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# Property–activity relations of multifunctional reactive ensembles in cation-exchanged zeolites: a case study of methane activation on Zn<sup>2+</sup>-modified zeolite BEA†

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The reactivity theories and characterization studies for metal-containing zeolites are often focused on probing the metal sites. We present a detailed computational study of the reactivity of Zn-modified BEA zeolite towards C–H bond activation of the methane molecule as a model system that highlights the importance of representing the active site as the whole reactive ensemble integrating the extra-framework Zn<sub>EF</sub><sup>2+</sup> cations, framework oxygens (O<sub>F</sub><sup>2-</sup>), and the confined space of the zeolite pores. We demonstrate that for our model system the relationship between the Lewis acidity, defined by the probe molecule adsorption energy, and the activation energy for methane C–H bond cleavage performs with a determination coefficient  $R^2 = 0.55$ . This suggests that the acid properties of the localized extra-framework cations can be used only for a rough assessment of the reactivity of the cations in the metal-containing zeolites. In turn, studying the relationship between the activation energy and pyrrole adsorption energy revealed a correlation, with  $R^2 = 0.80$ . This observation was accounted for by the similarity between the local geometries of the pyrrole adsorption complexes and the transition states for methane C–H bond cleavage. The inclusion of a simple descriptor for zeolite local confinement allows transferability of the obtained property–activity relations to other zeolite topologies. Our results demonstrate that the representation of the metal cationic species as a synergistically cooperating active site ensembles allows reliable detection of the relationship between the acid properties and reactivity of the metal cation in zeolite materials.

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## 1. Introduction

Transition metal-containing zeolites are promising materials for a wide range of industrial and lab-scale catalytic applications.<sup>1</sup> The catalytic reactivity of the metal-containing zeolites could be described by the synergistic action of both extra-framework (EF) metal cation and framework oxygen atom forming an M<sub>EF</sub><sup>n+</sup>...O<sub>F</sub><sup>2-</sup> Lewis acid–base pair.<sup>2</sup> For instance,

extra-framework Zn<sup>2+</sup> cations confined in zeolite micropores could form highly reactive sterically hindered Zn<sub>EF</sub><sup>2+</sup>...O<sub>F</sub><sup>2-</sup> (EF = extra-framework, F = framework) Lewis acid–base pairs (FLPs) (Fig. 1a), capable of activating aliphatic C–H bonds.<sup>3</sup> An FLP is a chemical entity containing a combination of a sterically encumbered Lewis acid and a Lewis base.<sup>4</sup> Chemical systems of this type have been receiving a lot of attention in the homogeneous catalysis and molecular chemistry communities in the last decade since the pioneering work by Stephan and co-workers.<sup>4,5</sup> The FLP concept is also applicable to heterogeneous catalysts, such as zeolites modified with zinc ions due to the possibility of creation of the sites with undercoordinated Zn<sub>EF</sub><sup>2+</sup> cations leading to excess charges on separated Zn<sub>EF</sub><sup>2+</sup> and O<sub>F</sub><sup>2-</sup> sites (Fig. 1a).<sup>3</sup> In molecular chemistry, the rules for the design and modification of molecular scaffolds to tune the reactivity of FLPs have been established.<sup>6–8</sup> However, they are much less apparent in the more complex heterogeneous systems.<sup>9–11</sup> Because of the high variety of possible structures, locations, and local geometrical environments of the active sites in zeolite-based systems, the construction of universal

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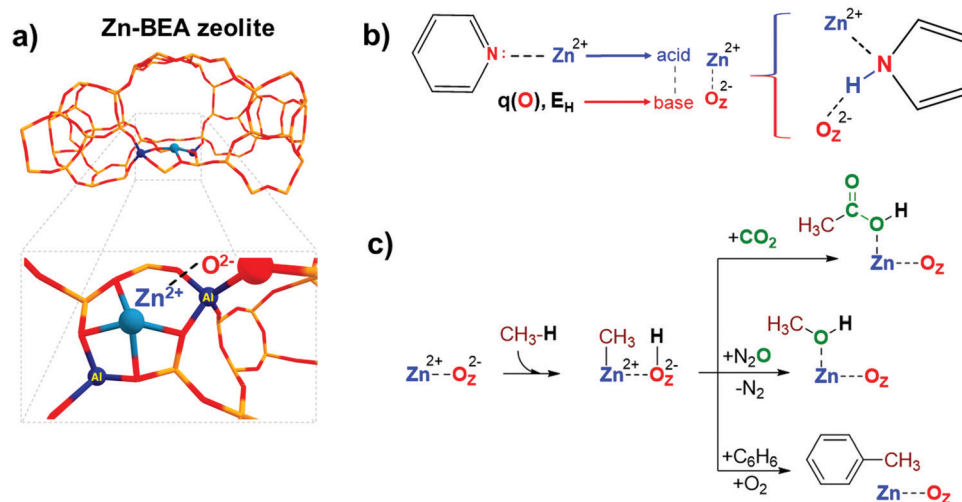


Fig. 1 Structure of the  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  active site in the BEA zeolite framework (a). A schematic representation of the  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  Lewis acid–base pair reactivity descriptors (b). Possible pathways of the methane catalytic valorization for Zn-containing zeolites (c).  $q(\text{O})$  and  $E_{\text{H}}$  denote the charge on the oxygen atom and proton affinity, respectively.

property–reactivity relationships in the confined space is particularly challenging.<sup>12–15</sup> Even relatively straightforward relations between the acidity and reactivity of Brønsted acidic zeolites are not transferrable from one zeolite topology to another.<sup>16</sup> Understanding how the nature and local zeolite environment of a  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  site influence its reactivity towards methane activation is key to developing strategies for the rational design of zeolite-based catalysts for light alkane valorization.<sup>15</sup>

It is generally accepted that the Lewis acidity of the  $\text{Zn}^{2+}$  cations in the zeolite is the key driving force behind light alkane activation.<sup>17–19</sup> In theoretical studies, the qualitative relationships between the partial charge on the  $\text{Zn}^{2+}$  cation and Zn-zeolite activity have been discussed.<sup>3,14,19</sup> The acidity of the exchangeable cations can be assessed by the indirect response from experiments, *e.g.*, by measuring the adsorption energy or the change in the spectral characteristics of basic adsorption probe molecules interacting with  $\text{M}^{n+}$  cations.<sup>20–23</sup>

However, commonly used probes of a basic nature, such as CO or pyridine, are poor probes of the chemistry of the reactive environment and the adjacent basic sites represented by the  $\text{M}_{\text{EF}}^{n+} \cdots \text{O}_{\text{F}}^{2-}$  Lewis acid–base pair reactive ensembles. Adding an extra descriptor for the basicity of the adjacent oxygen atom could be very useful for constructing the property–activity relationships.

The basicity of zeolite framework oxygen atoms can be characterized by adsorption of probe molecules,<sup>24</sup> such as  $\text{CO}_2$ ,<sup>25</sup>  $\text{CH}_3\text{OH}$ ,<sup>26–28</sup>  $\text{N}_2\text{O}_4$ ,<sup>29</sup> propyne,<sup>30</sup> and pyrrole.<sup>31,32</sup> However, the interpretation of the resulting data and the quantification of the framework basicity in the real catalysts is much more challenging.<sup>26</sup> The major complication arises from the fact that most of the molecular probes interact with both the metal site and the conjugated lattice basic oxygen atoms upon adsorption.<sup>26</sup> For instance, pyrrole forms hydrogen bonds between its N–H group and the basic site on the framework, simultaneously interacting by the  $\pi$ -electron system with the conjugated Lewis-acidic  $\text{Zn}_{\text{EF}}^{2+}$  site.

Electronic structure calculations provide an opportunity to investigate directly the fundamental properties of oxygen atoms by computing and analyzing the parameters of net atomic charges or proton affinity in various environments (Fig. 1b). On the other hand, if the reactivity is a function of the components of the entire reactive ensemble and the adsorbed molecules can probe all the components of the ensemble, we can anticipate a correlation between the parameters of the adsorption complexes of the probe molecules and the reactivity of the  $\text{M}_{\text{EF}}^{n+} \cdots \text{O}_{\text{F}}^{2-}$  sites. Indeed, Sun *et al.* obtained good correlations between the adsorption enthalpy of  $\text{CO}_2$  and the activation barrier of heterolytic methane C–H bond dissociation on various  $\text{La}_2\text{O}_3$  clusters using electronic structure calculations at the CCSD(T) level of theory.<sup>33</sup> In this regard, it is of interest to compare the correlations between the key reactivity descriptors and the characteristics of probe molecules interacting simultaneously with  $\text{M}_{\text{EF}}^{n+}$  and  $\text{O}_{\text{F}}^{2-}$  sites, compared to the probe molecules interacting solely with the metal cation Lewis sites.

Methane is an abundant and readily accessible feedstock<sup>34</sup> for the production of various valuable liquid chemicals, such as oxygenated<sup>35–42</sup> or aromatic compounds.<sup>43–47</sup> Zn-Modified zeolites are promising catalysts for the activation and conversion of light alkanes.<sup>48–52</sup> These materials feature highly reactive  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  Lewis acid–base pairs that enable heterolytic cleavage of C–H bonds in alkanes to produce a Zn-alkyl intermediate and an adjacent Brønsted acid site under mild conditions.<sup>17,46,53–56</sup> Such reactivity was first observed by Kazansky *et al.* with DRIFTS spectroscopy<sup>57</sup> and was confirmed later with  $^{13}\text{C}$  MAS NMR spectroscopy.<sup>46,54,55,58,59</sup> Room-temperature methane activation by Zn-containing zeolites has been experimentally observed.<sup>54,60,61</sup> The reaction of the zeolite-stabilized Zn-methyl intermediates with such reactants as  $\text{O}_2$ ,<sup>52,61</sup>  $\text{CO}_2$ ,<sup>56,62</sup> propane (benzene),<sup>46,58</sup> and  $\text{N}_2\text{O}^3$  opens pathways for methane valorization to industrially relevant and highly valuable chemicals (Fig. 1c). Understanding the fundamental



factors that control the reactivity and catalytic behavior of metal-containing zeolites is critical for their further optimization and the development of new zeolite-based catalysts.

In this work, we computationally analyze the correlations between the kinetic and thermodynamic parameters of different  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  reactive ensembles in a Zn-BEA zeolite framework with the parameters (such as the shift of the infrared bands and adsorption energies) of adsorption complexes with representative molecular probes. We focus specifically here on Zn-BEA, whose reactivity towards light alkane activation was earlier investigated by some of us in a series of experimental solid-state NMR studies.<sup>48,49,51</sup> We report a periodic DFT study on the property–reactivity relationships for methane activation by the  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  Lewis acid–base pairs localized in between the different T-positions of the zeolite BEA framework.

## 2. Computational details

### Models

Calculations were carried out using the full periodic BEA zeolite unit cell with lattice parameters of  $a = b = 12.61 \text{ \AA}$ ,  $c = 26.32 \text{ \AA}$ ,  $\alpha = \beta = \gamma = 90^\circ$  as optimized by DFT with an all-silica BEA polymorph A periodic model was used for the periodic DFT calculations.<sup>63</sup> The optimized values are close to the experimental values of  $a = b = 12.63 \text{ \AA}$  and  $c = 26.19 \text{ \AA}$ . To compensate for the positive charge of the extra-framework  $\text{Zn}^{2+}$  cation, two framework Si atoms in the BEA unit cell were substituted by two aluminum atoms, resulting in a lattice Si/Al ratio of 31. The optimized local geometries for all configurations of the reactive ensembles considered in this study are summarized in Fig. S1 in the ESI†. The BEA lattice contains 9 inequivalent T sites, thus creating a great diversity of Al atom locations and therefore possible types of  $\text{Zn}^{2+}$  cations (Fig. S1, ESI†). In this study, 11 types of  $\text{Zn}^{2+}$  cations were considered (Fig. S1, ESI†). However, because of the highly symmetrical structure of the BEA framework, one pair of T-atoms may be present in different cation sites, providing distinctly different coordination environments to  $\text{Zn}^{2+}$  ions. To avoid ambiguity, we explicitly note that pairs “T2T6”–“T6T2” and “T2T3”–“T3T2” belong to different structures. The respective optimized periodic structures and their relative stabilities are summarized in Fig. S1 (ESI†), and the optimized coordinates are provided as supplementary material. The relative stabilities ( $\Delta E_{\text{Zn-BEA}}$ ) are defined as the energy difference between the given model and the most stable configuration (T6T6).

**DFT method.** Periodic DFT calculations were performed using the Vienna *Ab initio* Simulation Package (VASP 5.3.5).<sup>64</sup> The PBE functional was used to describe the exchange–correlation energy term.<sup>65</sup> To account for van der Waals interactions, the semi-empirical D3 correction by Grimme<sup>66</sup> with Becke–Johnson damping<sup>67</sup> was applied. A Gaussian smearing of the partial occupancy population with a width of 0.05 eV was used. Brillouin zone sampling was restricted to the  $\Gamma$  point. A plane-wave basis set with a cutoff energy of 450 eV was used in combination with the projected augmented wave (PAW) method.<sup>68</sup> The number of

points in the FFT-grid along the  $a$ ,  $b$ , and  $c$  lattice vectors was equal to 140, 140, and 280, respectively. All geometries were considered optimized when the maximum forces on all atoms were less than  $0.04 \text{ eV \AA}^{-1}$ . During geometrical optimizations, all atoms were allowed to fully relax. This technique was previously applied for the calculations of the zeolite systems.<sup>12,15,69</sup> All data analysis and discussion in this study were done based on the relative electronic energies. This inclusion of the entropic corrections does not significantly change the reaction trend. The justification of this choice is made based on the studies by Szécsényi *et al.* for Fe-ZSM-5 zeolites containing different Fe-oxo sites.<sup>15,70</sup>

Vibrational frequencies were calculated using the finite differences method ( $0.02 \text{ \AA}$  atom displacement applied to extra-framework atoms only) as implemented in VASP. To correct for the systematic errors in the computed IR frequencies, the respective values were scaled by  $\nu_{\text{exp}}/\nu_{\text{calc}}$ , where  $\nu_{\text{exp}}$  and  $\nu_{\text{calc}}$  correspond to the experimentally obtained and calculated frequencies of the gas-phase probe molecule, respectively. The scaling coefficients are listed in Table S1 (ESI†).

**Transition states.** The minimum energy reaction paths and the corresponding transition states were determined by the climbing image nudged elastic band (CI-NEB) method.<sup>71</sup> The maximum energy geometries along the reaction path obtained with the CI-NEB method were further optimized using a quasi-Newton algorithm. Transition state geometries were confirmed by the presence of a single imaginary frequency along the reaction path.

**DDEC6 net atomic charges and bond orders.** The Density Derived Electrostatic and Chemical (DDEC6) method was used to calculate net atomic charges and bond orders, as implemented in the Chargemol package.<sup>72–75</sup> DDEC6 bond order analysis was successfully implemented in the works of Rohling *et al.*<sup>76,77</sup> for the theoretical study of the Diels–Alder cycloaddition mechanistic insights into metal-containing zeolites. For the DDEC6 calculations, DFT integration grids with 360, 360, 768 points along the  $a$ ,  $b$  and  $c$  lattice vectors were implemented.<sup>76,78</sup> We refer to original papers by Manz *et al.*<sup>72–75</sup> for the extensive derivation of the equations necessary to execute DDEC6-based charge partitioning and compute the bond orders.

In brief, the bond order of an atom pair A and j is described as:

$$B_{\text{A,j}} = \text{CE}_{\text{A,j}} + \text{A}_{\text{A,j}}, \quad (1)$$

where  $B_{\text{A,j}}$  is a bond order between the A and j atoms,  $\text{CE}_{\text{A,j}}$  is the contact exchange term and  $\text{A}_{\text{A,j}}$  is the dressed exchange hole delocalization term.

The term  $\text{CE}_{\text{A,j}}$  describes the electron exchange between atoms A and j in a material:

$$\text{CE}_{\text{A,j}} = 2 \int \frac{\bar{\rho}_{\text{A}}^{\text{avg}}(\vec{r}_{\text{A}}) \cdot \bar{\rho}_{\text{j}}^{\text{avg}}(\vec{r}_{\text{j}})}{\bar{\rho}^{\text{avg}}(\vec{r}) \cdot \bar{\rho}^{\text{avg}}(\vec{r})} \rho(\vec{r}) d^3\vec{r}, \quad (2)$$

where  $\bar{\rho}_{\text{j}}^{\text{avg}}$  is the average spherical electron density of atom j as a function of the atomic electron distribution and atomic spin magnetization density obtained through DDEC6-based partitioning of the electron density. The terms in the denominator



belong to the sum of all found in the material. The second term in eqn (1) is the dressed exchange hole delocalization term defined in eqn (3). This equation deals with the dressed exchange hole, which is an adjusted exchange hole (either more contracted or more diffuse) exchange hole to obtain more accurate bond orders.

$$A_{A,j} = \chi_{A,j}^{\text{coord.nr.}} \chi_{A,j}^{\text{pairwise}} \chi_{A,j}^{\text{con.}} \leq CE_{A,j}, \quad (3)$$

In eqn (3),  $\chi_{A,j}^{\text{coord.nr.}}$  accounts for coordination number effects,  $\chi_{A,j}^{\text{pairwise}}$  accounts for pairwise interactions and  $\chi_{A,j}^{\text{con.}}$  is a constraint on the density-derived localization index,  $B_{A,A}$ . The latter is a matrix that equals the total number of dressed exchange electrons in the material. This constraint ensures that the behavior of  $B_{A,A}$  is well controlled.

**CH...O intermolecular contacts.** To find CH...O contacts, optimized geometries in CONTCAR format were automatically processed with in-house Python script. The CH...O distance cut-off was set to 2.5 Å based on the distribution of CH...O distances in the considered zeolite-pyrrole complexes, and on the value of the most probable  $D_{\text{max}}(\text{CH}\cdots\text{O}) = 2.81$  Å in molecular crystals.<sup>79</sup> More sophisticated confinement descriptors were not used due to an insufficient amount of data, and because the goal was not to develop the best descriptor, but to show the transferability of  $\Delta E_{\text{int}}^{\ddagger} \sim \Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  correlation when complemented by a local geometrical descriptor between various zeolites.

### 3. Results and discussion

#### 3.1. Methane activation on different $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$ sites

To analyze the structure-activity factors driving the heterolytic dissociation of the C-H bond in methane, several distinct active site configurations formed by the  $\text{Zn}^{2+}$  cations stabilized at different sites of the BEA framework were considered (Fig. S1, ESI<sup>†</sup>).

In general, the most efficient stabilization to  $\text{Zn}^{2+}$  cations is provided by the six-membered ring (T6T6, T6T8, T8T8) sites featuring a highly symmetrical square-planar coordination environment. The smaller five-membered ring sites feature

tridentate coordination of the exchange  $\text{Zn}^{2+}$  cations and show on average longer Zn-O distances, giving rise to generally less stable configurations. The T2T3 model represents a charge-alternating site, in which the  $\text{Zn}^{2+}$  cation is directly interacting with only one lattice  $[\text{AlO}_2]^-$  anion, while the overall charge-neutrality is provided *via* an indirect charge-compensation by a distantly placed second lattice Al. Previous studies proposed such sites to be uniquely reactive towards light alkane activation.<sup>19,80</sup>

The highly constrained coordination environment of the four-membered ring sites in the T3T2 model gives rise to the least stable  $\text{Zn}^{2+}$  configurations. For  $\text{Zn}_{\text{EF}}^{2+}$  cations, we consider two vicinal lattice oxygen atoms to form the reactive  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  acid-base pairs (denoted as O1 or O2). The diverging reactivity of the resulting sites towards C-H activation is expected given the varied relative orientations of the respective Lewis acidic and proton-accepting base-sites.<sup>3</sup> In this study, the reactivity of  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  is probed by the intrinsic activation barrier of C-H activation.

A representative energy profile for methane activation by a  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  Lewis acid-base pair along with the respective intermediates and transition state structures is shown in Fig. 2. The figure also defines the adsorption energies ( $\Delta E_{\text{ads}}$ ), the intrinsic ( $\Delta E_{\text{int}}^{\ddagger}$ ), apparent ( $\Delta E_{\text{app}}^{\ddagger}$ ) activation barriers, and the reaction energies ( $\Delta E_{\text{r}}$ ).

The reference state (set as 0 kJ mol<sup>-1</sup>) denoted as “ $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-} + \text{CH}_4$ ” is defined as the separate methane molecule and Zn-BEA. The adsorption complex of methane ( $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-} \cdots \text{CH}_4$ ) is formed by methane  $\sigma$ -orbital donation to the 4s orbital of  $\text{Zn}^{2+}$ .<sup>3,81</sup> Such an interaction polarizes and activates the adsorbed molecule and gives rise to the increased  $\angle \text{H-C-H}$  angles and C-H distances. Such perturbations of the adsorbed methane have been evidenced by infrared spectroscopy.<sup>48,53</sup> The polarization of the C-H bond facilitates its heterolytic dissociation by the  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  pair, resulting in a  $\text{Zn-CH}_3$  species and an adjacent Brønsted acid site ( $\text{Si-O(H)-Al}$  group).

Computed reaction energy diagrams for methane C-H bond cleavage over the selected Zn-BEA configurations are presented

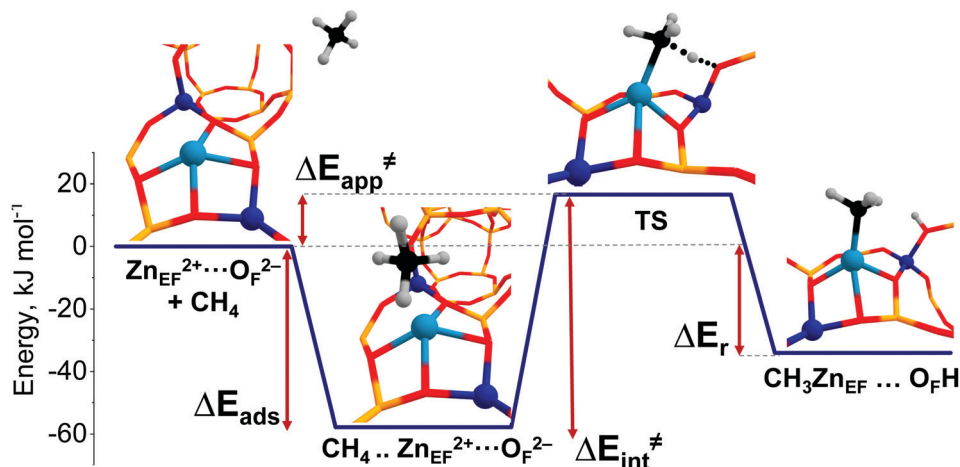


Fig. 2 Energy profile for methane activation on a T4T7O1  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  FLP.



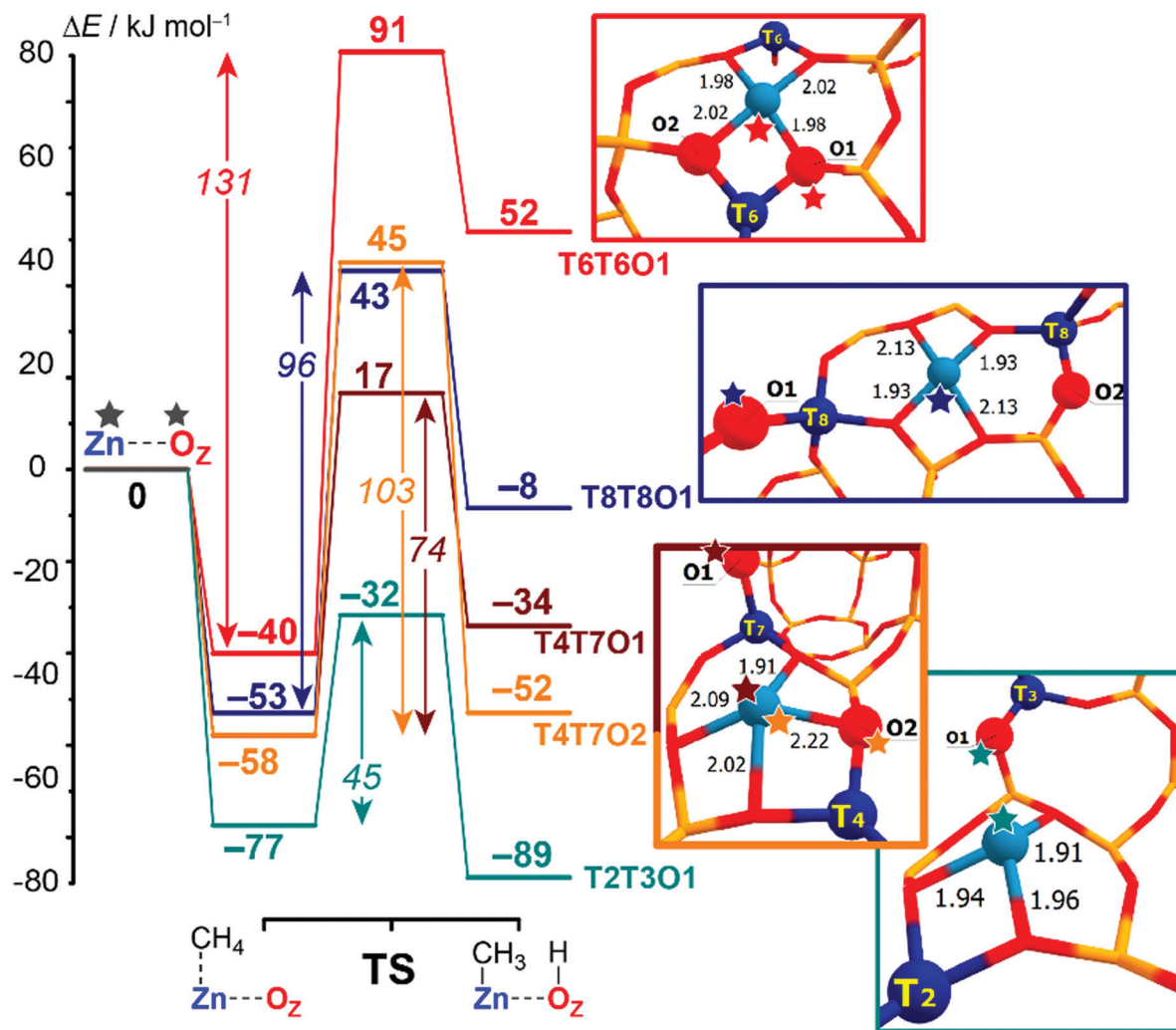


Fig. 3 Computed reaction energy diagrams for the heterolytic dissociation of methane by representative T6T6O1, T8T8O1, T4T7O1, T4T7O2 and T2T3O1 Zn-BEA configurations. All computed reaction paths are shown in Fig. S2 (ESI†).

in Fig. 3. The figure provides selected results for the representative extra-framework site configurations, illustrating the pronounced variation in the kinetic and thermodynamics of methane activation by different  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  active sites. The complete dataset for all reactive configurations considered in this study is summarized in Table S2 and Fig. S3–S5 of the ESI†. Computations reveal large variations in the activation barriers ( $\Delta E_{\text{int}}^{\ddagger} = 45\text{--}131 \text{ kJ mol}^{-1}$ ) and reaction energies ( $\Delta E_{\text{r}} = 62 \text{ to } -89 \text{ kJ mol}^{-1}$ ) depending on the type of the  $\text{Zn}^{2+}$  site. We find that  $\Delta E_{\text{r}}$  correlates well with the relative stability of the Zn-BEA framework model (determination coefficient  $R^2 = 0.93$ ), whereas a much worse correlation is observed with  $\Delta E_{\text{int}}^{\ddagger}$  ( $R^2 = 0.71$ ) (Fig. S6a, ESI†).

Note that similar active site configurations provide multiple reaction pathways involving different proton-accepting sites on the zeolite framework with strongly varying energetics. The highest activation barrier of  $131 \text{ kJ mol}^{-1}$  is found for the most stable T6T6  $\text{Zn}_{\text{EF}}^{2+}$  cation and T6T6O1  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  Lewis pair. The lowest intrinsic barrier of  $46 \text{ kJ mol}^{-1}$  belongs to the least stable T2T3O1 FLP configuration with the “distantly

stabilized”  $\text{Zn}^{2+}$  cation. The reaction is exothermic, except for the most stable configurations T6T6 and T6T8. The multisite nature of the reactive ensembles and their structural flexibility allowing for a substantial alteration in the geometry along the reaction coordinate give rise to substantial deviations from the expected linear Brønsted–Evans–Polanyi (BEP) relationships between  $\Delta E_{\text{int}}^{\ddagger}$  and  $\Delta E_{\text{r}}$  ( $R^2 = 0.60$ , Fig. S6b, ESI†).

The BEP relationship directly relates the activation energies to the corresponding reaction energies for the particular reaction family:  $\Delta E_{\text{int}}^{\ddagger} = \alpha \Delta E_{\text{r}} + \text{const}$ , where parameter  $\alpha$  reflects the position of the transition state along the reaction coordinate ( $0 < \alpha < 1$ ).<sup>82–84</sup> While the extreme values of  $\Delta E_{\text{int}}^{\ddagger}$  and  $\Delta E_{\text{r}}$  correspond to each other, the linear relations do not hold for the points in the middle of the BEP graph. For instance,  $\text{CH}_4$  dissociation on T4T7O1 configuration is more favorable kinetically than on T4T7O2 ( $\Delta E_{\text{int}}^{\ddagger} = 74 \text{ kJ mol}^{-1}$  vs.  $103 \text{ kJ mol}^{-1}$ ), while being less favorable thermodynamically ( $\Delta E_{\text{r}} = -34 \text{ kJ mol}^{-1}$  vs.  $-52 \text{ kJ mol}^{-1}$ ). Therefore, the estimation of the activation energy of the C–H bond cleavage on  $\text{M}_{\text{EF}}^{m+} \cdots \text{O}_{\text{F}}^{2-}$  pairs in varied zeolite confinements cannot be



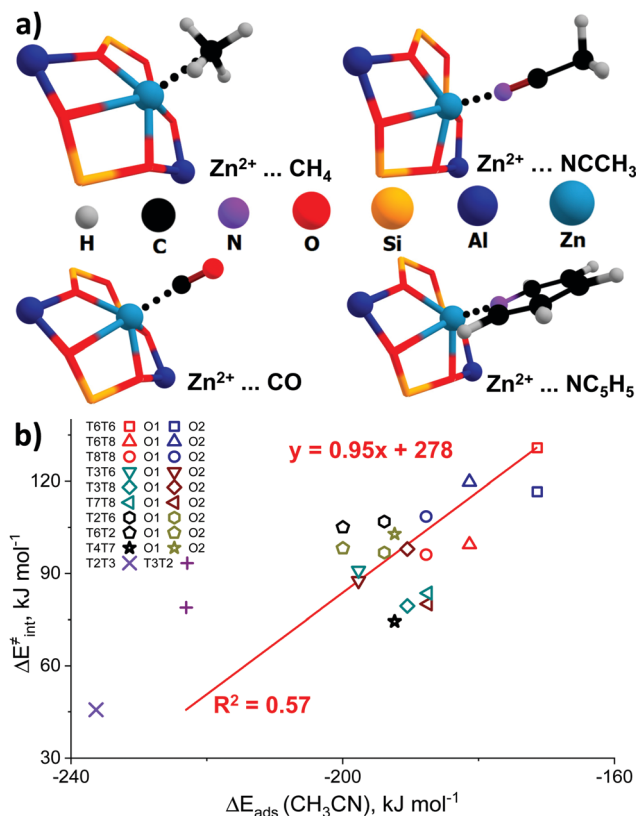


Fig. 4 The interaction of basic molecular probes with  $\text{Zn}^{2+}$  cations in BEA zeolite. The representative geometries of the probe molecule adsorption complexes (a). The relationship between the activation barriers for methane C–H bond cleavage and  $\Delta E_{\text{ads}}(\text{CH}_3\text{CN})$  (b). A complete summary of the adsorption energies is given in Table S4 (ESI†).

made unambiguously based on BEP-type relationships. A similar effect was observed earlier for homolytic  $\text{CH}_4$  activation by Fe-ZSM-5 catalysts.<sup>15</sup> Thus, the additional screening of alternative and more complex reactivity descriptors for the  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_F^{2-}$  pairs is needed to find better correlations.

### 3.2. $\text{Zn}_{\text{EF}}^{2+}$ Lewis acidity as the main reactivity descriptor

We further analyzed the Lewis acidity of  $\text{Zn}_{\text{EF}}^{2+}$  as a potential activity descriptor, as this parameter was earlier proposed as the key driving force behind the facile activation of light alkanes by Zn-zeolites.<sup>17–19</sup> Previous studies have shown that the activity and stability of the exchangeable  $\text{Zn}^{2+}$  cations in zeolite may correlate with their Lewis acidity.<sup>85–87</sup> To probe Lewis acidity experimentally, the adsorption of basic probe molecules, such as carbon monoxide (CO),<sup>88</sup> acetonitrile ( $\text{CH}_3\text{CN}$ ),<sup>89</sup> and pyridine ( $\text{C}_5\text{H}_5\text{N}$ ),<sup>23,90</sup> are often used. Kazansky and co-workers<sup>87,91</sup> also suggested using methane and other light alkanes as suitable and highly specific probes for the reactivity and Lewis acidity of the exchangeable cations. In this case, the Lewis acidity is assessed by monitoring with FTIR spectroscopy the degree of probe molecule perturbation or the interaction strength upon probe adsorption on the exchangeable  $\text{Zn}^{2+}$  cations.

In this regard, we have further investigated the possible correlations between the experimentally measurable responses

of different adsorption probes and the intrinsic reactivity parameters of  $\text{Zn}^{2+}$  cations for methane C–H bond cleavage. Such molecular modeling was also motivated by the fact that no correlations were observed between the fundamental properties of Zn-sites, such as DDEC6 charges on the Zn cation, and methane activation barriers (Fig. S6c, ESI†). Adsorption energies ( $\Delta E_{\text{ads}}$ ) were defined as the relative energy of the adsorption complex with respect to the free optimized Zn-BEA and the probe in the gas phase:  $\Delta E_{\text{ads}} = E_{\text{ads}} - E_{\text{zeolite}} - E_{\text{probe}}$ .

The representative geometries of the adsorption complexes of the selected probe molecules with Zn-BEA are shown in Fig. 4a. The geometry of the probe molecule changes considerably upon adsorption, resulting in a pronounced elongation of the C–O, C–H, and C–N bonds involved in the interaction with the  $\text{Zn}^{2+}$  site. The nature of the cation site does not impact strongly the perturbations of the probe itself but defines the interaction strength that is reflected in the  $\text{Zn}_{\text{EF}}^{2+}$ –probe molecule distances. The selected geometric parameters of the optimized adsorption complexes are listed in Table S5 (ESI†). The search for possible correlations between the adsorption strength and perturbations in the vibrational spectrum of the adsorbed probes revealed that, only in the case of methane, a relatively weak correlation between  $\nu_1(\text{C–H})$  and  $E_{\text{ads}}$  can be found ( $R^2 = 0.59$ ), suggesting that  $\text{CH}_4$  is the only probe capable of providing information on the  $\text{Zn}^{2+}$  Lewis acidity from the FTIR experiment (Fig. S7, ESI†). For an extended discussion related to the adsorption of the basic probe molecules, refer to ESI† (Fig. S8).

To further analyze the role of  $\text{Zn}^{2+}$  Lewis acidity in the reactivity of various  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_F^{2-}$  pairs, we investigated the relationships between the adsorption energies of the probes and the activation barriers of methane C–H bond dissociation. The representative results obtained for the case of  $\text{CH}_3\text{CN}$  adsorption are shown in Fig. 4b. The results for CO,  $\text{CH}_4$ , and  $\text{C}_5\text{H}_5\text{N}$  probes are summarized in Fig. S9 (ESI†). In all cases, rather weak linear correlations are obtained with  $R^2$  values in the range of 0.44–0.58. The best correlation is found between  $\Delta E_{\text{int}}^{\ddagger}$  and  $\Delta E_{\text{ads}}$  for  $\text{CH}_3\text{CN}$ . In this case, the complexes of the probe molecule with  $\text{Zn}^{2+}$  cations with the highest adsorption energies correspond to the configurations with the lowest activation energies for C–H bond cleavage and *vice versa*. These computational results indicate that the adsorption energies of commonly used molecular probes can be used as a rough approximation descriptor for C–H bond reactivity on Zn-modified zeolites.

We note that the deviations from the expected linearity in these correlations are not caused only by the presence of several activation pathways for each reactive configuration. The intrinsic reactivity of certain centers (*e.g.* T6T2, T7T8, T2T3, and T3T2) are not aligned with the common trend. Therefore, for the correct prediction of the activity of the  $\text{M}_{\text{EF}}^{n+} \cdots \text{O}_F^{2-}$  sites, we have to inquire further into the role of the conjugated base ( $\text{O}_F^{2-}$ ) in C–H bond activation. Therefore, we further analyze the basicity of  $\text{O}_F^{2-}$  as the second reactivity descriptor of the reactive ensemble to find out whether a combination of acidity and basicity of  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_F^{2-}$  pairs explicitly defines its reactivity.





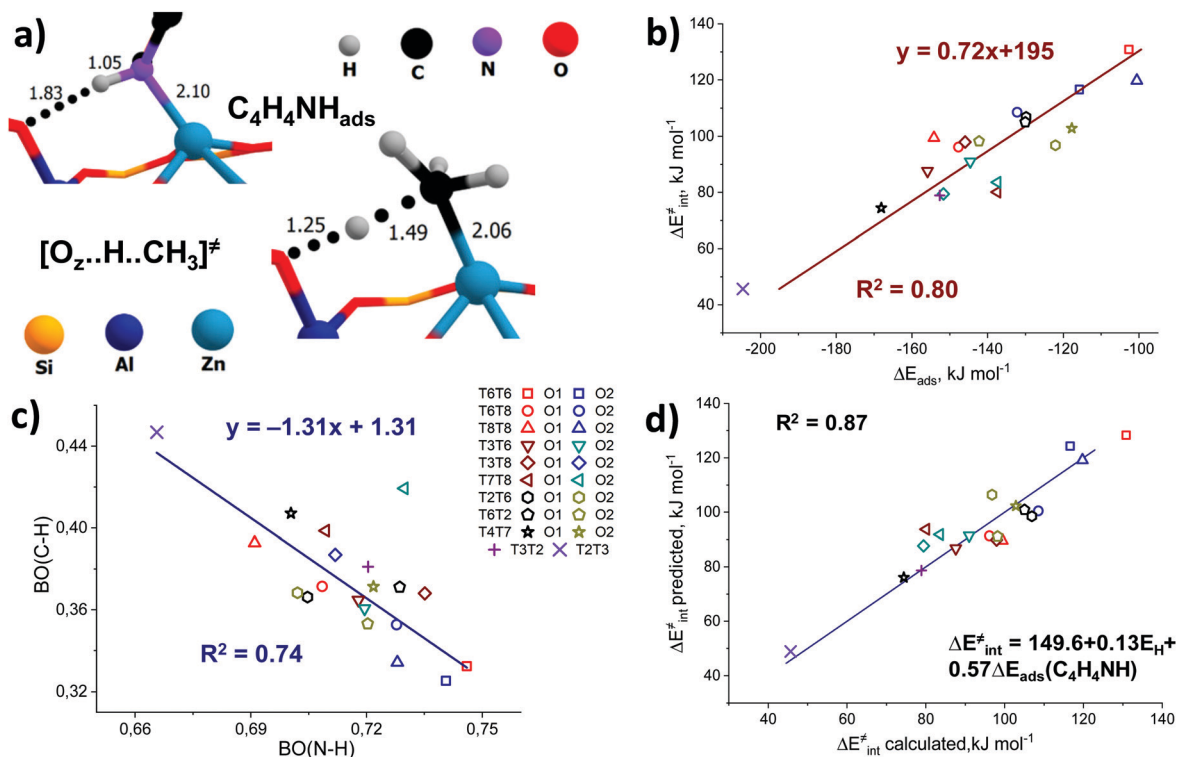


Fig. 6 The use of pyrrole as a multifunctional adsorption probe for the reactivity of  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  Lewis acid–base pairs. A comparison of the transition state for C–H cleavage and pyrrole adsorption complex geometries for the T8T8O1 configuration (a). Correlations between the intrinsic activation barrier and pyrrole adsorption energies (b). Correlation between bond orders of C–H and N–H in transition states and pyrrole adsorption complexes (c). Two-dimensional correlations between  $\Delta E_{\text{int}}^{\ddagger}$  and a linear combination of  $\Delta E_{\text{ads}}(\text{CH}_3\text{CN})$  and  $E_{\text{H}}$  (d). “ $\Delta E_{\text{int}}^{\ddagger}$  predicted” is the activation energy value predicted using the linear combination of  $\Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  and  $E_{\text{H}}$ , while “ $\Delta E_{\text{int}}^{\ddagger}$  calculated” refers to the DFT-calculated activation energy.

Due to specific zeolite confinement and bonding of the adsorbed pyrrole molecule with both  $\text{Zn}_{\text{EF}}^{2+}$  and  $\text{O}_{\text{F}}^{2-}$ , the configurational freedom of the probe is restricted. Therefore, the presented adsorption complexes herein are most stable. The interaction patterns range from weak adsorption on the  $\text{Zn}_{\text{EF}}^{2+}$  cation, complemented by the very weak interaction of the acid proton and  $\text{O}_{\text{F}}^{2-}$  atom at a distance of  $\sim 2.3$  Å, to strong adsorption on both sites with strong hydrogen bonding at a distance of  $\sim 1.8$  Å. Upon adsorption, the  $\angle \text{H-N}(\text{pyrrole ring})$  angles change from  $180^\circ$  (gas phase) to  $130^\circ$  in the adsorption complexes. Some of the selected geometrical parameters of the adsorption complexes are listed in Table S8 (ESI<sup>†</sup>). Our calculations reveal that these probes provide substantial sensitivity to the orientation of the  $\text{Zn}_{\text{EF}}^{2+}$  and  $\text{O}_{\text{F}}^{2-}$  sites with respect to each other in the intrazeolite reactive ensemble.

Fig. 6b shows the relationship between the pyrrole adsorption energies and the activation barriers of C–H bond cleavage, featuring high linearity with  $R^2 = 0.80$ . Table S8 (ESI<sup>†</sup>) summarizes the adsorption energies. In contrast, propyne adsorption energies produce a weak correlation with  $R^2 = 0.46$  (Fig. S16, ESI<sup>†</sup>). These data suggest that pyrrole could be a promising probe molecule for estimating the reactivity of the zeolite-confined  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  pairs towards heterolytic C–H bond cleavage. Based on this relationship one can expect the lower activation energy of the C–H bond cleavage for the higher experimentally estimated heat of pyrrole adsorption. The effects

of the dispersion corrections on the resulting correlations are estimated to be minor (Fig. S17, ESI<sup>†</sup>).

To analyze the origin of the good correlations between the  $\Delta E_{\text{ads}}(\text{pyrrole})$  and the activation barrier, we further investigated the changes in the DDEC6-derived bond orders (BO) of C–H and N–H in the transition state and the pyrrole adsorption complex, respectively. The C–H and N–H bond orders are listed in Tables S3 and S8 (ESI<sup>†</sup>), respectively. They form a good linear correlation with a negative slope (Fig. 6c): the increased reactivity of the  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  site is reflected in the increased C–H bond order in the TS and increased polarization of the N–H bonds in the adsorbed pyrrole. With the exception of the T7T8O2 site, for which an exceptionally short C–H bond (1.40 Å) in TS (Fig. S3, excluded from the statistical analysis, ESI<sup>†</sup>) is found, a stable linear correlation with the determination coefficient  $R^2 = 0.74$  is observed between the bond orders of N–H and C–H. This indicates that the nature of the correlations between the activation energy of C–H bond cleavage and pyrrole adsorption energy could be related to the similarity of local geometry and electronic structure perturbations in the pyrrole adsorption complex and the TS for C–H bond cleavage.

Vibrational frequencies of pyrrole and propyne adsorption complexes were also calculated to assess whether the perturbations of the  $\nu_1$  stretching vibration frequencies of X–H (X = N, C) could be used to assess the reactivity of the  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  pair. No direct relationship between the vibrational frequencies and activation



barriers was observed (Fig. S19, ESI<sup>†</sup>). The strongest redshift of the vibrational frequencies does not point to the most reactive sites but to the  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_F^{2-}$  FLPs containing an oxygen atom above the  $\text{Zn}^{2+}$  cation, resulting in very strong  $\text{O}_F \cdots \text{H}$  hydrogen bonding in the adsorption complex. Such interactions give rise to the strong redshifts of  $\nu_1(\text{N-H})$  in pyrrole adsorbed on T6T8O1, T8T8O1, T4T7O1, and T2T3O1 FLPs (Fig. S13–S15, ESI<sup>†</sup>), suggesting weak applicability of this probe for FTIR spectroscopic characterization of intrazeolite  $\text{Zn}^{2+}$  sites.

We next constructed multiple linear regressions using  $\Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  in combination with other potential descriptors considered in this study to represent better the multifunctional nature of the intrazeolite active site and find possibilities for improvement of the property–activity correlations. Additional descriptors are included based on solid mechanistic considerations. It is possible that an extra term could improve the correlation since additional descriptors could better account for the specific intrinsic characteristics of the  $\text{Zn}_{\text{EF}}^{2+} - \text{O}_F^{2-}$  active site (acidity or basicity) compared to using pyrrole alone. In this regard, we analyzed the correlations of the intrinsic activation barrier  $\Delta E_{\text{int}}^\ddagger$  with a linear combination of  $\Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  and  $\Delta E_{\text{ads}}(\text{CH}_3\text{CN})$  or with a combination of  $\Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  and  $E_{\text{H}}$ . The combination of  $\Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  and  $\Delta E_{\text{ads}}(\text{CH}_3\text{CN})$  improves the fit only slightly (Fig. S20, ESI<sup>†</sup>). Better linearity is obtained for the correlation of  $\Delta E_{\text{int}}^\ddagger$  with  $\Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  and  $E_{\text{H}}$  with a determination coefficient  $R^2 = 0.87$ . (Fig. 6d). Analyzing the  $p$ -values of the obtained correlation coefficients (Table S10, ESI<sup>†</sup>), we concluded that the inclusion of the  $\Delta E_{\text{ads}}(\text{CH}_3\text{CN})$  descriptor does not have any statistical value. On the other hand, the coefficient before the  $E_{\text{H}}$  term has statistical significance and could be included to improve the correlation quality significantly. This is not surprising because the adsorption of pyrrole is dominated by the interaction with the exchangeable cation, with a weaker interaction between the acid proton and the lattice oxygen. However, such a combination of descriptors seems to be of minor practical importance, because of the purely theoretical nature of the hydrogen affinity that can be derived only from electronic structure calculations.

We evaluated the predictive power of the correlations considered so far on alternative materials beyond the current zeolite system (Zn-BEA with  $\text{Si}/\text{Al} = 31$ , Zn-BEA-31). We first studied two additional zeolite models (Fig. S21, ESI<sup>†</sup>): namely, the Zn-BEA zeolite with  $\text{Si}/\text{Al} = 20$  (Zn-BEA-20) and the Zn-MOR zeolite (Zn-MOR-SP-1).

For Zn-BEA-20 we consider the  $\text{Zn}^{2+}$  cation located in the six-membered ring with 3 Al atoms placed at T4, T6, and T8 positions. Despite it being unlikely that this kind of Al arrangement will be met within a real experiment, we aimed to show the possible transfer of our correlations to a model with a  $\text{Zn}^{2+}$  cation in a completely different local environment. In the case of Zn-MOR, the  $\text{Zn}^{2+}$  cation was stabilized at the  $\gamma$ -site of the “side-pocket” with Al atoms placed in T1 and T2 positions. The correlation of  $\Delta E_{\text{int}}^\ddagger$  with  $\Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  established on Zn-BEA-31 provides predictions of the C–H bond dissociation barriers (Fig. 6b) that deviated by  $9 \text{ kJ mol}^{-1}$  from the DFT-computed  $\Delta E_{\text{int}}^\ddagger$ . The predictive power of the correlation for the determination of activation energy is improved when multiple linear regressions were applied to Zn-BEA-20

(Table S11, ESI<sup>†</sup>). However, all of the derived correlations failed to accurately predict the activation barrier over the Zn sites located at the different confinement environments of Zn-MOR. We, therefore, inferred that such purely energy-based property–activity relationships are reliably established only for the BEA zeolite topology. This is in line with a previous report by Liu *et al.*<sup>16</sup> demonstrating that the scaling relations for H-zeolites were not transferrable from one zeolite framework to another. We calculated additional points for the MOR framework (Fig. S21, ESI<sup>†</sup>) to see the possibility of establishing calculations in the other zeolite lattices. The obtained results demonstrate that such correlations exist in the main channel and “side pocket” of the MOR topology. The results are shown in Fig. S22 (ESI<sup>†</sup>). The coefficients in these linear equations are very different from those obtained in the Zn-BEA zeolite. The transferability of the relationships can be improved by complementing the pure energy-based correlations with a geometrical descriptor accounting for the varied confined spaces.

### 3.5. Transferable reactivity models with local confinement descriptors

The predictive power of the obtained energy-based correlations was poor for the MOR topology, providing deviations of *ca.*

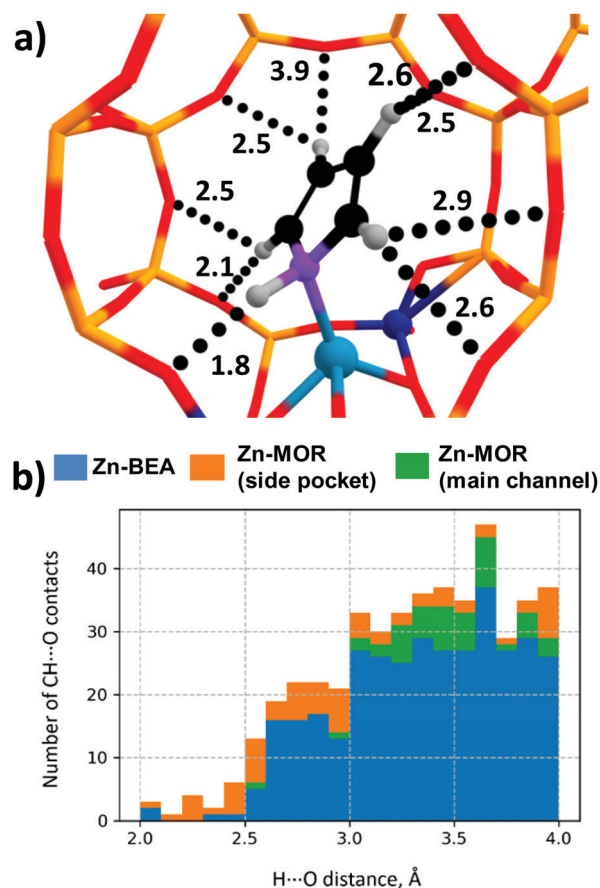


Fig. 7 (a) Multiple  $\text{CH} \cdots \text{O}$  contacts in the Zn-MOR-SP-1/pyrrole complex. ( $\text{CH} \cdots \text{O}$  distances are given in Angstroms.) (b) Histogram of  $\text{CH} \cdots \text{O}$  contact distances in Zn-zeolite/pyrrole systems.



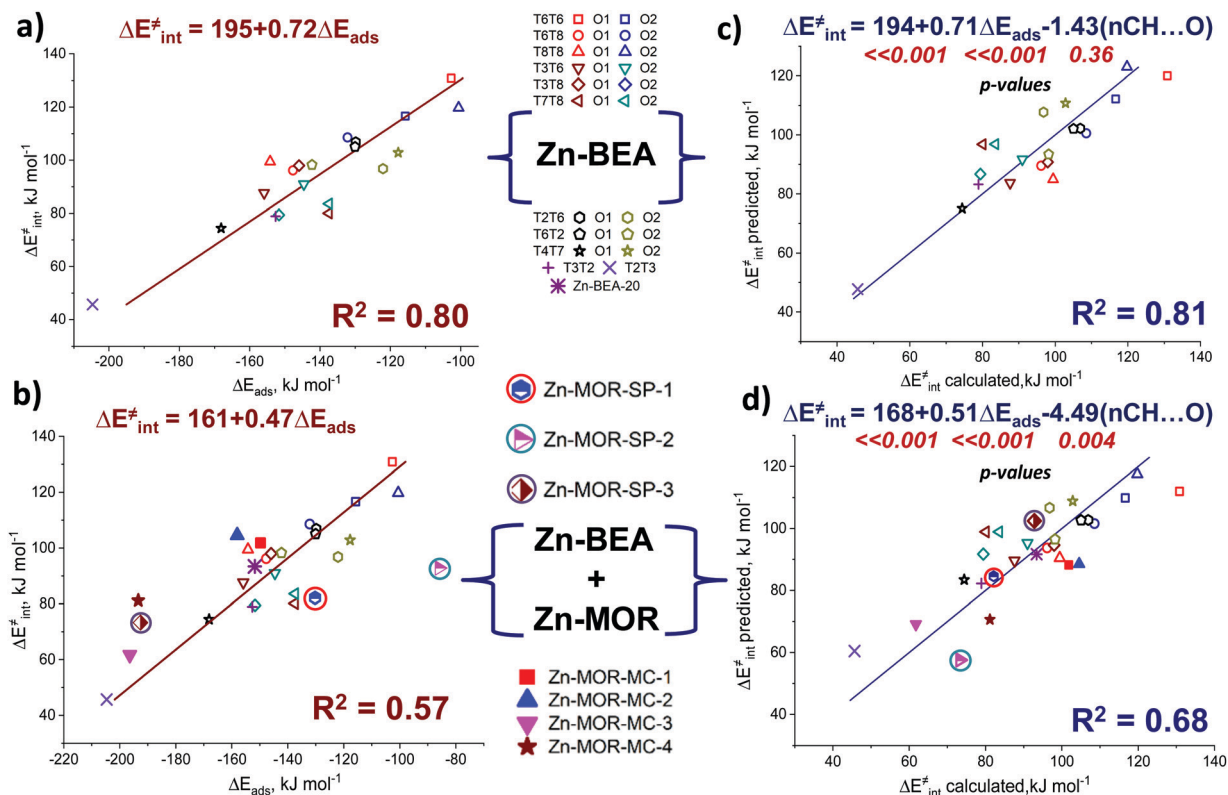


Fig. 8 Correlations between pyrrole adsorption energies and activation energies for (a) Zn-BEA only and (b) combined Zn-BEA and Zn-MOR sets. Two-dimensional correlations between  $\Delta E_{\text{int}}^{\ddagger}$  and a linear combination of  $\Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  and  $n(\text{CH}\cdots\text{O})$  for (c) Zn-BEA systems and combined Zn-BEA and Zn-MOR sets. “ $\Delta E_{\text{int}}^{\ddagger}$  predicted” is the activation energy value predicted using a linear combination of  $\Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  and  $n(\text{CH}\cdots\text{O})$ , while “ $\Delta E_{\text{int}}^{\ddagger}$  calculated” refers to the DFT-calculated activation energy.

20  $\text{kJ mol}^{-1}$  from the DFT-computed  $\Delta E_{\text{int}}^{\ddagger}$ , which is as bad as the worst outliers of the original correlation (Fig. 6b). This is attributed to the differences in confinement by different zeolite topologies. Confinement effects of the zeolite framework arise from the non-covalent interaction of the adsorbed molecules with the internal curvature of the internal zeolite surface. These effects are expected to be different for different zeolite frameworks because of the varied pore sizes and curvature.<sup>97</sup> Effects of the zeolite confinement could be quantitatively assessed by energy decomposition analysis<sup>98,99</sup> or topological analysis of the electron density distribution.<sup>100</sup> Szécsényi *et al.*<sup>15</sup> accounted for the confinement by adding terms describing the effects of the interaction of the methyl fragment with nearby oxygen atoms to the purely energetic correlations. We followed a similar approach in this work.

The geometries of the  $\text{Zn}-\text{CH}_3\cdots\text{H}\cdots\text{O}-\text{Al}$  and  $\text{Zn}-\text{N}_{\text{pyr}}-\text{H}\cdots\text{O}-\text{Si}$  moieties are very similar in the MOR lattice, whereas pyrrole, in contrast to methane, forms several  $\text{CH}\cdots\text{O}$  contacts with the zeolite wall surface. Thus, the deviation of the regression-predicted  $\Delta E_{\text{int}}^{\ddagger}$  to larger values can be interpreted as a decrease in the “effective” adsorption energy site due to noncovalent pyrrole-zeolite interactions. Indeed, the adsorption of pyrrole in the side-pocket of Zn-MOR (Fig. 7a) gives rise to a number of short  $\text{CH}\cdots\text{O}$  contacts with  $D(\text{H}\cdots\text{O}) < 2.5 \text{ \AA}$ , which are significantly shorter than the most probable

$\text{CH}\cdots\text{O}$  distance  $D_{\text{max}}(\text{CH}\cdots\text{O}) = 2.81 \text{ \AA}$ .<sup>79</sup> Furthermore, our analysis reveals that such multiple short  $\text{CH}\cdots\text{O}$  contacts are almost exclusively formed in Zn-MOR models, while in most other systems such interactions were absent (Fig. 7b and Table S12, ESI†).

To quantitatively evaluate this hypothesis, we introduced the number of short  $\text{CH}\cdots\text{O}$  contacts,  $n(\text{CH}\cdots\text{O})$ ,  $D(\text{H}\cdots\text{O}) < 2.5 \text{ \AA}$ , as a confinement descriptor to the  $\Delta E_{\text{int}}^{\ddagger} \sim \Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  correlation. Because of the similar confinement effects exerted by the models of one zeolite topology, this additional descriptor was found to be statistically insignificant and it did not affect the  $\Delta E_{\text{int}}^{\ddagger} \sim E_{\text{ads}}(\text{C}_4\text{H}_5\text{N})$  correlation established for a sub-set of 20 BEA systems (Fig. 8a and b). However, when applied to the complete set of systems, including seven additional Zn-MOR models, the resulting correlations showed a substantially increased  $R^2$  value from 0.57 to 0.68, and reduced error in predicted  $E_a$  (Fig. 8c and d). The “Zn-MOR-SP” notation refers to the structures in the MOR side pocket, while the “Zn-MOR-MC” notation refers to the structures in the MOR main channel. The effectiveness of using the simple confinement descriptor confirms the transferability of the  $\Delta E_{\text{int}}^{\ddagger} \sim \Delta E_{\text{ads}}(\text{C}_4\text{H}_4\text{NH})$  correlation between zeolites characterized by different topologies. By complementing the pure energy-based correlation with such a simple structural descriptor to account for the varied confinement effects, we were able to improve its



transferability between zeolites with different topologies. A further search for more complicated confinement descriptors could further improve the quality of the correlations, but such a search would require a substantial extension of the analyzed dataset that is not possible and is outside the scope of the current study.

## 4. Conclusions

We have computationally studied the reactivity of the various  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  sites in the Zn-BEA zeolite framework with respect to the cleavage of methane C–H bond as a model system that highlights the importance of the representation of the transition metal zeolites active sites as a reactive ensemble. Our calculations reveal the highly varied values of the activation barriers and reaction energies for  $\text{Zn}_{\text{EF}}^{2+}$  sites stabilized at different cation-exchanged sites featuring various geometries and Al distributions within the BEA framework.

The Lewis acidity of differently confined  $\text{Zn}_{\text{EF}}^{2+}$  cations was approximated by the adsorption energies of a range of representative probe molecules widely used for the experimental characterization of intrazeolite active sites. Our computational analysis reveals only a weak correlation with determination coefficient  $R^2 = 0.45\text{--}0.58$  between the reactivity of  $\text{Zn}_{\text{EF}}^{2+}$  sites towards methane C–H bond dissociation and adsorption energy of Lewis acidity probes (carbon monoxide, acetonitrile, pyridine, methane). Such molecular probes are suitable only for a rough assessment of the reactivity of cation-modified zeolites towards C–H bond activation in methane. These correlations of the C–H bond cleavage activation energy with both Lewis acid–base properties of the zeolite-confined  $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$  pairs are slightly improved, compared to the correlations between the activation barrier and either the Lewis acidity of the cation or the basicity of the framework oxygen.

The analysis identifies pyrrole as the optimal probe molecule that simultaneously interacts with both the acidic and basic parts of the reactive site and, at the same time, allows us to effectively assess the local confined environment. This results in an improved correlation with a determination coefficient  $R^2 = 0.80$ . Thus, we have obtained a fundamentally important structure–reactivity relationship bridging the reactivity of the Lewis acid–base ( $\text{Zn}_{\text{EF}}^{2+} \cdots \text{O}_{\text{F}}^{2-}$ ) pairs towards heterolytic C–H bond cleavage and pyrrole adsorption energies, making pyrrole a potentially useful probe molecule for the characterization of the reactivity of metal-containing zeolite towards light alkane activation. The relationship between the activation energy of C–H bond cleavage and pyrrole adsorption energies with  $R^2 = 0.80$  was explained by the structural similarity and correlations of the N–H bond orders in adsorption complexes with the C–H bond orders in the transition states. Therefore, the representation of the metal-containing zeolite active sites as a synergistically cooperating active site ensemble allows the observation of the linear property–reactivity relationship. Further analysis has demonstrated that the inclusion of simple geometrical descriptors allows us to further extend the applicability of the obtained

property–activity relations outside the BEA zeolite topology. Large-scale *in silico* screening with modern data analysis tools of the sizeable set of zeolite topologies, active cations, and confinement descriptors would help to establish truly universal property–activity relationships.

Finally, we state that the correlations between the adsorption energies of the acidity probe molecules and the reactivity of the metal cation active sites could help guide the design and development of catalysts based on zeolites, modified with transition metal cations, for various catalytic applications.

## Author contributions

The manuscript was written with the contribution of all authors. All authors have given their approval for the final version of the manuscript.

## Conflicts of interest

The authors declare no competing financial interests.

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