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The impacts of molecular adsorption on antiferromagnetic MnPS<sub>3</sub> monolayers: enhanced magnetic anisotropy and intralayer Dzyaloshinskii–Moriya interaction<sup>†</sup>

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In two-dimensional (2D) magnetic systems, significant magnetic anisotropy is required to protect magnetic ordering against thermal fluctuation. In this paper, we explored the effect of molecular adsorption on the magnetic anisotropy and intralayer Dzyaloshinskii-Moriya interaction (DMI) of monolayer MnPS<sub>3</sub>, combining the first-principles calculation and theoretical analysis. We find that molecular adsorption can break the spatial inversion symmetry in a 2D magnet, and results in a significant DMI, which is rare in pristine 2D magnets. For example, in an MPS-NO system, the magnitude of the asymmetric DMI vector increases 9 times, and the magnetocrystalline anisotropy increases 600 times compared with the pristine MPS monolayer. It is found the DMI mainly comes from the structural deformation after adsorption, whereas the increase of magnetocrystalline anisotropy mainly originates from a new 'bridge' super-exchange interaction between Mn ions and NO gas molecules. The calculated Mn-NO-Mn 'bridge' super-exchange coupling strength is much higher than the Mn-S-Mn coupling strength. Our findings offer a new strategy to increase the magnetic anisotropy and induce chiral magnetic structures in 2D magnets.

#### New concepts

In two-dimensional (2D) magnetic materials, the sizable magnetic anisotropy is a key factor in resisting thermal fluctuations and protecting long-range magnetic ordering, while the antisymmetric exchange interaction, Dzyaloshinskii-Moriya interaction (DMI), is a prerequisite to generate chiral magnetic structures, such as chiral domain walls, helical spins, and skyrmions. However, significant DMI is rare in pristine 2D magnetic materials. In this paper, molecular adsorption is employed to enhance the magnetic anisotropy and induce DMI in antiferromagnetic MnPS3 monolayers. In the MnPS3-NO system, the magnitude of the asymmetric DMI vector increases 9 times, and the magnetocrystalline anisotropy increases 600 times as compared with the pristine MnPS3 monolayer. Combining the first-principles calculations and theoretical analysis, we find that the induced DMI mainly comes from the structural deformation after adsorption, whereas the increase of magnetocrystalline anisotropy mainly originates from a new 'bridge' super-exchange interaction between Mn ions and NO gas molecules. This study not only demonstrates the effect of molecular adsorption on inducing the intralayer DMI in centrosymmetric structures, but also provides an insightful understanding of the mechanism of superexchange interaction between gas molecules and 2D magnets.

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## 1. Introduction

In the past decades, magnetic materials have received substantial attention for their wide application in data storage,<sup>1,2</sup> energy harvesting,<sup>3,4</sup> biomedicine<sup>5</sup> and water purification.<sup>6</sup> In 1966, the Mermin–Wagner theorem suggested that long-range ferromagnetic or antiferromagnetic ordering is extremely rare in two-dimensional (2D) materials at non-zero temperature because of thermal fluctuations.<sup>7</sup> In magnetic materials, thermal fluctuation may destroy the ordered arrangement of spins (ferromagnetism or antiferromagnetism), resulting in a paramagnetic state. The discovery of long-range ferromagnetic ordering in few-layer  $CrGeTe_3^8$  and  $CrI_3^9$  in 2017 has stimulated a large number of theoretical and experimental efforts in studying the properties and applications of a diverse library of 2D magnets. Now it is widely accepted that the magnetic anisotropy energy (MAE) is one possibility to resist thermal fluctuation. The existence of magnetic anisotropy can

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reduce the total energy of the system and result in the presence of a spin-wave excitation gap. Overall, the magnetic anisotropy can make the spin orientation more stable, which improves the stability of magnetic ordering to withstand thermal fluctuations.<sup>8,10</sup> Thus, the magnetic anisotropy is a key factor in protecting the long-range magnetic ordering in 2D materials.<sup>11,12</sup> Furthermore, the successful synthesis of 2D magnets provides a promising platform to study the Dzyaloshinskii–Moriya interaction (DMI).<sup>13–15</sup> DMI, an antisymmetric exchange interaction between two magnetic atoms within one surface layer,<sup>16,17</sup> originates from spin–orbit coupling (SOC) and competes with the perpendicular magnetic anisotropy and the Heisenberg exchange coupling to generate chiral magnetic structures like chiral domain walls, helical spins, and skyrmions.<sup>18–20</sup> These chiral magnetic structures possess great application potential in next-generation memory devices.<sup>21</sup>

Unfortunately, the Curie/Néel temperature of 2D magnets is always much lower than room temperature, such as  $\sim 60$  K for CrGeTe<sub>3</sub>,<sup>8</sup> ~45 K for  $CrI_3$ ,<sup>9</sup> and ~130 K for Fe<sub>3</sub>GeTe<sub>2</sub>.<sup>22</sup> Consequently, the effects of thickness,<sup>23</sup> strain,<sup>24,25</sup> charge doping,<sup>26-29</sup> atomic doping,<sup>30,31</sup> intercalation,<sup>32-34</sup> and surface functionalization<sup>35-39</sup> on the Curie/Néel temperature of 2D magnetic materials were widely explored. For instance, the Curie temperature of Fe3GeTe2 can be increased from 180 K to 210 K under 0.65% stretch strain.40 Meanwhile, non-magnetic hexagonal boron nitride was functionalized with fluorine atoms, accounting for room-temperature ferromagnetism.<sup>36</sup> He et al.<sup>41</sup> found that the Curie temperature of CrGeTe<sub>3</sub> can be enhanced from  $\sim 61$  K to 81 K via NO<sub>2</sub> molecular adsorption. Besides, Wang et al.42 found that molecular adsorption could also strengthen the magnon-phonon scattering significantly. However, the influence of these strategies on magnetic anisotropy and DMI, indispensable prerequisites for long-range magnetic ordering<sup>11,12</sup> and chiral spin texture in 2D magnets,43-46 has been rarely studied. Although Ni et al.<sup>47</sup> detected a strain-dependent magnetic anisotropy in the inplane direction of few-layer MnPSe3 using the second-harmonic generation, while several studies reported the generation and manipulation of intralayer DMI in 2D magnets by strain<sup>48,49</sup> and defects,<sup>50</sup> and the effect of molecular adsorption is still unclear.

In this paper, density functional theory (DFT) calculations are used to investigate the magnetic anisotropy and DMI of an antiferromagnet MnPS<sub>3</sub> (MPS) monolayer, and the impacts of molecular adsorption are explored. 2D MPS has been synthesized in experiments, and also been demonstrated as an excellent adsorbent for NO<sub>2</sub> gas.<sup>51,52</sup> We find a new magnetic coupling induced by magnetic molecule adsorption according to the covalency, which has impressive impacts on the isotropic magnetic exchange coupling and the magnetocrystalline anisotropy of the MPS monolayer. Besides, we also observe significant intralayer DMI in the MPS monolayer with molecular adsorption. These findings offer a new insight to understand the influence of molecular adsorption on the magnetic properties of 2D materials.

## 2. Computational methods

For all DFT calculations, we employed the *Vienna ab initio* Simulation Package (VASP)<sup>53,54</sup> with the projected augmented wave (PAW) method and a cut-off energy of 550 eV. Meantime, the Perdew-Burke-Ernzerhof (PBE) of general gradient approximation  $(GGA)^{55,56}$  with the Hubbard ' $U^{57}$  was chosen as the exchange-correlation functional. It has been proved that when the effective 'U' value is 5 eV, the electronic bandgap of MPS is predicted as 2.40 eV,<sup>58</sup> which is close to the experimental result (2.96 eV).<sup>59</sup> The same 'U' value is also adopted in previous theoretical calculations by other authors.<sup>60,61</sup> So in this work, the 'U' value is set as 5 eV. To suppress the non-physical interaction between the MPS monolayer and its adjacent imaging layer, a 20 Å vacuum space was imposed along the *c*-axis in all models, and the adsorption models were built based on a  $2 \times 2 \times 1$  supercell. The MPS monolayer was relaxed until the energy and the Hellmann-Feynman force converged to 10<sup>-8</sup> eV and 0.001 eV  $Å^{-1}$ , while adsorption models were optimized until the energy converged to  $10^{-6}$  eV. Monkhorst–Pack (MP) grids of  $9 \times 9 \times 1$  and  $13 \times 13 \times 1$  were used to sample the Brillouin zone in structure optimization and the self-consistent calculation, respectively. SOC is considered for the noncollinear calculation of the MPS monolayer with and without molecular adsorption. For the adsorption models, the van der Waals (vdW) interaction between the MPS monolayer and gas molecules was calculated at the DFT+D3 level.62

### 3. Results and discussion

# 3.1 Geometric structure and energy of the MPS-molecule system

MPS monolayers are exfoliated from the bulk, and the top view of the 2  $\times$  2  $\times$  1 supercell is shown in Fig. 1a. The lattice parameters of the optimized MPS are a = b = 6.05 Å, slightly larger than the experimental result (5.88 Å)<sup>63</sup> but consistent with previous theoretical results.<sup>64,65</sup> In each unit cell, there are two Mn atoms, six S atoms, and two P atoms. Obviously, every Mn atom is surrounded by six S atoms centrosymmetrically, while these S atoms connect to two P atoms forming five sublayers as shown in Fig. 1b. For clear illustration, the top and side views of MPS after deleting the repeated atoms are presented in Fig. 1c and d. In Fig. 1c, the smallest bridge between Mn pairs is up to 3.493 Å, while that between S and P pairs is 3.529 Å and 6.050 Å, respectively. These distances are so large that the bridge sites can be neglected in molecular adsorption. Therefore, we choose three adsorption sites including the top sites on Mn, S and P atoms as initial sites for gas molecular adsorption, which are remarked by square, triangle, and rhombus in Fig. 1c. It is noted that the gas molecules would move in a small range during geometry relaxation, resulting in a slight deviation from the initial adsorption site. To identify the most stable adsorption site, adsorption energy is defined as the energy difference between the MPS-molecule system, the isolated MPS and gas molecule, as shown in eqn (1).66,67

$$E_{\rm Ad} = E_{\rm MPS-Gas} - (E_{\rm MPS} + E_{\rm Gas}) \tag{1}$$

The calculated results are shown in Fig. 1e and Table S1 (ESI<sup>†</sup>). As is well-known, the lowest adsorption energy



Fig. 1 Top (a) and side (b) views of the MnPS<sub>3</sub> (MPS). (c and d) are the top and side views of MPS after removing the P and S atoms in the bottom layers for clean view. (e) The adsorption energy of the MPS-molecule system. In (c), the square, triangle, and rhombus represent the possible initial adsorption site for the top Mn, top P and top S sites, respectively.

corresponds to the most stable adsorption configuration. Thus, it can be concluded that the most stable adsorption site for CO, NH<sub>3</sub>, and NO is around the P atom, while that for N<sub>2</sub> and NO<sub>2</sub> is near the Mn atom, based on the obtained  $E_{Ad}$  results. Besides, the perpendicular orientation of CO, NH<sub>3</sub>, NO and NO<sub>2</sub> molecules is also tested, as shown in Fig. S1 (see the ESI<sup>†</sup>). We find that the MPS-CO, MPS-NH<sub>3</sub>, and MPS-NO systems with C/N atom pointing to the surface of the MPS substrate are more stable, while the O atom pointing toward the top surface of MPS is preferred for the MPS-NO<sub>2</sub> system. The adsorption energies for NO and NO<sub>2</sub> are up to -0.446 meV and -0.492 meV indicating strong binding, comparable to the values of NO and NO<sub>2</sub> absorbed on black phosphorus.<sup>68</sup> The different views of the stable adsorption system are presented in Fig. 2, where the vertical distance from the bottom of the molecule to the top surface of the MPS monolayer (black dotted line) is represented by 'd'. The smallest 'd' of 2.578 Å occurs in the MPS-NH<sub>3</sub> system, while the largest 'd' is 3.145 Å in the MPS-N<sub>2</sub> system. In the following section, we would explore the magnetic properties of these adsorption systems based on the stable structure presented in Fig. 2, especially the magnetic anisotropy and DMI.

#### 3.2 Magnetic properties of the MPS-molecule system

First, the magnetic ground state of the MPS monolayer is determined by its energies with four possible magnetic



Fig. 2 Geometric structure of MPS–CO (a), MPS–N<sub>2</sub> (b), MPS–NH<sub>3</sub> (c), MPS–NO (d) and MPS–NO<sub>2</sub> (e). The distance between the bottom of the molecule and the top surface of MPS is defined as 'd'.

configurations including ferromagnetic (FM), Néel-antiferromagnetic (Néel-AFM), zigzag-AFM, and stripy-AFM. The diagram of these four magnetic configurations are shown in Fig. S2 (ESI<sup>†</sup>) where the red and blue balls represent Mn atoms with spin-up and spin-down states, respectively. Based on the DFT calculations, we find that the Néel-AFM phase with the lowest energy thus is the magnetic ground state of the MPS monolayer. To identify the magnetic ground state, the spin density distribution of MPS is presented in Fig. 3a where the spin up and spin down states are represented by the orange and cyan isosurface, respectively. It can be observed that the magnetism of MPS mainly arises from Mn and S atoms, not the P atom. Furthermore, the magnetic moments on two Mn atoms in each unit cell ally in antiparallel, agreeing well with the magnetic ground state determined by energy.

According to local spin density approximation calculations, the magnetic moment on Mn is ~ 4.2  $\mu_{\rm B}$ , which is smaller than the ideal value of 5  $\mu_{\rm B}$ . Here, the altitude of spin vector *S* (*S*) is gained using eqn (2) based on the magnetic moment:

$$M = g\mu_{\rm B}\sqrt{S(S+1)} \tag{2}$$

where *g* is the Landau factor and  $\mu_{\rm B}$  is the Bohr magnetic moment. We obtained *S* of 1.66 when *g* of 2 is used. It has been proved that the value of next-nearest-neighboring exchange constant  $J_2$  in the MPS monolayer is one order of magnitude lower than the nearest-neighboring exchange constant  $J_1$ .<sup>60,63,65</sup> Therefore, we would focus on the nearest-neighboring magnetic exchange coupling for the MPS monolayer with and without molecular adsorption.

For a magnetic system, its Hamiltonian can be written as:  $^{\rm 14,69}$ 

$$H = H_{\text{EX}} + H_{\text{C-MAE}} + H_{\text{DMI}} + H_{\text{SIA}} + H_{\text{Zeeman}}$$
$$= -\frac{1}{2} \sum_{\substack{l, f \in NN \\ l \neq f}} \left[ J_{lf} \boldsymbol{S}_{l} \cdot \boldsymbol{S}_{f} + K_{lf} S_{l}^{z} S_{f}^{z} + \boldsymbol{D}_{lf} \cdot (\boldsymbol{S}_{l} \times \boldsymbol{S}_{f}) \right]$$
$$- \sum \left[ A_{zz} (S_{l}^{z})^{2} + g \mu_{\text{B}} \boldsymbol{B} \cdot \boldsymbol{S} \right]$$
(3)



**Fig. 3** Spin density distribution of MPS (a), MPS–CO (b), MPS–N<sub>2</sub> (c), MPS–NH<sub>3</sub> (d), MPS–NO (e), and MPS–NO<sub>2</sub> (f) systems. The orange and cyan isosurfaces represent the spin up and spin down states which are separated by  $\pm 0.001 \text{ e}$  Å<sup>3</sup>, respectively.

where  $H_{\text{EX}}$ ,  $H_{\text{C-MAE}}$ ,  $H_{\text{DMI}}$ ,  $H_{\text{SIA}}$  and  $H_{\text{Zeeman}}$  represent the energies from isotropic magnetic exchange coupling, magnetocrystalline anisotropic energy (C-MAE), DMI, single ion anisotropy (SIA) and Zeeman effect, respectively. In this paper, the external magnetic field is not considered, so that the Zeeman term is absent. *I*<sub>lf</sub> is the isotropic exchange coupling parameter between the nearest-neighboring (NN) Mn pairs, which can be calculated by the energy difference between FM and Néel-AFM states (see Fig. S2 in the ESI<sup>+</sup>). Here, we calculated three exchange coupling parameters  $(J_{lf}^{xx}, J_{lf}^{yy}, \text{ and } J_{lf}^{zz})$  of the pristine MPS monolayer when spins point along x-, y-, and z-axes, respectively. We found the difference  $(K_{lf} = J_{lf}^{zz} - (J_{lf}^{yy} + J_{lf}^{xx})/2)$ between these exchange coupling parameters is only  $-4.37 \mu eV$ , three orders of magnitude lower than  $(J_{lf}^{yy} + J_{lf}^{xx})/2$ , indicating an ignorable magnetocrystalline anisotropy along the z-axis in the pristine MPS monolayer. In this paper,  $(f_{lf}^{yy} + f_{lf}^{xx})/2$  is employed as the isotropic exchange coupling parameter  $J_{lf}$ .  $D_{lf}$  is the antisymmetric DMI parameter between the l-th and f-th Mn ions, including three elements  $(D_{lf}^x, D_{lf}^y, and D_{lf}^z)$ . The  $H_{DMI}$  can be written as

$$H_{\text{DMI}} = -\frac{1}{2} \sum_{\substack{l, f \in NN \\ l \neq f}} \boldsymbol{D}_{lf} \cdot \left(\boldsymbol{S}_{l} \times \boldsymbol{S}_{f}\right).$$

$$= -\frac{1}{2} \sum_{\substack{l, f \in NN \\ l \neq f}} \left[ \boldsymbol{D}_{lf}^{x} \left(\boldsymbol{S}_{l}^{y} \boldsymbol{S}_{f}^{z} - \boldsymbol{S}_{l}^{z} \boldsymbol{S}_{f}^{y}\right) - \boldsymbol{D}_{lf}^{z} \left(\boldsymbol{S}_{l}^{x} \boldsymbol{S}_{f}^{z} - \boldsymbol{S}_{l}^{z} \boldsymbol{S}_{f}^{x}\right).$$

$$(4)$$

The calculation of the three components of vector  $D_{lf}$  can be referred to Fig. S3 in the ESI.† The three components of vector  $D_{lf}$  are 0.096 meV, 0.036 meV, and -0.466 meV in MPS without gas molecules, much smaller than the absolute value of  $J_{lf}$ , which reveals very little asymmetry in the pristine MPS monolayer. Besides, if the magnetic system has an anisotropy along its easy-axis or easy-plane, the SIA coefficient  $A_{zz}$  can be estimated from the four magnetic states where the spins on the *l*-th Mn ion arrange along the  $\pm z$ - and  $\pm x$ -directions with spins on the *f*-th Mn ions along the *y*-axis.<sup>70</sup> Hence, it can be found that  $A_{ZZ} = (E_1 + E_2 - E_1 - E_4)/8S^2$ . The calculated  $J_{lf}$ ,  $K_{lf}$ ,  $D_{lf}$ and Azz of the MPS monolayer with and without molecular adsorption are presented in Table 1. We find that all of the parameters  $J_{lf}$  are negative, demonstrating antiferromagnetic interaction in the MPS substrate, which is consistent with the spin density distribution as shown in Fig. 3. To describe the strengthening of magnetic exchange coupling and antisymmetric DMI quantitatively, the increase ratio of  $J_{lf}$  and the magnitude of  $D_{lf}(|D_{lf}|)$  are defined as follows and are shown in Fig. 4.

$$\eta_{\rm B} = \frac{B_{\rm MPS_molecule} - B_{\rm MPS}}{B_{\rm MPS}} \times 100\% (B = J_{lf}, |\boldsymbol{D}_{lf}|)$$
(5)

The enhanced ratios of  $J_{lf}$  and  $|D_{lf}|$  are shown in Fig. 4a and b, respectively. We can find that the impact of molecular adsorption on the antisymmetric DMI is much more impressive

Table 1 The effective magnetic exchange constant  $(J_{tf})$ , the magnetocrystalline anisotropic constant  $(K_{tf})$ , the antisymmetric Dzyaloshinski–Moriya interaction (DMI) parameters ( $D_{lf}^{v}$ ,  $D_{f}^{v}$ , and  $D_{lf}^{z}$ ), the single ion anisotropic coefficient ( $A_{zz}$ ) and the charge transfer of the MPS monolayer with and without molecule adsorption. A positive charge transfer means the molecule donates the charge to the MPS substrate

SYSTEM	$J_{lf}$ (meV)	$K_{lf}$ (µeV)	$\boldsymbol{D}_{lf}^{x}$ (meV)	$\boldsymbol{D}_{lf}^{\boldsymbol{y}}\left(\mathrm{meV}\right)$	$\boldsymbol{D}_{lf}^{z}$ (meV)	$A_{\rm zz}$ (meV per atom)	Charge Transfer (e)
MPS	-5.958	-4.37	0.096	0.036	-0.466	-0.042	
MPS-CO	-6.013	-3.92	1.507	0.198	2.658	-0.046	0.024
MPS-N <sub>2</sub>	-6.026	-4.13	-0.788	1.157	-1.153	-0.046	0.033
MPS-NH <sub>3</sub>	-6.014	-4.22	-0.163	-0.794	1.903	-0.047	0.043
MPS-NO	-8.294	-2703.62	4.732	-1.126	-0.211	-4.602	0.030
MPS-NO <sub>2</sub>	-5.935	-5.05	1.644	0.030	1.864	-0.040	0.019

than on the isotropic magnetic exchange interaction. In the MPS-N<sub>2</sub> system, although  $J_{lf}$  only increases with 1.141%,  $|D_{lf}|$  is enhanced by 280.08%. In the MPS–NO system, both  $J_{lf}$  and  $|D_{lf}|$ increase noticeably, and the enhanced ratios are up to 39.208%  $(I_{lf})$  and 920.37%  $(|D_{lf}|)$ , respectively. This phenomenon is distinct from the results in previous studies.<sup>37,41</sup> Besides, we also investigate the effect of molecular adsorption on the C-MAE  $(K_{lf})$  and the SIA  $(A_{zz})$  through their ratios to  $J_{lf}$ , as shown in Fig. 5. It is worth emphasizing that both  $K_{lf}$  and  $A_{zz}$ are critical parts in the overall magnetic anisotropy, and play important roles in resisting thermal fluctuations in 2D magnetic materials.<sup>71</sup> There is little increase on  $K_{lf}$  and  $A_{zz}$  after molecular adsorption except for NO, and the corresponding ratios of  $K_{lf}$  and  $A_{zz}$  to  $J_{lf}$  are much smaller than 10% revealing very weak magnetic anisotropy. Surprisingly, the  $K_{lf}$  and  $A_{zz}$  in the MPS-NO system are increased from 0.073% and 0.705% to 32.597% and 55.468% of  $J_{lf}$  respectively, suggesting the significant effect of NO adsorption on magnetic anisotropy.

#### 3.3 Origin of the enhanced asymmetric DMI and magnetic anisotropy with molecular adsorption

To analyze the origin of the enhanced antisymmetric DMI and magnetic anisotropy, we present the total density of states (DOS) in Fig. 6. It is difficult to observe spin splitting in total DOS, revealing antiferromagnetism whose total magnetic moment is close to zero. The partial DOS of Mn, S, and P atoms is shown in Fig. 6b-d, where the Mn-d orbital splits into  $d_{xy}$ ,  $d_{yz}$ ,  $d_{z^2}$ ,  $d_{xz}$ , and  $d_{x^2-y^2}$  five orbitals while the S-p orbital and P-p orbital have  $p_x$ ,  $p_y$  and  $p_z$  components. Obviously, the values of partial DOS of Mn and S atoms are much larger than





that of the P atom, indicating their main contribution to the magnetic properties of the MPS monolayer. Besides, the nearest distances of Mn–S and Mn–Mn pairs are 2.04 Å and 3.493 Å in pristine MPS, respectively. Obviously, the distance between the nearest Mn-Mn pairs is much longer than the bond length of Mn-S bonds. Based on the partial DOS in Fig. 6 and the spin



Fig. 4 Enhanced ratios of effective magnetic exchange constant  $J_{lf}$  (a), and the magnitude of the asymmetric DMI vector  $\mathbf{D}_{lf}$  (b).



density distribution in Fig. 3, we can conclude that the Mn–S– Mn super-exchange coupling is the dominating mechanism of the antiferromagnetic interaction in MPS, which obeys the Goodenough–Kanamori–Anderson rules.<sup>72,73</sup> The schematic representation of the Mn–S–Mn super-exchange coupling is presented in Fig. S5, (ESI†) where t<sub>2g</sub> represents three-fold degenerate orbitals (d<sub>xy</sub>, d<sub>xz</sub>, and d<sub>yz</sub> orbitals) and e<sub>g</sub> represents two-fold degenerate orbitals (d<sub>z<sup>2</sup></sub> and d<sub>x<sup>2</sup>-y<sup>2</sup></sub> orbitals). The halffilled t<sub>2g</sub> and e<sub>g</sub> orbitals result in a Néel-type AFM spin arrangement, as shown in Fig. 3.

To study the influence of molecular adsorption on the superexchange coupling, we define the difference between orbital band centers  $BD_{n,l_{*},n_{p}l_{p}}$  as the covalency, as follows:<sup>74</sup>

$$BD_{n_{A}l_{A}}, n_{B}l_{B} = -|BC^{A}(n_{A}, l_{A}) - BC^{B}(n_{B}, l_{B})|$$
(6)

where  $BC^{4}(n_{A}, l_{A})$  is the short form of  $BC^{4}(n_{A}, l_{A}, m_{l}, m_{s})$  representing the band centre of atomic orbital  $|n_{A}, l_{A}, m_{l}, m_{s}\rangle$ . Here, the dependence of the principle quantum number *n* on the notation referring to  $BD_{n_{A}l_{A}}$ ,  $n_{B}l_{B}}$  is omitted for simplicity.  $BC^{4}(n, l, m_{b}, m_{s})$  is defined as:

$$BC^{A}(n_{A}, l_{A}, m_{l}, m_{s}) = \frac{\int_{\varepsilon_{0}}^{\varepsilon_{1}} \varepsilon g^{A}_{[n_{A}, l_{A}, m_{l}, m_{s})}(\varepsilon) d\varepsilon}{\int_{\varepsilon_{0}}^{\varepsilon_{1}} g^{A}_{[n_{A}, l_{A}, m_{l}, m_{s})}(\varepsilon) d\varepsilon}$$
(7)

where  $g_{[n_A, l_A, m_I, m_s\rangle}^A(\varepsilon)$  is the contribution from the atomic orbital  $|n_A, l_A, m_I, m_s\rangle$  of atom *A* to the total DOS (*g*( $\varepsilon$ )). According to this definition, a larger covalency corresponds to a higher overlap between two orbitals, revealing a stronger coupling. To calculate the covalency between Mn–d and S–p orbitals (*BD*<sub>Mn–d,S–p</sub>), the

partial DOSs in the MPS monolayer with and without molecular adsorption are shown in Fig. 7a and b, and the values are presented in Fig. 7c. We find that systems with the molecular adsorption around the Mn atom exhibit slightly larger BD<sub>Mn-d,S-p</sub> than pristine MPS, corresponding to a little enhancement in the parameter  $J_{lb}$ such as the phenomenon observed in MPS-N2. Unexpectedly, the adsorption of CO, and NH3 around the P atom also increases BD<sub>Mn-</sub>  $_{d,S-p}$  and leads to a weak increase in the  $J_{lf}$  parameter, which is a combined effect of the charge transfer between the molecule and MPS and the structural distortion induced by molecular adsorption. The charge transfer is shown in Table 1 where the positive value reveals a charge transfer from the gas molecule to the substrate. This charge transfer is obtained by the Bader charge method, and can be validated by the results of charge density difference as presented in Fig. S4 (ESI<sup>+</sup>). The structural distortion can be found through the change of bond length as shown in Table 2.

It can be found that the molecular adsorption has a different effect on Mn–Mn distances (including Mn<sub>0</sub>–Mn<sub>1</sub>, Mn<sub>0</sub>–Mn<sub>2</sub>, and Mn<sub>0</sub>–Mn<sub>3</sub>, as presented in Fig. S3, ESI<sup>†</sup>), but shortens the Mn–S bond length. With the bond length changing, the magnetic moments on Mn and S atoms also vary, and the spatial inversion symmetry in pristine MPS is broken. The compression of the Mn–S bond and the increase of the magnetic moment on S atom are helpful in strengthening the Mn–S–Mn super-exchange interaction, while the generation and remarkable enhancement of antisymmetric DMI can be attributed to the difference of the magnetic moment between these four Mn atoms and the variety on distances of three Mn–Mn pairs. Surprisingly, the adsorption of NO results in the most obvious increase of  $J_{lj}$ ,  $K_{lj5}$ ,  $|D_{lj}|$  and  $A_{zz}$  among all



Fig. 7 The partial DOSs of the Mn-d orbital (a) and S-p orbital (b), and the covalency (c) between Mn-d and S-p orbitals for the MPS monolayer before and after molecular adsorption.

Table 2 The magnetic moment on Mn and S atoms, the bond lengths of Mn–S, and Mn–Mn bonds in the MPS monolayer with and without molecular adsorption

System	$Mn_0 (\mu_B)$	$\mathrm{Mn}_{1}\left(\mu_{\mathrm{B}}\right)$	$Mn_2 (\mu_B)$	$Mn_3 (\mu_B)$	$Mn_0$ – $Mn_1$ (Å)	$Mn_0$ – $Mn_2$ (Å)	$Mn_0$ – $Mn_3$ (Å)	Mn–S (Å)	$S(\mu_{\rm B})$
MPS	4.210	-4.210	-4.210	-4.210	3.493	3.493	3.493	2.601	$\pm 0.001$
MPS-CO	4.206	-4.205	-4.207	-4.206	3.494	3.488	3.496	2.597	$\pm 0.001$
MPS-N <sub>2</sub>	4.206	-4.206	-4.205	-4.206	3.495	3.493	3.493	2.598	$\pm 0.001$
MPS-NH <sub>3</sub>	4.202	-4.202	-4.208	-4.202	3.500	3.495	3.476	2.576	$\pm 0.001$
MPS-NO	4.201	-4.205	-4.202	-4.206	3.495	3.493	3.490	2.590	$\pm 0.003$
MPS-NO <sub>2</sub>	4.200	-4.193	-4.205	-4.207	3.493	3.496	3.491	2.599	$\pm 0.010$

adsorption systems, although its  $BD_{Mn-d,S-p}$  is the smallest and its asymmetric distortion is also not the largest.

Next, we consider the NO–MPS system as an example to investigate separately the influence of structural distortion and charge transfer quantitatively. The pristine MPS doped with 0.030 e is used to investigate the effect of charger transfer on magnetic properties. It is found that the enhanced ratios of  $J_{lf}$  and  $|D_{lf}|$  with such charge transfer are -2.74% and 95.18%, while  $A_{zz}$  and  $K_{lf}$  are up to -2.178 meV per atom and 708.52 µeV, respectively. To explore the impact of structural distortion, we removed the NO molecule from the NO–MPS system, and

then keep the distorted lattice of the MPS monolayer. The calculated enhanced ratios are -0.20% ( $J_{if}$ ) and 503.56% ( $|D_{if}|$ ), as shown in Table 3. Meanwhile, the absolute values of  $A_{zz}$  and  $K_{if}$  induced by structural distortion are 0.284 meV per atom and 124.61 µeV, respectively. It is obvious that the structure distortion has larger influence on the antisymmetric DMI than charge transfer, while the charge transfer affects the isotropic magnetic exchange coupling, C-MAE and SIA more significantly.

However, the total enhancement caused by the distortion and charger transfer is still much lower than that of the

**Table 3** Parameters  $J_{lf}$ ,  $K_{lf}$ ,  $D_{f}^{x}$ ,  $D_{f}^{y}$ ,  $D_{f}^{y}$ ,  $D_{f}^{y}$ ,  $D_{f}^{y}$ ,  $|D_{t}|$ , and  $A_{zz}$  of pristine MPS, MPS only with charge doping (MPS-Charge), MPS only with structural distortion (MPS-Distortion), and MPS with NO adsorption (with both doping and structural distortion, MPS-NO)

MPS-5.958-4.370.0960.036-0.4660.477-0.042MPS-Charge-5.795708.520.428-0.262-0.7840.931-2.178MPS-Distortion-5.946-124.61-1.488-0.8382.3182.879-0.284	SYSTEM	$J_{lf}$ (meV)	$K_{lf}$ (µeV)	$\boldsymbol{D}_{lf}^{x}\left(\mathrm{meV}\right)$	$\boldsymbol{D}_{lf}^{\boldsymbol{\gamma}}\left(\mathrm{meV}\right)$	$\boldsymbol{D}_{lf}^{z}\left(\mathrm{meV}\right)$	$ \boldsymbol{D}_{lf} $ (meV)	$A_{\rm zz}$ (meV per atom)
MPS-NO -8.294 -2703.62 4.732 -1.126 -0.211 4.869 -4.602	MPS MPS–Charge MPS–Distortion MPS–NO	-5.958 -5.795 -5.946 -8.294	-4.37 708.52 -124.61 -2703.62	$0.096 \\ 0.428 \\ -1.488 \\ 4.732$	$0.036 \\ -0.262 \\ -0.838 \\ -1.126$	-0.466 -0.784 2.318 -0.211	0.477 0.931 2.879 4.869	-0.042 -2.178 -0.284 -4.602

MPS-NO system. For instance, both the charge transfer and structural distortion result in a decrease in  $J_{lf}$ , which is contrary to the 39.208% increase induced by the NO adsorption. From the first-principles calculations, we find that the magnetic moment of NO is up to  $-0.421\mu_{\rm B}$ , much larger than that of the S atom  $(\pm 0.003 \mu_{\rm B})$  in the MPS–NO system, providing possible superexchange coupling with Mn atoms. In order to explore the super-exchange coupling between the Mn atom and NO molecule, we calculated the covalency between the Mn atom and NO molecule (BD<sub>Mn,NO</sub>) based on the partial DOSs as shown in Fig. S6 (ESI<sup> $\dagger$ </sup>). The calculated BD<sub>Mn,NO</sub> is up to -2.329 higher than  $BD_{Mn-d,S-p}$  of the NO-MPS system (-2.449), indicating the stronger Mn-NO-Mn super-exchange coupling with respect to the Mn-S-Mn super-exchange coupling. Moreover, we also calculate the covalency between Mn ions and NO<sub>2</sub> molecules  $(BD_{Mn,NO2})$ . The calculated  $BD_{Mn-NO2}$  is -9.82, which is much lower than  $BD_{Mn-NO}$  (-2.329) and  $BD_{Mn-S}$  in the MPS-NO<sub>2</sub> system (-2.41), suggesting weak super-exchange interaction between Mn ions and NO<sub>2</sub> molecules. This highlights the important effect of magnetic moment on the adsorbed molecule. Therefore, in addition to structural distortion and charge transfer, the newly generated Mn-NO-Mn super-exchange coupling also contributes to the enhancements of magnetic exchange interaction, C-MAE, DMI and SIA.

### 4. Conclusions

In summary, the influence of molecular adsorption on the magnetic properties of the MPS monolayer is investigated by the firstprinciples calculation. Based on the stable configuration, we find that although the molecular adsorption enhances the isotropic magnetic exchange coupling constant slightly, it increases magnetic anisotropy and induces DMI in the MPS monolayer significantly. Among all the studied systems, the enhancements of the isotropic magnetic exchange coupling constant  $(J_{lf})$ , DMI  $(|D_{lf}|)$ , C-MAE  $(K_{lf})$ , and SIA (Azz) caused by NO molecular adsorption are the largest, with the enhanced ratios being 39.208%, 920.37%, 32.524% and 54.763% (of  $J_{lf}$ ), respectively. It is found that the enhancement of DMI is mainly attributed to the structural deformation, while the super-exchange interaction between Mn atoms and magnetic molecules accounts for the remarkable enhancements of  $J_{lf}$  and  $K_{lf}$ . Our finding not only demonstrates the effect of molecular adsorption on inducing the intralayer DMI in centrosymmetric structures, but also provides an insightful understanding of the mechanism of superexchange interaction between gas molecules and 2D magnets.

## Author contributions

G. Z. conceived the idea. K. W. did the DFT calculation. K. W., and G. Z. did data analysis. All the authors discussed the results and participated in writing the manuscript.

## Conflicts of interest

The authors declare no competing financial interest.

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