

## RESEARCH ARTICLE

[View Article Online](#)  
[View Journal](#) | [View Issue](#)Cite this: *Mol. Omics*, 2022,  
18, 853A knowledge graph representation learning  
approach to predict novel kinase–substrate  
interactions†Sachin Gavali,<sup>a</sup> Karen Ross,<sup>b</sup> Chuming Chen,<sup>a</sup> Julie Cowart<sup>a</sup> and  
Cathy H. Wu<sup>a</sup>

The human proteome contains a vast network of interacting kinases and substrates. Even though some kinases have proven to be immensely useful as therapeutic targets, a majority are still understudied. In this work, we present a novel knowledge graph representation learning approach to predict novel interaction partners for understudied kinases. Our approach uses a phosphoproteomic knowledge graph constructed by integrating data from iPTMnet, protein ontology, gene ontology and BioKG. The representations of kinases and substrates in this knowledge graph are learned by performing directed random walks on triples coupled with a modified SkipGram or CBOW model. These representations are then used as an input to a supervised classification model to predict novel interactions for understudied kinases. We also present a post-predictive analysis of the predicted interactions and an ablation study of the phosphoproteomic knowledge graph to gain an insight into the biology of the understudied kinases.

Received 30th December 2021,  
Accepted 22nd July 2022

DOI: 10.1039/d1mo00521a

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## 1 Introduction

Proteins are a fundamental building block of the complex molecular machinery employed by all living organisms. The collection of all the possible proteins that can be synthesized by an organism is known as the proteome.<sup>1</sup> Proteins interact with each other through distinct biochemical events to actuate the desired biological functions. Protein post-translational modification (PTM) is one such biochemical event that has played a major role in almost all the biological functions.<sup>2</sup>

Fundamentally, any given PTM event is made up of two members – an enzyme and a substrate. An enzyme is a protein responsible for facilitating the PTM event and the substrate is the protein undergoing the post-translational modification. Among all the types of PTM events, phosphorylation is the most common and well-studied and is implicated in a majority of cellular functions.<sup>3</sup> Phosphorylation is carried out by a class of enzymes known as kinases. Previously it was believed that the kinase–substrate interaction networks are fairly linear, and perturbation of a kinase would primarily affect its immediate substrate. But recent studies have shown that these interaction networks are highly interconnected and perturbation of a

particular kinase or a substrate has the potential to affect large parts of the network.<sup>4</sup>

With the advent of techniques such as mass spectrometry based high throughput proteomics, many new phosphorylation sites have been identified<sup>5</sup> but identifying kinases that phosphorylate these sites remains a challenging problem. Experimental studies on kinase–substrate interactions are time-consuming and expensive and most research has been focused on a small subset of the 550 protein kinases found in humans. Computational approaches that can accurately predict novel kinase–substrate interactions have the potential to increase our understanding of the human proteome. This increased understanding will in turn help accelerate identification of new therapeutic targets and the development of accompanying drugs to modulate these targets.

To this date, many tools have been developed to predict kinase–substrate interactions. Tools such as Scansite,<sup>6</sup> NetPhosphK,<sup>7</sup> PPSP,<sup>8</sup> GPS<sup>9,10</sup> and PredPhosph<sup>11</sup> rely on the properties of protein sequences around the phosphorylation site also known as “sequence motifs”, to predict kinases most likely to be associated with the given phosphorylation site. But kinase–substrate interactions involve much more than sequence motifs and hence it is necessary to include contextual factors when making these predictions. Thus tools such as NetworKIN,<sup>12</sup> PhosphoPICK,<sup>13</sup> PhosphoPredict<sup>14</sup> and HeteSim<sup>15</sup> were developed that combine sequence and contextual information to make better predictions. But many of the above tools have significant limitations in terms of kinome coverage. This is

<sup>a</sup> University of Delaware, Newark, DE 590 Avenue 1743, Suite 147, Newark, DE, USA. E-mail: [saching@udel.edu](mailto:saching@udel.edu)

<sup>b</sup> Georgetown University Medical Center, Washington DC, USA

† Electronic supplementary information (ESI) available. See DOI: <https://doi.org/10.1039/d1mo00521a>

partly due to the fact that these tools primarily rely on properties that can only be directly mapped to the kinases or substrates. Understudied kinases by their very nature have limited information and hence are not annotated with these properties making it difficult to use these tools.

Inspired by recent advancement in deep learning a new generation of tools are being developed to address these shortcomings. DeepKinZero<sup>16</sup> is a tool that takes inspiration from deep learning techniques in computer vision and employs a zero shot learning approach to transfer knowledge from well known kinases to understudied kinases. But similar to the first generation tools, it relies primarily on sequence information. LinkPhinder<sup>17</sup> takes a significantly different approach and formulates the task of predicting kinase–substrate interactions as a link-prediction task. It considers kinases, substrates and phosphorylation sites to be constituting a knowledge graph and uses knowledge graph completion algorithms to predict possible kinase–substrate interactions. A significant limitation of all the above tools is that they do not take advantage of the long range dependencies between kinases and substrates that are encoded in existing kinase–substrate interaction networks. In addition to this, they also fail to model the deeper biological connections that are only evident by looking at the vast body of biomedical knowledge being collected and organized in semantic databases such as gene ontology and protein ontology.

In recent years, there has been a significant increase in the amount of biological data. This has made it increasingly difficult to organize and derive knowledge from this data. Subsequently, semantic technologies that define a set of standards for organizing and linking data were adopted. Using such linked (semantic) data can provide us with knowledge that cannot be derived purely from protein sequences. They can help us craft algorithms that can truly capture the biological roles of kinases and substrates. In this work we present a novel approach of learning from semantic data. Since the goal of this work was to investigate if knowledge graph/semantic data can be useful in predicting kinase–substrate interactions we simplified the task by only predicting interactions at the kinase/substrate level instead of the kinase/phosphorylation site level. Nevertheless, we think that the kinase/substrate representations learned by our approach can be combined with tools working at sequence level such as DeepKinZero to obtain better predictions at finer resolutions.

## 2 Methods

### 2.1 Data

We construct the knowledge graph by including data from iPTMnet,<sup>3</sup> Protein Ontology (PRO),<sup>4</sup> Gene Ontology (GO)<sup>5</sup> and BioKG.<sup>6</sup> To begin with, we use human PTM data [Taxon code – 9606] from iPTMnet to construct a kinase–substrate interaction network. The iPTMnet data contains 26411 phosphorylation PTM events. Any given kinase–substrate pair can have multiple PTM events. We normalize these events to triples in the form of kinase → phosphorylates → substrate.

PRO defines protein classes and represents the hierarchical relationships among proteins, protein forms (proteoforms) and protein complexes within and across species.<sup>7</sup> The PRO data is arranged in the form of an acyclic directed graph. Thus using PRO data we construct triples in the form of kinase/substrate → is\_a → pro\_entity and inverse triples in the form of pro\_entity → has\_a → kinase/substrate extending all the way to the root of the PRO tree to capture evolutionary relationships among the proteins encoded by the PRO ontology.

Gene Ontology organizes biological knowledge by specifying a controlled vocabulary to precisely describe the biological processes, molecular functions and subcellular localizations associated with gene products. Using GO we create triples in the form of kinase/substrate → annotated\_with → go\_term. Since GO terms themselves are arranged in the form of a directed acyclic graph (DAG), we create new triples in the form go\_term\_a → is\_a → go\_term\_b extending until the root of the GO tree to capture the knowledge defined by the relational hierarchy of GO.

Similar to the above-mentioned data sources, there are many more data sources that can be integrated in our knowledge graph. Rather than performing this integration ourselves, we decided to take advantage of the BioKG database.<sup>6</sup> The authors of BioKG database provide a framework to automatically integrate data from numerous biomedical databases. Since BioKG framework is geared towards drug discovery analysis we integrated only a subset of the biomedical databases. Specifically we include data from UniPROT,<sup>8</sup> Reactome,<sup>9</sup> KEGG<sup>10</sup> and STRINGS-DB.<sup>11</sup> This resulted in addition of new triples with following relations – protein–pathway associations, protein–disease associations, protein–genetic disorder associations, disease–genetic disorder associations, disease–pathway associations, protein–complex associations and complex–pathway associations to our knowledge graph.

Once the above knowledge graph was built, we used it as a data source to train a machine learning model to predict interactions for understudied kinases.

### 2.2 Data preparation

As mentioned in the previous section, we start with a kinase–substrate interaction network constructed using PTM data and then enrich it with auxillary data to construct our knowledge graph. When training a machine learning model it is necessary to ensure proper separation of training, validation and testing data to prevent information leakage. Thus, even before we enrich the vanilla kinase–substrate network with auxillary data, we split the network into three subnetworks – training, validation and testing. The training network contains “kinase → phosphorylates → substrate” triples in addition to the triples from auxillary data. Validation and testing networks contain only the kinase–substrate interaction triples in the form kinase → phosphorylates → substrate.

### 2.3 Knowledge graph learning approach

In recent years, many approaches to learn from knowledge graphs have been proposed. These approaches can be broadly



grouped into four categories – (1) tensor decomposition, (2) Geometric distance, (3) deep learning and (4) random walk.<sup>12</sup> Tensor decomposition based approaches represent the entities and the relations as a giant 3D adjacency matrix (Tensor). This matrix is then decomposed into low dimensional vectors while still retaining the latent information about the graph structure and connectivity.<sup>13,14</sup> Geometric distance based approaches learn an embedding of the knowledge graph by representing the relation between the head and tail as a geometric transformation in the latent space.<sup>15</sup> Deep learning based approaches represent the entities and relations using a low dimensional embedding vector. Instead of deriving these embeddings using tensor decomposition or geometric factorization, these models use a neural network to optimize the embeddings to predict the probability of a triple in the knowledge graph being true or false.<sup>16</sup> Random walk based approaches take inspiration from advancements in natural language processing. They involve sampling a series of nodes (entities) from the knowledge graph. These series of nodes can be thought of as sentences in a language with every node representing a word in the sentence. These sentences are then used as an input corpus for a language model such as word2vec<sup>17</sup> to learn a dense embedding for every node in the graph.<sup>18</sup>

A glaring short-coming of the random walk based approaches is that they do not take into account the triple structure of the knowledge graph. Specifically, existing methods such as DeepWalk<sup>18</sup> and Node2Vec<sup>19</sup> do not consider the directionality and the heterogeneity encoded by a triple when performing the random walk. They treat the relations in a knowledge graph as any other node in the graph. Hence, they cannot adequately capture the semantic meaning of the entities in the knowledge graph. To alay these shortcomings, alternative approaches that rely on metapaths have been proposed.<sup>20</sup> But contrary to the simpler approaches such as DeepWalk and Node2Vec, the performance of metapath based approaches is highly dependent on the choice of metapath. Additionally, choosing a metapath requires an in-depth knowledge of the schema of the knowledge graph under study, further diminishing their utility.

Hence, in this work, we propose a modified random walk based approach that takes inspiration from DeepWalk,<sup>18</sup> one of the simplest knowledge graph learning algorithms, to learn a representation of kinases and substrates in our phospho-proteomic knowledge graph. The fundamental assumption of any random walk based approach is that entities with similar meaning occur in similar contexts. But in a knowledge graph, the context is not only defined by the connectivity, but also by the type and the direction of the relationships. Hence, our approach makes a slightly different assumption. It assumes that the heterogeneous knowledge graph is a superimposition of three distinct graphs. The first graph contains only head entities, the second graph contains only relations and the third graph contains only tail entities. [Fig. 1]. The heterogeneous knowledge graph can then be thought of as a function of the latent interactions between the entities from each of these three sub-graphs. To model this function, we modify the manner in

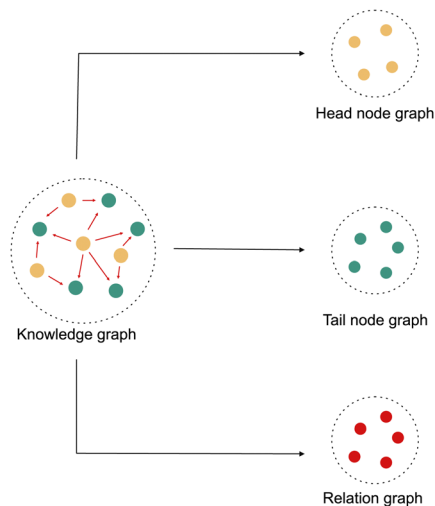


Fig. 1 Knowledge graph represented as an overlapping graph of heads, relations and tails.

which random walks are performed. Instead of sampling a series of nodes using traditional random walks, we sample a series of “triples” by performing a Triple Walk. This series of triples is then used as an input to a modified skip gram model to learn an embedding of all the entities and relations in the knowledge graph.

## 2.4 Deepwalk overview

Since our approach is inspired by DeepWalk approach, it is essential to understand all the steps that constitute the DeepWalk algorithm. On a very high level, the DeepWalk algorithm combines random walks on a graph with a language model such as Word2Vec<sup>17</sup> to learn a vector representation of every node in the graph. Since the Word2Vec model plays a major role in the DeepWalk algorithm, it is essential to understand the steps involved in training a Word2vec model.

Word2Vec is a simple model used to learn dense vector embeddings of words<sup>21</sup> in a given language. At its core it contains a single layered neural network that predicts if a particular word would occur in a given sentence. This task is similar to the task of filling the blanks in an incomplete sentence. For example, given an incomplete sentence – the quick brown fox \_\_\_\_ over the lazy dog, the word2vec model tries to predict a word that would occur in the blank space [Fig. 2]. The word to be predicted is known as the target word and the words already present in the sentence are known as the context words. The target word can be either a positive\_target or a negative\_target. A positive\_target is a word that is definitely known to “occur” in the given blank space. A negative\_target is a word that is definitely known to “not occur” in the given blank space. The negative\_target is created by randomly choosing a word from all the words constituting the vocabulary of the language. The length of the sentence is known as the window\_size or the context\_size of the model and the number of words in the entire corpus is known as the vocabulary of the language.

So to recapitulate, the inputs to a function training the Word2Vec model are the context, the positive\_target and the



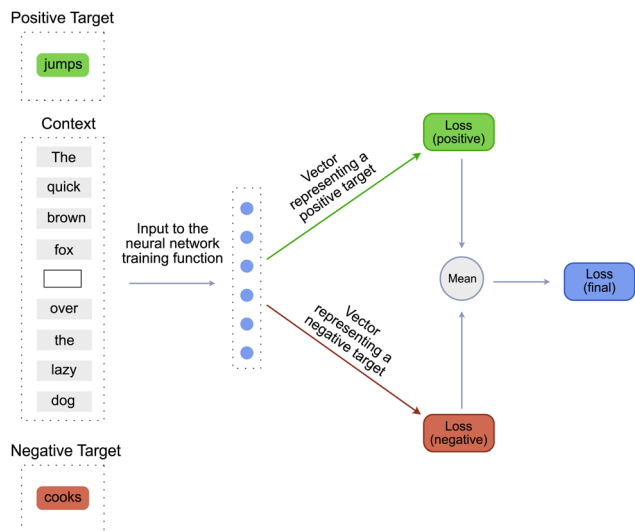


Fig. 2 Word2vec model (CBOW) that predicts the target word given the context.

negative\_target [Fig. 2]. This function then trains the model using the following three-step process.

1. The context words are used as an input to a single layered neural network to predict a vector representing the positive\_target. The predicted vector is then compared with the vector of the ground truth positive word to calculate a positive\_score. This score is then used to calculate a positive\_loss.

2. The same context words, coupled with the same neural network are then used to predict a vector representing the negative\_target. Then similar to step 1, the predicted vector is compared with the ground truth to calculate a negative\_score. This score is then used to calculate a negative\_loss.

3. The positive\_loss and negative\_loss are then combined using the mean function to calculate the final\_loss. This final\_loss is then used to backpropagate the errors and adjust the weights and biases of the neural network as well the embedding vectors of the context words.

The above process is repeated for every word in each sentence of the entire corpus. As the training progresses, the model learns which target words occur in which context. Once the model training is complete, the embeddings vectors of context words are retrieved to be used as a part of further downstream analysis.

Word2Vec model has two variants, CBOW (Continuous Bag of Words) and SkipGram. The model described above is the CBOW variant of the Word2Vec model. SkipGram variant is the exact inverse of the CBOW variant. In the SkipGram variant, instead of predicting a target\_word, the model predicts a target\_context. So the inputs to the training function of the SkipGram variant are the target\_word, the positive\_context and the negative\_context [Fig. 3]. The positive\_context contains the words that are definitely known to “occur” around the target\_word and negative\_context contains the words that are definitely known to “not occur” around the target\_word. The negative\_context is created by randomly sampling words from

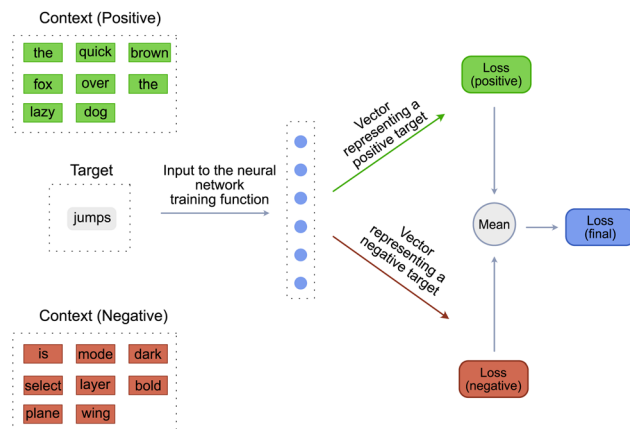


Fig. 3 Word2vec model (SkipGram) that predicts the context given the target word.

the vocabulary of the language. The remaining steps in the training function are similar to the CBOW variant except for the inputs to the single layered neural network. Contrary to the CBOW variant, the input to the neural network is a target\_word and the output is a tensor representing the context. This tensor is then compared with the tensor of the ground truth positive and negative contexts to obtain a positive and negative score. These scores are then used to calculate the respective losses, which are combined to get the final loss.

The authors of the DeepWalk algorithm hypothesized that the language models work by sampling from a hidden unobservable language graph.<sup>18</sup> This means that every graph can be thought of as encoding the semantics of a hidden unobservable language. So, the first step of the DeepWalk algorithm is to perform short random walks on the graph to sample a series of nodes. The random walks performed in DeepWalk are a classical Markovian process<sup>22</sup> *i.e.*, the probability of selecting the next node in the walk is only dependent on the currently selected node. Now, these series of nodes can also be thought of as a series of words adding up to form a complete sentence. Thus performing  $N$  random walks on the graph can be thought of as sampling a set of  $N$  sentences from a graph. These sentences *i.e.*, series of words are now used as an input to a language model such as the Word2Vec model to learn a dense vector representation of every node in the graph [Fig. 4].

## 2.5 TripleWalk approach

As described earlier, a unit of information in a knowledge graph is encoded by a triple in the form of head  $\rightarrow$  relation  $\rightarrow$  tail. Thus, to learn an effective representation of a knowledge graph it is essential to consider this triple structure. The TripleWalk algorithm modifies the DeepWalk algorithm to effectively exploit this triple structure. It does so by modifying the process of performing the random walks and also the process of using these random walks to train the Word2Vec model.

In the DeepWalk approach of performing random walks, the directionality of the edges is not considered. At any point of time when the walker is on a head or a tail node, it has a choice of either selecting one of the tail nodes that come after a head



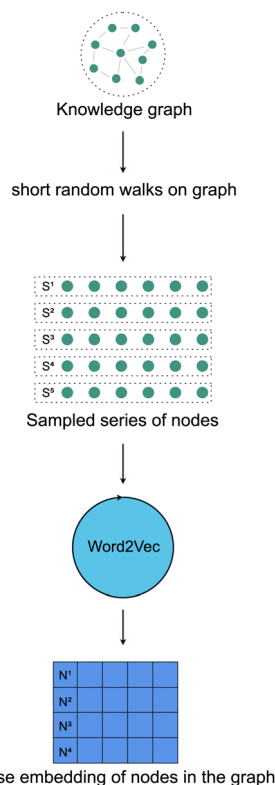


Fig. 4 DeepWalk model.

node or one of the head nodes that come before the tail node. Since the walker does not take into account the directionality of the edges, it has an equal probability of choosing a head node or a tail node. If it samples a head node then it inadvertently ends up breaking the semantic organization of the underlying knowledge graph.

Contrary to the DeepWalk approach, the TripleWalk approach does not sample one node at a time, but samples one triple at a time. Thus, the probability of choosing the next triple in the walk is dependent only on the currently selected triple. Further, the TripleWalk approach also considers the directionality of the relation between triples. At any point of time, given a triple sequence  $T_1 \rightarrow T_2 \rightarrow T_3 \rightarrow T_4 \rightarrow T_5$ , a triple walker at position  $T_3$  will only sample  $T_4$  and not  $T_2$ . Thus, by sampling one triple at a time and by considering the directionality of the triple relations, the TripleWalk approach is able to preserve the semantic structure of the underlying graph when sampling a sequence to be used in the Word2Vec model (Fig. 5).

Once these triple are sampled, the next step is to learn an embedding of entities that make up these triples. For this we lean on our assumption mentioned earlier, that considers a knowledge graph as a combination of three distinct graphs – head\_graph, relation\_graph and tail\_graph that hold the heads, relations and tails respectively.<sup>1</sup> To model this assumption, the sampled triple sequence  $S = \{(h_1, r_1, t_1), (h_2, r_2, t_2), (h_3, r_3, t_3), (h_4, r_4, t_4)\}$  is split into three independent sequences holding heads ( $H = \{(h_1, h_2, h_3, h_4)\}$ ), relations ( $R = \{(r_1, r_2, r_3, r_4)\}$ ) and tails ( $T = \{(t_1, t_2, t_3, t_4)\}$ ) respectively. These three

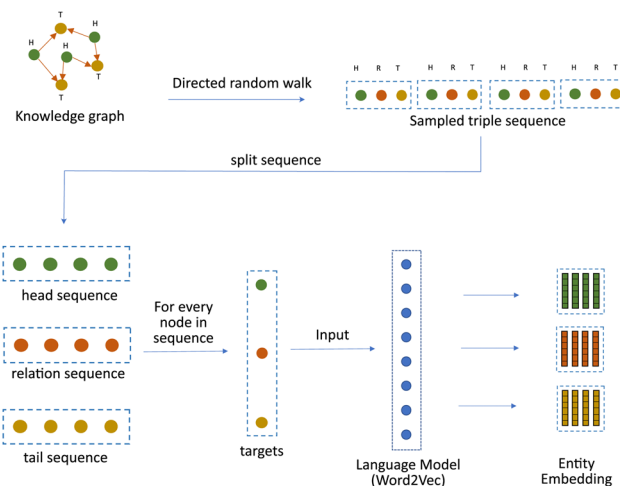


Fig. 5 TripleWalk model.

independent sequences are then used to train a modified Word2vec model.<sup>5</sup>

As described in Section 2.4, the input to the function used to train Word2Vec model are the context, the positive\_target and the negative\_target. Thus, for every independent sequence, a context, a positive\_target and a negative\_target is created. This gives us a set of three contexts – head\_context ( $H_c$ ), relation\_context ( $R_c$ ) and tail\_context ( $T_c$ ), a set of three positive targets – head\_pos\_target ( $H_p$ ), rel\_pos\_target ( $R_p$ ) and tail\_pos\_target ( $T_p$ ) and a set of three negative targets – head\_neg\_target ( $H_n$ ), rel\_neg\_target ( $R_n$ ) and tail\_neg\_target ( $T_n$ ). All the above contexts and targets are then used as an input to a function used to train the Word2Vec model [Fig. 6].

The function used to train the Word2Vec model is similar to the one used in DeepWalk model. As described earlier, the DeepWalk training function optimizes the embedding vectors of the context nodes using a single layered neural network. Similar to the DeepWalk training function, the TripleWalk training function also contains a single layered neural network, but instead of optimizing a single context embedding, it jointly optimizes the three independent sets of context embeddings corresponding to the head, relation and tail contexts. To do so, it follows a four-step process.

1. The head\_context ( $H_c$ ) along with the head\_pos\_target ( $H_p$ ) and head\_neg\_target ( $H_n$ ) are used to calculate a head\_loss.
2. The relation\_context ( $R_c$ ) along with the rel\_pos\_target and rel\_neg\_target ( $R_n$ ) are used to calculate a relation\_loss.
3. The tail\_context ( $T_c$ ) along with the tail\_pos\_target ( $T_p$ ) and tail\_neg\_target ( $T_n$ ) are used to calculate a tail\_loss.
4. All these losses are then combined using the mean function to obtain a final\_loss. This final\_loss is then used to backpropagate the errors and adjust the weights and biases of the neural network as well the embedding vectors of all the three contexts.

The above process is repeated for every triple sequence sampled by the TripleWalk algorithm to minimize the final\_loss. Once the training process is complete, the embedding





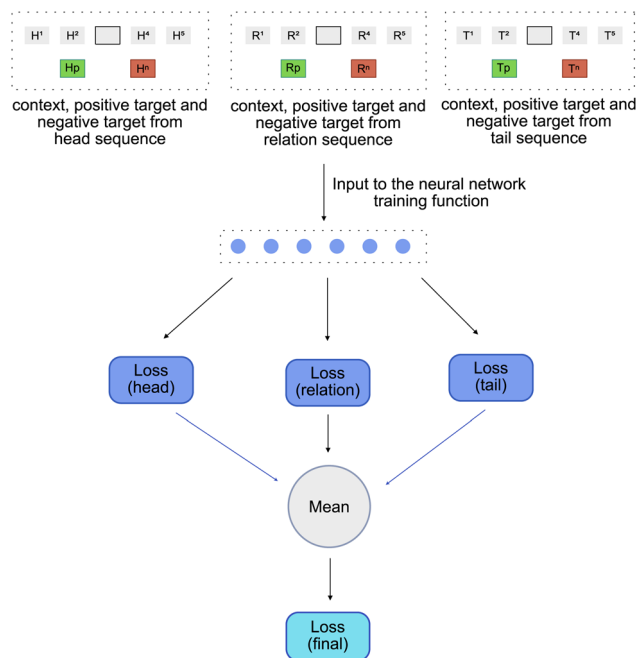


Fig. 6 Modified Word2Vec model.

vectors of the head context, relation context or the tail context are retrieved to perform further downstream analysis.

## 2.6 Supervised learning

The task of identifying new interactions in the kinase–substrate interaction network can be generalized to a binary classification task of predicting if a given interaction is true or false. For this, we use a classical supervised machine learning algorithm – Random Forest.<sup>23</sup> The input to the model is an embedding vector representing the target interaction and the output is a binary value representing the plausibility of the interaction being true or false. To construct an embedding vector denoting this interaction, we retrieved a list of all the kinase → phosphorylates → substrate triples from the knowledge graph. Then, in a given triple we retrieve the embedding vector for kinase entity from the head\_context embeddings and for the substrate entity from the tail\_context embeddings. Then according to the approach described by the authors of Node2Vec algorithm,<sup>19</sup> we combine these embeddings using the hadamard ( $\odot$ ) operator to obtain the final interaction embedding vector ( $\vec{I}$ ).

## 2.7 Negative sampling

Since the supervised model is a binary classification model, we also need to have negative samples to represent the interactions that have a lower likelihood of being true. But adequate ground truth data about negative interactions is not available. There are existing databases such as negatome<sup>24</sup> that provide a catalog of manually curated negative interactions, but we found that their coverage of negative interactions is not adequate. Hence, it is important to adopt a well-thought-out approach to generating negative samples to augment existing negative

interaction data. Since knowledge graphs contain only positive samples, some approaches to generating negative samples have been proposed.<sup>25</sup> The most simple approach being corrupting a triple by randomly changing the head, relation or tail.

In this case, we were only interested in negative samples involving kinase–substrate interaction triples. Initially, we trained the supervised classification model using the naive negative sampling approach of corrupting the tails. The resulting model did not perform sufficiently (AU-ROC = 0.57). We hypothesized that the drop in performance was due to the fact that randomly corrupting the tails of triples did not yield samples that truly represented the underlying biology of a kinase–substrate interaction. Also, since the number of unknown kinase–substrate interactions is very high, there is an increased likelihood of true positive samples being labelled as negative samples. Hence, we decided to develop a better approach to generating negative samples. We assumed that if a kinase and a substrate were physically apart by being located in two distinct cellular components then the probability of them interacting is lower than if they were located in the same cellular component. To model this assumption, we generated negative samples using the following four-step process:

1. Create a filtered knowledge graph containing only kinase–substrate interaction triples and triples from the cellular component subtree of the GO ontology.
2. Generate an embedding of every kinase and substrate in terms of its subcellular location by performing graph representation learning on this knowledge graph.
3. Using this embedding, for every kinase sample  $N$  substrates that are as far away as possible in the embedding space by use cosine similarity to calculate the distance between a kinase and a substrate.
4. To balance out the possibility of the model being biased towards the subcellular location, combine the above sampled list with ground truth negative samples from negatome – a database containing manually curated negative samples.<sup>24</sup>
5. Finally, sample from the above list to create a definitive list of negative interactions.

After generating the negative samples using the above approach, we needed to verify if the generated negative samples contained substrates in cellular compartments that were distinct from kinases. Hence, we created a list of kinases that were located in the nucleus of the cell. Then we retrieved the negative interaction partners (substrates) for these kinases. We then visualized the embedding vectors of these kinases and substrates using a tSNE plot [Fig. 7]. It can be observed that the nuclear kinases and the corresponding sampled negative substrates are fairly well separated in the tSNE space.

## 2.8 Model training and evaluation

Our model training pipeline starts with a simple kinase–substrate interaction network containing only one type of triple: kinase → phosphorylates → substrate. We split this network into three subnetworks – training (60%), validation (20%) and testing (20%). We then augment the training network with auxiliary triples to construct the full phosphoproteomic



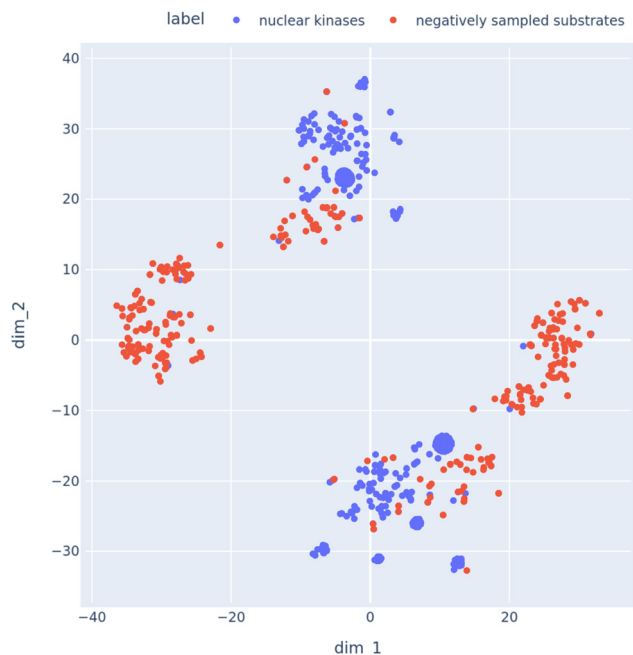


Fig. 7 tSNE plot to visualize the embeddings of kinases and their analogous sampled substrates using the negative sampling technique described in Section 2.7.

knowledge graph. This knowledge graph is then used to train the unsupervised component (Triple Walk model). The unsupervised component learns embeddings for every kinase and substrate in the phosphoproteomic knowledge graph. These entity embeddings are then passed to the supervised component (Random Forest model).

The input to the supervised component is a vector constructed by concatenating the embedding of a kinase and a substrate. This vector represents an interaction event between a kinase and a substrate. The output from the supervised component is a probability of the given kinase–substrate interaction being true. The validation network is used for hyperparameter tuning and the testing network is used to evaluate the final model performance [Fig. 8]. We evaluate the model using area under receiver operating characteristic curve (AU-ROC), Precision and recall [Table 3].

## 2.9 Evaluation of unsupervised learning component

In addition to evaluating the final model, we also compare the unsupervised learning component (TripleWalk algorithm) with existing unsupervised knowledge graph learning methods. We compare our approach with two of the most commonly used random walk based approaches – DeepWalk<sup>18</sup> and Node2vec,<sup>19</sup> one tensor decomposition based approach – DistMult<sup>26</sup> and one distance based approach – TransE.<sup>15</sup> In addition to comparison with above methods, we also compare the SkipGram and the Continuous Bag of Words (CBOW) variants<sup>17</sup> of all the random walk based methods. Finally, in addition to evaluating the interaction prediction performance, we also evaluate the embeddings on following tasks.

1. Kinase – Substrate classification: We formulate a binary classification task to classify kinases and substrates based on

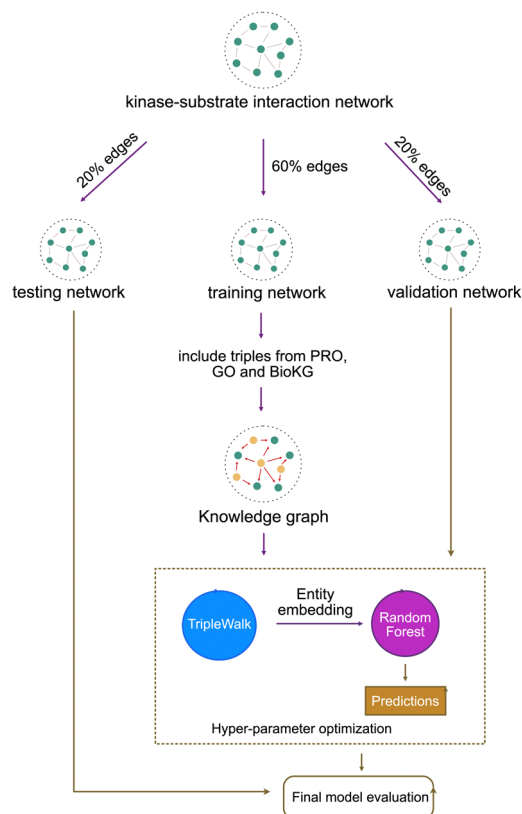


Fig. 8 TripleWalk model training and hyperparameter optimization.

the learned embeddings. The classification task is a balanced classification task where we sample one substrate for each of the 408 human kinases. We then use the embeddings obtained by unsupervised learning to train a classifier to classify the entities as either a kinases or substrates.

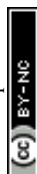
2. Enzyme classification: All kinases can be generalized as enzymes. Enzymes are classified into six broad categories and numerous sub-categories based on the chemical reactions they catalyze. These enzyme categories are represented by an enzyme classification (EC) number. We use these EC numbers to create three sub-categories for kinases present in our kinase–substrate interaction network. We then use the embeddings of the kinases to formulate a one vs rest classification task to classify kinases into their respective categories.

## 3 Results

### 3.1 Model hyperparameters and performance

We optimize the parameters for the unsupervised component by using the adaptive asynchronous halving algorithm (ASHA)<sup>27</sup> and for the supervised component using Random Grid Search algorithm. The best performing hyperparameters for the TripleWalk model are provided in Table 1.

The results from training all the models using the best hyperparameters are shown in Table 2. To generate the results we split the kinase–substrate interaction network into  $K$  folds where  $K = 10$ . This gave us 10 sets of training, validation and



**Table 1** Best performing hyperparameters for the TripleWalk (SkipGram) model

Unsupervised (TripleWalk and SGNS)	
Parameter	Value
Batch size	128
Learning rate	0.0004
Embedding dimension	256
Random walk length	17
Random walks per node	6
Early stopping delta (loss)	0.1
Early stopping patience (epochs)	5
Number of negative samples per positive sample	2.0
Supervised (Random Forest)	
Parameter	Value
Number of Estimators	420
Max depth	176
Split criterion	Entropy
Max features	128
Min samples for split	5
Min samples at leaf	4

testing networks. Then for every fold we augmented the training network with auxiliary triples and performed a complete training and evaluation run as shown in Fig. 8. This gives us 10 scores where every score is slightly different from each other. The final score is the mean of all the 10 scores. The error measures indicate the standard deviation of the 10 scores. The data for training, validation and testing data for every fold is available in ESI† file 1 and the raw scores for every fold are available in ESI† file 2. It can be observed that for our primary task of predicting a kinase–substrate interaction, the TripleWalk algorithm coupled with the SkipGram model outperforms all other types of algorithms. For the kinase classification task the TripleWalk algorithm coupled with CBOW model outperforms all other algorithms and for the enzyme classification task DeepWalk model coupled with the CBOW model gives the best results. It is worth noting that CBOW model has a much more consistent performance compared to the SkipGram model irrespective of the type of random walks. This might be due to the fact that in the CBOW model contrary to the SkipGram model, we predict the target word given the context words. This might have a regularising effect on the model, preventing it from learning the noise in the data and thus leading to a much more stable performance. It is also interesting to observe that Distmult, a tensor decomposition based approach shows competitive performance with random walk based

methods, despite being a much simpler algorithm. The final predictions from our model are available in ESI† file 3.

After comparing our model with existing random walk based methods, we also compared our model with other kinase–substrate prediction models. Since many of the existing models do not publish their training, testing datasets and hyperparameters, it is difficult to perform a fair comparison among all the models. Hence for the purpose of this study, we used the predictions datasets published by authors of the LinkPhinder<sup>28</sup> study. One thing to note is that compared to existing models, our model can only make predictions at the kinase–substrate level instead of the kinase–substrate–site level. The predictions from our model are in the form of a three column vector containing – [kinase, substrate, probability] and the predictions from existing models are in the form of a four column vector containing – [kinase, substrate, site, probability]. This means that for a given [kinase–substrate] pair our model will have only probability, but other models will have *N* probabilities corresponding to *N* sites. Hence, to make this comparison possible we reshaped the predictions data from other models to match our predictions data. To do so, we just selected the probability assigned to the top scoring site and used it as the probability of the given [kinase–substrate] pair interacting with each other.

The results from our comparison are shown in Table 3 and the predictions used to generate the results are available in ESI† file 2. It can be observed that the knowledge graph based models such as TripleWalk and LinkPhinder show a significantly better performance compared to the sequence based models such as NetPhosphK<sup>29</sup> and Scansite.<sup>30</sup> Further, it can be observed that the TripleWalk model shows competitive performance compared to the LinkPhinder model despite not including sequence based features in the knowledge graph. This might be indicative of the fact that it would be beneficial to combine the knowledge graph construction approach proposed by LinkPhinder with the knowledge graph learning algorithm proposed by TripleWalk to further improve the performance.

### 3.2 Ablation study

After building our models, we wanted to understand the factors that contribute to the improved predictive performance. Model interpretability can be achieved by either building simpler models that are intrinsically explainable or by post predictive analysis of the trained models. Since our framework consists of multiple models working together, the simplest approach to

**Table 2** Comparative performance of unsupervised learning components on interaction prediction, kinase classification and enzyme classification

Model	Interaction prediction	Kinase classification	Enzyme classification	Model type
TripleWalk (skip gram)	<b>0.79</b> ( $\pm 0.01$ )	0.67 ( $\pm 0.03$ )	0.59 ( $\pm 0.02$ )	Directed random walk
TripleWalk (CBOW)	0.71 ( $\pm 0.03$ )	<b>0.84</b> ( $\pm 0.02$ )	0.68 ( $\pm 0.03$ )	Directed random walk
DeepWalk (skip gram)	0.60 ( $\pm 0.01$ )	0.57 ( $\pm 0.01$ )	0.61 ( $\pm 0.02$ )	Undirected random walk
DeepWalk (CBOW)	0.69 ( $\pm 0.01$ )	0.72 ( $\pm 0.02$ )	<b>0.72</b> ( $\pm 0.03$ )	Undirected random walk
Node2Vec (skip gram)	0.62 ( $\pm 0.01$ )	0.60 ( $\pm 0.04$ )	0.62 ( $\pm 0.03$ )	Biased random walk
Node2Vec (CBOW)	0.71 ( $\pm 0.01$ )	0.70 ( $\pm 0.03$ )	0.67 ( $\pm 0.03$ )	Biased random walk
Distmult	0.63 ( $\pm 0.01$ )	0.78 ( $\pm 0.02$ )	0.67 ( $\pm 0.04$ )	Tensor decomposition
TransE	0.61 ( $\pm 0.01$ )	0.57 ( $\pm 0.01$ )	0.57 ( $\pm 0.03$ )	Geometric distance





**Table 3** Comparison of TripleWalk with existing kinase–substrate interaction prediction models

Model	AU-ROC	Precision	Recall
TripleWalk	0.76	0.62	0.88
LinkPhinder	0.75	0.60	0.76
NetPhospK	0.52	0.61	0.17
Scansite	0.53	0.60	0.17
NetworKIN	0.55	0.59	0.36

achieving interpretability in our system would be to quantify the change in predictive performance on changing the input data. For this we follow a two-part approach. In the first part we remove only a particular set of triples while keeping all other triples in knowledge graph. We then train the model using the hyperparameters shown in Table 1. In the second part, we keep triples related to only a particular subset of knowledge graph while removing all other triples.

Tables 4 and 5 show the relative performance of models trained on specific subsets of the knowledge graph. It can be observed that on removing triples related to BIOKG while keeping triples related GO and PRO ontologies leads to a modest drop in performance. On the other hand training models with only the BIOKG triples without any ontology information leads to a pretty significant drop in performance. Further, training models with only GO or only PRO ontologies leads to a pretty significant increase in performance.

These results though interesting, are not entirely surprising. When we integrated the GO and PRO ontology information into our knowledge, we included the triples denoting relations all the way up to the root node of the ontology. This allowed our model to learn a much better representation of kinases and substrates in terms of their shared evolutionary, molecular and functional ancestry. BIOKG on the other hand includes triples that denote relationships only at the leaf node without

following them up the ontology tree. Thus, even though it brings a lot of information, it is only useful in conjunction with a more complete picture provided by the ontologies.

### 3.3 Functional enrichment analysis

After validating our frameworks predictive performance, we studied the highest confidence predictions for kinases with the least amount of information. We retrieved the list of understudied kinases from illuminating the druggable genome project (IDG).<sup>31</sup> This gave us a list of 144 potentially understudied kinases. We further filtered these kinases to only include the kinases that have at-most two recorded interactions in the iPTMnet database. This gave us a list of 68 kinases that are potentially understudied with respect to both IDG and iPTMnet. We then used the PredKinKG framework to predict novel interactions for these kinases. We filtered the predictions to only include high confidence predictions by setting the probability score cutoff at 0.95. Below we present the functional enrichment analysis of Q02779 (MAP3K10) using its 188 novel predicted substrates.

Since the target kinase is understudied and its biological functions is poorly understood, we hypothesized that studying the functions of the predicted substrates may provide us with clues about its biological roles. For this we perform a GO enrichment analysis using STRING DB.<sup>11</sup> Table 6 provides an overview of the top five GO terms (according to strength and FDR) enriched for every GO sub-ontology.

GO enrichment analysis of the interaction network of Q02779 (MAP3K10) suggests that it might play an important role in the maintenance and upkeep of the cellular DNA and regulation of DNA transcription. We can observe that the GO term – GO:0090240 (positive regulation of histone h4 acetylation) has the highest enrichment strength. Histone-H4 is a part of the nucleosome complex which is one of the fundamental structures related to DNA organization in eukaryotes. Acetylation of Histone-H4 is associated with a relaxation of the nuclear chromatin leading to an increased transcription factor binding<sup>32</sup> and recruitment of protein complexes for repair of double-stranded breaks in the DNA.<sup>33</sup> In addition to histone acetylation, we can also observe that several GO terms related to DNA damage and repair are enriched: GO:0090400 (DNA ligation involved in DNA repair), GO:0006978 (DNA damage response, signal transduction by p53), GO:0042771 (intrinsic apoptotic signaling pathway in response to dna damage by p53 class mediator). Analyzing the GO terms related to cellular component, it is evident that the interaction partners of Q02779 (MAP3K10) are mostly located in the nucleus near the chromosomes thus further cementing its role in DNA repair and transcription.

## 4 Discussion and future work

In this work we have presented our framework for learning from a heterogeneous knowledge graph to predict substrates for understudied kinases. We build a kinase–substrate knowledge

**Table 4** (Part A) Abalation study showing relative importance when a set of triples are removed from KG

Data	Interaction prediction
BIOKG complex (removed)	0.75 ( $\pm 0.01$ )
BIOKG pathways (removed)	0.77 ( $\pm 0.01$ )
BIOKG diseases (removed)	0.78 ( $\pm 0.01$ )
PRO (removed)	0.79 ( $\pm 0.01$ )
GO biological process (removed)	0.79 ( $\pm 0.03$ )
GO molecular function (removed)	0.79 ( $\pm 0.01$ )
COMPLETE KG	0.79 ( $\pm 0.01$ )

**Table 5** (Part B) Abalation study showing relative importance when including only one set of triples in KG

Data	Interaction prediction
BIOKG complex (only)	0.60 ( $\pm 0.02$ )
BIOKG pathways (only)	0.61 ( $\pm 0.02$ )
BIOKG diseases (only)	0.63 ( $\pm 0.02$ )
GO biological process (only)	0.84 ( $\pm 0.01$ )
GO molecular function (only)	0.83 ( $\pm 0.01$ )
PRO (only)	0.82 ( $\pm 0.01$ )
COMPLETE KG	0.79 ( $\pm 0.01$ )



Table 6 Enriched GO terms for Q02779 (MAP3K10) interaction partners

Biological process			
GO:ID	Description	Strength	FDR
GO:0090240	Positive regulation of histone h4 acetylation	1.65	0.005
GO:0070601	Centromeric sister chromatid cohesion	1.65	0.005
GO:0090400	DNA ligation involved in DNA repair	1.60	0.00091
GO:0006978	DNA damage response, signal transduction by p53 class mediator resulting in transcription of p21 class mediator	1.45	0.0019
GO:0042771	Intrinsic apoptotic signaling pathway in response to dna damage by p53 class mediator	1.24	0.0014
Molecular function			
GO:ID	Description	Strength	FDR
GO:0031490	Chromatin dna binding	1.03	0.0003
GO:0070491	Repressing transcription factor binding	1.00	0.0014
GO:0019901	Protein kinase binding	0.78	$9.3 \times 10^{-15}$
GO:0051721	DNA-binding transcription factor binding	0.78	$6.02 \times 10^{-8}$
GO:0061629	RNA polymerase II-specific DNA-binding transcription factor binding	0.75	$4.32 \times 10^{-5}$
Cellular component			
GO:ID	Description	Strength	FDR
GO:0005719	Lateral element	1.48	0.0013
GO:0005721	Pericentric heterochromatin	1.40	0.0003
GO:0000778	Condensed nuclear chromosome kinetochore	1.37	0.0029
GO:0000780	Condensed nuclear chromosome, centromeric region	1.24	0.0012
GO:0051233	Spindle midzone	1.16	0.0025

graph by integrating data from ontologies such as GO and PRO and existing knowledge graphs such as BIOKG. We then developed a novel knowledge-graph representation learning approach to learn better representations of kinases and substrates in this knowledge graph. Unlike many existing approaches, our framework can take advantage of semantic data from existing databases to exploit the knowledge of well studied kinases to make predictions for understudied kinases. We also perform an ablation study to quantify the relative importance of various components of our knowledge graph. We found that the hierarchical information from ontologies in combination with the factual information from existing knowledge graphs contributes significantly to learning a better representation of kinases and substrates.

A significant advantage of our methods over existing methods is the simplicity of the data representation and the simplicity of learning from this data representation. Existing machine learning systems require complex preprocessing and data transformation before the data is used for model training. These data transformations take a lot of manual effort and also have the potential to influence the model performance if done incorrectly. In our work, we present an alternative approach. We arrange the data in a very simple form containing only a list of triples. Each triple represent a discrete fact about the real world. We then propose a very simple random walk based algorithm to learn from this data. Since random walk based methods do not require the user to have any knowledge about the semantics or the structure of the underlying graph, our approach allows the user to scale their analysis without spending a lot of manual effort on studying the semantics of the underlying data. This property also means that our approach can be easily repurposed to target alternative domains. For example,

the user could change the kinase–substrate knowledge graph to include only mouse data and thus repurpose the system to predict kinase–substrate interactions in mouse models. The user can also use our triple walk algorithm to learn a representation of knowledge graphs in a completely different domains such as social-networks, citation-networks or computer networks by using our publicly available python package.<sup>34</sup>

A significant shortcoming of our approach is that it can make predictions only at kinase/substrate level and not at the kinase/phosphorylation site level. Thus, as a next step of our study we plan to extend our model to make predictions at the phosphorylation site level by integrating with the approach proposed by Deznabi *et al.* in their DeepKinZero model. In addition to extending to model to site level, we also plan to integrate attention mechanism in our unsupervised knowledge graph learning component to get a better insight into the factors that contribute to learning a good representation of kinases and substrates.

Since the goal of this work was to develop a system to utilize semantic data (knowledge graphs) for the purpose of predicting kinase–substrate interactions, we did not perform an in depth comparison with existing kinase–substrate interaction prediction tools but only a superficial comparison as shown in Table 3. Alternatively, since we proposed a new knowledge graph learning algorithm that exploits the triple structure of the graph, we performed an in-depth comparison with existing knowledge graph learning algorithms [Table 2]. A direct comparison between our tool and the existing tools is not possible due to the differences in the data used for training the algorithms used in these tools. The data for positive samples is readily available from established databases, but data about



negative samples is not readily available. Thus, every tool uses its own method to generate negative samples which complicates the comparison. A comprehensive evaluation will require a more focused approach that uses a standardized dataset with properly specified training, testing splits and negative samples. Since developing such a dataset is a non-trivial task, we plan to perform this comparison as its own independent study.

## Data availability

The data and code used to perform the above analysis can be found at: [https://github.com/udel-cbcb/ikg\\_v2\\_public.git](https://github.com/udel-cbcb/ikg_v2_public.git). The code for the triple walk algorithm can be found at: [https://github.com/udel-cbcb/triple\\_walk.git](https://github.com/udel-cbcb/triple_walk.git). The training, testing and validation data are available in supplementaryESI† file 1, the evaluation scores are available in supplementaryESI† file 2 and the predictions from the final model are available in supplementaryESI† file 3.

## Author contributions

Sachin Gavali: conceptualization, data curation, methodology, software, formal analysis, writing – original draft. Karen E. Ross: data curation, validation, writing – review and editing. Chuming Chen: data curation, writing – review and editing, supervision. Julie Cowart: data curation, writing – review and editing. Cathy H. Wu: supervision, project administration, funding acquisition.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

This work has been supported by the National Institutes of Health (Grant-R35GM141873) and Sigma Xi Grants in Aid of Research (Grant-G20201001105037737). We would also like to acknowledge the Data Science Institute and Center for Bioinformatics and Computational Biology at University of Delaware for providing computing resources through the Caviness and Biomix high performance computing clusters respectively.

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