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Comprehensive Raman study of orthorhombic κ/ε -Ga₂O₃ and the impact of rotational domains†

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Gallium oxide (Ga₂O₃) is an ultra-wide bandgap material, which has recently attracted widespread attention for holding promising applications in power electronics and solar blind UV photodetectors, outclassing GaN or SiC in terms of a larger bandgap and higher breakdown voltages. The orthorhombic κ phase (also referred to as ε) has sparked particular interest for offering higher symmetry than β , while featuring ferroelectric behavior paired with a large predicted spontaneous polarization, paving the way to fabricating high-quality two-dimensional electron gases for application in heterostructure field effect transistors. The presently available κ phase samples are characterized by a domain structure, in which orthorhombic domains are rotated 120° against each other within the c -plane forming a pseudo-hexagonal structure, which has previously often been ascribed to ε -Ga₂O₃ and incorrectly been viewed as this polymorph's true crystal structure. A detailed investigation into the phonon modes of orthorhombic κ -Ga₂O₃ provides insights into fundamental material properties such as crystal structure and orientation as well as the vibrational symmetries of Raman active modes. We investigate the Raman active phonon modes of an MBE-grown orthorhombic κ -Ga₂O₃ thin film featuring the domain structure deposited on (0001)-Al₂O₃ by experiment and theory: Polarized micro-Raman spectroscopy measurements in conjunction with density functional perturbation theory (DFPT) calculations enable the identification of both the frequencies and vibrational symmetries of the Raman active phonons. Presenting comprehensive Raman spectra of the orthorhombic κ phase, the experimental frequencies of more than 90 Raman modes are determined and correlated with the 117 modes predicted by the calculations. Angular-resolved Raman measurements are utilized to provide an experimental verification of phonon mode symmetries. We present an analytical tool to deal with the domain structure and its effect on the obtained Raman spectra.

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1 Introduction

Gallium oxide (Ga₂O₃) is a transparent, semiconducting oxide, which may form five different polymorphs: α , β , γ , κ (mostly referred as ε)¹ and δ .^{2–11} As further explained in Section 1.1, from now on in this manuscript we will refer to the orthorhombic polymorph of Ga₂O₃ just as κ . While the majority of the Ga₂O₃ related research focuses on the thermodynamically-most

stable monoclinic β -phase,^{2,3,9} the second-most stable orthorhombic κ polymorph offers unique features and has recently been gaining momentum. The reported optical bandgap energies of the κ phase at room temperature range between 4.91 and 5.04 eV,^{12–18} slightly higher than those of β -Ga₂O₃ (~ 4.8 eV^{19,20}). Moreover, outclassing competing wide bandgap materials like SiC (3.3 eV) or GaN (3.4 eV) makes the material a promising candidate for future applications in power electronics or solar-blind UV photodetectors.^{18,21–24} Aside from providing higher symmetry than β , density functional *ab initio* calculations^{25,26} predicted the presence of ferroelectric behavior, which has been experimentally²⁷ verified using dynamic hysteresis measurements. The combination of ferroelectric behavior and a large predicted spontaneous polarization (≈ 23 – 26 $\mu\text{C cm}^{-2}$)^{25,28,29} along its c -axis might further pave the way to fabricating high-quality two-dimensional electron gases (2DEG) as conduction channels in heterostructure field effect transistors. While a pair of other calculations^{1,27} and an

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experimental study²⁷ obtained lower values of $\approx 0.2 \mu\text{C cm}^{-2}$ and $\approx 0.0092 \mu\text{C cm}^{-2}$, the experimental feasibility of creating a 2DEG at the interface of a $\kappa\text{-Ga}_2\text{O}_3/\text{GaN}$ heterostructure was recently demonstrated,³⁰ which might open the possibility of realizing high electron mobility transistors without doping. Moreover, a $\kappa\text{-(Al}_x\text{Ga}_{1-x})_2\text{O}_3/\kappa\text{-Ga}_2\text{O}_3$ quantum well superlattice heterostructure was recently realized.³¹ Featuring even larger polarization differences, the incorporation of In³² or Al³³ into $\kappa\text{-Ga}_2\text{O}_3$ enabled bandgap tuning between 4.25 and 6.2 eV³⁴ and is expected to enable 2DEGs with even higher sheet carrier densities.

The κ phase was found to thermally transition to β only under annealing at high temperatures $T > 700\text{--}800^\circ\text{C}$,^{14,35} allowing for applications in devices requiring sufficiently high working temperatures. To date, the orthorhombic phase has been grown successfully³⁶ on a number of different substrates, including $\text{Al}_2\text{O}_3(0001)$, $\text{GaN}(0001)$, $\text{AlN}(0001)$, 6H-SiC or $\beta\text{-Ga}_2\text{O}_3(201)$, using halide vapour phase epitaxy,^{14,37,38} atomic layer deposition,³⁹ metal-organic chemical vapor deposition,^{15,18,22,27,30,35,37,39–44} metal-organic vapor phase epitaxy,^{1,45–48} mist CVD,^{16,17,32,33,49,50} plasma-assisted molecular beam epitaxy,^{51,52} laser molecular beam epitaxy,^{21,53} and pulsed laser deposition.^{12,13,24,54–57}

1.1 Crystal structure

Some ambiguity was related to the real crystal structure of the κ or ϵ polymorph in the past. An initial XRD study investigated a 3 μm MOCVD-grown thin film on (0001)- Al_2O_3 and hinted at a hexagonal symmetry ascribed to the $P6_3mc$ space group,²⁷ usually referred to as $\epsilon\text{-Ga}_2\text{O}_3$. A subsequent TEM study¹ found the probed film to consist of 5–10 nm large (110)-twinned domains with orthorhombic structure corresponding to the space group symmetry $Pna2_1$ (Schoenflies: C_{2v}^9), called $\kappa\text{-Ga}_2\text{O}_3$. Within the c -plane the individual domains are rotated 120° with respect to each other, forming a pseudo-hexagonal pattern observed in the initial XRD study, whose limited resolution provided a mediated view and did not allow to detect the individual domains. Newer XRD^{1,12,24,49,51} and TEM^{24,51} analyses confirmed the orthorhombic nature of the/polymorph. To avoid confusions we will, throughout this work, relate to κ when discussing the orthorhombic polymorph.

Fig. 1 depicts the unit cell of orthorhombic $\kappa\text{-Ga}_2\text{O}_3$ with lattice parameters¹⁰ $a = 5.0566 \text{ \AA}$, $b = 8.6867 \text{ \AA}$ and $c = 9.3035 \text{ \AA}$. The oxygen atoms order in a 4H (ABAC) close-packed stacking, with Ga^{3+} ions occupying tetrahedral (Ga_I) and octahedral (Ga_{II} , Ga_{III} , Ga_{IV}) sites.¹

1.2 Lattice dynamics

Raman spectroscopy enables the study of vibrational properties by providing access to a material's Raman-active phonon modes. Raman-active phonons of different vibrational symmetries can be discriminated utilizing different polarization geometries. While the Raman- and IR-active phonons of $\beta\text{-Ga}_2\text{O}_3$ have been calculated theoretically and verified experimentally in a number of publications,^{59–64} comprehensive Raman spectra of $\kappa\text{-Ga}_2\text{O}_3$ are not yet available in the literature. One previous work⁶⁵

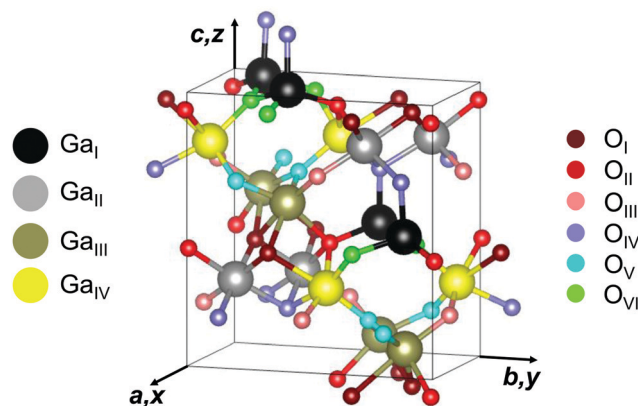


Fig. 1 Unit cell of orthorhombic $\kappa\text{-Ga}_2\text{O}_3$. Four types of Ga (Ga_I , Ga_{II} , Ga_{III} , and Ga_{IV}) and six types of O (O_I , O_{II} , O_{III} , O_{IV} , O_V and O_{VI}) lattice sites are illustrated in different colors. The axes of a Cartesian coordinate system x , y , z are aligned along the crystallographic directions a , b and c . The crystallographic plot was created using VESTA.⁵⁸

investigated the IR- and Raman-active phonons of orthorhombic gallium-substituted epsilon iron oxide ($\kappa/\epsilon\text{-Ga}_{0.5}\text{Fe}_{1.5}\text{O}_3$) by first-principles phonon-mode calculations. The authors probed a powder sample of $\kappa/\epsilon\text{-Ga}_{0.48}\text{Fe}_{1.52}\text{O}_3$ nanoparticles using Raman spectroscopy and experimentally identified 17 distinct Raman-active phonon modes. Another experimental study⁵¹ employed Raman spectroscopy in a confocal set-up to investigate the Raman spectra of a $\kappa\text{-Ga}_2\text{O}_3$ thin film deposited on $\alpha\text{-Al}_2\text{O}_3(0001)$. The obtained spectra were dominated by the Raman lines of the underlying sapphire substrate, making the identification of Ga_2O_3 related Raman modes a challenging endeavor. The authors identified eight Raman modes associated with the $\kappa\text{-Ga}_2\text{O}_3$ thin film and provided an initial correlation to the mode symmetries predicted by the orthorhombic ($Pna2_1$) or hexagonal ($P6_3mc$) crystal structures. An alternative to overcome the challenges posed by the strong substrate signal in the confocal geometry is the employment of cross-sectional Raman spectroscopy, in which the laser is focused onto the sample's edge to maximize or minimize the signal contributions from the film or substrate, respectively. This approach was successfully applied in a preceding study⁶³, in which the edge of a square-shaped (010)-oriented homoepitaxially grown $\beta\text{-Ga}_2\text{O}_3$ thin film was irradiated to determine the Raman modes associated with it.

1.3 This work

In this work, a combination of confocal and cross-sectional polarized micro-Raman spectroscopy is applied to investigate the phonon frequencies of an MBE-grown orthorhombic $\kappa\text{-Ga}_2\text{O}_3$ thin film on top of an $\alpha\text{-Al}_2\text{O}_3(0001)$ substrate. The acquired experimental data are complemented with the results of DFPT calculations. By applying different polarization geometries in combination with Raman selection rules, we separate Raman modes of different vibrational symmetries and present the first comprehensive Raman spectra of $\kappa\text{-Ga}_2\text{O}_3$. We provide a detailed table of all calculated and more than 90 experimentally determined phonon frequencies and identify



the symmetries of most experimental modes by combination of polarized measurements and *ab initio* calculations. The identified modes' vibrational symmetries are verified using angular-resolved Raman measurements. We provide an analytical tool to treat the effect of the domain structure on the Raman spectra, paving the way to discriminating domain structured from monocrySTALLINE films in future studies.

2 Experimental and theoretical methods

The investigated κ -Ga₂O₃ layer was deposited by molecular beam epitaxy *via* indium-mediated metal-exchange catalysis (MEXCAT-MBE)^{51,52} on a *c*-plane sapphire substrate. Differently from the homoepitaxial growth on β -Ga₂O₃ substrates,^{66–69} the MEXCAT-MBE (In- or Sn- mediated) in heteroepitaxy results in the stabilization of the metastable orthorhombic polymorph of Ga₂O₃. A Ga and In flux were provided with beam equivalent pressure of 6.5×10^{-7} mbar and 7.6×10^{-7} mbar, respectively. At first, an approximately 10 nm-thick β -Ga₂O₃ nucleation layer (usually necessary for the heteroepitaxial growth of κ -Ga₂O₃ in MBE) was deposited without providing the In flux, at a substrate temperature $T_g = 600$ °C and an oxygen flux of 1 standard cubic centimeters (sccm) with a 300 W plasma power for 1 minute. The In-mediated κ -layer was then deposited with In and Ga-fluxes present in an O-flux of 0.75 sccm ($P = 300$ W) at $T_g = 700$ °C for 210 minutes. The thickness of the κ -layer (monitored by *in situ* laser reflectometry) is around 800 nm.

The symmetric out-of-plane 2θ - ω XRD scan reported in Fig. 2(a) of the sample highlights the presence of an (001)-oriented orthorhombic κ -Ga₂O₃ layer; the left-hand side peaks to the κ ones are related to the β -Ga₂O₃ nucleation layer⁵². The layer is composed of orthorhombic κ -Ga₂O₃ domains that are rotated in-plane by 120° with respect to each other.¹ This can be unveiled by performing ϕ -scans on particular reflexes, as in the case of the 204 one reported in Fig. 2(b): the observed six peaks (red curve) indicate the occurrence of three rotational domains in the orthorhombic structure⁴⁹. The good crystal quality of this layer is also proven by the relatively small full width at half maximum of the 004 reflection in ω -scan (FWHM = 0.14°, *cf.* Fig. 1(f) in a preceding study⁷⁰). High-resolution 2θ - ω XRD scans of the sample (not shown) were performed for the symmetric 004 as well as the skew-symmetric 131 and 202 reflexes. The corresponding diffraction angles $2\theta = 38.855^\circ$ as well as 37.011° and 40.784° , respectively, allowed us to estimate the lattice parameters of the orthorhombic layer. The results (shown in Table 1) are consistent with previous experimental and theoretical studies.

Raman scattering at room temperature (293 K) was excited by a 532.16 nm frequency stabilized single longitudinal mode diode-pumped solid-state (DPSS) laser (Laser Quantum Torus 532) on a LabRAM HR 800 spectrometer (Horiba Jobin-Yvon). The laser beam was focused onto the sample using a 100× Olympus objective with a numerical aperture (NA) of 0.9, with the scattered light being collected in backscattering geometry.

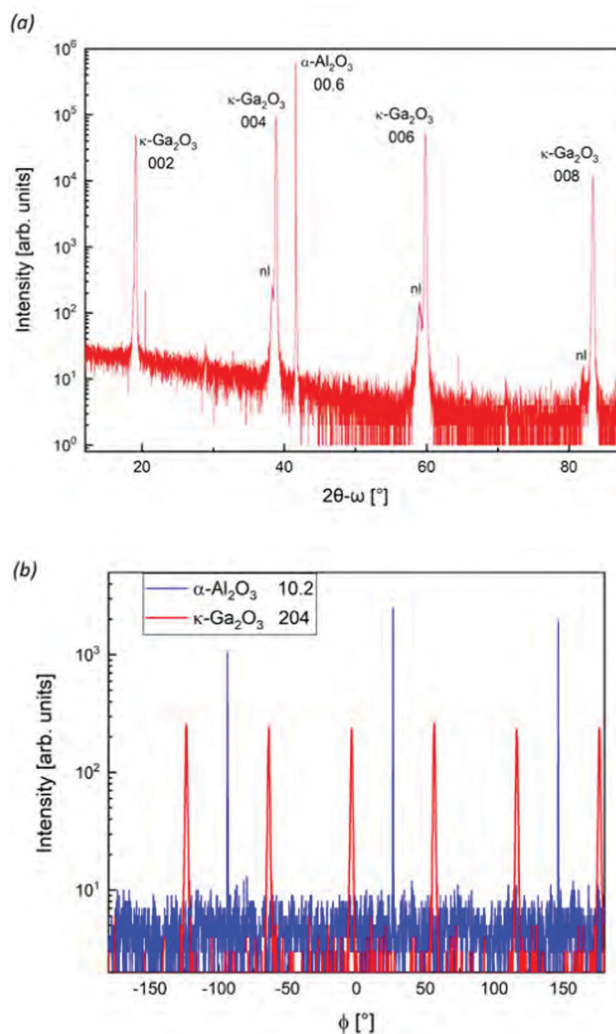


Fig. 2 XRD (a) 2θ - ω and (b) ϕ -scan of the κ -Ga₂O₃ investigated sample. In (a) the label nl stands for nucleation layer of β -Ga₂O₃. Reflexes of the Al₂O₃ substrate are given using the reduced three-digit notation.¹²

Table 1 Lattice constants *a*, *b*, *c* obtained from experiment or DFT-LDA calculations in this work compared to previous data. The utilized experimental method or exchange–correlation functional applied in each experimental or theoretical work is specified. RSM abbreviates reciprocal space maps

| | <i>a</i> (Å) | <i>b</i> (Å) | <i>c</i> (Å) |
|---|--------------|--------------|--------------|
| Experiment (2θ - ω) ^a | 5.032 | 8.710 | 9.264 |
| Experiment (2θ - ω) ¹² | 5.066 | 8.700 | 9.261 |
| Experiment (RSM) ¹² | 5.053 | 8.701 | 9.265 |
| Experiment ¹ | 5.046 | 8.702 | 9.283 |
| LDA ^a | 5.028 | 8.621 | 9.211 |
| AM05 ¹⁰ | 5.0566 | 8.6867 | 9.3035 |
| PBE ³ | 5.120 | 8.792 | 9.410 |
| B3LYP ²⁹ | 5.07 | 8.69 | 9.30 |

^a This work.

Backreflected and elastically scattered light (Rayleigh component) was filtered using an ultra low frequency filter (ULF) unit and then spectrally-dispersed by a monochromator with a grating of



1800 lines per mm. The light was detected by a charge-coupled device (CCD). The sample was placed beneath the objective with a respective surface's normal parallel to the direction of light propagation. A $\lambda/2$ wave plate in the excitation was set at 0° or 45° to polarize the incident light parallel or crossed with respect to the scattered light, which was selected using a fixed polarizer in the detection. Prior to each measurement, the Raman spectrometer was calibrated using the spectral lines of a neon spectral lamp.

Angular-resolved Raman scans were performed by incorporating a second $\lambda/2$ wave plate in the tube above the objective. The automatized rotation of the wave plate by an angle $\phi/2$ rotated the polarization of both the incident and scattered light by an angle ϕ with respect to the fixed sample, constituting a ϕ virtual rotation of the investigated sample.

The theoretical phonon spectra were simulated within the frame of density functional perturbation theory (DFPT) on the level of the local density approximation (LDA) as implemented in the QUANTUM ESPRESSO suite.⁷¹ The Ga(3d, 4s, 4p) and the O(2s, 2p) states were treated as valence electrons using multiprojector optimized normconserving Vanderbilt (ONCV) pseudopotentials from the sg15 library.⁷² The electronic wavefunctions were expanded in a plane-wave basis with a cutoff energy of 100 Ry. All reciprocal space integrations were performed by a discrete Monkhorst–Pack sampling of $6 \times 4 \times 4$ k -points in the Brillouin zone. We fully optimized the atomic positions and cell parameters until the residual forces between atoms and the cell stress were smaller than $0.001 \text{ eV \AA}^{-1}$ and 0.01 GPa , respectively. The atomic positions and lattice parameter for the initial geometry before and after the structure optimization are provided in the ESI.† The threshold for the total energy was set to 10^{-14} Ry, which ensured tightly converged interatomic forces for the geometry optimization and of the ground state density and wave functions for the DFPT calculations. The phonon dispersion and the density-of-states (Fig. S2 in the ESI†) was obtained through Fourier interpolation using the explicitly calculated phonon frequencies on a regular grid of $6 \times 4 \times 4$ q -vectors. As a result of the intrinsic underbinding of the LDA exchange–correlation functional, our optimized lattice constants are less than 1% underestimated compared to the experimental values (Table 1). On the other hand, it is well-known that the LDA overbinding gives rise to a typically very good agreement of the DFT phonon frequencies,⁷³ motivating our choice for the purposes of this work.

3 Results and discussion

3.1 Polarization dependence of monocrystalline orthorhombic crystals

The primitive unit cell of the orthorhombic κ structure consists of 40 atoms (4 Ga and 6 O atoms, each fourfold degenerate).¹⁰ At the Γ -point, these correspond to 117 optical phonons:

$$\Gamma^{\text{opt}} = 29A_1 + 30A_2 + 29B_1 + 29B_2$$

All modes are Raman-active, with modes of A_1 , B_1 and B_2 symmetry also exhibiting IR-activity. The Raman tensors of

the orthorhombic $Pna2_1/C_{2v}^9$ space group read⁷⁴

$$A_1(z) = \begin{pmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & c \end{pmatrix}, \quad A_2 = \begin{pmatrix} 0 & d & 0 \\ d & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad (1)$$

$$B_1(x) = \begin{pmatrix} 0 & 0 & e \\ 0 & 0 & 0 \\ e & 0 & 0 \end{pmatrix}, \quad B_2(y) = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & f \\ 0 & f & 0 \end{pmatrix},$$

where the coordinate in parentheses denotes the phonon polarization direction. Raman selection rules predict the presence or absence of modes of different vibrational symmetries in dependence of the applied scattering geometry and are obtained by substituting the above Raman tensors into the well-known relation between scattering intensity I_s and the polarization geometry

$$I_s \propto |\vec{e}_i \mathcal{R} \vec{e}_s|^2. \quad (2)$$

Here, \mathcal{R} denotes the second-rank Raman tensor and \vec{e}_i or \vec{e}_s are the polarization vectors of the incident or scattered light, respectively. Scattering geometries are expressed using the Porto notation $\vec{k}_i(\vec{e}_i\vec{e}_s)\vec{k}_s$, where \vec{k}_i and \vec{k}_s point into the propagation direction of the incident or scattered light. Polar phonons induce an oscillating macroscopic electric field in the direction of atomic displacements, leading to a splitting of A_1 , B_1 and B_2 modes into transverse-optical (TO) and longitudinal-optical (LO) phonons. The non-polar A_2 modes, in turn, exhibit no LO–TO-splitting.

Raman selection rules of single-crystalline κ -Ga₂O₃ are summarized in Table 2: modes of $A_1(\text{TO})$ symmetry are allowed for parallel polarization vectors when probing the (100) and (010) planes in backscattering configuration. For crossed polarization, the $B_1(\text{TO})$ modes are visible exclusively on the (010) plane whereas $B_2(\text{TO})$ modes are allowed on the (100) plane. Conversely, $A_1(\text{LO})$ and A_2 modes can be accessed by probing the (001) facet in parallel and crossed polarization, respectively. $B_1(\text{LO})$ and $B_2(\text{LO})$ modes are not allowed in backscattering geometry.

Table 2 Selection rules of monocrystalline κ -Ga₂O₃ for backscattering geometries calculated using eqn (2). The incident or scattered light propagates along the \vec{k}_i or \vec{k}_s directions, with \vec{e}_i and \vec{e}_s being the respective polarization direction. Modes not listed have vanishing intensities in the respective polarization configuration. a , b and c denote the crystallographic directions, with LO and TO abbreviating longitudinal or transverse optical phonons

| Plane | Polarization $\vec{k}_i(\vec{e}_i\vec{e}_s)\vec{k}_s$ | Allowed modes |
|-------|---|------------------|
| (100) | $a(bb)\bar{a}$, $a(cc)\bar{a}$ | $A_1(\text{TO})$ |
| | $a(bc)\bar{a}$, $a(cb)\bar{a}$ | $B_2(\text{TO})$ |
| (010) | $b(aa)\bar{b}$, $b(cc)\bar{b}$ | $A_1(\text{TO})$ |
| | $b(ac)\bar{b}$, $b(ca)\bar{b}$ | $B_1(\text{TO})$ |
| (001) | $c(aa)\bar{c}$, $c(bb)\bar{c}$ | $A_1(\text{LO})$ |
| | $c(ab)\bar{c}$, $c(ba)\bar{c}$ | A_2 |



In angular-resolved Raman measurements, the polarization vectors of both the incident \vec{e}_i and scattered \vec{e}_s light are rotated by an angle ϕ relative to the sample's edge, yielding an angular-dependent intensity variation. Mathematically, the polarization vectors' rotations in the plane of incidence are expressed by parameterizing \vec{e}_i and \vec{e}_s using cylindrical coordinates. Substituting the parameterized polarization vectors \vec{e}_i and \vec{e}_s into eqn (2) yields angular-dependent intensity functions for an orthorhombic crystal.

As an example, when exciting the (100) plane of monocrystalline orthorhombic κ -Ga₂O₃ using a parallel polarization of the incident with respect to the scattered light, the polarization vectors become

$$\vec{e}_i = \vec{e}_s = \begin{pmatrix} 0 \\ \cos(\phi) \\ \sin(\phi) \end{pmatrix}. \quad (3)$$

$A_1(\text{TO})$ modes in parallel (\parallel) polarization on the (100) plane are thus predicted to obey the intensity function

$$I_{(100)}^{A_1(\text{TO}), \parallel} \propto \left| \begin{pmatrix} 0 \\ \cos(\phi) \\ \sin(\phi) \end{pmatrix} \cdot \begin{pmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & c \end{pmatrix} \cdot \begin{pmatrix} 0 \\ \cos(\phi) \\ \sin(\phi) \end{pmatrix} \right|^2 \quad (4)$$

$$= |b \cdot \cos^2(\phi) + c \cdot \sin^2(\phi)|^2.$$

This approach is, strictly speaking, only applicable for isotropic crystals. A complete derivation of angular intensity functions for anisotropic crystals would necessitate a description in the framework of an extended Raman tensor formalism for anisotropic crystals as proposed and applied to β -Ga₂O₃ in a pair of previous studies.^{58,75} For the presently available κ -Ga₂O₃ samples the domain structure and comparatively large phonon linewidths paired with the overlapping of Raman modes inhibit a quantitative analysis of Raman tensor elements, allowing us to limit our analysis to the common Raman tensor formalism. Table 3 summarizes the intensity functions expected for monocrystalline κ -Ga₂O₃ on the basis of the common Raman tensor

Table 3 Angular-dependent intensity functions of monocrystalline κ -Ga₂O₃ for backscattering geometries calculated by substituting parameterized polarization vectors \vec{e}_i and \vec{e}_s into eqn (2). \parallel or \perp denote a parallel or crossed polarization of the incident light with respect to the scattered. ϕ designates the rotational angle of the polarization vectors with respect to the sample. a , b , c , d , e and f are the Raman tensor elements, with LO and TO abbreviating longitudinal or transverse optical phonons. Modes not listed have vanishing intensities in the respective polarization configuration

| Plane | Phonon mode | \parallel | \perp |
|-------|------------------|---|---|
| (100) | $A_1(\text{TO})$ | $ b \cdot \cos^2(\phi) + c \cdot \sin^2(\phi) ^2$ | $ (c - b) \cdot \sin(\phi) \cos(\phi) ^2$ |
| | $B_2(\text{TO})$ | $f^2 \cdot \sin^2(2\phi)$ | $f^2 \cdot \cos^2(2\phi)$ |
| (010) | $A_1(\text{TO})$ | $ a \cdot \cos^2(\phi) + c \cdot \sin^2(\phi) ^2$ | $ (c - a) \cdot \sin(\phi) \cos(\phi) ^2$ |
| | $B_1(\text{TO})$ | $e^2 \cdot \sin^2(2\phi)$ | $e^2 \cdot \cos^2(2\phi)$ |
| (001) | $A_1(\text{LO})$ | $ a \cdot \cos^2(\phi) + b \cdot \sin^2(\phi) ^2$ | $ (b - a) \cdot \sin(\phi) \cos(\phi) ^2$ |
| | A_2 | $d^2 \cdot \sin^2(2\phi)$ | $d^2 \cdot \cos^2(2\phi)$ |

formalism. The quantitative values of the Raman tensor elements of all 117 optical phonon modes calculated by DFPT are listed in Tables S1–S3 in the ESI.†

For excitation on the (100) or (010) facets, $B_1(\text{TO})$ and $B_2(\text{TO})$ angular mode intensities should be characterized by equally-intense maxima, whereas the linear combination of $\cos^2(\phi)$ and $\sin^2(\phi)$ functions may give rise to distinctively intense maxima for $A_1(\text{TO})$ modes, enabling to distinguish $A_1(\text{TO})$ from $B_1(\text{TO})/B_2(\text{TO})$ modes on the basis of their angular intensity variations. Modes of $A_1(\text{LO})$ and A_2 symmetries may be distinguished analogously when exciting the (001) plane.

3.2 Polarized Raman spectra of the investigated orthorhombic thin film containing rotational domains

The Raman-active phonon modes of different vibrational symmetries are separated by measuring in the geometries illustrated in Fig. 3.

The sample is irradiated in a confocal (a) and cross-sectional (b) setup to access the (001) plane or the edge, respectively. The choice of the (001) plane or the edge is advantageous as it enables the selected detection of Raman modes with different vibrational symmetries and thus facilitates the separation of modes with closely matching phonon frequencies.

In the confocal measurements (Fig. 3a), the microscope's z-focus was moved to maximize or minimize the signal contribution from the thin film or sapphire substrate, respectively. For the cross-sectional configuration (Fig. 3b), we performed line scans with 200 nm step size to identify a position for long integration Raman measurements, for which the κ -Ga₂O₃ or Al₂O₃ related Raman modes reach maximum or minimum intensities.

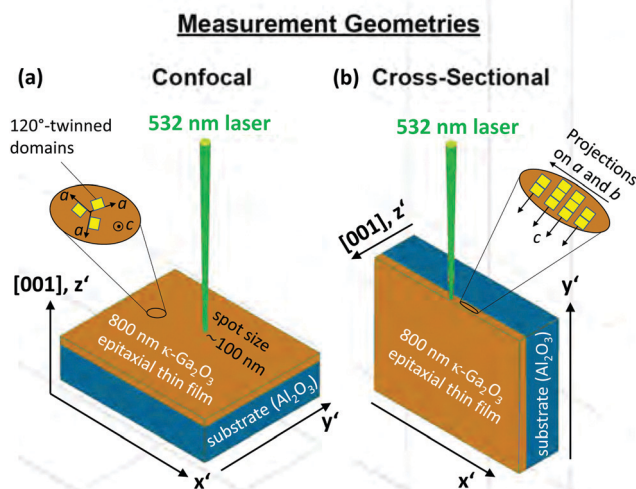


Fig. 3 Schematic illustration of sample setup, plane orientation, and measurement geometry. The (001) plane was accessible in (a) confocal micro-Raman scattering. The z' and x' , y' directions of a Cartesian coordinate system are oriented perpendicular to the (001) plane and parallel to the edges. Spectra recorded in a (b) cross-sectional set-up are acquired by focusing the laser onto the edge (right). The insets indicate (a) the 120° rotation of orthorhombic domains around the c -axis or (b) the columnar c -oriented structure perpendicular to the (001) plane.



Though the domain structure, characterized by the 120° rotation of orthorhombic domains within the (001)-plane, inhibits the direct application of monocrystalline selection rules, our analysis indicates that selection rules can, with certain constraints, be utilized to account for the observed Raman spectra in Fig. 4a–d.

Owing to the orthorhombic domains being rotated 120° against each other, the orientations of the crystallographic a and b directions within the (001)-plane are not well-defined (cf. Fig. 3a). As a result, the sample's edges do not coincide with the a or b axes (cf. Fig. 2), yet are orthogonal to the [001] direction (c -axis). Moreover, as the a and b axes are perpendicular to each other, each edge represents a linear superposition of these two crystallographic directions. Thus, by exciting the edge and selecting the polarization vectors parallel to it (scattering geometry $y'(x'x')\bar{y}'$ or $(x'x')$ in short), the observed Raman spectrum in Fig. 4a corresponds to neither the monocrystalline orthorhombic (aa) nor (bb) configurations, but a superposition (aa + bb). As predicted by selection rules (cf. Table 2), solely $A_1(\text{TO})$ modes are allowed in this configuration. Identical Raman spectra are obtained by probing the other edges of the sample with polarization vectors parallel to the respective edge. For this reason, we restricted the subsequent measurements to the edge exhibiting the strongest signal intensity.

The $y'(z'z')\bar{y}'$ configuration (Fig. 4b) is obtained by rotating the polarization vectors by 90° . As the polarization vector z' coincides with the crystallographic c -direction (cf. Fig. 3), the recorded spectrum should be correlated with the orthorhombic (cc) spectrum, for which all but $A_1(\text{TO})$ modes are prohibited.

In the crossed polarization configuration $y'(z'x')\bar{y}'$ (Fig. 4c) the polarization vectors \bar{e}_i and \bar{e}_s align with the $z' \parallel c$ and x' directions, respectively. With the x' axis being parallel to neither a nor b , the observed Raman spectrum contains contributions from the orthorhombic (ac) and (bc) polarization geometries. The occurring modes are hence of $B_1(\text{TO})$ and $B_2(\text{TO})$ symmetry.

In the confocal geometry utilized to probe the (001) plane (Fig. 4d), the polarization vectors are oriented perpendicular to the c -axis, hence lie within the c -plane. As a result, the parallel polarized confocal Raman spectra nearly replicated the $(x'x')$ Raman spectrum in Fig. 4a, revealing no additional Raman modes. Switching the polarization vectors from parallel to crossed led to a suppression of the Raman modes dominant in the $(x'x')$ configuration, providing access to closely-matching modes or modes residing in the flanks of their more intense neighbors. Despite the recorded Raman spectrum in Fig. 4d not being strictly (ab), the majority of the occurring modes was not observed in the preceding spectra, suggesting this experimental spectrum to be dominated by modes of A_2 symmetry. Intriguingly, no directional dependence is observed when rotating the sample around its surface normal (*i.e.* the c -direction) with respect to a fixed polarization, *i.e.* either parallel or crossed. The absence of any polarization dependence suggests a quasi isotropic behavior, the reasons of which are discussed in detail in Section 3.3.

The spectral positions of the occurring Raman modes in Fig. 4a–d are derived by fitting Lorentzian lineshape functions,

with the obtained peak positions listed in Table 4. For each measurement configuration, we compare the experimental Raman spectra with theoretical spectra obtained by the DFPT calculations to correlate experimentally observed and calculated phonon frequencies (summarized in Table 4). For practical reasons, an LO–TO phonon splitting was neglected in the calculations. We further list modes which are solely Raman-active (R) or both infrared- and Raman-active (I + R).

As an example of allocating experimental and theoretical modes, we first consider the measured $(x'x')$ spectrum in Fig. 4a. As pointed out above, the $(x'x')$ spectrum corresponds to the superimposed calculated orthorhombic (aa + bb) spectrum. Fig. 5 shows a direct comparison of the experimentally and theoretically obtained spectra in this configuration. Calculated phonon frequencies and intensities are indicated by vertical magenta lines. The theoretical spectrum is generated by applying a line broadening of 10 cm^{-1} with Lorentzian line shape to facilitate a direct comparison with the experimental spectrum in Fig. 4a. A good qualitative agreement between experimental and calculated spectra is evident. As a general observation, the obtained peak positions are slightly underestimated by the calculations for the majority of the modes. A compilation of all measured Raman spectra shown in conjunction with their theoretical analogues are presented in Fig. S1 in the ESI†

The experimental Raman mode frequencies are allocated to their most likely theoretical counterparts on the basis of the calculated Raman spectra utilizing the following algorithm: (1) the symmetries of Raman modes allowed in a specific polarization geometry as predicted by selection rules are correlated with the theoretical modes of the same symmetry. (2) Given Fig. 5 or one of the spectra in Fig. S1a–d (ESI†), we presume the same energetic order for both experimental and theoretical modes. (3) Experimental frequencies are usually associated with their energetically closest matching theoretical counterparts. (4) If several theoretical modes are closely-matching and might be allocated to a certain experimental mode, the assignment is based on considering the best matching intensity of experimental and theoretical modes.

A few modes deserve particular attention, as the allocation of experimental and theoretical frequencies is challenging due to closely-matching or overlapping modes or experimental-theoretical analogues not being apparent. By linking the most intense experimental and theoretical modes in the $(x'x')$ (Fig. 5 and Fig. S1a, ESI†) and $(z'z')$ configurations (Fig. S1b, ESI†), we did not identify the theoretical analogues for the experimental modes observed at 93.3 cm^{-1} and 777.5 cm^{-1} . Their presence in the applied polarization geometries suggests an $A_1(\text{TO})$ vibrational symmetry as predicted by selection rules. A small peak observed at 202.6 cm^{-1} corresponds to the strained A_g^3 mode originating from the $\beta\text{-Ga}_2\text{O}_3$ MBE nucleation layer.

Considering the $(z'x')$ spectra in Fig. 4c (or Fig. S1c, ESI†), the experimental mode at 82.4 cm^{-1} corresponds to the A_1 mode previously recorded in Fig. 4a and b (or Fig. S1a and b, ESI†). Further spikes at frequencies lower than 82.4 cm^{-1} are related to neither κ/ε - nor $\beta\text{-Ga}_2\text{O}_3$ nor the Al_2O_3 substrate but originate from randomly scattered light being collected by the



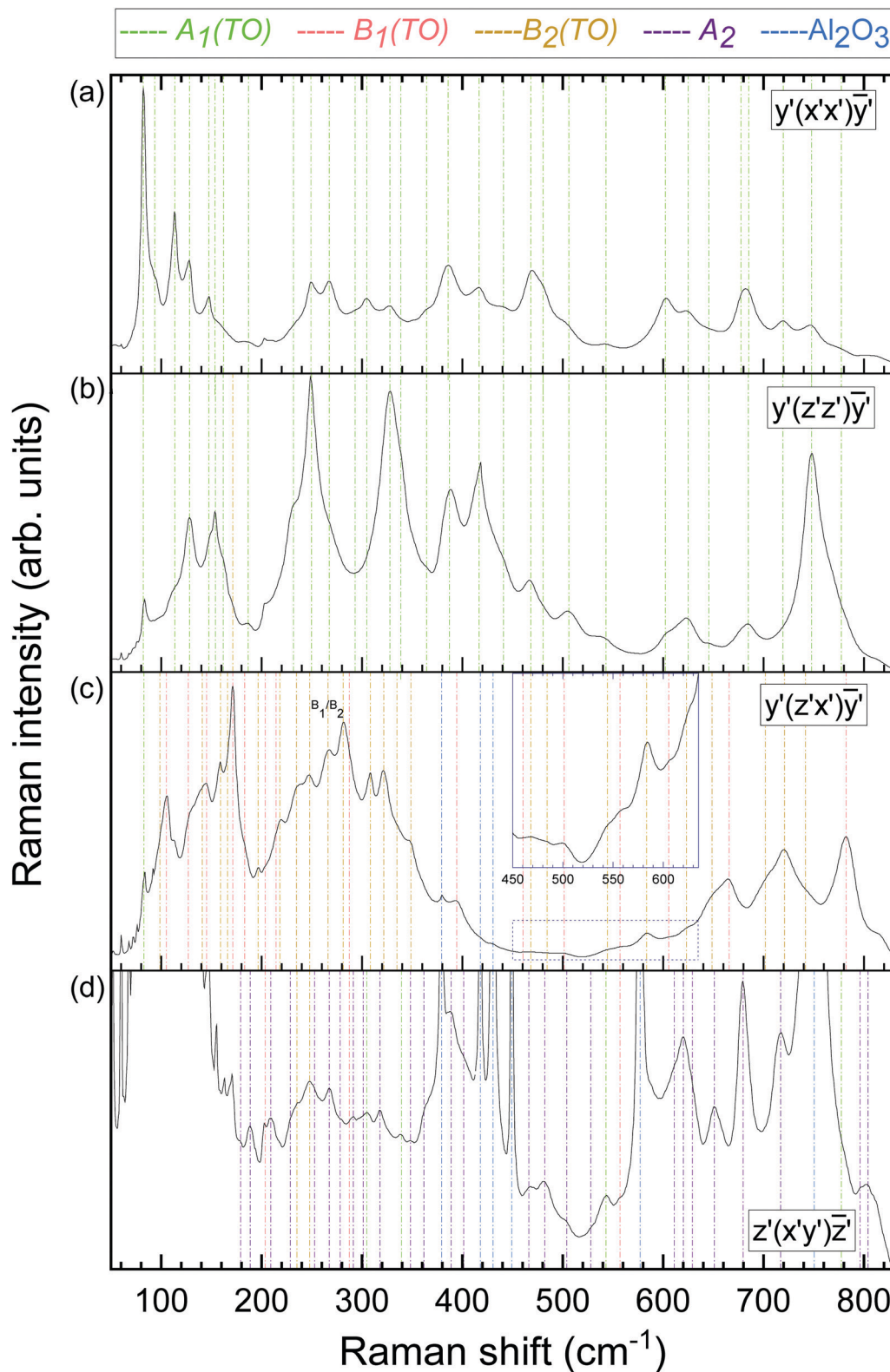


Fig. 4 Raman spectra of the MBE-grown κ -Ga₂O₃ thin film on (0001)-oriented Al₂O₃. (a) Raman spectra in parallel polarization for excitation on the edge. The Cartesian coordinate system x' , y' , z' is chosen such that z' -axis aligns with the [001] direction, with the x' and y' directions oriented according to Fig. 3. In the $y'(x'x')\bar{y}'$ configuration, the polarization vectors are aligned along the excited edge. Mode symmetries of Raman peaks associated with the κ -Ga₂O₃ thin film or sapphire substrate are indicated by vertical dashed lines. A respective line's color denotes the vibrational mode symmetry as provided on top of the graphs. (b) Raman spectra in parallel polarization with polarization vectors aligned along the $z' \parallel c$ axis. (c) Raman spectra of the edge in crossed polarization, with the incident or scattered light aligning with the [001] or x' directions. The inset depicts the spectrum between 450 and 640 cm^{-1} with magnified y -scale. $B_1(\text{TO})$ and $B_2(\text{TO})$ modes are labeled based on their correlation to the calculated Raman frequencies as explained in the text. (d) Confocal Raman spectra in crossed polarization. The spectrum is multiplied by a constant factor to magnify low-intensity modes.



Table 4 Spectral positions of Raman peaks of the phonon modes of κ -Ga₂O₃ obtained experimentally and by DFPT calculations. Peak positions are determined from Fig. 4a–d by fitting Lorentzian lineshape functions. Experimental frequencies are linked to their most likely theoretical analogues. Mode symmetries and activities are derived from the DFPT calculations. I or R denote IR- or Raman-active phonon modes. † denotes experimental modes without theoretical counterparts. Mode symmetries for † experimental modes are deduced based on their occurrence in the respective scattering geometry

| Frequency (exp.) (cm ⁻¹) | Frequency (theo.) (cm ⁻¹) | Mode symmetry | Mode activity | Frequency (exp.) (cm ⁻¹) | Frequency (theo.) (cm ⁻¹) | Mode symmetry | Mode activity |
|---|--|------------------|------------------|---|--|------------------|------------------|
| 82.4 | 73.5 | A ₁ | I + R | 364.0 | 348.4 | A ₁ | I + R |
| 93.3 | | A ₁ † | | 361.7 | 364.5 | A ₂ | R |
| | | A ₂ | R | | 370.4 | B ₁ | I + R |
| 98.7 | 88.8 | B ₂ | I + R | 385.5 | 371.9 | A ₁ | I + R |
| 105.3 | 90.3 | B ₁ | I + R | 394.4 | 386.2 | B ₁ | I + R |
| | 102.1 | A ₂ | R | 416.3 | 386.4 | A ₁ | I + R |
| 113.4 | 106.2 | A ₁ | I + R | | 395.8 | B ₂ | I + R |
| 127.1 | 118.7 | B ₁ | I + R | 389.4 | 396.8 | A ₂ | R |
| 128.0 | 119.2 | A ₁ | I + R | | 398.0 | B ₁ | I + R |
| | 123.2 | A ₂ | R | 440.5 | 411.9 | A ₁ | I + R |
| 140.7 | 135.0 | B ₂ | I + R | | 415.6 | B ₂ | I + R |
| 147.1 | 140.6 | A ₁ | I + R | 401.2 | 420.8 | A ₂ | R |
| 145.1 | 141.1 | B ₁ | I + R | | 422.4 | B ₂ | I + R |
| 153.7 | 149.3 | A ₁ | I + R | 466.2 | 439.6 | A ₂ | R |
| | 149.7 | A ₂ | R | 460.5 | 447.6 | B ₁ | I + R |
| 158.7 | 151.0 | B ₂ | I + R | 468.3 | 454.8 | A ₁ | I + R |
| | 161.0 | A ₂ | R | 482.2 | 462.6 | A ₂ | R |
| | 162.5 | B ₂ | I + R | 480.3 | 464.3 | A ₁ | I + R |
| 162.0 | 165.6 | A ₁ | I + R | 468.4 | 468.5 | B ₂ | I + R |
| 165.9 | 166.1 | B ₂ | I + R | 503.9 | 486.3 | A ₂ | R |
| 171.4 | 167.7 | B ₁ | I + R | 484.2 | 491.2 | B ₂ | I + R |
| 179.0 | 171.6 | A ₂ | R | 504.7 | 497.0 | A ₁ | I + R |
| 186.6 | 183.0 | A ₁ | I + R | 501.8 | 498.3 | B ₁ | I + R |
| 188.8 | 183.7 | A ₂ | R | 544.4 | 530.5 | B ₂ | I + R |
| 182.4 | 191.2 | B ₁ | I + R | | 533.2 | B ₁ | I + R |
| 209.2 | 197.5 | A ₂ | R | 527.5 | 540.1 | A ₂ | R |
| 196.5 | 204.6 | B ₂ | I + R | 542.8 | 541.6 | A ₁ | I + R |
| | 206.1 | B ₁ | I + R | 557.8 | 553.5 | B ₁ | I + R |
| 214.5 | 213.6 | B ₁ | I + R | 583.4 | 577.4 | B ₂ | I + R |
| 230.7 | 220.1 | A ₁ | I + R | 610.8 | 583.0 | A ₂ | R |
| 218.3 | 221.1 | B ₂ | I + R | 602.0 | 595.8 | A ₁ | I + R |
| 228.4 | 223.8 | A ₂ | R | 619.6 | 610.1 | A ₂ | R |
| 234.7 | 225.7 | B ₂ | I + R | 605.7 | 610.9 | B ₁ | I + R |
| | 227.6 | B ₁ | I + R | 623.2 | 615.6 | B ₂ | I + R |
| 248.9 | 228.6 | A ₁ | I + R | 624.6 | 616.6 | A ₁ | I + R |
| | 241.3 | B ₁ | I + R | 629.2 | 617.5 | A ₂ | R |
| 247.8 | 243.9 | B ₂ | I + R | 648.7 | 631.2 | B ₂ | I + R |
| 252.5 | 245.5 | A ₂ | R | 645.4 | 643.5 | A ₁ | I + R |
| | 252.0 | B ₁ | I + R | 650.2 | 648.3 | A ₂ | R |
| 267.4 | 257.0 | A ₁ | I + R | 658.6 | 653.8 | B ₁ | I + R |
| | 259.5 | A ₂ | R | | 653.9 | B ₂ | I + R |
| 266.0 | 263.3 | B ₁ | I + R | 665.7 | 656.6 | B ₁ | I + R |
| 279.3 | 265.7 | A ₂ | R | 676.6 | 667.9 | A ₁ | I + R |
| 266.0 | 270.8 | B ₂ | I + R | 685.2 | 676.3 | A ₁ | I + R |
| 281.2 | 278.3 | B ₂ | I + R | | 677.6 | B ₁ | I + R |
| 291.3 | | A ₂ † | | 701.7 | 684.9 | B ₂ | I + R |
| 293.4 | 282.0 | A ₁ | I + R | | 685.2 | A ₂ | R |
| 287.4 | 284.7 | B ₁ | I + R | | 689.7 | B ₁ | I + R |
| | 289.3 | B ₁ | I + R | | 693.4 | B ₂ | I + R |
| 308.4 | 291.5 | B ₂ | I + R | | 704.4 | B ₁ | I + R |
| 301.4 | 298.6 | A ₂ | R | 719.3 | 705.0 | A ₁ | I + R |
| 304.5 | 302.7 | A ₁ | I + R | 679.3 | 705.6 | A ₂ | R |
| 318.0 | 303.4 | A ₂ | R | 721.0 | 708.2 | B ₂ | I + R |
| 327.9 | 311.4 | A ₁ | I + R | 715.8 | 715.0 | A ₂ | R |
| | 315.4 | B ₁ | I + R | 747.5 | 733.1 | A ₁ | I + R |
| 348.2 | 320.0 | A ₂ | R | 741.8 | 733.4 | B ₂ † | I + R |
| 321.5 | 320.1 | B ₂ | I + R | 777.5 | | A ₁ † | |
| 338.9 | 329.7 | A ₁ | I + R | 796.9 or 803.7 | 733.8 | A ₂ | R |
| 334.5 | 331.5 | B ₂ | I + R | 782.3 | 764.6 | B ₁ | I + R |
| | 342.7 | B ₁ | I + R | 815.9 | | | |
| 348.8 | 343.2 | B ₂ | I + R | | | | |

CCD camera. Moreover, the experimental mode at 266.0 cm⁻¹ might relate to a pair of closely-spaced theoretical modes of symmetries B₁ and B₂. We therefore consider this experimental

mode to be of symmetry B₁(TO) or B₂(TO) (labeled as B₁/B₂). An experimental mode at 815.9 cm⁻¹ occurring in the (x'x') (z'z') and (z'x') spectra cannot be linked to any theoretical



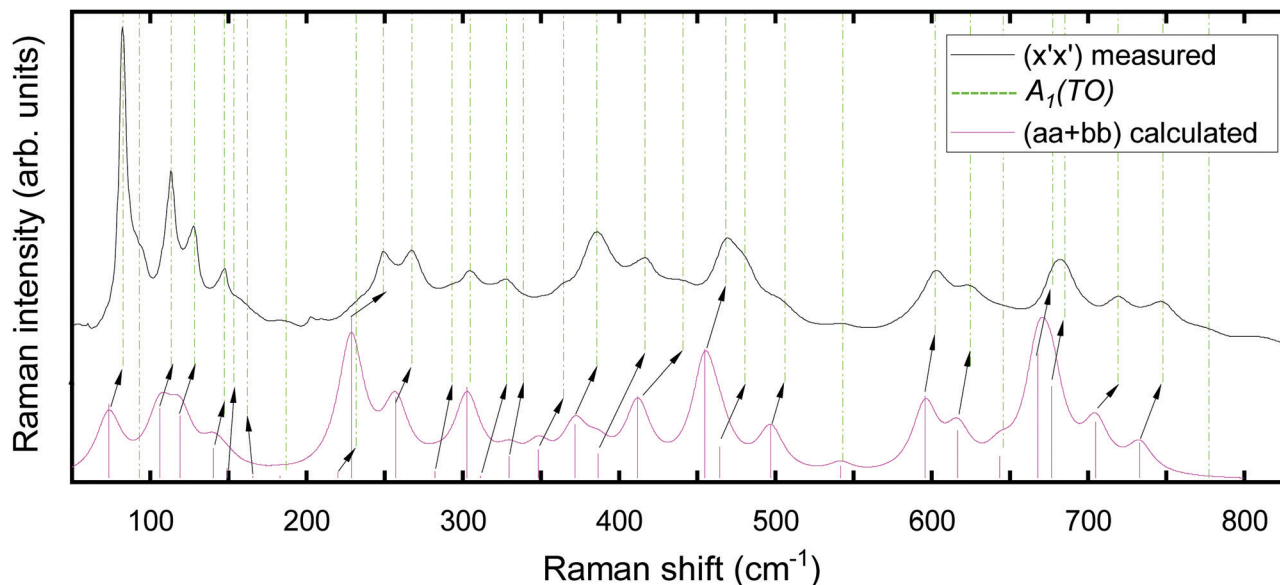


Fig. 5 Raman spectra of the MBE-grown κ -Ga₂O₃ thin film on (0001)-oriented α -Al₂O₃. The measured (black) spectrum in the $y'(x'x')z'$ configuration is shown in conjunction with the calculated (magenta) Raman spectrum and peak intensities (magenta bars) for the orthorhombic (aa + bb) configuration. For clarity, spectra are normalized and vertically offset. The Cartesian coordinate system x', y', z' is chosen according to Fig. 3. Experimental Raman modes of $A_1(\text{TO})$ symmetry (indicated by green dashed vertical lines) are correlated with their calculated (magenta bars) counterparts. Where necessary the correlation is indicated using arrows. The theoretical spectra were generated using the phonon frequencies and intensities based on a FWHM of 10 cm^{-1} .

frequency. As this mode seemingly does not obey Raman selection rules, it might originate from a second-order Raman scattering event.

With regard to the confocal measurements (Fig. 4d or Fig. S1d, ESI[†]), selection rules allow only modes of A_2 symmetry in the (ab) configuration. The appearance of additional modes at energies already observed in Fig. 4a–c is attributed to a relaxation of selection rules due to the (i) orthorhombic domain structure paired with the (ii) utilized objective's large NA (0.9), conditioning the presence of $A_1(\text{TO})$, $B_1(\text{TO})$ and $B_2(\text{TO})$ modes. All modes at frequencies not previously observed are attributed to an A_2 vibrational symmetry and correlated to their respective theoretical counterpart. The experimental mode at 291.3 cm^{-1} can not be linked to any theoretical frequency. Since this mode is present only in the confocal configuration, we ascribe it to an A_2 symmetry. The two closely-spaced experimental modes at 796.9 and 803.7 cm^{-1} might correspond to the theoretical A_2 mode at 733.8 cm^{-1} .

Our detailed analysis enables the determination of the spectral positions of more than 90 experimental Raman modes (summarized in Table 4), which we linked to the orthorhombic crystal structure's 117 theoretical frequencies with their respective vibrational symmetries.

The interplay of several orthorhombic domains produces a pseudo-hexagonal ε structure, associated with the $P6_3mc$ space group, for which the primitive unit cell is expected to contain on average four O atoms and $2\frac{2}{3}$ Ga atoms,⁹ yielding 17 optical phonon modes. Even if all modes were Raman-active, the higher number of phonons obtained in the experimental spectra of the present study provides strong evidence that the

observed Raman modes are not of hexagonal nature, but originate from the orthorhombic film with domains.

3.3 Angular-resolved Raman scans, vibrational dynamics of Raman-active phonons, and the impact of rotational domains

From an experimental perspective, the symmetries of Raman-active phonon modes can be verified by applying angular-resolved Raman scans. By rotating the polarization vectors of both the incident \vec{e}_i and scattered \vec{e}_s light by an angle ϕ relative to the sample's edge, the individual Raman modes generally experience an angular intensity variation. Using Lorentzian lineshape functions to model the individual Raman peaks, the intensities of the individual Raman modes are obtained as the amplitudes of the model fits. Fig. 6 illustrates the Raman intensities plotted against the rotational angle ϕ for a selection of $A_1(\text{TO})$ -, $B_1(\text{TO})$ -, $B_2(\text{TO})$ and A_2 -modes acquired in cross-sectional or confocal measurements.

The selected Raman modes are spectrally well-separated (*i.e.* show little or no overlap with neighboring modes), have comparatively high Raman intensities or allow to identify the symmetries of experimental modes which could not be linked to any theoretical frequencies (*e.g.* the mode observed at 93.3 cm^{-1}).

To model the experimental points, the angular fit formulae in Table 3 need to be modified to account for the domain structure. With regard to the measurements on the sample's edge, which corresponds to a linear combination of the (100) and (010) facets, the experimental Raman intensities of $A_1(\text{TO})$ modes in Fig. 6 are modeled using a linear combination of the (100) and (010) monocrystalline intensity functions from Table 3. As an example, $A_1(\text{TO})$ mode intensity functions in



parallel (\parallel) polarization are thus modified to

$$I_{\text{edge}}^{A_1(\text{TO})\parallel} \propto \underbrace{\left| \begin{pmatrix} 0 \\ \cos(\phi) \\ \sin(\phi) \end{pmatrix} \cdot \begin{pmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & c \end{pmatrix} \cdot \begin{pmatrix} 0 \\ \cos(\phi) \\ \sin(\phi) \end{pmatrix} \right|^2}_{\text{contribution from (100)}} + \underbrace{\left| \begin{pmatrix} \cos(\phi) \\ 0 \\ \sin(\phi) \end{pmatrix} \cdot \begin{pmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & c \end{pmatrix} \cdot \begin{pmatrix} \cos(\phi) \\ 0 \\ \sin(\phi) \end{pmatrix} \right|^2}_{\text{(contribution from (010))}} \\ = |b \cdot \cos^2(\phi) + c \cdot \sin^2(\phi)|^2 + |a \cdot \cos^2(\phi) + c \cdot \sin^2(\phi)|^2 \quad (5)$$

On the contrary, $B_2(\text{TO})$ and $B_1(\text{TO})$ modes occur solely on the (100) and (001) planes. Therefore, their intensity functions need not to be modified. Probing the (001) plane with a laser spot of several hundreds of nanometers in diameter size provides an averaged signal over a large number of orthorhombic domains rotated 120° against each other (*cf.* Fig. 3). As a result, the detected Raman signals originate from three differently oriented species of orthorhombic domains, each species i contributing a fraction of the total Raman signal from a volume fraction ν_i . This necessitates the confocal fit formulae from Table 3 to be modified by containing a linear combination of orthorhombic intensity functions at angles ϕ , $\phi + 120^\circ$ and $\phi + 240^\circ$, scaled with coefficients ν_i . As an example, A_2 modes in parallel polarization thus become

$$I_{(001)}^{A_2\parallel} \propto \nu_1 \cdot \left| \begin{pmatrix} \cos(\phi) \\ \sin(\phi) \\ 0 \end{pmatrix} \cdot \begin{pmatrix} 0 & d & 0 \\ d & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \cdot \begin{pmatrix} \cos(\phi) \\ \sin(\phi) \\ 0 \end{pmatrix} \right|^2 + \nu_2 \cdot \left| \begin{pmatrix} \cos\left(\phi + \frac{2\pi}{3}\right) \\ \sin\left(\phi + \frac{2\pi}{3}\right) \\ 0 \end{pmatrix} \cdot \begin{pmatrix} 0 & d & 0 \\ d & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \cdot \begin{pmatrix} \cos\left(\phi + \frac{2\pi}{3}\right) \\ \sin\left(\phi + \frac{2\pi}{3}\right) \\ 0 \end{pmatrix} \right|^2 + \nu_3 \cdot \left| \begin{pmatrix} \cos\left(\phi + \frac{4\pi}{3}\right) \\ \sin\left(\phi + \frac{4\pi}{3}\right) \\ 0 \end{pmatrix} \cdot \begin{pmatrix} 0 & d & 0 \\ d & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \cdot \begin{pmatrix} \cos\left(\phi + \frac{4\pi}{3}\right) \\ \sin\left(\phi + \frac{4\pi}{3}\right) \\ 0 \end{pmatrix} \right|^2 \quad (6)$$

For an even distribution of orthorhombic domains the volume fractions are related by $\nu_1 = \nu_2 = \nu_3 = \frac{1}{3}$, allowing to

simplify the above equation to

$$I_{(001)}^{A_2\parallel} \propto \frac{3}{2} d^2. \quad (7)$$

The modified fit formulae accounting for the investigated sample's domain structure are listed in Table 5. While the modified angular functions qualitatively resemble their monocrystalline counterparts for $A_1(\text{TO})$ or are identical in the cases of $B_1(\text{TO})$ and $B_2(\text{TO})$ modes, the modified formulae suggest constant angular Raman intensities when illuminating the (001) plane.

By modeling the experimental points in Fig. 6 using the intensity functions from Table 5, an $A_1(\text{TO})$ mode symmetry is proven for a selection of four Raman-active modes for excitation on the edge. Explicitly, the $A_1(\text{TO})$ symmetry for the mode observed at 93.3 cm^{-1} is verified. Furthermore, there exist two species of $A_1(\text{TO})$ modes: (i) One for which the Raman polarizability in parallel polarization is maximal when the polarization vectors align with the edge (x' direction in Fig. 3b) and (ii) one for which modes are 90° phase-shifted. An analogous phase shift was previously observed for $\beta\text{-Ga}_2\text{O}_3$, where the A_g^5, A_g^6, A_g^9 and A_g^{10} are shifted with respect to the $A_g^1, A_g^2, A_g^3, A_g^4, A_g^7$ and A_g^8 modes.⁵⁹ On the basis of angular intensity functions the $B_1(\text{TO})$ and $B_2(\text{TO})$ modes observed at 171.4 cm^{-1} and 281.2 cm^{-1} are qualitatively indistinguishable from each other, but clearly vary from $A_1(\text{TO})$ modes in displaying equally intense maxima. At this point, modes of $B_1(\text{TO})$ and $B_2(\text{TO})$ symmetry can be distinguished from one another solely based on the computed mode symmetries. In consistency with the modified fit formulae for excitation of the (001) plane derived for an even distribution of orthorhombic domains, the Raman intensities remain constant as a function of the rotational angle ϕ for the selected A_2 and A_1 modes. The orthorhombic domains being rotated 120° against each other produce a pseudo-hexagonal ϵ structure (*cf.* Fig. 3a), in which the signals originating from each of the three species of domain orientation compensate each other. Any monocrystalline κ phase components would deviate from the expected curves, demonstrating the investigated film's domain structure through Raman spectroscopy. A preceding study employed angular-resolved Raman scans to investigate the Raman-active A_1, E_1 and E_2 modes in ZnO.⁷⁶ For wurtzite ZnO, ascribed to the same space group as the pseudo-hexagonal $\epsilon\text{-Ga}_2\text{O}_3$ structure, selection rules analogously predict constant Raman intensities as a function of the rotational angle when probing the (0001) plane. On the contrary, the signals from each of the three domain orientations do not compensate each other in the cross-sectional measurement configuration (*cf.* Fig. 3b) in which the laser propagation direction is orthogonal to the c -axis. In this case, the excitation occurs on the lateral faces of several c -oriented orthorhombic columns, giving rise to angular-dependent Raman intensity variations.

In order to obtain insights into the atomic displacements of the Raman modes selected in Fig. 6, the vibrational schemes of the computed Raman modes corresponding to the discussed experimental modes are illustrated in Fig. 7. Since we did not



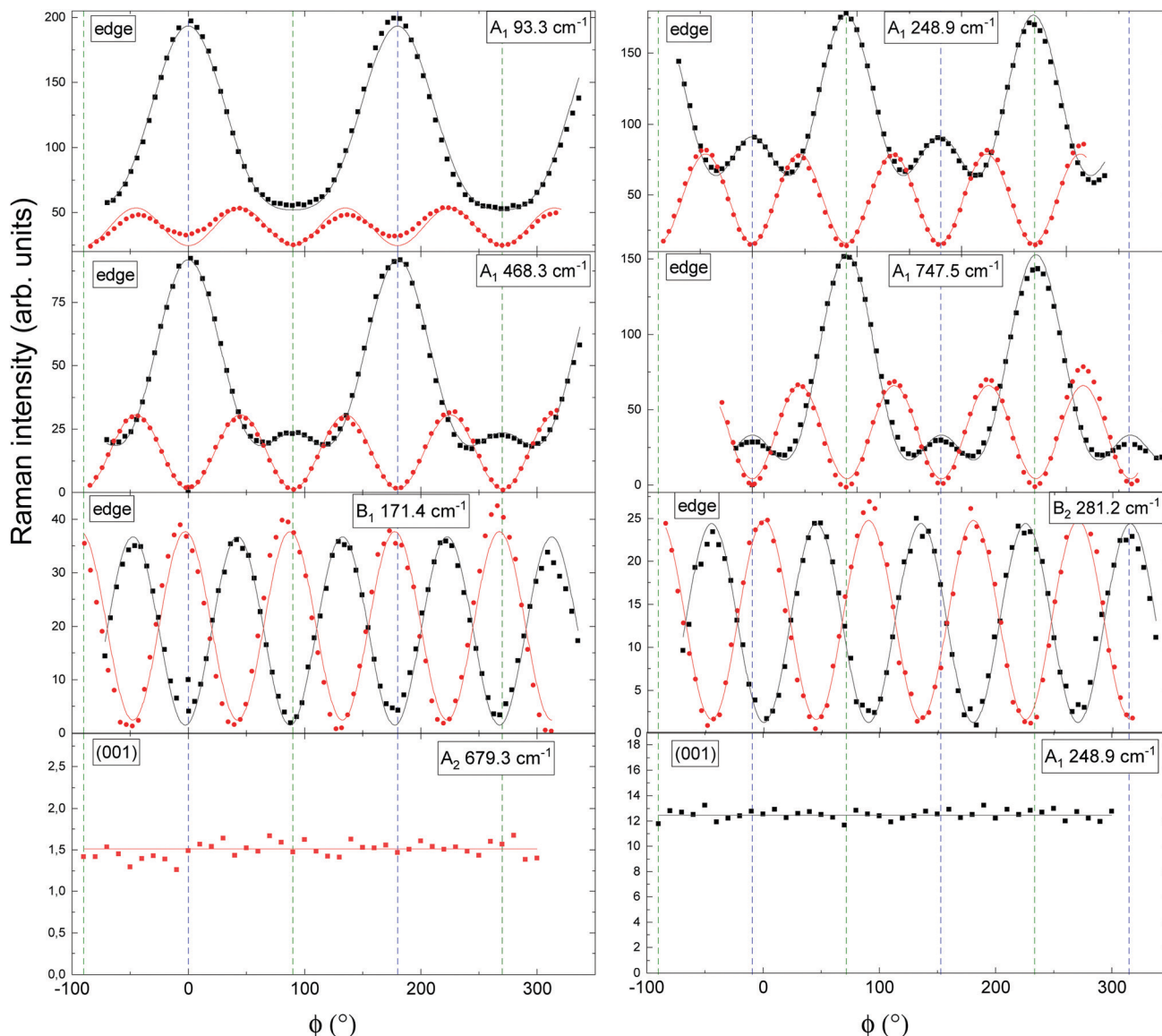


Fig. 6 Angular-resolved Raman spectra of $A_1(\text{TO})$ -, $B_1(\text{TO})$ -, $B_2(\text{TO})$ - and A_2 modes in $\kappa\text{-Ga}_2\text{O}_3$ for cross-sectional or confocal excitation. Points and lines indicate experimental Raman scattering intensities and model fits. Fit functions are listed in Table 5. Black and red color denote parallel and crossed polarization of the incident light with respect to the detected light. The mode symmetry and experimental frequency of each mode is indicated in the top right of each graph. Cross-sectional or confocal measurements are indicated by "edge" or (001). $\phi = 0^\circ$ is set such that it coincides with the x' direction (cf. Fig. 3). In the cross-sectional geometry $\phi = 90^\circ$ corresponds to the [001] direction, while in the confocal geometry it coincides with the y' direction. $\phi = 0^\circ$ and $\phi = 90^\circ$ are indicated by vertical dashed blue and green lines.

Table 5 Modified angular-dependent intensity functions to account for the domain structure of the investigated $\kappa\text{-Ga}_2\text{O}_3$ thin film for backscattering geometries. An even distribution of volume fractions $\nu_1 = \nu_2 = \nu_3 = 1/3$ is considered in the fit formulas' derivation. \parallel or \perp denote a parallel or crossed polarization of the incident light with respect to the scattered. ϕ designates the rotational angle of the polarization vectors with respect to the sample. a , b , c , d , e and f are the Raman tensor elements, with LO and TO abbreviating longitudinal or transverse optical phonons. Modes not listed have vanishing intensities in the respective polarization configuration

| Facet | Phonon mode | \parallel | \perp |
|-------|------------------|---|---|
| Edge | $A_1(\text{TO})$ | $ b \cdot \cos^2(\phi) + c \cdot \sin^2(\phi) ^2 + a \cdot \cos^2(\phi) + c \cdot \sin^2(\phi) ^2$ | $ (c - b) \cdot \sin(\phi) \cos(\phi) ^2 + (c - a) \cdot \sin(\phi) \cos(\phi) ^2$ |
| | $B_1(\text{TO})$ | $e^2 \cdot \sin^2(2\phi)$ | $e^2 \cdot \cos^2(2\phi)$ |
| | B_2 | $f^2 \cdot \sin^2(2\phi)$ | $f^2 \cdot \cos^2(2\phi)$ |
| (001) | $A_1(\text{LO})$ | $\frac{3}{8} \cdot (3a^2 + 2ab + 3b^2)$ | $\frac{3}{8}(a - b)^2$ |
| | A_2 | $\frac{3}{2}d^2$ | $\frac{3}{2}d^2$ |



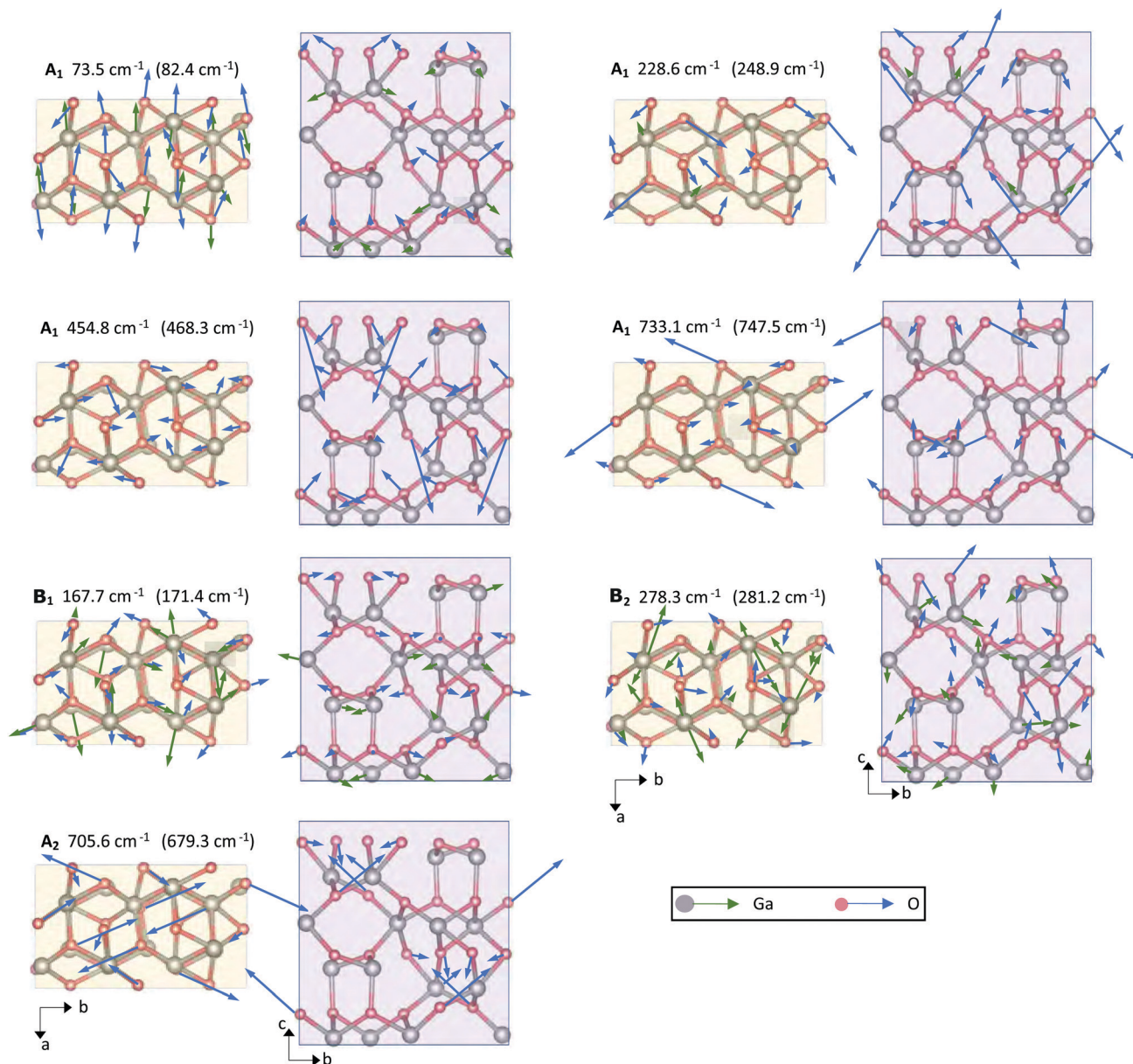


Fig. 7 Schematic illustration of the Raman-active A_1 , B_1 , B_2 and A_2 modes' vibrational schemes within the primitive unit cell of κ - Ga_2O_3 . Modes are shown in projection on the c - or a -plane, with the crystallographic directions denoted by black arrows. A respective mode's vibrational symmetry and computed theoretical frequency are listed on top of each graph. Brackets specify the experimental frequency assigned to the computed mode frequency. Green or blue arrows indicate the displacements of basis atoms, with lengths denoting the amplitude of vibration. Grey or red color denote Ga or O lattice site atoms.

identify a theoretical analogue for the experimental Raman mode at 93.3 cm^{-1} , we consider the vibrational scheme of its lower-energetic neighbor at 73.5 cm^{-1} (theoretical) or 82.4 cm^{-1} (experimental). The depicted vibrational schemes reveal two noteworthy results: (i) irrespective of the mode symmetry, both Ga and O lattice site vibrations occur for the low-frequency modes at theoretical frequencies 73.5 cm^{-1} , 167.7 cm^{-1} , 228.6 cm^{-1} and 278.3 cm^{-1} . Thus, the energy of the low-frequency modes is carried by both Ga and O atoms. (ii) On the contrary, oscillations from Ga lattice site atoms vanish for the high-frequency modes at computed frequencies

454.8 cm^{-1} , 705.6 cm^{-1} and 733.1 cm^{-1} . The high-frequency modes are hence solely governed by O lattice site vibrations. A similar behavior was previously observed for β - Ga_2O_3 , where the relative contribution to a Raman mode's energy from Ga (or O lattice sites) decreased (or increased) with rising Raman frequency.⁶³

4 Conclusions

In summary, we studied the optical phonon spectrum of κ/ϵ - Ga_2O_3 by experiment and theory. Polarized micro-Raman



measurements were conducted on a MBE-grown epitaxial κ -Ga₂O₃ thin film, deposited on top of an (0001)-oriented Al₂O₃ substrate. Cross-sectional and confocal measurement geometries were applied to separate modes of different vibrational symmetries. Our experimental analysis enabled the identification of the spectral positions of more than 90 first-order Raman modes related to orthorhombic κ -Ga₂O₃, which were linked to the calculated 117 Raman active phonons. For the vast majority of Raman modes the vibrational symmetries obtained by the calculations were consistent with the symmetries predicted for the applied measurement configurations based on Raman selection rules. The high number of phonons recorded in the present study ruled out the possibility of Raman modes to originate from the hexagonal phase, for which a significantly lower number of phonons was predicted by theory, proving the orthorhombic nature of the thin film. Further, by applying angular-resolved Raman measurements in cross-sectional and confocal geometry, we experimentally verified the mode symmetries of Raman-active phonons, demonstrating the A₁(TO), B₁(TO), B₂(TO) and A₂ symmetries for a selection of phonon modes. We provided an analytical tool to deal with the effect of the domain structure on the recorded angular Raman intensities. The derived fit formulae exhibited perfect agreement with the experimental data. Explicitly, when exciting the (001) plane in the confocal setup, no angular-dependent intensity variation was observed, which arises from the rotational domain structure producing a pseudo-hexagonal structure, in which the signals originating from each of the three species of 120°-twinned domain orientation compensate each other. Our analysis further indicated that any angular dependence on the (001) plane would result from the presence of monocrystalline components, paving the way to discriminating domain structured from monocrystalline films in future studies. While the employment of specific polarization geometries and angular measurements enabled to distinguish modes of A₁(TO), B₁(TO)/B₂(TO) or A₂ symmetry, the selected detection of B₁(TO) and B₂(TO) modes would necessitate the availability of monocrystalline κ -Ga₂O₃ without rotational domains and make use of the respective selection rules. Lastly, we showed the vibrational schemes for a selection of Raman modes, providing insights into the directions of atomic vibrations within the orthorhombic unit cell. In particular, we showed that while both Ga and O lattice site vibrations occur in the low-frequency modes, high frequency modes are characterized by the absence of Ga and domination of O lattice site vibrations.

Conflicts of interest

There are no conflicts to declare.

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