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# Strain- and field-induced anisotropy in hybrid elastomers with elongated filler nanoparticles†

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The implementation of anisotropy to functional materials is a key step towards future smart materials. In this work, we evaluate the influence of preorientation and sample architecture on the strain-induced anisotropy in hybrid elastomers containing covalently attached elongated magnetic filler particles. Accordingly, silica coated spindle-type hematite nanoparticles are incorporated into poly(dimethylsiloxane)-based elastomers, and two types of composite architectures are compared: on the one hand a conventional architecture of filled, covalently crosslinked elastomers, and on the other hybrid elastomers that are crosslinked exclusively by covalent attachment of the polymer chains to the particle surface. By the application of external strain and with magnetic fields, the orientational order of the elongated nanoparticles can be manipulated, and we investigate the interplay between strain, magnetic order, and orientational order of the particles by combining 2D small angle X-ray scattering experiments under strain and fields with Mössbauer spectroscopy under similar conditions, and supplementary angular-dependent magnetization experiments. The converging information is used to quantify the order in these interesting materials, while establishing a direct link between the magnetic properties and the spatial orientation of the embedded magnetic nanoparticles.

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## Introduction

Living matter is an important source of inspiration for scientific research, as biological tissue shows an enormous amount of functionality that is unreached by man-made objects in many fields.<sup>1,2</sup> While the elastic modulus of common biological tissue is very similar to typical polymer matrices, the latter are far from reaching the complexity and functionality biological tissues possess.<sup>3</sup> One major difference between biological and common synthetic systems is the degree of anisotropy. While biological structures, like muscles as a prominent example, are built up from hierarchically organized anisotropic structures, which enable their functionality,<sup>4</sup> common polymer matrices such as gels and elastomers are synthesized by homogeneous polymerization techniques, yielding macroscopically isotropic materials.<sup>5</sup>

The incorporation of functionality into polymer matrices is a major field of scientific research in the context of

stimuli-responsive or smart materials.<sup>6,7</sup> Yet, these materials significantly lack to show similar properties to biological tissues, when the responsiveness is not directed by the anisotropy of the matrix. Comparing actuation behavior, the biological system, which is a muscle, allows a reversible uniaxial contraction. The analogous isotropic polymer matrix, *e.g.* a poly(*N*-isopropylacrylamide) hydrogel, only allows a complete collapse of the structure, and thus a significantly smaller contraction effect per spatial direction.<sup>8</sup> In the case that the implementation of anisotropic structural and mechanical properties to a functional material becomes accessible, manifold options arise towards the development of bioinspired, more complex functional or even stimuli-responsive materials. It becomes possible to tailor the direction-dependent behavior of such systems towards strain, temperature, or external fields. A prominent example that has attracted considerable attention and is still an active area of research is liquid crystalline elastomers, that, if processed with manifested anisotropy in the monodomain, can show an uniaxial contraction similar to a natural muscle fiber when exposed to elevated temperatures.<sup>9,10</sup> The incorporation of anisotropy in polymer matrices thus opens the opportunity for directing the response.<sup>11</sup>

In this work, we focus on the introduction of anisotropic material response by using elongated magnetic nanoparticles in elastomeric matrices. The peculiar properties of the filler

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particles allow the manifestation of two types of anisotropy into the nanocomposites. On the one hand, in the case of anisotropic filler particles, if the particles show a preferred orientation in the polymer matrix, the resulting mechanical properties of the network become direction-dependent, as shown for fiber reinforced elastomers.<sup>12</sup> On the other hand, the magnetic moment of the particles can be aligned with an external magnetic field. If the particles are subsequently immobilized by the crosslinking process, the magnetic order is retained for thermally blocked particles, leading to direction-dependent magnetic properties.<sup>13,14</sup>

The aim of this study is to in-depth analyze and compare the interplay between mechanical strain, magnetic field, and the internal geometric and magnetic order of the nanoparticles by using a combination of complementary methods. We investigate the strain- and field-induced geometric and magnetic orientation of the elongated magnetic filler particles in an elastomeric matrix, and how this interplay is influenced by the network architecture and by an intrinsic preorientation of the filler particles.<sup>15</sup> Therefore, we compare conventionally crosslinked poly(dimethylsiloxane) elastomers filled with spindle-like hematite nanoparticles with materials of similar composition, but with an architecture based on covalent particle crosslinking. The latter materials are recently introduced by us as a novel architecture of elastomers, that are crosslinked exclusively *via* surface-attachment of the polymer chains to magnetic nanoparticles.<sup>16–20</sup> These novel hybrid materials show strongly particle content dependent properties. In the case of poly(dimethylsiloxane)-based elastomers crosslinked *via* elongated hematite fillers, the mechanical properties are characterized by an enormous strain at break of up to 1700% and a pronounced strain-hardening regime.<sup>16</sup> Due to their unique properties, they are excellent candidates for an in-depth analysis of the influence of network architecture on the strain-induced order in particle filled elastomers, and their properties will be compared to conventionally crosslinked elastomers throughout this paper. In addition, we investigate the influence of intrinsic particle preorientation in conventionally crosslinked elastomers by immobilization of a preoriented particle structure during the crosslinking process.<sup>13,21</sup> The strain- and field-induced geometric and magnetic order in the elastomers of different architecture and preorientation is investigated in detail using 2D small angle X-ray scattering experiments and Mössbauer spectroscopy, accomplished by angular-dependent magnetization experiments.

## Experimental section

### Chemicals

Ammonium hydroxide (25 m% in water), bis(2-ethylhexanoate) tin, hydroxyl terminated poly-dimethylsiloxane (PDMS-OH-S, 90 000–150 000 cSt,  $M_n = 34\,400\text{ g mol}^{-1}$ , PDI = 3.2; molar mass determined by GPC), tetraethoxysilane (TEOS,  $\geq 99.9\%$ ), and trimethylsiloxy terminated polydimethylsiloxane (PDMS-TMS, 5.0 cSt,  $M = 770\text{ g mol}^{-1}$ ; according to supplier) are purchased

from ABCR. Sodium dihydrogen phosphate monohydrate is obtained from Alfa Aesar in ACS reagent grade. Iron(III) chloride hexahydrate is purchased in pure quality from Applichem. Diethyl ether and acetone in technical grade is purchased from BCD Chemie. Absolute ethanol ( $\geq 99.8\%$ , HPLC grade), toluene ( $\geq 99.8\%$ , HPLC grade), iron(III) nitrate nonahydrate (laboratory reagent grade), and technical grade nitric acid (65 m% in water) are obtained from Fisher Chemicals. Citric acid monohydrate ( $\geq 99.5\%$ ) is obtained from Jungbunzlauer GmbH. Hydroxyl terminated poly-dimethylsiloxane (PDMS-OH-S, 750 cSt,  $M_n = 17\,450\text{ g mol}^{-1}$ , PDI = 1.6; molar mass determined by GPC) and tetramethylammonium hydroxide solution (TMAOH, 25 m% in water) are obtained from Sigma Aldrich. Deionized water is used in all the following experiments generated by a reverse osmosis system (RO2000Dss + ME + KS\_SPS\_BA, Stakpure GmbH, Niederahr, Germany) with a residual conductance of  $< 10\text{ }\mu\text{S}$ .

The following material constants and literature values are used: bulk density of hematite:  $\rho_{\text{Fe}_2\text{O}_3} = 5256\text{ kg m}^{-3}$ ,<sup>22</sup> density of amorphous silica:  $\rho_{\text{SiO}_2} = 2200\text{ kg m}^{-3}$ ,<sup>23</sup> density of poly(dimethylsiloxane):  $\rho_{\text{PDMS}} = 980\text{ kg m}^{-3}$  according to supplier, density of PDMS-TMS:  $\rho_{\text{PDMS-TMS}} = 913\text{ kg m}^{-3}$  according to supplier.

### Synthesis

**Silica coated spindle-type hematite nanoparticles.** Spindle-type hematite nanoparticles are prepared according to a procedure described by Ozaki *et al.*<sup>24</sup> For this purpose, 1.3 L of an aqueous solution of iron(III) chloride in water ( $c = 0.02\text{ mol L}^{-1}$ ) are heated to reflux in the presence of  $\text{NaH}_2\text{PO}_4$  ( $c = 400\text{ }\mu\text{mol L}^{-1}$ ) for 48 h. The obtained particle dispersion is purified by repeated centrifugation with deionized water as dispersion medium.

In a next step, the particles are electrostatically stabilized following the procedure proposed by Ewijk *et al.*<sup>25,26</sup> The particles dispersed in water ( $V = 45\text{ mL}$ ,  $c \approx 45\text{ mg mL}^{-1}$ ) are added to 25 mL of nitric acid ( $c = 2.0\text{ mol L}^{-1}$ ). After 5 min, 25.0 mL of an aqueous iron(III) nitrate solution ( $c = 0.35\text{ mol L}^{-1}$ ) are added, and the dispersion is heated to  $100\text{ }^\circ\text{C}$  for 1 h. After cooling the dispersion to ambient temperature, the particles are washed once with 25.0 mL nitric acid and afterwards three times with water by collection in a centrifuge. Subsequently, a solution of citric acid in water ( $c = 0.01\text{ mol L}^{-1}$ ) is added until the particles flocculate ( $V \sim 100\text{ mL}$ ). The particles are redispersed by raising the pH to 8 by addition of TMAOH. Excess ions are removed by washing with water three times.

In order to coat the nanoparticles with silica, a modified Stöber synthesis is employed.<sup>26,27</sup> The particles are therefore dispersed in a mixture of ethanol, water and ammonium hydroxide solution with a volume-based composition of 32:8:1 at a particle-concentration of  $1.17\text{ mg mL}^{-1}$ . The reaction is carried out at room temperature in an ultrasound bath at a frequency of 45 kHz.

Two different batches of silica coated hematite nanoparticles are prepared under analogous synthetic conditions ( $\text{Fe}_2\text{O}_3@\text{SiO}_2\text{-1}$  and  $\text{Fe}_2\text{O}_3@\text{SiO}_2\text{-2}$ ). For the both batches, in each case  $8.3\text{ }\mu\text{mol}$  TEOS per mg hematite particles are used.



The respective amount of TEOS is divided into three portions, with one portion added every 60 min. After the last addition, the reaction is allowed to proceed for 0.5 h under ultrasound and is then kept overnight at room temperature under magnetic stirring. The obtained particle dispersion is purified by repeated centrifugation with ethanol and then transferred to toluene by centrifugation.

**Particle-crosslinked elastomers (FE-1, FE-2, FE-3).** For the synthesis of particle-crosslinked elastomers, the silica coated hematite nanoparticles from batch  $\text{Fe}_2\text{O}_3@\text{SiO}_2\text{-1}$  dispersed in toluene are mixed with PDMS-OH-L ( $M_n = 34\,400\text{ g mol}^{-1}$ ) and the catalyst bis(2-ethylhexanoate)tin. By variation of the ratio of PDMS-OH-L to the particle dispersion the particle volume fraction,  $\Phi_v$ , of the final elastomers is varied. For all reactions, a catalyst concentration of 3 m% is chosen. After thorough mixing, the reaction mixture is transferred to a poly(tetrafluoroethylene) mold ( $20\text{ mm} \times 15\text{ mm} \times 2.5\text{ mm}$ ) and the dispersant toluene is removed at room temperature by application of a vacuum. Subsequently, the polymerization mixture is placed in a vacuum drying oven at 363 K for 33 d.

After the reaction time, the sample is removed from the polytetrafluoroethylene mold and swollen in a large excess of diethyl ether for at least 48 h, in order to remove the catalyst and any unreacted PDMS-OH-L. During this time the solvent is exchanged at least once. The sample is then deswollen in acetone, a non-solvent to polydimethylsiloxane, and dried overnight at 348 K.

**Conventionally crosslinked particle-filled elastomers (CE, ACE-1, ACE-2).** For the synthesis of conventionally crosslinked particle-filled elastomers, the prepared silica coated hematite nanoparticles from batch  $\text{Fe}_2\text{O}_3@\text{SiO}_2\text{-2}$  dispersed in toluene are mixed with PDMS-OH-S ( $M_n = 17\,450\text{ g mol}^{-1}$ ) in order to achieve a homogeneous distribution. Subsequently, the toluene is removed from the mixture at ambient temperature in vacuum. By variation of the ratio of PDMS-OH-S to the particle dispersion the particle mass fraction of the final elastomers is varied. To a poly(tetrafluoroethylene) mold ( $20\text{ mm} \times 15\text{ mm} \times 2.5\text{ mm}$ ), an amount of TEOS is added directly, corresponding to a molar ratio of TEOS to PDMS-OH-S of 0.125 ( $n_{\text{TEOS}} = 0.125n_{\text{PDMS-OH-S}}$ ). For all reactions a catalyst concentration of 3 m% is chosen. After addition of the catalyst, the reaction mixture is thoroughly mixed, bubbles are removed by application of reduced pressure, and the reaction is allowed to proceed for 1 hour at ambient conditions. Subsequently, the polymerization mixture is placed in a vacuum drying oven at 363 K for 7 d.

The samples with an anisotropic orientational distribution of the embedded filler particles (ACE-1 and ACE-2) are obtained by placing the reaction mixture in a homogeneous magnetic field with a flux density of  $200\text{ kA m}^{-1}$  generated by two rectangular permanent magnets. The reaction time is 7 d for sample ACE-1 and 8 d for sample ACE-2. After the reaction time, the sample is removed from the polytetrafluoroethylene mold and directly analyzed without further swelling or purification.

## Instrumentation

**Transmission electron microscopy (TEM).** Images are acquired with a Zeiss LEO 912 Omega (Carl Zeiss, Oberkochen, Germany). For this purpose, a diluted dispersion of the particles is drop casted onto a copper grid with a carbon-hole film (Quantifoil® Multi A, Quantifoil Micro Tools GmbH, Großlöbichau, Germany) and the solvent is afterwards evaporated at room temperature.

**Quasi-static vibrating sample magnetometry (VSM).** Magnetograms are conducted on a EV 7 vibrating sample magnetometer (MicroSense, Lowell, MA, USA) operated at room temperature with a magnetic field ranging from  $-1430\text{ kA m}^{-1}$  to  $1430\text{ kA m}^{-1}$ . The samples are sealed in cylindrical Teflon vessels and attached to a glass sample holder vibrating at a head drive frequency of 75 Hz. Angle-dependent measurements are conducted in the plane parallel to the field vector during synthesis and field during measurement. For  $\beta = 0^\circ$  both fields are parallel to each other. For a series of angular-dependent measurements, a rectangular sample specimen is cut from the bulk sample with one side of the sample parallel to the applied field during synthesis. The sample is placed in a Teflon vessel and the position of the field during synthesis is marked and manually aligned with the field direction during VSM measurements. Due to the manual alignment, the angle  $\beta$  may have a comparably large experimental error, estimated around  $\pm 5^\circ$ . However, all measurements in one series are recorded relative to the same initial configuration.

Throughout this work the particle content is given as a mass fraction. By VSM, the experimental mass fraction  $\Phi_m$  is directly accessible as the fraction of the spontaneous magnetization of the respective elastomer  $M_{s,\text{elast.}}$  over the spontaneous magnetization of the pure core-shell particles in powder state  $M_{s,\text{part.}}$

$$\Phi_m = \frac{M_{s,\text{elast.}}}{M_{s,\text{part.}}} \quad (1)$$

**Gel content  $G$  and equilibrium swelling degree  $\Gamma_V$ .** The network properties are determined gravimetrically. The gel content denotes the insoluble fraction of the reaction mixture after swelling in a good solvent and thorough drying of the residue,  $m_{\text{dry}}$ , and is corrected for the mass of the catalyst  $m_{\text{cat}}$  according to eqn (3).

$$G = \frac{m_{\text{dry}}}{m_{\text{syn}} - m_{\text{cat}}} \quad (2)$$

Here,  $m_{\text{syn}}$  denotes the mass of the elastomer after synthesis (before swelling). The volume based equilibrium swelling degree  $\Gamma_V$  is given by the ratio of the volume of the swelling medium taken up by the elastomer sample relative to its own volume without the magnetic nanoparticles, as those due not contribute to the swelling.<sup>18,20</sup>

$$\Gamma_V = \frac{V_{\text{pol}} + V_{\text{fl}}}{V_{\text{pol}}} \quad (3)$$



$$= 1 + \rho_{\text{pol}} \cdot \left( \frac{m_{\text{q}} - \mu_{\text{MNP}} \cdot m_{\text{d}}}{m_{\text{d}}(1 - \mu_{\text{MNP}}) \cdot \rho_{\text{fl}}} - \frac{1}{\rho_{\text{fl}}} \right) \quad (4)$$

Here,  $V_{\text{pol}}$  and  $V_{\text{fl}}$ , and  $\rho_{\text{pol}}$  and  $\rho_{\text{fl}}$  denote the volume and the bulk density of the polymer and the swelling medium, respectively.  $m_{\text{q}}$  is the mass of the swollen network,  $m_{\text{d}}$  the mass of the dry elastomer and  $m_{\text{MNP}}$  the mass of the embedded nanoparticles, as obtained from static magnetometry. For all swelling experiments PDMS-TMS is employed as swelling medium and the equilibrium swelling is determined after swelling in a great excess of PDMS-TMS for at least 7 days.

**Small angle X-ray scattering (SAXS).** 2D X-ray diffractograms are obtained employing a Double Ganesha AIR system (SAX-SLAB/Xenocs, Grenoble, France). The laboratory-based system is equipped with a D2-MetalJet X-ray source (Excillum, Kista, Sweden), which operates a liquid metal anode at 70 kV and 3.57 mA, providing a highly brilliant, small beam ( $<100 \mu\text{m}$ ) of Ga-K $\alpha$  radiation (wavelength  $\lambda = 0.13414 \text{ nm}$ ). An even smaller and intense beam at the sample position is obtained by slightly focusing with a focal length of 55 cm using a specially made X-ray optics (Xenocs, Grenoble, France). Two pairs of scatterless slits are used to adjust the beam size depending on the detector distance. A Pilatus 300 K detector (Dectris, Baden-Daettwil, Switzerland) is employed for data acquisition at two different detector positions (0.53 m and 1.93 m) to cover a scattering vector range of  $0.04 \text{ nm}^{-1}$  to  $5.0 \text{ nm}^{-1}$ , which is calibrated using the Bragg reflexes of a silver behenate sample. The measurement is performed in a custom built straining apparatus. The apparatus consists of two metal clamps and an electromotor, enabling the uniaxial elongation of the rubber sample to the desired sample length  $L$  with an accuracy of  $\pm 0.01 \text{ mm}$ . The actual tensile strain  $\varepsilon$  is calculated from the initial sample length  $L_0$  and final length  $L$  as  $\varepsilon = (L - L_0)/L_0$ . The immobilized and strained sample is placed directly into the beam. Due to the absence of an additional sample holder in the beam no further background correction is necessary. The initial sample dimensions are approximately  $20 \text{ mm} \times 2 \text{ mm} \times 0.9 \text{ mm}$ . The recorded scattering intensity is normalized to the intensity value at  $Q = 0.32 \text{ nm}^{-1}$  in order to ensure overlap of the  $I(Q)$  curves recorded at different detector distances. The scattering data is analyzed and fitted using the software program jscatter.<sup>28</sup> For the determination of the order parameter, the 2D scattering patterns are azimuthally averaged in two sectors with an opening angle of  $3^\circ$  within a defined  $Q$  regime, either  $0.07 \text{ nm}^{-1}$  to  $0.15 \text{ nm}^{-1}$  or  $0.4 \text{ nm}^{-1}$  to  $1.5 \text{ nm}^{-1}$ .

**Mössbauer spectroscopy.** The Mössbauer spectra are recorded in transmission geometry at ambient temperature. During the experiments, a magnetic field of up to 500 mT can optionally be applied perpendicular to gamma ray direction. For the zero field measurement, the coil current of the electromagnet is turned off, which results in a remanent magnetic field of  $<2 \text{ mT}$ . We use a  $^{57}\text{Co}$  source (Rh-matrix) in constant acceleration mode in the low velocity regime ( $<20 \text{ mm s}^{-1}$ ). For velocity calibration a  $20 \mu\text{m}$   $\alpha\text{-Fe}$  foil is used. To perform the measurements at various strains between 0% and 400%, a custom-built strain setup for the elastomers is utilized. A schematic of the setup can be seen in Fig. 12. The actual

tensile strain  $\varepsilon$  is calculated from the initial sample length  $L_0$  and final length  $L$  as  $\varepsilon = (L - L_0)/L_0$ . Both, the initial length as well as the final sample length, are manually determined with an accuracy of  $L = \pm 0.01 \text{ mm}$ . The initial sample dimensions are approximately  $20 \text{ mm} \times 15 \text{ mm} \times 0.9 \text{ mm}$ . Mössbauer data evaluation is done by the software pi [<https://www.uni-due.de/~hm236ap/hoersten/home.html>].

**Simulation.** Information of the intercorrelation between the orientation of the magnetic moments and the spatial distribution of the particles that finally lead to the observed signal intensity distribution in Mössbauer spectroscopy is obtained employing a Monte Carlo simulation protocol. Hereby, the line intensity ratio  $A_{23}$  is determined depending on the orientation of the particles'  $c$  axis to either the strain direction or the applied magnetic field, represented by the angles  $\alpha_s$  and  $\alpha_B$ , respectively. For the simulations, the programming language Python 3.7 is utilized together with the libraries scipy, numpy, random and pandas.  $10^6$  particles were randomly created for each simulation. For each particle the  $c$  axis is perpendicular to the spin and both directions are perpendicular to the magnetic moment of the particle. These geometric considerations are fixed and not altered during the simulation. The artificial order of the particles is introduced by elongation of the long particle axis vector distribution. The alignment of the magnetic moment along the applied magnetic field is considered by assuming a uniform spin distribution up to a value of  $25^\circ$  around the magnetic field direction within the basal plane. This small deviation is suggested by calculations in a Stoner-Wohlfarth model for the magnetic landscape in a sixfold symmetry with the corresponding fields and anisotropy constants.

## Results and discussion

The idea of this work is to investigate the interplay between the magnetic, and geometric degrees of order found in hybrid elastomers filled with elongated magnetic nanoparticles. For this purpose, we analyze the internal structure in well-defined hybrid elastomers of different architecture by means of a combination of methods under the influence of strain or magnetic fields. We compare the behavior of elastomers exclusively crosslinked *via* covalent polymer-particle linkage,<sup>16</sup> to that of conventionally crosslinked networks of similar composition with initially either isotropic or anisotropic distribution of the nanoparticles within the matrix. Comparing the materials with different architecture, we correlate the differences in material behavior and architecture to the strain-induced orientation behavior of the embedded filler particles.

As particulate fillers, spindle type hematite nanoparticles are employed, which show a magnetic as well as a tunable geometric anisotropy. In order to induce a functional particle surface and to compatibilize the particles with the PDMS matrix, in a first step the analyzed particles are coated with a silica shell. After incorporation in the elastomer matrix, the strain- and magnetic field-induced orientation behavior of these nanoparticles with anisotropic shape is analyzed.





### Particle characteristics

Spindle-type hematite nanoparticles bring along a number of peculiar properties that make them attractive as a model system. The synthesis and surface modification chemistry of these nanoparticles is well-studied and scalable, so that in one lab-scale step, highly stable particles in dispersion are accessible in a gram scale yield.<sup>17,24,29</sup> The shape of the nanoparticles can be varied between spherical and spindle-like in different aspect ratios by variation of the synthesis conditions.<sup>30</sup> Under proper conditions, the nanoparticles are reproducibly obtained with low polydispersity. The latter property greatly facilitates the analysis of the internal structure and order in their composites by scattering techniques.<sup>31,32</sup>

Further, spindle-type hematite nanoparticles have particulate magnetic properties that arise from their internal atomic structure. Hematite crystallizes in the trigonal-hexagonal scalenohedral class structure with the space group  $R\bar{3}c$ .<sup>33</sup> Hematite is an antiferromagnet with a Morin transition temperature at 263 K in bulk that decreases rapidly with the grain size for nanoparticles below 100 nm.<sup>34</sup> Below the Morin transition the spin moments are arranged parallel to the trigonal  $c$  axis. Above the Morin transition, the spins are located within the basal plane and are slightly canted, leading to a minor net magnetic moment perpendicular to as well the  $c$  axis and the spin preferred alignment, respectively.<sup>35</sup> For the silica coated, spindle-shaped hematite nanoparticles employed in this study, over the whole temperature range spanning from 4 K to ambient, a nuclear quadrupole level shift of approximately  $-0.2 \text{ mm s}^{-1}$  is experimentally observed,<sup>34</sup> proving a perpendicular orientation between the individual spins and the hematite polarization axis. This result confirms that the magnetic cores are really in the weakly ferromagnetic state that is usually found above the Morin transition. Consequently, as in the spindle-type nanoparticles the  $c$  axis is parallel to the long particle axis, the small net magnetic moment  $m$  of an individual particle is, contrary to most anisotropic magnetic nanoparticles, oriented perpendicular to the long particle axis  $l$ .<sup>36</sup>

This preferred orientation of the magnetic moment opens the possibility to orient the particles giving access to anisotropic materials and can additionally be used as a probe to detect order of the magnetic nanoparticles due to the coupling of the magnetic moment to the geometric anisotropy. The nanoparticles are reported to show three magnetic easy axes located within the basal plane and one magnetic hard axis given by the long particle axis parallel to the  $c$  axis.<sup>13</sup> The energy barrier for transition of the magnetic moment to another easy axis within the basal plane is low, thus almost superparamagnetic behavior is observed within the basal plane.<sup>13</sup>

The shape and geometric parameters of the nanoparticles with and without silica shell are determined using TEM as exemplarily shown in Fig. 1, and the results for the geometric scales of the parameters according to TEM are summarized in Table 2 in comparison to the results of other methods. Two batches have been prepared with analogous synthesis conditions, resulting in two particle batches with similar size and aspect ratio within the reproducibility expectations. For both batches, a particle ensemble of uniform size is observed with a clear

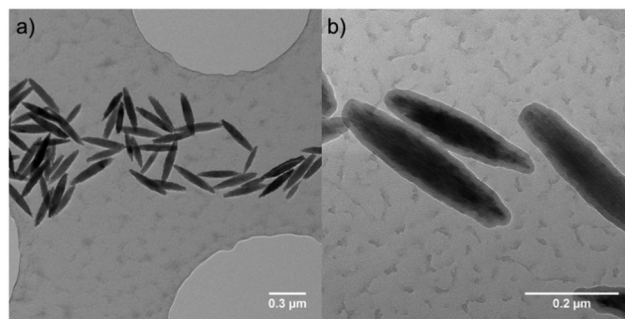


Fig. 1 Representative TEM image of spindle-type hematite nanoparticles from batch  $\text{Fe}_2\text{O}_3@\text{SiO}_2$ -1 (a) without silica shell and (b) with silica shell.

spindle-like shape of the core particle. The particles have a mean core length of 370 nm, a core width of 71 nm, and a silica shell thickness of 12 nm (see Table 2). The silica shell around the particle is homogeneous, and pores are not observed. Furthermore, the silica shell is of homogeneous thickness on the surface. The spindle-type shape of the core particle transforms consequently to a more ellipsoid-like shape.

The composite materials synthesized in this work either show a permanent or temporarily induced anisotropic orientation of the embedded spindle-type hematite nanoparticles, which is schematically illustrated in Fig. 2. Under isotropic conditions, thus without action of an external orienting field or strain, the dipolar particle interactions due to the low magnetic moment of the particles are neglectable, and accordingly on a global scale, the orientation of the particles with respect to the axis of investigation

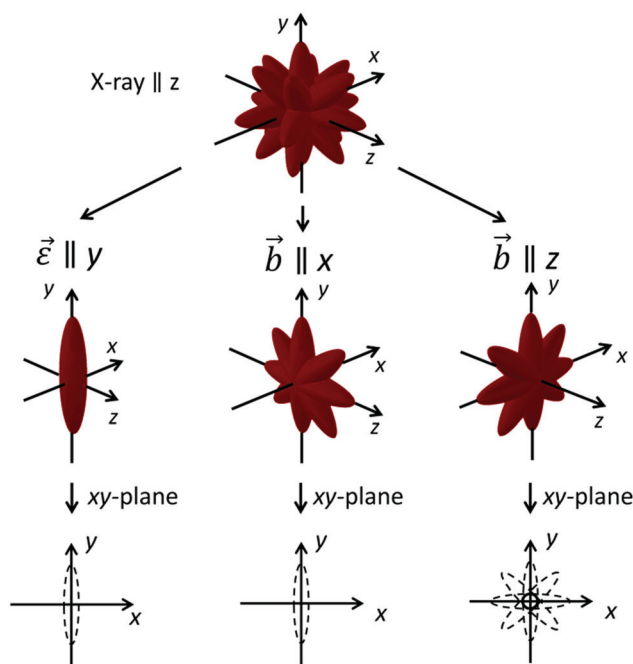


Fig. 2 Schematic representation of the orientational distribution of spindle-type hematite nanoparticles in the composite materials investigation in this work, in response to either strain  $\epsilon$  or a homogeneous magnetic field  $b$ , applied during the synthesis. Additionally, the electron density as effectively illuminated by a X-ray beam from the  $z$ -direction is shown.



is isotropic in all directions. Upon application of a homogeneous magnetic field along the  $x$  direction, the magnetic moment within the basal plane of the particles preferably orients along the field, with arbitrary angles of the long particle axis perpendicular to the field direction, thus in the  $yz$  plane. This leads to a preferred uniplanar orientation of the particle geometry. On the other hand, straining of the matrix surrounding elongated particles is expected to induce a preferential uniaxial orientation of the particle long axis parallel to the applied strain,<sup>15</sup> as response to a torque produced by the surrounding matrix. For conventionally crosslinked elastomer networks with a mesh size smaller than the particle size, the torque is obvious, as the mesh will be deformed in direction of the applied strain. For the novel particle-crosslinked elastomers, this will only lead to very small torques on the particle, as the mesh size is essentially the particle distance and the particles are connected by very long polymer chains.<sup>16</sup> Thus, we interpret the torque on the particles as additionally originating from a friction component of the disentangling polymer chains on the particle surface, in analogy to the orientation of elongated particles dispersed in a viscous matrix in shearing experiments.

### Synthesis and properties of particle-filled elastomers with different architectures

Samples with three different architectures are prepared, and the influence of sample architecture on the strain-induced ordering of dispersed spindle-type hematite nanoparticles is analyzed by a combination of methods.

Particle-crosslinked elastomers,<sup>16</sup> contrary to other elastomer networks, contain no specific crosslinker except for the multifunctional, inorganic nanoparticles, which leads to networks having highly functional nodes based on inorganic nanoparticles connected by long polymer chains. The resulting material properties of these particle-crosslinked elastomers are strongly dependent on the particle content. The samples are denoted as FE ("ferroelastomer") throughout this work.

The particle-crosslinked elastomers are obtained by reacting hydroxy-terminated poly(siloxanes) in bulk in the presence of catalyst and silica-coated hematite particles. As shown in our previous work,<sup>16</sup> using a reaction temperature of 90 °C and an efficient removal of the forming water in vacuum, stable elastomers are obtained, without additional crosslinker, except for the nanoparticles. By condensation of hydroxy end groups of the polymer chains with the particle surface, the nanoparticles serve as multifunctional inorganic crosslinkers for the network, and a unique architecture results.

These structures are compared to conventional networks based on crosslinked polymer chains. Here, the tetrafunctional crosslinker TEOS is employed at low molar fraction and in the presence of bifunctional PDMS-OH-S, the filler particles and catalyst. TEOS and PDMS-OH-S readily react at ambient temperatures to form a prepolymer, which is then completely cured at 90 °C in vacuum.<sup>37,38</sup> Due to the employed stoichiometry ( $n_{\text{TEOS}} = 0.125n_{\text{PDMS-OH}}$ ) and the functionality of PDMS-OH-S ( $f = 2$ ) and TEOS ( $f = 4$ ), we expect the formation of a prepolymer. After formation of the prepolymer, 75% of the employed

PDMS-OH hydroxyl functionalities have not reacted and in the following reaction steps at 90 °C the network is cured completely under reaction of hydroxyl functionalities of the PDMS-OH-S reactant with itself and additionally covalent attachment to the surface of the embedded filler particles. The obtained conventionally crosslinked elastomers are denoted CE ("conventionally crosslinked elastomer").

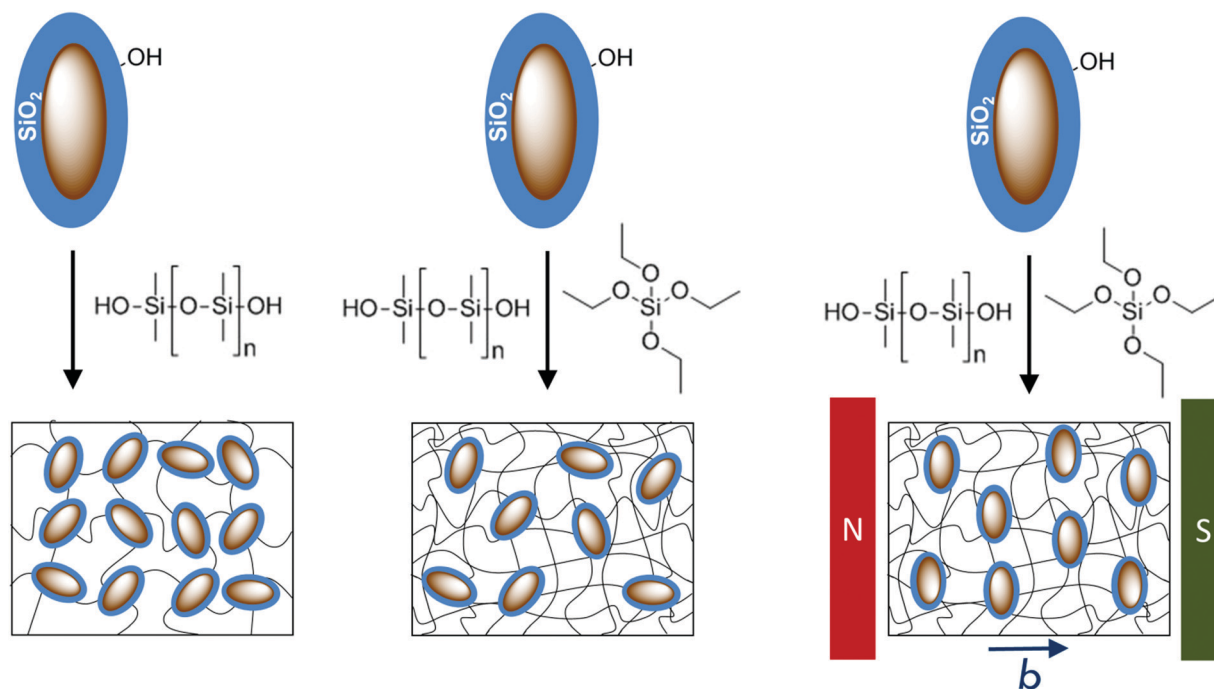
In addition, a particle-related anisotropy structure can be manifested in the materials already during the synthesis by the application of an external homogeneous magnetic field during the crosslinking process. The magnetic moment of spindle-type hematite nanoparticles allows their magnetic orientation, and opens a pathway to inscribe a preordered structure to the sample, if the magnetically induced order is conserved by dense crosslinking around the oriented particles. The magnetic moment is coupled to the basal plane leading to an orientation with the basal plane oriented parallel to the applied field, while the long particle axis is statistically distributed in the plane perpendicular to the applied field direction (see Fig. 2). Samples with this architecture, based on conventionally crosslinked elastomers with an anisotropic orientational distribution of the embedded filler particles are denoted ACE (anisotropic conventionally crosslinked elastomer) in the following, and the direction of the magnetic field during synthesis is referred to as axis  $b$ .

A reaction scheme for all architectures is found in Fig. 3 and relevant parameters of the prepared elastomers are compiled in Table 1. For all samples, high gel contents above 75 m% are found. The gel content is the mass fraction of initial monomers and particles that is irreversibly immobilized in the final network after synthesis. A high gel content is important to ensure a good homogeneity of the sample. For the particle-crosslinked elastomers, the part of the sample that has not been attached to the network yet is removed. This is achieved by swelling the sample in a large amount of diethyl ether and careful deswelling in acetone. For analysis of the final compositions, see Table 1.

For the chemically crosslinked elastomer samples, the gel content is so high that this procedure is not necessary. Additionally, for the sample ACE upon swelling a reorientation of the embedded filler particles is conceivable, which should be prevented for proper analysis.

For the particle-crosslinked elastomers, the volume-based equilibrium swelling degree decreases with increasing particle content attributed to denser crosslinked network structure upon increasing the content of crosslinking particles.<sup>18,20</sup> For the conventionally crosslinked samples, lower values for the swelling degree are observed, due to the higher crosslinking density resulting from addition of the crosslinker TEOS. The equilibrium swelling degree of the sample ACE-1 and ACE-2 is equal within error margin. For sample CE a lower value is observed, which is still in a similar size range considering the error margins. The higher swelling degrees for the samples ACE-1 and ACE-2 furthermore correlate to their lower gel contents. The deviations may be attributed to a fluctuation of the crosslinking density due to either a locally or globally different crosslinker concentration or network defects, such





**Fig. 3** Schematic representation of the network architecture of the hybrid elastomers analyzed in this work. Left: Particle-crosslinked elastomer (FE); mid: conventionally crosslinked particle-filled elastomer (CE); right: conventionally crosslinked particle-filled elastomer with anisotropic orientational distribution of the embedded particles (ACE).

**Table 1** Relevant parameters of the prepared hybrid elastomers. The equilibrium swelling degree is determined by swelling in PDMS–TMS

Sample	FE-1	FE-2	FE-3	CE	ACE-1	ACE-2
Particle mass fraction $\phi_m$ [m%]	16.7	27.5	32.3	9.6	10.9	11.8
Gel content $G$ [m%]	$78.5 \pm 1.0$	$75.9 \pm 1.0$	$80.0 \pm 1.0$	$98.2 \pm 2.3$	$94.0 \pm 3.2$	$86.3 \pm 3.2$
Equilibrium swelling degree $\Gamma_v$	$23.7 \pm 1.4$	$14.0 \pm 1.9$	$11.0 \pm 1.1$	$3.8 \pm 0.4$	$5.2 \pm 0.8$	$6.1 \pm 0.7$

as dangling ends. As the crosslinker concentration is low, even small deviations may have a large impact on the crosslinking density.

For this study, we in-depth analyze the internal structure for the different architectures based on 2D small angle X-ray scattering, Mössbauer spectroscopy, magnetization measurements, and Monte Carlo simulations.

### Small angle X-ray scattering analysis of strain- and field-induced order phenomena

Small angle X-ray scattering (SAXS) is a powerful tool to investigate the internal structure of complex matter on the nanoscale, including the size, shape, and structure of nanoparticles in various media.<sup>39</sup> In the case of anisotropic nanoparticles, a suitable experimental setup with two-dimensional detection gives access to the angular distribution of particle orientation. In case of elongated (prolate) particles with a preferential orientational axis within a polymer composite, an azimuthally anisotropic distribution of the scattered intensity is expected and can be analyzed for its information on the order parameter using well-established approaches.<sup>31,32</sup>

In this work, the X-ray scattering contrast between elongated core-shell nanoparticles and their PDMS matrix is exploited to extract information on the strain- and field-induced particle orientation in filled elastomers of different architecture (FE, CE, and ACE, see above). After discussing the small angle X-ray diffractograms of the samples without external field or deformation, we demonstrate how the application of external strain or magnetic fields influences the internal orientational order of the nanoparticles in the elastomeric matrix.

The analyzed  $Q$  regime is  $0.07 \text{ nm}^{-1}$  to  $3.0 \text{ nm}^{-1}$ , and thus the accessible real space according to Braggs law is approximately between  $90 \text{ nm}$  and  $2 \text{ nm}$ .<sup>40</sup> Hence, structural and orientational information from scattering experiments in the accessible  $Q$  regime is mainly expected from the particle shell (thickness  $\sim 12 \text{ nm}$  according to TEM, see Table 2) and from the short particle axis ( $\sim 71 \text{ nm}$ ), while the long axis ( $\sim 370 \text{ nm}$ ) is too long for a significant contribution. An exemplary set of 2D scattering patterns as obtained in this work are shown in Fig. 4.

**SAXS analysis of the reference samples.** As a starting point for the strain-induced structure analysis, we have a close look into the 2D scattering patterns of the unstrained samples FE-1, CE, and ACE-1.





For the reference samples that are prepared without external field, (FE-1 and CE), the scattering patterns are isotropic for the unstrained case (see Fig. 4a and d), as we would expect for essentially isotropic samples. The scattering response of sample ACE-1, prepared under field influence, is discussed further below.

A detailed analysis of the scattering intensity over the observable  $Q$  regime is performed based on a proper model that takes into account the contributions of the different characteristic length scales present in the filler particles, and the polymer matrix. A proper description of the experimental data is obtained using a linear combination of the form factor of a polydisperse ellipsoid with a constant shell thickness with a structure factor based on the Ornstein-Zernicke correlation function, accounting for the polymer scattering. The Ornstein-Zernicke scattering function is defined as:<sup>41</sup>

$$F(Q) = \frac{F_0}{1 + Q^2 \xi^2}, \quad (5)$$

where  $\xi$  is correlation length describing the density fluctuation in the polymer network and  $F_0$  is the scattering amplitude. Both are treated as free parameters in our fits. The polymer scattering contribution is similar irrespective of the sample architecture. The polymer scattering is a result density fluctuations around local inhomogeneities in the sample. In both sample materials the inhomogeneities mainly originate from entanglements of the polymer chains between the crosslinks, as the length of the polymer chains are significantly larger than the entanglement molar mass for PDMS, which is around 21 kg mol<sup>-1</sup> to 33 kg mol<sup>-1</sup>.<sup>42</sup> In the case of conventionally crosslinked elastomers, the polymer segment length is around 4 times the molar mass of the PDMS-OH reactant ( $4 \times 17.5$  kg mol<sup>-1</sup> = 70 kg mol<sup>-1</sup>) due to the reaction conditions. In the case of particle-crosslinked elastomers it is reported to be around 275 kg mol<sup>-1</sup> for the analyzed particle content.

The form factor of the ellipsoid  $P_{\text{MSE}}$  with a shell of constant thickness is described as follows, where  $F_a$  denotes the form factor amplitude.<sup>28,43,44</sup>

$$P_{\text{MSE}} = |F_a \cdot F_a^*| = |F_a^2| \quad (6)$$

$$F_a(Q) = \int_0^1 V_c \rho_c f_c + \rho_{\text{sil}} \cdot (V_f - V_c f_c) dx \quad (7)$$

$$f = \frac{3(\sin(u) - z \cos(u))}{u^3} \quad (8)$$

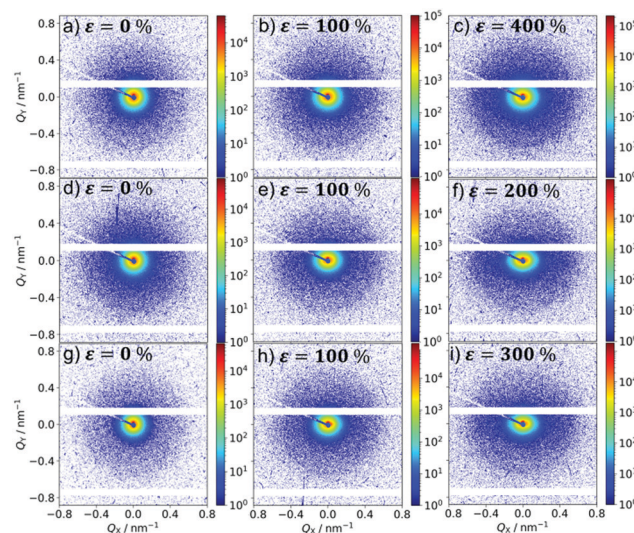


Fig. 4 Representative 2D scattering patterns at detector distance  $d = 1.93$  m for sample FE (a–c), CE (d–f) and ACE (g–i) at different strains. The respective strain is indicated in the upper left of each scattering pattern, and amounts to  $\varepsilon = 0\%$  for the images on the left,  $\varepsilon = 100\%$  for the images in the middle, and the maximum applied strain for the images on the right. The strain is parallel to  $Q_y$ . For sample ACE, the X-ray direction corresponds to the magnetic field direction during synthesis.

$$u = Q \cdot R_c \left( 1 + x^2 \left( \frac{R_p^2}{R_c^2} - 1 \right) \right)^{\frac{1}{2}} \quad (9)$$

$$V = \frac{4}{3} \pi R_c^2 R_p \quad (10)$$

In these equations the index  $c$  characterizes the hematite core,  $sil$  denotes the silica shell, and no index is used for the whole particle, as obtained as the sum of both respective radii. The volume of the particles is calculated according to eqn (10), where  $R_c$  denotes the equatorial radius and  $R_p$  is the radius at the poles. The X-ray scattering length densities are denoted as  $\rho$  and are calculated using the calculator supplied by NIST from the elemental composition, the bulk density, and the energy of the employed radiation (Ga-K $\alpha$ ). The employed scattering length densities are corrected for the scattering of the polymer by subtraction of the scattering length density of PDMS. Polydispersity is introduced to the system by considering a distribution of the equatorial and polar radius, as well as the silica shell. As the polar radius is not visible in the analyzed  $Q$  regime, it is set to an arbitrary value of 220 nm and a

**Table 2** Comparison of the geometrical parameters for silica-functionalized spindle-type hematite nanoparticles obtained from  $I(Q)$  analysis of SAXS measurements in the corresponding hybrid elastomers to the particle size as determined by TEM

Batch/parameter	Fe <sub>2</sub> O <sub>3</sub> @SiO <sub>2</sub> -1		Fe <sub>2</sub> O <sub>3</sub> @SiO <sub>2</sub> -2		
	TEM	SAXS FE	TEM	SAXS CE	SAXS ACE
Particle core length [nm]	377 ± 42	—	363 ± 39	—	—
Particle core width [nm]	70.6 ± 8.7	54 ± 22	72.0 ± 8.4	55 ± 22	54 ± 22
Shell thickness [nm]	12.3 ± 1.3	11.7 ± 0.3	11.7 ± 1.4	12.2 ± 0.3	12.6 ± 0.3





polydispersity of 40 nm is employed to prevent contributions from this semiaxis in the fit. The distribution of the particle core is modeled by a lognormal function, in agreement with the growth mechanism, and the distribution of the silica shell is considered as a Gaussian distribution.

The final model for description of the scattering of our samples is obtained by linear coupling of the discussed equations and considering a constant background as a free parameter. All form factors and functions employed for the fit are taken from the program jscatter.<sup>28</sup> The individual contributions of the respective form and structure factors to the overall fit can be seen as the solid red and green line in Fig. 5. As the system consists of spindle-type hematite particles with a rather ellipsoidal silica shell in a continuous polydimethylsiloxane matrix, this combination describes our system very well. Deviations of the fit from the experimental data at high  $Q$  values might originate from a small background resulting from diffuse background scattering, as no proper background subtraction is possible due to the unique network architecture of the particle-crosslinked elastomers and thus no background subtraction is performed. The satisfying agreement of the fits of the sample system with the experimental data is a good indication that the observed anisotropy really originates from a preferred orientation of the embedded silica coated hematite particles.

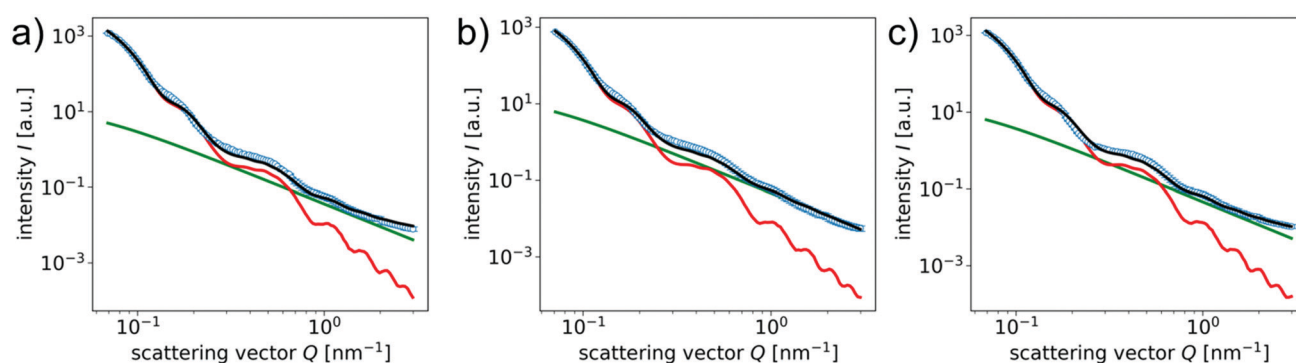
In Table 2 the important fit parameters for the size of the particles and their polydispersity are summarized. The silica shell thickness is in excellent agreement with the experimental value determined by TEM analysis and can be described with low values for the polydispersity. For the particle core, deviations are expected as the radius of curvature for an ellipsoid differs significantly from the respective one of a spindle.<sup>30</sup> In our model this is found as a high value for the polydispersity of the particle core, which is necessary to describe the first feature of the curve of the experimental data at low values for  $Q$ . Another reason for the high polydispersity is the surface roughness of the particles as observed in the TEM images in Fig. 1.<sup>31</sup> The value for the particle core width itself is considering the error margins in good agreement with the value determined by TEM, although it is lower, which might be due to the larger ensemble of particles probed.

In case of the anisotropic reference sample ACE-1 that is prepared in the presence of a homogeneous magnetic field, we expect a preferred orientation of one of the nanoparticles magnetic easy axes in the basal plane parallel to the field direction, and a resulting preferred orientation of the long particle axis in the plane perpendicular to the original field axis  $b$  during synthesis,<sup>30</sup> as schematically shown in Fig. 2. For the SAXS investigation we therefore have to distinguish two geometric configurations.

If the sample is probed by SAXS in a configuration, where the beam is parallel to the original field direction  $b$ , this results in an isotropic scattering pattern in SAXS measurements according to the isotropic, disk-like shape of the electron density, as schematically indicated in Fig. 2. The obtained isotropic scattering pattern is shown in Fig. 4g. It is readily analyzed following the model described above, and the corresponding parameters for the particle geometries are shown in Table 2 with good correspondence to the TEM results. For the investigation of the strain-induced order in ACE-1, this axis of investigation (beam direction  $z$  parallel to  $b$ ) is chosen in order to guarantee best comparability to the corresponding experiments involving the non-preoriented samples FE-1 and CE.

More interesting however, concerning the intrinsic anisotropy in the sample ACE-1 that is conserved during the synthesis is the analysis of the sample structure of ACE-1 perpendicular to the original field axis  $b$ . This is achieved, by probing the sample with the beam axis  $z$  perpendicular to  $b$ , with  $b$  placed along the  $x$  axis of the experimental setup. The resulting 2D scattering pattern is shown in Fig. 6a. The pattern, in contrast to the respective analysis along the  $b$  axis, shows an anisotropic scattering intensity, with enhanced scattering intensity parallel to  $Q_x$  on cost of intensity parallel to  $Q_y$ . This can be displayed in more detail by plotting the scattering intensity in a certain  $Q$  range in dependence on the azimuthal angle (Fig. 6b).

It can readily be anticipated that the observed anisotropy is a result of the preordering of the nanoparticles during the synthesis caused by the magnetic field, and its manifestation in the crosslinking process. In the configuration discussed here, the scattering pattern indicates that the particle short



**Fig. 5** Radially averaged scattering intensity vs. scattering vector  $Q$  for (a) sample FE-1, (b) sample CE, and (c) sample ACE-1 at zero applied different strain. The black lines are a best fit obtained by linear combination of a polydisperse core-shell ellipsoid form factor and a structure factor according to the Ornstein-Zernicke correlation function. The red lines represent the contribution of the polydisperse core-shell ellipsoid form factor and the green lines show the contribution of the Ornstein-Zernicke structure factor accounting for the polymer scattering.



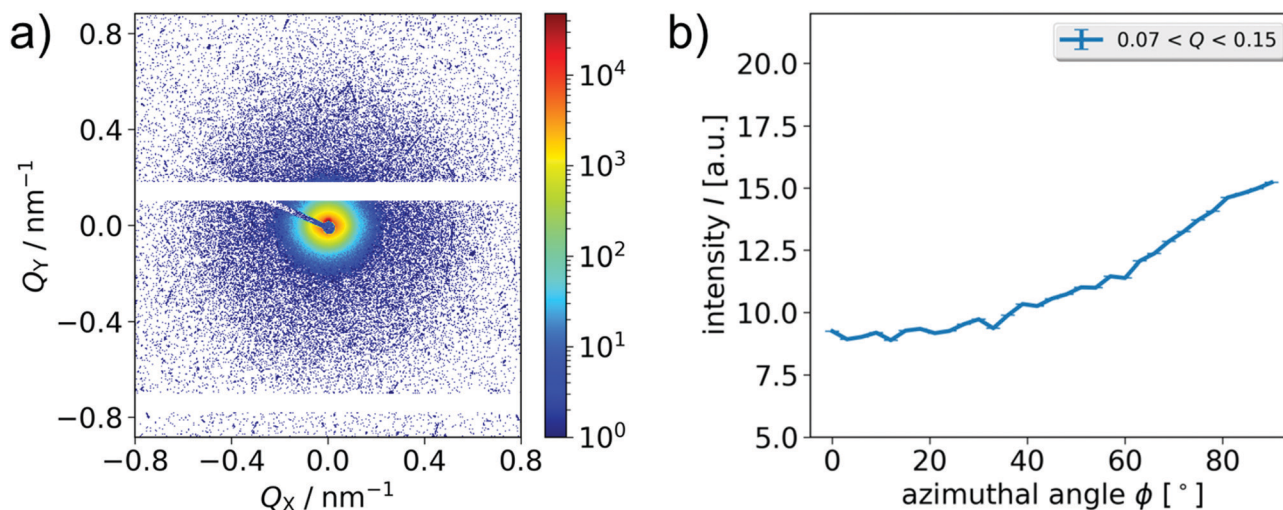


Fig. 6 (a) 2D scattering pattern and (b) azimuthal scattering intensity averaged in the low  $Q$  regime ( $0.07 \text{ nm}^{-1} < Q < 0.15 \text{ nm}^{-1}$ ) depending on the azimuthal angle in the interval  $[0^\circ, 90^\circ]$  for the unstrained sample ACE-1. The magnetic field during synthesis is parallel to the  $Q_x$  axis, and thus the X-ray beam is perpendicular to the intrinsic magnetic anisotropy axis of the sample.

axis show a preferred orientation in  $x$  direction. This is in full correspondence with the expectation, as the particles are preferably magnetized in the basal plane, see also Fig. 2 for an overview about the relevant orientations of X-ray beam, magnetic field, and particle orientation probed in this work.

From the azimuthal intensity distribution, we calculate the order parameter of the particle short axes with respect to the  $x$  axis of the setup following the procedure described further below in the context of SAXS analysis of strained samples (eqn (11)). The 2D scattering analysis of the intrinsic anisotropy of the ACE-1 sample in this specific geometry reflects the degree of order corresponding to a 2D projection of the ensemble and is actually of planar nature. For practical reasons, we prefer to define the order parameters in this study with respect to the long particle axis, and due to the perpendicularity, the result is equal to the order parameter of the long particle axis  $l$  with respect to the  $y$  axis and thus is assigned as  $S_y$ . The order parameter of this projection is obtained as  $S_y = 0.26 \pm 0.01$  in the low  $Q$  regime ( $0.07 \text{ nm}^{-1} < Q < 0.15 \text{ nm}^{-1}$ ) and  $S_y = 0.29 \pm 0.02$  obtained in the high  $Q$  regime ( $0.4 \text{ nm}^{-1} < Q < 1.5 \text{ nm}^{-1}$ ). For a completely ordered sample (here: perfect alignment of the long axis perpendicular to the axis  $b$ ),  $S_y$  is expected to be 1, while a value of 0 indicates no preferential orientation. The experimental result thus represents significant, but incomplete ordering of the particle axis in the expected plane.

The data can be used to estimate also the order parameter of the long axis  $l$  with respect to the original field axis  $b$  (assigned as  $S_b$ ), in order to better describe the actual, equatorial preference of the configuration, and to compare it to the results of Mössbauer spectroscopy (see below). Under this definition, a result of  $-0.5$  indicates full orientation of the long particle axes  $l$  in a plane perpendicular to  $b$ . This order can be quantified by a phase shift of the azimuthal scattering intensity by  $90^\circ$ , thereby the order parameter of the long particle axis  $l$  is determined with respect to  $b$ . Experimentally, we obtain

$S_b = -0.25 \pm 0.01$  in the low  $Q$  regime and  $S_b = -0.28 \pm 0.03$  in the high  $Q$  regime, respectively, confirming that the permanent geometric anisotropy as analyzed by SAXS in sample ACE-1 is significant, but not complete.

Additional information on the degree of magnetic order conserved by the crosslinking process in the magnetic field for ACE samples is accessible by magnetization experiments. The magnetic properties of isotropic conventionally and particle-crosslinked elastomers have been reported in our previous work,<sup>16</sup> and are thus not presented here again. Generally for the particle-filled elastomers, an open hysteresis loop and magnetic characteristics comparable to the nanoparticles in powder state are observed. As sample ACE-1 has an anisotropic distribution of the embedded magnetic nanoparticles, an angular-dependence of the magnetic properties are expected. In order to analyze this, angular-dependent magnetization curves are collected for sample ACE-1 at ambient temperature in  $15^\circ$  steps (Fig. 7 and 8). The reference axis ( $\beta = 0$ ) thereby is the anisotropy axis of the sample,  $b$ . Two series of experiments are performed with different field amplitude of  $0.8 \text{ kA m}^{-1}$  and  $24 \text{ kA m}^{-1}$ , respectively. The magnetization curves measured with the lower field amplitude do not show a hysteresis (Fig. 7a), yet a systematic shift of the curve along the  $M$  axis depending on the angle is observed. With increasing angle  $\beta$ , the curve intersects the  $M$  axis at a higher magnetization value. While the intersection for the curve obtained at  $90^\circ$  crossed nearly the origin, the curves at  $0^\circ$  and  $180^\circ$  intersect the axis at values of  $\pm 0.0015 \text{ A m}^2 \text{ kg}^{-1}$ . In contrast, for the higher maximum field amplitude of  $24 \text{ kA m}^{-1}$ , an open hysteresis loop is observed. Again, the curves are systematically shifted along the  $M$  axis depending on the field angle. In Fig. 8, the remanence and coercivity of both measurements are shown in dependence on the field angle. The measurements at lower maximum field strength show a decrease of the remanence from positive values at  $\beta = 0^\circ$  over zero at  $90^\circ$  to a negative maximum



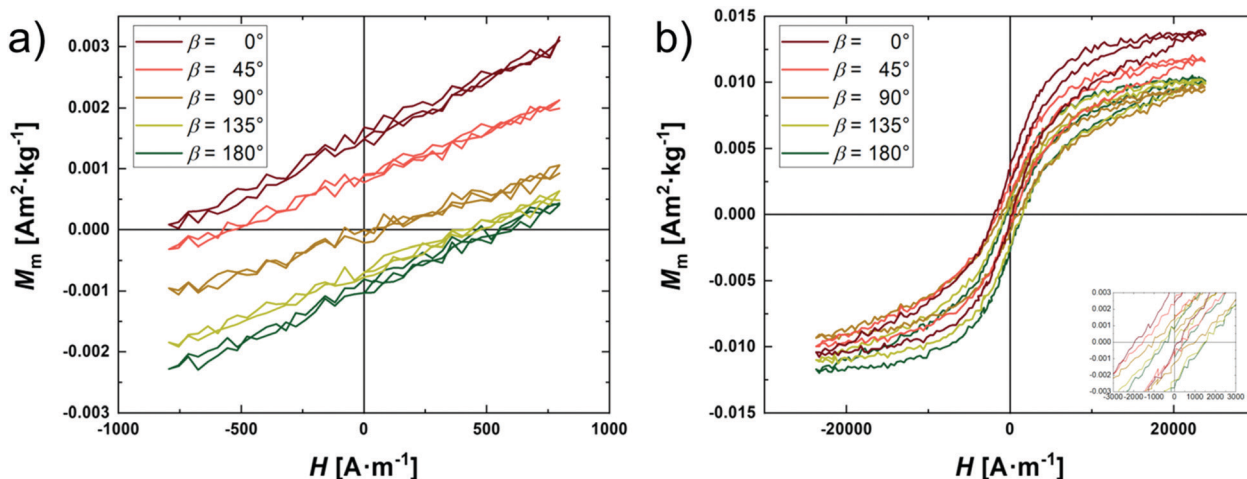


Fig. 7 Angular-dependent magnetization curves for sample ACE-1 with different maximum magnetic field strength (a)  $0.8 \text{ kA m}^{-1}$ ; (b)  $24 \text{ kA m}^{-1}$ . The angle represents the angle between the field axis during synthesis, and the field direction during the respective magnetization measurement.

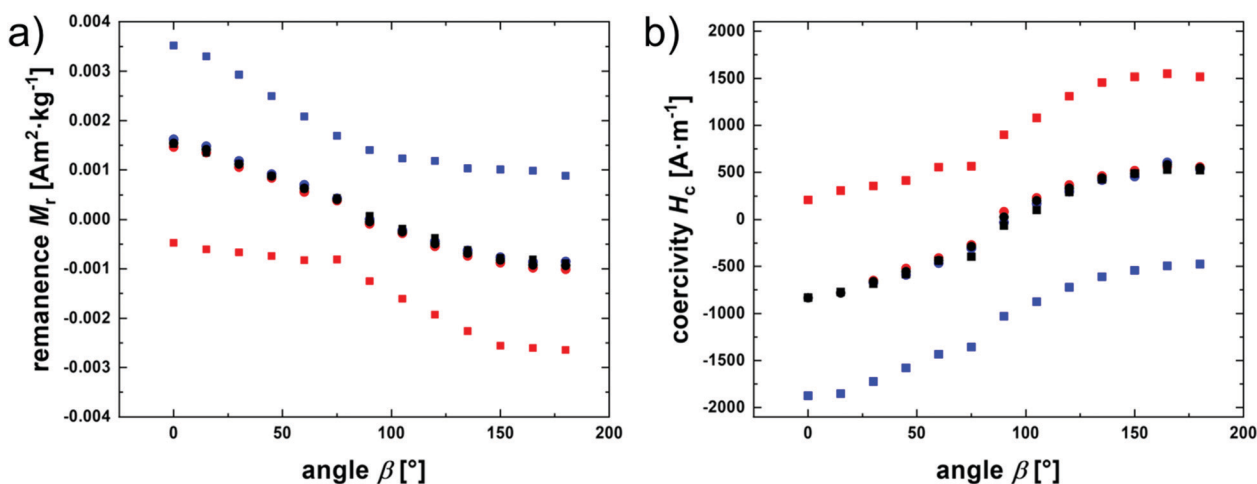


Fig. 8 (a) Remanence magnetization  $M_r$  and (b) coercivity  $H_c$  of sample ACE-1 depending on the angle between field direction during synthesis and field direction during magnetization measurement shown for measurements with a maximum field strength of  $0.8 \text{ kA m}^{-1}$  (circles) and  $24 \text{ kA m}^{-1}$  (squares). Blue: results from the increasing field strength branch; red: from the decreasing branch; black corresponding mean value.

at  $180^\circ$ . The coercivity in Fig. 8a shows the opposite trend, starting from a minimum at  $0^\circ$  going to the maximal, negative value at  $\beta = 180^\circ$ , while also crossing zero at  $90^\circ$ .

The courses are qualitatively understood on the base of the Stoner–Wohlfarth model by considering a respective particle ensemble that is probed with a maximum field amplitude either below or above the coercivity caused by the particles.<sup>45,46</sup> In the case that the maximum field strength is well below the critical strength for an internal (Néel type) remagnetization of the particles, the magnetic moment of the particles will return to its initial easy axis, and thus, full reversibility is achieved, and no hysteresis is observed. In the direction of the original magnetization, even in the field-free case, a net magnetization of about  $0.0015 \text{ A m}^2 \text{ kg}^{-1}$  is detected, representing the preferential orientation of the local magnetic moments with the field axis. The intersection of the magnetization curves with the  $M$  axis then decreases with increasing field angle,

until at  $90^\circ$  an intersection at about  $M = 0$  is observed, in correspondence with the model. By further increasing the angle, the magnitude of the remanence increases again with opposite sign. An analogous argumentation is valid for the angular coercivity trend.

For the measurements at higher field amplitude, an internal magnetization reversal of the particles becomes possible, and accordingly, the results for  $M_r$  and  $H_c$  depend on the history of the material. Consequently, the corresponding magnetization curves are hysteretic, and different values for the increasing and decreasing field branches are found. Information on the respective, angular-dependent curve shift can be obtained by calculating the average between the two values, and the corresponding values match those for the small field amplitude series, as seen in Fig. 8a, showing that the conserved magnetic anisotropy leads to magnetic switching at higher fields, but under conservation of the preferred axis.



The model this qualitatively explains the dependence of the outcomes on the maximum applied field strength, attributed to the critical field strength for an internal reorientation of the magnetic moment inside the particles at high fields. A more quantitative interpretation of the magnetization curve with this model, however, is beyond the scope of this work, realizing that in contrast to a simple Stoner–Wohlfarth particle that typically is assigned to have one, strongly preferred, easy magnetization axis, the hematite nanoparticles are shown to have a more complex magnetic signature. In place of one easy axis, the nanoparticles are discussed to show three easy magnetization axes organized in the basal plane of the spindle.<sup>13</sup> By magnetic saturation at high fields, a reorientation of the magnetic moment toward the opposite or into one other axis is thus still possible.

**SAXS analysis of strain-induced order.** Based on the model introduced above and our insight into the qualitative evolution of anisotropy in particle-filled elastomers and its manifestation in 2D SAXS diffraction patterns, the next step is the in-depth investigation of elastomer samples under strain and subsequent comparison of the behavior of the different architectures.

Therefore, stripes of the samples FE-1, CE, and ACE-1 are placed in a house-built straining apparatus, and 2D SAXS scattering pattern are recorded for various degrees of strain for the different samples. The strain is varied between 0% and 400%. In all experiments, the X-ray beam is along the  $z$  axis, and the strain is applied perpendicular to the beam along the  $Q_y$  axis, as visualized in Fig. 2.

For all samples, upon increasing the strain, an anisotropic, non-spherical 2D scattering pattern is obtained. The shape of the scattering pattern is elongated along the  $x$  axis, if a strain is applied. The patterns become increasingly anisotropic with increasing applied strain  $\varepsilon$ .

As only the orientation of the short axis and the preferred silica shell orientation is relevant in the accessible  $Q$  range, the shape of the scattering pattern indicates a preferential orientation of the two vectors parallel to the  $Q_x$  axis, resulting in an enhancement of the scattered intensity parallel to  $Q_x$  on cost of intensity parallel to  $Q_y$ . Due to the perpendicularity, a preferred orientation of the short axis and silica shell vectors in  $Q_x$  indicate a preferred orientation of the long axis in  $Q_y$  (along the strain  $\varepsilon$ ).

The behavior is qualitative similar for all three investigated samples. This effect is explained by an increasingly preferred orientation of the elongated nanoparticles in the strain direction due to a matrix-induced reorganization of the fillers. Once strain is applied, the polymer coils inside the elastomer matrix elongate in direction of the applied strain. The nanoparticles are on the one hand covalently attached to the polymers and on the other hand are influenced by the elongating polymer coils due to viscous friction on the particle surface, and both effects lead to an orientation of the particles with their long axis parallel to the applied strain (Fig. 2, left).

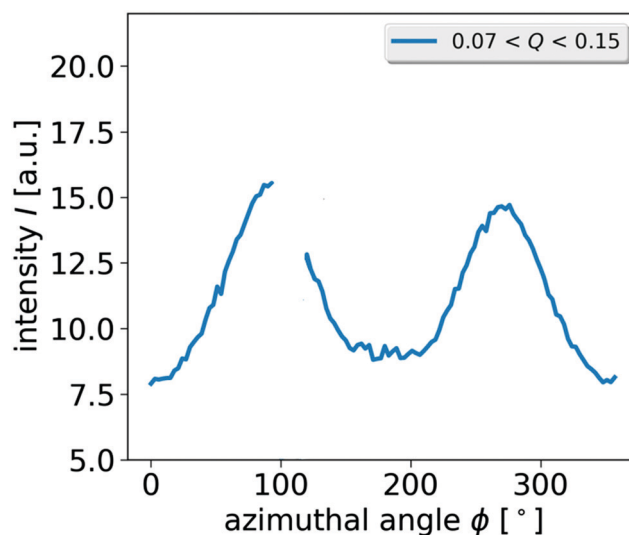
For a more quantitative analysis of the strain-induced order, we plot the azimuthal distribution of the intensity by averaging it in sectors with a width of  $3^\circ$  in two different  $Q$  regimes. In the regime  $0.07 \text{ nm}^{-1} < Q < 0.15 \text{ nm}^{-1}$ , which corresponds to

dimensions in real space of 42 nm to 90 nm, and thus mainly contributions from the short axis of the particle core are expected. Additionally, the regime  $0.4 \text{ nm}^{-1} < Q < 1.5 \text{ nm}^{-1}$  is analyzed, where the scattered intensity predominantly arises from contributions of the silica shell.

In Fig. 9, the azimuthal dependence of the averaged intensity is shown exemplarily for FE at a strain of  $\varepsilon = 400\%$  for the complete scattering image (angles from  $0^\circ$  to  $360^\circ$ ) for the lower  $Q$  regime ( $0.07 \text{ nm}^{-1} < Q < 0.15 \text{ nm}^{-1}$ ). Additional plots of the azimuthally averaged intensity can be found in the ESI† (Fig. S2). Although between  $\phi = 100^\circ$  and  $120^\circ$ , no experimental data is accessible due to the beam stop position, we can report the confirmation of the expected high symmetry of  $I(\phi)$  with two mirror planes at  $90^\circ$  and  $180^\circ$  within the limits of experimental accuracy for all samples investigated under the respective geometric circumstances (Fig. 4). For further analysis of the data, it is therefore sufficient to analyze the interval between  $\phi = 0^\circ$  and  $90^\circ$ .

In Fig. 10, the azimuthal intensity distributions for the 2D scattering patterns in Fig. 4 are shown. If no strain is applied ( $\varepsilon = 0\%$ ), the intensity depending on the azimuthal angle is a flat line for all samples, indicating an isotropic orientational distribution of the dispersed nanoparticles. Upon increasing the strain a systematic, significant change in the structure of the  $I(\phi)$  curve is observed, with the maximum at  $90^\circ$  and  $270^\circ$  ( $x$  axis) getting more and more pronounced with increasing  $\varepsilon$  on cost of intensity along the  $y$  axis ( $\phi = 0$ ).

For quantitative analysis of the strain-induced order in particle-filled elastomers, the order parameter is evaluated. The calculation is performed according to an approach presented by Lovell and Mitchel as an averaged over the second



**Fig. 9** Azimuthal scattering intensity depending on the azimuthal angle for sample FE at  $\varepsilon = 400\%$ . The intensity is averaged in the  $Q$  regime  $0.07 \text{ nm}^{-1} < Q < 0.15 \text{ nm}^{-1}$  representative for the small nanoparticle axes. The lack of experimental data and the significant drop of the intensity at angles between  $\phi = 100^\circ$ – $120^\circ$  originate from the beam stop (compare also to the 2D scattering patterns in Fig. 4).





Legendre polynomial, which is given by the following equation.<sup>47</sup>

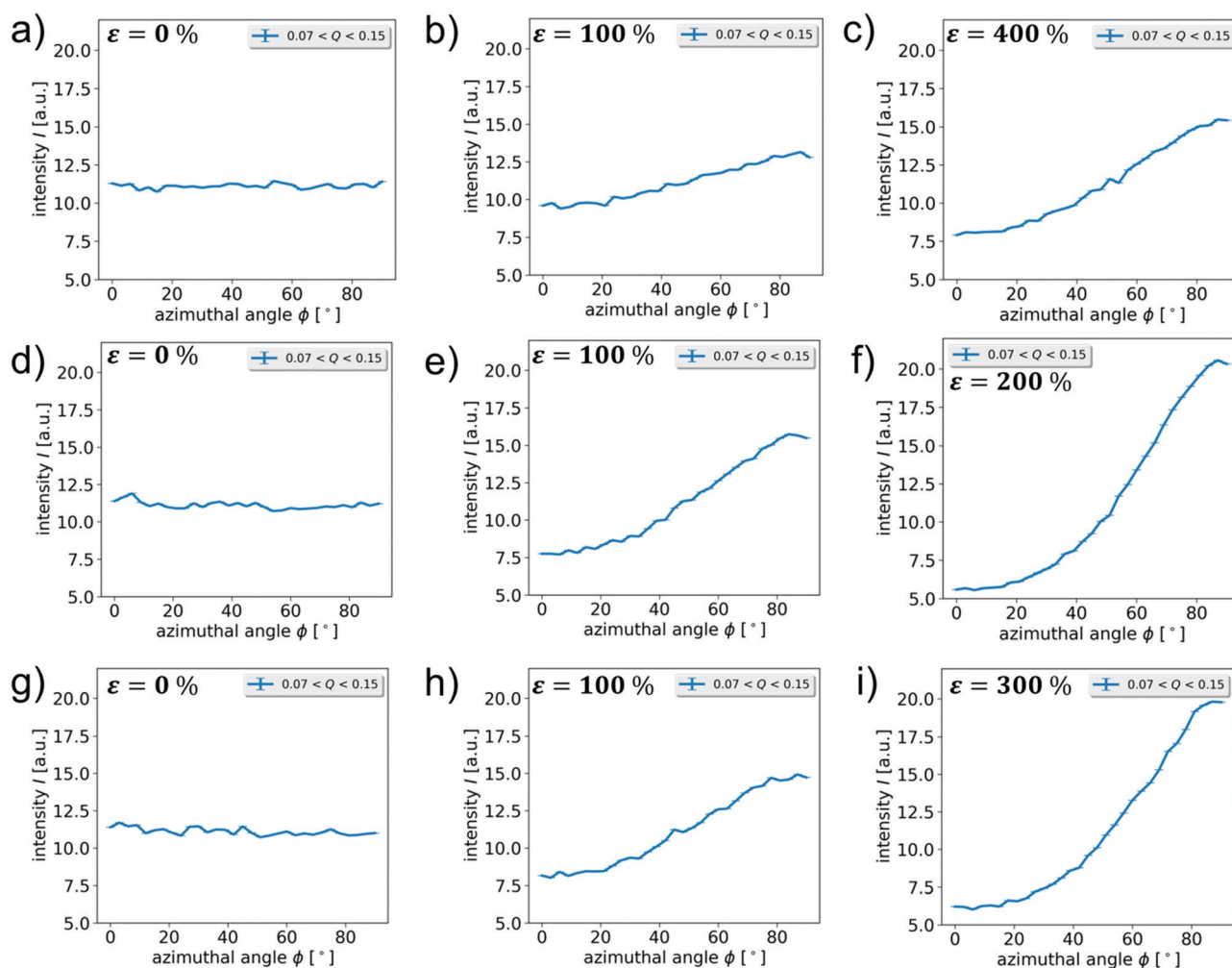
$$S = -2 \cdot \frac{\int_0^\pi I(\phi) \cdot 1/2 \cdot (3 \cos^2 \phi - 1) \cdot \sin \phi d\phi}{\int_0^\pi I(\phi) \cdot \sin \phi d\phi} \quad (11)$$

Here,  $S$  is the order parameter,  $\phi$  is the azimuthal angle ( $y$  axis corresponds to  $\phi = 0$ ), and  $I(\phi)$  is the intensity value at a given azimuthal angle. The order parameter  $S$  is expected to be 0 for statistically distributed, non-oriented particles, 1 for particles whose director is parallel to the test axis, and  $-0.5$  for perfectly orthogonal alignment perpendicular to the test axis. In this case, the short particle axis is defined as the director and the direction  $Q_x$  is the test axis. As explained earlier, the perpendicularity allows to equally ascribe this value to the order of the long particle axis  $l$  with respect to the  $y$  axis, which is strain direction. Thus, the determined order parameter is assigned as  $S_e$  here. Hence, we expect  $S_e = 1$  for perfect alignment of the short axis to  $Q_x$  and, thus, alignment of

the long axis parallel to the applied strain, as is exemplarily shown in the scheme in Fig. 2.

For a quantitative analysis, a background intensity originating from diffuse air scattering as well as unspecific scattering contributions from the sample has to be subtracted before eqn (8) can be used correctly.<sup>48</sup> The procedure on how to determine the background intensity is described in detail in the ESI† (see Section S3).

The obtained order parameters for all samples depending on strain are shown individually in the ESI† (Fig. S4) and sorted by the respective  $Q$  regime of averaging in Fig. 11. The courses of the data points obtained for the low  $Q$  regime, at  $0.07 \text{ nm}^{-1} < Q < 0.15 \text{ nm}^{-1}$ , corresponding to the short axis of the particle core and for the higher  $Q$  regime, at  $0.4 \text{ nm}^{-1} < Q < 1.5 \text{ nm}^{-1}$ , corresponding to the silica shell show the same trend and the individual data points for one sample are almost always identical within error margin. By assuming the azimuthal trend in the two different  $Q$  regimes to originate from predominantly the short particle axis orientation and the silica shell normal



**Fig. 10** Azimuthal scattering intensity depending on the azimuthal angle in the interval  $[0^\circ, 90^\circ]$  for sample FE (a)–(c), CE (d)–(f) and ACE (g)–(i) at different strains. The intensity is averaged in the  $Q$  regime  $0.07 \text{ nm}^{-1} < Q < 0.15 \text{ nm}^{-1}$  representative for the small nanoparticle axes. The respective strain is indicated in the upper left of each scattering pattern and is  $\varepsilon = 0\%$  for the images on the left,  $\varepsilon = 100\%$  for the images in the middle, and the maximum applied strain for the images on the right. For sample ACE the X-ray beam is parallel to the magnetic field applied during synthesis.



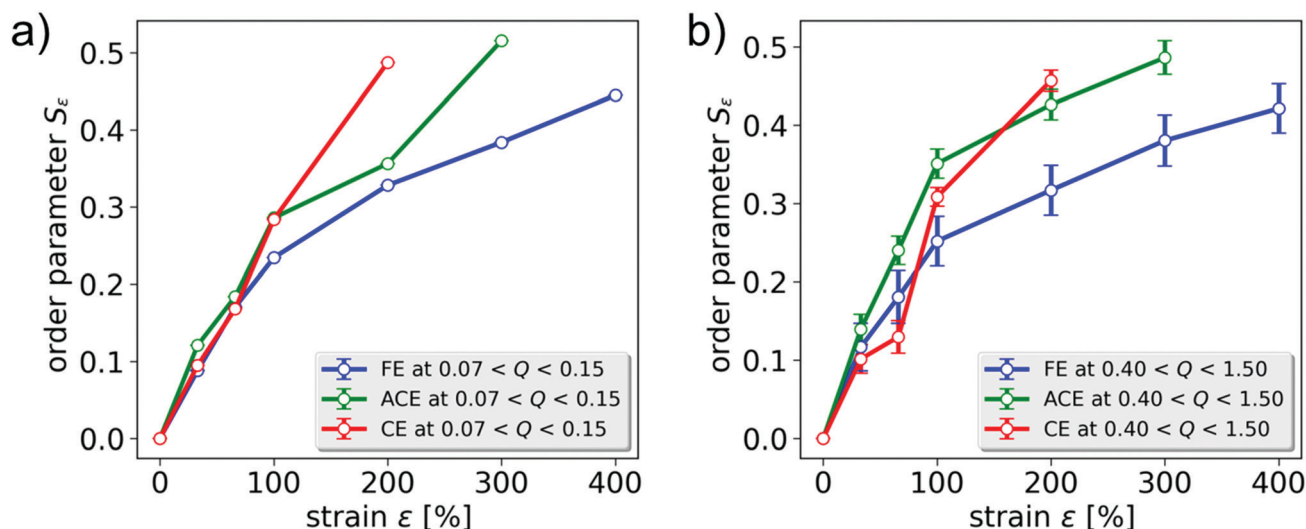


Fig. 11 Order parameter depending on the applied strain determined in the  $Q$  regime (a)  $0.07 \text{ nm}^{-1} < Q < 0.15 \text{ nm}^{-1}$  and (b)  $0.4 \text{ nm}^{-1} < Q < 1.5 \text{ nm}^{-1}$  for varying network architecture (blue: FE-1; red: CE; green: ACE-1). For (a), the errorbars are within the diameter of the symbols.

vector, this coincidence can easily be explained by the predominately parallel orientation of the shell layer with the long particle axis (Fig. 2 and Fig. S4, ESI†) and thus confirms the expectations.

In Fig. 11, the strain-induced order parameters  $S_e$  of all samples are shown sorted by their respective  $Q$  regime. For all samples, the degree of order as calculated from the scattering patterns, thus assigned to the preferred orientation of short particle axis in the  $x$  direction, increases steadily with increasing strain, indicating a preferred orientation of the long axis in the direction of strain. This is thus in accordance with the expectations discussed above.

In comparison of the three investigated samples, we observe that the obtained value and trend of the order parameter  $S_e$  with strain is found to be coinciding for the two chemically crosslinked samples, CE and ACE, within the experimental accuracy, in both  $Q$  regimes. In order to understand this, we should point out that in the given geometry, the scattering patterns of the unstained samples CE and ACE-1 are found to be isotropic, and that the intrinsic order in sample ACE-1 is limited to the axis that is now oriented parallel to the beam. In addition, both samples are synthesized under identical synthetic conditions, including composition and reaction time, and can thus be expected to be of similar chemical crosslinking density. As discussed above, the scattering pattern of magnetically oriented particles is either isotropic or anisotropic depending on the test axis, parallel or perpendicular to the applied field respectively. For maximal comparability of the experimental data, the isotropic direction is chosen as the test axis in our strain-dependent experiments. With respect to the axis of observation, the architecture and distribution of nanoparticles inside the chemically crosslinked elastomers is thus comparable, and no direct influence on the strain-induced orientation behavior is found. We thus conclude that for the analyzed test axis the strain-induced order of the embedded magnetic nanoparticles is

independent of the preorientation of the analyzed filler particles in the  $xy$  plane.

In contrast, for the particle-crosslinked sample FE-1, two regimes can be identified. For small strains up to  $\epsilon = 66\%$ , no significant difference in the strain-induced order parameter  $S_e$  between chemically and particle-crosslinked elastomers is found, and a nearly linear increase of the order parameter with strain is observed. For larger strain values, the strain dependence for the particle-crosslinked elastomers is weaker than for the conventionally crosslinked elastomers. This behavior coincides with the differences found for the mechanical properties of corresponding elastomers with different sample architectures as reported in our previous report: for particle crosslinked-elastomers, the stress-strain curves show a saddle point and a following regime with a low slope of the stress-strain curve, sometimes referred to as rubber elastic plateau, beginning above strains of  $\epsilon = 50\%$ . This plateau is characterized on the mesoscopic length scale by a disentanglement of the long polymer chains linking the particles. The chemically crosslinked elastomers on the other hand do not show a significant rubber elastic plateau and only a small decrease of the slope of the stress-strain curve, similarly observed for the order parameter of these samples in Fig. 11.<sup>16</sup> Additionally, they show significantly lower strain at break, leading to material failure of the analyzed samples CE, and ACE-1 at 200% and 300%, respectively.

We therefore address the nearly linear increase of the order parameter at small strains to the Hookean-type elongation of the sample, that follows similar principles in particle-crosslinked as well as chemically crosslinked elastomers. Upon reaching the rubber elastic plateau, the additional elongation accessible in both architectures is gained by different mechanisms. For the particle-crosslinked sample FE-1, the particle orientation towards the strain direction results from a minimization of the friction on the particle surface that is induced by the polymer chains orienting parallel to the applied



strain vector. In case of the chemically crosslinked sample CE-1 and ACE-1, the meshes of the polymer network are elongated in the strain direction in the tensile deformation. The elongation of the network meshes generates a torque on the particle directing the long axis parallel to the applied strain. This torque is additional for chemically crosslinked polymer networks, and thus a systematically higher order parameter is observed at strains above 66%. It can be anticipated that this reduced strain-induced ordering of particle-crosslinked elastomers is correlated to the high extensibility of these elastomers with strains at break of up to 1700%.

### Mössbauer spectroscopy of strain-and field-induced order in magnetic elastomers

In contrast to the SAXS measurements,  $^{57}\text{Fe}$  Mössbauer spectroscopy is sensitive to the iron-bearing particle cores and provides a powerful technique to unravel their spin and spatial dynamics simultaneously. This has already been shown for spherical nanoparticles in liquid solutions by employing an uniaxial magnetic anisotropy approximation.<sup>49</sup> Here, we exploit this technique to investigate the spatial alignment of spindle-shaped hematite nanoparticles, which exhibit a more complex, sixfold anisotropy within the crystals' basal plane.<sup>22,50</sup>

In this work, Mössbauer spectra of the samples FE-2, FE-3 and ACE-2 are recorded with and without the application of an external magnetic field, and with or without uniaxial deformation of the sample at different strain values at ambient conditions as well as at 4 K.

**Mössbauer analysis of isotropic samples.** A typical Mössbauer spectrum obtained for the isotropic, unstrained samples is shown in Fig. 14a. The absorption lines are commonly indexed with increasing integers from left to right.

In order to get information on the orientation of the magnetic filler particles in the non-isotropic samples, and under the influence of strain and/or external fields, we make use of the condition that the intensity ratios in the typical sextet as obtained in Mössbauer spectroscopy depends on the magnetic alignment of the spins, and can be related to the spatial orientation of the nanoparticles using a Monte Carlo simulation, as described below. The angle  $\theta$  between the spin orientation, determined as the average over all individual spin orientations in the particle, and incident gamma ray, as obtained by Mössbauer spectroscopy, follows from the Wigner-Eckart theorem, from which an exact angular relationship can be described, resulting in an angle-dependent relative line intensity ratio  $A_{23}$  of Mössbauer line 2 and 3 (or 4 and 5 due to the inherent symmetry), respectively:<sup>51</sup>

$$A_{23}(\theta) = \frac{I_2(\theta)}{I_3(\theta)} \quad (12)$$

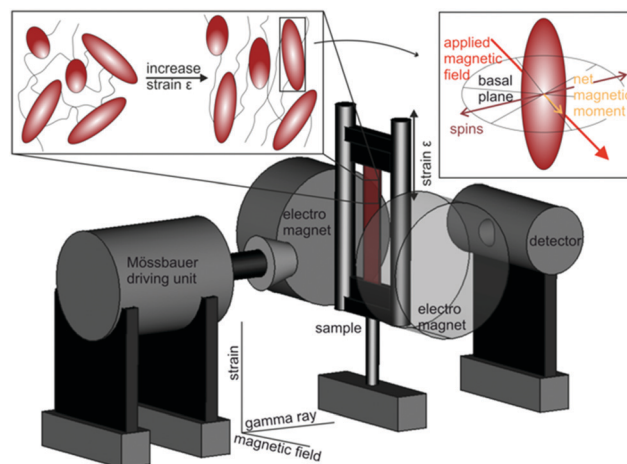
$$= \frac{4 \cdot \sin^2(\theta)}{(1 + \cos^2(\theta))} \quad (13)$$

In order to obtain this value, the experimentally obtained Mössbauer spectra are reproduced by superpositioning two sextet subspectra, as shown as inlay in the upper right

spectrum of Fig. 14a. The two sextets indicate two different types of particle dynamics within the sample. The line intensity ratio  $A_{23}$  is calculated based on the area of the respective absorption lines of the fitted spectrum. Based on  $A_{23}$  and Monte Carlo simulations (see below), information on the mutual orientation of the magnetically and strain-induced order becomes accessible. In the following, the procedure is confirmed for the reference samples and the theoretical limiting cases for the line absorption ratio for statistically oriented as well as completely aligned particles are elaborated.

For zero field and no strain, the particles are randomly oriented within the sample for the isotropic sample FE-2 and FE-3. The experimentally observed line intensity ratio  $A_{23}$  is about 2 for the reference case of no strain and no applied field for the samples FE-2 ( $1.96 \pm 0.06$ ) and FE-3 ( $1.93 \pm 0.05$ ), thus confirming the expectations for isotropic samples.

There are a few other configurations relevant in this study, each of which corresponds to a characteristic line intensity ratio  $A_{23}$ . First, for a particle ensemble that is perfectly uniaxially oriented with the long particle axis perpendicular to the beam, in the absence of magnetic fields the spins are randomly distributed in the particles' basal plane, and the corresponding line intensity ratio expected for this particle ensemble is 4/3. Second, in case that a sufficiently strong magnetic field is applied to a randomly oriented particle ensemble, the particles' magnetic moment aligns with the applied field. In consequence, the direction of the spin alignment, being perpendicular to particles' magnetic moment, is in a two dimensional random distribution, with the corresponding expected  $A_{23}$  value of 4/3. Third, for a fully uniaxially oriented particle ensemble perpendicular to the gamma ray subjected to a strong magnetic field that is both, perpendicular to strain as well as the incident gamma ray, the spins orient



**Fig. 12** Schematic illustration of the Mössbauer setup and alignment behavior of the hematite particles within the strained elastomer. The inset in the top right illustrates the magnetic structure of a hematite particle exposed to an applied magnetic field, as outlined in the Particle characteristics section. Without an applied magnetic field, the net magnetic moment lies randomly in one of the six easy directions within the basal plane.

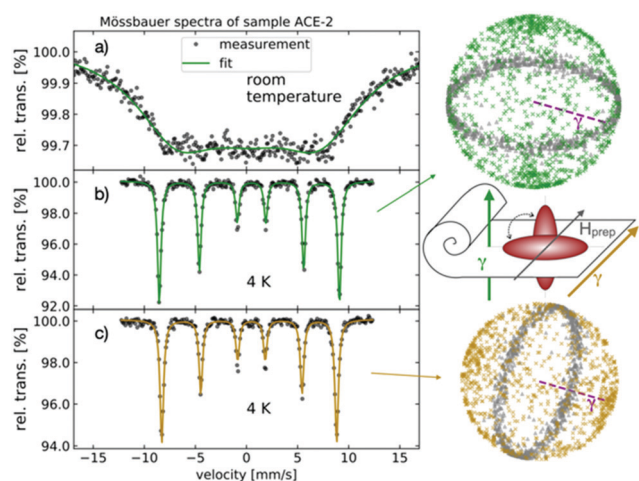


parallel to the gamma ray, and a line intensity ratio of 0 is observed. Finally, a numerically calculated reference value of  $A_{23} = 2.35$  is obtained for a completely aligned particle ensemble in the sample ACE-2, when the preparation field is parallel to the Mössbauer gamma ray. A scheme of the respective particle orientations for this last case can be found in Fig. 13.

**Monte Carlo simulation used for analysis.** For more insights based on the line intensity ratios, a series of Monte Carlo simulations is performed as a valuable tool to extract information on the preferred orientation of the particles'  $c$  axes and the spins. Thereby, a correlation of spatial particle orientation and the experimental  $A_{23}$  line ratio is found. To achieve this, we make use of the fact that the line absorption ratio from the Mössbauer spectra delivers information on the angle between gamma ray and the spin vector. In the simulations, an artificial anisotropic orientational distribution of the particle ensemble is generated by elongation of the long particle axis vector distribution. Afterwards, the correlation between the line absorption ratio and the mean particle orientation is used as an input to extract the corresponding order parameters and allow a direct comparison with the SAXS experiments. Therefore, it is possible to link the spatial alignment to magnetic information by the combination of the two methods.

We introduce the order parameter  $S_i(\alpha)$  for the quantification of the spatial distribution. It is based on the average of the second Legendre polynomial, where  $\alpha$  is the angle between the particles'  $c$  axis and the reference axis  $i$ . In this study, dependent on the experiment at hand,  $i$  can be either the anisotropy axis of the sample  $b$ , or an experimental axis (e.g.,  $y$  or strain direction  $\varepsilon$ ):

$$S_i(\alpha) = \left\langle \frac{3 \cos^2(\alpha) - 1}{2} \right\rangle \quad (14)$$



**Fig. 13** Mössbauer spectra at ambient (a) and cryogenic (4 K), (b) conditions of sample ACE-2, both in geometry with the gamma ray perpendicular (a and b) and parallel (c) to the samples anisotropy axis  $b$  (parallel to  $H_{\text{prep}}$ ). The purple dashed line shown in the spheres indicates the direction of the gamma ray.

Accordingly, the order parameters assigned with  $S_i$  are extracted from the straining experiments, where  $\alpha$  is the angle between particle long axis and straining direction. Order parameters denoted as  $S_b$  correspond to the configuration of the particle axes  $l$  with respect to the sample anisotropy axis  $b$  in ACE samples.

The correlation between the experimentally observed  $A_{23}$  values and the simulated particle configuration is obtained by starting from an ensemble of isotropically oriented particles with a spherical vector distribution that represents the particles'  $c$  axes in the absence of an external stimulus like strain or magnetic field. In this configuration, the magnetically easy directions are located randomly in the basal plane. We simulate a preferential orientation of the particles by uniaxial elongating the vector distribution, while in-field a statistic magnetic alignment is considered by assuming a statistically uniform spin distribution up to a value of  $25^\circ$  around the magnetic field direction within the basal plane. This small deviation is suggested by calculations in a Stoner–Wohlfarth model for the magnetic landscape in a sixfold symmetry with the corresponding fields and anisotropy constants. The calculated order parameters from Mössbauer spectroscopy as well the order parameters obtained from SAXS measurements are compared in Fig. 14c. Here, the simulation is employed to link the orientational distribution of the simulated particle ensemble to the experimentally accessible line absorption ratio of the analyzed samples.

#### Mössbauer analysis of magnetic and geometric anisotropy.

The anisotropically prepared sample ACE-2 is measured without field or strain *via* Mössbauer spectroscopy. At ambient temperatures, the spectral lines appear broadened due to fast particle dynamics on the time scale of a typical Mössbauer experiment, as can be seen in Fig. 13a. In order to enhance the resolution of individual spectral features, Mössbauer spectra at 4 K are recorded and analyzed, as can be seen in Fig. 13b and c.

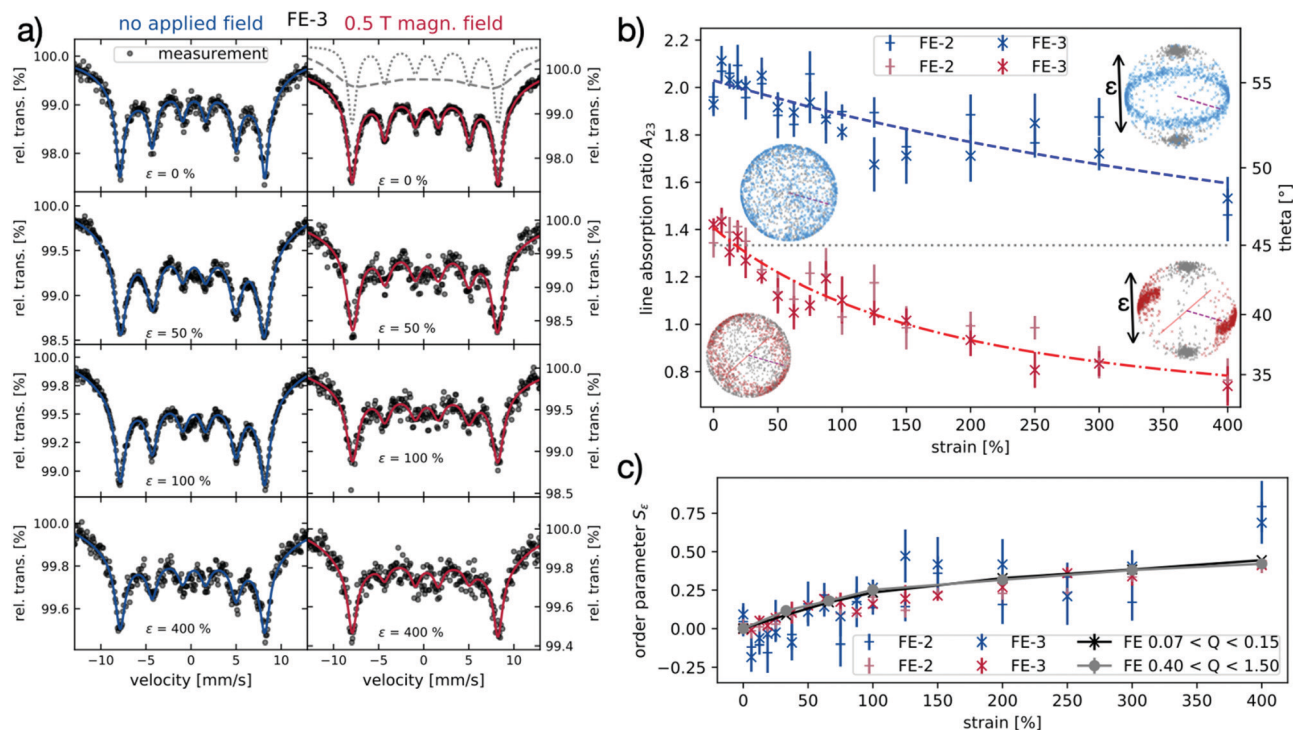
Although the sample is cooled down below the Morin transition temperature of *ca.* 260 K observed in macroscopic samples, no indication for a Morin transition is observed, which would be indicated as a distinct change in the nuclear quadrupole level shift.<sup>52</sup> From the line intensity ratio  $A_{23}$ , it is possible to extract information on the particle spatial distribution, as indicated above in eqn (12) and (13) and the Monte Carlo simulation results. As for this sample ACE-2, we expect different degrees of anisotropy in parallel and in perpendicular direction with respect to the sample anisotropy axis  $b$ , the sample is analyzed in both configurations to obtain the full picture.

In one configuration (depicted in yellow in Fig. 13), the incident gamma ray is out of plane defined by particles'  $c$ -axes and parallel to  $b$ , the magnetic field axis employed during synthesis, while in the second case, a perpendicular arrangement between the beam and anisotropy axis  $b$  is chosen.

In the first case, a narrow, regular sextet is obtained, that allows the calculation of line intensity ratios, as shown in Fig. 13c. The result for the line absorption ratio is 1.81. As discussed above, for completely aligned nanoparticles a







**Fig. 14** Combined results from room temperature Mössbauer spectroscopy without applied magnetic field (blue representations) and in an applied magnetic field of 0.5 T (red representations) with magnetic field direction perpendicular to the incident gamma ray. (a) Selection of Mössbauer spectra for  $\epsilon = 0, 50\%, 100\%$  and  $400\%$ , and two calculated sextet subspectra to illustrate the Mössbauer fitting procedure in the upper right inset; (b) strain-dependent line intensity ratio  $A_{23}$ : the spheres show  $c$ -axis distribution (grey dots) and spin distribution (blue respectively red dots) from Monte Carlo simulations (black arrow, purple dashed line: direction of incident gamma ray, red solid line: magnetic field direction); (c) strain-dependent order parameter  $S_e$  of selected FE samples as obtained from Mössbauer spectroscopy and Monte Carlo simulation, and from SAXS measurements.

reference value of  $4/3$  would be expected in this case. The corresponding geometric order parameter  $S(\alpha)$  that is obtained by the simulation approach amounts to  $S_b = -0.15 \pm 0.03$ . For the second configuration, in the case of a perpendicular arrangement (Fig. 13b), a line intensity ratio of 2.18 is obtained. The completely ordered sample would show an  $A_{23}$  value of 2.35. The experimental value accordingly corresponds to a geometric order parameter of about  $S_b = -0.25 \pm 0.06$ . The negative value of the order parameter, in accordance with the finding from SAXS (see above), describes that the  $c$  axes of the nanoparticles are oriented within a plane perpendicular to the applied field during preparation (see schematic drawing of sample in Fig. 13). Results from Mössbauer spectroscopy and SAXS are nearly equivalent, and their variation is due to experimental limits.

To get information on the intercorrelation of particle order parameter  $S_e$ , strain and magnetization, the isotropically prepared samples FE-2 and FE-3 are analyzed by Mössbauer spectroscopy under the influence of strain and magnetic field perpendicular to the beam direction, respectively. Therefore, the samples are stretched to various extension values of up to  $400\%$ . In contrast to the ACE-2 sample, the samples FE-2 and FE-3 show a sufficiently high line resolution even at ambient conditions. This indicates a different mobility of the embedded nanoparticles in the hybrid elastomer networks of different architecture at the time scale of the Mössbauer experiment,<sup>19</sup>

which is an interesting effect that may be subject of future investigations, but is beyond the scope of this paper. When the particle-crosslinked elastomers are uniaxially strained, a continuous change in the Mössbauer spectra (see Fig. 14a (left)) is obvious. The second and fifth line of the spectrum decrease in intensity with increasing strain, both in the field-off ( $B_0 = 0$  T) and the field-on case ( $B_0 = 0.5$  T, see Fig. 12). The corresponding line intensity ratio  $A_{23}$  is depicted in Fig. 14b for all experiments. For the field-free case, this change in the line intensity ratio, although originally caused by preferential alignment of spins, can be straightly quantified by help of eqn (12) and (13), indicating a narrowing angle between gamma ray and spin with decreasing intensity ratio. This can be explained by the nanoparticles' long axes aligning along the strain direction, leading to a preferred orientation of the easy axes of the particles and thus their basal planes in the beam direction. A lucid visualization of the strain process can be also obtained from Monte Carlo simulations, exemplarily shown in Fig. 14b. For a fully oriented sample, the expected intensity ratio reaches its theoretical limit of a 2-dimensional random orientation at ( $A_{23} = 4/3$ ). This can be confirmed by the experimental findings as seen in Fig. 14: at high strain values, an intensity ratio  $A_{23}$  of about 1.6 is observed. This course is identical within error margin for both samples, FE-2 and FE-3, indicating that the particle fraction does not have an effect on the strain-induced particle orientation, as determined within the accuracy of the Mössbauer experiment.

In the next experiment, we analyze the situation where instead of strain, a magnetic field of 0.5 T is applied perpendicular to the beam during the Mössbauer experiment. Under the influence of the magnetic field, in the absence of mechanical strain, the intensity ratio  $A_{23}$  is about 1.4, thus being close to the expected ideal value of  $4/3$  for the case of a full orientation of the magnetic spins in the plane perpendicular to the beam, which arises due to the unique magnetic characteristics of the nanoparticles. The deviation between theoretical and experimental result is attributed to remaining thermal fluctuation at this field strength and the simplicity of the underlying model.

When the sample is additionally subjected to external strain in the third available dimension, the line intensity ratio decreases further, as seen in Fig. 14b. For this configuration, we can expect the two external stimuli (magnetic field and strain) both to support the orientation of the filler particles. In a case that a full geometric and magnetic orientation would be achieved, the intensity ratio  $A_{23}$  of 0 is expected, corresponding to a spin orientation being completely coaxial to the gamma ray propagation direction. The spins behave differently in the field-free and field-on case and thus the corresponding expected reference values for the line absorption ratio differ, as the particles' canted magnetic moment interacts with the applied magnetic field. Again, for the field-assisted experiments under strain, no significant influence of the particle content on intensity ratio  $A_{23}$  parameter nor the order parameter is found.

Employing the results of Monte Carlo simulations the obtained  $A_{23}$  values are converted to the order parameter  $S_b$ , which is found to systematically increase with the applied strain in Fig. 14c.

**Comparison of SAXS and Mössbauer experiments.** In this study we obtain information on the magnetic and geometric orientation distribution in elastomers filled with magnetic anisometric nanoparticles based on two very complementary methods. Starting from the analysis of the isotropic cases, methods are presented to extract the order parameters of the strain- and/or magnetic field-induced orientation of the filler particles in the matrix.

Thereby, the order parameter  $S_b$  is calculated for anisotropically synthesized elastomers, that possess an intrinsic anisotropy axis  $b$  arising from the field vector during synthesis. From SAXS, the result for ACE-1 is  $S_b = -0.25 \pm 0.01$  for the low  $Q$  regime, while from Mössbauer spectroscopy, the two different configurations give two individual results of  $-0.25 \pm 0.06$  and  $-0.15 \pm 0.03$ , respectively. All results are negative in a similar range, and confirm the preferred orientation of the long particle axis preferentially in a plane perpendicular to  $b$ . While SAXS results show a higher accuracy, the information from Mössbauer spectroscopy additionally comprises the magnetic orientation, which is not accessible by SAXS alone. This is possible, as contrary to SAXS, Mössbauer spectroscopy does not probe a two dimensional projection of the real system, but is sensitive to contributions of all nanoparticles, irrespective of their orientation.

Comparing the results based on Mössbauer spectroscopy experiments and Monte Carlo simulations with the results

obtained from SAXS measurements for strain-induced ordering experiments (see Fig. 14c), a good consistency regarding the strain-dependent degree of spatial particle ordering is found. The observed trend is analogous from the both methods. Here, the better accuracy of SAXS is obvious, while Mössbauer results confirm the magneto-geometric expectations from the particle intrinsic properties. In addition, the application of an external field is shown to increase the reliability of the analysis, yet a stronger particle orientation is not observed under the conditions analyzed. In an upcoming study, this aspect will be addressed in further detail by performing corresponding field-assisted experiments in the SAXS setup. In addition, we look for more sensitive information on the influence of the particle volume fraction for this relatively complex magnetic system.

In this work, a direct link between the magnetic properties and the spatial orientation is achieved. We prove that Mössbauer spectroscopy is a powerful tool to analyze the spatial orientation as well as anisotropic distributions of the spin moments of iron-bearing nanoparticles in complex matrices. It becomes obvious that just the combination of both methods, as performed in this work, delivers the full set of data that is necessary to understand the mutual interdependence of particle orientation, strain, and magnetic field, and is thus particularly valuable for the precise determination of the magnetic as well as orientational anisotropy of magnetic particles in elastic matrices. While SAXS results are more accurate, the results from Mössbauer spectroscopy in combination with Monte Carlo simulations are shown to be advantageous in terms of the information content, as, contrary to SAXS, the analysis allows access to the full orientational information. SAXS data allows analysis of the two-dimensional projection of the true 3D orientation, only. In a follow up paper, we aim to further investigate the influence of applied magnetic fields as well as the particle volume fraction on the orientational anisotropy in particle-crosslinked elastomers.

## Conclusions

In this work, a series of exclusively particle-crosslinked elastomers with systematically varied particle volume fraction and crosslinking degree is prepared, and their strain- and magnetic field-induced increase in geometric and magnetic order is compared to additionally conventionally crosslinked hybrid elastomers.

For this, we employ a combination of Small Angle X-ray Scattering (SAXS) and Mössbauer spectroscopy. Detailed analysis of the 2D SAXS scattering patterns of respective samples in various geometries allow insight into the interplay between orientational and magnetic order in such materials, in dependence of their internal architecture. In addition, in a fully new approach, Mössbauer spectroscopy is employed to in-depth analyze in analogous experiments the orientational order of the magnetic spins by line intensity analysis and Monte Carlo simulations.



By synthesizing the conventionally crosslinked elastomer network in the presence of an external homogeneous magnetic field, the magnetically induced order of the embedded filler particles can be conserved in the subsequent crosslinking process. The resulting intrinsic anisotropy of this architecture conserved in the crosslinking process is analyzed by SAXS and Mössbauer spectroscopy, in order to determine the resulting orientational and magnetic degree of order within the elastomeric matrices. For such samples, an order parameter of  $S_b = -0.25 \pm 0.01$  in the low  $Q$  regime and  $S_b = -0.28 \pm 0.03$  in the high  $Q$  regime is obtained from SAXS analysis, while from line intensity analysis in Mössbauer spectroscopy values of  $S_b = -0.15 \pm 0.03$  and  $-0.25 \pm 0.06$  are determined, depending on the probed direction. Both results are in good correspondence, considering the experimental limits and the fact that two fully independent methods are employed, and indicate not fully aligned nanoparticles, but still a significant degree of order. The correlation between experimentally measured magnetic and the structural orientation is determined *via* Monte Carlo simulation. This orientational order is also found to translate to a magnetic anisotropy. Systematically angular-dependent magnetic properties are observed for sample ACE-1 that can be qualitatively explained on the base of a modified Stoner–Wohlfarth model.

Upon straining the elastomer samples, for all samples the order parameter of the embedded nanoparticles increases systematically with the applied strain. The strain-induced order is probed by SAXS as well as Mössbauer spectroscopy, and the results of both techniques are found to coincide. For the conventionally crosslinked elastomers, the strain-induced anisotropy seems to be independent on the preorientation, and a strong increase of order parameter depending on strain is found with maximum order parameters of  $S_e = 0.50$ . For the particle-crosslinked elastomers, lower values are obtained, but as the structures can be extended to significantly higher extends, here also maximum order parameters of  $S_e = 0.45$  are achieved. The dependence of the order parameter on the strain of the respective samples is related to the mechanical properties, and thereby also to the molecular architecture of the prepared hybrid elastomers.

Using this unique method, additional information becomes available by analysis of the strain-induced order in dependence of an externally applied magnetic field. Although in the configurations employed here, an external field has no significant impact on the strain-induced order within the experimental error, this option will be investigated in more detail in future experiments under optimized conditions.

Our results use new and original approaches based on SAXS and Mössbauer spectroscopy to obtain a detailed picture on the interplay between orientational and magnetic strain induced order and find a direct link between the magnetic structure and the spatial orientation of anisotropic magnetic nanoparticles in elastomeric matrices with different architecture.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

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