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Disentangling the resonant Auger spectra of ozone: overlapping core-hole states and core-excited state dynamics†

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We investigate the resonant and non-resonant Auger spectra of ozone with a newly implemented multi-reference protocol based on the one-center approximation [Tenorio *et al.*, *J. Chem. Theory Comput.* 2022, **18**, 4387–4407]. The results of our calculations are compared to existing experimental data, where we elucidate the resonant Auger spectrum measured at 530.8 and 536.7 eV, that correspond to the $1s_{O_T} \rightarrow \pi^*(2b_1)$ and $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonances, and at 542.3 eV, which lies near the $1s_{O_C} \rightarrow \sigma^*(7a_1)$ excited state and above the $1s_{O_T}^{-1}$ ionization threshold. Using molecular dynamics simulations, we demonstrate the relevance of few-femtoseconds nuclear dynamics in the resonant Auger spectrum of ozone following the $1s_{O_T} \rightarrow \pi^*(2b_1)$ core-excitation.

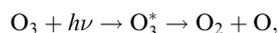
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1 Introduction

Ozone is a highly reactive homonuclear triatomic molecule oriented with C_{2v} point group symmetry. The two molecular sites are denoted O_C for the central oxygen atom, and O_T for the terminal ones.^{1,2} Besides its fundamental relevance in Earth's atmosphere, ozone has also vast industrial and medicinal applications.^{3–6} Due to its relevance, the electronic spectroscopy of ozone has been extensively studied both at the valence^{7–11} and core-excited^{12–19} regions. Deep ultraviolet photodissociation of ozone following an excitation from the ground electronic state to the excited $B(^1B_2)$ state [Hartley state], according to



is responsible for the protective function of the ozone layer in the stratosphere, although the fourth ionized state of O_3^+ was also found to lead to photofragmentation of $O_3^+ \rightarrow O_2 + O^+$ by visible light.² Recently, the photodynamics of ozone leading to fast photofragmentation has been investigated using time-resolved photoelectron spectroscopy (PES) experiments.^{20,21}

Molecular Auger electron spectroscopy^{22,23} (also known as Auger–Meitner²⁴) is a very attractive experimental tool that encodes the electronic structure of a core-excited or core-

ionized molecule into the kinetic energy of the ejected Auger electron mapping bound states to the continuum, and, essentially, probing molecular relaxation mechanisms. Processes involved in resonant Auger electron spectroscopy (RAES) are the ones that occur when a core-excited state decays to a singly ionized state, where the outgoing electron can be either the core-excited electron, resulting in a one-hole (1h) final state (participator Auger), or an inner-valence electron, resulting in a two-hole-one-particle (2h1p) state (spectator Auger). In normal (or non-resonant) Auger electron spectroscopy (AES), a core-ionized 1h initial state decays into a manifold of doubly charged (2h) valence states of different spin multiplicity. In the past few years, Auger spectroscopy has been extensively used in connection to X-ray absorption spectroscopy (XAS) and/or X-ray photoelectron spectroscopy (XPS) to probe site-specificity in molecular photofragmentation.^{25–29} Because of their high sensitivity to electronic and nuclear dynamics, AES/RAES are becoming increasingly popular techniques to unravel underlying electronic structure,³⁰ and nuclear dynamics of photoexcited molecules.^{31–35}

RAES measurements of ozone have been obtained with photon energies of 530.8 and 536.7 eV, which correspond to the $1s_{O_T} \rightarrow \pi^*(2b_1)$ and $1s_{O_T} \rightarrow \sigma^*(7a_1)$ excitations,^{12,13} and at 542.3 eV, that lies near the $1s_{O_C} \rightarrow \sigma^*(7a_1)$ excited state and above the $1s_{O_T}^{-1}$ ionization threshold.¹³ For the case of the resonant $1s_{O_T} \rightarrow \sigma^*(7a_1)$ state, a Doppler-type energy-split in the kinetic energy of atomic Auger electrons arising after fast fragmentation has been reported.^{13,36} The promotion of a core-electron into a repulsive intermediate electronic state can lead to fragmentation on a time scale compatible with a core-hole

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lifetime—that is, a few femtoseconds (fs).³⁷ Ultrafast dissociation has been demonstrated to be an important mechanism of distributing the internal energy in core-excited small molecules like H₂O,³⁸ NH₃,³⁹ HCl^{40–42} as well as in heavier ones, such as CH₂Cl₂ and CHCl₃.^{43–45}

On the theory side, one of the main challenges in devising approaches to simulate Auger spectra is how to properly account for the contributions due to the electronic continuum wave function, whose asymptotic behavior is poorly described within the quadratically integrable finite (L^2) basis sets typically employed for bound states. Notice, however, that total decay widths have been obtained with purely L^2 basis sets and a Stieltjes imaging procedure,⁴⁶ or by use of complex scaling of the Hamiltonian.⁴⁷ Some attempts to bypass – or simplify – the problem of the electronic continuum in the context of Auger electron spectroscopy are methodologies based on simple population analysis of the final cationic states,⁴⁸ or on the use of precalculated atomic bound-continuum two-electron integrals within the one-center approximation (OCA).^{49–52} Other computational strategies relying on explicit evaluation of the bound-continuum Auger intensities have been reported based on different flavours of electronic structure approximations for the bound and the continuum states.^{53–59} A second important issue is how to achieve a reasonably accurate description of the manifold of final states, and the relaxation associated with the core hole state. Resonant Auger typically explores a very large manifold of valence singly ionized states, covering some tens of eV, and spanning the inner valence part of the spectrum, so that, in addition to primary holes, mostly 2h1p states, and the large correlation effects associated with them become involved. Some methods may show a progressive drift of final states towards higher energies, due to insufficient correlation of the physical 2h1p states.^{57,58} Moreover, in propagator or linear response approaches employing a single set of orbitals, usually of the ground state, an accurate description of the core hole state, and its matrix elements with the final states, is also an additional problem, which calls for higher excitation levels. This is circumvented in configuration interaction (CI) approaches, which can employ separate orbital bases for the initial and final states. In this respect, O₃ is a particularly challenging case, as already its ground state is highly correlated, and configuration mixing is dramatic in the ionic states, even at the start of the spectrum. Similar considerations apply to the normal Auger, where already the density of final primary 2h states is much higher, and 3h2p will be likely to be significantly excited, although this has not yet been investigated in so much detail.

Here we use the OCA to evaluate Auger decay rates based on a restricted-active-space perturbation theory of second order (RASPT2) description of the bound states. We recently implemented this OCA-RASPT2 approach⁵² within the OpenMolcas program.⁶⁰ More specifically, we here demonstrate the capabilities of OCA-RASPT2 on the resonant and non-resonant Auger spectra of ozone, especially in a situation of overlapping core-hole states, as observed for the $1s_{O_C} \rightarrow \sigma^*(7a_1)$ and $1s_{O_T}^{-1}$ states. Moreover, we demonstrate the relevance of few

femtoseconds nuclear dynamics in the resonant Auger spectrum following the $1s_{O_T} \rightarrow \pi^*(2b_1)$ core-excitation.

The paper is organized as follows: in Section 2, we give a brief description of the underlying theory of molecular Auger decay rates based on the Wentzel ansatz.^{61,62} In Section 3, the information about our computational protocol, and the molecular dynamics simulations is detailed. The results are presented and discussed in Section 4. Outlook and conclusions are given in Section 5.

2 Theory

Auger decay rates are here obtained from the Fermi golden rule^{61,62} (a.k.a. Wentzel's Ansatz) for the rate of decay of an isolated resonance interacting with a continuum, *i.e.*, the transition

$$\Psi_I^N \rightarrow \Psi_K^{N-1} + e^-, \quad (1)$$

where N is the number of electrons in the initial state I. In this process, Ψ_I is either a core-excited state of a N -electron system decaying into singly ionized ($N - 1$)-electron states (RAES), or a ($N - 1$)-electron core-ionized state (of a N -electron system) decaying into a doubly ionized ($N - 2$)-electron state manifold (AES).

In the Wentzel approximation,^{62,63} the core-excitation or core-ionization process that prepares the initial state is uncoupled from the subsequent decay processes, *i.e.*, initial core-excitation/ionization and subsequent decay are treated as two independent steps. Only the decay process is explicitly considered.

For fixed initial (I) and final (K) states, the partial decay rate Γ_{KI} (also known as Auger intensity or decay width) is obtained by a sum over all possible angular momenta of the Auger electron

$$\Gamma_{KI} = \sum_{lm} \Gamma_{KI;Elm}. \quad (2)$$

The individual rates $\Gamma_{KI;Elm}$ (in atomic units) are given by⁶³

$$\Gamma_{KI;Elm} = 2\pi |\langle \Psi_{K;Elm} | \hat{H} - E_I | \Psi_I \rangle|^2. \quad (3)$$

with E_I as the energy of the initial state Ψ_I .

Here $\Psi_{K;Elm}$ is the total N -electron final state wave function, which is approximated as an antisymmetrized product of a final ($N - 1$)-electron state wavefunction Ψ_K^{N-1} and a continuum orbital ϕ_{Elm} with kinetic energy E and angular momentum quantum numbers l and m ,

$$\Psi_{K;Elm} = \phi_{Elm} \Psi_K^{N-1}. \quad (4)$$

Assuming orthogonality between the continuum and the bound-state orbitals, the relevant Auger decay matrix element in eqn (3) reduces to^{52,55}

$$\Gamma_{KI;Elm} = 2\pi |A_{KI;Elm} + B_{KI;Elm}|^2, \quad (5)$$



where

$$A_{\text{KI};Elm} \equiv \langle \hat{a}_{Elm}^\dagger \Psi_K^{N-1} | \hat{h} | \Psi_I^N \rangle = \sum_p \langle \phi_{Elm} | \hat{h} | \phi_p \rangle R_{\text{KI};p} \quad (6)$$

$$B_{\text{KI};Elm} \equiv \langle \hat{a}_{Elm}^\dagger \Psi_K^{N-1} | \hat{g} | \Psi_I^N \rangle = \sum_{qrs} \langle \phi_{Elm} \phi_q | \phi_r \phi_s \rangle R_{\text{KI};qsr} \quad (7)$$

In the equations above, \hat{a}_{Elm}^\dagger is a creation operator for an electron in the continuum, \hat{h} is the one-electron part of the Hamiltonian operator, and \hat{g} is the two-electron repulsion operator; ϕ_{Elm} is the continuum orbital and ϕ_p is a generic molecular orbital.

The matrix elements $R_{\text{KI};p}$ in eqn (6) are the expansion coefficients of the one-particle Dyson orbital over the spin-orbital MO basis $\{\phi\}$,^{64,65}

$$R_{\text{KI};p} = \langle \Psi_K^{N-1} | \hat{a}_p | \Psi_I^N \rangle. \quad (8)$$

The spin-adapted Auger matrix elements $R_{\text{KI};qsr}$ (also called two-particle Dyson matrix) in eqn (7) can be expressed as (see, e.g., ref. 52, 55 and 66)

$$R_{\text{KI};qsr} = \langle \Psi_K^{N-1} | \hat{a}_q^\dagger \hat{a}_s \hat{a}_r | \Psi_I^N \rangle \quad (9)$$

where the creation/annihilation operators \hat{a}_q^\dagger , \hat{a}_s , and \hat{a}_r refer to a complete set of molecular orbitals.

The remaining ingredients needed for the evaluation of the decay matrix element in eqn (5) are the one- and two-electron integrals involving the regular MO orbitals and the wave function of the continuum electron. As anticipated, we here use the technique called one-center approximation,^{49,50} which utilizes precalculated bound-continuum atomic two-electron integrals, and thereby avoids the explicit evaluation of the continuum wave function. OCA is based on the recognition of the strongly localized nature of the initial core hole, and it amounts to the neglect of coulomb matrix elements involving atomic orbitals (AOs) on different centers. Moreover, the continuum, expanded in partial waves centered on the core site, is approximated by the corresponding atomic one. Because of the high electron kinetic energy it is again a fair approximation. Due to the complexity and sheer number of final ionic states reached, OCA seems pretty adequate for an overall description of the spectral intensities in current spectra of complex molecules, unless an accurate study of specific, well-characterized, spectral features is warranted. A full description of the molecular continuum may be included, at a considerable computational cost, using for example a multicenter B-spline description of the continuum.⁶⁷

Moreover, the one-center approximation^{49,50} considers the amplitude based on the Wentzel ansatz, eqn (5), where the matrix element $\Gamma_{\text{KI};Elm}$ is reduced to the direct two-electron term (eqn (7)), as $A_{\text{KI};Elm}$ is generally very small compared to $B_{\text{KI};Elm}$ (see, e.g., ref. 52 and the investigation in ref. 56)

$$\Gamma_{\text{KI};Elm} \simeq 2\pi |B_{\text{KI};Elm}|^2. \quad (10)$$

Thus, we fix the index q in eqn (7) to the core-hole site c of a particular atom A, and replace the exact two-electron integral term $\langle \phi_{Elm} \phi_c | \phi_r \phi_s \rangle$ involving the continuum orbital ϕ_{Elm} and

the MOs $\{\phi_r\}$ with an approximate sum of atomic two-electron integrals,

$$\langle \phi_{Elm} \phi_c | \phi_r \phi_s \rangle \simeq \sum_{\mu\nu\rho} \langle \chi_{Elm}^\Lambda \chi_\mu^\Lambda | \chi_\nu^\Lambda \chi_\rho^\Lambda \rangle D_{\mu c} D_{\nu r} D_{\rho s} \quad (11)$$

where $\{\chi_\lambda^\Lambda\}$ indicates a basis of atomic orbitals (AOs) of atom A and $D_{\nu r}$ are expansion coefficients. The atomic two-electron integrals can be computed (for a fixed electron kinetic energy E , e.g., relative to the Auger transition in the free atom) and stored once for all. Tabulated radial atomic two-electron integrals are available in the literature,^{68–70} whereas the angular parts are computed analytically (see notes in the ESI† or ref. 52 for more details).

Various recipes, largely equivalent, can be employed to obtain the coefficients $D_{\nu r}$ from the molecular orbitals $\{\phi_r\}$, typically by projecting $\{\phi_r\}$ onto the space spanned by a minimal basis set (MBS).⁵⁰ The most practical choice, which we adopt here, is to use, as MBS, the first fully contracted functions of the atomic Gaussian Type orbital (GTO) basis, which are accurate representations of the atomic orbitals.⁵² For further details about our OCA-RASPT2 implementation and the selection of a MBS, please consult Tenorio *et al.*⁵²

3 Computational details

Calculations of resonant and non-resonant Auger spectra, as well as of PES, XPS and XAS, have been performed at the multi-state RASPT2 (MS-RASPT2) level^{71–74} using the OpenMolcas program package.⁶⁰ Auger transition rates were obtained according to the one-center approximation.⁵² PES and XPS spectra have been obtained from the squared norm of the Dyson orbitals representing the ionization channels (see, e.g., ref. 65 for details). The OCA-RASPT2 Auger intensities⁵² were obtained with a developer version of OpenMolcas.

We adopted the cc-pVTZ basis set⁷⁵ in all calculations. Multi-reference calculations of core-excited and core-ionized states^{28,76,77} relevant to, respectively, resonant and non-resonant Auger spectra were carried out by placing the relevant core orbitals in the RAS1 space and enforcing single electron occupation in RAS1 by means of the HEXS projection technique⁷⁸ available in OpenMolcas,⁶⁰ which corresponds to applying the core-valence separation technique.⁷⁹ RAS2 was used for complete electron distribution, *i.e.*, to define the complete active space. RAS3 was kept empty. An imaginary level shift of 0.25 Hartree was applied to avoid intruder state singularities in the MS-RASPT2 calculations. The employed active space is illustrated in Fig. 1. Three inner valence orbitals with O 2s character were kept out of the active space. Three 1s_O orbitals were added to the RAS1 subspace, whereas twelve electrons are distributed over nine molecular orbitals in the RAS2 subspace. Final cationic states were obtained by state-averaging over several final states for each irreducible representation of the C_s point group symmetry.

At its ground state the ozone molecule belongs to the C_{2v} point group symmetry with experimentally determined structural parameters⁸⁰ of $r_{\text{O-O}} = 1.28 \text{ \AA}$, $\angle = 116.8^\circ$. The two different atomic sites are denoted O_T for the pair of terminal



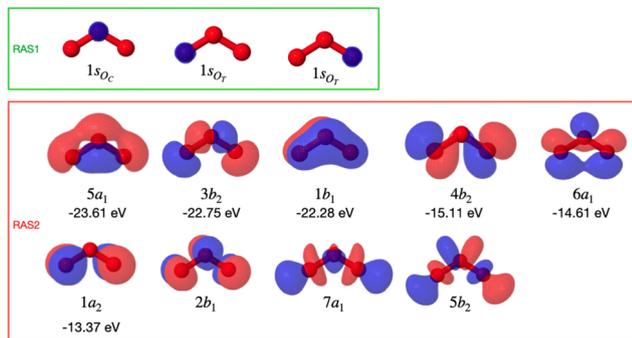


Fig. 1 Molecular active orbitals of O_3 from a Hartree–Fock calculation with C_{2v} point group symmetry. The core orbitals (RAS1 subspace) have been localized. The HF binding energies of the valence occupied orbitals are shown with the corresponding MO.

oxygen atoms and O_C for the central oxygen atom. Similar to what we did in previous studies,^{52,66} to facilitate the application and analysis of the OCA projection on symmetry equivalent atomic sites, we have reduced the point group symmetry from C_{2v} to C_s , and localized the core orbitals by applying a Cholesky localization procedure.⁸¹ Moreover, we find it particularly convenient to use C_s symmetry because we calculate Auger spectra along a (dissociative) molecular dynamics trajectory, where C_s symmetry can always be applied. Auger transitions involving the pair of terminal oxygen atoms are obtained by summing the contributions of each localized O_T site. The localized $1s$ orbitals are visualized in Fig. 1. Notice that the valence orbitals are not affected by the localization procedure.

Additionally, RASSCF adiabatic molecular dynamic simulations of core-excited states of ozone have been performed using the DYNAMIX program in OpenMolcas.⁶⁰ The dynamics simulate 30 fs using step size of 0.242 fs for the $1s_{O_T} \rightarrow \pi^*(2b_1)$ core-excited state. A Nosé–Hoover chain of thermostats was used to reproduce dynamics at a constant temperature of 300 K. Sixteen random initial conditions (geometries and momenta) were generated following a Maxwell–Boltzmann distribution at 300 K, based on a frequency calculation of the ground state.

A heuristic Lorentzian broadening of the discrete stick spectra (energies and transition rates) was used to simulate the spectra. The value of the full-width-at-half-maximum (fwhm) parameter used in all the Auger spectra was 0.30 eV, except for the average spectra. In the latter case, the average is obtained by broadening all discrete sticks together with fwhm of 0.20 eV, while the convoluted intensity is divided by the number of time steps considered in the interval. Since all theoretical methods employ approximations, they inherently include some error, which, however, can often be remedied by an overall shift to align with the energy axis of the experiment. Sources of error can be basis set limitation, or unaccounted correlation effects (most probably a combination of both), lack of relativistic effects. The rigid shift and other parameters used for plotting the XAS, XPS and PES are given in the corresponding figures.

All calculations were carried out on the DTU High-Performance Computer Cluster.⁸²

4 Results and discussion

The electronic ground state of ozone has a pronounced bi-radical character. It mixes the HF configuration with another orbital configuration reached by double excitation from the $1a_2$ to the $2b_1$ orbital.⁸³ The leading valence configurations and their squared amplitudes given by a CASSCF wave function are given below:

$$(5a_1)^2(3b_2)^2(1b_1)^2(4b_2)^2(6a_1)^2(1a_2)^2(2b_1)^0[0.77] \\ + (5a_1)^2(3b_2)^2(1b_1)^2(4b_2)^2(6a_1)^2(1a_2)^0(2b_1)^2[0.11].$$

We start with the description of the PES, XAS and XPS spectra. Notice that the final states on a PES spectrum are singly-charged cationic states, and they are usually the same as the final states reached after a resonant Auger decay process. Therefore, besides an appropriate description of the (initial) core-excited state, it is extremely important to be able to reproduce well the entire PES in order to have a decent description of the RAES. The multi-configurational character of ozone poses additional challenges for highly correlated methods based on a single determinant reference because of the configuration interaction already in the ground state. In Fig. S1 (ESI[†]), we show the PES obtained at the EOM-CCSD/cc-pVTZ level with the experimental ground state geometry⁸⁰ $r_{O-O} = 1.28 \text{ \AA}$, $\angle = 116.8^\circ$ (calculations performed with Q-Chem⁸⁴). From Fig. S1 (ESI[†]), we observe that except for the first two peaks below 14 eV, the remaining part of the spectrum, dominated by multi-electron excitations, is not well reproduced by the EOM-CCSD method. Further improvements on the PES spectrum of ozone could possibly be reached with an EOM-CC3 (or EOM-CCSDR(3)) description of the ground and ionized states, as it was recently shown by Moitra *et al.*⁸⁵ A recent implementation of multireference algebraic diagrammatic construction theory (MR-ADC)⁸⁶ has also demonstrated excellent performance on the XPS spectrum of ozone.

Here we profit from the characteristics of the MS-RASPT2 level of approximation, as a multi-reference method allowing for a full-CI description of the excitation manifold within an active space, with dynamical correlation recovered by perturbation theory of second order.

4.1 PES, XAS and XPS

Valence photoelectron spectra of ozone have been extensively investigated experimentally and theoretically over the past decade.^{8–12,20,21,87} Our results are presented in Fig. 2 alongside with the experimental data.¹² The peaks labeled I to V are characterized in Table 1. Peaks I and II are the only direct photoionization channels—that is, they can be represented by the removal of one electron from an occupied orbital. A direct ionization is also referred to as a $1h$ configuration. These peaks were also captured in the EOM-CCSD spectrum of Fig. S1 (ESI[†]). Peaks III to V are mostly satellites, and they can be generally represented by $2h1p$ orbital configurations. The calculation of PES comprising direct and satellite ionization channels is a useful test to check whether the electronic structure method



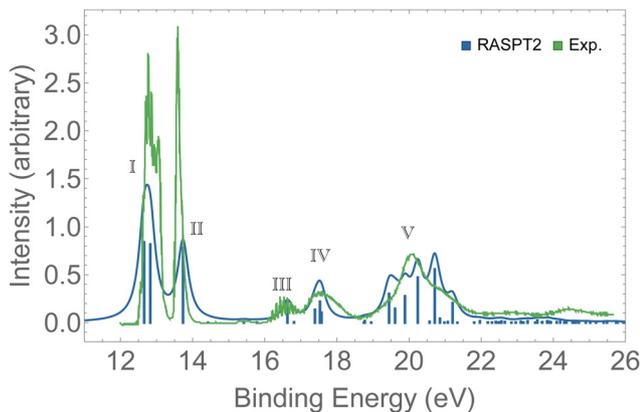


Fig. 2 PES of O_3 . The spectrum was shifted by +0.3 eV and broadened with Lorentzian functions with fwhm = 0.18 eV. For the assignments of the peaks, see Table 1.

employed is well suited for the calculation of resonant Auger spectra, which are known to be dominated by $2h1p$ spectator decay channels. From the observed agreement of our PES with the experimental measurement,¹² we conclude that our protocol, based on the RASPT2 description of the bound states, is appropriate for the representation of the relevant states involved in the resonant Auger spectra of ozone.

Here, we give only a brief description of our results for the XAS and XPS spectra since the absorption and ionisation spectra of ozone near the O 1s edge are well documented elsewhere.^{13,15,16,19,86,89,90} The assignments of the main features of the XAS and XPS are given in Table 2. The intense peak calculated at 528.9 eV in the XAS spectrum is assigned to the $1s_{O_T} \rightarrow \pi^*(2b_1)$ state. The next core-excited state, computed at 535.7 eV, corresponds to an excitation of an $1s_{O_C}$ electron to the same $\pi^*(2b_1)$ orbital. Notice that the separation between these two core-excitations involving the $\pi^*(2b_1)$ is around 6 eV.

Table 2 Core-excited and core-ionized states of O_3 . Excitation/ionization energies, oscillator strengths (O.S.) and pole strengths (R_i) were obtained at the MS-RASPT2 level with the cc-pVTZ basis set. The state characterization is based on the main CI configuration

Label	Energy (eV)			O.S.	Excitation character
	This work	Exp. ¹³	Exp. ¹⁹		
A	528.95	529.4	529.25	0.074	$1s_{O_T} \rightarrow \pi^*(2b_1)$
B	535.75	~535.0	534.80	0.031	$1s_{O_C} \rightarrow \pi^*(2b_1)$
C	536.41	~536.7	535.75	0.067	$1s_{O_T} \rightarrow \sigma^*(7a_1)$
D	538.76	~538.0	537.90	0.039	$1s_{O_T} \rightarrow \sigma^*(5b_2)$
E	541.05	~542.3	539.70	0.031	$1s_{O_C} \rightarrow \sigma^*(7a_1)$
F	543.02		542.00	0.062	$1s_{O_C} \rightarrow \sigma^*(5b_2)$

This work	IE (eV)			R_i	Ionization
	Exp. ¹³	Exp. ¹⁹			
541.52	541.5	541.75	0.46	$1s_{O_T}^{-1}$	
541.52			0.46	$1s_{O_T}^{-1}$	
547.25	546.2	546.44	0.52	$1s_{O_C}^{-1}$	

A similar energy separation is also observed in the XPS for the ionization channels $1s_{O_T}^{-1}$ and $1s_{O_C}^{-1}$, calculated at 541.5 and 547.3 eV, respectively. Our core-ionization energies are also in good agreement with other calculated results based on MR-ADC.⁸⁶ The excitation energies for the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ and the $1s_{O_C} \rightarrow \sigma^*(7a_1)$ states were calculated as 536.4 and 541.0 eV, respectively.

In the following we concentrate on the discussion of the resonant Auger spectra of O_3 at the $1s_{O_T} \rightarrow \pi^*(2b_1)$, $1s_{O_T} \rightarrow \sigma^*(7a_1)$ and $1s_{O_C} \rightarrow \sigma^*(7a_1)$ resonances. The red arrows drawn in Fig. 3 – placed at 530.8, 536.7 and 542.3 eV – point to the regions of the spectrum where Auger spectra have been measured.^{12,13} The first arrow indicates an energy matching with the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance. The second arrow shows the photon energy intentionally blue-shifted relative to the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonance to avoid overlap with the $1s_{O_C} \rightarrow \pi^*(2b_1)$ state.

Table 1 Calculated binding energies of the O_3^+ states, square norms of the Dyson orbital (pole strengths R_i) of the photoelectron spectrum, and decay rates (Γ) in the autoionization spectrum following the $1s_{O_T} \rightarrow \pi^*(2b_1)$ excitation. Experimental values from ref. 12

Binding energy (eV)		PES ^a		RAES ^b		Ionization character ^c
This work	Exp. ¹²	Peak	R_i	Peak	$\Gamma (\times 10^{-4} \text{ a.u.})$	
12.52	12.8	I	0.84	A	0.40	$6a_1^{-1}[0.73]$
12.59	12.8	I	0.81	A	0.39	$4b_2^{-1}[0.75]$
13.50	13.5	II	0.77	B	1.21	$1a_2^{-1}[0.83]$
14.61			0.18×10^{-3}	C	0.66	$6a_1^{-2}2b_1^1[0.47] + 4b_2^{-2}2b_1^1[0.38]$
15.67			0.87×10^{-2}	D	1.41	$6a_1^{-1}1a_2^{-1}2b_1^1[0.83]$
15.81			0.46×10^{-2}	D	1.40	$4b_2^{-1}1a_2^{-1}2b_1^1[0.81]$
16.67	~16.5	III	0.24	E	1.28	$1a_2^{-2}2b_1^1[0.58]$
17.29			0.33×10^{-2}	E'	1.72	$4b_2^{-1}6a_1^{-1}2b_1^1[0.62]$
17.78	~17.5	IV	0.18		0.40	$4b_2^{-1}1a_2^{-1}2b_1^1[0.44] + 6a_1^{-2}2b_1^1[0.19]$
17.80		IV	0.12	E''	1.23	$6a_1^{-2}2b_1^1[0.24] + 4b_2^{-2}2b_1^1[0.29]$
19.07			0.11×10^{-3}	F	0.40	$6a_1^{-2}1a_1^{-1}2b_1^2[0.37] + 4b_2^{-2}1a_1^{-1}2b_1^2[0.38]$
20.05	~20.0	V	0.39		0.12	$5a_1^{-1}[0.29] + 6a_1^{-2}7a_1^1[0.15]$
20.35		V	0.55		0.16	$4b_2^{-1}1b_1^{-1}2b_1^1[0.39] + 3b_2^{-1}[0.18]$
21.01		V	0.51	G	1.37	$1b_1^{-1}[0.38]$
21.61			0.26	H	0.77	$3b_2^{-1}[0.43]$
24.16			0.79×10^{-2}	I	1.07	$3b_2^{-1}1a_2^{-1}2b_1^1[0.65]$
24.16			0.74×10^{-2}	I	1.07	$4b_2^{-1}6a_1^{-1}1b_1^{-1}2b_1^2[0.25]$

^a See also Fig. 2. ^b See also Fig. 4. ^c The numbers within square brackets correspond to the CI weight of the given configuration.



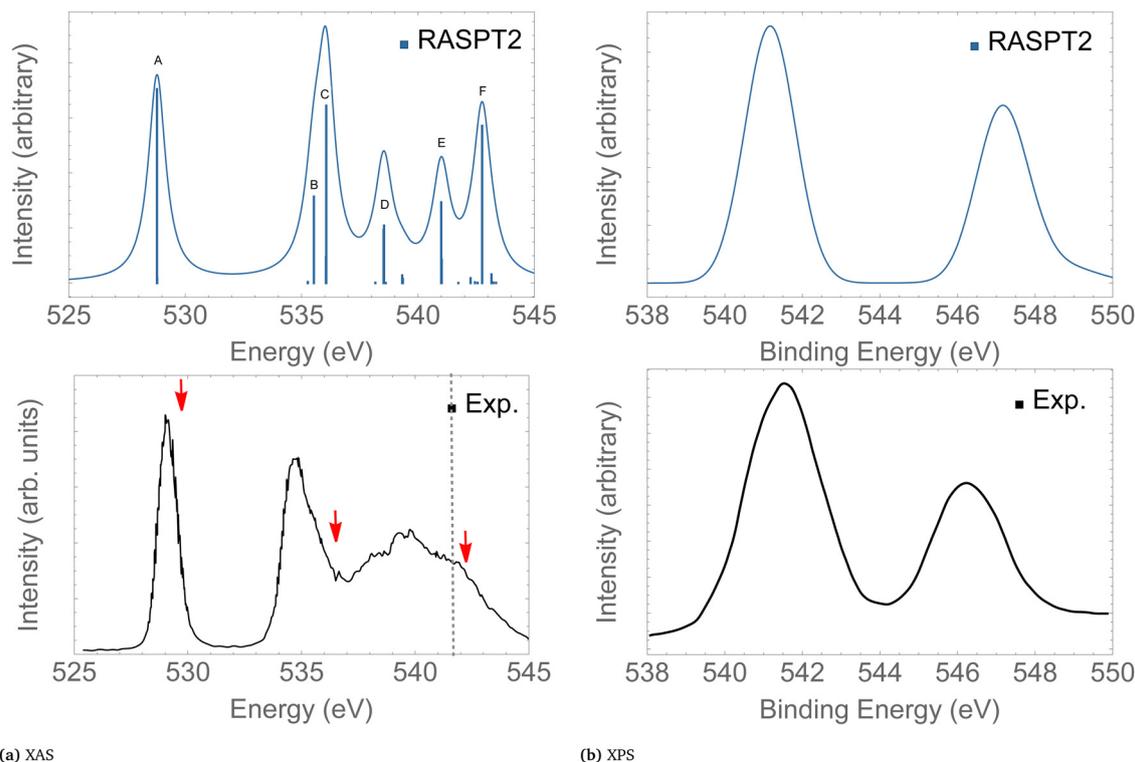


Fig. 3 XAS (left) and XPS (right) of O_3 . The computed XAS and XPS spectra were shifted by +0.15 and +0.25 eV, and broadened with Gaussian functions with fwhm = 0.45 and 0.65 eV, respectively. The dashed vertical line in the experimental XAS spectrum indicates the first $O1s$ ionization potential. The XAS and XPS experimental spectra were digitized from ref. 13 and 88, respectively. For a characterization of the labeled peaks, see Table 2. The red arrows indicate the photon energies where RAES have been measured.

The third arrow is found in a region of the spectrum where the $1s_{O_C} \rightarrow \sigma^*(7a_1)$ resonance and the $1s_{O_T}^{-1}$ ionization are close. In our calculations, the $1s_{O_C} \rightarrow \sigma^*(7a_1)$ and the $1s_{O_T}^{-1}$ states are separated by just 0.5 eV, and therefore, they can be both accessed in the same measurement with photon energy of 542.3 eV, which lies above the ionization threshold of the 1s electron of the terminal O.¹³

4.2 Auger spectroscopy

The RAES at the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance of O_3 is presented in Fig. 4. The assignments of the main features of the spectrum are given in Table 1. In the calculation we used the experimental equilibrium geometry of the ground state⁸⁰ ($r_{O-O} = 1.28$ Å, $\angle = 116.8^\circ$). The calculated spectrum was shifted by -0.6 eV to better compare with the experiment.

By comparing the calculated RAES spectrum of Fig. 4 with experiment,¹² we observe a satisfactory match only in the initial part of the spectrum, that is, for the three weak peaks observed between 517–514 eV, labeled A, B and C. These peaks are assigned to the participator decay channels $6a_1^{-1}$ (A), $4b_2^{-1}$ (A), and $1a_2^{-1}$ (B) calculated at 515.9, 515.9, 515.1 eV, respectively, and the spectator decay channel $6a_1^{-2}2b_1^1 + 4b_2^{-2}2b_1^1$ (C), calculated at 514.2 eV. Notice that, in contrast to peaks A and B, peak C is a dark state in the PES.¹² The wave function of the ionic state corresponding to peak C has multiconfigurational character $6a_1^{-2}2b_1^1 + 4b_2^{-2}2b_1^1$ with similar squared

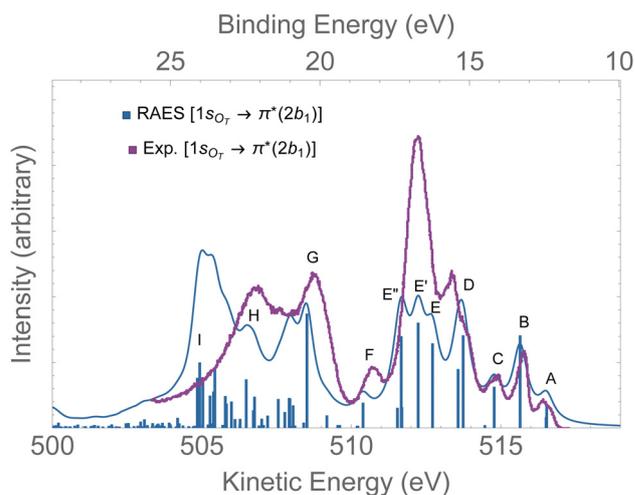


Fig. 4 RAES of O_3 at the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance calculated with the FC geometry. The computed spectrum was shifted by -0.6 eV and broadened with Lorentzian functions with fwhm = 0.30 eV. The experimental spectrum was digitized from ref. 12. For the assignments, see Table 1.

amplitudes. Thus, the photoionization probability for such state will be naturally very low due to configuration mixing, while resonant excitation leads to intensity redistribution *via* excitation to the $\pi^*(2b_1)$ orbital, enhancing the probability for such state in RAES.⁸³ The most intense peak on the RAES is



observed in the experimental spectrum at around 512 eV (ionic states E, E', and E''), and it is underestimated to a large extent in our calculation. Peaks E, E', and E'' are mainly attributed to the decay channels $1a_2^{-2}2b_1^1$, $4b_2^{-1}6a_1^{-1}2b_1^1$, and $6a_1^{-2}2b_1^1 + 4b_2^{-2}2b_1^1$ (see Table 1). The broad peaks observed in the experiment between 509 and 507 eV are shifted to lower energies by ~ 2 eV in the calculated spectrum. These peaks have characteristics of spectator as well as participator decay channels involving the deep valence molecular orbitals $1b_1$, $3b_2$ and $5a_1$, as one can see from the assignments in Table 1.

Overall, except for the peaks A–C, the agreement between the calculated spectrum obtained in the Franck–Condon regime and the experiment is quite poor. We note that another computed RAES at the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance with characteristics very similar to the ones obtained here was reported in ref. 12, although it is unclear to us why the authors chose to use structural parameters ($r_{O-O} = 1.19$ Å and $\angle = 117.4^\circ$) so different from the experimentally determined ground state equilibrium geometry⁸⁰ ($r_{O-O} = 1.28$ Å and $\angle = 116.8^\circ$) or any other calculated structural parameters obtained for ozone.^{83,91–94}

Our computed total decay rate for the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance is $\Gamma = 25.6 \times 10^{-4}$ a.u. This value can be possibly underestimated as any contribution from decay channels below 500 eV is neglected in our calculation. Full diagonalization of the Hamiltonian matrix would be necessary for a better estimate of the total decay rate, which is beyond our reach. Therefore, our model provides a lower bound of the total decay rate. The decay rate is converted to lifetime by the taking the reciprocal of Γ , $\tau = 1/\Gamma \approx 9$ fs. This value is higher than the approximate lifetime of the O1s core hole in water,⁹⁵ that is, ~ 4 fs, possibly a consequence of an underestimation of Γ in our calculation.

In the following we combine trajectory molecular dynamics with Auger spectral calculations to characterize the features observed on the RAES of ozone following the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance.

The trajectories were obtained in the adiabatic regime, thus neglecting autoionization and possible interference between different pathways. According to the analysis of the XAS, the separation between the first $1s_{O_T} \rightarrow \pi^*(2b_1)$ and the second electronic core-excited state $1s_{O_C} \rightarrow \pi^*(2b_1)$ amounts to 6 eV, and therefore the adiabatic condition is expected to be a good approximation for a short time regime. It is important to highlight that our major interest is in describing the influence of molecular dynamics following the $1s_{O_T} \rightarrow \pi^*(2b_1)$ excitation on the Auger spectrum of O₃, and, particularly, the dynamics in a time regime compatible to the core-hole lifetime. Ultrafast dissociation was experimentally demonstrated in ozone for the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonance,¹³ but it was not observed in the experimental RAES at the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance.¹²

The core-excited molecular dynamics of ozone leads to the O₃ → O₂ + O fragmentation if we allow the dynamics to run long enough, above the core-hole lifetime. In Fig. S2 (ESI†) we plot, for both the $1s_{O_T} \rightarrow \pi^*(2b_1)$ and the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ states, the bond distance r_{O-O} of the leaving oxygen (relative to the central

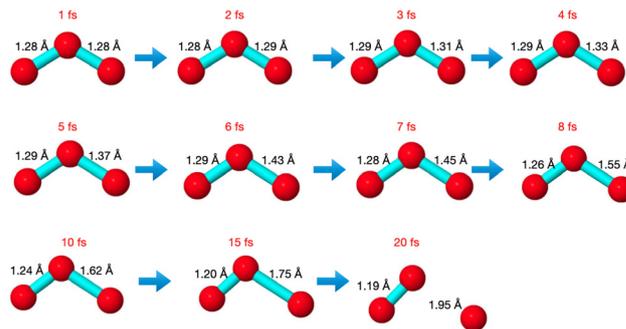


Fig. 5 Snapshots along a selected trajectory of O₃ at the $1s_{O_T} \rightarrow \pi^*(2b_1)$ core-excited state.

oxygen) against the dynamics time up to 30 fs. The slope of the curves can be interpreted as an estimate of the velocity of the leaving oxygen ($v \approx \frac{\Delta r}{\Delta t}$). From the slopes of Fig. S2 (ESI†), we can see that the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ dynamics is clearly faster compared to the $1s_{O_T} \rightarrow \pi^*(2b_1)$ dynamics. For example, at 8 fs, the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ dynamics shows $r_{O-O} \sim 1.8$ Å, whereas the $1s_{O_T} \rightarrow \pi^*(2b_1)$ dynamics shows $r_{O-O} \sim 1.5$ Å. In Fig. 5, we show some snapshots along a selected trajectory where the fragmentation of O₃ into O₂ + O can be visualized up to 20 fs. A common behaviour shared by all trajectories is that when one O–O bond increases, the other O–O bond decreases to be ultimately stabilized around 1.20 Å, which is nearly the equilibrium bond length of the O₂ molecule.

In Fig. 6, we show the molecular dynamics of the $1s_{O_T} \rightarrow \pi^*(2b_1)$ state below 10 fs. A visual inspection shows that all the trajectories share similar characteristics, and therefore we will concentrate the analysis that follows only on the most central trajectory, that is the one represented by the dashed blue line.

The dynamics described by the trajectory shows almost zero velocity and practically no alteration on the bond length up to 2 fs. After 4 fs, the velocity (slope) becomes nearly constant.

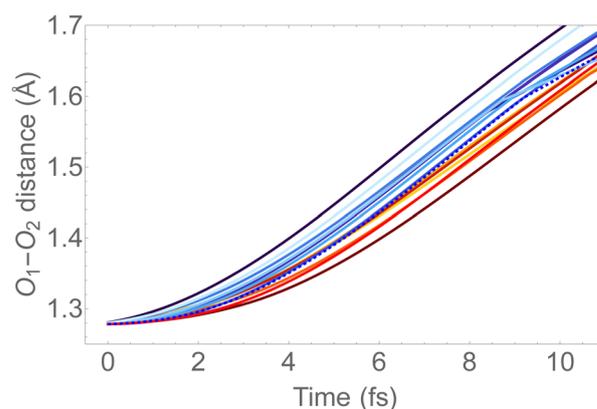


Fig. 6 O–O bond length vs. time extracted from the trajectory molecular dynamics at the $1s_{O_T} \rightarrow \pi^*(2b_1)$ core-excited state at the RASSCF level. We used sixteen initial conditions obtained from a Maxwell-Boltzmann distribution at 300 K (see Fig. S2 (ESI†) for the complete dynamics simulation up to 30 fs).



In the region between 4 and 8 fs, the bond lengths increase from ~ 1.35 Å to ~ 1.55 Å (see also Fig. 5).

For the sake of comparison, we can consider an approximately linear behaviour on the trajectories of Fig. S2 (ESI†) from 4 to 10 fs. Then, we estimate the average velocity $v \simeq \frac{\Delta r}{\Delta t}$ from our dynamics as ~ 0.04 and 0.07 Å fs $^{-1}$, for the $1s_{O_T} \rightarrow \pi^*(2b_1)$ and $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonances, respectively. The velocity of the leaving O atom relative to the O₂ fragment, estimated from a classical mechanical model for the dissociation derived from the Doppler-split resonant Auger lines for the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonance, was reported as 0.0756 Å fs $^{-1}$ in

ref. 13. Comparing the approximate velocity of the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance with the one estimated with the classical mechanical model for the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonance,¹³ we find that our estimate is indeed in the same order of magnitude, but about 40% lower. This deviation was expected since we are comparing velocities from different excitation states, and we expect the relative velocity of the leaving oxygen obtained for the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance to be slower, since this state is less dissociative. On the other hand, the agreement between our molecular dynamics and the classical model¹³ concerning the relative velocity for the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonance is remarkable. These results suggest that the dynamics of the O₃

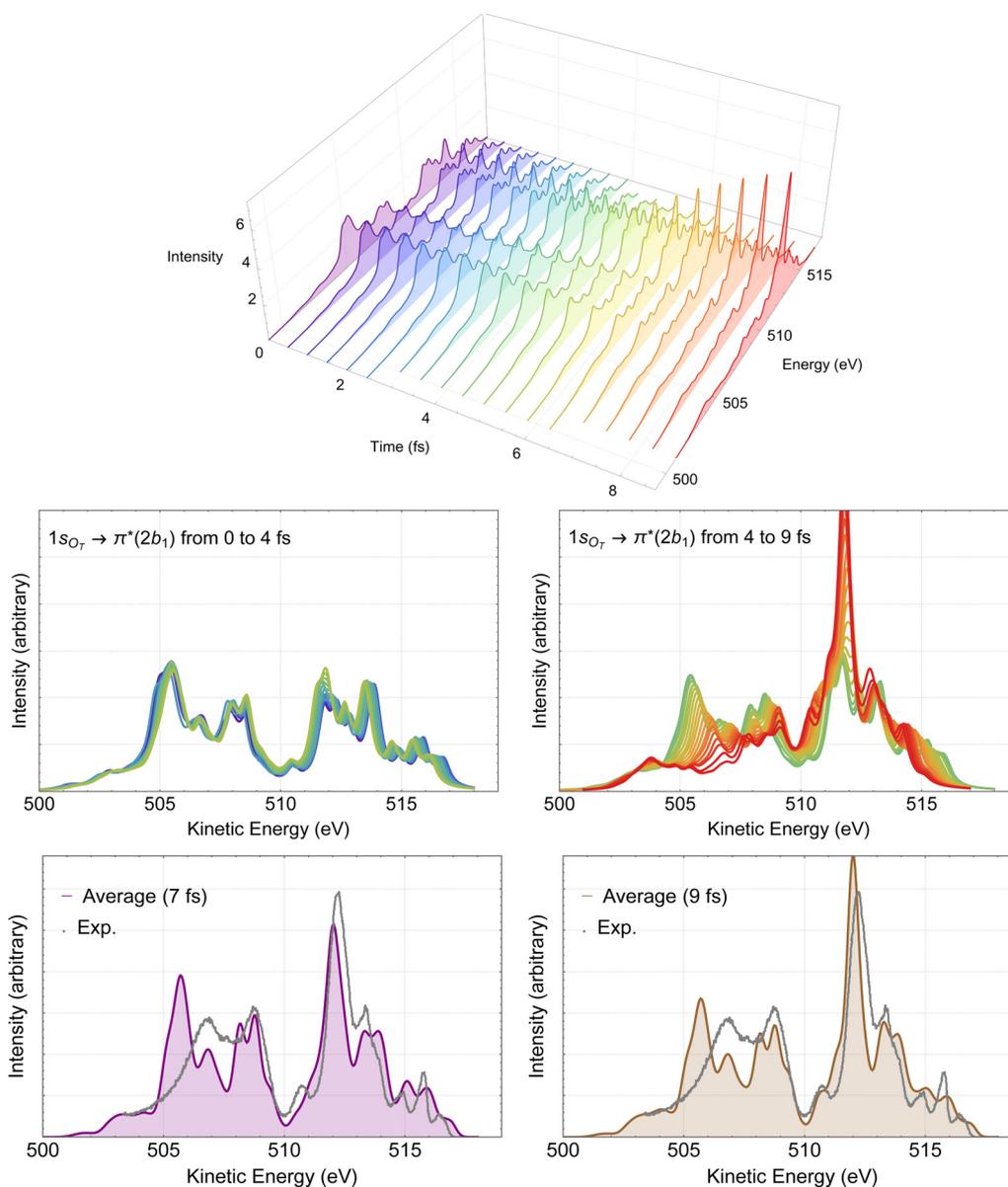


Fig. 7 RAES of O₃ at the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance. The selected trajectory along which the simulation is performed corresponds to the central trajectory represented by the dashed blue curve in Fig. 6. The computed spectra were shifted by -0.6 eV and broadened with Lorentzian functions with $\text{fwhm} = 0.30$ eV. In the top we show the 3D plot of the time-resolved spectra. In the middle, on the left we have the superposition of all spectra up to 4 fs, and on the right, from 4 to 9 fs. In the bottom, we consider the averaged (time integrated) spectra of the central trajectory up to 7 fs (left) and to 9 fs (right), plotted together with the experimental data digitized from ref. 12.



at the few femtoseconds regime is described by our simulations quite decently.

To keep the time-resolved Auger spectra simulation computationally amenable, and to make sure that we are sampling the molecule within the core-hole lifetime, we simulate the first 9 fs along the most central trajectory represented by the dashed blue curve in Fig. 6, using a step size of 0.242 fs.

The time-resolved RAES spectra based on the most central trajectory is presented in details in Fig. 7. In the 3D plot (top panel of Fig. 7) we use a rainbow color code, in which the colors go from violet to red as the time increases. In the middle part of Fig. 7, the calculated spectra up to 4 fs are plotted in the left panel, and the spectra obtained from 4 to 9 fs are plotted in the right panel. Here, it is already possible to make a few comments. Before 4 fs, very little changes compared to the spectrum obtained with Franck–Condon geometry. Only above 4 fs, some meaningful changes in the spectra can be noticed. These observations are in agreement with our previous discussion of the structural parameters. The effect of the dynamics on the Auger spectra is revealed by the peak centered at around 512 eV which starts getting intensity at around 5 fs, and by the features between 505 and 509 eV, that decrease as time evolves. Using the snapshot corresponding to the molecular structure obtained at around 7 fs, we assign the intense peak near 512 eV to two spectator decay channels with the following orbital characteristics: $6a_1^{-1}1a_2^{-1}2b_1^1 + 4b_2^{-1}1a_2^{-1}2b_1^1$ and $1a_2^{-2}2b_1^1$, calculated at 512.56 and 512.70 eV, respectively. The spectrum and the effect of the distorted geometry on the involved molecular orbitals is shown in Fig. S3 (ESI†). At the distorted geometry, the electronic density of the valence molecular orbital $6a_1$ becomes similar to an O 2p orbital localized on the leaving oxygen. The electronic density of the virtual $2b_1$ orbital remains practically unaltered.

The time-integrated spectrum (bottom panels of Fig. 7) is given by the average of all the calculated spectra along the selected trajectory. Here we consider two averages, one obtained integrating on the time up to 7 fs (left panel), and one up to 9 fs (right panel). We observe that both averages agree quite well with each other, as well as with the experiment. Overall, the agreement between these averaged spectra and experiment is much nicer than what we observed at the Franck–Condon geometry, see Fig. 4. Similar analysis based on different trajectories (not shown) yielded very similar characteristics as the ones presented in Fig. 7. Therefore, we suggest that the intense peak around 512 eV, as well as the features between 505 and 509 eV observed in the experimental spectrum are the result of ultrafast nuclear relaxation of ozone following the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance.

Notice that we ruled out ultrafast dissociation as the cause of the increase of the peak at 512 eV since there is no correspondence in the atomic oxygen Auger spectrum matching this energy,⁹⁶ and the dynamics given in Fig. 6 have no indication of bond fragmentation below 10 fs.

In Fig. 8, the computed RAES following the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonance of ozone is presented together with the experimental spectrum.¹³ The calculation was performed at the ground state

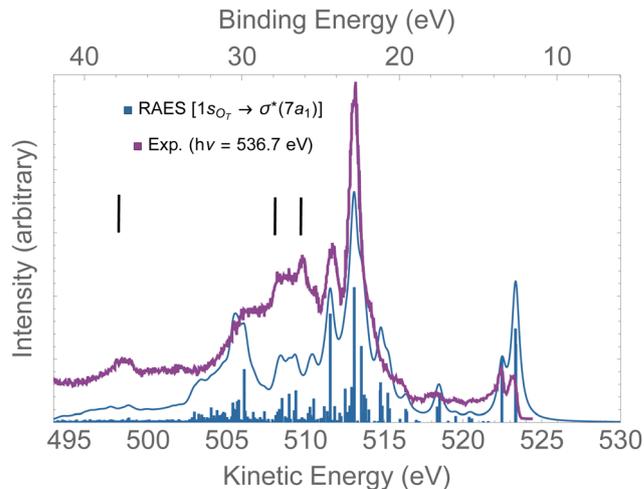


Fig. 8 RAES of O_3 at the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonance. The computed spectrum was shifted by +0.15 eV and broadened with Lorentzian functions with $fwhm = 0.30$ eV. The experimental data were digitized from ref. 13. The black bars indicate the energies of the atomic oxygen Auger decay.

equilibrium geometry. The computed spectrum was shifted by +0.15 eV to better compare with experiment. The computed total decay rate was obtained as $\Gamma = 28.1 \times 10^{-4}$ a.u. As anticipated, the ozone molecule undergoes ultrafast dissociation at the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonance,¹³ which is characterized by the presence of atomic Auger lines together with the molecular Auger features. In Fig. 8, we used black bars to indicate the energies of the atomic oxygen Auger lines corresponding to the multiplets $^4P(498.5$ eV), $^2P(508.4$ eV) and $^2D(510.1$ eV), which values were obtained from ref. 96. The Auger spectrum calculated at the ground state equilibrium geometry shows a nice agreement with the experimental spectrum, except for the features corresponding to purely atomic decay. The first two peaks of the RAES are assigned to the participator Auger decays to the direct ionization channels $6a_1^{-1}(523.2$ eV), $4b_2^{-1}(523.2$ eV) and $1a_2^{-1}(522.3$ eV). The strongest peak observed around 513 eV is assigned to a spectator decay state with mixed configuration [with squared amplitudes] $1a_2^{-2}7a_1^1[0.26] + 4b_2^{-2}7a_1^1[0.21] + 6a_1^{-2}7a_1^1[0.15]$. Notice that the mixed configurations of the cationic state have in common a double hole in one upper valence orbital, and an excited electron in the $\sigma^*(7a_1)$ orbital. In ref. 59, resonant Auger spectra of ozone following core-excitations from the O_T and O_C to a σ^* orbital are reported from a CIS description of the bound states that incorporates post-collision effects by explicitly evaluating the continuum electronic wavefunction. Despite the poor electronic structure description of the bound states given by CIS, which prevents direct comparison with the experimental resonant Auger spectrum, our results are in fair agreement with the findings of the authors.⁵⁹

Overall, for the case of the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ resonant Auger decay, as the dynamics is significantly faster compared to the $1s_{O_T} \rightarrow \pi^*(2b_1)$ state, we then suggest that most of the features exhibited by the experimental measurement¹³ resulted from resonant Auger decay of ozone either around



the Franck–Condon structure, or when the molecule is already dissociated, yielding atomic Auger lines.

In Fig. 9, we investigate the experimental spectrum obtained with photon energy of 542.3 eV.¹³ As we already anticipated, at

that energy one can access both the $1s_{O_C} \rightarrow \sigma^*(7a_1)$ resonance and the $1s_{O_T}^{-1}$ ionization due to the small energy separation between these two states. In the top panel of Fig. 9, we have the resonant Auger spectrum computed for the $1s_{O_C} \rightarrow \sigma^*(7a_1)$ resonance plotted together with the experimental spectrum.¹³ The calculated spectra (resonant and non-resonant) were shifted by +1.3 eV to better compare with the experiment. On the region comprising kinetic energies ranging from 530 to 510 eV, we observe a very good match with the experiment. The intense peak around 504 eV present in the experiment does not come from any contribution observed in the resonant Auger spectrum. However, from the normal Auger spectrum, shown in the middle panel of Fig. 9, we see the intense peak around 504 eV, and nothing in the region between 530 to 510 eV – which was otherwise rich in the resonant decay spectrum. If we now assume that both core-hole states can be accessed equally by the photon flux, we can thus plot the Auger spectrum stemming from the average of both the RAES ($1s_{O_C} \rightarrow \sigma^*$) and AES ($1s_{O_T}^{-1}$). The average spectrum is presented in the bottom panel of Fig. 9. The intensity distribution of the average spectrum approximates quite well the relative intensities of the experimental spectrum, suggesting that our assumption of equal proportions of RAES ($1s_{O_C} \rightarrow \sigma^*$) and AES ($1s_{O_T}^{-1}$) being obtained in the experimental spectrum recorded with photon energy of 542.3 eV¹³ is fairly reasonable.

5 Summary and conclusions

In the present study, we have given insights to and new interpretations of the experimental resonant Auger decay spectra of ozone measured at different regions of the XAS spectrum.^{12,13} Our study is based on a newly implemented RASPT2 one-center-approximation protocol⁵² and on molecular dynamics simulations. For the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonant Auger spectrum, we have demonstrated the relevance of few femtosecond molecular dynamics, specially connected with a prominent feature observed at around 512 eV, emerging after 4 fs from the creation of the core-hole state. The average resonant Auger spectra that includes all snapshots along a selected central molecular dynamics trajectory up to either ~ 7 or 9 fs (that is, compatible with the core-hole lifetime) demonstrate excellent agreement with the experimental spectrum measured with synchrotron light source.¹²

Due to the much faster dynamics of the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ state, we observed that the resonant Auger spectrum obtained at the Franck–Condon geometry compares quite well with the experimental spectrum,¹³ except for a few atomic features. As a consequence of the dynamics of the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ state, the excited molecule initiates an ultrafast fragmentation process, resulting in the possibility of the Auger decay to take place either around the Franck–Condon region, or as dissociated fragments, yielding atomic Auger lines. Our argument agrees with the experimental observations that have demonstrated ultrafast dissociation following the $1s_{O_T} \rightarrow \sigma^*(7a_1)$ state, but not for the $1s_{O_T} \rightarrow \pi^*(2b_1)$ resonance. Additionally, to disentangle the experimental spectrum recorded with a photon energy of 542.3 eV,¹³ that lies above the core ionization threshold

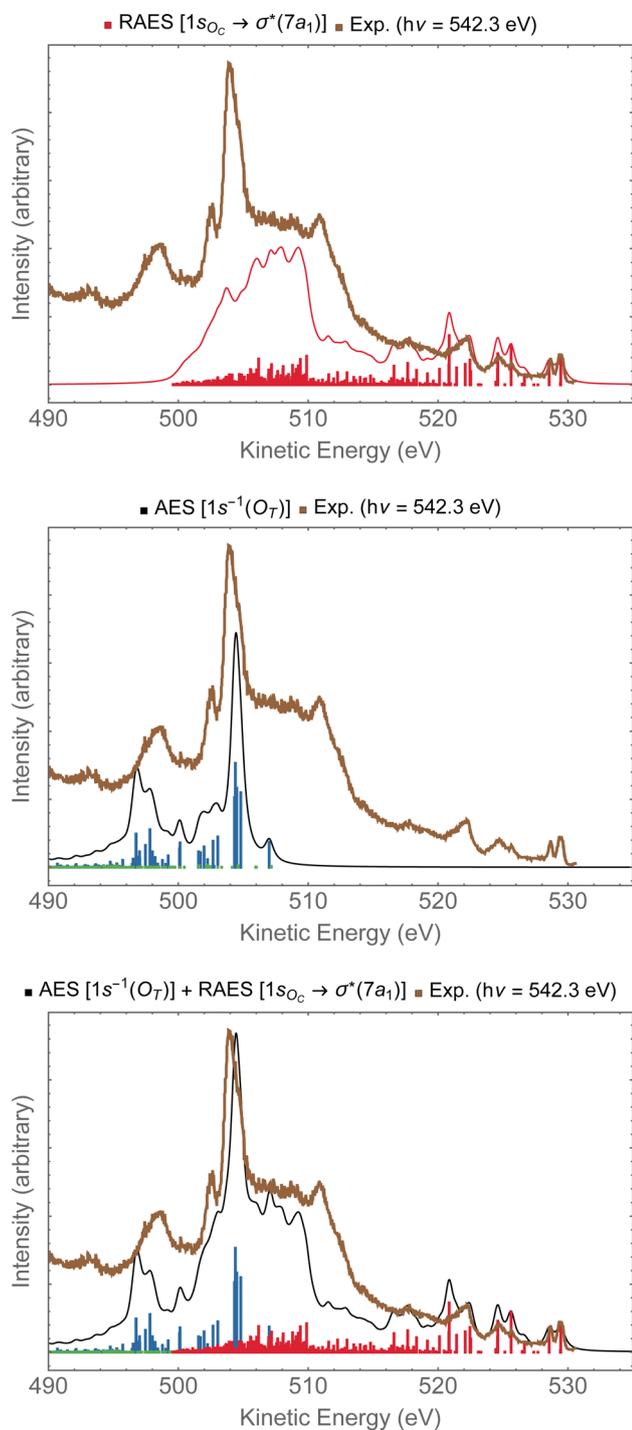


Fig. 9 In the top panel, the RAES of O_3 at the $1s_{O_C} \rightarrow \sigma^*(7a_1)$ resonance is plotted alongside with the experimental spectrum.¹³ In the middle panel, the AES at the $1s_{O_T}^{-1}$ edge is shown. In the bottom panel, the sum of AES and RAES contributions are plotted. The computed spectra (RAES and AES) were shifted by +1.3 eV and broadened with Lorentzian functions with $fwhm = 0.30$ eV. The experimental data were digitized from ref. 13.



of the terminal oxygen, we evaluated the individual contributions stemming from the RAES ($1s_{O_C} \rightarrow \sigma^*(7a_1)$) and AES ($1s_{O_r}^{-1}$) spectra. Assuming that the photon flux can produce a $1s_{O_C} \rightarrow \sigma^*(7a_1)$ excitation or a $1s_{O_r}^{-1}$ core-ionized state with equal probability, we plotted the average spectrum obtained from the RAES and AES together, which shows excellent agreement with the experimental measurement.¹³

Hence, we have obtained accurate Auger spectra based on a cost-effective computational protocol that, thanks to the one-center approximation, simplifies the electronic continuum problem.⁵² In situations where Auger experiments are recorded in a spectral region of overlapping core-hole states, the protocol presented here can give valuable insights to the interpretation of such experiments. Affordable computational protocols like ours are extremely useful for simulating time-resolved Auger spectra, e.g., based on molecular dynamics simulations. In future works, we also plan to incorporate the simulation of ultrashort pump pulses, as the ones used in modern pump-probe experiments,²⁰ to capture manifestation of ultrafast chemistry in the Auger spectrum of excited molecules.

Within the OCA, post-collisional interaction effects and interference between the resonant Auger and direct channels are neglected, since the continuum wavefunction in the molecular environment is not calculated. Another possible limitation of the OCA concerns its ability to properly describe angular distributions. Despite previous work based on the OCA,⁹⁷ one could argue that for an accurate description of angular distribution of the escaping electron, the shape of the continuum wavefunction within the scattering region must be explicitly evaluated. We are currently extending our method to utilize an explicit multicenter Bspline description of the continuum⁶⁷ which will remedy these limitations. The Auger-Bspline approach is, of course, computationally more demanding compared to the cost-effective Auger-OCA method. Hence, the choice between using OCA or the explicit Bspline continuum will depend on the final application.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

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