Peculiar anharmonicity of Ruddlesden Popper metal halides: temperature-dependent phonon dephasing†

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The anharmonicity of the Ruddlesden Popper metal-halide lattice, and its consequences for their electronic and optical properties, are paramount in their basic semiconductor physics. It is thus critical to identify specific anharmonic optical phonons that govern their photophysics. Here, we address the nature of phonon–phonon scattering probabilities of the resonantly excited optical phonons that dress the electronic transitions in these materials. Based on the temperature dependence of the coherent phonon lifetimes, we isolate the dominant anharmonic phonon and quantify its phonon–phonon interaction strength. Intriguingly, we also observe that the anharmonicity is distinct for different phonons, with a few select modes exhibiting temperature-independent coherence lifetimes, indicating their predominantly harmonic nature. However, the population and dephasing dynamics of excitons are dominated by the anharmonic phonon.

1 Introduction

The ionic lattice of metal-halide perovskites is a deterministic component of their photophysical behaviour.1 The lattice dynamics are mostly driven by multiple optical phonons in the 1–10 meV energy range and acoustic phonon modes at energies <2 meV.2 The optical phonons, in particular, have been identified to play a critical role in the electronic dynamics via strong polaronic coupling mechanisms.3 The consequences of the strong phonon interactions in the structural stabilization,4 carrier thermalization,3 carrier recombination,6,7 carrier transport8,9 and dephasing dynamics10,11 are widely reported. The acoustic modes, on the other hand, determine the thermal properties of the material, including thermal conductivity, molar specific heat, and thermal expansion of the lattice. These are clear manifestations of the anharmonicity of the lattice, models for which are available in any basic textbook for solid-state physics such as ref. 12. The distinction of metal-halide perovskites from classical semiconductors lies, however, in the softness of the lattice and rather large anharmonicity induced by substantially high multiphonon scattering probabilities.1,2 In addition, the non-polar dynamic fluctuations from the independent motion of the organic cation5,14 lead to a rapid escalation of the complexity of the microscopic picture of the carrier-lattice dynamics, where the polaronic nature of the material is described as an interplay...
between long (Frolich-like) and short range (dynamic disorder) carrier-lattice coupling.8

A similar photophysical scenario can be identified in other derivatives of metal-halide perovskites, including layered two-dimensional systems such as the Ruddlesden–Popper (RP) metal halides.15,16 However, given the globally neutral character of excitons that are the primary photo-excitation in these systems, one might expect a diminished role for the Coulomb-mediated polaron coupling.17 We have previously highlighted, on the contrary, the critical role played by the phonon interactions in various exciton dynamics using a number of unambiguous experimental observations. We demonstrated that distinct excitonic states are distinctly phonon-dressed,18 elastically scattered19 and coupled non-adiabatically to the lattice phonons.20 We have also suggested that the photoexcitations must, in fact, be treated within the exciton polaron framework.17,18,21 As a corollary to this hypothesis, one may expect to perceive the seemingly independent many-body dynamics of phonons in the dynamics of exciton polarons.

For example, consider the thermal dephasing of excitons, which is primarily driven by the elastic scattering of a coherent exciton population with the thermally populated phonons. If the coherent population is that of exciton polarons, then the thermal dephasing of phonons (in other words, phonon–phonon interactions driven by the anharmonicity of the polaron dressing phonons) will also contribute to the elastic scattering. The models used to fit the temperature dependence of the exciton dephasing rates or the exciton linewidths do not, however, consider phonon–phonon scattering explicitly. Moreover, direct observations of the structural dynamics and lattice anharmonicity in RP metal halides are missing.

In this manuscript, we provide an experimental measurement of the anharmonicity of optical phonons in phenethylammonium lead iodide ((PEA)2PbI4, Fig. 1(a)), a prototypical Ruddlesden–Popper metal halide, by analysing the temperature dependence of the dynamics of impulsively generated coherent phonons. We clearly identify the co-existence of a dominant anharmonic mode with energy of 4.40 meV and various harmonic phonons, the most important one with energy 2.61 meV. We attribute the anharmonic behaviour of the 4.40 meV mode to its decay into two lower-energy acoustic phonons via a three-phonon interaction mechanism, as has been reported in other polar semiconductors.22,23 This mechanism has a direct influence on the exciton dephasing rates, especially at higher temperatures. We compare the strength of the anharmonicity of the dominant phonon with that in other semiconductors, and find that it approaches values found in the most highly anharmonic lattices such as SrTiO3.

2 Results and discussion

In this work, we analyze the temperature dependence of the coherent phonon dynamics reported previously in ref. 18. Fig. 1(b) shows the periodic modulations observed in the ultrafast differential transmission experiment (details in ESIf) by photo-exciting the free carriers at 3.06 eV with a train of ultrashort optical pulses at sample temperatures ranging over 5–100 K. Note that no first-order phase transitions are present within this temperature range.24,25 These periodic modulations of the optical absorption of the sample are the signatures of coherent phonons generated by resonant impulsive stimulated Raman scattering (RISRS). Briefly, the ultrashort optical pulse generates a coherent wavepacket – a superposition state of phonon modes that are excited with a common phase – and cause a coherent lattice motion. The coherent motion influence the complex refractive index which modulates the differential transmission. An exhaustive description of the physical processes responsible for the generation of the coherent wavepacket can be found in ref. 26. The intensity of transmission modulation reduces with time due to the dephasing of the coherent phonon population. The dephasing rate becomes faster at higher temperatures, indicating that the scattering with the thermally-generated incoherent phonon population is the primary dephasing mechanism. The RISRS spectrum at 5 K, shown in Fig. 1(c), is obtained by taking the Fourier transform of the time dynamics (the temperature dependence of the RISRS spectrum is shown...
Two dominant phonon modes are clearly observed, labelled M1 at 2.61 meV and M2 at 4.40 meV, in addition to a few modes between 5–6 meV. All the observed phonons have been previously assigned to the lattice vibrations predominantly within the lead iodide layer.\textsuperscript{18} Specifically, M1 and M2 correspond to octahedral twisting along one of pseudocubic axes and octahedral twist and Pb–I–Pb bending, respectively (see ref. 18 for details of the assignment).

It is worth noting that M1–M6 (assigned in the ref. 18) correspond to the modes coupled to electronic transitions, identified in the resonant excitation condition. There are several other lattice modes at higher energies, including those involving vibrations of the organic cation, which have been identified previously under non-resonant conditions\textsuperscript{27,28} and thus are not relevant for the polaronic coupling of charge carriers. Accordingly, we limit ourselves to these low energy modes. Even among M1–M6, only M1 and M2 are dominant dressing modes for the free carriers, evident from their larger spectral intensity.

The temperature dependence of the dephasing rates of M1 and M2 reflects differences in their multi-phonon interactions. While one can fit the experimental dynamics to several damped oscillators to estimate the coherence lifetimes of each of the modes, the large number of fitting parameters and possible energy shifts that cannot be rigorously accounted make the fitting routine unreliable. We instead implement a continuous wavelet transform (CWT) approach based on a complex Morlet wavelet\textsuperscript{29} (the details are presented in ESI\textsuperscript{†}) to analyze and visualize the coherence evolution in time for each of the individual modes. The wavelet transformation decomposes the impulsive oscillatory signals allowing time-frequency visualization. This was described in detail by Stasiewski for simulated examples of multi-component impulsive responses.\textsuperscript{30} Briefly, the CWT transform of an oscillatory function generates two-dimensional spectra, shown in Fig. 3 for selected temperatures, where the normalized amplitude is plotted as a function of the beating energy and the pump–probe delay. The complete range of temperatures studied can be found in the ESI.\textsuperscript{†} The amplitude of the observed modes represents the modulation depth in the differential transmission experiment and correlates directly with the intensity of the RISRS spectrum of Fig. 1(c). We observe that, for all observed modes, it decays in tens of picoseconds at all temperatures.

We first focus on the most prominent feature at a beating energy of 4.40 meV, which corresponds to the mode M2. Qualitatively, it can be noted that as the temperature increases the mode amplitude decays at a faster rate. This can be qualitatively explained by the increased probability of elastic many-body interactions with a thermally generated incoherent phonon population. We also observe that the relative amplitude of M2 decreases at higher temperatures in comparison to the other modes, which can also be observed in the temperature-dependent resonant Raman spectra (Fig. SI1, ESI\textsuperscript{†}). On the other hand, mode M1 (2.61 meV) presents a very different scenario in which its dynamics are not sensitive to the temperature, at least within the temperature range of the measurement. This implies a significantly different anharmonic interaction potential for M1 compared to M2. To further highlight the differences between M1 and M2, kinetic traces at their energies, at selected temperatures, are shown at Fig. 3(a and b). The amplitude of M2 decays exponentially with a clear temperature-dependent dynamics. The effective lifetime of this mode can be estimated \textit{via} mono-exponential fits; the inverse of the decay time constant is plotted in Fig. 3(c) for all the temperatures. The amplitude of M1, on the contrary, exhibits a non-exponential,
temperature-independent decay. An effective lifetime can be estimated, for the sake of comparison, as the time taken for the signal to reach \(1/e\) of its maximum value. The corresponding values of dephasing rate are shown in Fig. 3(c). The difference in the temperature dependence of M1 and M2 is further evidenced here. Additionally, in Fig. S19 (ESI†), we show the time-integrated spectrum between 5–10 and 10–15 ps. From this data it is clear that M1 dominates at longer times and at higher temperatures.

As noted earlier, the temperature dependence of the phonon dephasing dynamics is interpreted as a consequence of phonon–phonon interactions that are mediated by the anharmonicity of the lattice. The latter was theoretically modelled as a third-order anharmonic Hamiltonian considering three-phonon interactions, which reads as:

\[
H_{\text{anhar}} = \sum_{k,k'} \left( \lambda_{kk'} l_k l_{-k} a_{k'} a_{-k'} + \lambda_{k'k} l_{-k} l_{-k'} a_k a_{k'} \right). \tag{1}
\]

Here \(\lambda_{kk'}\) is the phonon–phonon coupling, \(l_k\) and \(a_{k'}\) represent the quantum operators that destroy optical and acoustic phonons respectively. The dispersion relations for optical and acoustic phonons, respectively, are characterised by \(\omega_{o,k}(k)\) and \(\omega_{a,k}(k')\). This model includes phonon downconversion – decay of the generated longitudinal optical phonon into two lower energy acoustic phonons and upconversion – fusion of two acoustic phonons to generate one optical phonon. Both these processes when conserving both energy and momentum act as plausible pathways for the phonon decoherence. In the case of (PEA)_2PbI_4, the higher-energy phonons correspond to localized, dispersionless vibrations of the organic moiety\(^{32,33}\) and it is unlikely that such an upconversion process will conserve momentum. Thus, we only consider downconversion processes as the primary dephasing mechanisms. It is worth noting that four-phonon interactions, where the phonon decays into three or more phonons, are also plausible decay pathways; however, these are not significant at low temperatures.\(^{32,33}\) Hence, we consider the simplest case of downconversion of the optical phonon into two acoustic phonons of equal energy, referred to as the cubic overtone model. We disregard any constraints from the wavevector mismatch, but we do note that this mechanism can be expected given the measured phonon dispersion for similar metal-halide derivatives.\(^{34}\) Moreover, the polycrystalline nature of the thin film studied here, with grain sizes of hundreds of nanometers, might compromise the long range lattice order as perceived by phonons, thus relaxing the momentum conservation condition and reducing the relevance of wavevector mismatch. In such a scenario, the anharmonic potential results in a dephasing rate \(\Gamma\) which can be written as:

\[
\Gamma = \Gamma_0 + \gamma_0 \left[ 1 + \frac{2}{\exp(h\nu_0/2k_B T) - 1} \right]. \tag{2}
\]

where \(\gamma_0\) is the anharmonic coefficient of the phonon mode which is related to \(\lambda\), the optical phonon – acoustic phonon coupling matrix, in eqn (1). \(\Gamma_0\) is a temperature independent dephasing rate and as discussed by Némec,\(^{35}\) it represents the scattering of phonons by defects in the lattice,\(^{36}\) apart from the pure intrinsic dephasing. Such analysis is not possible, unfortunately, for mode M1 due to its temperature independent behaviour and diminished anharmonic nature. The fit of the temperature dependent dephasing rate of M2 with the cubic overtone model is shown in Fig. 3(c). It yields an anharmonic constant and a phonon-defect scattering constant of \(\gamma_0 = 0.030 \pm 0.005\) ps\(^{-1}\) and \(\Gamma_0 = 0.09 \pm 0.02\) ps\(^{-1}\), respectively. We highlight that the model cannot reproduce the experimental trend without the inclusion of the defect-scattering contribution \(\Gamma_0\) even if the energies of two decay phonons are set as fitting parameters, with energy conservation as a condition. This implies that the phonon decoherence at low temperature is dominated by scattering by defects.\(^{36,37}\) This is not entirely surprising for a solution-processed polycrystalline material, but it is intriguing to observe the relevance of defects in the phonon dynamics and not just in the electronic processes. The role of grain boundaries in phonon scattering is also encompassed in \(\Gamma_0\), although a more rigorous analysis of the microscopic picture of defect scattering is out of scope of the current work.
Table 1 Comparison of the anharmonic constants and Frohlich coupling constants ($\chi_F$) for different materials reported in the literature and that of (PEA)$_2$PbI$_4$ extracted from Fig. 3(c) and eqn (2)

<table>
<thead>
<tr>
<th>Material</th>
<th>$\chi_F$ (meV)</th>
<th>$\gamma_0 \times 10^2$ (ps$^{-1}$) $\omega/2\pi\gamma_0$ (meV)</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>MoS$_2$</td>
<td>—</td>
<td>47.6, 1.6</td>
<td>1000</td>
</tr>
<tr>
<td>GaAs</td>
<td>0.068</td>
<td>36.6, 11</td>
<td>83</td>
</tr>
<tr>
<td>CsPbCl$_3$ NCS</td>
<td>~1–2$^a$</td>
<td>4.46, 1.5</td>
<td>71</td>
</tr>
<tr>
<td></td>
<td></td>
<td>9.42, 4.8</td>
<td>48</td>
</tr>
<tr>
<td></td>
<td></td>
<td>11.78, 4.2</td>
<td>67</td>
</tr>
<tr>
<td>(PEA)$_2$PbI$_4$</td>
<td>2.2</td>
<td>4.40, 3.0 ± 0.5</td>
<td>33</td>
</tr>
<tr>
<td></td>
<td></td>
<td>2.61 —</td>
<td>—</td>
</tr>
<tr>
<td>SrTiO$_3$</td>
<td>4.5</td>
<td>5.58, 8.0</td>
<td>12</td>
</tr>
<tr>
<td></td>
<td></td>
<td>1.65, 1.5</td>
<td>27</td>
</tr>
</tbody>
</table>

$^a$ Specific value is not reported, this range reported covers distinct lead-halide perovskites with similar compositions.

In Table 1 we compare the anharmonicity constants of different materials reported in the literature with that of (PEA)$_2$PbI$_4$ determined in this work. We tabulate the materials going from covalent to strongly ionic systems, thus moving towards strongly anharmonic lattices. However, it is evident that there is no apparent trend in the value of $\gamma_0$. Given that we are comparing phonons of varying softness, and for our comparison to be independent of the phonon energy, we calculate a dimensionless parameter $-\omega/2\pi\gamma_0$, which is the ratio of the frequency of the phonon and the anharmonicity constant. We interpret this parameter as the average number of cycles in the phonon oscillation before the phonon encounters a scattering event with another phonon. We clearly observe an increase in the value of this parameter with increasing ionicity of the material. In single-layer MoS$_2$, the optical phonon is fairly immune to thermal dephasing, while in GaAs, which is a slightly polar compound, the phonon scatters in about 80 oscillation cycles. Optical phonons in inorganic lead-halide perovskite nanocrystals appear to have comparable anharmonicity to that of GaAs, although the presence of an organic cation is most likely to reduce $\omega/2\pi\gamma_0$. We observe much higher anharmonicity in (PEA)$_2$PbI$_4$ with $\omega/2\pi\gamma_0$ comparable to that of strongly ionic solids such as SrTiO$_3$.

As we have already discussed, in Fig. 3 the mode M1 exhibits weak temperature dependence and thus we deduce a very low degree of anharmonicity. One could rationalize this with the cubic overtone model, wherein M1 does not have access to two acoustic modes of exactly half its energy. This claim can be qualitatively substantiated through the density of states for acoustic phonons of low frequency in isotropic media, which can be shown to scale as $\omega^2$, where $\hbar\omega$ is the energy of the acoustic phonon. This suggests that M1 will have access to a lower density of acoustic phonons and thus, will be less likely to undergo downconversion. Similar scenarios have been proposed for CsPbBr$_3$, where a higher density of states, between 1–3 THz, increase the dephasing rate in comparison to lower energy modes. Similarly, for (n-butylammonium)$_2$PbI$_4$, the phonon lifetime was calculated to be higher at lower frequencies following an $\omega^{-2}$ trend. This interpretation relies on the assumption of M1 decaying into two acoustic phonons of similar energy. However, different pathways including phonons of higher energy with larger density of states might also be plausible. It is imperative here to have detailed knowledge of the entire dispersion of the low-energy acoustic phonons to obtain better insight into the different scattering pathways that are energetically allowed and that obey momentum conservation. Unfortunately, such data is not yet available for Ruddlesden–Popper metal halides.

The disparity in the dynamics of M1 and M2 can also be rationalized by invoking the dipolar nature of the lattice vibrations. Due to the polar character of the lattice, asymmetric phonon modes may be perceived as oscillating dipoles and, accordingly, phonon–phonon interactions as dipolar. Based on the assignment of M1 and M2 presented in ref. 18, we recall that M1 primarily involves the motion of the iodide ions while M2 has a substantial additional contribution from the motion of the lead ion around its equilibrium position. This indicates that the M2 mode, with its larger asymmetry, can induce larger lattice dipoles, and accordingly acquires greater anharmonicity. More detailed modelling of the lattice motion combining first-principles calculations and molecular dynamics, albeit being computationally expensive, can offer pertinent insights in this context.

It is worth noting that the anharmonic phonon M2 was observed to play deterministic role in the polaronic interactions of carriers and excitons in these materials. Such interactions are typically treated within the Fröhlich framework, which considers weak coupling of electronic excitations with harmonic lattice vibrations although its applicability in metal-halide perovskites has been questioned. More detailed modelling of the lattice motion combining first-principles calculations and molecular dynamics, albeit being computationally expensive, can offer pertinent insights in this context.

In Table 1, we also show the Fröhlich coupling constants ($\chi_F$), which relates to the size of the polaron in different materials. We note a clear anti-correlation between $\chi_F$ and the anharmonic parameter $\omega/2\pi\gamma_0$. Material systems which host large polarons such as GaAs are composed of comparatively harmonic vibrational potentials, while strongly ionic lattices such as SrTiO$_3$, which are known to host small polarons have substantially larger anharmonicity. Ruddlesden Popper metal halides studied here are clearly in the intermediate regime and importantly beyond the weak coupling limit. We invoke again the interpretation of the vibrations in ionic lattices as oscillating dipoles, in which phonon–phonon interactions (anharmonicity) can be thought in terms of dipole–dipole interactions, and its strength will be determined by the asymmetry of the vibration (dipole moment), the ionic character and softness of the lattice. It then becomes clear that the size of the polaron and the anharmonicity of the vibrational mode are both consequences of the same physical problem – Coulomb interactions in an ionic lattice. This train of thought indicates the
need to include anharmonicity in the description of polarons as the small polaron limit is approached in highly ionic lattices, where the harmonic potential approximation is compromised by strong phonon–phonon (dipole–dipole) interactions. Recent work has aimed for the inclusion of anharmonicity into the Fröhlich formalism, which is a necessary step in the description of polarons even in metal halide perovskites although contributions from dynamic disorder from the short-range fluctuations of the organic cation will add to the complexity. The anharmonicity of the phonons that dress the electronic transitions is of relevance in the context of exciton polarons, which we consider as the primary photoexcitations in Ruddlesden–Popper metal halides. Exciton polarons are stationary eigenstates of a system where the Coulomb interactions between the electrons and holes and their respective coupling with phonons are the integral components. Due to the inherent mixing of exciton and phonon eigenstates, the phonon–phonon interactions assume relevance in the exciton dephasing dynamics. Such a consideration was initially put forward by Verzelen et al. in the context of semiconductor quantum dots.

In this context, we recall the spectral fine structure at the exciton energy ubiquitous to Ruddlesden–Popper metal halides with a characteristic energy spacing of 35–40 meV (see numerous references in ref. 17). We had hypothesised, based on a series of experimental observations, that the resonances observed in this fine structure correspond to distinct exciton polaron states with different binding energies and effective masses, which is different from the more widely used vibronic replica interpretation. We concluded that two of the observed excitonic resonances, labelled \( X_A \) and \( X_B \), are dressed by distinct lattice modes. Specifically, \( X_A \) is dressed predominantly by \( M_2 \), while \( X_B \) had additional dressing from \( M_4 \) and \( M_6 \), which are the higher-energy modes at 5.22 and 5.75 meV. Note that these higher-energy modes exhibit large anharmonicities similar to that of \( M_2 \), as evident in their comparable dynamics to that of \( M_2 \) at higher temperatures, Fig. 2. Intriguingly, \( M_1 \) does not contribute significantly to the exciton polaron while it dresses the carrier polaron. Coincidentally, no evidence was found for the participation of \( M_1 \) in the exciton polaron dynamics. On the contrary, the strongly anharmonic \( M_2 \) mode was identified to be the primary phonon participating in the non-adiabatic mixing of \( X_A \) and \( X_B \), eventually driving the population exchange between these two states, see ref. 20. Anharmonic phonons can also be clearly identified to be playing a role in the thermal dephasing of excitons, as reported in ref. 19. The increase in the homogeneous linewidths of excitonic resonances with temperature can be analysed to estimate the energy of the phonons that scatter the exciton. Such an analysis revealed that average energy of the phonon that broadens \( X_A \) is about 6 meV, clearly indicating the role of the higher energy anharmonic modes, dominated by \( M_2 \), in the exciton–phonon elastic scattering. The temperature dependence of the \( X_B \) linewidth, on the other hand, yielded a phonon energy of over 20 meV. However, the vibrational modes at such energies correspond to the motion within the organic layer and thus should not contribute to the scattering of excitons that are confined within the inorganic layer. We consider that this discrepancy is due to inadequacy of the LO phonon scattering model of exciton polarons, which does not explicitly consider the contributions from phonon–phonon interactions to the exciton dephasing.

3 Conclusions

In conclusion, we quantified the anharmonicity of optical phonons that are impulsively generated via photoexcitation of free carriers in polycrystalline thin films of (PEA)$_2$PbI$_4$. We find that each of the observed lattice eigen modes that are associated with the motion of the lead-iodide network exhibit distinct dynamics. The lower energy mode, labelled \( M_1 \), exhibits temperature independent dephasing dynamics, indicating a low probability of phonon scattering. The higher energy modes, however, exhibit temperature dependence, which we analysed considering downconversion of optical phonons into two acoustic modes. We also extracted the anharmonicity constant, which is a measure of phonon–phonon scattering, and based on the comparison with other material systems, we conclude that the anharmonicity of the Ruddlesden–Popper metal halides is as large as in strongly ionic solids. Based on a critical comparison of polaron coupling constants and the lattice anharmonicities of different material systems, we conclude that the electron–phonon coupling mechanism goes beyond the weak coupling limit, and the lattice anharmonicity quantified in this work has to be rigorously considered in its description.

Many previous works on carrier dephasing\(^ {10, 11} \) and thermalization\(^ {5} \) in three dimensional lead halide perovskites have clearly identified the role of anharmonic lattice interactions in electronic processes. On a very similar note, albeit in the context of electrically neutral excitons, we find that all the phonons that dress the excitons and thus are the integral components of the exciton polaron wavefunction exhibit strong anharmonicity. Based on this observation, we emphasize the need to expand the theoretical model for excitons in these systems, similar to what was proposed by Verzelen et al., but also to include phonon anharmonicity in the exciton many-body dynamics. We consider that the coherent phonon dynamics presented in this work, along with the independent observations of phonon dressing of excitons, thermal dephasing of excitons, and exciton many-body interactions, establish a solid experimental ground to build a theoretical framework to comprehend exciton polarons in semiconductor materials beyond the metal halides addressed in this manuscript.

Author contributions

E. R. G. analyzed the data under the supervision of A. R. S. K. and C. S. A. A. R. S. K. participated in the original data collection and analysis reported in ref. 18. The intellectual basis for this work was conceived by A. R. S. K. and C. S. A. All co-authors contributed to the redaction of this manuscript.
Conflicts of interest

There are no conflicts to declare.

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Notes and references