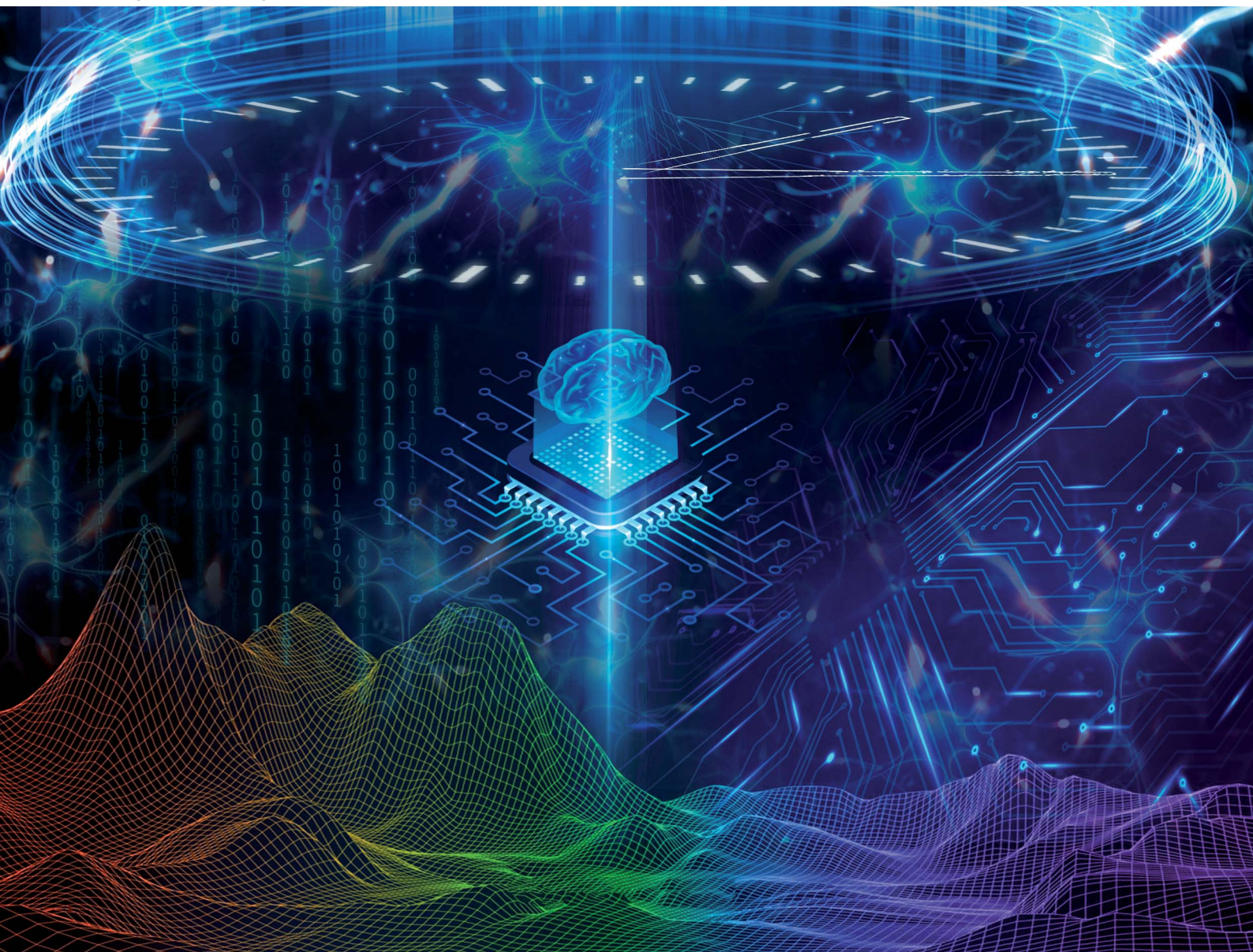


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Hyperconverged autonomous organic reaction infrastructure (HAORI) driven by SpecSNN, for low dielectric constant polymer research†

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We developed a hyper-converged autonomous organic reaction infrastructure (HAORI) that integrates reactions, characterization, and closed-loop optimization, driven by the Spectrum Spiking Neural Network (SpecSNN) architecture. Most of the previous data-driven autonomous lab platforms in organic reactions lack a time-resolved algorithm, which creates a gap with the optimization progress in a non-negligible time. Driven by SpecSNN, HAORI receives *in situ* spectroscopic feedback from the automatic synthesis unit and outputs the alternated reaction conditions considering time differences. Compared with the previous autonomous lab systems and architecture, HAORI can achieve higher efficiency and accuracy. We showed a working example in HAORI for a relative optimum reaction to synthesize a low dielectric constant polymer, producing a polymerized product with a DC (ϵ) from 1.32 to 2.56 and $\epsilon_0 = 2.46$, which is also double validated using *ab initio* calculations. We believe that the SpecSNN-HAORI could be one of the next-generation autonomous lab architectures.

efficiency. The barriers mainly come from the complications of chemical experiments, diversity, and time consumption. Most well-developed deep learning architectures could only handle a minimal amount of information, both for properties and reactions.

In chemical experiments, most of the reaction optimization algorithm are per-experiment based, for which they treat an experiment as the minimum analysis unit. This trade-off is acceptable in ultra-fast reactions such as the synthesis of perovskite quantum dots^{14–17} but would significantly affect the efficiency of relatively long experiments. All chemical reactions should be regarded as time-dependent procedures; however, most reaction optimization algorithms reported^{18,19} ignored the time factor. For instance, some continuous flow optimization systems²⁰ aim to receive spectroscopic feedback and dynamically alter the reaction conditions. However, during these minutes, massive variations may happen in the reaction mixture, for which the outdated optimizing strategy may not be suitable. In solution, a considerable time gap exists between the extracted and current mixture during this cycle. The dynamic control should not be applied to the condition where the sample represents, but when analysis results come out instead. Previous studies mainly focussed on a few specific parts of the whole workflow but could not provide a thoughtful solution for the entire task. Furthermore, their approaches to particular parts can further be optimized.

Two main requirements are essential to construct a real-time closed-loop reaction system: (1) suitable characterization techniques and (2) a well-tested feedback control algorithm. Previous studies have applied various optical spectroscopies, and the proportion parameter from the spectrum to product quality can be well adjusted.^{21–23} Aiming to determine the properties of products from spectroscopic feedback, implementing in-line optical spectroscopy such as Fourier transform infrared (FT-IR), ultraviolet-visible (UV-Vis), and Raman spectroscopies is practical. They can be used as a structural indicator for bonds and groups. By applying well-researched deep learning feature extraction models, both dominance and

Introduction

The development of AI in chemistry has been remarkable in the past decade, including property prediction,^{1–3} synthesis routine planning,^{4–6} and reaction optimization.^{7–13} Together with these implementations, lots of assistance in a throughout developing routine, from structure design to compound synthesis and property characterization. However, this workflow has not been widely accepted by researchers worldwide, as there are still plenty of problems that significantly affect the discovery

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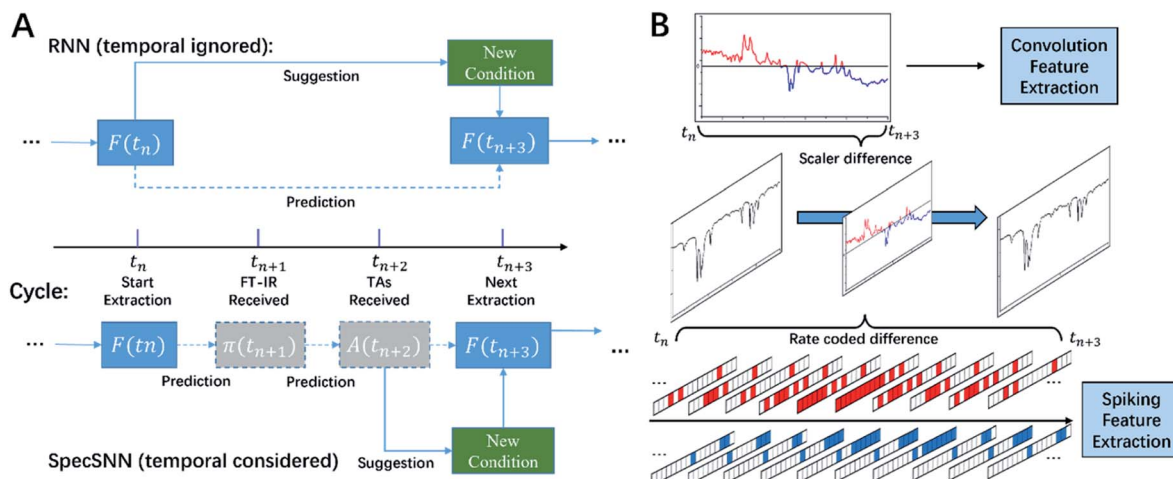


Fig. 2 Basic comparison between CNN-RNN and SpecSNN in two aspects. (A) The comparison between the non-time dependent RNN and SpecSNN in terms of training details. Spiking coding authentically covers the time gap between two characterization time points, supporting recurrent state prediction to secure the accuracy. All the results must be received at t_{n+1} and t_{n+2} corresponding to the reactant at t_n , which caused a time gap between the tested condition and the real condition which needs to be optimized. (B) The transfer methodology from the spectrum to time-dependent 1D-spiking feature in comparison to the traditional CNN. Two feature maps, recoding positive and negative spiking, respectively, are used. The segmentation precision can be adjusted by changing the trigger threshold of spectrum intensity and neuron width in the spectrum.

stability. Therefore, the temporal gap must be narrowed (oversampling) so that rate coding can be used to quantify the intensity change between each testing time point. After transforming from a one-dimensional absolute value coded spectrum into a spiking rate coded sequence, an event-based spiking convolutional network (SCNN) is implemented to extract features from transferred data. Inspired by the spiking convolution operation proposed by Cao,²⁶ we developed a similar method to code and trained our scalar data in a spiking way.

The structure of our optimizer, SpecSNN, is shown in Fig. 3. It receives transferred spiking coded signals from the FT-IR and outputs the quality prediction of target samples and the next condition alternation path. As illustrated in Fig. 2B, the input spiking sequence $s(n)$ will first be separated into $s(l_x, t_n)$ to get an output tensor shaped in (l, T_{\max}, P) . In this tensor, l is the spatial segment of the spectrum which depends on the spectrum resolution R_s , T_{\max} is the temporal segment based on a pre-defined time resolution r , and P is the activation trigger (see Fig. 3A and ESI S2† for details).

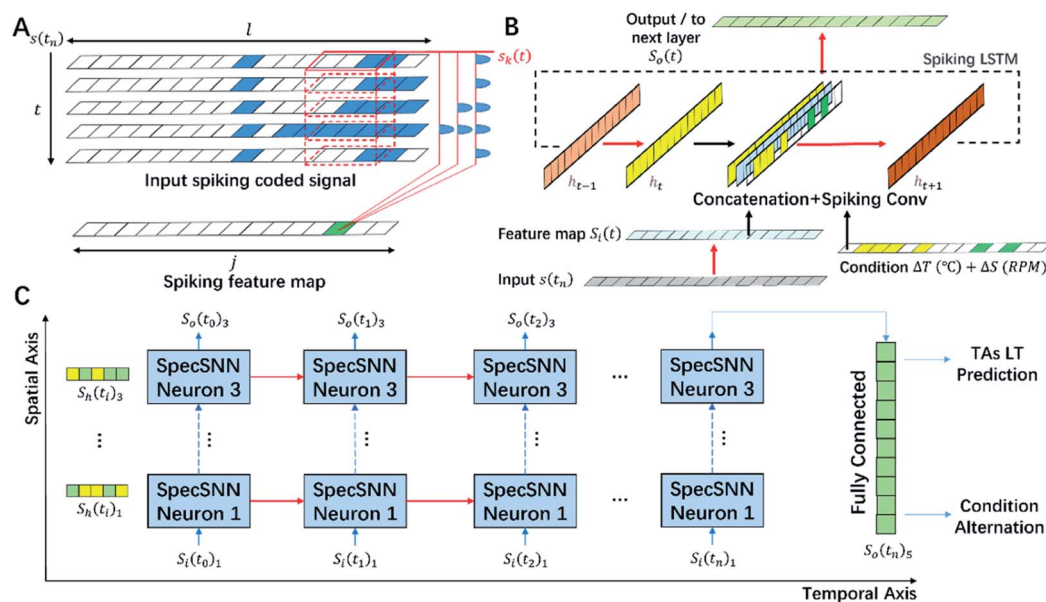


Fig. 3 Structure of SpecSNN: the SNN based experiment optimizer. (A) The progress of transferring spectrum data into pseudo-event-based rate coding feature maps. (B) The brief structure of a single SpecSNN cell and its functionality in the expanded view over time. (C) The structure of a 3-layer deep SpecSNN neural network.



The $s(\mathbf{l}_x, \mathbf{t}_n)$ with the shape of $(\mathbf{l}, T_{\max}, P)$ will then be convoluted with a temporal-based convolutional kernel to generate a spiking feature map. Considering an initial 1D spiking input signal $S(\mathbf{t}_n)$, for one segment on \mathbf{l} , all the spikes will form a spike series $s_k(t)$ (k represents the position in the spectrum). For all spike trains to be covered inside one 1D convolutional kernel, we use the model of spike layer error reassignment (SLAYER)²⁷ to handle the generation of the potential of that neuron. For this model, all spike trains $s_k(t)$ transmitted at t will be convoluted by a spike response kernel $\sigma(t)$. With this progress, a spike response signal of the SRM neuron will be generated as $a(t) = \sigma(t)s_k(t)$, after which an input feature map $S_i(t)$ with a length of j will form.

Like most deep neural network structures, to further extract features on different scales from existing features, we implement similar multilayer structures to expand the depth of the neural network to 5 layers. This structure is inspired by ConvLSTM²⁸ and SCRNN,²⁵ where the core structure of a single neuron and the whole recurrent framework is presented in Fig. 3C. Specifically, the temporal-based spiking convolution will be applied to both the input-internal stage and the temporal state update stage (see Fig. 3B black arrows). It will generate an input state $S_i(t)$ and a hidden state h_t , respectively. Finally, three feature maps in Fig. 3B are concatenated to form a single map and further used to generate two output states, current state output $S_o(t)$ and hidden state h_{t+1} by the spiking convolution part of the neuron. h_{t+1} will be directly used as an input for the same neuron at the next time point of the spiking LSTM part, while the $S_o(t)$ is functional as a further input to the next layer in the deep SNN structure, which is illustrated in Fig. 3C. The details of input pre-processing, the network layer structure, and calculation details are given in ESI S2.†

Experiments

To test the performance of SpecSNN, a trial optimization task was designed to discover new low DC and luminescent materials with a specific wavelength. Furthermore, we have also implemented the most well-researched neural network, CNN-RNN,²⁹ to compare the effectiveness during the *in situ* optimization. As stated above, unlike entirely data driven conditions, most experiment operations require a period to take effect. In detail, FTIR spectra need 1–2 minutes from sample injection to result collection, and it will be 3–7 minutes for TA spectra. This delay makes the time-dependent optimization module vital in our scenario, which is further discussed in ESI S1.† Back to the *in situ* optimization, the HAORI will run independently under various conditions for 24 hours to generate an initial map of this set of experiments. Except for this, no prior knowledge is provided to both algorithms. They are currently being tested on the identical product tree with basic BFS search, while they aim to alter reaction conditions to achieve better efficiency continuously. For all experiments in this tree, adjustable conditions are limited to temperature and the flow rate due to the feasibility of experiments and the comparison accuracy between algorithms.

For one experiment, excluding two benchmark trials initially, a maximum search number of 18 is also applied due to

the same reason. Testing is conducted every 10 minutes during the reaction by extraction from tubes. Finally, the system supports up to three channels simultaneously among all seven due to the number of pumps. The alternation procedure will be triggered every 10 minutes to match the characterization period. The other traditional CNN-RNN algorithm will modify the reaction conditions when two *in situ* characterization results are available without considering the time factor. The maximum reaction time is set to be 3 hours. However, it could be terminated in advance if the algorithms think that the optimal has been reached.

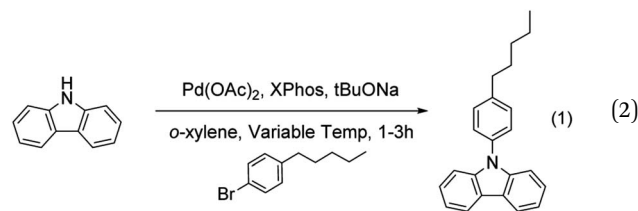
For the measurement of the optimization objective during the reaction, the dielectric constant could be indirectly derived using the transient absorption lifetime, which can be calculated from the Fermi Golden Rule.³⁰ Via the wave functions defined by Dexter,³¹ where i is the initial state and f is the final state, with the static dielectric constant ϵ , the lifetime can be expressed as

$$\tau_{i \rightarrow f}^{-1} = \frac{16\pi^2}{3} \frac{ne^2}{h^2 m^2 c^3} E |\langle i|r|f \rangle|^2 \propto \frac{n\omega_{if}}{c^3} \propto \sqrt{\epsilon}\omega_{if} \quad (1)$$

Thus, since the absorption peak, *i.e.*, ω_{if} , did not change for the samples measured, one can compare the dielectric constant directly using the lifetime. The longer the lifetime, the lower the dielectric constant.

Discussion

As a result, all the reactions could successfully synthesize the desired monomer of the polymer. We chose to present the key *in situ* characterization results of the best-optimized reaction (the structure 6 in Fig. 5A) using SpecSNN in Fig. 4A and B. The formula for this specific reaction is shown below. It can be clearly seen that the most noticeable change during the reaction is the formation of C–N stretches, which is also the main spiking weight to be triggered in the SpecSNN. It successfully tracked the FT-IR spectrum change in the fingerprint region and thus successfully optimized the reaction conditions to boost the speed eqn (1).



Meanwhile, the TAS lifetime collected also increased rapidly, which indicates a drop in DC using eqn (1). To examine the performance of the final polymer, we manually treated and purified the product above and polymerized it to get the final polymer, which can be viewed in ESI S3.† We chose to conduct it manually because the polymerization is difficult to conduct automatically because of its strong acidity condition, complicated pre-processing requirements, and long reaction time.

The final product is spin-coated and tested for the refractive index using an ellipsometer with a thickness of 200 μm . The



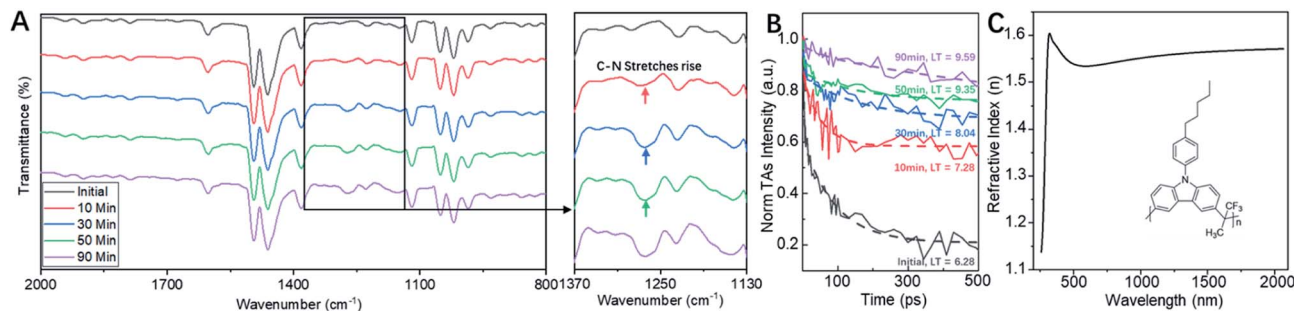


Fig. 4 The illustration of an experiment to be optimized and the *in situ* testing results. Here, we present the final optimized reaction details from SpecSNN. (A) and (B) share the same legend. (A) The *in situ* FTIR testing results of the final experiment, from start to 90 min. The experiment is nearly done at 50 min. Note that the spectrum increases significantly at around 1250 cm^{-1} . These spectra have been smoothed for better clarity. (B) The fitted TAS lifetime derived from normalized TAS intensity, which significantly increases the TAS lifetime and dielectric constant ϵ . (C) The refractive index tested after polymerization. According to $n = \sqrt{\epsilon}$, the ϵ is about 1.32–2.56 and the $\epsilon_0 = 2.46$, which are relatively low compared with PVDF in the terahertz area.

dielectric constant ϵ could then be calculated according to the formula $n = \sqrt{\epsilon}$; the dielectric constant ϵ is about 1.32–2.56 and the $\epsilon_0 = 2.46$, which is relatively low and has high potential for

use in wireless communication. Compared with PVDF, the most widely discussed polymer used for wireless connections in the 3G/4G/5G era, it has an apparent lower DC in the terahertz area,

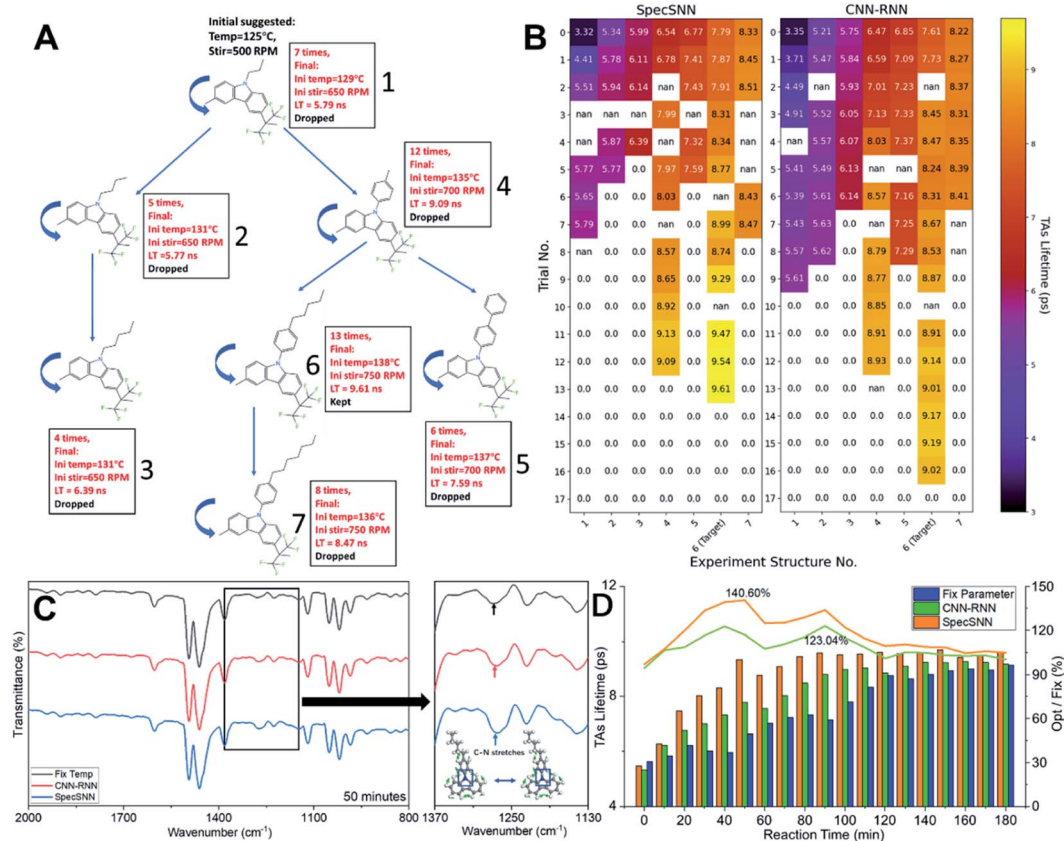


Fig. 5 The comparison of the two optimization pathways and results obtained using SpecSNN and CNN–RNN. (A) The optimization pathway suggested by the random forest algorithm and a brief final optimized condition and repetition times by SpecSNN are also listed. (B) The optimization results in each trial of the experiment handled by SpecSNN and CNN–RNN, respectively. Note that a 0 value indicates that the experiment has converged, and the corresponding trial has not been conducted. The NaN value means that the experiment has been dropped before it reaches a steady state (complete), mostly because the TAS results showed that the sample is coagulated. (C) The FT-IR spectra comparison at 50 minutes of the final optimization round among the SpecSNN, CNN–RNN and benchmark ($T = 138\text{ }^{\circ}\text{C}$ constant). (D) The comparison of *in situ* TAS lifetime changes in the final optimized reaction, structure 6 among the SpecSNN, CNN–RNN and fix-parameter ($T = 138\text{ }^{\circ}\text{C}$ constant). Both the lifetime and the ratio between the applied optimization algorithm and none (Opt/Fix) are plotted. Note that the optimization of SpecSNN and CNN–RNN was terminated at 100 min and 160 min respectively. The later TAS results are manually overridden to test for comparison.



which is probably the working frequency for 6G. The refractive index for PVDF is nearly 2 for a 200 μm film,³² while for our synthesized polymer, it should be much lower considering expanding the wavelength area to the terahertz area near ϵ_0 as shown in Fig. 4D. A further theoretical calculation has been performed and is illustrated in Fig. S6,[†] supporting the finding that our synthesized polymer has relatively low DC.

The optimization results clearly show that dynamically altering the reaction conditions guided by algorithms during the organic reaction could improve both the efficiency and quality of the product. Fig. 5C illustrates that reaction efficiency has been improved as the C–N stretch peak grows faster. In a comparison between optimization models, SpecSNN shows relatively better performance. Furthermore, the TAS lifetime trend in Fig. 5B reveals that both the algorithms could automatically learn from previous experiments and improve product quality. This is achieved by applying dynamic reaction conditions, which pushed the reaction optimization to a smart and on-demand era. Almost all experimentally reported conditions are discrete or even static, as only the initial condition would be considered to report and change and then keep it invariant during the whole process. Though the benefits of applying dynamically controlled reactions have been discussed for a long period,³³ most proposals could not be completed because of two problems. First, there is a lack of an instrument to control the reaction conditions automatically. Second, it is difficult for human researchers to keep monitoring the reaction at high throughput, which indicates that human optimizers are of low efficiency. These two problems listed above are both solved using SpecSNN we proposed, as it could automatically conduct experiments and automatically suggest condition optimization during the experiments. It would improve if a precise *in situ* adjustment could be applied to all experiments, and even better, the best condition can be found automatically by the neural network.

We have also compared the efficiency between the two algorithms listed in Fig. 5, which revealed significant differences in performance and efficiency. As a result, SpecSNN performed better for nearly all experiment structures in both aspects, as it could achieve better product quality in fewer trials. In detail, as shown in Fig. 5D, SpecSNN has evident benefits, especially at the beginning of the reaction (<60 min). Considering that the reaction with SpecSNN reaches a relatively steady state after 90 minutes, compared with CNN–RNN, the 30 minute speed advantage boosts the efficiency of this reaction by 25%. SpecSNN can beat its opponent by 5–7% in the product quality. Furthermore, as shown in Fig. 5B, the CNN–RNN spent 11 more trials than SpecSNN, which only performed 60 times of reaction to reach relative optimal. All the comparisons above proved that SpecSNN has a faster optimization speed and higher accuracy in our proposed task.

In principle, many aspects contribute to the final improvement. In our view, the main reason is the non-negligible temporal influence during the experiment. As stated above, most of the *in situ* characterization techniques cannot be completed inside the reaction tunnel. Instead, it requires the sample to be filled in

a testing container. Moreover, the automatic testing procedure of TAS takes several minutes. Considering that it is impossible to remain in a reaction environment outside the tunnel, the characterization result does not represent the state of the current time but the state of extraction time instead. Therefore, it is essential to handle this time gap between states and decide the condition alternation. Otherwise, there will be a significant bias between the optimization strategy and real conditions, which sets up a theoretical upper bound for non-time considered models. This is why the time aspect in SpecSNN takes full advantage.

Another point is the training data volume. The training of CNN–RNN requires a large data volume of spectra with distinguishing features, which is not suitable to handle the minor difference between the *in situ* testing results. In solution, together with real-time condition input, the temporal segmentation of SpecSNN further increases the data volume in a surrogate approach. Moreover, spiking-based learning would be more efficient in catching slight differences over time. Together, these two reasons secure a better learning outcome for SpecSNN.

Conclusions

To conclude, this work proposed a material synthesis optimizer with an SNN based algorithm (SpecSNN) and autonomous experiment system and used this system to successfully optimize the synthesis of a low DC polymer with alternation of temperature during the reaction. Compared with static temperature or CNN–RNN-based optimizers, our SpecSNN surpassed them mostly in reaction efficiency by shortening the reaction time by at least 25%. This high performance is mainly because of temporal coded spikes, which ensure a real-time-based optimization suitable for inferring the current state when the condition needs to be dynamically controlled. Many targeted pre-processing methods such as conditional normalization, interpolation, and high sensitivity have been applied to the input. Though limited by the *in situ* characterization speed, only 10 min per sample of the testing rate can be achieved. For now, this algorithm still performed well, which revealed the high potential of SpecSNN in small sample temporal-related optimization tasks. It could be foreseen that the time gap between the tested state and the current state will still be a significant problem to solve in the future of *in situ* reaction optimization. By conducting a series of experiments to find a low DC polymer and optimize its synthesis for better efficiency, HAORI shows its value in new material discovery and potential for being industrialized in chemical engineering.

Data availability

All the SpecSNN model related code can be found at <https://github.com/Spider-scnu/Spiking-ConvLSTM>.

Conflicts of interest

There are no conflicts to declare.



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Notes and references

- 1 A. Mishra, S. Satsangi, A. C. Rajan, H. Mizuseki, K.-R. Lee and A. K. Singh, *J. Phys. Chem. Lett.*, 2019, **10**, 780–785.
- 2 J. Lee, A. Seko, K. Shitara, K. Nakayama and I. Tanaka, *Phys. Rev. B*, 2016, **93**, 115104.
- 3 S. Wu, Y. Kondo, M.-a. Kakimoto, B. Yang, H. Yamada, I. Kuwajima, G. Lambard, K. Hongo, Y. Xu and J. Shiomi, *npj Comput. Mater.*, 2019, **5**, 1–11.
- 4 B. A. Grzybowski, S. Szymkuć, E. P. Gajewska, K. Molga, P. Dittwald, A. Wołos and T. Klucznik, *Chem*, 2018, **4**, 390–398.
- 5 T. Klucznik, B. Mikulak-Klucznik, M. P. McCormack, H. Lima, S. Szymkuć, M. Bhowmick, K. Molga, Y. Zhou, L. Rickershauser and E. P. Gajewska, *Chem*, 2018, **4**, 522–532.
- 6 B. Mikulak-Klucznik, P. Gołębiowska, A. A. Bayly, O. Popik, T. Klucznik, S. Szymkuć, E. P. Gajewska, P. Dittwald, O. Staszewska-Krajewska, W. Beker, T. Badowski, K. A. Scheidt, K. Molga, J. Mlynarski, M. Mrksich and B. A. Grzybowski, *Nature*, 2020, **588**, 83–88.
- 7 J. Li, J. Li, R. Liu, Y. Tu, Y. Li, J. Cheng, T. He and X. Zhu, *Nat. Commun.*, 2020, **11**, 1–10.
- 8 B. J. Reizman, Y.-M. Wang, S. L. Buchwald and K. F. Jensen, *React. Chem. Eng.*, 2016, **1**, 658–666.
- 9 C. W. Coley, D. A. Thomas, J. A. M. Lummiss, J. N. Jaworski, C. P. Breen, V. Schultz, T. Hart, J. S. Fishman, L. Rogers, H. Gao, R. W. Hicklin, P. P. Plehiers, J. Byington, J. S. Piotti, W. H. Green, A. J. Hart, T. F. Jamison and K. F. Jensen, *Science*, 2019, **365**, eaax1566.
- 10 B. J. Shields, J. Stevens, J. Li, M. Parasram, F. Damani, J. I. M. Alvarado, J. M. Janey, R. P. Adams and A. G. Doyle, *Nature*, 2021, **590**, 89–96.
- 11 D. Angelone, A. J. Hammer, S. Rohrbach, S. Krambeck, J. M. Granda, J. Wolf, S. Zalesskiy, G. Chisholm and L. Cronin, *Nat. Chem.*, 2021, **13**, 63–69.
- 12 C. W. Coley, N. S. Eyke and K. F. Jensen, *Angew. Chem., Int. Ed.*, 2020, **59**, 23414–23436.
- 13 W. Gao, P. Raghavan and C. W. Coley, *Nat. Commun.*, 2022, **13**, 1–4.
- 14 R. W. Epps, M. S. Bowen, A. A. Volk, K. Abdel-Latif, S. Han, K. G. Reyes, A. Amassian and M. Abolhasani, *Adv. Mater.*, 2020, **32**, 2001626.
- 15 K. Abdel-Latif, R. W. Epps, F. Bateni, S. Han, K. G. Reyes and M. Abolhasani, *Adv. Intell. Syst.*, 2021, **3**, 2000245.
- 16 J. Li, Y. Tu, R. Liu, Y. Lu and X. Zhu, *Adv. Sci.*, 2020, **7**, 1901957.
- 17 J. Li, M. Hu, Z. Wang, Y. Lu, K. Wang and X. Zhu, *J. Mater. Chem. A*, 2019, **7**, 27241–27246.
- 18 D. Reker, E. A. Hoyt, G. J. L. Bernardes and T. Rodrigues, *Cell Rep. Phys. Sci.*, 2020, **1**, 100247.
- 19 A. D. Clayton, J. A. Manson, C. J. Taylor, T. W. Chamberlain, B. A. Taylor, G. Clemens and R. A. Bourne, *React. Chem. Eng.*, 2019, **4**, 1545–1554.
- 20 M. Rueping, T. Bootwicha and E. Sugiono, *Beilstein J. Org. Chem.*, 2012, **8**, 300–307.
- 21 A. Rao, M. Schoenenberger, E. Gnecco, T. Glatzel, E. Meyer, D. Brändlin and L. Scandella, *J. Phys.: Conf. Ser.*, 2007, **61**, 192.
- 22 A. E. Vladár and V.-D. Hodoroaba, in *Characterization of nanoparticles*, Elsevier, 2020, pp. 7–27.
- 23 T. Li, A. J. Senesi and B. Lee, *Chem. Rev.*, 2016, **116**, 11128–11180.
- 24 J. Liang, S. Xu, L. Hu, Y. Zhao and X. Zhu, *Mater. Chem. Front.*, 2021, **5**, 3823–3829.
- 25 Y. Xing, G. Di Caterina and J. Soraghan, *Front. Neurosci.*, 2020, **14**, 1143.
- 26 Y. Cao, Y. Chen and D. Khosla, *Int. J. Comput. Vis.*, 2015, **113**, 54–66.
- 27 S. B. Shrestha and G. Orchard, arXiv preprint arXiv:1810.08646, 2018.
- 28 S. Xingjian, Z. Chen, H. Wang, D.-Y. Yeung, W.-K. Wong and W.-c. Woo, 2015.
- 29 S. Khaki, L. Wang and S. V. Archontoulis, *Front. Plant Sci.*, 2020, **10**.
- 30 D. J. Griffiths and D. F. Schroeter, *Introduction to Quantum Mechanics*, Prentice Hall, 1994.
- 31 D. Dexter, in *Solid state physics*, Elsevier, 1958, vol. 6, pp. 353–411.
- 32 S. Wang, S. Wang, C. Wang, Q. Li, L. Han and W. Kong, Terahertz Dielectric Properties of Polyvinylidene Fluoride Films, in *The International Photonics and Optoelectronics Meeting 2017, OSA Technical Digest (online)*, Optica Publishing Group, paper ASu3A.5, Wuhan, 2017.
- 33 C. D. Armstrong and A. R. Teixeira, *React. Chem. Eng.*, 2020, **5**, 2185–2203.

