An experimental and computational study of the reaction between pent-3-en-2-yl radicals and oxygen molecules: switching from pure stabilisation to pure decomposition with increasing temperature†

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We have used laser-photolysis–photoionization mass spectrometry, quantum chemical calculations, and master equation simulations to investigate the kinetics of the reaction between (E/Z)-pent-3-en-2-yl (CH3=CH=CH=CH3), a resonance-stabilised hydrocarbon radical, and molecular oxygen. The time-resolved experiments were performed over a wide temperature range (240–750 K) at relatively low pressures (0.4–7 Torr) under pseudo-first-order conditions (excess [O2]). Helium bath gas was used in most experiments, but nitrogen was employed in a few measurements to investigate the effect of a heavier collider on the kinetics of the studied reaction. The experimental traces were directly used to optimise parameters in the master equation model using the recently implemented trace fitting feature in the MESMER program. At low temperatures (T < 300 K), the reaction proceeds by barrierless recombination reactions to form peroxyl adducts, and the radical traces are single-exponential. Between 326 K and 376 K, equilibration between the reactants and the peroxyl adducts is observed, and the radical traces are multi-exponential. Interestingly, at temperatures above 500 K, single-exponential decays were again observed, although the reaction is much slower than at low temperatures. The master equation simulations revealed that at both low and high temperatures, the radical decay rate is governed by a single eigenvalue. At low temperatures, this eigenvalue corresponds to recombination reactions, and at high temperatures to the phenomenological formation of bimolecular products. Between low and high temperatures (the exact temperature thresholds depend on [O2]), there is a region of avoided crossing in which the rate coefficient “jumps” from one eigencurve...
to the other. Although chemically significant eigenvalues are not well separated from internal energy relaxation eigenvalues at elevated temperatures (600 K at 0.01 bar, 850 K at 100 bar), we observed that many of the Bartis–Widom rate coefficients produced by the master equation model were valid up to 1500 K. Our simulations predict that the most important reaction channel at high temperatures is the formation of (E/Z)-penta-1,3-diene and hydroperoxyl. The experimentally constrained master equation model was used to simulate the title reaction over a wide range of conditions. To facilitate the use of our results in autoignition and combustion models, modified Arrhenius representations are given for the most important reaction channels.

1 Introduction

Reactions between hydrocarbon radicals and oxygen molecules are key reactions in understanding the oxidation of hydrocarbons both in atmospheric and combustion chemistry. Pent-3-en-2-yl radicals are formed in these environments when an allylic hydrogen is abstracted from the fourth carbon of pent-2-ene. Understanding the oxidation mechanism of pent-2-ene is of particular importance because it is used in surrogate fuels to mimic the behaviour of the alkenes present in real fuels.\textsuperscript{1} Pent-2-ene is also a minor component of gasoline. Furthermore, pent-2-enes are formed in the oxidation of \( n \)-pentane by the reactions

\[
\begin{align*}
\text{C}_5\text{H}_{11}^\cdot + \text{O}_2 & \rightarrow \text{C}_5\text{H}_{10} + \text{HO}_2^\cdot \\
\text{C}_5\text{H}_{11}^\cdot + \text{O}_2 & \rightleftharpoons \text{C}_5\text{H}_{10}\text{O}_2^\cdot \rightarrow \text{C}_5\text{H}_{10} + \text{HO}_2^\cdot.
\end{align*}
\]

Pent-3-en-2-yl (see Fig. 1) is a resonance-stabilised hydrocarbon radical (RSHR) and such radicals usually react slower with \( \text{O}_2 \) than similar-sized hydrocarbon radicals that lack resonance stabilisation. RSHRs lose their resonance stabilisation when they recombine with \( \text{O}_2 \) and, consequently, these reactions have shallow wells (zero-Kelvin binding enthalpies). Typical well depths for allylic radicals are between \(-85\ \text{kJ mol}^{-1}\) and \(-70\ \text{kJ mol}^{-1}\),\textsuperscript{2-12} much shallower than those of alkyl and alkenyl(vinyl) radicals. For example, ethyl and ethenyl (vinyl) have well depths of \(-137\ \text{kJ mol}^{-1}\) and \(-182\ \text{kJ mol}^{-1}\), respectively.\textsuperscript{13,14} A consequence of the shallow RSHR + \( \text{O}_2 \) wells for allylic radicals is that the reverse reaction back to reactants becomes significant already at around 300–400 K. As temperature is increased, the equilibrium begins to overwhelmingly favour the reactants and no net reaction is observed unless there are low-barrier reaction channels that permit the peroxyl radical to react further.

Above 500 K, the allylic propenyl, 2-methylpropenyl, and but-3-en-2-yl radicals react slowly with \( \text{O}_2 \) (\( k < 2 \times 10^{-16} \text{ cm}^3 \text{ s}^{-1} \)),\textsuperscript{1,7,15} whereas relatively fast reactivity has been observed for pent-1-en-3-yl and 2-methylbut-3-en-2-yl (\( k > 1 \times 10^{-15} \text{ cm}^3 \))

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**Fig. 1** The equivalent resonance structures of pent-3-en-2-yl.
The phenomenological rate coefficients are comparable to those of propargylic radicals. For pent-1-en-3-yl and 2-methylbut-3-en-2-yl, the fast reactivity is explained by the presence of low-barrier reaction channels (4–17 kJ mol$^{-1}$ above the energy of the reactants)

$$\text{CH}_2\equiv\text{CH}\equiv\text{CH}\equiv\text{CH} + \text{O}_2 \rightarrow \text{CH}_2\equiv\text{CH}\equiv\text{CH}\equiv\text{CH} + \text{HO}_2^*$$

that form conjugated dienes and hydroperoxyl radicals (HO$_2^*$) through formally direct transition states. Conjugated dienes are more stable than regular alkenes, and this additional stabilisation is, to a degree, present in the transition states, which lowers their energy relative to the reactants. The relative energies of the transition states are further lowered by the alkyl substituents next to the radical centres. Substituting hydrogens next to a radical centre with alkyl groups typically makes R$^+$O$^*$ and R$^-$H + HO$^*$ transition states as well. For example, the well depths for ethylperoxyl and 2-methylpropyl-2-peroxyl are $-137$ kJ mol$^{-1}$ and $-150$ kJ mol$^{-1}$, respectively, and the relative energies of the formally direct transition states are $-9.54$ kJ mol$^{-1}$ and $-23.4$ kJ mol$^{-1}$, respectively. The propenyl + O$_2$ and 2-methylpropenyl + O$_2$ reactions cannot form conjugated dienes, which likely explains their small rate coefficients at elevated temperatures. The but-3-en-2-yl + O$_2$ reaction can form buta-1,3-diene, but Knyazev and Slagle did not observe any reaction even at 700 K, which suggests that the relative energy of the formally direct transition state is appreciably higher for but-3-en-2-yl than for pent-1-en-3-yl and 2-methylbut-3-en-2-yl. For both allylic and propargylic radicals, chemically significant eigenvalues (CSEs) begin to converge with internal energy relaxational eigenvalues (IEREs) at relatively low temperatures because the R$^+$ + O$_2$ recombination wells are shallow. The exact temperature is system- and pressure-dependent, but it is typically at the low end of temperatures relevant for autoignition (500–1000 K). The convergence and overlapping of CSEs and IEREs is a problem because the Bartis–Widom analysis that is used to obtain elementary rate coefficients from master equation (ME) models relies on them being well separated. Thus, it is difficult to obtain (or even define) phenomenological rate coefficients at exactly the temperatures where autoignition models need them. In this work, we look for practical ways of expressing the results of ME simulations when this is an issue. The system we have investigated in this work is the reaction between (E/Z)-pent-3-en-2-yl radicals and oxygen molecules,

$$\text{CH}_3\equiv\text{CH}=:\equiv\text{CH}+\text{O}_2 \rightarrow \text{products}$$ (1)

To our knowledge, the kinetics of this reaction have not been studied before. Both experimental and computational methods were used. The experiments consisted of direct kinetic measurements using laser-photolysis–photoionization mass spectrometry. The potential energy surface (PES) of reaction (1) was explored with density functional theory and the energies of the stationary points were refined with wave function methods. A ME model was constructed to simulate reaction (1) over wide temperature and pressure ranges. The results were carefully
analysed, particularly at temperatures where IEREs and CSEs overlap, to find ways to express the results in a form that is usable for combustion modelling.

2 Methods

2.1 Experimental

The experimental apparatus has been described in a previous publication, so only the details relevant to the current work are given here. The experiments were performed in tubular laminar flow reactors. Stainless steel reactors with inner diameters of 0.80 cm or 1.7 cm were used to perform measurements at low temperatures (238–298 K). Halocarbon wax coating was used with these reactors. The purpose of the coating is to make the reactor surface more inert to minimise the rate at which pent-3-en-2-yl reacts with the surface. Above room temperature, we used Pyrex® (304–376 K) and quartz (304–752 K) reactors with inner diameters of 1.7 cm and 0.85 cm, respectively. The Pyrex® and quartz reactors were coated with polydimethylsiloxane and boric oxide, respectively. The experiments were performed under pseudo-first-order conditions with the bath gas (He or N₂) typically being in huge excess over O₂. Above 500 K, huge O₂ concentrations had to be used in order to observe a reaction; up to half of the flowing gas mixture was O₂ in these measurements. Pent-3-en-2-yl radicals were homogeneously produced along the reactor by photolysing 4-bromopent-2-ene with a pulsed KrF exciplex laser. We also observed that the photolysis forms penta-1,3-diene (and presumably HBr). The laser fluences used were between 18 mJ cm⁻² pulse⁻¹ and 250 mJ cm⁻² pulse⁻¹. The radical precursor was synthesised in our laboratory as described in the literature. The purity of the precursor was ~93%, the main impurities being 1-bromobut-2-ene (~5%) and methoxymethane. The E : Z isomer ratio of the precursor was 11 : 1. The liquid precursor was purified with several freeze–pump–thaw cycles before use. A small hole on the side of the tubular reactor was used to sample a portion (5–20%) of the flowing gas mixture into a vacuum chamber containing a quadrupole mass spectrometer. A nitrogen lamp (7.1 eV) with a quartz or sapphire window was used to ionise the radical for mass spectrometric detection. A chlorine lamp (8.9–9.1 eV) with a CaF₂ window and a hydrogen lamp (10.2 eV) with a MgF₂ window were used in the search of reaction products. In a typical bimolecular rate coefficient measurement, we first determined the first-order-loss rate coefficient of pent-3-en-2-yl in the absence of O₂. We call this rate coefficient the wall rate \(k_w\) for short. The wall rate mainly describes the rate at which the radical reacts with the reactor surfaces. The self-reaction of the radical and the reaction between the radical and the precursor molecule also contribute to \(k_w\), but we minimise these contributions by using very low radical and precursor concentrations. A practical way of checking that these two reactions are not important is that one either double or halves the precursor concentration (or the laser pulse energy) and checks that the wall rate remains unchanged. The wall rate
was determined by monitoring the pent-3-en-2-yl trace in real time and fitting a single-exponential function

\[ [R^-]_t = A + [R^-]_0 e^{-kt} \]

to the obtained trace. Here, \( A \) is the signal background and \([R^-]_0\) is a value that is proportional to the initial radical concentration. The wall rate measurement was repeated at the end of a bimolecular rate coefficient determination to ensure it had remained approximately constant. After the initial wall rate measurement, a known concentration of \( \text{O}_2 \) was added to the reactor and the pent-3-en-2-yl trace was monitored. A single-exponential function was fitted

\[ [\hat{R}]_t = A + [\hat{R}]_0 e^{-k't} \]

to the trace to obtain the pseudo-first-order rate coefficient

\[ k' = k_w + k[\text{O}_2]. \]

Here, \( k \) is the bimolecular rate coefficient we wished to determine. The pseudo-first-order rate coefficient was typically measured at 4–7 different \( \text{O}_2 \) concentrations. The \( k' \) values so obtained were then plotted as a function of \([\text{O}_2]_0\). The slope of the linear fit performed on this data yields the bimolecular rate coefficient \( k \). The intercept gives a value for \( k_w \), which should be in good agreement with the measured values. We report both values in this work. Examples of bimolecular plots are shown in Fig. 2.

When equilibration between reactants and products is significant, single-exponential functions cannot be fitted to the radical traces because the radical decays are multi-exponential. If only one peroxyl adduct is formed, a double-exponential function needs to be fitted to obtain all the relevant rate coefficients.\(^{26}\) In the current case, two peroxyl adducts are formed (\((E/Z)\)-pent-3-enyl-2-peroxyl) and the radical decays are, in principle, triple-exponential. Previously, such cases have been handled by fitting a double-exponential function to triple-exponential decays to obtain average rate coefficients for the forward and reverse rate coefficients.\(^7\) However, the recently implemented trace fitting feature\(^{27}\) in MESMER largely obviates the need to do this (see the Master equation section). Nonetheless, we performed double-exponential fits to the measured equilibration traces for comparison purposes. These fits also provide reasonable estimates for the peroxyl radical wall rates – information that is needed for trace fits. Fig. 3 describes how the radical trace changes from single- to multi-exponential as temperature is increased from 298 K to 371 K.

2.2 Quantum chemistry

The geometries of the stationary points of reaction (1) were optimised at the MN15/Def2TZVP level of theory.\(^{28,29}\) This level of theory was also used to obtain harmonic frequencies and one-dimensional hindered rotor potentials (five-degree increments). The harmonic frequencies were scaled by a factor of 0.979 to partially account for anharmonic effects.\(^{30}\) Single-point energies were computed for the stationary points with the ROHF-DLPNO-CCSD(T1) method.\(^{31,32}\) The T1 in the parentheses stands for an improved, iterative calculation of the triples correction\(^{33}\) and is not the T1 diagnostic.\(^{34}\) The tightPNO keyword was specified in the DLPNO-CCSD(T1) optimisation.
The calculations were performed with the cc-pVDZ, cc-pVTZ, and cc-pVQZ basis sets. The Hartree–Fock (HF) energies were extrapolated to the complete basis set (CBS) limit using a three-parameter exponential function,\(^{35}\)

\[
E_{\text{HF}}(X) = E_{\text{HF},\infty} + B_{\text{HF}}e^{-\alpha_{\text{HF}}X}.
\]

The slower converting correlation energies were extrapolated to the CBS limit using\(^{36}\)

Fig. 2  Examples of bimolecular plots at (a) 268 K and (b) 601 K. The radical traces shown in the upper left and bottom right corners were recorded in the presence and absence of O\(_2\), respectively. In both figures, the coloured symbols depict the measurements that correspond to the shown traces. Above 500 K, the fitted and measured wall rates do not match. Possible reasons for this are discussed in the Results and discussion section.
\[ E_{\text{corr}}(X) = E_{\text{corr},\infty} + B_{\text{corr}}X^{-\alpha_{\text{corr}}}. \]

Here \( X = 2, 3, \) and \( X = 4 \) for the basis sets cc-pVDZ, cc-pVTZ, and cc-pVQZ, respectively. The CBS energy is obtained in both cases by solving a system of three equations. An analytical solution exists for the former, but the latter needs to be solved numerically. We performed CASPT2 calculations for many of the species to check if multi-reference treatment was needed. The CBS energy difference of these calculations was estimated from

\[ \Delta E_{\text{inf}} = \Delta E_{\text{cc-pVQZ}} - (\Delta E_{\text{cc-pVQZ}} - \Delta E_{\text{cc-pVQZ}}) \frac{4^4}{5^4 - 4^4}. \]  

(2)

The CASPT2 calculations were run with the default settings (no IPEA or level shifts were used). The ORCA software package 4.2.0 was used for the ROHF-DLPNO-CCSD(T1) and CASPT2 calculations. The MN15/Def2TZVP calculations were run with Gaussian 16. The output files of our electronic structure calculations are available upon request.

2.3 Master equation modelling

We used MESMER 6.1 program to perform our ME simulations. It is a one-dimensional ME code, meaning that angular momentum dependence is
neglected. Microcanonical rate coefficients were calculated with RRKM theory. For the barrierless pent-3-en-2-yl + O2 recombination reactions, we used the inverse Laplace transform (ILT) approach to obtain the number of states for the loose transition states. The expression we transformed was the modified Arrhenius expression

\[ k_a(T) = A \left( \frac{T}{300 \text{ K}} \right)^m e^{-\frac{E_a}{RT}}. \]

Here \( A \), \( m \), and \( E_a \) are the modified Arrhenius parameters. The exponential factor \( E_a \) is typically set to zero for barrierless reactions, and this was also done in this work. Reaction (1) can form two different peroxy adducts ((E/Z)-pent-3-enyl-2-peroxyl) and both channels were given their own Arrhenius expression. Collisional energy transfer was described with the standard exponential down model

\[ \langle \Delta E \rangle_{\text{down}} = \langle \Delta E \rangle_{\text{down,ref}} \left( \frac{T}{300 \text{ K}} \right)^n. \]

Here \( \langle \Delta E \rangle_{\text{down,ref}} \) is the average energy transferred downward at 300 K; \( n \) accounts for its temperature dependence. The same exponential parameters were used for all intermediates (\( \text{C}_5\text{H}_9\text{O}_2 \) species). If experimental data is supplied, automated fitting routines in MESMER can be used to optimise the values of the Arrhenius and exponential down parameters. Note that the angular momentum dependence is implicitly accounted for when calculating microcanonical rate coefficients from an experimental \( k_a(T) \) expression with the ILT method. Collision frequencies were calculated with Lennard–Jones (LJ) interaction potentials. The LJ parameters for He and N2 were obtained from the literature. We assigned the LJ parameters of (E)-pent-3-ene-2-peroxyl for the \( \text{C}_5\text{H}_9\text{O}_2 \) intermediates. These values were estimated with the Joback method using the online resources of Cantherm. The used LJ-parameters are listed below:

\[ \varepsilon_{\text{LJ}}(\text{He}) = 10.22 \text{ K}, \quad \sigma_{\text{LJ}}(\text{He}) = 2.551 \text{ Å} \]
\[ \varepsilon_{\text{LJ}}(\text{N}_2) = 71.4 \text{ K}, \quad \sigma_{\text{LJ}}(\text{N}_2) = 3.798 \text{ Å} \]
\[ \varepsilon_{\text{LJ}}(\text{C}_5\text{H}_9\text{O}_2^+) = 466.0 \text{ K}, \quad \sigma_{\text{LJ}}(\text{C}_5\text{H}_9\text{O}_2^+) = 6.55 \text{ Å}. \]

An energy grain of 75 cm\(^{-1}\) was used in all simulations, and the cut-off energy was set to be \( 25k_BT \) above the energy of the highest stationary point. Tunnelling corrections were calculated for hydrogen abstraction reactions using the Eckart tunnelling model. For species with three or more hindered rotors, we used the method of Gang \textit{et al.} to treat coupling between internal and external rotations. This method is completely classical, so to avoid double-counting the zero-point energy (ZPE) contributions from hindered rotors for a species, we subtracted these ZPEs from the ZPE-corrected energy of the species. The hindered rotor ZPEs were obtained from one-dimensional, quantum mechanical hindered rotor calculations. The current implementation of the method of Gang \textit{et al.} in MESMER does not explicitly treat potential coupling between hindered rotors. We
used the recently implemented trace fitting feature in MESMER for parameter optimization. With this feature, simulated and experimental traces are directly compared and parameter optimisation attempts to minimise the difference between the two. This feature is useful when the experimental traces are multi-exponential in nature and/or when CSEs and IEREs overlap. Both of these are issues in the current work. In the former case, it is generally difficult to fit multi-exponential functions to experimental traces and obtain reliable values for the fitting parameters. If the uncertainties in the fitting parameters are large, then this uncertainty will be reflected in the rate coefficients that are functions of these parameters. In the latter case, the Bartis–Widom analysis that is used to obtain phenomenological rate coefficients may not be applicable and, if so, there are no rate coefficients that can be compared with experimental ones. The traces produced by ME simulations are unaffected by the overlap of IEREs and CSEs and can always be compared with experimental traces. Sometimes, wall reactions and/or diffusion can affect the time-dependent behavior of experimental traces, and to account for this, first-order rate coefficients that describe these phenomena need to be specified in the MESMER input file. In the simulations, rotations around allylic Cfc bonds were treated as hindered rotations, meaning that the E and Z isomers of pent-3-en-2-yl were not treated as separate species. At the MN15/Def2TZVP level of theory, the barriers for these rotations were around 60–70 kJ mol$^{-1}$. Due to the height of the rotation barrier, it would actually be more accurate to treat the isomers as separate species at cold temperatures ($T < 300$ K). However, because the photolysis of the precursor produces an unknown mixture of E and Z isomers (we cannot be certain that the E/Z ratio of the radicals will be that of the precursors), we chose to lump the isomers into a single species. This also simplifies the simulations by reducing the number of wells by one. Furthermore, at higher temperatures ($T > 500$ K), it is more appropriate to treat the isomers as a single species.

3 Results and discussion

3.1 Experimental

The results and conditions of our bimolecular rate coefficient measurements are reported in the ESI (Table S1†). We observed that there were three different temperature regimes in which the time-dependent behaviours of the measured traces were visibly different. We will refer to these as the low-temperature regime ($T \leq 300$ K), the equilibration regime ($300$ K $< T < 500$ K), and the high-temperature regime ($T \geq 500$ K). Single-exponential decays are observed in the low- and high-temperature regimes, but reaction (1) is several orders of magnitude slower in the high-temperature measurements. Multi-exponential decays are observed in the equilibration measurements. At low temperatures, pent-3-en-2-yl recombines with O$_2$ to form (E/Z)-pent-3-enyl-2-peroxyl. The recombination rate coefficient is pressure-dependent and has negative temperature dependence. A few experiments were performed in N$_2$ bath gas. The bimolecular rate coefficient is roughly 20–30% larger in N$_2$ than He bath gas in the covered pressure range. Since N$_2$ is a more effective collider, this result is as one would expect. However, the He and N$_2$ rate coefficient measurements are within experimental uncertainty ($\pm 20\%$). The low-temperature measurements are depicted in Fig. 4a. We estimate that the overall uncertainty of the low-temperature bimolecular rate coefficient
measurements is ±20%. This uncertainty mainly originates from the uncertainties in the measured gas flow rates, particularly that of O₂.

Fig. 5 displays R’ + O₂ → RO₂⁺ fall-off curves for several allylic radicals. One can immediately observe that reactivity increases with radical size, both in the fall-off region and at the high-pressure limit. Interestingly, reaction (1) is the fastest of the five-carbon allylic radicals. A possible explanation for this is that the reactivity is enhanced by the presence of alkyl groups next to the radical centres. In pent-3-en-2-yl, both of the possible radical centres are methyl-substituted,

\[
\text{CH}_3\text{CH}==\text{CH}==\text{CH}_3 + \text{O}_2 \rightarrow \text{CH}_3\text{CH}==\text{CH}==\text{CH}_3 + \text{O}_2
\]

Fig. 4 This figure depicts the CH₃⁻⁻CH═CH═CH−CH₃ + O₂ rate coefficient as a function of temperature and pressure. Below 300 K (a), the rate coefficient describes the CH₃⁻⁻CH═CH═CH−CH₃ + O₂ → CH₃⁻⁻CH(ÖO⁻)⁻⁻CH═CH−CH₃ recombination reaction. Above 500 K (b), the (phenomenological) rate coefficient describes the pressure independent CH₃⁻⁻CH═CH═CH−CH₃ + O₂ → bimolecular products reaction.
whereas in pent-1-en-3-yl and 2-methylbut-3-en-2-yl, only one radical centre is alkyl substituted. In 2-methylbut-3-en-2-yl, the aforementioned radical centre is doubly substituted, but given its lower reactivity compared to that of pent-3-en-2-yl, it would appear that the reactivity enhancing effect of alkyl substitution is subject to diminishing returns. For pent-1-en-3-yl and 2-methylbut-3-en-2-yl, the experiments are in close agreement, well within experimental uncertainty, and it is difficult to assess which one is more reactive. The extrapolated high-pressure rate coefficients are not accurate enough to make that distinction either. The argument based on the reactivity enhancing effects of alkyl substitution can also be used to explain why the five-carbon allylic radicals are more reactive than the four-carbon ones, which in turn are much more reactive than allyl.

At slightly above room temperature (326–376 K), equilibration between the reactants and the peroxyl radicals is observed, and the pent-3-en-2-yl traces are triple-exponential. We were not able to reliably fit a triple-exponential function to these traces, so we fitted a double-exponential function and used the averaging scheme of Knyazev and Slagle\(^7\) to obtain “average” forward and reverse rate coefficients. These were then used to evaluate an “average” equilibrium constant. The standard states of the gases were chosen as the pure ideal gas at \(p^\ominus = 1\) bar at the temperature of interest. The results and conditions of the equilibration measurements are reported in Table S2 in the ESI\(^†\) and shown in Fig. 6.

At high temperatures (\(T > 500\) K), single-exponential decays were again observed and bimolecular rate coefficient measurements were resumed. The phenomenological rate coefficient at these temperatures is pressure independent and has positive temperature dependence. The results of the measurements are displayed in Fig. 4b. As can be seen from Fig. 2 and Table S2 in the ESI,\(^†\) in the high-temperature measurements, the fitted wall rates are systematically about 10 s\(^{-1}\) higher than the measured ones. This kind of behaviour is observed, for example, when the reaction under study forms a product that sticks to the reactor walls, where it can then react with the radical whose trace is monitored. Fig. 2 shows that the \([O_2]\)-dependence of \(k'\) is nonetheless linear, which indicates that even a small amount of oxygen is able to saturate the reactor surface with
whatever it is that sticks to the walls. Thus, the wall rate remains constant in these measurements, although it is not the same wall rate as the one that is measured in the absence of O₂. When we measured the wall rate immediately after a measurement with O₂ present, we noticed that the wall rate was higher than the rate measured in the beginning of the day, but it fairly quickly decayed back to its original value, usually within 30 minutes. We have included in the ESI† all the high-temperature bimolecular plots. These show that the discrepancy in the measured and fitted wall rates was systematic. The plots also demonstrate that the [O₂]-dependence of k₀ was linear in all of the measurements, meaning that the slopes of the linear fits gave the bimolecular rate coefficient of reaction (1). However, this atypical behaviour on the walls adds some uncertainty to our measurements, and therefore, we assign a higher uncertainty to the high-temperature measurements, ±40%.

The expected high-temperature products of reaction (1) are (E/Z)-penta-1,3-diene and hydroperoxyl.⁴⁻⁶,¹⁶ We searched for penta-1,3-diene with a hydrogen lamp (10.2 eV) and a formation signal was found at m/z = 68. A similar but noisier signal was also observed with a chlorine lamp (8.9–9.1 eV). Unfortunately, the formation signal was also seen in the absence of O₂. The two formation signals were compared, but there is no obvious difference between the two. Thus, the experimental evidence for penta-1,3-diene formation from reaction (1) at high-temperatures is inconclusive. At present, we are unable to give an explanation for the product-like formation signal at m/z = 68 in the absence of O₂. Given that a rising signal is observed after photolysis (t = 0), it is clear that the signal must
result from chemistry between the photolysis products and the precursor and/or the reactor surface. The measured product signals are displayed in the ESI (Fig. S2†). In Fig. 4b, we compare the current high-temperature results to the estimate of Baldwin et al. for the rate coefficient of the phenomenological reaction

\[
\text{CH}_3\text{CH}=\text{CH}=-\text{CH}=\text{CH} + \text{O}_2 \rightarrow \text{CH}_2\text{CH}=\text{CH}=-\text{CH} + \text{HO}_2^-
\]

at 753 K. They estimate their value to be accurate within a factor of 1.4. Their estimate is in reasonable agreement with the current results; there is about a factor of two deviation. The results are also compared with similar measurements for pent-1-en-3-yl and 2-methylbut-3-en-2-yl. The high-temperature results for pent-3-en-2-yl and pent-1-en-3-yl agree within experimental uncertainty, but the results for pent-3-en-2-yl are systematically a bit smaller. 2-Methylbut-3-en-2-yl reacts about 2–3 times faster with O\textsubscript{2} at high temperatures than pent-3-en-2-yl and pent-1-en-3-yl. Fig. 4b also shows that there is a reasonable agreement between our recent pent-1-en-3-yl + O\textsubscript{2} measurements (ref. 6) and the results of Baldwin et al. for that reaction.

3.2 Quantum chemistry

Altogether, three different reaction channels were investigated:

P1: this product channel forms (E/Z)-penta-1,3-diene and hydroperoxyl from the peroxy adducts through a formally direct transition state.

P2: in this product channel, (Z)-pent-3-enyl-2-peroxyl first isomerises to pent-4-en-3-yl-2-peroxol (QOOH) by abstracting an allylic hydrogen from the first carbon. The non-terminal oxygen then forms a bond with the adjacent allylic system, simultaneously breaking the O–O bond, leading to the formation of (2\textsuperscript{R},3\textsuperscript{R}/2\textsuperscript{S},3\textsuperscript{R})-2,3-epoxypent-4-ene and hydroxyl.

P3: here, the terminal oxygens of the peroxy adducts react with the double bond, forming five-membered rings. The O–O bond then breaks (a very exothermic reaction), ultimately leading to the formation of ethanal and (R/S)-1,2-epoxypropane. Preliminary ME simulations revealed this product channel to be kinetically unimportant, so it was left out of the final ME model. The structures of the stationary points of this product channel are displayed in the ESI (Fig. S3†).

We assumed the other product channels to have significantly higher barriers than these three and did not investigate them systematically. The results of our quantum chemistry calculations are reported in Table S3 in the ESI.† An optical symmetry number of two was specified for all species with chiral carbons. The zero-Kelvin reaction enthalpy profile used in the ME simulations is shown in Fig. 7.

In our CASPT2 calculations, a (13,11) active space was used for product channels P1 and P2. This active space consisted of the bonding and anti-bonding C–O and O–O σ-orbitals (4,4), the bonding and anti-bonding C=C π-orbitals (2,2), the non-bonding lone-pair orbitals of the oxygen (4,2), the radical orbital (1,1), which is either on the terminal oxygen or the non-bonding C=C=C orbital, and the bonding and anti-bonding C–H σ-orbitals of the hydrogen that is abstracted from the first and fifth carbons in product channels P1 and P2, respectively. The C–H bond that was chosen was the one closest to the terminal
oxygen. For product channel P3, the same active space was selected, except that the C–H orbitals were omitted and the anti-bonding lone pair orbitals of the oxygens were included. This adds up to an (11,11) active space. For the intermediates and the internal hydrogen abstraction transition structures (ts1Z2a–d), the ROHF-DLPNO-CCSD(T1) and CASPT2 energies are in good agreement, generally within 5 kJ mol$^{-1}$. Single-reference methods appear to be suitable for these species, so we decided to use the ROHF-DLPNO-CCSD(T1) energies for them in the ME simulations. We believe the ROHF-DLPNO-CCSD(T1) method to be more accurate than CASPT2 when non-dynamical correlation is not important. For the other transition structures, there is a clear and systematic disagreement between the ROHF-DLPNO-CCSD(T) and CASPT2 energies, the latter energies being between 10 kJ mol$^{-1}$ and 30 kJ mol$^{-1}$ lower in energy. We have observed the same behaviour for other allylic systems.$^{3,4,6}$ We believe that the large energy differences are a sign that multi-reference effects are important, although the T1 diagnostic does not always reflect this. In the previous studies, we also noticed that the CASPT2 barriers are more consistent with experimental observations. Thus, we used the CASPT2 energies for the other transition structures. The CASPT2 calculations predict the dominant product channel to be the one that produces (E/Z)-penta-1,3-diene and hydroperoxyl (P1). As mentioned in the previous section, we did not find conclusive experimental evidence for this. However, in our previous studies of other allylic systems, we have seen experimental evidence for the diene producing channel.$^{4,6}$ Furthermore, as already discussed, Baker et al. and Baldwin et al. have observed diene formation for C$_4$- and C$_5$-allylic radical + O$_2$ reactions.$^{16,44}$ Therefore, we believe that P1 is the dominant reaction channel for reaction (1) at high temperatures.

### 3.3 Master equation simulations

#### 3.3.1 Parameter optimisation

We used our low-temperature He bath gas data to optimise the modified Arrhenius parameters of the ILT expressions, the
The exponential down model parameters, and the well depths of Int1E and Int1Z. The parameter optimisation was done with the recently implemented trace fitting feature in MESMER. An unweighted trace fit was first performed to obtain weights\(^{27}\) for a weighted trace fit. In the fits, the energy difference between Int1E and Int1Z was fixed to the computed value. The computed energy difference between the two very similar species should be very reliable due to error cancellation. By doing this, we also reduced the number of adjustable parameters in the model. After the weighted trace fit, we used the high-temperature traces to optimise the transition state energies of ts1E1E and ts1ZP1Z. We again fixed the energy difference of the two species to the computed value. After the He bath gas fits, we used our N\(_2\) bath gas data to optimise \(\langle \Delta E \rangle_{\text{down,ref}}^{(N_2)}\). In this optimisation, all other parameters were fixed to the values yielded by the He bath gas fit. Of the fixed parameters, only \(n\) was bath gas-dependent. We did not try to optimise \(n\) separately for N\(_2\) because we did not have enough kinetic data in N\(_2\) bath gas to do so. The parameters yielded by the optimisations are tabulated in Table 1. The \(\langle \Delta E \rangle_{\text{down,ref}}\) values of 164 cm\(^{-1}\) and 330 cm\(^{-1}\) obtained for He and N\(_2\), respectively, are reasonable. The well depth and transition state energy adjustments are less than four kJ mol\(^{-1}\), so well within computational uncertainties. It is harder to assess if the modified Arrhenius parameters are reasonable, but the fall-off curves plotted in Fig. 4 and 5 based on these values seem sensible. Simulated traces produced by the optimised ME model are displayed in Fig. 3. The model predicts that reaction (1) primarily forms (\(E\))-pent-3-enyl-2-peroxyl (70–80\%), Int1E, at low temperatures. Due to its shallower well, (\(Z\))-pent-3-enyl-2-peroxyl (Int1Z) begins to equilibrate with the reactants much earlier than Int1E and the R\(^+\) + O\(_2\) \(\rightleftharpoons\) Int1Z equilibrium has shifted almost completely to the side of the reactants already at the lower temperature end (\(\sim\)330 K) of our equilibration measurements. Thus, our measurements between 326 K and 376 K mainly monitor the R\(^+\) + O\(_2\) \(\rightleftharpoons\) Int1E equilibrium reaction and the average forward and reverse rate coefficients obtained from the double exponential fits mostly describe this reaction. In Fig. 6, we plot the experimental equilibrium constant together with the R\(^+\) + O\(_2\) \(\rightleftharpoons\) Int1E and

<table>
<thead>
<tr>
<th>Optimised parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(A_E)</td>
<td>(3.03 \times 10^{-12}) cm(^3) s(^{-1})</td>
</tr>
<tr>
<td>(A_Z)</td>
<td>(1.59 \times 10^{-12}) cm(^3) s(^{-1})</td>
</tr>
<tr>
<td>(m_E)</td>
<td>(-1.38)</td>
</tr>
<tr>
<td>(m_Z)</td>
<td>(-0.539)</td>
</tr>
<tr>
<td>(\langle \Delta E \rangle_{\text{down,ref}}^{(He)})</td>
<td>164 cm(^{-1})</td>
</tr>
<tr>
<td>(\langle \Delta E \rangle_{\text{down,ref}}^{(N_2)})</td>
<td>330 cm(^{-1})</td>
</tr>
<tr>
<td>(n)</td>
<td>0.362</td>
</tr>
<tr>
<td>Int1E</td>
<td>(-83.08) kJ mol(^{-1})</td>
</tr>
<tr>
<td>Int1Z</td>
<td>(-77.35) kJ mol(^{-1})</td>
</tr>
<tr>
<td>ts1E1E</td>
<td>13.42 kJ mol(^{-1})</td>
</tr>
<tr>
<td>ts1ZP1Z</td>
<td>17.57 kJ mol(^{-1})</td>
</tr>
</tbody>
</table>
R’ + O₂ ⇋ Int1Z equilibrium constants computed with our ME model, and indeed, one observes that the experimental equilibrium constant is for the R’ + O₂ ⇋ Int1E reaction. From this point onward, all simulations were run in N₂ bath gas with the values reported in Table 1.

3.3.2 High-temperature mechanism. The optimised ME model was able to reproduce the experimental observation of three distinct temperature regimes. At low temperatures, the reaction proceeds by a barrierless recombination reaction to form peroxyl adducts. The recombination rate coefficient is pressure-dependent and has negative temperature dependence. As temperature is increased, there is significant equilibration between the reactants and the peroxyl adducts, and the pent-3-en-2-yl traces are multi-exponential. As the temperature is further increased, “good” rate coefficients are again observed. The phenomenological high-temperature rate coefficient is pressure independent and has positive temperature dependence. We noticed that it is related to the least negative CSE by the simple relation \( k_{ph} = -\lambda_1/[O₂] \). In Fig. 8, we plot the CSEs (\( λ_1, λ_2, λ_3, \) and \( λ_4 \)) as a function of temperature, pressure and [O₂]. The used oxygen concentration, \([O₂] = 10^{15} \text{ cm}^{-3}\), is unphysical in the low-pressure (\( p = 10^{-8} \text{ bar} \)) simulations, but it was used so that a reaction would occur at a reasonable timescale. The unphysical [O₂] does not invalidate the results of the simulations—it is simply there to turn a bimolecular rate coefficient into a pseudo-first-order rate coefficient. Several observations can be made from the plots.

(1) At low and high temperatures, the bimolecular rate coefficient of reaction (1) is given by the relations \( k_{rec} = -λ_4/[O₂] \) and \( k_{ph} = -λ_1/[O₂] \), respectively. There is a region of avoided crossing between the two temperature regions in which the rate coefficient “jumps” from eigencurve 4 to eigencurve 1. It is in this temperature range that multi-exponential radical traces and equilibration between reactants and peroxyl adducts are observed. The width of the transition range is pressure-dependent. At 100 bar and \([O₂] = 10^{15} \text{ cm}^{-3}\), it spans from 350 K to 450 K. As pressure is reduced, the temperature range gets narrower, eventually disappearing at \( 10^{-8} \text{ bar} \), where there is an instantaneous jump from eigencurve 4 to eigencurve 1.

(2) The location of the transition range depends on [O₂], as it should. At 1 bar and \([O₂] = 10^{10} \text{ cm}^{-3}\), it is located between 250 K and 350 K, whereas at 1 bar and \([O₂] = 10^{20} \text{ cm}^{-3}\), it is located between 700 K and 800 K.

(3) The total [O₂]-independence of \( λ_3 \) indicates that it should be associated with well Int2. We also noticed that the total loss rate from this well was equal to \( λ_3 \).

(4) At high temperatures, \( λ_4 \) is pressure independent for all practical purposes. Based on this, one would assume that the branching ratios of the different product channels at high temperatures are also pressure independent, and indeed, they were found to be virtually identical at \( 10^{-8} \text{ bar} \) and 100 bar.

(5) At high temperatures, \( λ_2 \) and \( λ_4 \) describe the equilibration between R, Int1E, and Int1Z. The least negative CSE, \( λ_1 \), describes the loss from the “combined R, Int1E, and Int1Z well”. The reactions between R, Int1E, and Int1Z happen very fast (\( λ_2 \) and \( λ_4 \) are orders of magnitude larger than \( λ_1 \) under realistic pressures and O₂ concentrations). Thus, R, Int1E, and Int1Z reach chemical equilibrium almost instantly after the reaction is initiated and the equilibrium is maintained whilst \( λ_1 \) slowly depletes their populations.
Because chemical equilibrium between the reactants and peroxyl adducts is established very quickly at high temperatures and favours the reactants, the pre-equilibrium approximation can be used to derive a high-temperature phenomenological rate coefficient for reaction (1). An approximate phenomenological description of the reaction system is given by the reactions.
The “WS” in the rate coefficients stands for well-skipping. After writing down the rate laws, using the pre-equilibrium approximation, and doing some algebra, an approximate phenomenological rate coefficient is obtained for reaction (1):

\[
k_{\text{ph}} = k_{WSP1E} + k_{WSP1Z} + k_{WSP2RR} + k_{WSP2SR} + k_{\text{Int}2} + \frac{k_{1Z2} k_{1ZP1Z} k_{1ZP2RR} k_{1ZP2SR}}{k_{1ZP2RS} k_{2ZP1Z} k_{1ZP2RR} k_{1ZP2SR}} \frac{k_{1ZP1Z} k_{1ZP2RR} k_{1ZP2SR}}{k_{1ZP2RS} k_{2ZP1Z} k_{1ZP2RR} k_{1ZP2SR}}
\]

We tested the validity of this expression by comparing it with \(-\dot{\lambda}_v/O_2\). The elementary rate coefficients were obtained from Bartis–Widom analysis. The comparison is shown in Fig. 9. As one can see, the two expressions are virtually identical as pre-equilibrium conditions begin to apply at around 450 K. The phenomenological rate coefficient is pressure independent, even though the Bartis–Widom rate coefficients from which it is calculated are not (also shown in Fig. 9). Surprisingly, eqn (3) seems to be valid even at 1500 K, long after CSEs and IEREs have begun to converge. Therefore, we are inclined to believe that the Bartis–Widom rate coefficients in eqn (3) are valid throughout the investigated temperature range (200–1500 K). A possible reason why the Bartis–Widom rate coefficients are valid is that CSEs and IEREs do not overlap until around 1500 K (see Fig. 8), even though the separation between the smallest CSE and largest
IERE is less than an order of magnitude at temperatures above 600–850 K (depending on pressure).

In the high-temperature regime, reaction (1) can form products through well-skipping (first row in eqn (3)) or through a sequential mechanism where first the peroxyl intermediates are formed and then decompose (the second and third rows in eqn (3)). At 0.01 bar, the products are almost completely formed by the well-skipping reactions, even at 400 K. As the pressure is increased, the sequential mechanism becomes more important. At 100 bar and 850 K, half of the products are still formed through the sequential mechanism. The emergence of a pressure
independent rate coefficient at high temperatures is an interesting phenomenon. The reasons for this have been discussed by Miller and Klippenstein for the ethyl + O₂ reaction. In their study, they also discovered that the least negative eigenvalue is pressure-independent at high temperature. We believe that the same arguments can be used to explain the pressure-independence of the high-temperature rate coefficient in the current study. At high temperatures, many of the peroxyl radicals that are formed by the recombination reaction will have sufficient energy to well-skip directly to bimolecular products. Increasing the pressure will decrease well-skipping, as Fig. 9b demonstrates, but there will be a compensating increase in the role of the sequential mechanism. Above 400 K,

![Boltzmann grain populations for Int1E](image)

**Fig. 10** (a) The Boltzmann populations of the energy grains of Int1E as a function of temperature. (b) Average energies transferred as a function of energy at different temperatures.
a significant portion of the Boltzmann population of the peroxyl adducts will reside at energy levels that are above the energies of the formally direct transition states (see Fig. 10a). Peroxyl adducts at these levels will be depleted by chemical reactions, but collisions continually repopulate the energy levels as they try to establish thermal equilibrium. So collisions both inhibit and promote reactivity by preventing well-skipping and repopulating reactive states. Fig. 10 also shows how the magnitude of the average energy transferred in activated collisions grows faster with temperature than in deactivating collisions. This helps to repopulate the reactive states and hinders stabilisation to unreactive states.

To better understand the pressure-independence of the high-temperature rate coefficient, we investigated how the populations of the energy grains of Int1E evolve in time. These results are presented in Fig. 11 and 12. The shown
populations are absolute (the initial condition in the simulations was that the population of the reactants was unity at $t = 0$). The results are consistent with the arguments we make in the previous paragraph. Three interesting observations can be made from the figures:

1. At 100 bar, as soon as Int1E is formed, the energy grain populations become thermalised. At $10^{-8}$ bar, Int1E grain populations eventually become thermalised at 200 K and 300 K. At higher temperatures and at $10^{-8}$ bar, there is not enough time for the Int1E energy grains to become thermalised.

2. Above 400 K, the populations of the energy grains above the reaction threshold are virtually identical at $10^{-8}$ bar and 100 bar.

3. At $10^{-8}$ bar, there is a quasi-stationary population of the energy grains above 0 kJ mol$^{-1}$ that is maintained as long as there are reactants left (0–0.1 s). At low

---

**Fig. 12** The time-dependent energy grain populations of Int1E at $10^{-8}$ bar and $10^2$ bar between 500 K and 700 K. The horizontal lines show where the relative energies of the reactants and ts1EP1E are.
temperatures, the population in the reactive grains eventually gets stabilised to unreactive grains. As temperature is increased, lower and lower amounts of the population ever get stabilised to the unreactive grains.

3.3.3 Parameterisation of the results. Once pre-equilibrium conditions begin to apply, one does not need to actually worry if the Bartis–Widom rate coefficients are valid or not. Nor is it necessary to provide Bartis–Widom rate coefficients for all the kinetically important elementary reactions. Approximate, channel-specific phenomenological rate coefficients can be obtained simply by multiplying the least negative eigenvalue with the branching ratio of the reaction channel and dividing the value by $[O_2]$. The branching ratios are obtained by simulating reaction (1) long enough that all the population is in the sinks. Modified Arrhenius fits can then be performed on these approximate rate coefficients to provide the ME results in a form that is usable for combustion modelling. The results of this procedure in the current work are given in Table S4 in the ESI.† These results show that the P2 product channel is not very important. The advantages of this scheme are obvious; we provide the results of our simulations with four modified Arrhenius expressions. The current model outputs 28 pressure-dependent Bartis–Widom rate coefficients, so reducing this to four pressure-independent Arrhenius expressions without a great loss of accuracy is very helpful. Even the approximate reaction mechanism from which eqn (3) was derived contained 14 Bartis–Widom rate coefficients. A drawback of the scheme is that modellers using the results must know if pre-equilibrium conditions apply in their specific applications. For the current system at realistic $O_2$ concentrations, the condition is fulfilled at least at temperatures above 700 K. We provide the MESMER input file of our ME model in the ESI† (www.mesmerInput.xml).

4 Conclusions

We have investigated the kinetics of the reaction between $(E/Z)$-pent-3-en-2-yl (CH$_3$–CH=CH=CH–CH$_3$) and molecular oxygen using both experimental and computational methods. The experiments were performed with laser-photolysis–photoionization mass spectrometry. The computational work consisted of quantum chemical calculations and master equation simulations. At low temperatures (238–300 K), barrierless $(E/Z)$-pent-3-en-2-yl + O$_2$ recombination reactions form peroxyl adducts. These reactions are pressure-dependent and exhibit negative temperature dependence. As the temperature is increased above room temperature, the peroxyl adducts begin to equilibrate with the reactants and multi-exponential decays are observed. At around 400 K, the equilibrium is already fully on the side of the reactants with the employed oxygen concentrations. Above 500 K, a phenomenological reaction is observed. The rate coefficient for this reaction changes from $4.30 \times 10^{-16}$ cm$^3$ s$^{-1}$ at 551 K to $22.1 \times 10^{-16}$ cm$^3$ s$^{-1}$ at 752 K. Such a fast reaction at these temperatures is most likely explained by low-barrier reaction channels that lead to the formation of $(E/Z)$-penta-1,3-diene and hydroperoxyl. The computed barriers for these reactions are only 13–18 kJ mol$^{-1}$ above the energy of the reactants. The high-temperature phenomenological $(E/Z)$-pent-3-en-2-yl + O$_2$ rate coefficient has positive temperature dependence and is pressure-independent. A
A master equation model was constructed to simulate the studied reaction over a wide range of conditions. Trace fitting with MESMER was used for parameter optimisation. The master equation model confirms and explains the experimental finding that a pressure-independent phenomenological rate coefficient emerges at higher temperatures. Modified Arrhenius expressions are given for the most important product channels to facilitate the use of our results in auto-ignition and combustion modelling.

Author contributions

The experiments were conceived of by Arkke Eskola. The kinetic measurements were performed primarily by László Valkai, Satya Joshi, and Timo Pekkanen, with some assistance from Raimo Timonen. The quantum chemical calculations and master equation simulations were performed by Timo Pekkanen with the help of György Lendvay. Petri Heinonen synthesised the radical precursor. Timo Pekkanen primarily wrote the manuscript. The manuscript was substantially amended by Arkke Eskola and György Lendvay. The other authors reviewed and commented the manuscript.

Conflicts of interest

There are no conflicts to declare.

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Notes and references


