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Surfactant-laden droplet size prediction in a flow-focusing microchannel: a data-driven approach†

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The control of droplet formation and size using microfluidic devices is a critical operation for both laboratory and industrial applications, e.g. in micro-dosage. Surfactants can be added to improve the stability and control the size of the droplets by modifying their interfacial properties. In this study, a large-scale data set of droplet size was obtained from high-speed imaging experiments conducted on a flow-focusing microchannel where aqueous surfactant-laden droplets were generated in silicone oil. Three types of surfactants were used including anionic, cationic and non-ionic at concentrations below and above the critical micelle concentration (CMC). To predict the final droplet size as a function of flow rates, surfactant type and concentration of surfactant, two data-driven models were built. Using a Bayesian regularised artificial neural network and XGBoost, these models were initially based on four inputs (flow rates of the two phases, interfacial tension at equilibrium and the normalised surfactant concentration). The mean absolute percentage errors (MAPE) show that data-driven models are more accurate (MAPE = 3.9%) compared to semi-empirical models (MAPE = 11.4%). To overcome experimental difficulties in acquiring accurate interfacial tension values under some conditions, both models were also trained with reduced inputs by removing the interfacial tension. The results show again a very good prediction of the droplet diameter. Finally, over 10 000 synthetic data were generated, based on the initial data set, with a Variational Autoencoder (VAE). The high-fidelity of the extended synthetic data set highlights that this method can be a quick and low-cost alternative to study microdroplet formation in future lab on a chip applications, where experimental data may not be readily available.

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1 Introduction

The control of droplet formation and size using microfluidic devices is a major challenge for both laboratory and industrial applications (e.g. emulsification, encapsulation, ink-jet printing). Over the last few decades, numerous works have been done to produce droplets with a high-degree of monodispersity.^{1–4} Surfactants are often used to modify the interfacial properties of droplets and improve their stability.^{5–8} For example, Lawrence and Rees⁹ identified micro-emulsion-based formulations which are key to a better

drug delivery process with an ability to control drug release and increase drug solubility.

Nowadays, improvements in imaging techniques and in microfluidic devices enable collection of high-quality data to estimate the droplet parameters for various configurations.^{10–12} Roumpea *et al.*¹³ used a two-colour Particle Image Velocimetry setup to study the effect of surfactants during droplet formation in a flow-focusing microchannel. Recently, Kiratzis *et al.*¹⁴ studied the effect of surfactant addition in the aqueous dispersed phase during droplet generation using Ghost Particle Velocimetry (GPV). Such studies enable better understanding of surfactant transfer and adsorption. Usage of high-speed cameras with improved spatial and time resolution led to large data collections and development of semi-empirical models. These models are based on physical parameters (e.g. capillary number, flow rates, channel size) and provide new data that can be used as droplet predictors (droplet size, formation time).^{15–17} Furthermore, improvements in algorithms and computational capacity now enable numerical simulations of drop formation inside microchannels in complex configurations. Kahouadji *et al.*¹⁸ presented a very accurate

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prediction of surfactant-free droplet formation in complex microchannel geometries using a front-tracking scheme. Using Lattice Boltzmann simulations, Riaud *et al.*¹⁹ studied the formation of water droplets inside octane with Span 80 and showed the non-uniformity of the interfacial distribution of surfactant.

This ease of accessing good experimental and/or numerical data coincides with the emergence of data-driven models for microfluidics. Mahdi and Daoud²⁰ used artificial neural networks to predict the droplet size of a water-in-oil micro-emulsion. Khor *et al.*²¹ used the same method to predict the emulsion stability inside a microchannel. Deep neural networks were used to predict the flow rate or the concentration of isopropanol for different formation patterns of water-isopropanol droplets in silicone oil.²² Recently, machine learning was used to predict the performance of flow-focusing droplet generators.²³

Whilst the aforementioned papers had access to a large data set of experimental data, it is crucial to perform data augmentation for small experimental data sets. The generation of high-quality synthetic data allows the augmentation of small-sample data sets,^{24,25} such as in healthcare to generate high-fidelity synthetic patient data.²⁶ Though the use of synthetic data needs to be carefully developed and adapted for each case,²⁷ it can be a powerful tool to increase the robustness and adaptability of data-driven models.^{28,29}

This paper presents both physics-based and data-driven approaches to predict droplet size inside a flow-focusing microchannel in the presence of surfactants. A data set of 476 measurements was collected for different phase flow rates, surfactant types, including anionic, cationic, and non-ionic at several concentrations below and above the critical micelle concentration (CMC). An adaptation of the recent model of Kalli *et al.*¹⁷ was used as a benchmark, considering that this type of empirical models remains the principal approach for droplet size prediction in microfluidic configurations. For the first time, two predictive models for the surfactant-laden droplet size were built using a Bayesian regularised artificial neural network (BRANN) and the XGBoost regression. Additionally, a Variational Autoencoder (VAE) was used to generate synthetic data to enlarge the experimental data set, to access an unexplored part of the parameter space, and to decrease the uncertainty on the droplet size estimation. Finally, to quantify the effect of the data set on the final uncertainty of the prediction, a convergence analysis was performed. This aims to highlight the sensitivity on data of this type of prediction model and will help optimise further studies related to machine learning and microfluidics.

2 Materials and methods

In order to build large-scale sets of high quality data, experiments were conducted in parallel at laboratories in University College London (UCL) and the University of

Birmingham (UoB). All experiments were focused on the dripping regime where the formed drops have spherical shape.³⁰ This regime is very important for short time scale (high flow rate) applications, such as drug delivery, drop encapsulation or emulsification. The transition to drops with pancake shape⁵ was avoided to eliminate the effects of the channel walls. Machine learning models have been developed for both data augmentation, *i.e.* to generate realistic synthetic data and predict the diameter of the droplets.

2.1 Droplet generation and data acquisition

The experiments were performed in an oval cross-section flow-focusing microchannel made with glass from Dolomite Microfluidics, which has already been used in previous works.^{5,13,17} At the cross-junction the inlet dimensions are equal to $195\ \mu\text{m} \times 190\ \mu\text{m}$ (width \times depth) and the dimensions of the wide channels are equal to $390\ \mu\text{m} \times 190\ \mu\text{m}$ (width \times depth). The continuous phase was introduced *via* the side channels and then the aqueous phase was introduced *via* the central channel of the junction (see Fig. 1a). For all configurations, silicone oil (density: $\rho_c = 920\ \text{kg m}^{-3}$, viscosity $\mu_c = 4.6\ \text{mPa s}$ at $20\ ^\circ\text{C}$) was used as the continuous phase. To match the refractive index of the continuous phase and avoid optical distortions, a mixture of 52% w/w glycerol and 48% w/w water (density: $\rho_d = 1132\ \text{kg m}^{-3}$, viscosity $\mu_d = 6.8\ \text{mPa s}$ at $20\ ^\circ\text{C}$) without and with surfactant was selected as the dispersed phase. Syringe pumps were used to precisely deliver both dispersed and continuous phases at flow rates (Q_d and Q_c) respectively: KDS Scientific for UCL ($\pm 5 \times 10^{-9}\ \text{mL min}^{-1}$) and World Precision Instruments for UoB ($\pm 1.7 \times 10^{-8}\ \text{mL min}^{-1}$).

63 measurements at different flow rates were obtained without surfactant. To observe the impact of surfactant composition on the droplet diameter, 5 different surfactants were dissolved in the aqueous phase which can be categorised into three groups: anionic, cationic, and non-ionic surfactants (see Table 1). A total of 468 different measurements (392 with surfactant) at various flow rates ($Q_c \in [0.012, 0.4]$ and $Q_d \in [0.001, 0.10]$) and 34 different concentrations below the CMC and 43 above the CMC were obtained. As mentioned previously, this study focuses on spherical droplets, and all droplet diameters d are below the channel depth D ($d < 195\ \mu\text{m}$). The full list of experimental parameters used in this paper is available in Zenodo open data file.

All images were taken with a 12-bit high-speed camera (Phantom v1212 with a 1280×800 pixel resolution (UCL) and Photron SA5 with 1024×1024 pixels resolution (UoB)) both equipped with a Nivatar 12 \times zoom lens. A backlight system using LED ensured a homogeneous illumination of the main channel (see Fig. 1b) and did not affect the properties of the fluid by minimising its heating. Due to the oval geometry of the channel, it is possible to accurately position the focal plan at the centreline of the channel where the sharpest image of the channel walls is obtained by the optical system.



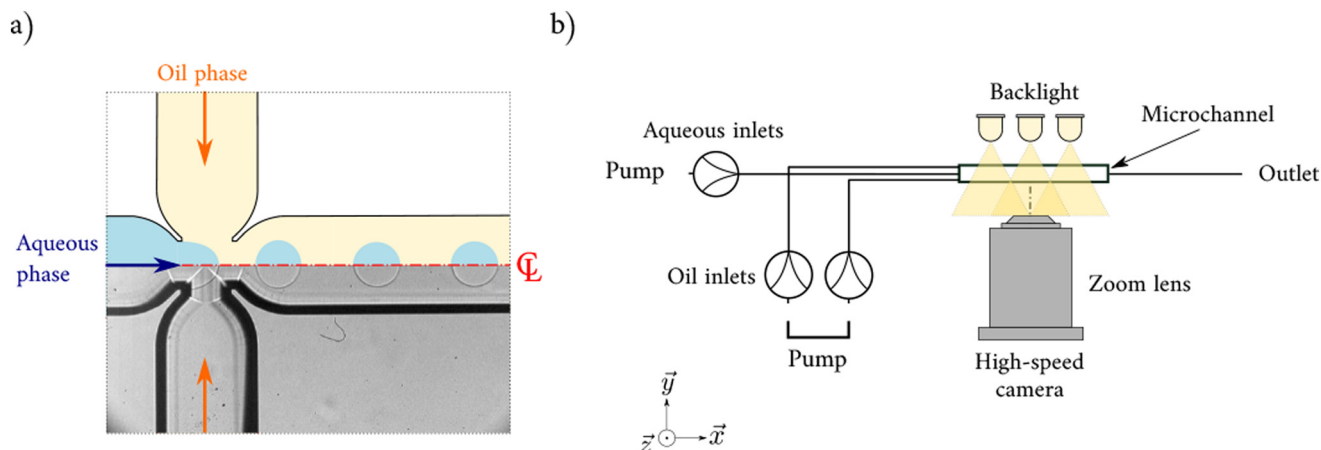


Fig. 1 a) Sketch of the microchannel during dripping regime. b) Sketch of the optical setup.

The measurement of the droplet size was directly performed on the 2D images using ImageJ and MATLAB (see ESI†). A minimum of 15 droplets was used to calculate the average size for each case with a droplet size polydispersity of <3%. According to Christopher and Anna,³¹ this is considered extremely accurate for microfluidic experiments. The spatial error is 3 μm per pixel (2.5% of the smallest drop diameter).

2.2 Modelling with machine learning

Recent advances in machine learning have shown strong predictive power that can determine complex correlations and find patterns between inputs and outputs.³² In this work two different machine learning approaches were used to predict the diameter of the droplets generated in the flow-focusing microchannel (see Fig. 1) obtained at different flow rates, surfactant type and surfactant concentration. In order to prevent overfitting, the experimental measurements were randomised and split into two distinct data sets: a training data set of 392 configurations used to train the machine learning models and a test data set of 76 configurations used to quantify the accuracy of the prediction. Different randomisations were tried and showed very similar results.

Two predictive models were developed to use different numbers of features to predict the droplet size. The data \hat{x} can then be split into predictive features $\hat{x}_{\text{predictors}}$ and the target $\hat{x}_{\text{diameter}}$. Two regressors were trained to predict the droplet diameter size $\hat{x}_{\text{diameter}}$, where f is a Bayesian regularised neural network or a XGBoost regressor. The predictions are then compared to the holdout test data set from real experimental data.

2.2.1 Bayesian regularised artificial neural network.

Recently, the Bayesian regularised artificial neural network (BRANN) has been successfully used in a variety of data-driven studies with applications including, industrial processes,³³ financial market forecasting³⁴ and engineering.³⁵ The aim of this method is to reduce overfitting by turning the non-linear system into a ‘well-posed problem’.^{36,37} The BRANN minimise the objective function F by adding the weight attenuation function E_W to classic mean squared error function E_D through the equation:

$$F = \beta E_D + \alpha E_W, \quad (1)$$

where α and β are the objective function parameters.³⁶ In the BRANN, the initial weights are randomly set and their density function follows Bayes's rule:

Table 1 Surfactant and regime parameters

Name	Type	ϕ_{CMC} mM	ϕ/ϕ_{CMC} —	M_w g mol ⁻¹	Q_d mL min ⁻¹	Q_c mL min ⁻¹	γ mN m ⁻¹	Number of data —
di-BC ₉ SG	Anionic surfactant	4.3	[1.0...50.0]	486.00	[0.003...0.04]	[0.012...0.2]	[1.4...4.2]	16
SDS	Anionic surfactant	11.0	[0.2...5.0]	288.38	[0.003...0.06]	[0.040...0.4]	[10.0...18.0]	178
C ₁₂ TAB	Cationic surfactant	20.0	[0.3...7.5]	308.34	[0.001...0.06]	[0.040...0.4]	[10.0...20.0]	94
C ₁₆ TAB	Cationic surfactant	2.0	[0.2...2.5]	364.45	[0.001...0.04]	[0.040...0.2]	[7.3...20.0]	30
TX100	Non-ionic surfactant	3.5	[1.0...8.6]	646.85	[0.010...0.02]	[0.040...0.4]	[2.8...8.7]	87
No surfactant	—	—	0	—	[0.001...0.10]	[0.080...0.4]	32	63

ϕ is the surfactant concentration; ϕ_{CMC} , the critical micelle concentration; M_w , the molar mass; Q_d and Q_c the dispersed and continuous flow rates; γ , the equilibrium interfacial tension. Full name of the surfactants: sodium bis(2,6-dimethyl-4-heptyl)-2-sulfoglutarate (di-BC₉SG), sodium dodecylsulfate (SDS), dodecyltrimethylammonium bromide (C₁₂TAB), hexadecyltrimethylammonium bromide (C₁₆TAB) and Triton X-100 (TX100).



$$P(w|D, \alpha, \beta, M) = \frac{P(D|w, \alpha, \beta, M)P(w|\alpha, M)}{P(D|\alpha, \beta, M)}, \quad (2)$$

where w is the vector of network weights, D the data vector, and M is the neural network used; $P(w|\alpha, M)$ represents the knowledge of the weights before any data is collected, $P(D|w, \alpha, \beta, M)$ the probability of the data occurring with given weights w and $P(D|\alpha, \beta, M)$ is a normalisation factor. Note, in this case, optimising weights means maximising the term $P(w|D, \alpha, \beta, M)$, which is equivalent to minimising the objective function F (eqn (1)).

Finally, another advantage of BRANN is that the model is robust and a validation process such as back propagation is unnecessary,³⁷ which can save data for the training and test processes.

The simulation of the neural network model was performed on the MATLAB Statistics and Machine Learning Toolbox.

2.2.2 XGBoost. XGBoost is the implementation of gradient boosted decision trees whilst performing at higher speeds by pushing the limits of the computational resources. XGBoost stands for eXtreme Gradient Boosting and it was implemented by Chen and Guestrin.³⁸ XGBoost uses accurate approximations by employing second-order gradients and advanced regularisation. The most important factor behind the success of XGBoost is its scalability in all scenarios. The system runs more than ten times faster than existing popular solutions on a single machine and scales to billions of examples in distributed or memory-limited settings.

The objective function is the sum of loss function, which is evaluated across all predictions with a regularisation function for all j predictors. The prediction of the j th tree is defined as:

$$\text{obj}(\theta) = \sum_i^n l(y_i - \hat{y}_i) + \sum_{j=1}^J \Omega(f_j) \quad (3)$$

For regression problems, like our case, XGBoost uses the mean squared error (MSE) as a performance metric. The XGBoost regressor was implemented in Python using the xgboost package.

2.2.3 Variational autoencoder. Autoencoders (AE) were developed to reconstruct high-dimensional data using a neural network model composed of an encoder and a decoder.³⁹ AEs can also reduce the dimensionality of the system with the encoder mapping the input onto a bottleneck layer. Furthermore, a Variational Autoencoder (VAE)⁴⁰ instead of mapping onto a fixed vector, maps the input onto an arbitrary distribution.

Let \mathcal{Q} and \mathcal{P} be the encoder and decoder, respectively. Moreover, let $q(\mathbf{z}|\mathbf{x})$ and $p(\tilde{\mathbf{x}}|\mathbf{z})$ be the encoding and decoding distributions, respectively. Here, \mathbf{x} is the vector of experimental data. As suggested by Makhzani *et al.*,⁴¹ a Gaussian posterior can be used assuming that $q(\mathbf{z}|\mathbf{x})$ is a Gaussian distribution, where its mean and variance are

predicted by the encoder \mathcal{Q} : $\mathbf{z} \sim \mathcal{N}(\mu(\mathbf{x}), \sigma(\mathbf{x}))$. This is achieved by adding two dense layers of means μ and $\log \sigma$ to the final layer of the encoder \mathcal{Q} , and return \mathbf{z} as a vector of samples. To ensure that $\mathbf{z} \sim q(\mathbf{z}) = \mathcal{N}(\mu, \sigma^2)$, the aggregated posterior, the reparameterisation trick described by Kingma and Welling⁴⁰ was used for backpropagation through the network $\mathbf{z} = \mu + \sigma \odot \varepsilon$, where ε is an auxiliary noise variable $\varepsilon \sim \mathcal{N}(0, \mathbf{I})$.

The minimisation of the Kullback–Leibler Divergence Score (KL) loss (\mathcal{L}^{KL}) quantifies how much the probability distribution $a(x)$ differs from the probability distribution $b(x)$ as:

$$\text{KL}(a||b) = -\sum_{x \in \mathcal{X}} a(x) \log \left(\frac{b(x)}{a(x)} \right) \quad (4)$$

where, in this case, $a = q(\mathbf{z}|\mathbf{x})$ and $b = Pr(\mathbf{z}) = \mathcal{N}(0, \mathbf{I})$, the arbitrary prior. The Nesterov Adam (Nadam) is used as the optimizer.⁴² The total loss \mathcal{L}_θ is then defined as $\mathcal{L}_\theta = \mathcal{L}^{\text{KL}} + \mathcal{L}^{\text{mse}}$ where the reconstruction error \mathcal{L}^{mse} is the mean squared error defined as:

$$\mathcal{L}^{\text{mse}} = \text{argmin} ||\tilde{\mathbf{x}} - \mathbf{x}||^2 \quad (5)$$

where $\tilde{\mathbf{x}}$ is the reconstructed input of experimental data, defined as $\tilde{\mathbf{x}} = \mathcal{P}(\mathcal{Q}(\mathbf{x}))$ and the synthetic data $\hat{\mathbf{x}}$ generated by the VAE is then defined as $\hat{\mathbf{x}} = \mathcal{P}(\mathbf{z})$, $\mathbf{z} \sim \mathcal{N}(0, \mathbf{I})$, where \mathbf{I} is the identity matrix defined by the number of inputs. The logarithms of the inputs were used and scaled between 0 and 1, to account for physical inaccuracies, *i.e.* none of the experimental features can be negative. The implementation of the VAE is in Python using tensorflow with the keras wrapper.

2.3 Statistical comparison with existing models

Many studies have used physics-based methods to find correlations for droplets in microfluidic devices, especially for T-junctions. In this case, to determine the droplet size, the models are mainly based on the dynamics of the break-up of the interface which is affected by the ratio Q_d/Q_c .^{43–45}

Xu *et al.*¹⁵ studied squeezing and dripping regimes in a T-junction and argued that the equilibrium between the shear forces from the continuous flow and the inertial force plays an important role in the drop formation process. The authors assume that the droplet size should be predicted by the generic equation:

$$\frac{d}{D} = \varepsilon + k \left(\frac{Q_d}{Q_c} \right)^\alpha \left(\frac{1}{\text{Ca}_c} \right)^\beta, \quad (6)$$

with ε is a parameter dependent on the geometry of the channel, d is the droplet diameter, D the channel depth, Q_d the flow rate of the dispersed phase, Q_c the flow rate of the continuous phase, and $\text{Ca}_c = \mu_c Q_c / (\gamma S)$ the capillary number for the continuous phase (where S is the cross-sectional area of the inlet junction, γ is the equilibrium interfacial tension, and μ_c is the continuous phase viscosity). Recently, Kalli



*et al.*¹⁷ used eqn (6) with $\alpha = 0.188$, $\beta = 0.161$, $\varepsilon = 0$, and $k = 0.642$ to predict with good agreement the size of surfactant-laden droplets generated in a flow-focusing microchannel:

$$\frac{d}{D} = 0.642 \left(\frac{Q_d}{Q_c} \right)^{0.188} \left(\frac{1}{Ca_c} \right)^{0.161} \quad (7)$$

Using the same flow-focusing microchannel, eqn (7) was applied to the present data-sets. Fig. 2 compares the experimental test data with those calculated from the model using eqn (7), showing a mean absolute percentage error (or MAPE) of 11.4%. The MAPE is defined by:

$$MAPE = \frac{1}{n} \sum_{i=1}^n \left| \frac{d_{\text{exp}} - d_{\text{model}}}{d_{\text{exp}}} \right|, \quad (8)$$

with n being the number of data points, d_{exp} the experimental value of the droplet diameter, and d_{model} the prediction of the droplet diameter. This MAPE of 11.4% based on a physics-based model can be used as a reference to measure the effectiveness of the following data-driven models.

3 Results

3.1 Droplet size prediction

3.1.1 Model comparison. Physics-based models can help determine the inputs needed for the droplet diameter estimation. Then, as seen in eqn (6) the flow rates Q_d , Q_c and the capillary number of the continuous phase Ca_c play an important role in the estimation of the droplet diameter. Moreover, as highlighted by Mahdi and Daoud²⁰ in their study of microdroplet formation in a T-junction using

artificial neural network modelling, the relative importance of Ca_d is of the same order of magnitude as that of Ca_c for the droplet size prediction. The authors based their model on four main inputs which are the Reynolds and capillary numbers: Re_c , Re_d , Ca_c and Ca_d of both continuous and dispersed phases respectively, defined as:

$$Re_i = \frac{\rho_i Q_i D}{\mu_i S} \text{ and } Ca_i = \frac{\mu_i Q_i}{\gamma S}, \quad (9)$$

with Q_i the flow rate, ρ_i the density, and μ_i the viscosity ($i = d, c$).

As the role of surfactants is central to the present study, the ratio ϕ/ϕ_{CMC} is used for their comparison, where ϕ is the surfactant concentration and ϕ_{CMC} is the critical micelle concentration. This is used in the data-driven model to improve the droplet size prediction. However, as described in section 2, all experiments were performed in the same channel with the same phases. As a result, the variation of the Reynolds numbers depends only on the flow rates while that of the capillary numbers on the flow rates and interfacial tension: $Re_i(\rho_i, \mu_i, S, D, Q_i) \equiv Re_i(Q_i)$ and $Ca_i(\mu_i, S, \gamma, Q_i) \equiv Ca_i(\gamma, Q_i)$. Finally, the model can be trained with the 4 following inputs: Q_d , Q_c , γ and ϕ/ϕ_{CMC} .

Fig. 3 shows dimensionless droplet diameter predictions with both BRANN and XGBoost trained using the test data set with these 4 inputs. To get robust predictions, both models were run 50 times and averaged. The standard errors are low ($\max(\text{errors}) < 1.6\%$) which highlights the excellent repeatability of the models. The MAPEs for the test data set are 3.9% for both data-driven models which highlight the good selection of the 4 inputs. Moreover, this result shows the superior prediction of the dimensionless droplet diameter d/D by both BRANN and XGBoost to that of the semi-empirical model (with associated MAPE = 11.4%, as shown in Fig. 2).

As proposed by the Garson equation, the neural network weight matrix can be used to determine the relative importance of inputs^{20,46,47} using the following equation:

$$I_j = \frac{\sum_{m=1}^{N_h} \left[\left(|W_{jm}^{ih}| / \sum_{k=1}^{N_i} |W_{km}^{ih}| \right) \times |W_{mn}^{ho}| \right]}{\sum_{k=1}^{N_i} \left[\sum_{m=1}^{N_h} \left(|W_{km}^{ih}| / \sum_{k=1}^{N_i} |W_{km}^{ih}| \right) \times |W_{mn}^{ho}| \right]}, \quad (10)$$

where, I_j is the relative importance of the j th input, N_i and N_h are respectively the number of input and hidden neurons; W is the connection weight; i, h, and o refer to input, hidden, and output layers; k , m , and n refer to input, hidden, and output neurons.

Fig. 4 shows a diagram of the relative importance of each input variable for both models. For the BRANN and the XGBoost, the flow rate of the continuous phase Q_c has the most important effect on the dimensionless droplet size prediction at respectively 55.2% and 32.1%. This result

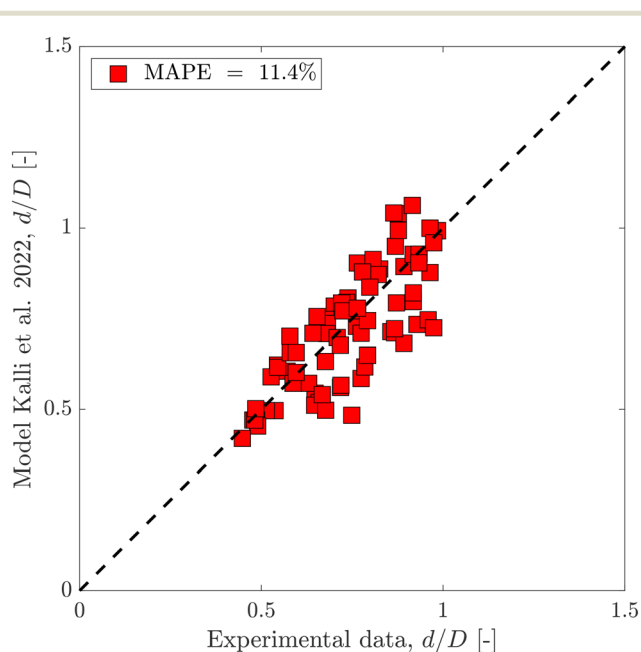


Fig. 2 Predicted dimensionless droplet diameter using the semi-empirical equation eqn (7) compared to the experimental test data set.



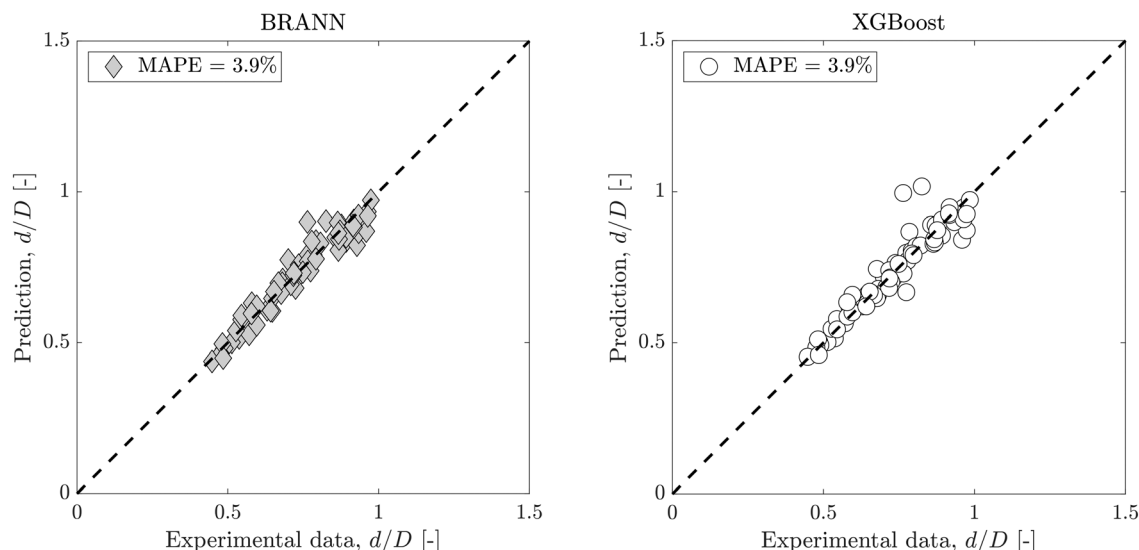


Fig. 3 Predicted dimensionless droplet diameter using 4 inputs (Q_c , Q_d , γ , ϕ/ϕ_{CMC}) compared to the experimental test data set; (left) dimensionless droplet diameter prediction using BRANN, and (right) dimensionless droplet diameter prediction using XGBoost.

confirms the strong impact of Q_c on the droplet formation, already highlighted by the semi-empirical eqn (6), directly through the term Q_c and indirectly through $Ca_c(\mu_c, S, \gamma, Q_c)$. The flow rate of the dispersed phase Q_d (BRANN: 18.8%, XGBoost: 17.7%) and the ratio ϕ/ϕ_{CMC} (BRANN: 17.3%, XGBoost: 29.2%) have a lower contribution but still a significant impact on this model. Although, the relative importance of the interfacial tension γ , is still significant for the XGBoost (21.0%), it become less crucial for the BRANN prediction (8.6%).

3.1.2 Effect of reduced inputs. As recently shown by Kalli and Angeli,⁴⁸ it is preferred to use the dynamic interfacial

tension instead of the equilibrium value, to generate universal flow pattern maps. However, it can be difficult to obtain an accurate estimation of the dynamic interfacial tension for forming droplets because classical methods based on a fixed interface (as pendant drop tensiometry or force tensiometry) may not be representative.¹⁷ Moreover, it was shown in the previous section that γ seems to have a small impact on the BRANN prediction.

Fig. 5 shows the dimensionless droplet diameter predictions on the test data set for both BRANN and XGBoost trained with only 3 of the inputs: Q_c , Q_d and ϕ/ϕ_{CMC} . Although there is a small increase of the MAPE (6.4% for the BRANN and 5.2% for the XGBoost), these errors are smaller than the semi-empirical model eqn (7). This result highlights the accuracy of the data-driven models, especially when compared with the reference semi-empirical models, even with reduced inputs. However, for this case, XGBoost shows a significantly lower uncertainty than BRANN and demonstrates its usefulness when reduced inputs need to be used (e.g. inaccessibility of experimental data).

These reduced input models with a low uncertainty can be key to predicting accurately the droplet size for low-cost or rapid measurements, with a limited number of parameters available.

3.2 Generation of a synthetic data set

Based on the full training data set, high-fidelity synthetic data were generated using VAE (see section 2.2.3). This technique enables experimental data sets, which can be costly and time-consuming to acquire, to be enlarged easily.

Fig. 6a, shows an example of the classic flow pattern map for the dripping regime, often used in droplet generation works with different microfluidic configurations. The colourmap corresponds to the droplet diameter. As the

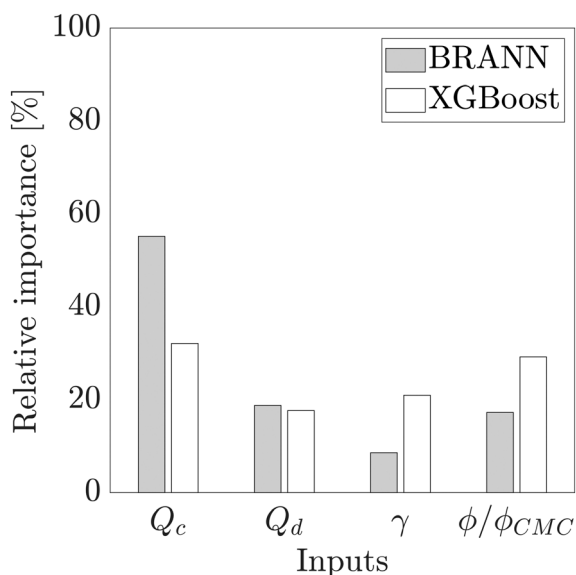


Fig. 4 The relative importance (%) of neural network inputs (Q_c , Q_d , γ , ϕ/ϕ_{CMC}) on the output (d/D) of both the neural networks, BRANN (grey) and XGBoost (white).



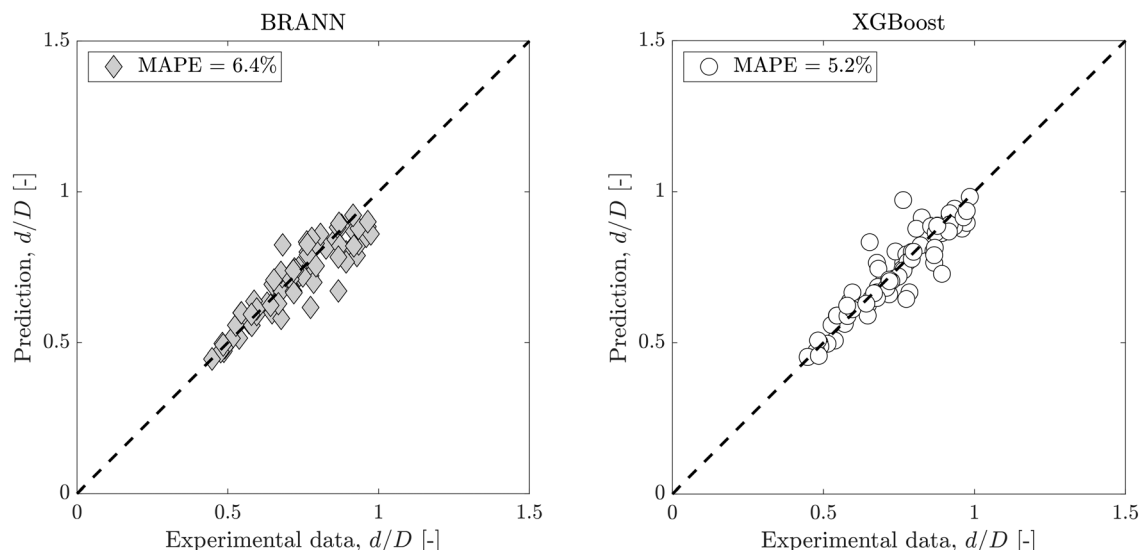


Fig. 5 Predicted dimensionless droplet diameter using 3 inputs (Q_c , Q_d , ϕ/ϕ_{CMC}) compared to the experimental test data set; (left) dimensionless droplet diameter prediction using BRANN, and (right) dimensionless droplet diameter prediction using XGBoost.

experimental measurement acquisition is a long process, the same flow rates were often used for the experiments with different surfactants and surfactant concentrations to enable

comparison, resulting in an overlap of the experimental points and a large undefined zone in the parameter space. Fig. 6b, shows 10 000 synthetic data generated in a random grid with all inputs (Q_c , Q_d , γ and ϕ/ϕ_{CMC}). In addition, the synthetic flow pattern map follows the exact shape of the real flow pattern map, while giving access to new information in the entire map and overcomes any experimental overlapping. Moreover, the synthetic data give access to a clear distribution of the droplet size in the flow pattern map. The excellent quality of these synthetic data can also be observed through Fig. 7. This figure shows the kernel density estimator (KDE) for the distributions of experimental against synthetic data for the four inputs and for the droplet diameter. For all cases, the synthetic data distribution is very similar to the experimental one which highlights the good mimicking capability of machine learning methods. Moreover, for 4 features, the KL divergence is 0.29, 0.62, 0.47, 1.49, and 0.04 for Q_c , Q_d , γ , ϕ/ϕ_{CMC} , and d/D , respectively.

To challenge the synthetic data, they were used to train the BRANN and XGBoost models and predict the droplet size d/D of the test data set. Fig. 8a shows the MAPE of the test data set using different amounts of synthetic data between 10 and 10 000. To be more robust, the figure shows the average of the MAPE for 50 different runs per point, where error bars of the standard error are smaller than the markers. When the BRANN model is trained with a small synthetic data set (<100), the MAPE is bigger than the semi-empirical model of eqn (7) (MAPE = 11.4%). However, both models converge respectively to a MAPE of 7.3% (BRANN) and 6.1% (XGBoost) after being trained with 250 synthetic data. To highlight the effect of the randomness of the data set on the droplet size prediction, 10 000 new synthetic data following a regular grid in Q_c and Q_d were built to mimic classic experimental investigations (see Fig. 6c). Fig. 8b shows the MAPE of the test data set using different number of synthetic

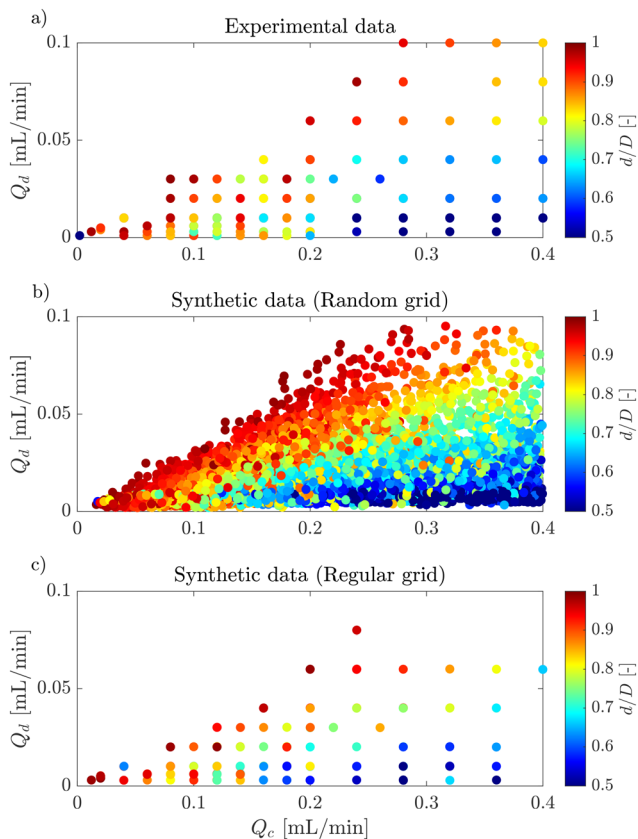


Fig. 6 Flow pattern map of the dripping regime for: a) experimental data, b) 10 000 random synthetic data, c) 10 000 regular synthetic data.



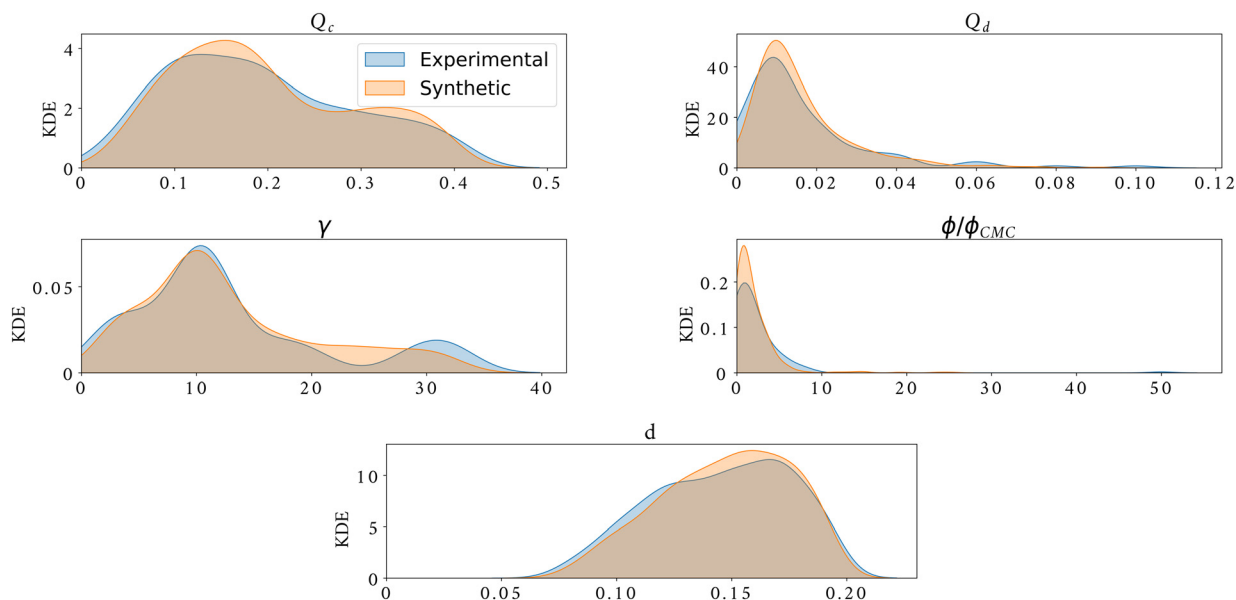


Fig. 7 Kernel density estimator of experimental data (shaded blue) against synthetic data (shaded orange) for the generation of 4 features plus droplet diameter size.

data with this new grid. Once again, for both models, the MAPE converge after 250 synthetic data. However, the droplet size prediction is more accurate with a regular grid than with a random grid (MAPE = 6.4% for BRANN and MAPE = 5.5% for XGBoost). These results define the minimum size of the

training data set needed and provide a direction for future experimental studies. Coupled with design of experiment methods⁴⁹ the synthetic data could be an excellent tool for elaborating strategies to sample complex experimental data sets.

Estimations using the real data even with only 3 inputs are closer to the experiments compared to the empirical model. The MAPEs of all models are summarised in Table 2. The mean absolute percentage error (MAPE) of the test data set was calculated for BRANN and XGBoost, and compared with the semi-empirical prediction (MAPE = 11.4%). Using Q_d , Q_c , γ and ϕ/ϕ_{CMC} as inputs, both models give an excellent prediction of the dimensionless droplet diameter d/D (MAPE = 3.9%) and show a great potential in linking machine learning with microfluidics to improve current predictive capabilities. Although the MAPEs are higher for the synthetic data than for the real data, the results are still more accurate than those obtained by using the semi-empirical model to predict the dimensionless droplet diameter. Therefore, this approach provides a quick and low-cost alternative to study droplet generation in a specific region of the flow pattern map with an acceptable uncertainty.

3.3 Validation of synthetic data in the laboratory

In order to further validate the synthetic data against laboratory experiments, 10 new experiments were performed using surfactant free and surfactant-laden solutions. For the former, the absolute errors between synthetic and observed droplet diameter sizes range from 2.2% to 5.7%, while for the latter the range was 0.9% to 5.9% using C₁₂TAB surfactant and 3.8% to 7.0% using TX100 surfactant. This shows good agreement with the synthetic

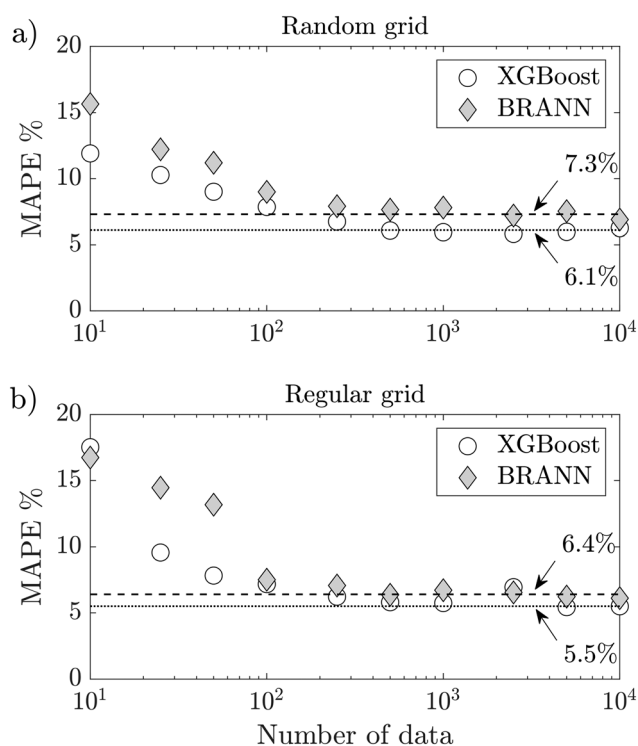


Fig. 8 Evolution of the MAPE of the test data set with the number of synthetic data for both BRANN and XGBoost: a) using a random grid, b) using a regular grid.



Table 2 Mean absolute percentage error (MAPE) comparison of the test data set for all models

Kalli <i>et al.</i> ¹⁷ Eqn (7)	BRANN			XGBoost		
	4 inputs (ED)	4 inputs (SD)	3 inputs (ED)	4 inputs (ED)	4 inputs (SD)	3 inputs (ED)
11.4%	3.9%	7.3%	6.4%	3.9%	6.1%	5.2%

ED: experimental data, SD: synthetic data.

data. For example, Lashkaripour *et al.*²³ reports absolute errors of ~1.6% to 10% between predicted and observed droplet diameter size after replicating surfactant free experiments in the laboratory.

4 Summary, discussion and future work

Based on high-speed imaging measurements of surfactant-laden droplets generated in a flow-focusing microchannel, a large drop size data set was produced. To predict the dimensionless droplet diameter for various flow rates, surfactant type and surfactant concentration, two data-driven models (BRANN and XGBoost) were used and compared to a recent semi-empirical model (Table 3).¹⁷

The mean absolute percentage error (MAPE) of the test data set was calculated for BRANN and XGBoost, and compared with the semi-empirical prediction. Using Q_d , Q_c , γ and ϕ/ϕ_{CMC} as inputs, both models give an excellent prediction of the dimensionless droplet diameter d/D and show a great potential in linking machine learning with microfluidics to improve current predictive capabilities. Moreover, as the experimental estimation of the interfacial tension can be subject to discussion⁴⁸ and hard to collect for dynamic and fast processes, the models were also trained with reduced number of inputs (Q_d , Q_c , and ϕ/ϕ_{CMC}). The results show that even if the MAPE increases slightly, the estimation of d/D is still more accurate with machine learning techniques than with semi-empirical methods. However, in this case, XGBoost gives a better prediction than BRANN. Finally, as experimental data sets can be costly and time-consuming to enlarge them, a synthetic data set of 10 000 new experiments was built using VAE with all available inputs. Training the BRANN and XGBoost models with this synthetic data set, the MAPEs still outperform the semi-empirical model (Table 4).

The real interest on synthetic data lies on gaining access to a part of the parameter space with a low uncertainty, where data is not available due to experimental difficulties. Experimental data often follow a discrete distribution and the synthetic data can transform this into a continuous distribution. In this way, the previous results can be seen as a tool to help experimentalists design their next experiments. For example, it can be an excellent strategy to improve the

filling of flow pattern maps extensively used in microfluidics but extremely time-consuming to acquire. Future work includes the exploration of other generative networks like generative adversarial networks,⁵⁰ diffusion models,⁵¹ or normalising flows.⁵² The latter could be of interest as they do not require a compression of the input data size *via* a bottleneck layer, but they rather work in the same input space which is advantageous if the number of features to generate synthetic data from is small.

Finally, while the purpose of this paper is to highlight the potential of data-driven models in predicting the droplet behaviour for a wide range of surfactants and surfactant concentrations, it remains focused on a specific regime and for the same fluid phases. Apart from dripping, however, other regimes of droplet generation (*e.g.* squeezing, jetting, tip-streaming) have been reported and have been extensively studied both experimentally and numerically in previous works.^{5,13,18,48,53} In addition, Kiratzis *et al.*¹⁴ showed the importance of the phase viscosity ratio on the drop formation process. This work aims to unravel the unexplored capabilities of data-driven-models for droplet microfluidics. The methodologies developed here can be extended to different regimes, fluid viscosity ratios or channel geometries, which will be the focus of our future work for building generalised models for droplet size prediction in microfluidic channels.

Appendix

A Predictive models

Table 3 Hyperparameters of predictive models

Name	Hyperparameters
XGBoost	Number of estimators: 100 Maximum depth: 3 Learning rate: 0.3 Random state: 42
Name	Hyperparameters
BRANN	Number of hidden layers: 1 Number of hidden nodes: 8 Optimisation: Bayesian regularisation Activation hidden layer: sigmoid Activation output layer: linear



B Variational autoencoder architecture

Table 4 Architectures and hyperparameters of the VAE

Name network	Hyperparameters
3Predictors	Number of features: 4 Encoder Number of hidden nodes (layer 1): 512 Activation hidden layer 1: LeakyReLU Number of hidden nodes (layer 2): 512 Activation hidden layer 2: LeakyReLU Number of nodes latent layer: 4 Decoder Number of hidden nodes (layer 1): 512 Activation hidden layer 1: LeakyReLU Number of hidden nodes (layer 2): 512 Activation hidden layer 2: LeakyReLU Number of nodes output layer: 4 Activation output layer: sigmoid Number of features: 5
4Predictors	Encoder Number of hidden nodes (layer 1): 512 Activation hidden layer 1: LeakyReLU Number of hidden nodes (layer 2): 512 Activation hidden layer 2: LeakyReLU Number of nodes latent layer: 5 Decoder Number of hidden nodes (layer 1): 512 Activation hidden layer 1: LeakyReLU Number of hidden nodes (layer 2): 512 Activation hidden layer 2: LeakyReLU Number of nodes output layer: 5 Activation output layer: sigmoid Further hyperparameters Optimiser: Nadam Dropout of 0.5 between layers Epochs: 2000 Batch size: 512 Random state: 42

Data and code availability

The code is available in <https://github.com/c-quilo/premiereDroplets>. The data are available in Zenodo: <https://zenodo.org/record/7055018#.Yxh40LTMKUK>.

Author contributions

Loïc Chagot: conceptualization, methodology, software, writing – original draft preparation/reviewing and editing, visualization, investigation, project administration, formal analysis. César Quilodrán-Casas: methodology, software, data curation, writing – original draft preparation/reviewing and editing visualization, formal analysis. Maria Kalli: data curation, conceptualization, investigation, validation, software, writing – original draft preparation/reviewing and editing, visualization. Nina M. Kovalchuk: data curation, investigation, validation, writing – reviewing and editing. Mark J. H. Simmons: writing – reviewing and editing, supervision, funding acquisition, resources. Omar K. Matar: supervision, funding acquisition, writing – reviewing and editing. Rossella Arcucci: supervision,

resources, writing – reviewing and editing. Panagiota Angeli: supervision, writing – reviewing and editing, funding acquisition, resources, conceptualization.

Conflicts of interest

There are no conflicts to declare.

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