{3} \right)} \tag{21}$$

where I is the observed intensity, I_0 is the initial intensity, D is the diffusion coefficient, γ is the gyromagnetic ratio, G is the gradient strength, δ is the gradient duration, and Δ is the delay period. To obtain the value of D, a series of measurements are taken by varying either the gradient strength, the gradient duration, or the delay period and fitting the intensity decay
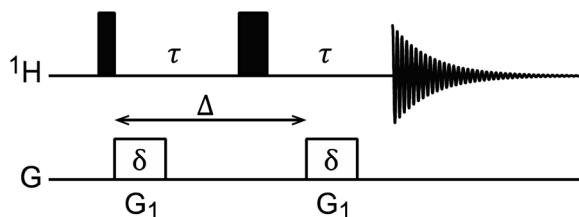
Fig. 5 ^{1}H DOSY pulse sequence.[168] The black narrow and wide rectangular-shaped pulses represent 90° and 180° pulses, respectively. The white rectangles represent gradient pulses. Δ is the delay period (*i.e.* time of diffusion), δ is the gradient duration, and G_1 is the gradient strength.

using eqn (21). 2D DOSY spectra are generated by plotting chemical shifts on one axis and diffusion constants on the other.[170] Each line in the NMR spectrum will give one or more lines in the diffusion dimension at the values corresponding to the diffusion coefficient of the associated species. Therefore, DOSY makes a powerful tool for analyzing mixtures containing more than one ligand–NP species. Moreover, for a spherical molecule, the diffusion coefficient can be used to determine the molecular size using the Stokes–Einstein equation:

$$D = \frac{k_B T}{6\pi\eta r_H} \tag{22}$$

where k_B is the Boltzmann constant, T is the temperature, η is the viscosity of the solution, and r_H is the hydrodynamic radius of a molecule. Therefore, an estimate of the NP size can be obtained from the value of D obtained for the bound species.

One very important aspect to notice is that the exchange regimes of a DOSY experiment are defined by the diffusion time (Δ). Considering a simple two-state exchange model where a molecule is in an exchange between states A and B (eqn (9)), the fast exchange regime in the diffusion timescale is defined when $\Delta \gg 1/k_{ex}$ (*i.e.* several exchange events between states A and B occur during Δ), and the slow exchange regime in the diffusion timescale is defined when $\Delta \ll 1/k_{ex}$ (*i.e.* very few exchange events between states A and B occur during Δ).[171–173] Therefore, by varying Δ, one can observe the system in either fast or slow exchange in the diffusion timescale. If the exchange is fast in the diffusion timescale, a single population weighted diffusion coefficient will be observed:

$$D_{obs} = p_A D_A + p_B D_B \tag{23}$$

where D_{obs} is the observed diffusion coefficient, and p_n and D_n are the fractional population and diffusion coefficient of state n, respectively. If the exchange is slow in the diffusion timescale, two different diffusion coefficients will be observed, resulting in a bi-exponential decay of signal intensity as a function of the varying parameter in the DOSY experiment (G, δ, or Δ in eqn (21) – see above).

Given that Δ defines the exchange regime in diffusion experiments, DOSY can be applied to exchange systems occurring on a wide range of timescales. However, if $\Delta \ll 1/k_{ex}$ and

$\Delta\omega \gg k_{ex}$ (*i.e.* the system is in slow exchange in both the diffusion and chemical shift timescales), no change in D will be observed by fitting the intensity of the NMR-visible signal of the free ligand with eqn (21). This limitation, together with the fact that Δ cannot be larger than $1/R_2$ (to avoid excessive intensity loss during the experiment), hampers the application of DOSY to ligand–NP systems for which $R_2 \gg k_{ex}$.

DOSY experiments have been used to characterize several ligand–NP systems. For example, Hens *et al.* investigated trioctylphosphine oxide (TOPO) capped colloidal InP nanocrystals using solution NMR.[174] From the diffusion coefficient obtained from DOSY measurements and comparing it to the nanocrystal diameter, the authors determined that the broad resonance superimposed on the free TOPO signal was coming from TOPO molecules adsorbed at colloidal nanocrystals. Similarly, Moreels *et al.* used DOSY measurements to identify the ligands that are tightly bound to the surface of the PbSe nanocrystals.[175] In another example, using DOSY, Hassinen *et al.* determined that octylamines are dynamic ligands for CdSe quantum dots and that free and bound octylamines exhibit fast exchange.[176]

Saturation transfer methods

When a small molecule is in an exchange between the free and NP-bound states, the large molecular size of the NP increases the R_2 of the bound small molecule. The increase in R_2 is often large enough to cause broadening of the NMR signal beyond detection level. Saturation transfer experiments achieve indirect detection of the bound state on the spectra of the NMR-visible desorbed state by selective saturation of the NP or the bound state itself. The saturation is then transferred to the visible state *via* chemical exchange. This section will discuss the two main saturation transfer experiments applied to ligand–NP systems: saturation transfer difference (STD) and dark-state saturation transfer (DEST).

Saturation transfer difference (STD) NMR. The STD NMR method has been widely used to study ligand–protein interactions.[177–180] The standard pulse sequence for 1D ^{1}H STD NMR is shown in Fig. 6a. It involves a train of Gaussian-shaped pulses to achieve the saturation of selected resonances before applying a hard 90° reading pulse. The STD NMR experiment requires taking the difference between an on-resonance spectrum obtained by selectively saturating the ^{1}H signals of the NP and a reference off-resonance spectrum in which the saturation field is moved to a region that does not contain peaks of the InP or the ligand. In the on-resonance experiment, the saturation applied to selective NP resonances is quickly transferred to the other ^{1}H spin on the NP as well as to protons of any ligand bound to the NP surface *via* spin diffusion (which is highly efficient among ^{1}H spins in high molecular weight systems such as proteins and NPs). Therefore, when bound ligands dissociate into the solution, they cause a decrease in the signal intensity of the free state due to the partial transfer of saturation from the NP-bound state. As a result, when the on-resonance spectrum is subtracted from the off-resonance reference, only signals from ligands that bind to the NP will persist (Fig. 6b).
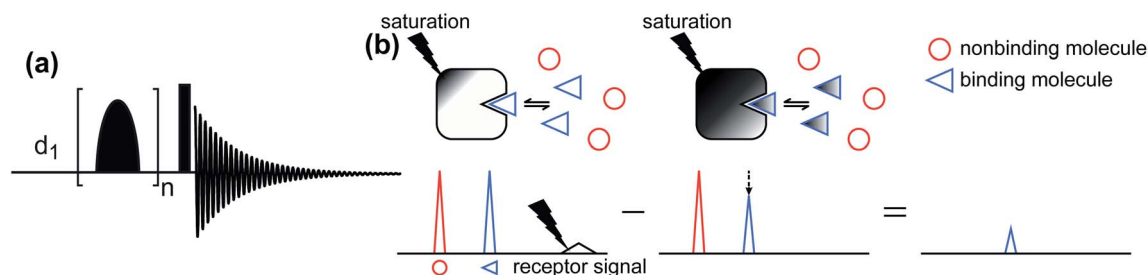
Fig. 6 (a) Standard pulse sequence for 1D STD NMR. The saturation is achieved by applying a train of n Gaussian-shaped pulses. After the saturation period, a 90° excitation pulse (represented by the rectangular-shaped pulse) is applied. d_1 identifies the recycling delay. (b) Schematic representation of the STD NMR protocol. Selective saturation is applied to a receptor proton signal. The saturation is transferred to the entire receptor and to any NMR-invisible attached ligand *via* spin diffusion. When the ligand dissociates from the receptor, it carries the saturation in the NMR-visible state, reducing the intensity of the observed NMR signal. Therefore, when the saturated spectrum is subtracted from a reference spectrum (acquired in the absence of saturation), only residual signals originating from small molecules that bind to the receptor are visible.

Quantitative interpretation of the STD experiment can be obtained by analyzing the magnitude of the STD effect measured as:

$$\text{STD effect} = \frac{I_0 - I_{\text{sat}}}{I_0} \tag{24}$$

where I_0 and I_{sat} are the signal intensities in the off- and on-resonance spectrum, respectively. The STD effect is then normalized by multiplying it by the ligand excess, yielding the STD amplification factor.[178]

$$\text{STD amplification factor} = \frac{I_0 - I_{\text{sat}}}{I_0} \times \frac{[\text{L}]}{[\text{R}]} \tag{25}$$

where [L] and [R] are the concentrations of ligand and receptor, respectively. A titration curve of the STD amplification factor as a function of the ligand concentration can be fit using a binding isotherm to determine the equilibrium constant for the binding process.[178]

STD NMR protocols and theoretical modeling have been extensively developed and tested for screening projects aimed at identifying ligands for protein drug targets.[177,181–183] More recently, several STD NMR applications to the investigation of NP adsorption have appeared in the literature. For example, STD NMR has been used to screen libraries of small molecules against NP targets,[184,185] to determine the affinities of NP–ligand adducts,[184,186] and to investigate the forces driving small molecule adsorption.[187] It is important to note that when using the STD NMR for NPs, the concentration of the receptor (noted as [R] in eqn (25)) should be the total concentration of binding sites. As discussed above, when introducing the Langmuir model, this quantity is not easily measurable for NP receptors and introduces ambiguities in the interpretation of the experimental data. To overcome this issue, Zhang *et al.* used a constant proportional to the surface area of the NP in place of the concentration of the binding sites to calculate the relative STD amplification factor.[184] STD NMR can also give structural insight into the adsorption process. For example, by analyzing the pattern of STD amplification factors measured for the ^{1}H nuclei of rhodamine B, it was observed that the small molecule binds to polystyrene NPs *via* its benzoic acid ring.[186]

Despite the successful applications described above, a number of factors limit the widespread use of STD NMR in the characterization of sorption equilibria. Indeed, while STD NMR is effective for $k_{-1} > R_1$ (note that a dissociation rate slower than the longitudinal relaxation would cause the ligand to relax back to equilibrium before returning into the NMR-visible free state), a very large k_{-1} may result in a population of bound state too low to be detected by the experiment.[179] Another limitation of the STD NMR experiment is that the NP must be protonated in order to permit efficient saturation transfer *via* ^{1}H spin diffusion. Such condition hampers the applicability of STD NMR to the analysis of adsorption on metal or metal oxide NPs.

Dark-state exchange saturation transfer (DEST). The DEST experiment was originally developed to obtain thermodynamic, kinetic, and structural information on the interaction between small, NMR-visible proteins and large aggregates.[154,188–190] Later, the application of DEST was expanded to the investigation of ligand–NP interactions.[191,192] The DEST experiment takes advantage of the fact that the NMR resonances of the NP-bound state can be saturated selectively by applying a weak radiofrequency (RF) field far off-resonance from the resonances of the free state. Indeed, although broadened out beyond detection level, the bound state resonances are still present within the NMR spectrum. Given their large linewidth, the bound state peaks can be selectively saturated by an RF field positioned at a large offset compared to the resonances of the NMR-visible state. The saturation is then transferred from the bound state to the free state *via* chemical exchange and observed as a reduction in the signal intensity of free species (Fig. 7). In a typical setup, the DEST experiment is repeated at several RF field offsets to obtain a DEST profile reporting the signal intensity of the NMR-visible state as a function of the offset. The presence of an NMR-invisible bound state in chemical exchange with the NMR-visible free state will be detected as a broadening of the DEST profile compared to the one measured in the absence of NP (Fig. 7). The width of the DEST profile depends on the R_2 of the bound state and the strength of the applied RF field, as shown in Fig. 8. The higher the R_2 of the bound state and the stronger the RF field, the broader the DEST profile will be.

The DEST profile can be modelled using the Bloch–McConnell equation to obtain populations of free and bound states
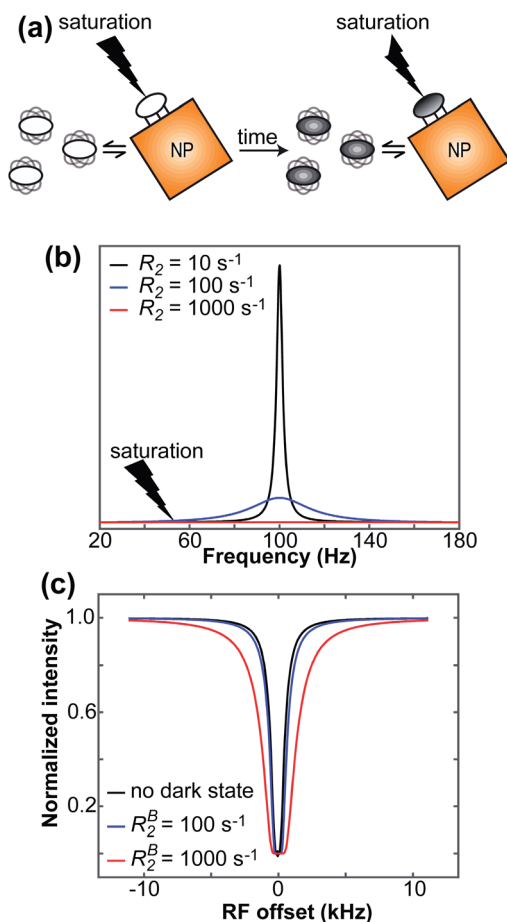
Fig. 7 (a) In the DEST experiment, the NMR-invisible surface-bound species is selectively saturated by an off-resonance RF field. The saturation is then transferred to the visible free species *via* chemical exchange, resulting in reduced signal intensity. (b) Simulated NMR signals for a free small molecule with $R_2 = 10$ s^{-1} (black line) and for a NP-bound small molecule with $R_2 = 100$ (blue line) or 1000 s^{-1} (red line). The broad resonance of the NP-bound state can be selectively saturated by an off-resonance RF. (c) A DEST profile is constructed by plotting the intensity of the NMR-visible peak as a function of the RF offset. The black line is the DEST profile simulated for a small molecule with $R_2 = 10$ s^{-1} in the absence of exchange. The blue and red lines are the DEST profiles simulated in the presence of exchange with an NP-bound state with $R_2 = 100$ and 1000 s^{-1}, respectively. In all simulations, $\omega_{rf} = 150$ Hz, $p_A = 0.95$, and $k_{ex} = 600$ s^{-1}. Note that, in the absence of exchange, a sharp DEST profile is obtained since saturation of the visible signal is achieved at small RF offsets only. In the presence of exchange with a species with large R_2, a broader DEST profile is obtained since saturation of the NP-bound state at large RF offsets is transferred to the NMR-visible state by chemical exchange.

and exchange rates.[189] For a two-site exchange system, the signal intensities for different RF offsets can be simulated by solving the following differential equation:

$$\frac{\mathrm{d}}{\mathrm{d}t}\boldsymbol{M} = -(\boldsymbol{E} + \boldsymbol{R} + \boldsymbol{K} + \boldsymbol{\Omega} + \boldsymbol{S})\boldsymbol{M} \qquad (26)$$

where $\boldsymbol{M}$ is the matrix representing the magnetization of each state in chemical exchange, $\boldsymbol{E}$ is the matrix representing the equilibrium magnetization, $\boldsymbol{R}$ is the matrix representing the relaxation rates of each state, $\boldsymbol{K}$ is the matrix representing the
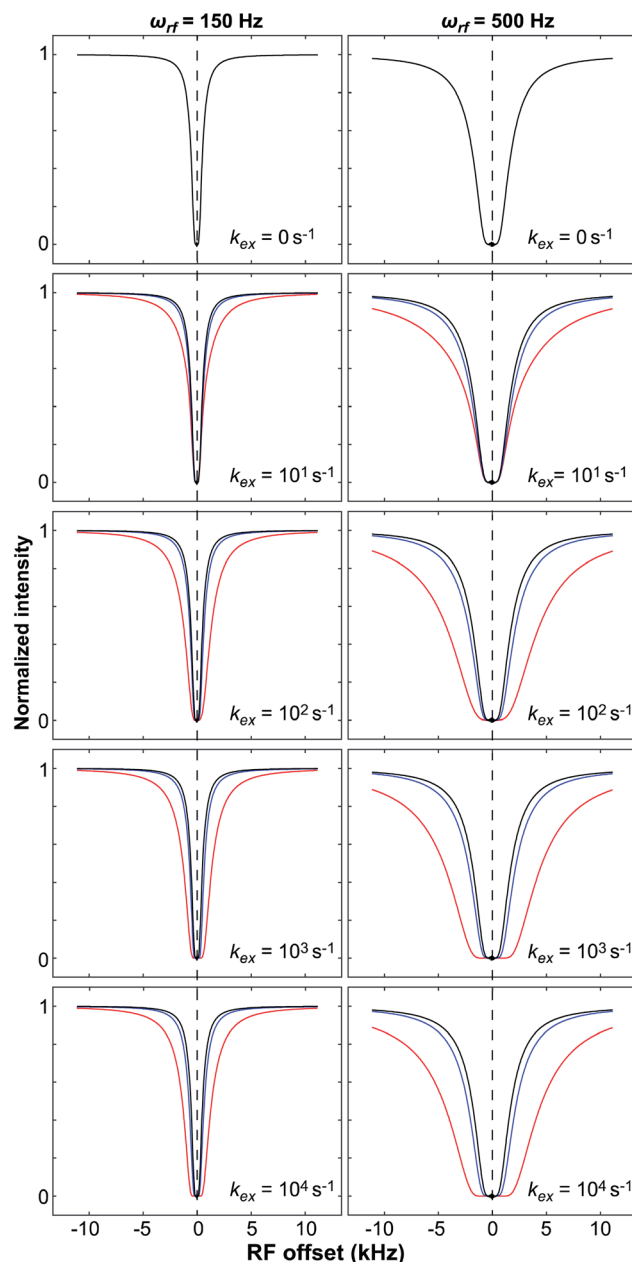
Fig. 8 Simulated DEST profiles for a two-site exchange equilibrium between the NMR-visible ($p_A = 0.95$ and $R_2^A = 10$ s^{-1}) and NMR-invisible ($p_B = 0.05$) states over a range of k_{ex} values (0 to 10 000 s^{-1}, top to bottom). R_2^B was set to 100 (blue line) or 1000 s^{-1} (red line) to simulate adsorption to a small or large NP, respectively. The DEST curve simulated at $k_{ex} = 0$ s^{-1} (corresponding to the data obtained in the absence of NP) is colored black. The saturation field strengths are 150 and 500 Hz for the left and right panels, respectively. Note that the DEST experiment is most efficient in detecting ligand–NP adduct with large R_2^B that exchange slowly with the desorbed state ($k_{ex} \ll R_2^B - R_2^A$). In the fast exchange limit, the shape of the DEST profile is no longer dependent from k_{ex}.

rate constants for the exchange kinetics, $\boldsymbol{\Omega}$ is the matrix representing the saturation offset, and $\boldsymbol{S}$ is the matrix representing the saturation field strength.[193] The matrices for each term are shown below:

$$
\boldsymbol{M} = \begin{bmatrix} E/2 \\ M_x^{\mathrm{A}} \\ M_y^{\mathrm{A}} \\ M_z^{\mathrm{A}} \\ M_x^{\mathrm{B}} \\ M_y^{\mathrm{B}} \\ M_z^{\mathrm{B}} \end{bmatrix}
\tag{27}
$$

$$
\boldsymbol{E} = \begin{bmatrix}
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
-2R_1^{\mathrm{A}} M_{\mathrm{eq}}^{\mathrm{A}} & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
-2R_1^{\mathrm{B}} M_{\mathrm{eq}}^{\mathrm{B}} & 0 & 0 & 0 & 0 & 0 & 0
\end{bmatrix}
\tag{28}
$$

$$
\boldsymbol{R} = \begin{bmatrix}
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & R_2^{\mathrm{A}} & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & R_2^{\mathrm{A}} & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & R_1^{\mathrm{A}} & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & R_2^{\mathrm{B}} & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & R_2^{\mathrm{B}} & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & R_1^{\mathrm{B}}
\end{bmatrix}
\tag{29}
$$

$$
\boldsymbol{K} = \begin{bmatrix}
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & k_1 & 0 & 0 & -k_{-1} & 0 & 0 \\
0 & 0 & k_1 & 0 & 0 & -k_{-1} & 0 \\
0 & 0 & 0 & k_1 & 0 & 0 & -k_{-1} \\
0 & -k_1 & 0 & 0 & k_{-1} & 0 & 0 \\
0 & 0 & -k_1 & 0 & 0 & k_{-1} & 0 \\
0 & 0 & 0 & -k_1 & 0 & 0 & k_{-1}
\end{bmatrix}
\tag{30}
$$

$$
\boldsymbol{\Omega} = \begin{bmatrix}
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & \varOmega^{\mathrm{A}} & 0 & 0 & 0 & 0 \\
0 & -\varOmega^{\mathrm{A}} & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & \varOmega^{\mathrm{B}} & 0 \\
0 & 0 & 0 & 0 & -\varOmega^{\mathrm{B}} & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0
\end{bmatrix}
\tag{31}
$$

$$
\boldsymbol{S} = \begin{bmatrix}
0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & -\omega_y & 0 & 0 & 0 \\
0 & 0 & 0 & \omega_x & 0 & 0 & 0 \\
0 & \omega_y & -\omega_x & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & -\omega_y \\
0 & 0 & 0 & 0 & 0 & 0 & \omega_x \\
0 & 0 & 0 & 0 & \omega_y & -\omega_x & 0
\end{bmatrix}
\tag{32}
$$

where E is unity, M_k^{n} represents the magnetization on the k-axis of state n, $\varOmega^{\mathrm{n}}$ represents the difference between the resonance frequency of state n and the frequency of the applied saturation field, and ω_k is the strength of the saturation field applied to the k-axis.

When modelling a DEST profile, R_1^{A}, R_2^{A}, ω_x, and ω_y are usually provided as input parameters and not optimized (note that R_1^{A} and R_2^{A} can be measured experimentally on samples of the ligand prepared without adding the NP). Therefore, data modelling returns R_1^{B}, R_2^{B}, $\varOmega^{\mathrm{A}}$, $\varOmega^{\mathrm{B}}$, k_1, and k_{-1}. The thermodynamics of the equilibrium can be calculated from the modelled parameters using the equations:

$$
p_{\mathrm{B}} = \frac{k_1}{k_{\mathrm{ex}}}
\tag{33}
$$

$$
p_{\mathrm{A}} = \frac{k_{-1}}{k_{\mathrm{ex}}}
\tag{34}
$$

The DEST experiment is an excellent method for detecting and characterizing large systems that are NMR-invisible due to their fast relaxation rates. Since the DEST experiment uses a relatively high saturation field strength (larger than 100 Hz) to maximize the detection of the NMR-invisible state (Fig. 8), the difference in chemical shift between the states in chemical exchange is usually not resolved[154] (note that this is the main difference between DEST and CEST,[194] another saturation transfer NMR experiment that uses low saturation field strengths to resolve chemical shift differences between chemical states with similar R_2's). Therefore, when modelling DEST profiles, $\varOmega_{\mathrm{A}}$ and $\varOmega_{\mathrm{B}}$ are often considered to be equal in order to reduce the number of variable parameters. Also, it is important to highlight that if the R_2 of the bound state is smaller than the applied saturation field, p_{B} and R_2^{B} cannot be determined independently with the DEST experiment alone, and additional experimental data are needed to decorrelate the two parameters.[195] Alternatively, the two parameters can be decorrelated by calculating R_2^{B} based on the rotational correlation time of the NP (τ_{NP}) that can be estimated by using the average size of the NP and the Stoke–Einstein equation.

DEST can characterize the exchange between a small molecule and a large receptor occurring on the slow timescale (ms–s) at the condition that k_{ex} is faster than R_1 (which implies that the exchange from free to bound and back to the free state has to occur before the longitudinal magnetization is lost via R_1 relaxation). For completeness, it should be mentioned that DEST data can also be acquired for systems exchanging on a fast timescale ($k_{\mathrm{ex}} > 1000$ s^{-1}).[154] However, as in a fast exchanging system, one single peak is observed with a population-averaged R_2^{obs} (eqn (11)), the R_2 of the bound state must be small to avoid the complete loss of the NMR signal.

Compared to STD NMR, the main limitation of DEST is the need to use heteronuclei for the saturation step, which limits its sensitivity and increases the experimental acquisition time. Indeed, when using ^{1}H DEST, the fast ^{1}H spin diffusion can cause unwanted intra and intermolecular magnetization transfers that complicate modelling of the experimental data.[189,192] To avoid this issue, several 2D and 1D proton detected pulse sequences were developed to perform ^{13}C or ^{15}N DEST

experiments on proteins and small molecules.[190,192,196] The pulse sequence used for 1D ^{13}C DEST is shown in Fig. 9. Although less sensitive than STD, the DEST experiment holds the advantage of not requiring a transfer of saturation from the NP to the ligand *via* spin diffusion, which allows investigation of non-protonated receptors such as metal and metal oxides NPs.

In recent years, several applications of DEST to the investigation of ligand adsorption on NPs were reported. Ceccon *et al.* determined the kinetics and thermodynamics of adsorption of the huntingtin peptide over titanium(IV) oxide (TiO_2) NPs by simultaneous analysis of ^{15}N DEST and ΔR_2 (difference in R_2 of the free state in the absence and the presence of NP – see below) data.[197] Similarly, using ^{15}N DEST, ΔR_2, and exchange-induced chemical shift, Hassan *et al.* characterized the dynamics and exchange kinetics of the interaction between ubiquitin and mercaptosuccinic acid-capped CdTe quantum dots.[198] The DEST experiment has also been used to investigate the structures of the surface-bound species. For example, we used ^{13}C DEST in combination with other NMR relaxation methods to characterize not only the kinetics and thermodynamics of binding but also the structure of phenol (PhOH) adsorbed on the surface of ceria (CeO_2) and Pd on ceria (Pd/CeO_2) NPs.[192] With the combination of ^{1}H DEST and molecular dynamics (MD) simulations, Xue *et al.* determined the adsorption mode of different amino acids on the surface of TiO_2 NPs.[199]

NMR relaxation

NMR relaxation is one of the most prevalent methods to study macromolecular dynamics due to its extreme sensitivity to molecular motions.[200–205] Since the overall tumbling and internal motions of a molecule are often significantly perturbed by the surface interaction (*e.g.*, decrease in molecular mobility of the ligand upon binding to NP surface), NMR relaxation makes an ideal method for detecting and characterizing adsorption processes in solution. This section will discuss how relaxation-based NMR methods have been applied to small molecule–NP systems. We will focus our attention on the R_1, R_2, and relaxation dispersion experiments.

Transverse relaxation (R_2). As discussed above, the transverse relaxation rate of a ligand is enhanced by chemical exchange with an NMR-invisible NP-associated state. Since the increase in R_2 of the free ligand reflects the properties of the bound state (*e.g.*, population, binding kinetics, and internal flexibility), the measured transverse relaxation can be used to characterize the ligand–NP interaction. In particular, the relevant observable is the increase in R_2 upon addition of NP (ΔR_2) measured as:

$$\Delta R_2 = R_2^{NP} - R_2^{noNP} = R_2^{NP} - R_2^{A} \tag{35}$$

where R_2^{NP} and R_2^{noNP} are the R_2 values measured for the free ligand NMR signals in the presence and in the absence of the
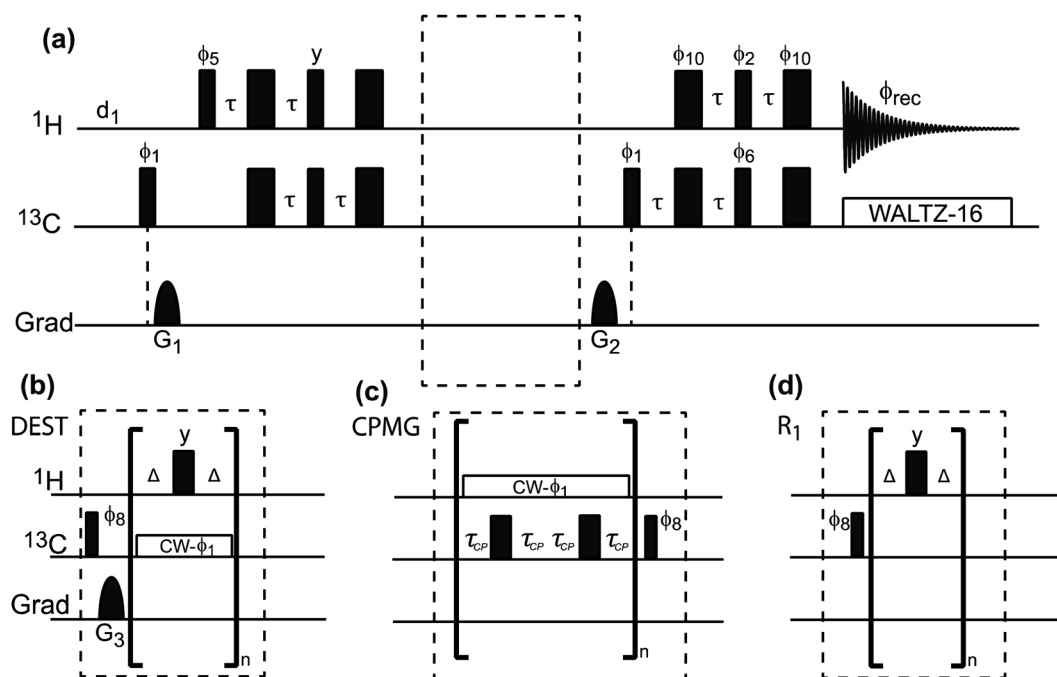

Fig. 9 (a) Pulse sequences used to measure proton-detected 1D ^{13}C DEST, CPMG, and R_1 experiments. Each experiment is measured by inserting the blocks shown in (b)–(d) into the dashed box shown in the double refocused-INEPT based sequence. Full details on the pulse sequences are available in Egner *et al.*[192] In the DEST experiment, CW represents the continuous wave used for saturation. During the saturation period, a train of 180° pulse (represented by the thicker rectangular-shaped pulse) is applied in the ^{1}H channel to remove relaxation artifacts coming from the [1]H–[13]C dipolar interaction. In the CPMG experiment, τ_{CP} is a variable parameter that determines the CPMG field ($\nu_{CPMG} = 1/4\tau_{CP}$ Hz). The CW applied in the CPMG experiment is for ^{1}H decoupling. The phase cycling employed is: $\phi_1 = (x, -x)$; $\phi_2 = 2(x), 2(-x)$; $\phi_5 = 8(x), 8(-x)$; $\phi_6 = 4(y), 4(-y)$; $\phi_8 = (y, -y)$; $\phi_{10} = 16(x), 16(-x)$; $\phi_{rec} = 2(x), 4(y), 2(x), 2(y), 4(x), 2(y)$. The duration and strength of the gradients are as follows: G_1, 1 ms, 30 G cm^{-1}; G_2, 0.05 ms, 35 G cm^{-1}; G_3, 0.1 ms, 40 G cm^{-1}.

NP, respectively. In the fast exchange regime, $\Delta R_2 = R_{\text{IIb}}$ (eqn (15)) and can be linked to the fractional populations of desorbed and adsorbed species and to their transverse relaxation rates using the formula:

$$\Delta R_2 = p_B(R_2^B - R_2^A) \sim p_B R_2^B \tag{36}$$

Therefore, R_2^B and the concentrations of free and bound ligand (C_L and q_{LS} in eqn (3)) can be obtained by modelling ΔR_2 data with eqn (36). As discussed above, in the slow exchange regime, if $R_2^B > k_{-1}$, $\Delta R_2 = R_{\text{IIb}} = k_1$ (eqn (17)). However, if the transverse relaxation rate of the NP-bound state is not sufficiently fast to destroy all magnetization (i.e. if $R_2^B < k_{-1}$), then the enhancement to the transverse relaxation rate will be less than k_1. In the case $p_A \gg p_B$ (which is very common in solution NMR investigation of sorption – see above), it can be shown that:[206]

$$\Delta R_2 = R_{\text{IIb}} = \frac{k_1(R_2^B - R_2^A)}{k_{-1} + (R_2^B - R_2^A)} \tag{37}$$

which is valid for both the fast and slow timescale regimes. However, it is important to note that in the most common scenario of the intermediate exchange regime, the experimental ΔR_2 is enhanced by R_{ex} (eqn (12) and (13)), and, if the exchange contribution cannot be completely suppressed by the pulse sequence used to measure R_2 (i.e. using a spinlock field of sufficient strength), the Bloch–McConnell equation should be used to model R_{ex} into the data analysis (see below).

Although the ΔR_2 values are often analyzed in combination with datasets from other NMR experiments (i.e. DEST and relaxation dispersion), a few standalone applications of ΔR_2 for quantitative investigation of sorption equilibria are available in the literature. Ceccon et al. have used ΔR_2 to investigate the adsorption of ubiquitin on liposome NPs.[191] Using the distribution of ^{15}N ΔR_2 along the amino acid sequence, they showed that ubiquitin undergoes fast rigid-body rotation about an internal axis while bound to the surface of the NP. In addition, using paramagnetically labeled NPs, they used ΔR_2 to measure the dipolar interaction between the protein and the paramagnetic center, which allowed the determination of the ubiquitin residues in direct contact with the NP surface. Xie and Brüschweiler used ^{13}C ΔR_2 to investigate how ligand modifications affect binding to silica NPs.[207] In particular, they used the fact that in the fast exchange regime $p_B \sim \Delta R_2/R_2^B$ (eqn (36)) to obtain the free energy of adsorption for a variety of ligand–NP interactions. We have shown that, if predicted binding modes are available for a ligand–NP system, a standalone interpretation of ΔR_2 can be used to obtain a semi-quantitative analysis of sorption based on the use of scaling factors that depend on the amount of small molecule in each binding mode.[208] Using this approach, we determined that functionalization of PhOH with an oxygen at position 2 or 4 greatly enhances adsorption on the Pd or CeO$_2$ component of Pd/CeO$_2$ nanorods, respectively.

Carr–Purcell–Meiboom–Gill (CPMG) relaxation dispersion (RD). RD relies on measuring the transverse relaxation at increasing repetition rate of 180° refocusing pulses to progressively suppress the R_{ex} contribution to the R_2 of a system in chemical exchange on the intermediate timescale ($k_{\text{ex}} \sim \Delta\omega \neq$

0).[154] In CPMG RD, the CPMG field is introduced as a series of refocusing 180° pulses spaced by a constant delay ($2\tau_{\text{CP}}$) (Fig. 9). As the CPMG field is equal to $1/4\tau_{\text{CP}}$, an RD profile can be obtained experimentally by plotting the R_2 measured at different τ_{CP} values as a function of the CPMG field. Fig. 10a shows an ideal RD profile simulated for the NMR-visible signal of a small molecule in an exchange between the desorbed and NP-adsorbed state on the intermediate timescale. The R_2 of such signal will be enhanced compared to the one measured in the absence of NP by both R_{ex} and R_{IIb}:

$$R_2^{\text{obs}} = R_2^A + \Delta R_2 = R_2^A + R_{\text{ex}} + R_{\text{IIb}} \tag{38}$$

Progressive suppression of R_{ex} by increasing the CPMG field introduces a curvature in the RD profile that plateaus when $R_{\text{ex}} \sim 0 \text{ s}^{-1}$ (note that only in this condition the experimental $\Delta R_2 = R_{\text{IIb}}$).

Fig. 10b shows the RD profiles simulated for two-state sorption equilibria occurring on different timescales. If the exchange is fast or slow on the chemical shift timescale ($k_{\text{ex}} \gg \Delta\omega$ or $k_{\text{ex}} \ll \Delta\omega$, respectively), $R_{\text{ex}} \sim 0 \text{ s}^{-1}$ and $R_2^{\text{obs}} = R_2^A + R_{\text{IIb}}$ for any CPMG field. However, within these limits, the shape of the RD profile is very sensitive to the timescale of the equilibrium, and modelling of experimental RD datasets can provide information on the kinetics and thermodynamics of sorption. The R_2 at any specific value of τ_{CP} can be calculated using the formula:

$$R_2 = \frac{1}{(t_2)} \ln\left[\frac{M(0)}{M(t_2)}\right] \tag{39}$$

where $M(0)$ and $M(t_2)$ are the transverse magnetization calculated for a duration of the CPMG block of 0 and t_2 s, respectively. $M(0)$ and $M(t_2)$ are the first elements of vectors $\mathbf{M}(0)$ and $\mathbf{M}(t_2)$, respectively:

$$\mathbf{M}(0) = \begin{bmatrix} M^A \\ M^B \end{bmatrix} \tag{40}$$

$$\mathbf{M}(t_2) = (AA^*A^*A)^n \mathbf{M}(0) \tag{41}$$

where M^A and M^B represent the transverse magnetizations of states A and B, respectively, n is the number of CPMG cycles used (see Fig. 9), A^* the complex conjugate of A, and A is given by:

$$A = e^{-R\tau_{\text{CP}}/2} \tag{42}$$

R is given by:

$$R = iR^{\text{CS}} + R^{\text{rel}} + R^{\text{ex}} \tag{43}$$

with

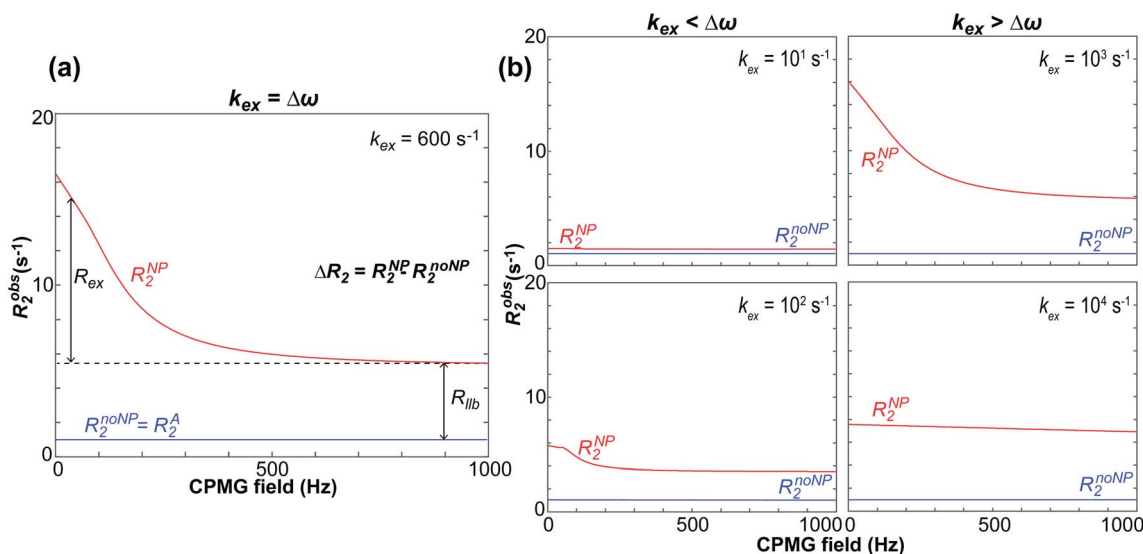$$R^{\text{CS}} = \begin{bmatrix} 0 & 0 \\ 0 & -\Delta\omega \end{bmatrix} \tag{44}$$

Fig. 10 Simulated CPMG relaxation dispersion curves over a range of k_{ex} values. The curves are shown as red solid lines for a two-site sorption equilibrium where the NMR-visible desorbed species is observed. The simulations were obtained with $R_2^A = 1$ s^{-1}, $R_2^B = 100$ s^{-1}, $p_B = 0.05$, and $\Delta\omega$ = 600 rad s^{-1}. The RD profile simulated in the absence of exchange between desorbed and adsorbed states (corresponding to the RD profile obtained in the absence of NP) is shown as a blue solid line. In (a) the RD curve for a system in the intermediate exchange regime ($k_{ex} = \Delta\omega$) is shown. The R_{llb} and R_{ex} contributions to ΔR_2 are shown as black solid lines. In (b) RD profiles simulated for the slow ($k_{ex} \ll \Delta\omega$, left column) and fast ($k_{ex} \gg \Delta\omega$, right column) exchange regimes are shown.

$$\boldsymbol{R}^{\text{rel}} = \begin{bmatrix} R_2^A & 0 \\ 0 & R_2^B \end{bmatrix} \qquad (45)$$

$$\boldsymbol{R}^{\text{ex}} = \begin{bmatrix} k_1 & -k_{-1} \\ -k_1 & k_{-1} \end{bmatrix} \qquad (46)$$

Modelling an RD profile returns R_2^B, $\Delta\omega$, k_1, and k_{-1} (note that R_2^A can be measured experimentally on samples of the ligand prepared without adding the NP). p_A and p_B can be obtained from the modelled parameters using eqn (33) and (34).

Although CPMG RD is commonly applied to characterize chemical exchange with k_{ex} values between 200 and 2000 s^{-1}, the method performs best for processes occurring on the intermediate to slow timescale.[154] Indeed, in the intermediate to fast regime, $\Delta\omega$ and p_B cannot be accurately modelled by a single CPMG data set, and it is common to acquire RD data at multiple static fields and external temperatures to improve the accuracy of modelling.[154,209] Also, when possible, it is preferable to measure RD profiles on ^{1}H spins. On conventional NMR spectrometers, the proton channel can sustain higher CPMG fields compared to channels dedicated to heteronuclei, which allows more efficient suppression of R_{ex} for intermediate to fast exchange processes. Also, given the high gyromagnetic ratio, ^{1}H spins tend to have larger $\Delta\omega$, which increases the ability of the RD method to detect and characterize exchange processes with small p_B and large k_{ex}. A pulse sequence for acquisition of 1D ^{1}H CPMG experiments on small molecule–NP systems is shown in Fig. 11.

Although CPMG RD has been one of the most popular methods to characterize protein conformational

equilibria,[210–216] its standalone application to the characterization of ligand–NP systems has been quite limited. Recently, CPMG RD has been combined with DEST, ΔR_2, and R_1 data to investigate sorption equilibria involving both protein and small molecule ligands.[155,192,217]

Longitudinal relaxation (R_1). Compared to R_2, the longitudinal relaxation is less sensitive to chemical exchange. Therefore, changes in R_1 upon adsorption are rarely analyzed. Nonetheless, as an estimate for R_1^B is obtained from the analysis of DEST (see above), measuring the R_1 of the NMR-visible ligand peaks in the absence ($R_1^{noNP} = R_1^A$) and in the presence (R_1^{NP}) of NPs can provide additional experimental restraints for modelling sorption equilibria.

R_1 can be obtained from inversion recovery experiments.[218,219] A pulse sequence for the 1D proton-detected ^{13}C R_1 experiment applied to small molecule–NP systems is shown in Fig. 9. In the presence of exchange between the free and NP-
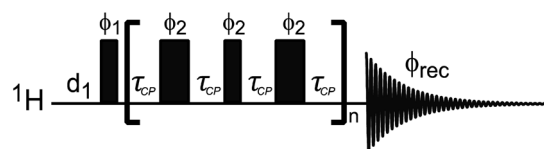

Fig. 11 PROJECT pulse sequence used for ^{1}H CPMG spectra of small molecules.[229] The narrow and wide rectangular-shaped pulses represent 90° and 180° pulses, respectively. The 90° pulse sandwiched between the refocusing CPMG pulses is used to suppress modulation from homonuclear scalar coupling. τ_{CP} is a variable parameter that determines the CPMG field ($\nu_{CPMG} = 1/4\tau_{CP}$ Hz). The phase cycling employed is: $\phi_1 = 2(x), 2(y), 2(-x), 2(-y)$; $\phi_2 = y, -y, y, -y, x, -x, x, -x$; $\phi_{rec} = 2(x), 2(-x), 2(y), 2(-y)$.

bound state, the experimental R_1^{NP} of the ligand can be modelled according to the following equation:

$$R_1 = \frac{1}{(t_2)} \ln\left[\frac{M(0)}{M(t_2)}\right] \quad (47)$$

where $M(0)$ and $M(t_2)$ are the detected magnetizations when the relaxation delay ($2n\Delta$ in Fig. 9d) is set to 0 and t_2 s, respectively. $M(0)$ and $M(t_2)$ are the first elements of vectors $\boldsymbol{M}(0)$ and $\boldsymbol{M}(\boldsymbol{t_2})$, respectively:

$$\boldsymbol{M}(0) = \begin{bmatrix} M^A \\ M^B \end{bmatrix} \quad (48)$$

$$\boldsymbol{M}(t_2) = (AA^*A^*A)\boldsymbol{M}(0) \quad (49)$$

Here, M^A and M^B represent the initial magnetizations of states A and B, respectively, A^* represents the complex conjugate of A, and A is given by:

$$A = \mathrm{e}^{-\boldsymbol{R}t_2} \quad (50)$$

where $\boldsymbol{R}$ is given by the summation:

$$\boldsymbol{R} = \boldsymbol{R}^{rel} + \boldsymbol{R}^{ex} \quad (51)$$

with

$$\boldsymbol{R}^{rel} = \begin{bmatrix} R_1^A & 0 \\ 0 & R_1^B \end{bmatrix} \quad (52)$$

$$\boldsymbol{R}^{ex} = \begin{bmatrix} k_1 & -k_{-1} \\ -k_1 & k_{-1} \end{bmatrix} \quad (53)$$

Modelling the ligand–NP adduct. In the sections above, we have discussed how modelling DEST, RD, R_1, and/or R_2 data measured for the NMR-visible signals of a free ligand in the presence of chemical exchange with a NP-bound state returns the thermodynamic (p_A and p_B) and kinetic (k_1 and k_{-1}) parameters of sorption. In addition, such analysis returns information on the structure and dynamics of the surface-bound species encoded in the modelled R_1^B and R_2^B values. Indeed, when the exchange contribution is completely suppressed, NMR relaxation is induced by the modulation of magnetic interactions caused by molecular motions occurring on the ps–ns timescale. In the case of spin-half nuclei in a diamagnetic system, the relevant magnetic interactions are dipolar couplings and chemical shift anisotropy (CSA).

For an isolated ^1H–^{13}C (or ^1H–^{15}N) bond vector, the ^{13}C (or ^{15}N) R_1 and R_2 are linked to the molecular dynamics using the model-free method developed by Lipari and Szabo:[220,221]

$$R_1 = \frac{d^2}{4}\left(J(\omega_H - \omega_C) + 3J(\omega_C) + 6J(\omega_C + \omega_H)\right) + c^2 J(\omega_C) \quad (54)$$

$$R_2 = \frac{d^2}{8}\Big(4J(0) + J(\omega_H + \omega_C) + 3J(\omega_C) + 6J(\omega_H)$$
$$+ 6J(\omega_C + \omega_H)\Big) + \frac{c^2}{6}\left(4J(0) + 3J(\omega_C)\right) \quad (55)$$

where

$$d = \frac{\mu_0}{4\pi}\hbar\gamma_C\gamma_H r^{-3} \quad (56)$$

$$c = \frac{\gamma_C B_0 \Delta\sigma}{\sqrt{3}} \quad (57)$$

Here, μ_0 is the magnetic permeability, $\hbar$ is the reduced Planck's constant, γ_n is the gyromagnetic ratio of the n nucleus, r is the internuclear bond distance, and $\Delta\sigma$ is the chemical shift anisotropy. $J(\omega)$ represents the spectral density function which describes how much local field is oscillating at the given frequency:

$$J(\omega) = \frac{2}{5}S^2\left[\frac{\tau_{NP}}{1 + \tau_{LNP}^2\omega^2}\right] + \frac{2}{5}\left(1 - S^2\right)\left[\frac{\tau_e}{1 + \tau_e^2\omega^2}\right] \quad (58)$$

where S^2 is a generalized order parameter representing the spatial restriction of the internal motion, τ_{LNP} is the correlation time of the ligand in a rigid interaction with the NP, and τ_e is the effective correlation time of the C–H (or N–H) bond vector given by:[191]

$$\frac{1}{\tau_{LNP}} = \frac{1}{\tau_{NP}} + k_1 + k_{-1} = \frac{1}{\tau_{NP}} + k_{ex} \quad (59)$$

$$\frac{1}{\tau_e} = \frac{1}{\tau_{LNP}} + \frac{1}{\tau_{loc}} \quad (60)$$

where τ_{NP} and τ_{loc} are the correlation time of the NP and of the local motion, respectively. In the model-free approach, if the motion of the C–H bond vector is restricted (*i.e.* the C–H bond is rigidly attached to the NP surface), $S^2 \sim 1$ and the overall tumbling of the NP and binding kinetics are the only contribution to relaxation (*i.e.*, τ_{LNP} is the only correlation time modulating the magnetic interactions – eqn (58)). On the other hand, if the C–H bond vector is highly flexible, $S^2 \sim 0$ and relaxation is determined by both τ_{LNP} and τ_{loc}.

Modelling ^{13}C and ^{15}N relaxation rates using the model-free approach was used to investigate the molecular dynamics of PhOH bound to CeO_2 and Pd/CeO_2 NPs[192,208] and of the protein ubiquitin adsorbed on liposome NPs.[191] However, it is important to notice that eqn (54)–(60) only apply to the spin-half heteronuclei covalently attached to single hydrogen (*i.e.* protein backbone amides, CH groups in aromatic rings, *etc.*), and more complex models are required for more complex systems.

Combining solution NMR experiments

Several solution NMR experiments have been described above that investigate chemical exchange processes occurring on different timescales. In particular, chemical shift analysis is very powerful for characterizing fast chemical exchange, CPMG RD is particularly suited for intermediate to slow exchange, while saturation transfer methods (STD and DEST) and the analysis of peak intensities work best for processes in the slow exchange regime. In addition to these methods, analysis of DOSY, ΔR_1 and ΔR_2 experiments can report on the chemical exchange between desorbed and NP-adsorbed states on a broad

range of timescales (Fig. 12). Although using these methods as standalone techniques can provide important insight into sorption equilibria, the utility of combining two or more NMR experiments sensitive to different timescales for investigating surface adsorption was demonstrated in several applications. Indeed, adsorption on a heterogeneous surface is often a complex process involving multiple intermediate states and adsorbed species in chemical exchange (among themselves and with the desorbed state) on different timescales, and the combined analysis of different NMR observables can help to deconvolute the contribution of each elementary step to surface adsorption. For example, Libich *et al.* investigated the interaction of the polypeptide amyloid β (Aβ40) with the molecular chaperone GroEL by using a combination of ^{15}N ΔR_2, ^{15}N DEST, ^{15}N CPMG RD, and exchange-induced chemical shift change analysis.[217] They showed that since these methods depend differently on the kinetics and thermodynamics of adsorption, their combined analysis increased the stability of data modelling and the precision of the fitted parameters. In addition, by combining ^{15}N ΔR_2, ^{13}C and ^{15}N DEST, and ^{1}H, ^{13}C, and ^{15}N CPMG RD, Libich *et al.* investigated the chaperonin activity of GroEL, demonstrating that the molecular machinery accelerates the interconversion between the native and partially folded states of a triple mutant of the Fyn SH3 domain.[222] Another series of studies explored the combination of ^{1}H R_1 and R_2 for investigating sorption in porous materials.[223] It was found that the ^{1}H R_2/R_1 ratio of ligands in saturated porous media provides information on the residence time of the NMR-visible small molecule inside the pore and on the energy of adsorption.[224]

In the following section, we highlight how the combination of ^{13}C R_1, ^{13}C R_2, ^{13}C DEST, and ^{1}H and ^{13}C CPMG RD was used to investigate small molecule–NP sorption with atomic resolution. In particular, using the interaction between PhOH and Pd/CeO$_2$ nanocubes as the model system, we will illustrate the combined use of multiple NMR methods to obtain kinetic, thermodynamic, and structural information on adsorption/desorption equilibria involving multiple elementary steps occurring on multiple timescales.

Application to the PhOH–Pd/CeO$_2$ system

Pd/CeO$_2$ NPs catalyze the hydrogenation of PhOH under mild reaction conditions (1 bar H$_2$ at room temperature) more efficiently than other Pd-based catalysts.[225] However, it is unclear whether the outstanding performance of Pd/CeO$_2$ is due to a higher dispersion of the Pd catalyst, better adsorption of PhOH on the catalyst surface, beneficial electronic effects of ceria on the supported metal, or a direct contribution of ceria in catalysis *via* H$_2$ spillover. To help address this question, in the last few years, we conducted a series of studies aimed at characterizing the adsorption of PhOH on Pd/CeO$_2$ NPs by solution NMR.[155,192,208,226]

Initially, we focused on studying the binding of PhOH onto bare CeO$_2$ NPs of cubic morphology using ^{1}H DEST and ^{1}H CPMG RD.[155] We noticed that the data could not be modelled using a two-site exchange mechanism and that expansion of the Bloch–McConnell matrices to account for the existence of two adsorbed species in chemical exchange with the desorbed state was required in order to fully reproduce the ^{1}H DEST profile. However, due to the high sensitivity of ^{1}H DEST to spin diffusion that overemphasizes contributions from surface-bound species and complications in modelling ^{1}H relaxation, an accurate determination of the kinetic, thermodynamic, and structural parameters of sorption was not obtained in this initial study.

In a follow-up study, we combined ^{1}H and ^{13}C CPMG RD, ^{13}C DEST, and ^{13}C R_1 experiments to investigate the adsorption of PhOH on CeO$_2$ and Pd/CeO$_2$ NPs of cubic morphology.[192] Consistent with our preliminary investigation using ^{1}H DEST, modelling of the data required a two-step adsorption process in which the desorbed species is in equilibrium with tightly adsorbed PhOH *via* a weakly associated intermediate state (Fig. 13). It is important to note that simultaneous analysis of all datasets was key to the determination of the two-step binding mechanism. Indeed, a one-step binding model was sufficient to describe the ^{1}H CPMG RD, ^{13}C DEST, and ^{13}C R_1 (but not the ^{13}C CPMG RD) measured for PhOH–CeO$_2$, or the ^{1}H and ^{13}C CPMG RD and ^{13}C R_1 (but not the ^{13}C DEST) measured for PhOH–Pd/
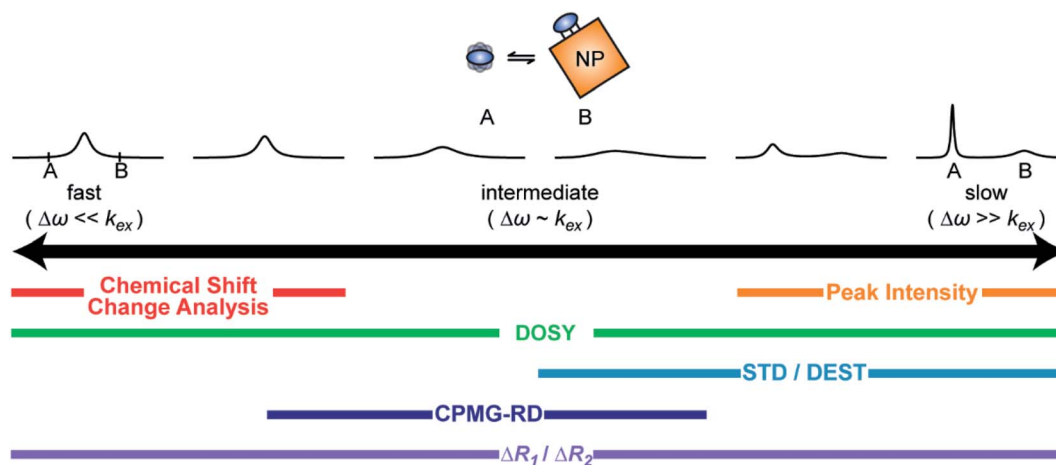

Fig. 12 Summary of solution NMR experiments for investigating sorption equilibria occurring on different exchange regimes.
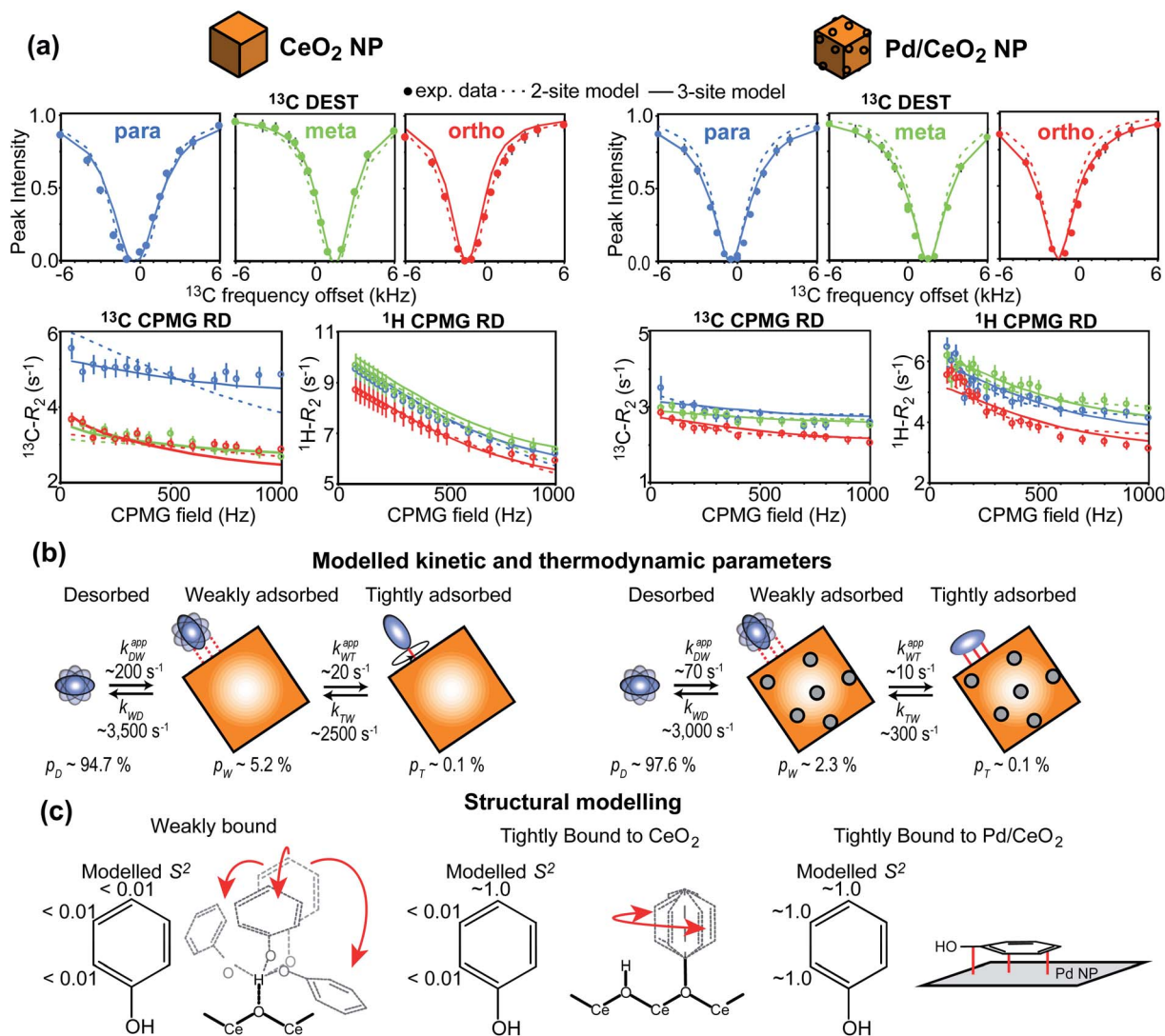
Fig. 13 Combined analysis of ^{13}C R_1, ^{13}C R_2, ^{13}C DEST, and ^1H and ^{13}C CPMG RD experiments on the PhOH–Pd/CeO$_2$ system. (a) ^{13}C DEST (saturation field strength = 1 kHz) and ^1H and ^{13}C CPMG RD profiles of PhOH in the presence of 1 wt% CeO$_2$ (left) and 1 wt% Pd/CeO$_2$ (right) NPs. Data were collected at 800 MHz. Experimental data for the *para*, *meta*, and *ortho* C–H bonds are represented in blue, green, and red circles, respectively. The dotted and solid lines represent the best fit to a two-site and three-site exchange model, respectively. (b) Modelled kinetic and thermodynamic parameters for PhOH adsorption on CeO$_2$ (left) and Pd/CeO$_2$ (right) NPs. PhOH is a blue oblate, CeO$_2$ is an orange square, and Pd sites are gray spheres. (c) Structural modelling of PhOH adsorbed on the CeO$_2$ and Pd/CeO$_2$ surface. The order parameter (S^2) obtained for each C–H group is shown. Adapted from Egner *et al.*[192]

CeO$_2$ (Fig. 13a). Removing spin-diffusion artifacts from the DEST experiment allowed for accurate modelling of the kinetics and thermodynamics of adsorption as well as for determination of the ^{13}C R_1 and R_2 values for PhOH in the NP-associated states (Fig. 13b). Next, we used the modelled R_1 and R_2 to calculate the order parameter for each C–H bond in the weakly and tightly associated state by eqn (54)–(60) (Fig. 13c). Analysis of the S^2 values indicated that irrespective of the NP, all C–H groups are highly mobile in the weakly associated state ($S^2 < 0.01$), which suggested that this intermediate species consists of PhOH hydrogen-bonded to the CeO$_2$ component of the NP (Fig. 13c, left). On the other hand, we noticed that the S^2 values obtained for PhOH tightly associated with CeO$_2$ are position-dependent, with very low S^2 values (<0.01) for the *ortho* and *meta* positions,

and $S^2 \sim 1$ for the *para* position. This S^2 trend (which is linked to the high ^{13}C R_2 measured for the para carbon – Fig. 13a) revealed that while the ortho and meta C–H groups reorient fast relative to the external magnetic field, the para C–H bond reorients with the same correlation time as the NP (see eqn (58)). These considerations brought us to conclude that PhOH associates tightly to CeO$_2$ by inserting the O atom into O-vacancies present on the NP surface. Indeed, the latter interaction mode keeps the *para* C–H group rigid with respect to the NP surface while allowing fast reorientation of the *meta* and *ortho* C–H bonds (Fig. 13c, middle). Finally, the modelling of the relaxation rates returned an $S^2 \sim 1$ for all C–H bonds of PhOH tightly associated with Pd/CeO$_2$. Such observation indicated that the molecule is rigidly attached to the NP and confirmed
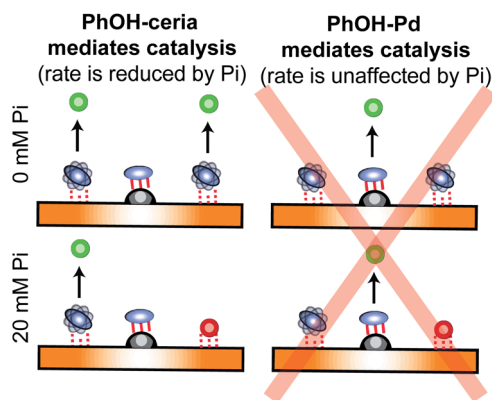
Fig. 14 Graphic representation of how the direct participation of CeO_2 in catalysis was revealed by the addition of inorganic phosphate (Pi). PhOH is a blue oblate, the product of the reaction (cyclohexanone or cyclohexanol) is a green circle, the CeO_2 surface is shown as an orange rectangle, the Pd site is a gray half sphere, and Pi is a red circle. The NMR data revealed that while the addition of 20 mM Pi reduced the population of weakly bound PhOH–CeO_2 intermediate by ~50%, it did not affect the population and exchange kinetics of PhOH tightly bound to Pd. Since the rate of PhOH hydrogenation catalyzed by Pd/CeO_2 is also reduced by ~50% by the addition of 20 mM Pi, the results reported in Egner et al.[192] suggest that the weak PhOH–CeO_2 interaction is catalytically relevant.

a "flat" binding of PhOH to Pd hypothesized by *ab initio* calculations (Fig. 13c, right).[227] In the same work, we have tested the proposed binding models by reacquiring the NMR data in the presence of 20 mM inorganic phosphate, which binds strongly to CeO_2 but does not interact with Pd.[228] We found that the addition of phosphate reduced the population of PhOH weakly bound to CeO_2 and Pd/CeO_2, and completely abolished the interaction of PhOH with O-vacancies on CeO_2. However, the population and exchange kinetics of PhOH tightly bound to Pd/CeO_2 were unaffected by the presence of phosphate, confirming that the tight adsorption of PhOH on Pd/CeO_2 is mediated by contacts between PhOH and the Pd component of the NP.

Finally, in order to address the possible direct involvement of CeO_2 in catalytic conversion of PhOH, we compared the kinetics of substrate hydrogenation measured in the presence and in the absence of 20 mM phosphate with the adsorption data obtained by solution NMR. The rationale for this comparison was that reaction rates are proportional to the concentration of active substrate–catalyst complex in solution. Therefore, we expected the reaction rate to be reduced in the presence of phosphate if catalysis is mediated by interactions between PhOH and CeO_2 (Fig. 14). The results of our experiment confirmed this scenario and revealed an active role for the support in catalytic hydrogenation of PhOH by Pd/CeO_2.

Conclusions

As applications of NP catalysts continue to expand, understanding sorption equilibria has become of utmost importance since the efficiency and selectivity of NP catalysis are highly dependent on the interactions that substrates, intermediates, and products establish with the NP surface. Over recent years, solution NMR spectroscopy is emerging as a powerful method for detecting and characterizing small molecule–NP interactions due to its exceptional sensitivity to molecular motions and capability of observing dynamic processes over a wide range of timescales. Through this comprehensive review of various solution NMR techniques for characterizing small molecule–NP interactions, we illustrated procedures for stable NMR sample preparation of insoluble NPs, introduced theoretical and practical aspects of the relevant NMR experiments, discussed how the combined analysis of multiple NMR methods can provide mechanistic insight into sorption equilibria involving multiple elementary steps, and reviewed a number of practical applications. We believe solution NMR spectroscopy has a bright future ahead in the investigation of ligand–NP interactions, and we expect it to become a crucial investigative tool for the development of new generations of heterogeneous catalysts.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

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