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Blistering failure of elastic coatings with applications to corrosion resistance†

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A variety of polymeric surfaces, such as anti-corrosion coatings and polymer-modified asphalts, are prone to blistering when exposed to moisture and air. As water and oxygen diffuse through the material, dissolved species are produced, which generate osmotic pressure that deforms and debonds the coating. These mechanisms are experimentally well-supported; however, comprehensive macroscopic models capable of predicting the formation of osmotic blisters, without extensive data-fitting, is scant. Here, we develop a general mathematical theory of blistering and apply it to the failure of anti-corrosion coatings on carbon steel. The model is able to predict the irreversible, nonlinear blister growth dynamics, which eventually reaches a stable state, ruptures, or undergoes runaway delamination, depending on the mechanical and adhesion properties of the coating. For runaway delamination, the theory predicts a critical delamination length, beyond which unstable corrosion-driven growth occurs. The model is able to fit multiple sets of blister growth data with no fitting parameters. Corrosion experiments are also performed to observe undercoat rusting on carbon steel, which yielded trends comparable with model predictions. The theory is used to define three dimensionless numbers which can be used for engineering design of elastic coatings capable of resisting visible deformation, rupture, and delamination.

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1 Introduction

The global cost of corrosion in 2019 is approximately 3 trillion USD, of which between 15% to 35% is preventable.^{1,2} For this reason, there have been concerted political efforts for a more rigorous implementation of corrosion prevention technology in civilian, military, and industrial contexts.^{3,4} Such technology includes, but is not limited to, manipulation of surface^{5,6} and bulk geometry,^{7–9} design of corrosion-resistant alloys,^{9,10} elimination of oxidative environments, application of corrosion inhibitors,^{11,12} anodic protection,¹³ cathodic protection *via* sacrificial anode¹⁴ or impressed current systems,¹⁵ and application of organic^{16,17} and inorganic coatings.^{18,19}

Of the existing corrosion prevention technology, aside from metallurgical modifications, protective coatings remain the most widely used. Various failure mechanisms have been

discussed in the literature, ranging from loss of adhesion due to particulate inclusions⁶ or chemical reactions,^{20–22} salt or solvent entrapment,^{23–27} microstructural defects,^{6,16,24,28} solvent absorption,²³ decreased plasticity due to polymer degradation^{29,30} or loss of plasticizers,^{31,32} and miscellaneous environmental stresses (e.g., accidental scratches).^{33,34} These mechanisms are well-supported by experimental and field observations;^{25,35} however, continuum models capable of predicting failure of protective coatings, without extensive data-fitting, is scarce. This limits the pace of coating development, which is presently reliant on time- and resource-intensive field tests.^{36–38}

In the present work, we focus on osmotic blistering as the primitive form of the failure mechanisms listed above, taking considerable inspiration from the macroscopic delamination physics of van der Meer-Lerk and Heertjes in ref. 35. Van der Meer-Lerk and Heertjes presented some of the earliest works on osmotic blistering on coated metallic surfaces. For example, they successfully predicted the volume of a blister as a function of time using a setup consisting of salt crystals trapped underneath polymeric coatings on steel immersed in deionized water.²⁵ However, their transport model relied on measured blister area as a function of time, which precludes its use for *a priori* model prediction. The aforementioned macroscopic delamination physics also lacks key dependencies on contact angle; as a consequence, van der Meer-Lerk and Heertjes were

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only able to use the pressure chamber data collected in³⁵ to correlate equilibrium adhesion parameters, *versus* the kinetic and equilibrium parameters obtained using the same data sets in Section 3.1 of the present work.

More recent theoretical works on osmotic blistering has been largely and exclusively focused on either the chemical or mechanical components of blistering, the latter usually investigated on a mesoscopic scale. On the chemical side, Li, Lo, and Chang⁶ considered osmotic pressure arising from dissolved soluble components as the primary cause of osmotic blistering, while the work of Leng, Streckel, and Stratmann²¹ hints at cathodic delamination as the primary cause of the phenomenon. The more comprehensive review works of Funke²³ and Hare²⁴ likewise treats the coating as an inert elastic substance that acts largely as a source of soluble components, if any.

On the mechanical side, Castaing, Lemoine, and Gourdenne³⁹ treated blistering as a bulk deformation phenomenon caused by swelling and models it as a circular clamped membrane. We note that the model is developed for polyester laminates with gelcoats, which typically contain considerable amounts of hygroscopic glycols.⁴⁰ This accounts for the exclusive focus on swelling. However, the model can be easily and perhaps more accurately applied to osmotic blistering, as it assumes axisymmetry. Affixed, swollen coats are known to wrinkle and crease instead of forming a smooth spherical segment at high deformations.⁴¹ The approximate quartic solution discussed by Castaing, Lemoine, and Gourdenne more closely resembles the typical morphology of an osmotic blister (see Fig. 7(a)). Nazir, Khan, and Stokes⁴² developed a theory of interfacial fracture at the perimeter of a blister based on the work of Dundurs and Mura.⁴³ While remarkably thorough and simple, *i.e.*, consisting of only algebraic equations, the model makes a strong assumption that interfacial stress is caused solely by transport; the stretching of the coating as a consequence of blister formation is eliminated by the buckling of the interface. This is in contrast to experimental measurements²¹ suggesting that interface buckling does not happen, at least not at the length scale suggested by the authors.

More recent works on mechanical modelling of blisters rely on continuum viscoelastic models solved at the mesoscale using finite element method or some variant of it. Graczyk, Zbiciak, Michalczyk, and Kowalewski⁴⁴ modelled the formation of blisters in between the isolation and subgrade layers of a waterproofed concrete, focusing on the viscoelastic properties of asphalt-aggregate mixtures. Hu, Zhang, He, Midson, and Zhu⁴⁵ modelled the formation of blisters on and in thixocast solids; in this case, pressure is caused by entrapped air which expand upon heating. The study focuses on extent of entrapment as a function of viscoelastic behavior and casting speed. Both of the aforementioned studies provide detailed insights into stress distribution (for ref. 44) and air entrapment/velocity field (for ref. 45) profiles, but do not provide generalized insights into the nature of blistering, as a consequence of the complex nature of the model.

Clearly, there is a need for a macroscopic model which takes into account the chemical and mechanical components of osmotic blistering, especially if such a model can be validated

with experimental data and possesses only a small number of parameters and key physics. The model can then provide generalized insights on osmotic blistering, or potentially blistering phenomenon as a whole, including effects caused by the interaction between the chemical and mechanical components of the model. The present work showcases one such model. In Section 2, we develop a general mathematical model capable of predicting the formation of blisters at a macroscopic scale, and simplify the formulation by assuming an axisymmetric blister overlaying carbon steel, a situation commonly encountered in field applications. In Section 3, we introduce the experimental data sets used to validate the model and the methodology used to analyze raw data sets taken from the literature. In Section 4, we show that the model is able to fit the experimental data sets, validating the hypothesis of an irreversible, nonlinear blister growth rate, and more generally, the growth and deformation of blisters under the influence of osmotic pressure. The model predicts a long-term behavior characterized by a stable, ruptured, or delaminated blister and outlines the initiation, propagation, and termination steps of the blistering process. We then use the theory to define three dimensionless numbers, each classified according to the source of osmotic pressure, which can be used for engineering design of polymeric coatings capable of resisting visible deformation, rupture, and delamination. In Section 5, we discuss the limitations of the model, as well the various other contexts within which the model may be applicable. In Section 6, we summarize the main findings of the work.

2 Mathematical model

Osmotic blisters are formed due to the tendency for water to move from regions of low solute activity to regions of high solute activity. When this transfer occurs across a semi-permeable membrane, *i.e.*, a membrane permeable to water but not to solutes, pockets of soluble materials hydrate and expand, exerting an osmotic pressure on the surrounding matrix. If these pockets are trapped between a coating and a metal surface, the resulting osmotic pressure can push the two materials apart, leading to coating failure.

The entrapped water-soluble components are often salts that are deliberately introduced to modify the properties of the coating or transferred to the metal surface during the coating application process.^{26,27} Small organic compounds have also been considered as possible water-soluble components, especially for poorly-formulated solvent-based paints.²³ Blisters may then develop upon exposure to rain, fog, or other domestic and industrial water sources (*e.g.*, bathroom and kitchen appliances, water tanks).

To illuminate the osmotic blistering mechanism, we will begin by presenting the general form of the model and then provide a more practical axisymmetric formulation.

2.1 Full Model

We treat the coated metal surface as an infinite two-dimensional surface with Cartesian coordinates x and y immersed in an



infinite reservoir of water. The adhesion state is characterized by a binary variable ξ , illustrated in Fig. 1(a):

$$\xi(x, y) = \begin{cases} 0 & \text{if the coating is debonded from the metal at } (x, y) \\ 1 & \text{otherwise} \end{cases}$$

With the implicit assumption that the debonded area is finite, the above formulation is equivalent to the set of perimeters $\{\Omega_i\}$, with each perimeter Ω_i describing a distinct contiguous debonded area. With no loss of generality, we will assume a single contiguous debonded area with perimeter Ω (see Fig. 1(b)) satisfying the parametric equation $\omega(s) = (\omega_x(s), \omega_y(s))$.

This perimeter is associated with a contiguous volume V containing blister fluid at pressure Π . Assuming elastic, isotropic, and sufficiently linear material properties, the coating deforms freely:

$$\Pi = \gamma \nabla \cdot \hat{\mathbf{n}} \quad (1)$$

Here γ is the effective surface tension of the coating and $\hat{\mathbf{n}}$ the unit vector normal to the deformed surface, illustrated in Fig. 1(c). Eqn (1) is solved with the boundary condition:

$$h(\omega_x(s), \omega_y(s)) = 0$$

Eqn (1) describes membrane deformation under pressure for a perimeter affixed on a surface. Here $h(\cdot, \cdot)$ is the blister height at a given coordinate.

Most coatings of practical interest are viscoelastic. However, their viscoelastic relaxation times (~ 1 hour^{46,47}) tend to be much shorter than the timescale associated with the formation of blisters and the attendant coating failure (~ 1 day to 1 year). We thus treat the coating as an elastic material, which can be modelled as a Mooney–Rivlin solid:^{48,49}

$$\gamma = s_1 l(t=0) \left(1 - \left[\frac{A_{\text{base}}}{A} \right]^3 \right) \left(1 - \frac{s_1}{s_{-1}} \frac{A}{A_{\text{base}}} \right) \quad (2)$$

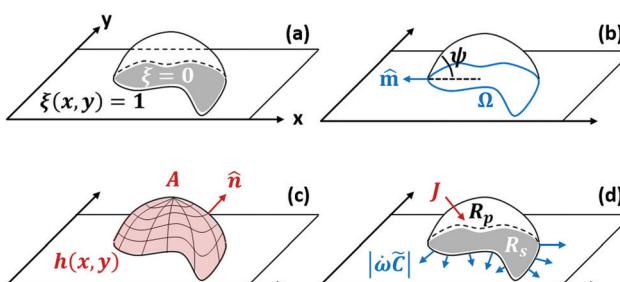


Fig. 1 (a) Isometric view of a blister. Adhesion state is characterized by a binary variable $\xi(x, y)$, which is 0 if the coating is debonded at (x, y) and 1 otherwise. (b) For finite blisters, adhesion state is dual to the perimeter Ω characterized by the unit normal vector $\hat{\mathbf{m}}$. The local contact angle ψ is evaluated in the direction of $\hat{\mathbf{m}}$. (c) Pressure differential (osmotic or otherwise) results in a surface curvature described by the height function $h(x, y)$ with total surface area A . The surface curvature is characterized by the unit normal vector $\hat{\mathbf{n}}$. (d) Our realization of the model considers the effect of heterogeneous reaction rate at the exposed surface R_s , homogeneous precipitation rate in the bulk volume R_p , diffusion through the polymeric coating J , and dissolution through the moving perimeter $|\dot{\omega}C|$.

Here s_1 and s_{-1} are parameters which depend upon the coating under consideration, $l(t=0)$ is the initial/unstretched thickness of the coating, and A and A_{base} are the stretched and unstretched areas of the coating associated with Ω , respectively. Eqn (2) is only valid up to elongation at failure ε :

$$\sqrt{\frac{A}{A_{\text{base}}}} \leq 1 + \varepsilon \quad (3)$$

Beyond this point, the blister breaks. Note that eqn (2) neglects bending moment, which can be included to obtain a more accurate understanding of coating deformation in cases whereby the blister size is of the same order as the coating thickness.

At the perimeter, the interface between the coating and the metal experiences an adhesion stress, which causes the coating to debond from the metal:

$$\frac{d\omega}{dt} \equiv \dot{\omega} = k_{\text{ad}} \hat{\mathbf{m}} (\sigma_{\text{ad}} - \sigma_{\text{ad}}^*) H(\sigma_{\text{ad}} - \sigma_{\text{ad}}^*) \quad (4)$$

Here k_{ad} is the mobility of the interface, $\hat{\mathbf{m}}$ is the unit vector normal to the perimeter at ω on the (x, y) plane (see Fig. 1(b)), σ_{ad} is the adhesion stress, σ_{ad}^* is the critical adhesion stress, and $H(\cdot)$ is the Heaviside function. The critical adhesion stress σ_{ad}^* is an interfacial property which describes stickiness. The adhesion stress describes the magnitude of debonding force at the perimeter:

$$\sigma_{\text{ad}} = \frac{\gamma}{\lambda(\psi)}$$

Here ψ is the local contact angle, which is evaluated from:

$$\tan \psi = -\nabla h \cdot \hat{\mathbf{m}}$$

and λ is a characteristic length over which elastic forces are spread. For an elastic coating with no bending moment, and assuming large blister size relative to coating thickness, this characteristic length is approximately the projected thickness of the coating (visualized in Fig. 2(c) and (d) for an axisymmetric blister),²⁵ which is obtained by solving eqn (1).

The pressure Π can be effected by inertial, viscous, or body forces, but the present work focuses on osmotic pressure. We assume quasi-steady solute distribution within the blister, which holds for most cases of practical interest:

$$Bi = \frac{D_{\text{coat}}}{D_{\text{fluid}}} \frac{L_{\text{fluid}}}{L_{\text{coat}}} \sim 0.001$$

Here Bi is the Biot number, which describes the mass-transfer resistance of the blister fluid relative to the coating, D_{coat} the mass diffusivity of the soluble components in the coating, D_{fluid} the mass diffusivity of the soluble components in the blister fluid, L_{coat} the thickness of the coating, and L_{fluid} the size of the blister. The osmotic pressure can then be calculated from the van't Hoff theory:

$$\Pi = \sum_i \left[\frac{\gamma_i n_i}{V} - \gamma_{i,\text{out}} C_{i,\text{out}} \right] k_B T$$



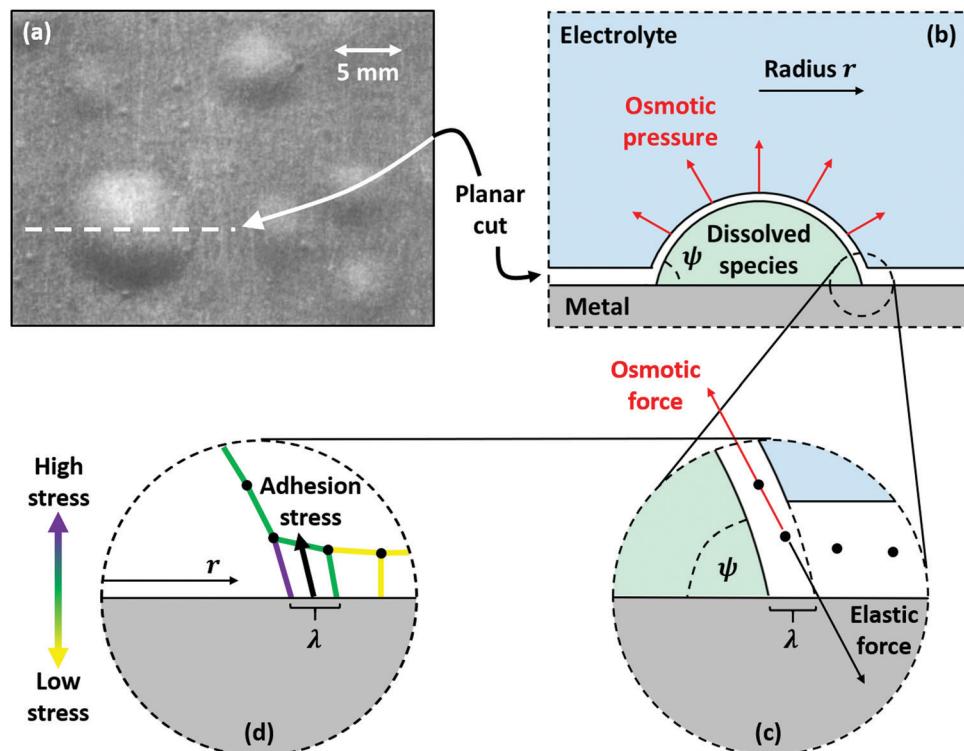


Fig. 2 (a) Light microscopy image of circular blisters formed on epoxy-coated aluminum, taken from ref. 27. Further evidence of circular blisters formed on polymer-coated metals can be found in ref. 6, 23, 24 and 51. (b) Schematic of the blister along the planar cut shown in (a). Osmotic pressure generated by corrosion products and soluble inclusions stretches the coating into a sphere segment with contact angle ψ and base radius r assuming isotropic mechanical properties. (c) A close-up view of the perimeter of the coating shows the balance between osmotic force, obtained by integrating osmotic pressure across the surface of the blister, and the elastic restoring force, which occurs due to polymer stretching. (d) The elastic restoring force incurs a stress on the polymer near the perimeter of the blister. This is the adhesion stress, which must exceed the yield strength of the polymer–metal interface for the blister to grow. The elastic restoring force is spread over a characteristic length scale λ , which is assumed to be the projected thickness of the coating.

Here γ_i is the activity coefficient of species i , n the amount of soluble species, C_{out} the concentration in the bulk electrolyte, k_B the Boltzmann constant, and T the temperature.

The amount of soluble species n_i is tracked using mass balance, as illustrated in Fig. 1(d):

$$\frac{dn_i}{dt} = J_i A + \nu_i R_s A_{\text{base}} + \eta_i R_p V + \oint |\dot{\phi} \tilde{C}_i| d\Omega \quad (5)$$

The four terms on the right-hand side of eqn (5) correspond to flux through the coating $J_i(V, n_i)$, heterogeneous reaction rate at exposed metallic surfaces $R_s(V, n_i)$ with stoichiometric coefficients ν_i , precipitation reaction rate in the blister fluid $R_p(V, n_i)$ with stoichiometric coefficients η_i , and flux through the moving perimeter of the blister, where $\tilde{C}(x, y)$ is the surface concentration of soluble species along the metal/coating interface. The forms of J_i , R_s , R_p , and \tilde{C} vary according to the choice of metal, coating, and coating application.

2.2 Axisymmetric blister

As illustrated in Fig. 2(a) and (b), most blisters of practical interest are approximately radially symmetric, and can be described by the contact angle ψ and the base radius r . With this geometry, eqn (1)–(3), which describe coating deformation

and failure, are simplified to:

$$\Pi = \frac{2\gamma \sin \psi}{r} \quad (6)$$

$$\gamma = s_1 l(t=0) \left[1 - \left(\frac{\sin^2 \psi}{2[1 - \cos \psi]} \right)^3 \right] \left[1 - \frac{s_1 2(1 - \cos \psi)}{s_{-1} \sin^2 \psi} \right] \quad (7)$$

$$\frac{2(1 - \cos \psi)}{\sin^2 \psi} \leq 1 + \varepsilon \quad (8)$$

The debonding rate, *i.e.*, eqn (4) simplifies to:

$$\frac{dr}{dt} = k_{\text{ad}} (\sigma_{\text{ad}} - \sigma_{\text{ad}}^*) H(\sigma_{\text{ad}} - \sigma_{\text{ad}}^*) \quad (9)$$

To reiterate, eqn (6) and (9) describe the balance between elastic and osmotic forces, and the tendency for interfacial bonds to break under stress, respectively. These are illustrated for the axisymmetric case in Fig. 2(c) and (d).

Evaluation of adhesion stress requires additional knowledge of material compressibility. Most coatings of practical interest are designed to be rubbery at room temperature and thus



approximately incompressible,⁵⁰ leading to the expression:

$$\sigma_{\text{ad}} = \frac{\gamma}{l(t=0)} \frac{2(1 - \cos \psi)}{\sin^2 \psi} \quad (10)$$

The osmotic pressure is evaluated assuming an ideal solution:

$$\Pi = \sum_i \left[\frac{n_i}{V} - C_{i,\text{out}} \right] k_B T \quad (11)$$

The mass balance, *i.e.*, eqn (5) is evaluated assuming that all soluble contaminants are initially concentrated at a spot:

$$\frac{dn_i}{dt} = J_i A + \nu_i R_s A_{\text{base}} + \eta_i R_p V \quad (12)$$

Mass transport in the coating is assumed to be Fickian and quasisteady with respect to C , leading to the simple expression:

$$J_i = D_i \frac{C_{i,\text{out}} - C_i 2(1 - \cos \psi)}{l(t=0) \sin^2 \psi} \quad (13)$$

Here $C_{i,\text{out}}$ is the concentration of species i in the bulk electrolyte.

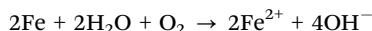
Eqn (6) through (13) complete the mechanical and transport components of the axisymmetric model, which is general with respect to the chemistry of the corrosion reaction. We now turn our attention to a specific realization of the corrosion chemistry.

2.3 Corrosion chemistry

To simplify the system under consideration, we will focus on polymer-coated iron, whose corrosion rate is known to be limited by the transport of oxygen.⁵²

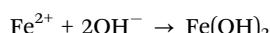
$$R_s = -\frac{D_{O_2}}{\nu_{O_2}} \frac{C_{O_2,\text{out}} - C_{O_2}}{l(t=0)} \left[\frac{2(1 - \cos \psi)}{\sin^2 \psi} \right]^2 \quad (14)$$

Our in-house experiments suggest that the concentration of oxygen within the blister is sufficiently low such that Fe^{2+} is preferentially formed over Fe^{3+} , up to the point where visible blisters form. This corrosion reaction proceeds according to the stoichiometry:



Thus $\nu_{O_2} = -1$, $\nu_{Fe^{2+}} = 2$, and $\nu_{OH^-} = 4$. A more complete discussion of these in-house experiments can be found in Section 4.2.

The corrosion reaction results in accumulation of soluble species, which eventually exceeds its maximum solubility:



In most cases of practical interest, iron corrodes within an electrolyte containing some amount of aggressive anions, *e.g.*, Br^- , Cl^- , $S_2O_3^{2-}$, which can greatly accelerate the corrosion process.⁵³⁻⁵⁶ To improve the utility of the model, we will consider an electrolyte containing NaCl, which modifies the precipitation equilibrium by associating with Fe^{2+} ions:



For simplicity, we will treat Fe^{2+} and $FeCl^+$ as identical as far as the mass balance, *i.e.*, eqn (12) is concerned. The effect of eqn (15) is thus limited to modifying the solubility limit of $Fe(OH)_2$:

$$S_{Fe(OH)_2}^* = S_{Fe(OH)_2} (1 + K_{FeCl^+} C_{Cl^-})$$

Here $S_{Fe(OH)_2}^*$ and $S_{Fe(OH)_2}$ are the solubility limits in the presence and absence of chloride ions, respectively, and K_{FeCl^+} is the equilibrium constant of eqn (15).

In the present work, we will assume a linear non-equilibrium expression for precipitation kinetics, driven by chemical potential difference:⁵⁷

$$R_p = k_p (-\eta_{Fe^{2+}} k_B T \ln C_{Fe^{2+}} - \eta_{OH^-} k_B T \ln C_{OH^-} - \mu^\ominus) \quad (16)$$

Here k_p is the rate constant of the precipitation reaction and μ^\ominus is the chemical potential at the solubility limit. The latter is evaluated from:

$$\mu^\ominus = k_B T \ln \left[S_{Fe(OH)_2}^* \right] - \left[\frac{\beta_p}{C_{Fe(OH)_2}} \right]^2 \quad (17)$$

The second term on the right-hand side of eqn (17) is a chemical potential barrier which prevents rust dissolution in the absence of rust. Eqn (16) is a simplification of true rust precipitation kinetics, which involves slow condensation of a gel-like polymer phase followed by a relatively fast dehydration/crystal growth step.⁵⁸ The true kinetics is further complicated by the presence of aggressive anions, whose impact is still not fully understood.⁵⁹ However, the timescale for rust precipitation (\sim minutes⁵⁸) is much smaller than the timescale for blister formation. In that regard, the exact form of the precipitation rate is not expected to be important, beyond the fact that k_p is large.

2.4 Nondimensionalization

We set the length scale of the problem to the initial thickness of the coating:

$$l_{\text{ref}} = l(t=0)$$

The concentration scale is set by the saturation limit of $Fe(OH)_2$:

$$C_{\text{ref}} = \left[S_{Fe(OH)_2} \left(\frac{z_{Fe^{2+}}}{z_{OH^-}} \right)^{\eta_{OH^-}} (1 + K_{FeCl^+} C_{Cl^-,\text{out}}) \right]^{-\frac{1}{\eta_{Fe^{2+}} + \eta_{OH^-}}}$$

The time scale is set by the transport of oxygen through the coating:

$$t_{\text{ref}} = \frac{l(t=0)^2}{D_{O_2}}$$

The resulting nondimensionalized equations are summarized in the ESI.[†]

2.5 Numerical implementation

The model presented in Table S1 of the ESI,[†] is solved on MATLAB R2020a using the command `ode15s`. The model



combines differential and algebraic equations, which necessitates the mass option. The code is sped up using the vectorized option. The absolute and relative tolerances are set to 10^{-8} and 10^{-6} , respectively. Each simulation takes less than a second to complete.

3 Experimental data and analysis

In this section, we briefly describe the key assumptions and consequences of the model, and describe the experiments which have been performed to validate those assumptions and the model in general. The data in Sections 3.1 and 3.2 is taken from the literature,^{25,35} while the data in Section 3.3 has been generated specifically for the present work.

3.1 Irreversible, nonlinear growth rate

Eqn (4) predicts a linear relationship between growth rate and adhesion stress, but only if the adhesion stress exceeds a critical value.⁶⁰ The bonds between the coating and the underlying metal may be thought of as elastic springs which fail irreversibly under excessive tensile stress (see Fig. 2(d)). This suggests the presence of a parameter which describes the failure stress σ_{ad}^* and a debonding rate which is driven by the tensile stress σ_{ad} . Finally, we speculate, based on considerations of simplicity, that this rate is linear with respect to the driving force beyond σ_{ad}^* .

Anticipating potential confusion in word use, we note that the Heaviside function $H(\cdot)$ renders eqn (4) nonlinear, even if the equation is linear for both $\sigma_{ad} < \sigma_{ad}^*$ and $\sigma_{ad} > \sigma_{ad}^*$. We thus refer to the growth rate as irreversible and nonlinear.

The data validating eqn (4) is taken from ref. 35. A simplified schematic of the experimental setup is shown in Fig. 3. In brief, the setup consists of an airtight deaerated vessel containing water. The top of the vessel is clamped shut with a coated metal

substrate; the metal substrate possesses a pinhole defect of known size. By displacing a piston attached to the vessel, the pressure in the vessel is temporarily raised, causing the coating to deform and detach from the underlying substrate about the pinhole defect. Coating deformation and blister growth causes the pressure to relax, and the pressure of the vessel is tracked as a function of time using a pressure transducer. An optical device consisting of parallel planar light sources of known separation is used to track the height and the contact angle as a function of time.

The experiment was performed using stainless steel substrates. The coatings investigated were polyurethane, epoxy, alkyd, and chlorinated rubber, although van der Meer-Lerk and Heertjes (the authors of ref. 35) were only able to obtain meaningful quantitative polyurethane and alkyd data, the remainder breaking before a sufficiently large data set could be gathered. The stated intention of their work was to investigate a parameter describing the adhesion strength of coating/substrate pairs. In this regard, our aims overlap with theirs; however, our definition of critical adhesion stress σ_{ad}^* is more comprehensive, as it accounts for the effect of deformation at the perimeter of the blister. Furthermore, our theoretical approach differs considerably from that of van der Meer-Lerk and Heertjes, who employed a graphical method reliant on visual extrapolation to zero rate of change of blister area.

In the present work, we have re-processed the polyurethane and alkyd data using eqn (6) and (10). Combining these two equations together, we get:

$$\sigma_{ad} = \frac{\Pi r}{2l(t=0)} \frac{2(1 - \cos \psi)}{\sin^2 \psi} \quad (18)$$

We then plot dr/dt as a function σ_{ad} to determine σ_{ad}^* and validate the form of eqn (4).

3.2 Deformation under osmotic pressure

Our second validation data set is taken from an earlier work by the same pair of authors.²⁵ In brief, droplets containing known amounts of magnesium acetate, potassium hydrogen sulfate, zinc sulfate, or sodium sulfite were deposited on top of polished, degreased stainless steel surfaces. These salts leave behind uniform deposits, which were subsequently coated over with polyurethane, epoxy, or chlorinated rubber. The coated substrates were then immersed in distilled water for 160 days. At irregular intervals, the coated substrates were removed from water, wiped dry, and analyzed using a light-section microscope. The maximum height and the size of the major and minor axes of the blisters were recorded. A summary of the experimental procedure is shown in Fig. 4.

This data set differs from their later work in several respects. Osmotic pressure, effected through entrapped soluble salts, was used in place hydrostatic pressure, which provides a more direct validation of the present work. The accuracy of the measurement was also improved through the use of light-section microscopy, and the analysis allows for ellipsoidal segments, which retains more information concerning the surface area and volume of the blister.

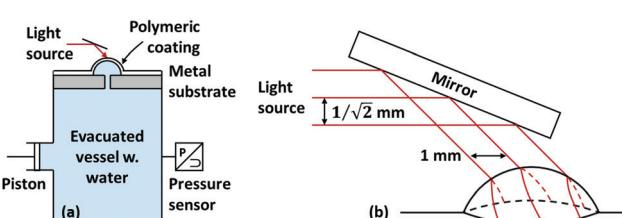


Fig. 3 A simplified schematic of the experimental setup used by ref. 35. (a) The setup consists of an airtight deaerated vessel containing water. A piston, used to modify the pressure within the vessel, and a pressure transducer, used to track the pressure within the vessel as a function of time, are attached to the vessel. The top of the vessel is clamped shut with a coated metal substrate. The metal substrate possesses a pinhole defect of known size. Upon application of pressure, the blister deforms and detaches from the underlying substrate. (b) The curvature of the blister is tracked using an optical device consisting of parallel planar light sources of known separation. The pattern formed on the surface of the blister is recorded and processed assuming that the blister is a sphere segment. Van der Meer-Lerk and Heertjes recorded the average radius, the pressure, and the contact angle as a function of time. For a more complete discussion on the experimental setup, which includes vessel evacuation and substrate replacements/reuse, see ref. 35.



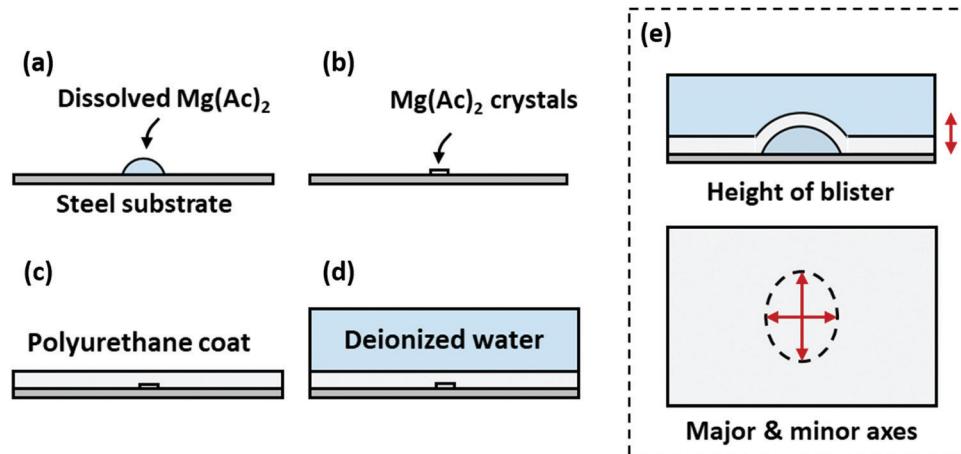


Fig. 4 A summary of the experimental procedure in ref. 25. In chronological order, (a) a known amount of salt dissolved in water is deposited on top of a polished, degreased stainless steel substrate, (b) the solution is allowed to evaporate, leaving behind a uniform layer of salt, (c) a coating is cured on top of the salt, and (d) the coated substrate is immersed in distilled water. (e) The height and the size of the major and minor axes are recorded at irregular intervals using light-sectioning microscopy. Note that the authors have only reported quantitative blistering data sets for magnesium acetate/polyurethane pairs; this has been reflected in the figure.

However, the only blistering data sets which were reported quantitatively by van der Meer-Lerk and Heertjes (in Fig. 2 of ref. 25) are the blister volume *versus* time data for three different amounts of magnesium acetate. Our attempts to recover the remaining data sets are not successful, as the data from the laboratory is lost. We extract the blister volume *versus* time data from Fig. 2 of ref. 25 using the *grabit* toolbox,⁶¹ downloaded from MATLAB central. This data set has been included in the ESI;† for posterity; we recommend not repeating the data extraction procedure using the figures presented in our work, to avoid error accumulation.

The experimental procedures reported in Fig. 4 requires some modification on the basic model reported in Table S1 of the ESI;† and some deductive work based on other data sets reported by van der Meer-Lerk and Heertjes. The model developed in Section 2 assumes that the transport of water is fast relative to the soluble species. This is needed to obtain a well-defined expression for osmotic pressure, which allows the curvature of the blister to be directly evaluated from eqn (6). However, the data sets presented by van der Meer-Lerk and Heertjes were obtained at timescales in which the transport of water dominates coating deformation, and osmotic pressure is not well-defined. We thus modify the basic model by eliminating eqn (6) and (11). The former is replaced by a mass balance for water, *i.e.*, eqn (12) and the latter is replaced with a thermodynamic expression:

$$V = V(n_i, T, P) \approx \sum_i n_i \tilde{V}_i \quad (19)$$

Here \tilde{V}_i is the molecular volume of pure species i . More exact expressions for $V(n_i, T, P)$ can be used, but this suffices for the present work, as most blister fluids of practical interest are dilute.

The diffusivity of water in the polyurethane coating, the Young's modulus of the coating, and the critical adhesion stress of the coating/substrate pair are the missing parameter values.

These parameter values are expected to influence the accuracy of the model substantially, but are strong functions of the coating composition and surface preparation method, which are not comprehensively discussed in the authors' body of work. Since the authors are no longer contactable, we did the next best thing, which is to infer parameters values from the authors' other works. The diffusivity of water is obtained by fitting the steady-state permeation data reported in Fig. 5 of ref. 25 to the following expression:

$$\frac{1}{D_{\text{H}_2\text{O}}} = k_1(1 - x_{\text{H}_2\text{O}}) + k_2 \quad (20)$$

Here k_1 and k_2 are empirical fitting parameters, and $x_{\text{H}_2\text{O}}$ is the mole fraction of water. This data set is obtained through Payne cup measurement and is independent of the validation data set. Refer to the aforementioned work for experimental details on the Payne cup measurement.

Eqn (20) is inspired by the Stokes–Einstein relation, wherein the diffusivity of the dilute soluble species is inversely proportional to size:

$$\frac{1}{D_{\text{H}_2\text{O}}} \sim r_{\text{H}_2\text{O}}$$

Here $r_{\text{H}_2\text{O}}$ is the size of water molecules. Water molecules tend to cluster about the soluble species, which increases the effective size of the species diffusing through the polymer matrix. The simplest form consistent with this expression is:

$$\frac{1}{D_{\text{H}_2\text{O}}} \sim 1 - x_{\text{H}_2\text{O}}$$

Finally, we acknowledge that the Stokes–Einstein relation only holds for dilute soluble species, whereas water is the dominant species of the blister fluid. In particular, it must have a finite self-diffusion coefficient within the coating, giving us the form of eqn (20). The fitting result for the diffusivity of water in



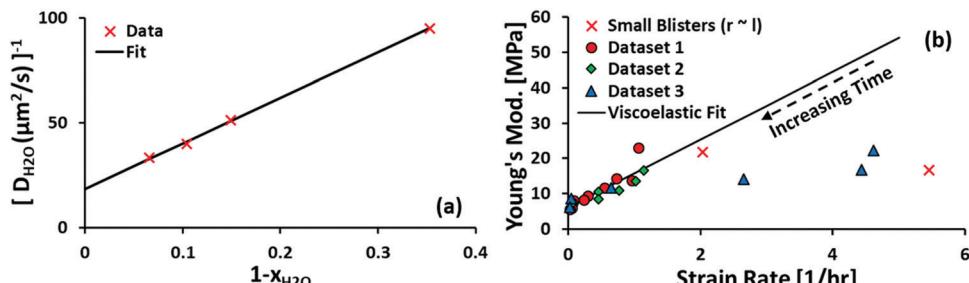


Fig. 5 (a) The semi-empirical fit for the diffusivity of water in polyurethane. The equation of the semi-empirical fit is $D_{H_2O}^{-1} [\text{s } \mu\text{m}^{-2}] = 216.7(1 - x_{H_2O}) + 18.4$. The trend of increasing mobility with decreasing fraction of soluble components is consistent with observations made in the literature^{62–64} for a fairly broad range of solute–solvent pairs. (b) The Young's modulus of polyurethane is found to vary linearly with strain rate at low strain rates. In the present work, and in most cases of practical interest, the strain rate is low, which gives the limiting value $E = 6.2 \text{ MPa}$.

polyurethane is shown in Fig. 5(a). The data used to fit the diffusivity of water in polyurethane is recorded for posterity in the ESI.†

The Young's modulus is obtained by fitting data from van der Meer-Lerk and Heertjes' later work.³⁵ In brief, we solve eqn (6) for each data point reported in Table 1 of ref. 35 assuming $K_{\text{MR}} = -s_1/s_{-1} = 1.5$.⁶⁵ The Young's modulus is obtained from the limiting expression:

$$E = 6s_1(1 + K_{\text{MR}})$$

The Young's modulus is then plotted against the strain rate:

$$\dot{\gamma} = \frac{1 \text{ dr}}{r \text{ dt}}$$

The result is shown in Fig. 5(b). Linear regression is performed for strain rates $\leq 1.5 \text{ h}^{-1}$; the dependence of Young's modulus on strain rate is a clear sign of viscoelastic behavior. For the timescale of practical interest ($\sim 24 \text{ h}$), the strain rate is expected to be negligible, which validates the elastic assumption made in Section 2. We note that the data is heteroscedastic about the best-fit line, which arises because the strain rate is inhomogeneous along the surface of the coating. The smallest strain rates correspond to coatings which have relaxed for the longest duration, for which the heterogeneity is expected to have vanished.

The critical adhesion stress is obtained from the first validation data set discussed in Section 3.1. The set of parameter values used for comparison against the second validation data set is listed in Table 1.

3.3 Critical delamination length

Our third validation data set, generated specifically for the present work, is obtained in relation to three intertwined hypotheses. Combining eqn (9) and (18), and assuming that adhesion stress exceeds critical adhesion stress, we obtain:

$$\frac{dr}{dt} = k_{\text{ad}} \left(\frac{\Pi r}{2l(t=0)} \frac{2(1 - \cos \psi)}{\sin^2 \psi} - \sigma_{\text{ad}}^* \right)$$

Ordinarily, the osmotic pressure Π is inversely proportional to volume ($\sim r^3$) and thus the blister growth stops. However, if the corroding surface can act as a source of soluble materials, then

Table 1 Table of parameter values used for comparison against the second validation data set. The initial blister size $r(t = 0)$ is calculated based on the volume of magnesium acetate droplet at the saturation limit (see ref. 66), assuming a 70° contact angle (see ref. 67). All parameter values are obtained independently of the second validation data set

Symbol	Value	Unit	Note
$C_{i,\text{out}}$	0	mol m^{-3}	
$C_{H_2O,\text{out}}$	55 600	mol m^{-3}	
D_{H_2O}	$216.7(1 - x_{H_2O}) + 18.4$	$\text{s } \mu\text{m}^{-2}$	See Fig. 5(a)
E	6.2×10^6	Pa	See Fig. 5(b)
k_{ad}	2.07×10^{-12}	$\text{m s}^{-1} \text{ Pa}^{-1}$	See Fig. 8(a)
K_{MR}	1.5		See ref. 65
$l(t = 0)$	80	μm	See ref. 25
$n_{\text{MgAc}_2}(t = 0)$	8.81×10^{-9} 2.98×10^{-8} 3.96×10^{-8}	mol	Case 1, ²⁵ Case 2, ²⁵ Case 3, ²⁵
$r(t = 0)$	107 161 177	μm	Case 1, ²⁵ Case 2, ²⁵ Case 3, ²⁵
t_{span}	160	days	See ref. 25
σ_{ad}^*	2.5×10^6	Pa	See Fig. 8(a)
T	298	K	

the osmotic pressure may not decrease with r^3 . Two possibilities arise here – if the solubility limit is not exceeded, then new soluble materials are produced at a rate proportional to the total surface area of the blister ($\sim r^2$). Then at $t \rightarrow \infty$,

$$r \sim t^2$$

Otherwise, the osmotic pressure is set by the solubility limit and is thus approximately constant, with an exponential limiting growth rate:

$$r \sim \exp t$$

We note that this analysis ignores the effect of hydrostatic pressure, which scales with r , but only if the blister is not immersed in electrolyte, which is beyond the scope of the present work.

Assuming that osmotic pressure is set by the solubility limit, a critical length scale emerges:

$$r_{\text{de}}^* = \frac{2l(t = 0)\sigma_{\text{ad}}^*}{\Pi_{\text{sat}}} \frac{\sin^2 \psi}{2(1 - \cos \psi)} \sim \frac{l(t = 0)\sigma_{\text{ad}}^*}{k_B T C_{\text{ref}}} \quad (21)$$



We call this length scale the critical delamination length, defined as the blister size above which unstable growth occurs, leading to delamination. We hypothesize that coating delamination in field applications arise due to this inherent instability.

It is immediately evident to us that Fe(OH)_3 cannot give rise to plausible critical delamination length values. The solubility product of Fe(OH)_3 ($\sim 10^{-38} \text{ M}^4$ ⁶⁸) gives rise to mPa-range osmotic pressure and km-range critical delamination lengths. More probable results are obtained with Fe(OH)_2 , whose solubility product ($\sim 10^{-15} \text{ M}^3$ ⁶⁸) leads to Pa-range osmotic pressure and m-range critical delamination lengths.

This is still large but is calculated assuming a critical adhesion stress of $\sim 1 \text{ MPa}$. There is a consensus within the organic coating literature that the critical adhesion stress of broad classes of polymeric coatings is lowered when corrosion occurs.^{21,23,24,69} This mechanism is termed coating saponification and occurs when ester bonds within the coating break in the high-pH environment of the blister:



Here R_1 and R_2 are hydrocarbon groups. For alkyd and acrylic coatings, ester bonds are located within the backbone and the side chain of the polymer, respectively. For epoxy coatings, ester bonds may be present depending on the choice of curing agent.

We thus have three hypotheses. First, corrosion-induced osmotic pressure can cause unstable delamination for blisters above a certain size. Second, Fe(OH)_3 cannot be reasonably expected to cause unstable delamination in field applications – however, Fe(OH)_2 can. Third, this event is made more probable if there is significant loss of adhesion due to saponification. Ultimately, we were only able to confirm the second hypothesis. However, it seems valuable to discuss our setup, if only to stimulate discussion of potential working variations. We wish to create blisters of known size; from there, we can study the rate of blister growth as a function of its initial size. Our setup consists of 4 by 6 in type-R Q-panels.⁷⁰ On each panel, we apply a circular patch of DuPont non-stick dry film lubricant with Teflon.⁷¹ The circular patch is applied using a small ($\sim 1 \text{ mm}$) cotton swab which has been immersed for 24 hours in excess DI water to remove water-soluble components and dried at room temperature and pressure for a further 24 hours. The lubricant evaporates almost immediately upon application, creating a thin but uneven layer of Teflon which is smooth to the touch. The average thickness of the Teflon layer is calculated from its mass, density, and surface area, and is found to be consistently in between 2 and 4 μm across all panels. At this thickness, the Teflon layer is not expected to provide significant mass-transfer resistance relative to the coating.

Afterwards, 200 μm (wet thickness) water-based coatings are applied using a BYK-Gardner steel drawdown bar. Two commercial acrylic latex anti-corrosion coating formulations (pigmented and non-pigmented), generously provided by Dow Chemical Company, are considered in the present work. The coatings are allowed to dry for 24 hours at room temperature and pressure. After the coatings dry, we affix a 300 mL VWR funnel glass

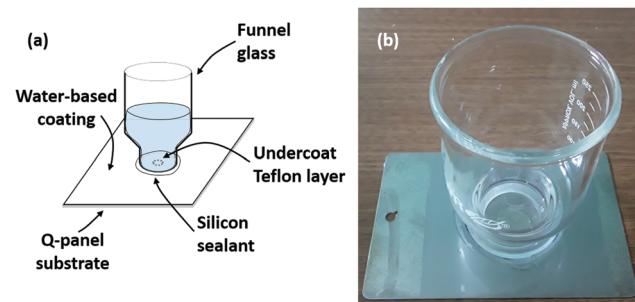


Fig. 6 (a) Schematic of the experimental setup and (b) a physical realization of the setup.

centered at the circular patch of Teflon using Gorilla clear silicone sealant. The sealant is applied over the outer edge of the funnel glass and allowed to dry at room temperature under pressure ($\sim 500 \text{ Pa}$ above atmosphere). The funnel is then filled with 100 mL of DI water equilibrated with air. The top view of the blister is photographed using a Samsung Galaxy S5 at 3, 6, 12, 18, 24, and every 12 hours hence up to 10 days. Every 24 hours, 25 mL of DI water is siphoned off from each container, and the solution is topped up to 100 mL with equilibrated DI water to ameliorate oxygen and water depletion due to corrosion and evaporation, respectively. A schematic of the setup is shown in Fig. 6.

This setup is exploratory in nature, in line with our goal of creating blisters with known initial size. We also explore the effect of adding a pinhole defect at the center of the coating using a 25G medical syringe as a way to initiate blister formation.²³ In all, a total of four factors are explored, namely (1) pigment *versus* no pigment, (2) Teflon *versus* no Teflon (*i.e.*, control), (3) diameter of circular Teflon patch ($\sim 0.5 \text{ cm}$ *versus* $\sim 1.5 \text{ cm}$), and (4) defect *versus* no defect. For each experiment, we perform a replicate, resulting in a total of 24 panels. The list of experiments and a selection of experimental results are shown in the ESI.[†]

4 Model predictions and validation results

Our model predicts the qualitative behavior summarized in Fig. 7. At time $t = 0$, blisters initiate at sites exhibiting a combination of low critical adhesion stress σ_{ad}^* and high solute concentration. Localized loss of σ_{ad}^* may occur due to interface contamination by oils, salts, solids, or other inclusions⁶ which prevent the coating from adhering to the surface. In particular, we note that uneven surfaces, in conjunction with low metal/coating surface energy, encourages entrapment of air bubbles, which behave like unprotected cavities. More generally, coating formulations with low metal/coating surface energy are expected to have low σ_{ad}^* and blister with relative ease. Interface contamination by salts also introduces soluble components which can generate osmotic pressure which drives osmotic blistering. These explain the field observation that coatings tend to last longer when applied on polished, degreased surfaces.



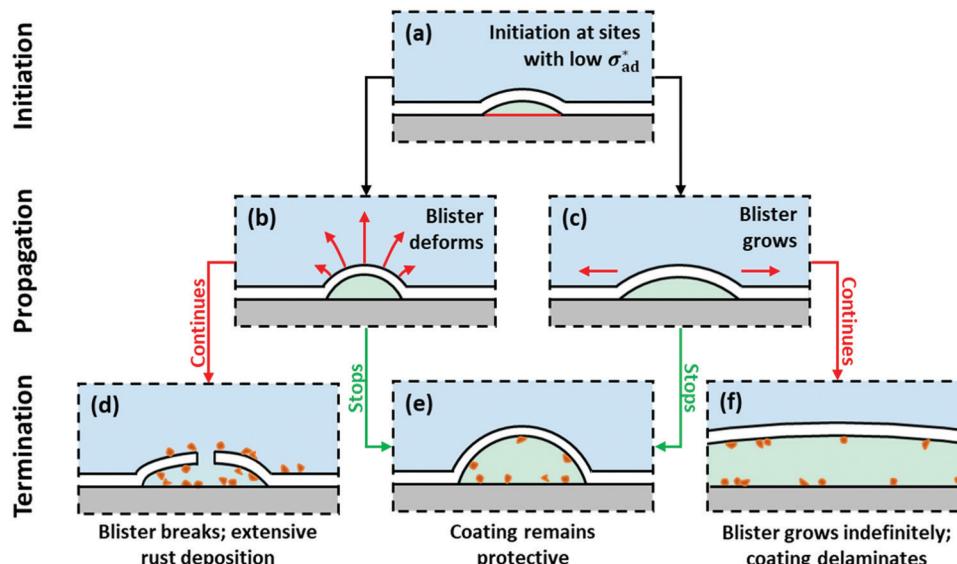


Fig. 7 (a) Blisters initiate at sites with low critical adhesion stress and/or high solute concentration. (b) Blisters propagate by deforming, thus increasing its contact angle, and/or (c) by growing, thus increasing its radius. (d) Deformation may cause the coating to exceed its maximum elongation, which then breaks. If this happens, the exposed steel surface corrodes freely, resulting in extensive rust formation. (e) In the ideal case, deformation and growth stops after some time, and the coating remains protective, i.e., acts as a barrier to transport. Sufficiently small blisters remain invisible to the naked eye, which preserves the aesthetics of the coating. (f) Sufficiently large blisters grow in an unstable manner, causing eventual delamination.

Blisters can propagate by deformation and/or growth, as shown in Fig. 7(b) and (c), respectively. Deformation occurs when adhesion is sufficiently strong to hold the perimeter in place – transport of water causes the blister to swell instead, and the contact angle increases. Growth occurs when adhesion stress exceeds its critical value, and the base radius increases. If deformation and growth stop, the coating remains protective (Fig. 7(e)); as discussed in Section 5, oxidation of Fe^{2+} to Fe^{3+} occurs and a protective oxide layer builds up. This reduces the rate of corrosion, and shifts the solution equilibrium to that of Fe_2O_3 , which does not generate enough osmotic pressure to deform the blister. The blister then deflates. If deformation continues unabated, the maximum elongation of the coating is eventually exceeded (see eqn (3)), and the blister breaks (Fig. 7(d)). If growth continues unabated, the critical delamination length is eventually exceeded, and the coating grows in an unstable manner (Fig. 7(f)), assuming that the surface does not passivate.

4.1 Endpoint classification

The endpoints summarized in the last row of Fig. 7 can be more comprehensively classified by asking three questions:

- (1) Does deformation stop?
- (2) Does growth stop?
- (3) What is the source of osmotic pressure?

In what follows, we discuss each of these possible outcomes and the dimensionless numbers that govern them. The limitations of this classification are discussed in Sections 5.1 and 5.2.

4.1.1 Case 1: deformation does not stop. If the osmotic pressure arises from entrapped soluble components, then blister growth must stop at some point, due to the scaling arguments presented in Section 3.3. Assuming that the coating

is immersed in water, we obtain a scale for the base radius and the osmotic pressure:

$$\bar{r}(\bar{t} \rightarrow \infty) \sim \sqrt{\frac{\sum_i \bar{n}_i}{\bar{\sigma}_{\text{ad}}^*}}$$

$$\bar{\Pi}(\bar{t} \rightarrow \infty) \sim \sqrt{\frac{(\bar{\sigma}_{\text{ad}}^*)^3}{\sum_i \bar{n}_i}}$$

Using these, and the third and fourth equations in Table S1 of the ESI,[†] we estimate the contact angle ψ .

If the osmotic pressure arises from corrosion products, and assuming that the solubility limit of the corrosion products is exceeded, then the osmotic pressure is constant. This osmotic pressure is unlikely to cause critical delamination, due to the small initial size of the blister. We thus expect:

$$\bar{r}(\bar{t} \rightarrow \infty) \sim \bar{r}(\bar{t} \rightarrow 0)$$

$$\bar{\Pi}(\bar{t} \rightarrow \infty) \sim \frac{\sum_i \bar{n}_i}{[\bar{r}(\bar{t} = 0)]^3}$$

As before, using these, as well as the third and fourth equations in Table S1 of the ESI,[†] we estimate ψ .

With ψ available, we calculate the dimensionless number:

$$\pi_{\text{break}} \equiv \frac{1}{\varepsilon} \tan^2\left(\frac{\psi}{2}\right)$$



This dimensionless number describes the tendency for a blister to break. In particular,

$$\pi_{\text{break}} \begin{cases} \gg 1 \rightarrow \text{Blister breaks} \\ \ll 1 \rightarrow \text{Blister does not break} \end{cases} \quad (23)$$

Note that the first line of eqn (23) is a trigonometric simplification of the fifth equation in Table S1 of the ESI.†

4.1.2 Case 2: growth does not stop. As discussed prior, if osmotic pressure is only generated by soluble components, then blister growth must stop at some point. Consequently, the coating cannot be said to be delaminated, *i.e.*, completely detached from the underlying substrate, aside from the subjective aesthetic element of a loosely attached coating.

Let $\bar{r}_{\text{aesthetic}}$ be the size of a blister which is visibly displeasing. Then, if osmotic pressure is generated by soluble components, we can evaluate the dimensionless number:

$$\pi_{\text{aesthetic}} \equiv \bar{r}_{\text{aesthetic}} \sqrt{\frac{\bar{\sigma}_{\text{ad}}^*}{\sum_i \bar{r}_i}}$$

This dimensionless number describes the tendency for the blister to be visibly displeasing:

$$\pi_{\text{aesthetic}} \begin{cases} \gg 1 \rightarrow \text{Blister is displeasing} \\ \ll 1 \rightarrow \text{Blister is not displeasing} \end{cases}$$

On the other hand, if osmotic pressure is generated by corrosion products, then we encounter the case of critical delamination length, as described in Section 3.3 and in eqn (21). The following dimensionless number arises:

$$\pi_{\text{delamination}} \equiv \frac{\bar{r}(\bar{t} = 0)}{\bar{r}_{\text{de}}^*}$$

This dimensionless number describes the tendency of the coating to undergo critical delamination:

$$\pi_{\text{delamination}} \begin{cases} \gg 1 \rightarrow \text{Blister undergoes unstable growth} \\ \ll 1 \rightarrow \text{Blister does not grow} \end{cases}$$

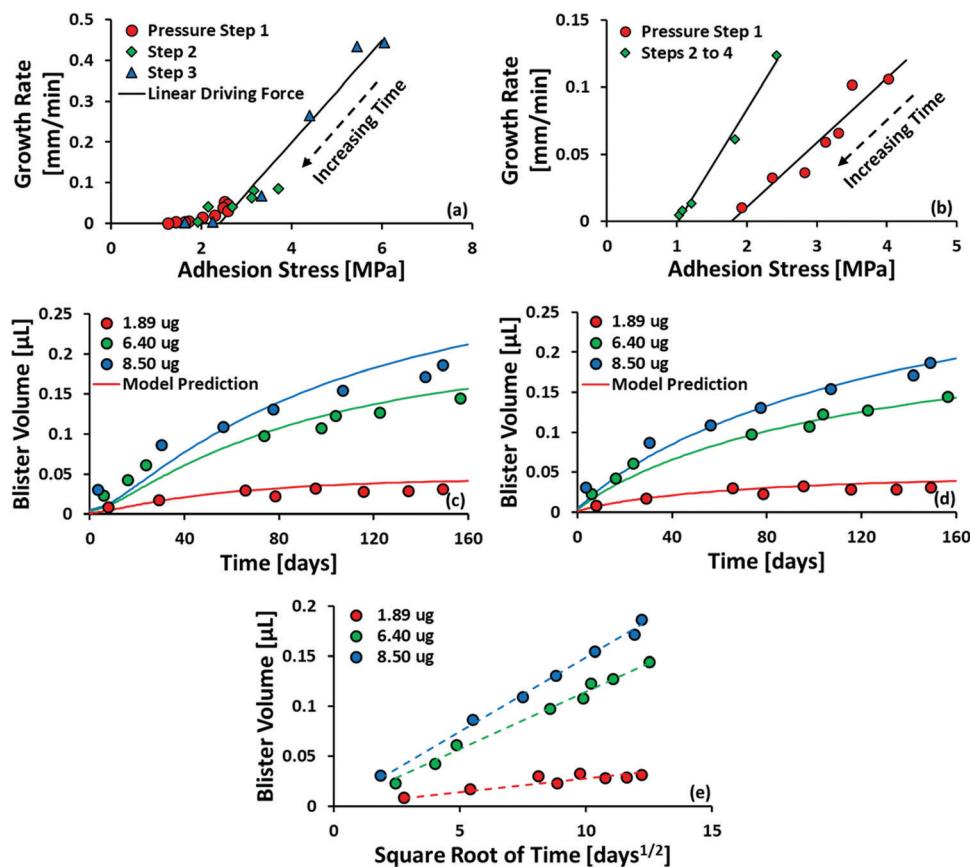


Fig. 8 (a and b) Plot of growth rate as a function of adhesion stress for steel/polyurethane and steel/alkyd, respectively. Adhesion stress is calculated using eqn (10) from the raw data published in ref. 35. Solid black lines are the fit from eqn (9). (c) Plot of blister volume as a function of time. Model prediction has no free parameters, *i.e.*, no fitting is performed. Data is taken from ref. 25. (d) Same as the previous plot, but the diffusivity of water in the coating is assumed to be constant w.r.t. composition and fitted to the data set. The resulting diffusivity is $3.36 \times 10^{-14} \text{ m}^2 \text{ s}^{-1}$, equivalent to the diffusivity at $x_{\text{H}_2\text{O}} \approx 0.95$ based on the correlation in Fig. 5(a). (e) Plot of blister volume as a function of \sqrt{t} . The dotted lines are best-fit linear equations passing through (0,0).

4.1.3 Case 3: deformation and growth do stop. This case is trivial, as it is characterized by the negation of cases 1 and 2, *i.e.*, $\pi_{\text{break}} \ll 1$, $\pi_{\text{aesthetic}} \ll 1$, and $\pi_{\text{delamination}} \ll 1$.

4.2 Model validation

The validation results corresponding to Sections 3.1 and 3.2 are summarized in Fig. 8(a), (b) and (c), (d), respectively. The fit in Fig. 8(a) is excellent, but there is a tendency to underestimate growth rate at low adhesion stress. We considered the possibility of a quadratic dependence on stress difference:

$$\frac{dr}{dt} = k_{\text{ad}} (\sigma_{\text{ad}} - \sigma_{\text{ad}}^*)^2 H(\sigma_{\text{ad}} - \sigma_{\text{ad}}^*) \quad (24)$$

This quadratic dependence could arise due to viscoelastic delay, which can be significant within the timescale of the experiment. To test this hypothesis, we performed a χ^2 test using eqn (10) as the null hypothesis. This leads to a *p*-value of 0.23 and rejection of the quadratic dependence.

Equally good fits are obtained using the alkyd data set (Fig. 8(b)), but only if the data is split into the first pressure step and all subsequent pressure steps. We speculate that there is a considerable time gap between these two subsets of data, during which the interface changes considerably by wetting or corrosion, although this is difficult to verify, as the authors are no longer contactable.

The model prediction in Fig. 8(c) shows good agreement with the data, especially considering that the model prediction is made completely *a priori*, *i.e.*, with no fitting parameters. For $t \lesssim 50$ days, the model under-predicts blister volume and, otherwise, over-predicts it. We suspect that this is caused by an

incorrect diffusion model. As shown in Fig. 8(e), the data set shows a linear dependence on \sqrt{t} for most of the duration of the experiment. This suggests that the diffusivity is constant, in contrast to the result obtained from the Payne cup experiment. A greatly improved fit is observed when $D_{\text{H}_2\text{O}}$ is used as a fitting parameter, as seen in Fig. 8(d).

The fitted value of $D_{\text{H}_2\text{O}}$ is found to be $3.36 \times 10^{-14} \text{ m}^2 \text{ s}^{-1}$, which corresponds to $x_{\text{H}_2\text{O}} \approx 0.95$ using the correlation in Fig. 5(a). We speculate that the failure of the correlation is caused by the unsteady-state nature of the experimental setup in Fig. 4. At time $t = 0$, the coating immersed in DI water is dry; the salt is trapped underneath the coating, and there should be no salt within the coating. Water thus penetrates from the outside into the inside of the blister in its pure state. When the water front begins wetting the salt, the salt dissolves and goes into the coating. This logic suggests that, for most of the early part of the experiment, the average concentration of salt within the pore volume of the coating would be lower than the idealized value of $n_i/2V$ present in the steady-state Payne cup experiment. We believe that the correlation in Fig. 5(a) is valid, but the proper value of $x_{\text{H}_2\text{O}}$ requires modelling of unsteady-state transport through a polymer matrix, which is beyond the scope of the present work.

As discussed in Section 3.3, we were ultimately unable to experimentally verify the existence of a critical delamination length. However, as shown in Fig. 9, there is a clear dark-green patina characteristic of mixed $\text{Fe}^{2+}/\text{Fe}^{3+}$ ions, with a tendency towards lighter green coloration near the delaminating edge of the blister indicating a higher proportion of Fe^{2+} . This is in general agreement with the qualitative prediction of the model

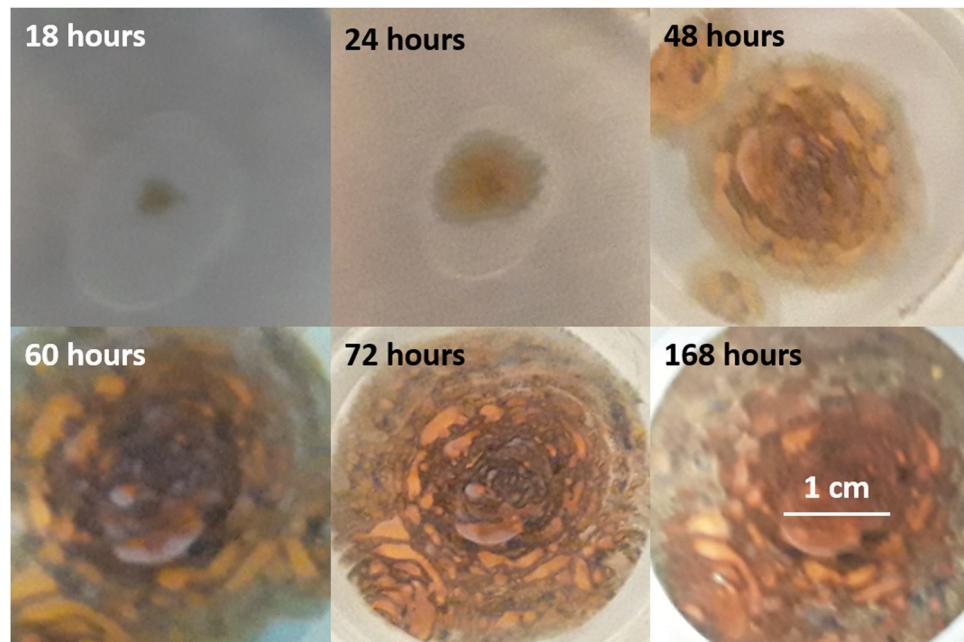


Fig. 9 Development of undercoat blister and rust. This set of figures correspond to experiment 9 as listed in the ESI.† Dark-green coloration is observed at the edge of the blister at all points in time, at least until the blister edge meets the funnel glass. As the blister grows, small pocket-shaped patterns develop. By hour 168, the surface coloration has turned mostly brown. Similar observations were made for other experiments listed in the ESI.† for brevity, these images are placed in the ESI.†



summarized in Fig. 7. As the blister progresses, corrosion produces Fe(OH)_2 , which appears as a green patina. A combination of osmotic pressure arising from corrosion products and saponification due to increased pH causes the coating to detach from the underlying metal substrate. The only aspect which has not been accounted for in the model is the tendency for Fe^{2+} to oxidize to Fe^{3+} near the center of the blister. We speculate on two possible explanations – rust precipitation at the center of the blister could create a protective oxide layer which reduces corrosion, thus increasing the availability of oxygen for oxidizing Fe^{2+} . Alternatively, this could be a consequence of chemical kinetics, *i.e.*, it takes time for Fe^{2+} to be oxidized to Fe^{3+} . In either hypothesis, it makes sense for a metallic surface freshly exposed by the delamination process to show a lighter green coloration.

At first glance, the accelerating growth shown in Fig. 9 seems to support the critical delamination hypothesis, although it is difficult to distinguish whether $r \sim t^2$ or $r \sim \exp t$ as $t \rightarrow \infty$. However, as discussed in the ESI,† the Teflon layer seems to impart a significant degree of corrosion resistance. As a consequence, it is not obvious whether the accelerating growth is due to increasing osmotic force, which scales with the surface area, or due to the corroding area spreading beyond the Teflon patch.

The formation of pocket-shaped patterns radiating outward from the initial defect suggests that coating delamination occurs in batch. In context of the present work, as osmotic pressure builds up, the coating deforms, causing the contact angle to be more obtuse. Following eqn (18), the adhesion stress increases until it exceeds the local critical adhesion stress. If the critical adhesion stress is inhomogeneous, then the boundary slips and the contact angle drops. The process then repeats itself, resulting in the pattern observed in Fig. 9. We note that the pocket-shaped morphology and the batch delamination mechanism closely resemble those observed and proposed by Watson, Coleman, Williams, and McMurray⁷² for filiform corrosion. If our description is accurate, we can further deduce that the length scale of critical adhesion stress inhomogeneity for the metal/coating pair in Fig. 9 is $\sim 100 \mu\text{m}$.

5 Discussion

In this section, we discuss the limitations and applications of the model within and beyond the field of corrosion.

5.1 Effect of surface passivation on model prediction

As illustrated in Fig. 9, a considerable amount of Fe_2O_3 is precipitated at the center of the blister. To what degree does this rust layer protect against corrosion and how does that impact the model predictions?

To our knowledge, even to present day, there is still uncertainty on the degree to which rust precipitation protects against corrosion. On the materials engineering side, the well-known Pilling–Bedworth theory⁷³ predicts a porous unprotective oxide layer, if the oxide is Fe_2O_3 , and a dense protective oxide layer, if

the oxide is Fe_3O_4 , provided that corrosion reaction is sufficiently rapid. Current studies suggest that, aside from the edge of the blister, the oxide produced by undercoat corrosion of iron contains mostly Fe_2O_3 ,²³ a conclusion which is supported by the undercoat visualization results shown in Fig. 9 and more clearly in the photo-micrograph taken by Hare.²⁴ However, other studies have suggested that underneath this layer of Fe_2O_3 , there is a thin layer of Fe_3O_4 .⁵⁴

Furthermore, due to finite oxidation and precipitation kinetics,⁵⁸ one would expect rust to precipitate away from the surface of the metal. This follows from the following sequence of events: Fe^{2+} ions are produced by corrosion, oxidizes in the bulk volume of the blister to Fe^{3+} , and then precipitates on the exposed surface. One would then expect the rust layer to be porous regardless of the Pilling–Bedworth ratio, a conclusion which is supported by high-temperature iron corrosion experiments.⁷⁴ However, the very same set of high-temperature iron corrosion experiments also show the formation of a thin, dense, protective oxide layer underneath a loose, porous one. This is attributed to the Arrhenius dependence of corrosion rate on temperature, which causes the formation of a large excess of Fe^{2+} and Fe^{3+} ions which then precipitate within the pore volume of the porous oxide layer.

The formation of a dense, protective oxide layer is likewise observed in electrochemical experiments. The existence of a passivation potential/regime for corroding steel in some electrolytes is well-known; in brief, as surface potential is increased, instead of an exponentially increasing corrosion rate, as expected from Butler–Volmer theory, the corrosion rate decreases when one goes above the passivation potential.^{52,75} This suggests that very fast corrosion produces excess Fe^{2+} and Fe^{3+} ions which precipitate as a dense, protective layer. However, this passivation regime can quickly vanish when a small amount of Br^- , Cl^- , $\text{S}_2\text{O}_3^{2-}$, *etc.* is added to the electrolyte.^{53–56} The mechanism for loss of passivation in the presence of these aggressive anions is still uncertain,⁵⁹ as is the mechanism by which SO_4^{2-} and NO_3^- reduce corrosion when added to electrolytes containing Cl^- ions.^{76–78}

Our model assumes that O_2 is completely reduced and that osmotic pressure within the blister is set by the solubility limit of the metal salt. This condition is satisfied for reactive alloys with no or no protective oxide layers trapped underneath a semi-permeable membrane, as is the case of the porous oxide layer formed on the carbon steel in Fig. 9. If a dense, protective oxide layer is formed, the osmotic pressure can be instead set by the balance between heterogeneous reaction flux and flux of ions through the semi-permeable membrane. If this is the case, then additional experiments are needed to elucidate the degree to which the oxide layer protects the surface, which can then be incorporated into the model. The difficulty lies in the lack of prior knowledge on the effect of alloy composition and other thermodynamic variables on the protectiveness of the oxide layer.

5.2 Coating defects

The model we present assumes a smooth, isotropic coating. In practice, coatings almost always exhibit some form of defect,



introduced during application or use, *e.g.*, air bubbles during spraying, rugosity due to the bristles of the brush used, and scratches from daily use. These impact the blistering process by providing small open sites where corrosion can take place – the resulting saponification reactions, if applicable, then causes localized loss of σ_{ad}^* , thus initiating osmotic blistering. This phenomenon is clearly observed in Fig. 10, wherein a scratch deliberately introduced to a coating causes the formation of blisters near the scratch, possibly compounded by loss of adhesion due to mechanical damage. At the same time, the presence of such defects can act as locations where ions leak, removing the osmotic pressure needed to cause blistering, provided that the defects are not sealed by the corrosion products.²³

In short, there is considerable uncertainty regarding the protectiveness of oxide layers and the effect of coating defects. Given that most practical setups incorporate some amount of aggressive anions and operate at corrosion potential, there should be a lack of protective oxide layers in most field applications. If the surface does form a protective oxide layer, or if there is a large pinhole defect which allows the content of the blister to escape, then critical delamination does not occur; otherwise, the qualitative conclusions of the study is unchanged. However, as far as conservative design is concerned, critical delamination should be considered.

5.3 Filiform corrosion

The present work has been largely focused on osmotic blistering, but the ideas we present can also be used to explain

or at least supplement existing explanations for other corrosion phenomena.

Filiform corrosion refers to the formation of finger-like patterns on coated metals, typically aluminum, when exposed to an environment with high relative humidity. The pattern initiates at macroscopic defects contaminated with aggressive anions and grows in the direction of the liquid-filled “head” while leaving behind a porous oxide-filled “tail”.^{23,72} Due to the large mass-transfer resistance of the coating, the macroscopic defect and oxide tail act as the primary channel through which oxygen is transported to the head.⁷⁹ The boundary between the oxide tail and the liquid-filled head is chevron-shaped due to the oxidation of Fe^{2+} to Fe^{3+} followed by rust precipitation near the relatively oxygen-rich fluid adjacent to the confining cylinder.⁸⁰ We note that the chevron shape can also arise from preferential precipitation at existing surfaces. As the head propagates, precipitation at the tail/head boundary causes a localized decrease in concentration, which drives evaporation through the coating, *i.e.*, loss of osmotic pressure. Non-volatile aggressive anions are concentrated by the evaporation process and diffuse towards the head, which increases the concentration at the head, attracts water from the surrounding, and begins the cycle anew.⁷²

There are three major hypotheses explaining the directional nature of filiform corrosion. In the cathodic delamination hypothesis, relative enrichment of oxygen at the tip of the head, caused by the curvature, encourages O_2 reduction, which increases the local pH, shift the saponification equilibrium (see reaction (22)), and delaminate the coating.^{21,81} In the anodic undermining hypothesis, the oxygen-rich tail/head boundary preferentially acts as the cathode, which induces the tip of the head to act as an anode. This undermines the tip of the head, causing the head to propagate over time.⁸⁰ In the electro-osmotic hypothesis, diffusion and electromigration “pumps” the content of the head in the direction of the tip of the head, causing a mechanical force which separates the coating from the substrate.^{82,83} To our knowledge, there is no clear consensus on the “correct” model for the delamination process.

The present work can contribute to the understanding of filiform corrosion in three ways. One, the aforementioned mechanisms predict growth in a straight line, which is clearly not the case in real setups.^{72,80,84} We propose that sudden changes in filiform growth is attributable to inhomogeneity in critical adhesion stress. If this is the case, then we expect the length scale of the inhomogeneity to be the distance in between sudden changes in growth direction. Two, with some modifications, *e.g.*, implementing kinetics of σ_{ad}^* loss due to saponification (for the cathodic delamination hypothesis) or metal dissolution (for anodic undermining), changing the definition of osmotic pressure to incorporate electro-osmotic forces (for electro-osmotic hypothesis), and/or adding spatial refinement across the fingers, the model presented in Section 2.1 can be adapted to describe filiform corrosion. Finally, due to the similarity in underlying physics, provided that the proper estimates for σ_{ad}^* and Π are available, the classification introduced in Section 4.1 should remain applicable, thus allowing

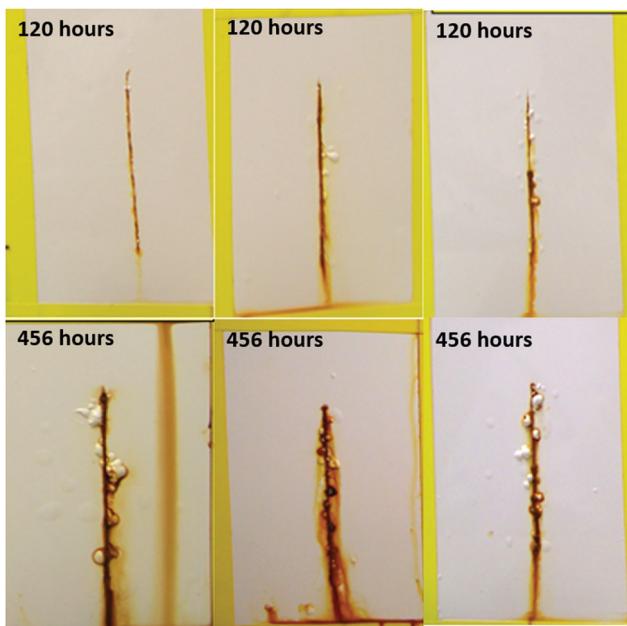


Fig. 10 Blisters develop about a scribe introduced to three different coating formulations undergoing salt spray test. This progression is in agreement with the qualitative description of a surface undergoing saponification about the scribe, followed by blistering driven by osmotic pressure generated by corrosion products. However, for this to happen, defects must become sealed by corrosion products.



prediction of unstable growth, coating rupture, and filiform visibility.

5.4 Other applications of the model

The particular use of metal/coating pairs is not intrinsic to the model. For example, with some modification to the expressions for surface tension (see eqn (2)) and pressure source (see eqn (11)), the model can be directly used to assess the risk associated with formation of hydrogen blisters in aluminum fusion reactors,⁸⁵ or indeed any metal/metal oxide pairs.

The present work focuses on anti-corrosion coatings, but is also applicable to osmotic blistering occurring on non-metallic or passive surfaces coated with other types of elastic coatings. For example, bituminous and polymer-modified bituminous roofings or coatings on concrete, as commonly observed on roads, bridges, buildings, and other infrastructures, often experience osmotic blistering.⁸⁶ For bituminous coatings on concrete, this can enhance corrosion of reinforcement bars affixed within.⁸⁷ In this case, a distinction needs to be made between waterproofed^{86,88} and non-waterproofed coatings.⁸⁹ The former does not allow water to pass through the coating; instead, water passes from the concrete structure underneath, which acts as an inelastic, semi-permeable membrane. This modifies the form of the transport equation, *i.e.*, eqn (5) considerably. Regardless of the direction from which water is transported into the blister, two further modifications are needed to adapt the present work for coated concrete: (1) the soluble components can arise from the concrete mixture^{90,91} and (2) the coating may exhibit orthotropic elasticity.⁸⁸ Nevertheless, the generality of the present work is such that we still expect the conclusions in Section 4.1 to hold despite these mismatches in the exact statement on the model.

The current state of anti-corrosion and bituminous coating design incorporates a significant amount of empirical observation, as evidenced by the plethora of standardized tests for coating development published by the International Organization for Standardization (ISO), the National Association of Corrosion Engineers (NACE), *etc.* Some of these tests can be time- and resource-intensive (see ref. 36–38 and 86, among many others). Classification based on the dimensionless numbers introduced in 4.1 can provide an affordable theoretical alternative for coating development, although more experimental verification is needed.

Our model could also be applied in medical settings, *e.g.*, formation of blisters on the skin upon exposure to heat sources^{92,93} or after excessive rubbing,⁹⁴ the latter possibly exacerbated by hereditary illnesses, *e.g.*, epidermolysis bullosa. In this context, the pressure source is the heart, from whence we make several predictions: (1) blistering should be more extensive when it occurs in the vicinity of arteries closer to the heart, (2) blistering should be more extensive in locations where the critical adhesion stress of neighboring pairs of skin layers is lower, (3) blisters exceeding a critical size undergo runaway growth – a situation which may assist in understanding the effect of extensive burns. We note that, in agreement with the prediction of the model, epidermolysis bullosa has been

extensively linked to the inability to form functional structural proteins, which is expected to reduce critical adhesion stress.^{95–97} The model is also more generally applicable to biological sciences, *e.g.*, to understand the mechanics of biofilm growth⁹⁸ or deformation of dentin adhesives.⁹⁹

6 Conclusion

The present work builds upon existing understanding of blister formation to arrive at a comprehensive macroscopic model of osmotic blistering. Blisters initiate at locations with low critical adhesion stress and/or high local solute concentration and propagate by growth and/or deformation. Irreversible blister growth occurs when adhesion stress exceeds the critical adhesion stress of the metal/coating pair, and deformation occurs when osmotic pressure exceeds the elastic stress of the coating. If the growth continues unabated, the coating eventually becomes delaminated, and if deformation continues unabated, the coating eventually ruptures. The present work distinguishes between osmotic pressure arising from entrapped solutes and osmotic pressure arising from corrosion products. In the former, blister growth eventually stops due to decaying osmotic pressure; however, depending on the kinetics of delamination and the critical adhesion stress, the maximum elongation of the coating may still be exceeded, causing rupture. In the latter, we predict the existence of a critical delamination length, beyond which unstable blister growth occurs.

The model has been validated against blister growth data. We were able to confirm that blister growth is irreversibly driven by difference between adhesion stress and critical adhesion stress using two separate data sets employing polyurethane and alkyd coatings on steel. We were also able to predict the volume *vs.* time data of polyurethane coatings immersed in water with various amounts of undercoat magnesium acetate with no fitting parameters. We then use the model to develop three dimensionless numbers, each classified according to the source of osmotic pressure, which can be used for engineering design of polymeric coatings capable of resisting visible deformation, rupture, and delamination.

Author contributions

Surya Effendy and Tingtao Zhou conceptualized the idea of a quantitative macroscopic model for osmotic blistering. Surya Effendy conceptualized the idea for irreversible blister growth driven by difference between adhesion stress and critical adhesion stress (see Section 3.1). Surya Effendy conceptualized the idea of endpoint classification using dimensionless numbers (see Section 4.1).

Surya Effendy investigated and curated the data published in ref. 25 and 35, specifically by extracting the data using an image analysis tool and reporting those data for posterity (see Tables S2 and S3 of the ESI†). The data were subsequently used, also by Surya Effendy, to validate components of the model.

Henry Eichman investigated the formation of blisters about macroscopic defects, leading to Fig. 10.

Michael Petr and Martin Z. Bazant acquired the funding needed to perform this study through the University Partnership Initiative. Michael Petr represented Dow Chemical Company at the time this work was conceived. Martin Z. Bazant heads the Bazant Research Group, in which this work was performed, and provided the resources needed to validate the critical delamination length hypothesis.

Surya Effendy created almost all aspects of the model; however, it should be made clear that pieces of the model were already in the literature when the model was conceived. Tingtao Zhou pointed out the relevance of free volume problem, which became eqn (1). Surya Effendy also wrote the software encoding the model leading to the predictions/fits shown in Fig. 8.

Tingtao Zhou and Martin Z. Bazant supervised the work and provided advice leading to the publication of the manuscript. Surya Effendy visualized the data, model predictions/fits, and schematics, and wrote the original draft of the manuscript. Tingtao Zhou, Michael Petr, and Martin Z. Bazant contributed in various ways towards reviewing and editing the manuscript.

Conflicts of interest

There are no conflicts of interest to declare.

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