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1. Introduction

Lime (CaO) and slaked lime (Ca(OH)₂) are essential components for a wide range of industries and applications worldwide,¹ such as steel manufacturing, construction, water treatment, mineral processing, and others. Given its very low toxicity and mild basic properties,^{2,3} Ca(OH)₂ is also widely used in the food industry.⁴ The production of Ca(OH)₂ is currently performed through a two-step process, involving (1) the calcination of limestone to give lime, CaO (eqn (1) and (2))⁵ its subsequent hydration "slaking" (eqn (2)).^{1,6}

$$CaCO_3 \rightarrow CaO + CO_2$$
 (1)

$$CaO + H_2O \rightarrow Ca(OH)_2$$
 (2)



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The decarbonisation of CaCO₃ is essential for the production of lime (Ca(OH)₂ and CaO), which is a commodity required in several large industries and the main precursor for cement production. CaCO₃ is usually decarbonised at high temperatures, generating gaseous CO₂ which will require post-process capture to minimise its release into the environment. We have developed a new process that can decarbonise CaCO₃ under ambient conditions, while sequestering the CO₂ as Na₂CO₃·H₂O or Na₂CO₃ in the same stage. Here, the effects of increasing stirring rates and residence times on reaction efficiency of the key reaction occurring between CaCO₃ and NaOH solution are studied. It is shown that the reaction is enhanced at lower stirring rates and longer residence times up to 300 seconds of contact between the reactants. The mass balance performed for Ca and CO₂ revealed that up to the 95% of the process CO₂ embodied in CaCO₃ was sequestered, with maximum capture rate assessed at *nn* moles CO₂ captured per second of reaction progress. A deeper insight into the precipitation of Na₂CO₃·H₂O or Na₂CO₃ under different reaction conditions was gained, and SEM-EDX analysis enabled the observation of the reaction front by detection of Na migrating towards inner regions of partially-reacted limestone chalk particles.

In the slaked lime manufacturing process, the calcination of limestone represents the most energy-demanding and CO₂ emitting step; it is conducted in several types of firing kilns,¹ and it leads to the release of the process CO2 from the decarbonisation stoichiometry (eqn (1)), and fuel-derived CO₂ by combustion of fossil fuels used to heat the kiln to provide the firing temperature required (between 800 and 1200 °C).^{7,8} The following step 2 (eqn (2)) mainly requires electrical energy input, to handle and mix the reactants and products of this exothermic hydration process.¹ Therefore, the efficiency linked to the energy usage within a given kiln plays a crucial role in defining the overall sustainability of the process; multiple factors may influence the energy input and the resulting efficiency for a given kiln type, such as the quality and the particle size of the limestone feed, the degree of conversion desired, and the moisture.⁹ About 1.0–1.8 kg of CO₂ are emitted per kg of lime produced,¹ and given the worldwide annual production (over 70 Mt in 2020¹⁰), the lime industry is a significant emitter of greenhouse gases (GHG) which are the main contributors to global warming.

Intense efforts and significant investment from this industry are needed to mitigate the emissions of CO₂ to the atmosphere.

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Considering the calcination of limestone in a broader sense, such a process is also the basis of the Portland cement production industry; over 6 Gt of limestone are annually processed to satisfy the cement market (over 4 Gt in 2018^{11}), resulting in about 3–4 Gt of CO₂ emitted from chemical and fuel contributions combined ($\approx 4\%$ of the total anthropogenic emissions^{12,13}). Given the size of both the lime and cement market worldwide, the validation of a more sustainable limestone decarbonisation route would be a significant contribution to meet the goal (overall 86% CO₂ emissions cut by 2050) set and agreed by the United Nations.^{8,14,15}

Our previous work demonstrated the technical feasibility of an alternative route to decarbonisation of limestone, achieved at ambient conditions without heating.¹⁶ The process is based on the reaction between CaCO₃ particles and highly concentrated NaOH solutions to produce Ca(OH)₂ and Na₂CO₃·H₂O or Na₂CO₃, allowing for the decarbonisation directly from the solid limestone and simultaneous sequestration of CO₂ into stable mineral forms (eqn (3)).

$$CaCO_3 + 2NaOH + xH_2O \rightarrow Ca(OH)_2 + Na_2CO_3 \cdot xH_2O (x = 0, 1)$$
(3)

This process is particularly beneficial because it does not require the combustion of fuels and avoids the associated CO_2 emissions, while the process CO_2 embodied in $CaCO_3$ is sequestrated as Na_2CO_3 ·H₂O or Na_2CO_3 . Our previous study also highlighted the feasibility of applying this process to impure industrial grade limestone with significant silica content.¹⁶

It is well known that the overall reaction rate in heterogeneous systems would depend on the reaction rate of the involved chemical reactions and the thickness of the product surface layer,¹⁷ according to the un-reacted core model.^{18,19} Both the residence time and the mixing rate might affect the reaction kinetic, since a longer contact between the reactants and a higher turbulence would generally enhance the efficacy of a reaction. It is also true that a greater centrifugal force on the solid particles compared with the liquid phase may also affect the overall reactivity of the components,²⁰ due to a separation of the phases resulting in a lower contact surface.²¹⁻²³ Given that, this work aims to clarify the dependence of the system studied on the stirring rate and residence time, in order to optimise the process with a view toward its industrialisation. It must be mentioned that such a study only represents a preliminary step towards the scaleup of the process, which needs to take into account evident technical difficulties before considering industrial applicability. These issues are mainly linked to the handling of highly-corrosive NaOH solutions, the management of chlorine gas deriving from the enhanced production of the required chemical NaOH, and the adjustment of the processing conditions in accordance with the scaling-up. Although, the liquid stream from the solid chlor-alkali process is a \approx 32 wt% NaOH solution (approximately 12 M),²⁴ comparable with the concentrations used here. Moreover, the excess of chlorine gas may be water scrubbed, and the resulting solutions may be used for the production of Cl-containing cements²⁵ for non-reinforced concrete. Considering that over

the 60% of the concrete worldwide is unreinforced,²⁶ significant proportions of the toxic chlorine gas from the chlor-alkali process might be immobilised upon cementation. Despite the title study aims to investigate the effect of crucial processing conditions, the authors are fully aware that the presented outcomes might fail in representing the system behaviour at larger scale. Although, this preliminary investigation offers that fundamental basic starting point for a more detailed investigation targeting the proper scale-up of the process.

The present study also aims to clarify the equilibrium between the species Na₂CO₃·H₂O and Na₂CO₃ at the processing conditions considered, since the co-production of Ca(OH)₂ and Na₂CO₃·H₂O implies the need for a following separation of the products, crucial for their individual sale or use, not discussed here. For instance, high Na contents (above 2 wt%) would prevent the use of Ca(OH)₂ for cement production,^{27,28} limiting the applicability of this novel technology. Since the solubility of the different species here involved would likely play a key-role for their effective separation, the present study also assessed the precipitation of the by-product Na₂CO₃·H₂O or Na₂CO₃ (x = 0, 1 in eqn (3), respectively) depending on the reaction conditions used. Finally, solid particles of an industrial grade chalk are reacted to quantify the reaction progress by visual tracking of the products surface layer *via* SEM-EDX analyses.

Materials and methods

2.1. Materials

The materials used in this work included commercial grade chemicals: Sigma-Aldrich CaCO₃ (\geq 99%) and Honeywell Fluka NaOH (\geq 97%). Additionally, the same industrial grade chalk used in a previous study were also considered as a source of CaCO₃;¹⁶ the oxide elemental composition is reported in Table 1 below. A dry-state Particle Size Distribution (PSD) analysis was chosen for targeted samples, in order to avoid the dissolution of the solids at any extent. About 10 g of material was used for the analysis, and the value reported for each sample is an average of 10 consecutive measurements.

2.2. Experimental procedure

Given the high conversion extent observed in a previous study¹⁵ for the ternary system of 27.1 wt% CaCO₃, 32.4 wt% NaOH, and 40.5 wt% H₂O, this starting composition was considered in the following experiments to assess the effect of varying selected parameters on the reaction efficiency. First, NaOH was mixed with distilled water, resulting in a temperature increase of the system to ~80 °C due to the exothermic dissolution reaction. The solutions were then heated to 90 °C in a PTFE beaker with a volume of 6.5 cm³, to achieve an identical initial temperature

Table 1	Elemental oxide composition (wt%) of the solid chalk used in the					
present work, including Loss On Ignition (LOI%) value						

	CaO	SiO_2	Al_2O_3	Fe ₂ O ₃	K ₂ O	MgO	Others	LOI%
Wt%	44.0	21.0	3.0	1.1	0.6	0.3	<2.0%	29.5

for all experimental runs; following this, 10 g of CaCO₃ were introduced and no further temperature control was applied as the reaction was allowed to progress under laboratory ambient conditions ($T \approx 20$ °C). To ensure mixing, a PTFE centrifugal stirrer shaft (flat propeller, diameter 4 cm) was used with a Heidolph RZR 2020 overhead mixer, rotating in the bottom centre of the PTFE beaker. The use of PTFE was essential to avoid corrosion that may be caused by the hyper-alkaline NaOH solutions used. To study the effect of the mixing rate on the reaction efficiency, a series of experiments were carried out at each of 40, 300, 500, 800 and 2000 rpm for durations of 30, 300, 720, and 1200 s. The conditions used for each sample are reported in Appendix. After the desired duration of reaction, 50 mL of methanol was added and the whole paste was stirred for 300 s to wash by dissolving any unreacted NaOH (NaOH solubility in methanol = 238 g L^{-129}). The very low solubility of Ca(OH)₂,³ CaCO₃,³⁰ Na₂CO₃·H₂O,³¹ and Na₂CO₃³¹ in methanol allows these solids to remain in the system without being lost during the washing.

The reagent grade chalk was reacted at slightly milder mixing regime, to better preserve the condition of the products. The reaction was performed in a plastic vessel with a magnetic stirring of 300 rpm for a total residence time of 300 s. 8.4 g of NaOH were added into 12.3 g of H_2O to form 17 M NaOH solution, and the solution was cooled down to room temperature before adding 2.5 g of chalk, making the initial system of H_2O (54.7 wt%), NaOH (37.2 wt%) and chalk (8.1 wt%). A significantly high water-to-solid ratio was chosen to ensure a satisfactory mixing of all the reactants, with the less energetic stirring; anyway, the chosen composition has been tested on reagent grade CaCO₃ already, and it led to an almost total conversion to products.¹⁶ After five minutes of reaction, 32 mL of methanol was added to the resulting paste and stirred for five minutes in order to remove any remaining NaOH.

Following their collection by vacuum filtration, all the solid products here discussed were dried in an 80 °C oven for 2 hours; following, the samples selected for TG and XRD analyses were finely ground and sieved below 63 µm. For the SEM analysis, selected samples were ground or not, to observe the targeted parameters discussed below.

2.3. Characterisation techniques

2.3.1. X-ray diffraction (XRD). X-Ray diffraction (XRD) was used to qualitatively identify the reaction products of the reaction. The analysis was conducted by using a Bruker D2 PHASER desk-top X-ray diffractometer in Bragg–Brentano geometry, with a Cu-K α radiation source running at 30 kV and 10 mA, a one-dimensional LYNXEYE detector, and a 1 mm divergence slit. All the samples were powders, and they were loaded onto sample holders with a diameter and depth of 2.5 cm and 1 mm, respectively. All the analyses were conducted between 5° and 80° 2 θ , with a step size of 0.02° at 0.5 seconds per step; the stage was set to rotate at 15 rpm. Qualitative phase identification was carried out using the Highscore-Plus software and the PDF-4 2019 database.

2.3.2. Thermogravimetry (TG/DTG). Thermogravimetric analysis (TGA) was carried out by sampling about 40 mg of

products to be analysed on a PerkinElmer TGA 4000 from 30 °C to 800 °C at a heating rate of 10 °C min⁻¹ with a 40 mL min⁻¹ N₂ flow. The temperature was kept at 800 °C for 1 hour to ensure complete loss of CO₂ from CaCO₃. To identify evolving gases, a Hiden mass spectrometer (HPR-20 GIC EGA) was used to record the signals for H₂O and CO₂, the only gases involved here. The reaction efficiency α , only reflecting the fraction of CaCO₃ converted to Ca(OH)₂, was calculated from the weight loss in the temperature ranges for the thermal decomposition of Ca(OH)₂ (310–470 °C³²) and CaCO₃ (560–800 °C³³), as reported in Fig. 1 and eqn (4).

$$\alpha = \frac{\frac{\frac{w\% [Ca(OH)_{2}]}{MW_{Ca(OH)_{2}}}}{(\frac{w\% (Ca(OH)_{2})}{MW_{Ca(OH)_{2}}} + \frac{w\% [CaCO_{3}]}{MW_{CaCO_{3}}})}$$
(4)

The content of Na₂CO₃·H₂O could similarly be estimated from mass loss in the temperature range 50–130 °C³⁴ (Fig. 1). The measurement was repeated 6 times for each sample to estimate the measurement error (± 0.16 wt%, ± 0.10 wt% and ± 0.16 wt% for Na₂CO₃·H₂O, Ca(OH)₂ and CaCO₃, respectively).

2.3.3. Scanning electron microscopy (SEM). A Hitachi TM3030 scanning electron microscope with energy-dispersive X-ray spectroscopy (SEM-EDX) was used to gain a deeper insight on the penetration of sodium upon reaction. The solids were mounted in epoxy resin without crushing and left to harden for 72 hours. The analysis surface was ground and polished with progressively finer abrasives, up to a 1 μ m finish;³⁵ in addition, the samples were polished on cashmere polishing cloths by using diamond pastes of 6, 3, 2, 1 and 0.25 μ m (MetPrep). The samples then underwent a three-step carbon coating and were back-loaded to a metallic holder. Electrically conductive silver paint (RS Components) was applied at the metallic base-epoxyresin interface to ensure sufficient conductivity and good quality of the SEM images, collected at a working distance of



Fig. 1 Generic temperature-trend from the TG (wt%) and DTG data (dw%/ dt), showing the weight loss events of the sample associated with: Na_2CO_3 ·H₂O (A), Ca(OH)₂ (B), and CaCO₃ (C).

 7.4 ± 0.1 mm. Separately, selected samples were crushed and sieved to targeted size ranges and attached to conductive carbon adhesive tapes (Agar Scientific).

3. Results and discussion

3.1. Reaction products

The system under consideration shows a good capability to convert CaCO₃ to Ca(OH)₂, Na₂CO₃·H₂O, and Na₂CO₃;¹⁶ here, the series of samples mixed at 300 rpm for all the residence times considered was taken as a representative baseline. The XRD analysis (Fig. 2) showed the presence of only CaCO₃, Ca(OH)₂, Na₂CO₃·H₂O and Na₂CO₃, with respective main reflection angles 2θ of 29.5° , 18.1° , 17.1° , and 30.2° , within the solid products.

Specifically, the intensity of the peaks linked to $Ca(OH)_2$ and $Na_2CO_3 \cdot H_2O$ was increasing at longer residence times, while $CaCO_3$ content appeared to decrease; in addition, the signals linked to Na_2CO_3 could be detected at residence times of up to 300 seconds, while at longer ones those were not observable. The relative proportions of $Na_2CO_3 \cdot H_2O$ and Na_2CO_3 will be discussed in detail in Section 3.3.

In accordance with the XRD outcomes, the TG/dTG analysis of the same baseline samples (Fig. 3) showed increasing weight losses in the temperature intervals 50–130 °C and 310–470 °C, referring to Na₂CO₃·H₂O³⁴ and Ca(OH)₂, ³² respectively, and a decreasing CaCO₃ content (560–800 °C³³) at longer residence times.

The quantification of phases from the TG analysis (Fig. 3) is reported in Fig. 4A. The amount of Na_2CO_3 could not be directly quantified, since its thermal decomposition would occur above 851 °C³⁶ and the analysis was conducted up to 800 °C. However, the quantification of Na_2CO_3 could be performed indirectly by taking into account the difference between the total (100%) and the sum of the other phases (CaCO₃, Ca(OH)₂, and $Na_2CO_3 \cdot H_2O$). This approach could be considered reliable, since the XRD analysis confirmed the presence of the only phases CaCO₃, Ca(OH)₂, $Na_2CO_3 \cdot H_2O$, and Na_2CO_3 in the solid system (Fig. 2).



Fig. 2 XRD patterns of the samples obtained at 300 rpm for all the residence times investigated, highlighting the peaks of all the species detected.



Fig. 3 TG and dTG analysis performed on the baseline series 500rpm_30-1200 s, showing the weight losses in the regions 50-130 °C, 310-470° and 560-800 °C which are assigned to Na₂CO₃·H₂O, Ca(OH)₂ and CaCO₃, respectively. The black arrows clarify the axes referred to the data shown.

The XRD analysis also suggested the absence of any amorphous phase since no raised baseline was detected in any pattern (Fig. 2). In addition, the weight uptake resulting from the incorporation of Na⁺ and OH⁻ ions from the solution may be used as a further confirmation of the phases detected by XRD and their quantification by TG. This value was calculated for each system by considering the ratio between the final measured weight of the dried products and the initial weight of CaCO₃. The weight uptake can represent the extent of reaction, assuming that any residual NaOH is removed from the system after washing. Such an assumption appeared to be confirmed by the absence of the NaOH characteristic peak at $2\theta = 16^{\circ 37}$ in the XRD analysis reported in Fig. 2. Fig. 4B shows the experimental weights registered for the representative series of samples, together with the theoretical lines that would result from the quantitative precipitation of Na2CO3·H2O or Na2CO3.

3.2. Effect of stirring rate

The characterisation performed on all samples allowed for the determination of the effect on the reaction extent linked to the stirring rate. A Ca mass balance was performed for all the samples discussed here, in order to validate the results from TG analysis; the difference between the inbound (CaCO₃) and outbound (Ca(OH)₂ and CaCO₃) calcareous species was considered to do that, revealing oscillations of ± 0.2 g of Ca. The Ca mass balance supported the TG analysis, and the specific values for each sample discussed is reported as ESI,[†] alongside an overview of the samples phase compositions gained by TG analysis. The XRD analysis was qualitatively reflecting the quantification performed, considering the decreasing intensity of the main peak related to CaCO₃ at $2\theta = 29.5^{\circ}$ at longer, whereas those related to the products Ca(OH)₂, Na₂CO₃·H₂O, and Na₂CO₃ were increasing in intensity (Fig. 5).

The TG quantification reported in Fig. 6 shows the highest conversion at a stirring rate of 40 rpm, while significant

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Fig. 4 Phase compositions of the samples reacted at 300 rpm at increasing residence times (A); trend of the weight uptake experimentally observed as a function of conversion (black labels), with lines indicating the relationships that would have been observed if the sodium carbonates were present solely as $Na_2CO_3 \cdot H_2O$ (red line), or solely as Na_2CO_3 (blue line) (B).

efficiency drops were observed at 2000 rpm. The loss of efficiency at increased stirring rate was most notable in those samples reacted for 30 seconds, with an efficiency drop of 34.1% between 40 and 300 rpm observed for this residence time; the impact was reduced at increasing ones. Generally, the increase in reaction extent above 300 seconds was limited.

These outcomes might be justified by physical reasons, as mentioned in Section 1, linked to the significantly different density of a 45 wt% NaOH solution ($1.42-1.48 \text{ kg dm}^{-3.38}$) and the reagent grade CaCO₃ ($2.93 \text{ kg dm}^{-3.39}$). That would be expected to cause a net separation of the liquid and solid phases within the paste at higher stirring rates due to centrifugation effects, leading to a lower contact between the reactants^{21–23} and a resulting hindered conversion, as shown in Fig. 7.

Alternatively, the lower conversion registered at higher stirring rates may be linked to the main mechanism ruling the reaction progress; several models were considered, including diffusion, and contracting volume or surface, but a nucleation mechanism was strongly suggested. Fig. 8 shows the fitting



Fig. 5 XRD patterns for the samples reacted for 300 seconds as a function of stirring rate.



Fig. 6 Conversion extents obtained at each residence time and stirring rate investigated.

between the whole set of experimental data reported here and the nucleation model proposed by Avrami–Erofeyev;⁴⁰ it is reflected in eqn (5), where *k* and α identify the kinetic constant and the conversion extent of the reaction, respectively and its integrated form (eqn (6)).

$$f(\alpha) = \left(\frac{1}{k}\right) \left(\frac{\delta\alpha}{\delta t}\right) = 3(1-\alpha) \left[-\ln(1-\alpha)\right]^{\frac{2}{3}}$$
(5)

$$g(\alpha) = [-\ln(1-\alpha)]^{\frac{1}{3}} = kt$$
 (6)

While α was calculated from eqn (4), the kinetic constant *k* was obtained by dividing α for the residence time considered; doing this, the kinetic related to the conversion of CaCO₃ to Ca(OH)₂ could be outlined, whereas the formation of Na₂CO₃·H₂O and Na₂CO₃ was not taken into account here. The decarbonisation



Fig. 7 Schematic representation of the partition occurring between the solid (CaCO₃) and liquid (NaOH sol.) phases at increasing centrifugal force (F_c) or stirring rate.



Fig. 8 Fitting between the experimental data for all the samples here discussed and the Avrami–Erofeyev nucleation model represented by eqn (6); the samples were grouped according to the stirring rate used, and R^2 values are highlighted for each one.

rate was significantly decreasing after 30 seconds of reaction, when a maximum rate of 2.7×10^{-3} moles of CaCO₃ converted

per second was achieved at 40 rpm, over the double than the kinetics observed at 2000 rpm (1.2 moles $CaCO_3 s^{-1}$). The slower kinetics registered at different rates confirms the need for a precise optimisation aiming to an eventual scale-up.

Given the heterogeneous reaction taken into account here, a nucleation mechanism involves the primary formation of small crystals of the new product phase within large ones of the reactant; this process is thermodynamically unfavourable at first, given the higher free Gibbs energy ΔG^{41} linked to the instability of the nuclei formed.⁴² Upon achievement of a critical size, the nucleus assumes a more stable configuration, while expanding and incorporating other potential nuclei; nucleation continues until the progression front covers the whole surface of the solid. From here, the nucleation kinetic lowers because of the surface product layer which reduces the contact surface between the reactants.

The effect of stirring rate on the nucleation density and crystal morphology has been empirically accepted in chemical and cast metals industries,⁴³ and the role of convection in single crystals forming has been widely discussed already.^{44,45} Generally, the studies report an enhanced nucleation density in dynamic conditions with respect to static ones,⁴⁶ leading to shorter residence times required.47 Taking into account the high R^2 values reported in Fig. 8 in correlation with the Avrami-Erofeyev model, the present study would introduce controversial outcomes at first sight. In fact, nucleation appears to be hindered at higher stirring rates, when the collisions between the reactants and the formation of surface irregularities and cracks should statistically be more frequent. Such a controversial observation might be likely explained by considering an enhanced partition of the solid and liquid bulks at higher stirring rates,²² preventing further contact and reaction progression (Fig. 7). In other words, despite the higher turbulence, the entropy of the system would lower as a consequence of the hindered contact between solid and liquid reactants, reflecting a higher ΔG at faster stirring rates. Such an effect could be furtherly increased by the eventual distorted expansion of the



Fig. 9 Schematic representation of the nucleation front progression (grey pattern) occurring at high (left) and low (right) stirring rates.

nuclei undergoing axial centrifugal forces F_c ,⁴⁸ as also outlined in Fig. 9.

3.3. Equilibrium between Na₂CO₃·H₂O and Na₂CO₃

As mentioned in Section 1, an effective separation of the products will be required upon reaction, and it may likely involve their dissolution in water or solvent. The separation would likely exploit the different solubility of $Ca(OH)_2$, Na_2CO_3 . H₂O, and Na₂CO₃, and the understanding of the equilibrium between Na₂CO₃·H₂O and Na₂CO₃ could dictate the optimal processing conditions. The proportioning of Na2CO3·H2O and Na₂CO₃ at different stirring rates and residence times has been here assessed, and useful information has been provided for an eventual scale-up of the process. Together with the phase quantification performed by TG, the XRD analysis confirmed the enhanced formation of Na₂CO₃·H₂O with respect to Na₂CO₃ up to a stirring rate of 800 rpm (Fig. 5) and at increasing residence times (Fig. 2). To gain further insight, the behaviour of Na₂CO₃·H₂O and Na₂CO₃ in the Na₂CO₃-NaOH-H₂O system was studied using PHREEQC - PH REdox EQuilibrium (in C language), a geochemical modelling software simulating a variety of reactions and processes at equilibrium,49 in particular focusing on the activity of water. The simulation was performed at 20, 60 and 100 °C; both Na₂CO₃·H₂O (0.1 mol) and Na₂CO₃ (0.1 mol) were initially introduced into 100 mL of pure water, and NaOH was added in successive steps up to 20 M; given the high NaOH concentrations taken into account, the Pitzer model was used here.⁵⁰ The Na₂CO₃·H₂O and Na₂CO₃ phases were specified by the equilibria reported below in eqn (7) and (8), respectively, while the total 2 moles of NaOH additions were performed in 20 steps up to a molality of 20 (2 moles NaOH in $0.1 \text{ kg H}_2\text{O}$).

$$Na_{2}CO_{3} + H^{+} \leftrightarrow HCO_{3}^{-} + 2Na^{+} \quad \log_{k} = 11.2$$

$$_{2}CO_{3} \cdot H_{2}O + H^{+} \leftrightarrow HCO_{3}^{-} + 2Na^{+} + H_{2}O \quad \log_{k} = 10.9$$
(8)

Precipitate compositions were then determined as a function of water activity, Fig. 10B, where the highest concentrations of NaOH correspond to the lowest calculated water activities (Fig. 10A). The simulation revealed the favourable ranges of the activity of water (aH_2O) for the precipitation of Na₂CO₃·H₂O (0.6 < aH_2O < 0.8) and Na₂CO₃ (aH_2O < 0.6), as shown in Fig. 10B. Increasing NaOH concentrations would lead to a higher viscosity^{51,52} while the activity of water would be significantly reduced^{53–55} (Fig. 10A).

Additionally, given the stoichiometry of the reaction (eqn (3)), and considering the concentration of dissolved Ca^{2+} to be negligible under these highly alkaline conditions due to the limited solubility of Ca(OH)₂, the final OH⁻ concentration would depend on the consumption of NaOH to convert CaCO₃ to products. In other words, a higher conversion would lead to lower final OH⁻ concentrations, as outlined by the experimental data reported in Fig. 11.

Following the quantification of the solid phase species within the system, the molar proportion of Na_2CO_3 ·H₂O formed



Fig. 10 PHREEQC simulation showing (A) the activity of water as a function of NaOH molalities at 20, 60 and 100 °C in a system with 100 g, 106 g, and 124 g of H₂O, Na₂CO₃·H₂O, and Na₂CO₃, respectively, and (B) precipitated moles of Na₂CO₃·H₂O and Na₂CO₃ at 20, 60 and 100 °C; the initial NaOH concentration of the solutions used for this set of samples is labelled as C₀.



Fig. 11 ν_{\approx} Na₂CO₃·H₂O values and final OH⁻ concentration, experimentally determined as a function of conversion.

Na

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in the binary system Na₂CO₃·H₂O/Na₂CO₃ can be calculated. Doing this, it was possible to observe that Na₂CO₃ was dominantly forming at the early stage of the reaction (or when the progress of the reaction is limited) because of the low activity of water due to the high concentration of NaOH in the system (Fig. 11). However, as the reaction progresses, the formation of Na₂CO₃·H₂O may have been enhanced by the rising H₂O activity due to the consumption of NaOH, as shown in eqn (3). This would explain the higher contents of Na₂CO₃ in the systems with a limited progress of the reaction, corresponding to shorter residence times (Fig. 4A) or faster stirring rates (Fig. 5). These outcomes are in accordance with the thermodynamic trends reported in Fig. 10B.

3.4. CO₂ capture

The quantification of Na₂CO₃·H₂O and Na₂CO₃ also allowed to calculate the fraction of CO₂ trapped out of the initial amount introduced as CaCO₃, and to outline the CO₂ capture rate. Eqn (9) outlines the mass balance for CO₂ upon reaction, taking into account the initial CO₂ introduced with CaCO₃ (gCO_{2,Initial}), the fraction of CO₂ captured through precipitation of Na₂CO₃·H₂O and Na₂CO₃ (gCO_{2,Captured}), and the CO₂ embodied into unreacted CaCO₃ (gCO_{2,Unreacted}). These parameters were calculated by taking into account CO₂ fractions of 44.0 wt%, 35.5 wt% and 41.5 wt% for CaCO₃, Na₂CO₃·H₂O, and Na₂CO₃, respectively, apart from the sample-specific phase assemblage.

$$gCO_{2,Initial} - gCO_{2,Captured} = gCO_{2,Unreacted}$$
 (9)

Approximately 4.4 g of CO₂ are embodied into the initial 10 g of CaCO₃ powders reacted, and for all the samples the mass balance depicted in eqn (9) was respected with uncertainties of ± 0.1 g. That may be observed in Fig. 12A, where $gCO_{2,Captured}$ and $gCO_{2,Unreacted}$ are plotted against the residence time for all the samples discussed. It is clear that the reaction between CaCO₃ and NaOH leads to the prompt immobilisation of the

process CO₂ upon precipitation of Na₂CO₃·H₂O and Na₂CO₃ (Fig. 12A). The rate of CO₂ capture, expressed as mol_{CO_2} captured s⁻¹, was reflecting the cumulative precipitation rate of Na₂CO₃·H₂O and Na₂CO₃; it is formulated in eqn (10), where the subscripts for the variable *t* indicate the consecutive intervals considered.

$$k_{\text{CO}_2 \text{ Captured}} = \frac{\left[\left(g \text{CO}_{2,\text{Captured}} \right)_{t_{n+1}} - \left(g \text{CO}_{2,\text{Captured}} \right)_{t_n} \right]}{(t_{n+1} - t_n)} \quad (10)$$

The capture rate *k*, plotted as $-\ln k$ in Fig. 12B, was decreasing for all the samples at longer residence times, in line with the limited reaction extent registered above 300 seconds (Fig. 6). The highest CO₂ capture rate $(2.7 \times 10^{-3} \text{ mol}_{\text{CO}_2} \text{ s}^{-1})$ was registered for the sample reacted at 40 rpm for 30 seconds, and a 94% CO₂ capture was achieved after 720 seconds of reaction progress at the same stirring rate. The high resemblance with the trends reported in Fig. 6 suggest that the precipitation of Ca(OH)₂ does not affect the trapping of the process CO₂ into Na₂CO₃·H₂O nor Na₂CO₃, and also reflecting a high accordance to the stoichiometry depicted in eqn (3).

3.5. Decarbonisation of industrial grade chalk

Chalk with larger particle sizes were subjected to the same reaction, and the size of the reacting solids was chosen upon sieving. The dry PSD analysis revealed a much higher mean particle diameter (Dx(50) of 1.29 mm, Fig. 13B) respect with the reagent grade $CaCO_3$ (Dx(50) of 26.6 µm, Fig. 13A); during the analysis, weighted residual and laser obscuration of 3.25% and 2.97%, respectively, were registered. Additionally, both XRF (Table 1) and TG analyses were performed on the solids, upon fine grinding and sieving below 38 µm.

Fig. 14 shows the outcomes of the XRD analysis performed on the ground products; the peaks related to the products $Ca(OH)_2$, $Na_2CO_3 \cdot H_2O$, and Na_2CO_3 could be observed in the



Fig. 12 Trends of $gCO_{2,Captured}$ and $gCO_{2,Unreacted}$ at increasing residence times registered for all the samples discussed here (A); CO₂ capture rate (mol_{CO2} Captured s⁻¹) calculated for all the samples from eqn (10) (B).



Fig. 13 Dry-state Particle Size Distribution (PSD) analysis was performed on reagent grade CaCO₃ (A) and industrial grade chalk (B); ten measurements per sample were performed, and the average value was considered.

reacted solids, together with a slight reduction in intensity of CaCO₃.

The TG analysis (Fig. 15) reported a total 30.6 wt% loss for the sample, and the extent of reaction α was estimated to be 0.3, given the contents of CaCO₃ (53.8 wt%) and Ca(OH)₂ (17.4 wt%). A 2.3 wt% loss observed in the temperature range of 50–130 °C, likely referring to the dehydration of Na₂CO₃·H₂O, whose content was estimated to be 16 wt%.

The XRD analysis could also reveal traces of Na_2CO_3 , which could not be reliably quantified by TG (Section 3.1) because of the significant presence of impurities (Table 1); for the same reason, it was not possible to reliably assess the proportioning between Na_2CO_3 ·H₂O and Na_2CO_3 . It must be mentioned that the large particle size here would significantly affect the yield of the reaction, by largely decreasing the contact surface between the liquid and solid reactants. The DTG curve also shows a small shoulder at 802.7 °C. Based on the XRD analysis (Fig. 14), this could be assigned to the decarbonisation of vaterite, a metastable



Fig. 14 XRD patterns of the reacted and unreacted industrial grade chalk, with labelled phases $cCaCO_3$ (calcite), $Ca(OH)_2$, $Na_2CO_3 \cdot H_2O$, Na_2CO_3 and $vCaCO_3$ (vaterite).



Fig. 15 TG (black line) and DTG (red line) trends for the industrial grade chalk reacted here, highlighting the key temperature ranges and the corresponding weight losses observed.

polymorph of calcite which is often observed during the synthesis of precipitated calcium carbonate,^{56–58} and which is seen in the XRD results for the reacted sample in Fig. 14. Fig. 16A–F show the SEM analysis performed on two representative samples taken from the reacted and unreacted chalk solid particles. As expected, Na could only be detected in the reacted particles (Fig. 16B), in line with the formation of Na₂CO₃·H₂O or Na₂CO₃, and higher signals were detected towards the external sections of the solid bead; such a detail will be discussed below, where the EDX analysis of a large number of reacted solid particles is taken into account. Here, the EDX quantification of Na was performed with the software Quantax-70 by considering internal and external sections of the solid particles, chosen by taking into account the Na mapping in Fig. 16B, which highlights a sharp change in Na concentration at a depth of about 200 μ m.

Specifically, sodium contents of 18.92 wt% and 7.32 wt% were detected in the external and internal sections of the



Fig. 16 SEM images of two representative reacted (A) and unreacted (C) solid chalk particles, with respective Na mapping (red highlighted) in (B) and (D), where the external (Ext) and internal (Int) areas discussed in the body text are displayed in white. Dispersive X-Ray (EDX) analysis performed on the (E) unreacted and (F) reacted chalk particles, with maps of the elements Na, Si and Ca.

reacted particle, respectively, whereas negligible sodium contents (0.01-0.06 wt%) could be observed in the unreacted chalk. In any case, the sodium peak seen in Fig. 16B and D is reflected in Fig. 16E and F, where the EDX analysis showed Na signals around 1 keV; as observed, no signals linked to Na could be detected for the unreacted particle, while a significant gap was observed between the external and internal sections of the reacted one. Moreover, rather homogeneous distribution of Ca (Fig. 17C, D and 18C, D) is observed, with slightly higher contents in the internal regions respect with the external ones. That is an expected result, since the stoichiometry of the reaction would lead to an overall weight increase given the reactant (CaCO₃) and products (Ca(OH)₂, Na₂CO₃·H₂O, and Na₂CO₃) involved (Section 3.1 and Fig. 4B). Despite Ca should not be lost from the solid surface throughout the reaction, as outlined from the Ca mass balance in ESI,† the uptake of sodium would result in a final lower Ca proportion in those local regions where the reaction occurred more extensively. As previously mentioned, the particles undergoing SEM analysis were grouped into two sets by their size: $700 \le D \le 1000 \,\mu\text{m}$ and $400 \,\mu\text{m} \le (D) \le 700 \,\mu\text{m}$.

In both groups, higher contents of Na could be detected in the peripheral regions of each solid particle, at the solid/liquid interface during the reaction. A significant presence of Na was detected within the particles up to a depth of $150-200 \mu m$ on average, as shown in Fig. 17B and 18B. A normalized radius DN was taken into account to display the results, and it was calculated by dividing the punctual length on the radius where the elemental quantification was performed by the total radius of the specific particle. As a DN of 0.5 identifies the centre of the particle, DN of 0 and 1 reflect its extremes; given that, the Na and Ca contents were detected at DN values of 0.0, 0.25, 0.50, 0.75 and 1.0 to better display the gradient observed at gradual depths from the surface. On average of five samples,



Fig. 17 Na wt% and Ca wt% contents plotted against the normalised particle size considered (D_N) for the 700 μ m \leq (D) \leq 1000 μ m group (A and C, respectively) and their distribution in a $D = 924 \,\mu$ m sample (B and D, respectively).



Fig. 18 Na wt% and Ca wt% contents plotted against the normalised length considered for the 400 μ m \leq (*D*) \leq 700 μ m group (A and C, respectively); specific Na wt% and Ca wt% gradients registered for a targeted size (*D* = 450 μ m) sample (B and D, respectively).



Fig. 19 SEM images of the reaction products from the chalk upon grinding and sieving between 150 and 250 μ m; the samples were attached on conductive carbon adhesive tapes.

Na contents were (wt%) of 11.1 \pm 2.5 (DN = 0) and 4.2 \pm 2.2 (DN = 0.5) for the larger group of particles, while 10.6 \pm 2.0 (DN = 0) and 7.2 \pm 2.7 (DN = 0.5) were observed for the smaller particles. Regarding Ca (Fig. 17C, D and 18C, D), slightly higher contents in the inner regions of the solids were observed; the lower local Na content would suggest limited reaction progress into these regions, consistent with the low overall extent of reaction α of 0.3.

Fig. 19 shows the SEM-EDX analysis performed on a single reacted chalk bead collected upon grinding and sieving between 150 and 250 μ m. Pseudo-hexagonal shaped crystals of Na₂CO₃·H₂O and Na₂CO₃⁵⁹ are surrounded by small-sized Ca(OH)₂ crystals, showing a facetted tetrakaidekahedral morphology.⁶⁰ As supported by the XRF and XRD analyses reported in Table 1 and Fig. 14, respectively, significant silica agglomerates could also be detected; in the reaction products, those were partially covered by Ca(OH)₂ layers.

4. Conclusions

The study of the reaction of $CaCO_3$ in NaOH solution allowed for the optimisation of processing parameters such as the residence time and the mixing rate. Close to optimum

conversion could be obtained after 300 seconds of stirring, while further contact between the reactants did not lead to significant yield improvements. A low stirring rate resulted in enhancing the conversion extent. It is likely that the lower conversion achieved at high stirring rates may be linked to enhanced events of nuclei incorporation or the solid/liquid partition at higher centrifugal force. The proportioning of Na₂CO₃·H₂O and Na₂CO₃ was found to be largely affected by the activity of water of the system considered; specifically, Na₂CO₃·H₂O and Na₂CO₃ were the favoured species in the final systems at higher and lower water activity, respectively. However, the reaction was effectively capturing the process CO₂ embodied in CaCO₃, up to the 95% of the total introduced into the system. The comparison between the SEM-EDX analysis of reacted and unreacted chalk samples suggested the possibility of assessing the reaction extent by detection of Na within the solid products. Assuming so, the reaction progression could be visually observed by detection of Na, whose gradient was defined for the solid reacted particles, and whose propagation was observed up to 150 µm deep from the solid/liquid interface. The lower reaction extent obtained for larger CaCO₃ solids ($D \sim 1 \text{ mm}$) suggested that this alternative route would require additional grinding to achieve a satisfactory decarbonisation, if compared to the average size of the raw CaCO₃ feed (2-200 mm) used in a conventional lime or cement plant.¹ Although, we believe that the additional emissions arising from the higher electrical consumption required for a finer CaCO₃ would be negligible, if compared with the avoided combustion and process CO₂.

In conclusion, the chemical decarbonisation of $CaCO_3$ allowed for the nearly total capture of the process CO_2 , while converting $CaCO_3$ to the essential lime. These positive outcomes may be obtained relatively simply, given the mild mixing conditions and heating required; despite that, the use of highlycorrosive NaOH solutions requires further investigation for an eventual scale-up.

Author contributions

Theodore Hanein and Hajime Kinoshita discovered and conceptualized the technology. Theodore Hanein, Hajime Kinoshita, John L. Provis, and Marco Simoni developed the technology and designed the methodology and experiments. Theodore Hanein, Marco Simoni, and Chun Long Woo carried out experiments. Marco Simoni drafted the original manuscript. Theodore Hanein, Hajime Kinoshita, and John L. Provis acquired funding, and supervised Marco Simoni and Chun Long Woo about authorship. Theodore Hanein, Hajime Kinoshita, John Provis, Mark Tyrer, Juan-Carlos Martinez, Magnus Nyberg, Alan Maries, John Stennet and Nestor I. Quintero-Mora reviewed and edited the manuscript.

Conflicts of interest

The authors declare that they have no competing interests as defined by Physical Chemistry Chemical Physics, or other

interests that might be perceived to influence the interpretation of the article.

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