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# Observation of suppressed diffuson and propagon thermal conductivity of hydrogenated amorphous silicon films

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Hydrogenated amorphous silicon (a-Si:H) has drawn keen interest as a thin-film semiconductor and superb passivation layer in high-efficiency silicon solar cells due to its low cost, low processing temperature, high compatibility with substrates, and scalable manufacturing. Although the impact of hydrogenation on the structural, optical, and electronic properties of a-Si:H has been extensively studied, the underlying physics of its impact on the thermal properties is still unclear. Here, we synthesize a-Si:H films with well-controlled hydrogen concentrations using plasma-enhanced chemical vapor deposition and systematically study the thermal conductivity of these a-Si:H films using time-domain thermoreflectance. We find that the reduction of thermal conductivity of a-Si:H films is attributed to the suppression of diffuson and propagon contributions as the hydrogen concentration increases. At the maximum hydrogen concentration of 25.4 atomic percentage, the contributions from diffusons and propagons to the thermal conductivity are decreased by 40% (from 1.10 to 0.67 W m<sup>-1</sup> K<sup>-1</sup>) and 64% (from 0.61 to 0.22 W m<sup>-1</sup> K<sup>-1</sup>), respectively. Such a significant reduction in the thermal conductivity of a-Si:H originates from the hydrogen induced material softening, the decrease in density, and phonon-defect scattering. The results of this work provide fundamental insights into the thermal transport properties of a-Si:H thin films, which is beneficial for the design and optimization of amorphous silicon-based technologies including photovoltaics, large-area electronics, and thermoelectric devices.

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## 1. Introduction

Amorphous silicon deposited *via* plasma-enhanced chemical vapor deposition (PECVD) contains a certain amount of hydrogen stemming from the silane (SiH<sub>4</sub>) precursor and is therefore called “hydrogenated amorphous silicon (a-Si:H)”. Compared to hydrogen-free amorphous silicon (a-Si), such as that deposited by sputtering, the hydrogen in a-Si:H greatly improves its electrical properties by terminating the dangling bonds and modifying its degree of short-range order,<sup>1–3</sup> making it a promising material candidate for thin-film semiconductor devices.<sup>4–9</sup> Despite its poorer electronic properties compared to those of crystalline silicon (c-Si), a-Si:H offers significant technical advantages including low manufacturing cost, low processing temperature, and great compatibility with flexible substrates and large-scale electronic manufacturing. Therefore, a-Si:H has received extensive interest leading to numerous studies focusing on its structural, optical, and electronic properties.<sup>10–14</sup>

The performance and reliability of semiconductor devices largely depend on their operating temperature, dictated by their thermal properties.<sup>15–17</sup> This is more important for amorphous materials since their low thermal conductivity<sup>18,19</sup> can result in considerably higher operating temperatures that are detrimental for devices.<sup>20</sup> Therefore, extensive research has been conducted to understand the thermal transport in a-Si films, which report a strong size-dependent thermal conductivity attributed to the contribution of long mean free path (MFP) propagons.<sup>21–23</sup> Due to the presence of H atoms, the thermal properties of a-Si:H can be significantly different from those of a-Si.<sup>24,25</sup> However, a systematic study of the impact of hydrogen on the thermal transport mechanisms and heat carrier characteristics of a-Si:H is still lacking. Although the thermal conductivity of a-Si:H films was reported in several studies,<sup>24,26,27</sup> an in-depth understanding of the impact of H atoms on the contribution of different heat carriers to the thermal transport in a-Si:H films is still lacking.

In this work, a-Si:H films with various H concentrations ( $\epsilon_{\text{H}}$ ) are prepared in a PECVD reactor at different substrate temperatures. Fourier transform infrared spectroscopy (FTIR) is used to examine the H bonding configuration and total H concentration in the films. The thermal conductivities of these films before and after annealing are measured with the ultrafast

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laser-based time-domain thermoreflectance (TDTR) technique.<sup>28,29</sup> The impact of H atoms on the contributions of different heat carriers to the thermal conductivity of a-Si:H films is discussed in detail, based on the interpretation of measurement data assisted by theoretical modelling.

## 2. Sample preparation and characterization

A conventional capacitively coupled PECVD reactor with an RF glow discharge of 13.56 MHz was used for film depositions. A mixture of 2 sccm (standard cubic centimeter per minute) SiH<sub>4</sub> and 41 sccm Ar was introduced into the reactor, resulting in a chamber pressure of 210 mTorr. Plasma was triggered by applying a low RF power of 4 W (power density of ~65 mW cm<sup>-2</sup>) at 13.56 MHz to parallel plate electrodes. A series of a-Si:H films with varying H concentrations were prepared by changing the substrate temperature systematically from 50 °C to 300 °C. Profilometric measurements (KLA-Tencor P-7 stylus profiler) show the film thicknesses ( $d_{\text{a-Si:H}}$ ) in the range of 350–460 nm. At each substrate temperature studied, samples were deposited on two quartz substrates for thermal conductivity measurements and two double-sided polished c-Si wafers for FTIR. One set of samples was studied as produced, while the other set was annealed in a furnace under a nitrogen flow at 460 °C for 30 hours with heating and cooling rates of 3 °C min<sup>-1</sup>. The annealing process was intended for H effusion with little to no crystallization of the films.<sup>30,31</sup>

Fig. 1(a) shows a schematic diagram of the as-produced a-Si:H deposited at different substrate temperatures as well as a-Si obtained by the post-annealing process. The H bonding configuration in the a-Si:H films was studied by FTIR (Bruker Alpha IR spectrometer) in the transmission mode. The Brodsky–Cardona–Cuomo (BCC) method was employed to convert the infrared transmittance to absorption coefficients.<sup>1</sup> Fig. 1(b) and (c) show the FTIR absorption spectra of the as-produced samples prepared at different substrate temperatures in the wagging and stretching bond regions, respectively. The stretching mode absorption could be deconvoluted into two Gaussian peaks centered at around 2000 cm<sup>-1</sup> and 2080 cm<sup>-1</sup>, representing silicon monohydride (SiH) and dihydride ((SiH<sub>2</sub>)<sub>n</sub>) bonds, respectively. The SiH bond is assigned to isolated H in a dense network structure, while the (SiH<sub>2</sub>)<sub>n</sub> bond is attributed to the presence of clustered H at the internal surfaces of microvoids.<sup>32</sup> For the sample prepared at 50 °C, the dihydride peak is predominant, indicating the high degree of microscopic voids at low temperatures. With increasing substrate temperature during deposition, the dihydride peak intensity decreases much faster than the monohydride peak intensity showing that a-Si:H thin films are less porous at higher temperatures.

The H concentration of the films was evaluated using the integrated absorption of the Si–H wagging bond at 640 cm<sup>-1</sup>, following:

$$\epsilon_{\text{H}} = \frac{A_{640}}{n_{\text{c-Si}}} \int \frac{\alpha(\omega)}{\omega} d\omega \quad (1)$$

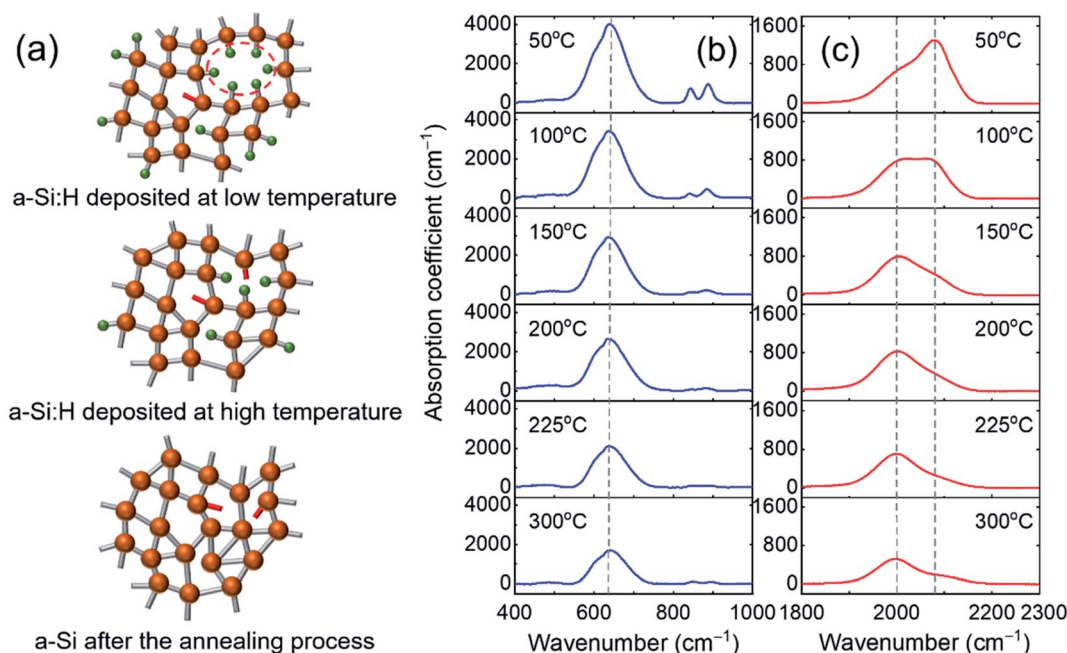


Fig. 1 (a) Two-dimensional (2D) schematic illustrations of a-Si:H deposited by PECVD at different substrate temperatures and hydrogen-free a-Si prepared by the post-annealing process. Orange and green spheres represent Si and H atoms, respectively, and red lines denote dangling bonds. The H atoms in a-Si:H passivate some of the dangling bonds and can form fully hydrogen-passivated nanovoids (indicated by the red dashed oval). After annealing, the effusion of H atoms leads to the elimination of voids and thus results in a denser film. (b) and (c) FTIR absorption spectra of the as-produced samples prepared at different substrate temperatures in the wagging and stretching bond regions, respectively. The wagging band has a peak at 640 cm<sup>-1</sup> and the stretching band has two peaks at around 2000 cm<sup>-1</sup> and 2080 cm<sup>-1</sup>, representing SiH and (SiH<sub>2</sub>)<sub>n</sub> groups, respectively.



**Table 1** Summary of the properties of the as-produced samples at 300 K: deposition temperature ( $T$ ), H concentration ( $\varepsilon_{\text{H}}$ ), porosity ( $\phi$ ), volumetric heat capacity ( $C_{\text{a-Si:H}}$ ), film thickness ( $d_{\text{a-Si:H}}$ ), and longitudinal speed of sound ( $v_{\text{L}}$ )

| $T$ (°C) | $\varepsilon_{\text{H}}$ (at%) | $\phi$ (%) | $C_{\text{a-Si:H}}$ (J cm <sup>-3</sup> K <sup>-1</sup> ) | $d_{\text{a-Si:H}}$ (nm) | $v_{\text{L}}$ (m s <sup>-1</sup> ) |
|----------|--------------------------------|------------|---|--------------------------|-------------------------------------|
| 50       | 25.4                           | 21         | 1.30  | 450                      | 7100 ± 200                          |
| 100      | 21.5                           | 13         | 1.43  | 425                      | 7800 ± 200                          |
| 150      | 18.4                           | 10         | 1.48  | 464                      | 7500 ± 200                          |
| 200      | 16.6                           | 8          | 1.51  | 388                      | 7600 ± 300                          |
| 225      | 13.6                           | 6          | 1.54  | 410                      | 7700 ± 200                          |
| 300      | 10.1                           | 5          | 1.56  | 449                      | 8000 ± 200                          |

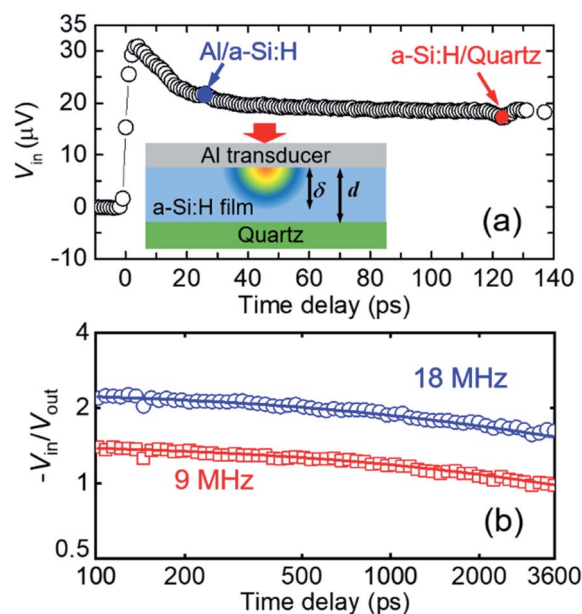
where  $n_{\text{c-Si}} = 5 \times 10^{22}$  cm<sup>-3</sup> is the atomic density of c-Si,  $A_{640} = 2.1 \times 10^{19}$  cm<sup>-2</sup> is the proportionality factor reported by Langford *et al.*,<sup>33</sup>  $\alpha$  is the absorption coefficient, and  $\omega$  is the wave-number (cm<sup>-1</sup>). The H concentration of the as-produced samples decreases from 25.4 to 10.4 atomic percentage (at%) with increasing the substrate temperature, as shown in Table 1. After the post-annealing process, the absorption peak intensities of both the wagging and stretching bond regions drop considerably, indicating H concentrations of less than 1 at% for all annealed samples.

Due to the mass difference between H and Si atoms, the mass density ( $\rho$ ) of a-Si:H films decreases with increasing H concentration. The relationship between the H concentration and  $\rho$  of a-Si:H films has been extensively examined in prior studies.<sup>33–35</sup> The film porosity ( $\phi$ ) can be obtained from the film mass density following:  $\phi = 1 - \frac{\rho}{\rho_0}$ , with  $\rho_0$  being the mass density of the pure a-Si film without hydrogenation. Table 1 summarizes the structural parameters and properties of the as-produced samples necessary for the thermal analysis as detailed in Sec. 3.

### 3. Thermal measurement results and discussion

The thermal conductivities of the films were measured with TDTR,<sup>28,36</sup> a technique that has been thoroughly validated and extensively employed in the study of thermal conductivities of thin films,<sup>37–40</sup> nanocomposites,<sup>41,42</sup> bulk specimens,<sup>43,44</sup> and thermal conductance of interfaces.<sup>45</sup> Prior to thermal measurements, a thin layer of Al was deposited onto the sample surface as a transducer and heating source, as illustrated by the schematic of the sample stack in the inset of Fig. 2(a). The thickness of the Al transducer ( $\approx 80$  nm) can be determined by picosecond acoustics, based on the longitudinal speed of sound of Al<sup>46,47</sup> and the time delay at which the acoustic wave makes a round trip within the Al layer, as shown in Fig. 2(a).<sup>48</sup> Similarly, using the acoustic echo reflected from the a-Si:H/quartz interface and  $d_{\text{a-Si:H}}$  from profilometry, the longitudinal speed of sound ( $v_{\text{L}}$ ) of a-Si:H films can be derived.

The data reduction of TDTR thermal measurements requires multiple inputs: the thickness ( $d_{\text{Al}}$ ), volumetric heat capacity ( $C_{\text{Al}}$ ), and thermal conductivity ( $\Lambda_{\text{Al}}$ ) of the Al transducer, and



**Fig. 2** (a) Picosecond acoustics measurements of an a-Si:H film deposited on quartz. The inset is the sample stack for thermal conductivity measurements. (b) Representative TDTR signals of the a-Si:H film (10.1 at%) with two modulation frequencies. The solid lines are the fitting curves following a heat diffusion model, which give a thermal conductivity of 1.42 W m<sup>-1</sup> K<sup>-1</sup>.

the thickness ( $d_{\text{a-Si:H}}$ ) and volumetric heat capacity ( $C_{\text{a-Si:H}}$ ) of the a-Si:H film.  $d_{\text{Al}}$  and  $d_{\text{a-Si:H}}$  are obtained from picosecond acoustics and profilometry, respectively, as described above.  $\Lambda_{\text{Al}}$  is converted from the electrical conductivity measured with the four-point probe method based on the Wiedemann–Franz Law and  $C_{\text{Al}}$  is taken from the literature.<sup>49</sup>  $C_{\text{a-Si:H}}$  is taken as the heat capacity of c-Si scaled down with the film porosity ( $C_{\text{a-Si:H}} = \phi \times C_{\text{c-Si}}$ ). Here, the H contribution to  $C_{\text{a-Si:H}}$  is neglected at room temperature since the vibrational frequency of H atoms ( $\sim 100$  THz) is much higher than that of Si atoms ( $\sim 10$  THz).<sup>50–54</sup> Also, the heat capacity of c-Si is approximately equal to that of fully dense amorphous silicon.<sup>18,27</sup> The values of  $v_{\text{L}}$ ,  $C_{\text{a-Si:H}}$ , and  $d_{\text{a-Si:H}}$  for the as-produced a-Si:H samples are summarized in Table 1.

By fitting the measurement data to a heat diffusion model with the aforementioned input parameters, the sample's thermal conductivity can be extracted.<sup>28</sup> Fig. 2(b) illustrates the representative TDTR signals of dual-modulation frequency measurements and associated best fitting to extract  $\Lambda$  for the a-Si:H film (10.1 at%) deposited on the quartz substrate. The fitted thermal conductivity is  $\Lambda_{\text{a-Si:H}} = 1.42 \pm 0.16$  W m<sup>-1</sup> K<sup>-1</sup>. At the modulation frequencies of 9 and 18 MHz, the thermal penetration depth ( $\delta = \sqrt{\Lambda/\pi C f}$ ) is calculated to be  $\sim 200$  nm, smaller than the film thickness. This suggests that our a-Si:H films are essentially thermally opaque, and therefore TDTR measurements are not sensitive to the quartz substrate and the thermal interface between the film and the substrate.

Fig. 3 summarizes the H concentration of the as-produced ( $\varepsilon_{\text{a-Si:H}}$ ) samples and the thermal conductivities of both the as-produced ( $\Lambda_{\text{a-Si:H}}$ ) and annealed ( $\Lambda_{\text{a-Si}}$ ) samples. The total uncertainty of measured thin-film thermal conductivity consists



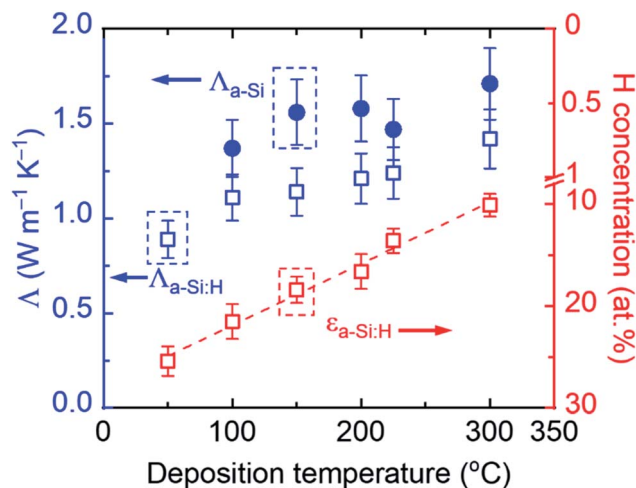


Fig. 3 The room-temperature thermal conductivity (left axis) and H concentration (right axis) of PECVD a-Si:H films as a function of the deposition temperature.  $\epsilon_{\text{a-Si:H}}$  represents the H concentration of the as-produced samples. The dashed line shows the linear dependence of H concentration on deposition temperature.  $\Lambda_{\text{a-Si:H}}$  and  $\Lambda_{\text{a-Si}}$  are the room-temperature thermal conductivities of the as-produced and annealed films, respectively.

of the random uncertainty ( $U_A$ ) and the systematic uncertainty ( $U_B$ ) via  $U_{\text{tot}} = \sqrt{U_A^2 + U_B^2}$ .  $U_A$  takes into account the deviation of measurements at two different locations and  $U_B$  is estimated based on the sensitivity analysis as detailed previously.<sup>29,40</sup> Among individual parameters, the transducer thickness makes the dominant contribution to  $U_B$  followed by the transducer heat capacity. Take the 21.5 at% a-Si:H sample as an example. A 4% uncertainty in the transducer thickness and a 3% uncertainty in the transducer heat capacity would lead to a  $U_B$  of  $\sim 10\%$ . Combined with  $U_A$ , the resulting total uncertainty of measurement results is  $\sim 11\%$ . Note that here all annealed samples are considered as “pure” a-Si films since their H concentrations are negligible ( $< 1$  at%) as a result of H effusion during the annealing processes. As shown in Fig. 3,  $\epsilon_{\text{a-Si:H}}$  decreases linearly with the deposition temperature, while  $\Lambda_{\text{a-Si:H}}$  increases with the deposition temperature (and thus decreases with  $\epsilon_{\text{a-Si:H}}$ ). The decreasing trend of  $\Lambda_{\text{a-Si}}$  versus deposition temperature is also observed in annealed samples, suggesting that the initial hydrogenation can impact the thermal properties of a-Si through the annealing processes. Due to the H effusion process during heat treatment, defects are more likely to occur in samples with higher H concentrations.<sup>55–57</sup> Likely due to the same reason, the film with a H concentration of 25.4 at% did not adhere to the substrate after annealing, despite several attempts. Therefore, there are only five data points for the annealed samples as compared to six data points for the as-produced samples.

To reveal the impact of hydrogenation on the thermal conductivity of a-Si:H films, we first discuss the thermal conductivities of a-Si, *i.e.*, annealed samples ( $\Lambda_{\text{a-Si}}$ ). Due to the lack of structural periodicity in amorphous materials, adaptation of the phonon picture is no longer applicable, and therefore the concepts of ballistic and diffusive transport that are

usually used in crystalline materials are not suitable here.<sup>58,59</sup> Instead, we adopt the concepts of propagons and diffusons that are commonly used in studies of amorphous materials. As has been reported in prior studies, diffusons and propagons are the two main heat carriers contributing to the thermal conductivity of a-Si films.<sup>59–62</sup> The diffuson contribution ( $\Lambda_{\text{diff}}$ ) is thickness independent and can be calculated by the minimum thermal conductivity model given by Cahill *et al.*:<sup>19</sup>

$$\Lambda_{\text{diff}} = \left(\frac{\pi}{6}\right)^{1/3} k_B n^{2/3} \sum_{j=1}^3 v_j \left(\frac{T}{\theta_j}\right)^2 \int_0^{\theta_j/T} \frac{x^3 e^x}{(e^x - 1)^2} dx \quad (2)$$

where  $n$  is the number density of atoms,  $T$  is the temperature, and  $v_j$  is the speed of sound with the subscript “ $j$ ” denoting the polarization of three phonon branches.  $\theta_j$  is the Debye temperature for each polarization:

$$\theta_j = v_j \left(\frac{\hbar}{k_B}\right) (6\pi^2 n)^{1/3} \quad (3)$$

The propagon contribution ( $\Lambda_{\text{prop}}$ ) increases with the film thickness, possessing similar features to phonons as a reflection of the size effect for thin films.<sup>21–23,58,63</sup>  $\Lambda_{\text{prop}}$  can be modeled following Braun *et al.*:<sup>21</sup>

$$\Lambda_{\text{prop}} = \frac{1}{3} \sum_j \int_0^{\omega_{p \rightarrow d,j}} \hbar \omega D_j(\omega) \frac{\partial f}{\partial T} v_j^2 \tau_j d\omega \quad (4)$$

where  $\omega_{p \rightarrow d}$  is the crossover angular frequency (at which the transition from the propagon regime to the diffuson regime occurs),  $f$  is the propagon equilibrium distribution function following the Bose–Einstein distribution, and  $D$  is the phonon density of states calculated with the Debye model:

$$D_j(\omega) = \frac{\omega_j^2}{2\pi^2 v_j^3} \quad (5)$$

The relaxation time is obtained based on a three-phonon scattering model involving the boundary scattering:

$$\tau^{-1} = A\omega^4 + BT\omega^2 \exp\left(-\frac{C}{T}\right) + \frac{2v_j}{d} \quad (6)$$

where  $A$ ,  $B$ , and  $C$  are fitting parameters with values given by ref. 21. The total thermal conductivity of a-Si is  $\Lambda_{\text{a-Si, model}} = \Lambda_{\text{prop}} + \Lambda_{\text{diff}}$ . Here, the locon contribution to thermal conductivity is not discussed since it is negligible in a-Si.<sup>59,62,64</sup>

The thickness-dependent thermal conductivity of a-Si films has been well documented in the literature. As shown in Fig. 4(a), the measured thermal conductivities of our a-Si samples agree well with literature data.<sup>18,21,22,24,27,65</sup> Since a-Si films were obtained from annealing the a-Si:H samples, structural defects induced by the initial hydrogenation and H effusion processes can exist in a-Si samples. Considering such defects and the small range of film thickness ( $\sim 350$ – $450$  nm), the thickness dependence of our measured  $\Lambda_{\text{a-Si}}$  is less apparent. The total thermal conductivity of  $\Lambda_{\text{a-Si}}$  is decomposed into the contributions from diffusons ( $\Lambda_{\text{diff}}$ ) and propagons ( $\Lambda_{\text{prop}}$ ), based on eqn (2) and (4) with parameters taken from ref.



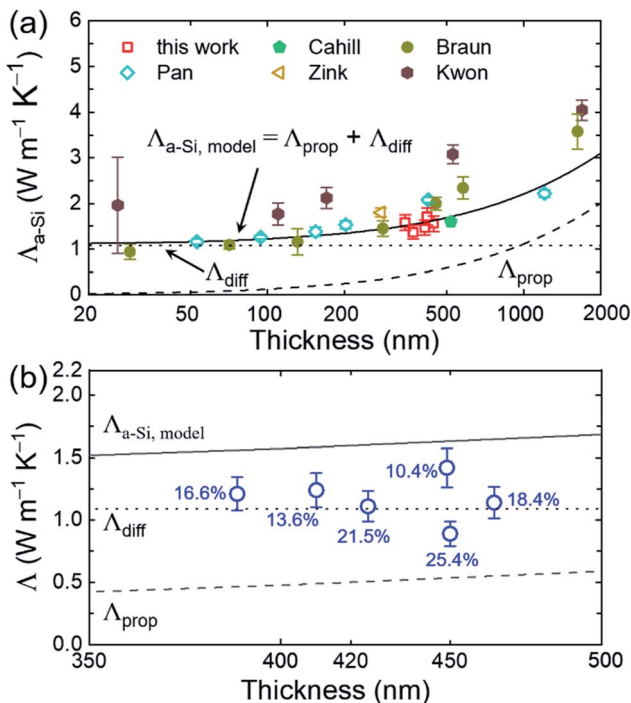


Fig. 4 (a) The comparison of experimental results of a-Si films with literature measurement data<sup>18,21,22,24,65</sup> and model predictions. The propogon (dashed line) and diffuson (dotted line) contributions are calculated using eqn (2) and (4), respectively. (b) The comparison of measured thermal conductivity of a-Si:H films with model predictions of a-Si. It is worth noting that  $\Lambda_{\text{a-Si:H}}$  with higher H concentrations approaches or is even lower than the diffuson-only thermal conductivity of a-Si.

21, which are denoted as dotted and dashed lines in Fig. 4(b). Among the a-Si films, the 420 nm a-Si film is grown under the highest deposition temperature, leading to the lowest H concentration before annealing. For the a-Si film of 420 nm thickness,  $\Lambda_{\text{diff}}$  and  $\Lambda_{\text{prop}}$  are calculated to be  $\sim 1.1$  and  $0.7 \text{ W m}^{-1} \text{ K}^{-1}$  which account for nearly 60% and 40% of the total thermal conductivity ( $\sim 1.8 \text{ W m}^{-1} \text{ K}^{-1}$ ), respectively, agreeing well with our measurement data ( $1.71 \text{ W m}^{-1} \text{ K}^{-1}$ ). It is noted that the literature data of  $\Lambda_{\text{a-Si}}$  actually scatter.<sup>18,21,22,24,27,65</sup> This is likely attributed to the variations of defects in a-Si prepared with different growth methods and conditions.

As the thermal conductivity of a-Si is understood, we proceed to the discussion of a-Si:H films. The thermal conductivities of a-Si:H films are plotted in Fig. 4 with the H concentrations denoted by percentages. It is seen that the thermal conductivity does not show any apparent dependence on the film thickness, suggesting that the size effect is not the dominant factor affecting thermal transport in these a-Si:H films. Rather, H concentration plays a much more important role in determining the thermal properties of a-Si:H films. This is reflected by the fact that for a-Si:H films with larger H concentrations, the measured thermal conductivity approaches or is even smaller than the  $\Lambda_{\text{diff}}$  of a-Si films. Fundamentally, the introduction of H atoms into a-Si leads to three main changes that can affect thermal transport. The first one is the mass loss, which

decreases the density and heat capacity of a-Si as shown in Table 1; the second one is the material softening induced by the voids, which lowers the sound velocity as shown in Table 1; and the last one is the enhanced heat carrier-defect scattering, where the defects include both H atoms and the voids they introduce, both of which predominantly impact propogons with low frequencies. In the latest theories,<sup>21,66,67</sup> diffusons are described as non-propagating modes, *i.e.*, they have zero group velocity, and therefore they are not participants in any scattering mechanism.<sup>58,66–68</sup> Thus, the diffuson thermal conductivity is related to the first two changes, while the propogon thermal conductivity is influenced by all three changes.

The diffuson thermal conductivity is impacted by the mass loss and material softening. Nilsson *et al.*<sup>69</sup> proposed a model ( $\frac{\Lambda}{\Lambda_0} = \frac{\rho}{\rho_0} \times \frac{v}{v_0}$ ) that accounts for both impacts, and this model has been extensively used in the literature.<sup>70–74</sup> However, the factor of  $\rho/\rho_0$  in this model oversimplifies the effect of porosity ( $\phi$ ) on thermal conductivity, which can be better predicted by the effective medium approximation (EMA) approach.<sup>75–77</sup> EMA assumes that the intrinsic properties of solid materials (*e.g.*, sound velocity) do not change, and thus avoids double counting the effect of sound velocity reduction. The diffuson thermal conductivity calculated with the EMA approach can be written as:

$$\Lambda_{\text{diff,EMA}} = \Lambda_{\text{diff},0} \left( \frac{1-\phi}{1+\phi/2} \right) \left( \frac{v_L}{v_{L0}} \right) \quad (7)$$

where  $\Lambda_{\text{diff},0}$  is the diffuson thermal conductivity of dense a-Si ( $1.10 \text{ W m}^{-1} \text{ K}^{-1}$ ) calculated based on eqn (2), and  $v_{L0}$  is the longitudinal speed of sound in a-Si. Our measured  $v_{L0}$  ( $8300 \text{ m s}^{-1}$ ) of annealed films is similar to previous reports for a-Si films.<sup>27,78</sup> Fig. 5(a) shows the  $\Lambda_{\text{diff}}$  of a-Si:H films calculated from eqn (7) in comparison with the experimental results. The measured thermal conductivity of the 0 at% sample is taken as the thermal conductivity of the 420 nm a-Si film with the lowest initial H concentration before annealing ( $1.71 \text{ W m}^{-1} \text{ K}^{-1}$ ).  $\Lambda_{\text{diff}}$  decreases from 1.10 to  $0.67 \text{ W m}^{-1} \text{ K}^{-1}$  when the H concentration increases from 0 to 25.4 at%.

The propogon contribution can be obtained by subtracting  $\Lambda_{\text{diff}}$  from the measured total thermal conductivity ( $\Lambda_{\text{prop}} = \Lambda_{\text{exp}} - \Lambda_{\text{diff,EMA}}$ ), which is plotted in Fig. 5(b).  $\Lambda_{\text{prop}}$  decreases from 0.61 to  $0.22 \text{ W m}^{-1} \text{ K}^{-1}$  as the H concentration increases from 0 to 25.4 at%. For 0 at% H concentration,  $\Lambda_{\text{prop}}$  approaches the calculated value of propogon thermal conductivity for a 420 nm a-Si film based on eqn (4) (dashed line in Fig. 5(b)). We further estimate the normalized MFP (mean free path) of propogons,  $l/l_0$ , with  $l_0$  being the propogon MFP of a pure a-Si film, for these a-Si:H films following the rule of  $\Lambda_{\text{prop}} \sim cvl$  (Fig. 5(c)). We find that even at a low H concentration ( $\sim 10$  at%), the propogon MFP is already affected by the introduction of H atoms. Propogons in amorphous silicon are long-wavelength phonons,<sup>23</sup> which cannot discern small-size defects such as H atoms or point-defect vacancies due to the short-wavelength preference of Rayleigh scattering.<sup>79</sup> It suggests that large voids may form due to the introduction of H atoms. Such large voids can scatter propogons with long wavelengths and lead to a clear drop in



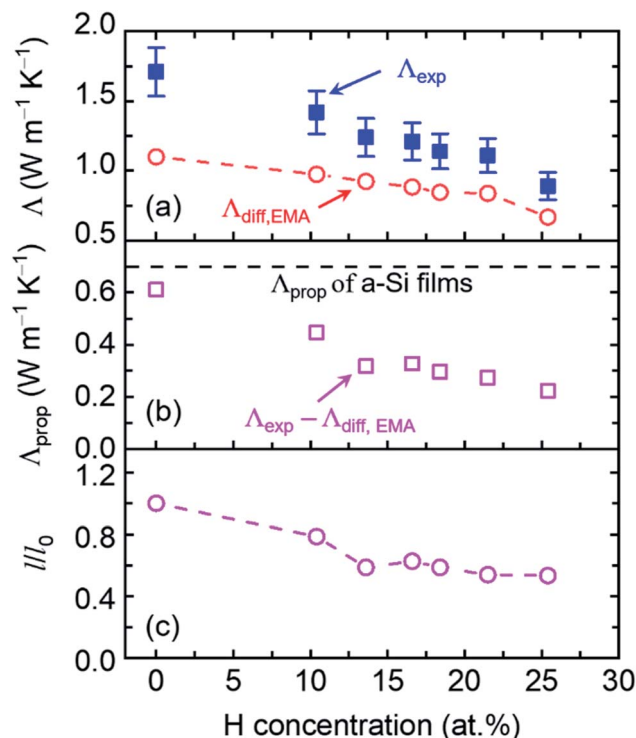


Fig. 5 (a) EMA calculated diffuson thermal conductivity of a-Si:H films with different H concentrations. The experimental data of total thermal conductivities are also shown. (b) Propagator thermal conductivity of a-Si:H films obtained by subtracting the diffuson contribution from the total thermal conductivity. The black dashed line denotes the propagator contribution for a 420 nm a-Si film. (c) Normalized propagator MFP as a function of the H concentration.

propagator MFP at  $\sim 10$  at%. The reduction of propagator MFP reaches nearly 50% as the H concentration increases to 25.4 at%.

## 4. Conclusions

This work experimentally investigated the impact of hydrogenation on thermal transport in a-Si:H films prepared by PECVD. Before hydrogenation, for an a-Si film of  $\sim 400$  nm thickness, the diffuson and propagator contribute  $1.10$  and  $0.61$   $W m^{-1} K^{-1}$ , which account for 64% and 36% of the total thermal conductivity, respectively. After H is introduced, the thermal conductivity decreases monotonically with increasing H concentration. At a maximum H concentration of 25.4 at%, we find that the diffuson and propagator thermal conductivities are decreased from  $1.10$  and  $0.61$  to  $0.67$  and  $0.22$   $W m^{-1} K^{-1}$ , with a decreasing ratio of 40% and 64%, respectively. Such decreases are attributed to three factors: (1) mass loss, or density decrease due to the replacement of H with Si and the introduction of nanovoids, (2) sound velocity reduction, and (3) heat carrier-defect scattering. While diffuson thermal conductivity is impacted by the first two factors, propagator thermal conductivity is impacted by all three. As a result, the impact of hydrogenation is more significant on propagator contributions to the thermal conductivity. Furthermore, we find that the propagator

MFP can be affected by H atoms even at a small H concentration ( $\sim 10$  at%). When H concentration further increases to 25.4 at%, the dominant propagator MFP is suppressed by  $\sim 50\%$ . With knowledge of the individual contributions from diffusons and propagators, the results of this work can potentially be applied to tune the thermal properties of a-Si:H and thus facilitate the design and optimization of Si-based technologies.

## Conflicts of interest

There are no conflicts to declare.

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