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Near-infrared tunable surface plasmon resonance sensors based on graphene plasmons *via* electrostatic gating control

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A tunable near-infrared surface plasmon resonance sensor based on graphene plasmons *via* electrostatic gating control is investigated theoretically. Instead of the traditional refractive index sensing, the sensor can respond sensitively to the change of the chemical potential in graphene caused by the attachment of the analyte molecules. This feature can be potentially used for biological sensing with high sensitivity and high specificity. Theoretical calculations show that the chemical potential sensing sensitivities under wavelength interrogation patterns are 1.5, 2.21, 3, 3.79, 4.64 nm meV⁻¹ at different wavebands with centre wavelengths of 1100, 1310, 1550, 1700, 1900 nm respectively, and the full width half maximum (FWHM) is also evaluated to be 10, 25.5, 43, 55.5, 77 nm at these different wavebands respectively. It can be estimated that the theoretical limit of detection (LOD) in DNA sensing of the proposed sensor can reach the femtomolar level, several orders of magnitude superior to that of noble metal-based SPR sensors (nanomolar or subnanomolar scale), and is comparable to that of noble metal-based SPR sensors with graphene/Au-NPs as a sensitivity enhancement strategy. The FWHM is much smaller than that of the noble metal-based SPR sensors, making the proposed sensor have a potentially higher figure of merit (FOM). This work provides a new way of thinking to detect in an SPR manner the analyte that can cause chemical potential change in graphene and provides a beneficial complement to refractive index sensing SPR sensors.

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1. Introduction

Surface plasmon resonance (SPR) is a powerful optical sensing technology which relies on plasmons, the collective density oscillations of an electron liquid that exist in many metals and semiconductors. In a conventional SPR sensing scheme, a thin metal film (Au, Ag, Cu, Al, *etc.*) is deposited on a prism base and p-polarized incident light excites the surface plasmon polariton at the metal/dielectric (analytes) interface. Due to the highly sensitive, label free, and real time sensing of the change of the refractive index of the analyte, SPR sensors are widely used in chemical and biological sensing. While there exist some limiting factors that hinder further applications of SPR sensors: (1) the nature of refractive index sensing of the SPR sensors makes them have poor specificity.¹ (2) When the change of the analyte concentration may not cause significant refractive index

variations (for instance of gas sensing), SPR sensors display poor sensitivity. (3) The working wavelengths of noble metal-based SPR sensors are limited to visible spectrum and near-infrared spectrum that very closed to visible waveband, and generally cannot be tuned.

Thanks for discovery of graphene, a two-dimensional sheet of carbon atoms arranged in honeycomb lattice, the limiting factors of SPR sensors mentioned above are expected to be overcome. Combining graphene with metal film to make graphene enhanced metal SPR (GEMSPR) sensors has attracted many attentions. Graphene-on-gold structure was firstly considered and the sensitivity enhancing was demonstrated theoretically.² To further enhance the sensitivity, some more complex heterostructures such as graphene-Si-metal,³ graphene-MoS₂-metal,⁴⁻⁶ graphene-WS₂-metal,⁷ graphene-black phosphorus-metal,⁸ WSe₂-WS₂-MoS₂-graphene-metal,⁹ *etc.*, were also considered. Graphene-on-gold SPR imaging platform with a *ca.* 40% sensitivity enhancement was demonstrated experimentally¹⁰ and highly sensitive GEMSPR sensors were used for biological sensing,¹¹⁻¹⁵ even gas sensing.^{16,17} Although GEMSPR sensors can greatly enhance the performance in term of sensitivity comparing with the conventional SPR sensors, their intrinsic refractive index sensing character are still reserved. Furthermore, the working wavelengths of GEMSPR

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sensors are also limited to visible spectrum and near-IR spectrum that very closed to visible waveband and are still nonadjustable.

As a two-dimensional semiconductor, graphene can also support plasmons that different from those in noble metals as they can be tuned by gating or doping.^{18,19} The optical studies of graphene plasmon in the early stage were mostly motivated by terahertz plasmon studies in traditional 2D electron gas system.²⁰ Therefore, the study of graphene plasmon mainly focuses on the terahertz to mid-IR waveband, such as localized plasmons in graphene nanostructures,^{21–23} propagating plasmons excited by metallic tip,²⁴ *etc.* Attempts have also been made to extend the study of graphene plasmon to near-IR and even visible waveband.^{25,26} The unique and intriguing fundamental properties, such as enabling strong confinement of electromagnetic energy at sub-wavelength scales,²⁷ tunable and controllable *via* electric field,²⁸ magnetic field,^{29,30} and light field,³¹ existing new polarization mode,^{32,33} *etc.*, provide an advantage for graphene plasmon over surface plasmon on a metal–dielectric interface. Graphene can be used instead of metal film to manufacture graphene SPR (GSPR) sensors. Despite the theoretically predicted tunability, a key challenge of GSPR sensors is to overcome the momentum mismatch between the free-space waves and the plasmon modes in graphene. Spatial-beam configuration tunable mid-IR graphene plasmonic sensors have been realized for protein detection³⁴ and gas identification³⁵ by using light beam incident directly on graphene nanoribbon arrays (GNA). A prism configuration GNA-based mid-IR GSPR sensor was also demonstrated theoretically which relies on the graphene chemical potential scan for refractive index sensing.³⁶ These all benefit from the plasmon resonances bounded in graphene nanoribbons which can be tuned by changing the ribbon width and the doping level of graphene.²¹ In addition to GNA, a silicon diffractive grating underneath a graphene sheet can also be used to excite mid-IR plasmon mode in graphene through guided-wave resonance caused by a normal-incidence light beam.³⁷ In terahertz spectrum, it was found that the momentum mismatch between the highly confined plasmon modes in homogeneous graphene sheets and the incident radiation could be alleviated by increasing the surface conductivity of graphene through high doping levels or with few layer graphene, and by adopting high-index coupling prism.³⁸ Several prism configuration GSPR sensors with doped graphene for angular interrogation sensing,³⁹ frequency interrogation sensing,⁴⁰ and phase interrogation sensing⁴¹ in THz spectrum were studied theoretically.

In this paper a design of prism configuration GSPR sensor that can work in near-IR spectrum *via* electrostatic gating control is put forward, and the sensing performance is investigated theoretically. The momentum mismatch between the plasmon modes in homogeneous graphene sheets and the incident near-IR radiation could be alleviated by adjusting the chemical potential to be close to the epsilon-near-zero (ENZ) point. By using Si_3N_4 as a dielectric layer, which has a large relative permittivity and a large breakdown field, the chemical potential of graphene can be adjusted to be close to the ENZ point in near-IR spectrum through electrostatic gating without

the breakdown. Based on this, the SPR sensing technology is expected to be realized in the near-IR spectrum which is slightly farther from the visible spectrum, especially in the wavelength range of 1310–2000 nm of existing mature light sources and light detection instruments. The chemical potential sensing (instead of refractive index sensing) feature make the proposed near-IR tunable GSPR sensor has great potential to be used in highly sensitive and high specificity biological and chemical sensing.

2. Structure design and physical mechanism

The proposed sensor takes Otto prism coupling structure as shown in Fig. 1. A 50 nm thick Si_3N_4 layer sandwiched between two graphene sheets (both 5-atom-layer) is placed on a substrate of MgF_2 . A prism is placed on the upside of the top graphene sheet with a gap between them for filling with analyte. A p-polarized laser beam incidents from a side of prism with an incident angle of θ , reflected by the bottom side, then emit through the another side of prism. By adding a gate voltage between the two graphene sheets, they can gate each other⁴² for adjusting their own chemical potentials (absolute value) to a proper value at which the SPR effect of graphene would happen. When the top graphene sheet is attached by analyte molecules, charge transfer (or electrostatic gating) between it and the analyte molecules would cause the chemical potential of it changing further, this would shift the resonance wavelength or resonance angle.

Since the chemically vapor deposited (CVD) mono-atom layer graphene with up to wafer size is already commercially available, it is realistic and feasible to fabricate the structure like in Fig. 1. Using and repeating the standard wet transfer method,⁴³ the randomly stacked few-atom layer bottom graphene sheet can be placed on the MgF_2 substrate. The Si_3N_4 dielectric layer can be deposited on the bottom graphene sheet by using plasma-enhanced chemical vapor deposition (PECVD) method.⁴⁴ The few-atom layer top graphene sheet can be prepared by using the same procedure as that used for the

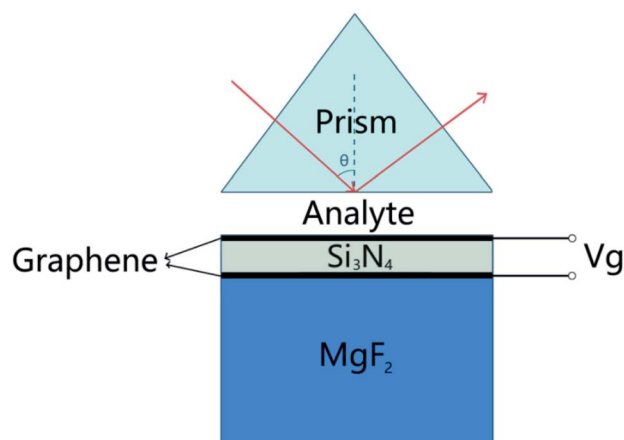


Fig. 1 Schematic diagram of the sensor.



bottom graphene sheet. The Au electrodes attached to graphene sheets (top and bottom) can be prepared by using e-beam evaporation method. The sensor structure can also be designed to adopt the Kretschmann configuration and it is found through calculation that the sensing performance are similar to that of Otto configuration one. The relevant research is described in our another paper in preparation.

The dynamic conductivity of graphene can be obtained from Kubo formula:⁴⁵

$$\sigma(\omega, \mu_c, \Gamma, T) = \frac{-je^2}{\pi\hbar^2(\omega + j2\Gamma)} \int_0^\infty \varepsilon \left(\frac{\partial f_d(\varepsilon)}{\partial \varepsilon} - \frac{\partial f_d(\varepsilon)}{\partial \varepsilon} \right) d\varepsilon + \frac{je^2(\omega + j2\Gamma)}{\pi\hbar^2} \int_0^\infty \frac{f_d(-\varepsilon) - f_d(\varepsilon)}{(\omega + j2\Gamma)^2 + (\varepsilon/\hbar)^2} d\varepsilon \quad (1)$$

where ω , μ_c , Γ , T , j , e , ε and \hbar are radian frequency, chemical potential, scattering rate, temperature, imaginary unit, electron charge, energy and reduced Planck constant respectively. $f_d(\varepsilon) = \{1 + \exp[(\varepsilon - \mu_c)/k_B T]\}^{-1}$ is the Fermi-Dirac distribution, k_B is Boltzmann's constant. The relative permittivity ε_g and the refractive index n_g of graphene is related to its dynamic conductivity by:⁴⁶

$$\varepsilon_g = n_g^2 = 1 + \frac{j\sigma}{\varepsilon_0\omega t_g} \quad (2)$$

where ε_0 and $t_g = 0.34$ nm are the permittivity of free space and thickness of graphene respectively. By using eqn (1) and (2) we can calculate the dielectric constant as a function of both the chemical potential and frequency of light under the condition of $T = 298$ K and $\Gamma = 1 \times 10^{12}$ Hz, as shown in Fig. 2. The demarcation chemical potential μ_{c0} for graphene changing from dielectric to metallic is called ENZ point at which the absolute value of relative permittivity of graphene is near zero. It is interesting that the ENZ point possesses almost linear

dependence on the frequency of light within near-IR spectrum, *i.e.* $\mu_{c0}(\omega) \approx 0.63\hbar\omega$, as shown in Fig. 2(b). So with the increase of frequency (decrease of wavelength), μ_{c0} would become larger, as shown in Fig. 2(c).

To excite the surface plasmon resonance in graphene sheet, the p-polarized incident light should match both the wave vector and energy of the surface plasmon in graphene sheet.

Generally speaking the wave vector of surface plasmon wave in graphene sheet is much larger than that of incident light.³³ While at ENZ point, the absolute value of refractive index of graphene reaches its minimum (near zero), the wave vector of the surface plasmon wave in graphene sheet can be greatly reduced. So the required chemical potential for arousing SPR effect in graphene sheet (called plasmon resonance point, or PR point, marked as μ_{cPR}) must be near the ENZ point and can be calculated through finite element mode analysis in COMSOL (see part 4 of this paper). The ENZ points as well as the PR points at different wavelengths are listed in Table 1. It can be found that the smaller the resonance wavelength λ , the larger the $\mu_{cPR}(\lambda)$ will be. It is also obvious that within near-IR spectrum the PR points are all larger than 0.3 eV (for naturally doped graphene, $\mu_c \leq 0.3$ eV (ref. 46)), which means that generally speaking the SPR effect of naturally doped graphene cannot be aroused by near-IR incident light (let alone by visible incident light). By adding gate voltage, the chemical potential of graphene can be adjusted to PR point for arousing SPR effect of graphene by incident light within near-IR spectrum. The corresponding required gate voltages can be calculated by using:⁴⁷

$$C(V_{DC} - V_{Dirac}) = en_s \quad (3)$$

and⁴⁵

$$n_s = \frac{2}{\pi\hbar^2 v_F^2} \int_0^\infty \varepsilon [f_d(\varepsilon) - f_d(\varepsilon + 2\mu_c)] d\varepsilon \quad (4)$$

where V_{Dirac} is the voltage at the Dirac point, V_{DC} is applied DC bias field, $C = \varepsilon_0 \varepsilon_r / t$ is the gate capacitance (on unit graphene area), ε_r and t are relative permittivity and thickness of Si_3N_4 layer respectively, and $v_F \approx 9.5 \times 10^5$ m s⁻¹ is the Fermi velocity. For undoped graphene, $V_{Dirac} = 0$, the required gate voltages (at wavelengths of 760, 850, 980, 1100, 1310, 1550, 1700, and 1900 nm respectively) can be calculated and listed in Table 1 too. The breakdown field of Si_3N_4 is about 11.5 MV cm⁻¹,⁴⁴ *i.e.* the breakdown voltage of 50 nm-thick Si_3N_4 is about 57.5 V. So the sensor can work in the waveband of $\lambda \geq 1100$ nm.

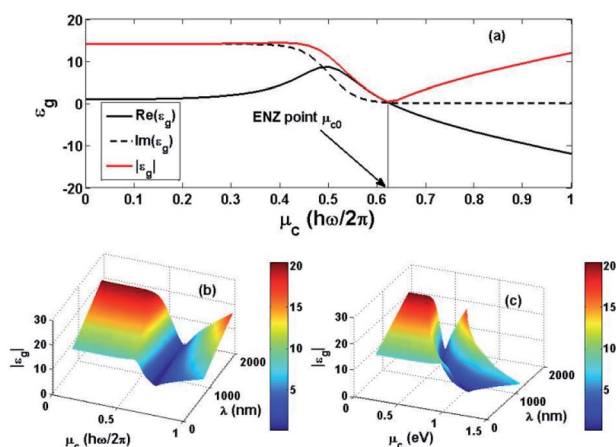


Fig. 2 (a) Relative permittivity of graphene as a function of its chemical potential under the conditions of $\lambda = 1310$ nm, $T = 298$ K, $\Gamma = 1 \times 10^{12}$ Hz; (b) the absolute value of relative permittivity with both wavelength and chemical potential in unit of $\hbar\omega/2\pi$; (c) the absolute value of relative permittivity with both wavelength and chemical potential in unit of eV.

Table 1 ENZ points, PR points, required gate voltages for arousing SPR effect of graphene at different wavelengths

λ (nm)	760	850	980	1100
μ_{c0} (eV)	1.037	0.923	0.798	0.709
μ_{cPR} (eV)	1.048	0.930	0.802	0.712
V_g (V)	122	96	72	57
λ (nm)	1310	1550	1700	1900
μ_{c0} (eV)	0.594	0.502	0.458	0.410
μ_{cPR} (eV)	0.596	0.503	0.459	0.411
V_g (V)	40	28	24	19



3. Numerical method and optimal consideration

The transfer matrix method (TMM) for N-layer model is applied for the calculation of reflectivity of the reflective light. The refractive index and the thickness of the k th layer are considered as n_k and d_k respectively. For p-polarized light, the characteristic matrix of the combined structure of sensor can be given as:⁴

$$M_{ij} = \left(\prod_{k=2}^{N-1} M_k \right)_{ij} = \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix} \quad (5)$$

with

$$M_k = \begin{pmatrix} \cos \beta_k & (-j \sin \beta_k)/q_k \\ -jq_k \sin \beta_k & \cos \beta_k \end{pmatrix} \quad (6)$$

where

$$q_k = \frac{(n_k^2 - n_1^2 \sin^2 \theta_1)^{1/2}}{n_k^2} \quad (7)$$

and

$$\beta_k = \frac{2\pi d_k}{\lambda} (n_k^2 - n_1^2 \sin^2 \theta_1)^{1/2} \quad (8)$$

where λ is the wavelength of the incident light. The reflection coefficient for p-polarized light is given as:

$$r_p = \frac{(M_{11} + M_{12}q_N)q_1 - (M_{21} + M_{22}q_N)}{(M_{11} + M_{12}q_N)q_1 + (M_{21} + M_{22}q_N)} \quad (9)$$

The reflectance of the defined multilayer configuration is:

$$R_p = |r_p|^2 \quad (10)$$

Several representative materials were considered to form prism: CaF₂ (1.4261), ZBLAN (1.4688), BK7 (1.515), SF11 (1.7786), 2S2G (2.241), Si (3.47). In order to choose an optimal material of prism, angular interrogation method is employed to inspect the SPR curves by using a monochromatic light beam incident. The refractive indices of analyte, Si₃N₄, and MgF₂ can be taken as 1.33, 2.57, and 1.37 respectively. The chemical potentials of the top and the bottom graphene sheets are adjusted to the PR points. The thicknesses of graphene sheets and Si₃N₄ are 5×0.34 nm, and 50 nm respectively. The thickness of analyte layer is temporarily set at 1 nm. The reflectance *versus* incident angle curve of monochromatic light beams (with wavelength of 1100, 1310, 1550, 1900 nm respectively) for different materials of the prism are calculated and depicted in Fig. 3. The first minimum reflectance point on the curve from the right-hand side indicates the occurrence of the SPR effect of the graphene. The vertical coordinate of this point can be marked as R_{\min} , and the horizontal coordinate of this point corresponds to resonance angle. For the case of 1100 nm, with the increase of the refractive index of the prism material, R_{\min} decrease gradually and reaches its minimum at Si (3.47), as shown in Fig. 3(a). For the case of 1310 nm, with the increase of

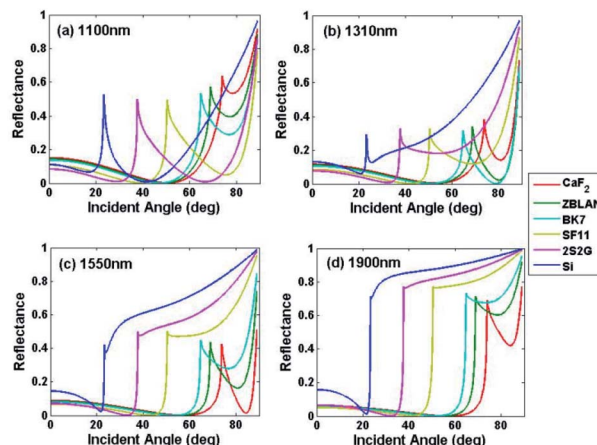


Fig. 3 Reflectance *versus* incident angle curves for different prism materials when using incident monochromatic light beam with different wavelength: (a) 1100 nm; (b) 1310 nm; (c) 1550 nm; (d) 1900 nm.

the refractive index of the prism material, R_{\min} firstly decrease gradually and reaches its minimum at BK7 (1.515), and then increase gradually, as shown in Fig. 3(b). For the cases of 1550 nm and 1900 nm, R_{\min} all reaches its minimum at CaF₂ (1.4261), as shown in Fig. 3(c) and (d). It can be seen that with the increase of the wavelength of the incident light, the refractive index of the optimal material of the prism becomes smaller.

The optimal thickness of the analyte layer t_a is then investigated through angular interrogation method. For the different wavelength of 1100, 1310, 1550, 1700, and 1900 nm, by adopting the optimal materials of prism for each wavelength, *i.e.* Si for 1100 nm, BK7 for 1310 nm, CaF₂ for 1550, 1700, and 1900 nm respectively, the SPR curves at different t_a can be calculated and the last four are depicted in Fig. 4(a)–(d) respectively. Accordingly, the R_{\min} *versus* t_a curves for the different wavelength of 1310, 1550, 1700, and 1900 nm are depicted in Fig. 5(a)–(d)

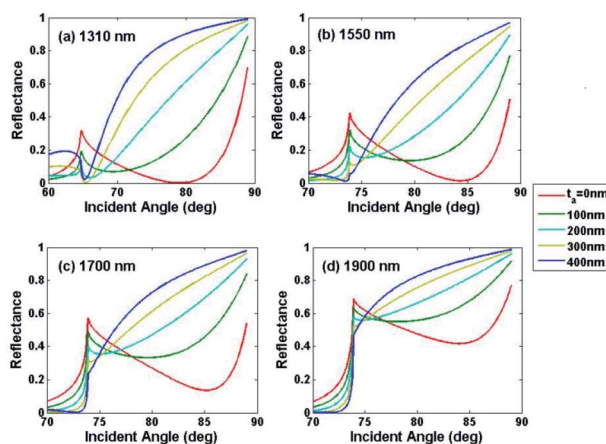


Fig. 4 Reflectance *versus* incident angle curves for different thickness of the analyte layer when using incident monochromatic light beam with different wavelength: (a) 1310 nm; (b) 1550 nm; (c) 1700 nm; (d) 1900 nm.



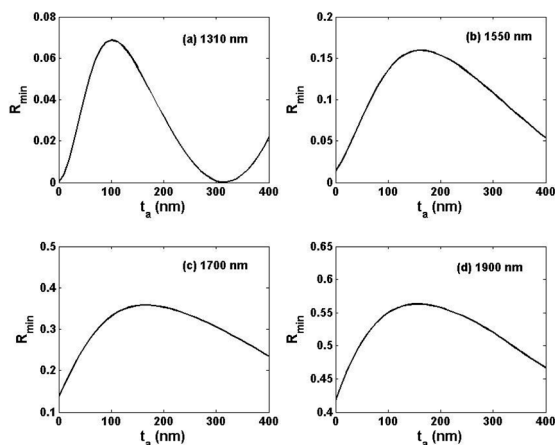


Fig. 5 R_{\min} as a function of t_a for different wavelength of incident light beam: (a) 1310 nm; (b) 1550 nm; (c) 1700 nm; (d) 1900 nm.

respectively. So considering not only R_{\min} , but also the actual size of the analyte molecules (such as biomolecules), we take the optimal thickness of the analyte layer to be 300 nm. The resonance angle also changes with t_a . When $t_a = 300$ nm, the resonance angle can be obtained as 24.1° , 65.4° , 74.2° , 74.1° , and 74° for different wavelength of 1100, 1310, 1550, 1700, and 1900 nm respectively.

In order to inspect the sensing characteristics of the sensor under wavelength interrogation pattern, the chemical potentials of the top and the bottom graphene sheets were all adjusted to the PR point $\mu_{\text{CPR}}(\lambda')$, and a broadband light beam with λ' as a central wavelength was incident. The refractive index of graphene $n_g(\lambda)$ as a function of λ (around λ') can be calculated through eqn (1) and (2) under the conditions of $\mu_c = \mu_{\text{CPR}}(\lambda')$, $T = 298$ K, $\Gamma = 1 \times 10^{12}$ Hz. The reflectance curves at different wavebands with central wavelengths of 1100, 1310, 1550, 1700, and 1900 nm respectively are calculated and the last four are depicted in Fig. 6. In calculation the thickness of the

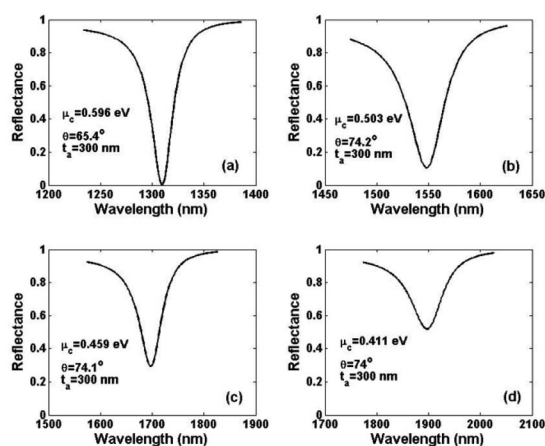


Fig. 6 Reflectance versus wavelength curves for the chemical potential of graphene reach the PR point of different wavelength: (a) $\mu_c = \mu_{\text{CPR}}$ (1310 nm); (b) $\mu_c = \mu_{\text{CPR}}$ (1550 nm); (c) $\mu_c = \mu_{\text{CPR}}$ (1700 nm); (d) $\mu_c = \mu_{\text{CPR}}$ (1900 nm).

analyte layer were taken as $t_a = 300$ nm; the optimal materials of prism are adopted for each central wavelength, *i.e.* Si for 1100 nm, BK7 for 1310 nm, CaF_2 for 1550, 1700, and 1900 nm, respectively. The resonance angles obtained from angular interrogation calculation are adopted for the incident angles, *i.e.* 24.1° , 65.4° , 74.2° , 74.1° , and 74° for the broadband light beam with central wavelengths of 1100, 1310, 1550, 1700, and 1900 nm, respectively. It can be seen that the FWHM becomes larger with the increase of the resonance wavelength, and they are 10, 25.5, 43, 55.5, and 77 nm for central wavelengths 1100, 1310, 1550, 1700, and 1900 nm respectively. Contrastingly, a graphene oxide–Au GEMSPR sensor with resonance wavelength located in the range of 600–900 nm has a FWHM larger than 100 nm.¹³ Generally, the FWHM will increase with the resonance wavelength. So it can be inferred that the FWHMs of the proposed near-IR GSPR sensor are much smaller than that of GEMSPR sensors assuming their resonance wavelengths can reach the same near-IR wavelengths (*i.e.* 1100–2000 nm).

4. Sensing performance based on wavelength interrogation pattern

By adding gate voltage, the chemical potential of the top and the bottom graphene sheets were set to an PR point $\mu_{\text{CPR}}(\lambda')$ (thereby the resonance wavelength would be λ'). When the analyte was injected into the space between the prism and the top graphene sheet, two changes would be brought about: one, the chemical potential of the top graphene sheet would be changed further (from the PR point) due to the charge transfer between graphene and the attached analyte molecules; two, the refractive index of the analyte layer would be changed. In order to estimate the response sensitivity of the resonance wavelengths to the change of the chemical potential of the top graphene sheet, the chemical potential of the bottom graphene sheet is set to keep at PR point (because no analyte was attached on it), and the chemical potential of the top graphene sheet is set to change around the PR point, meantime the refractive index of the analyte was assumed to be constant and set to 1.33. The variation of SPR curves in different wavebands with central wavelengths of 1100, 1310, 1550, 1700, and 1900 nm respectively with the change of the chemical potential of the top graphene sheet can be calculated and the last four are depicted in Fig. 7. In calculation the thickness of the analyte layer is taken as $t_a = 300$ nm; the optimal materials of prism are adopted for each central wavelength; the incident angles are 24.1° , 65.4° , 74.2° , 74.1° , and 74° for the broadband light beam with central wavelengths of 1100, 1310, 1550, 1700, and 1900 nm, respectively. With the increase of chemical potential of the top graphene sheet (meanwhile the chemical potential of the bottom graphene sheet keeps constant, *i.e.* PR point), the resonance wavelengths all shift to smaller values (blue shift). The response sensitivities of the resonance wavelengths to the change of the chemical potential of the top graphene sheet (called CP sensitivity) are about 1.5, 2.21, 3, 3.79, 4.64 nm meV^{-1} at different wavebands with central wavelengths of 1100, 1310, 1550, 1700, and 1900 nm respectively. With the decrease of the resonance



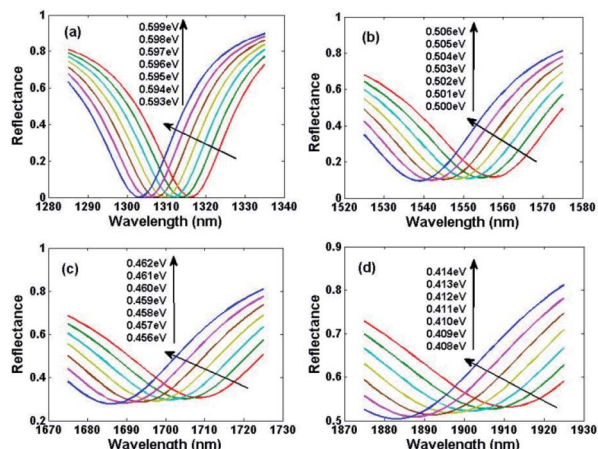


Fig. 7 The variation of SPR curves in different wavebands with central wavelengths of (a) 1310; (b) 1550; (c) 1700; (d) 1900 nm respectively with the change of the chemical potential of the top graphene sheet.

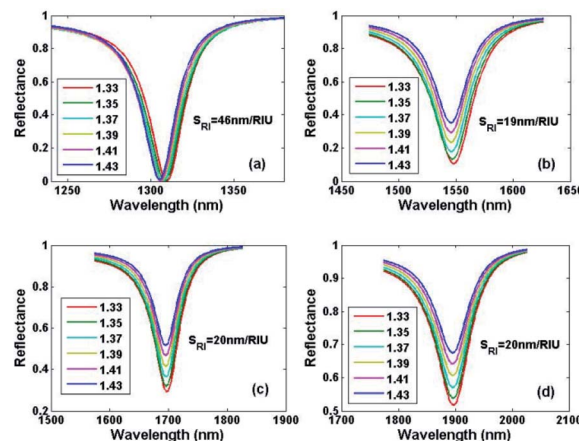


Fig. 9 The variation of SPR curves in different wavebands with central wavelengths of (a) 1310; (b) 1550; (c) 1700; (d) 1900 nm respectively with the change of the refractive index of the analyte layer.

wavelength, the CP sensitivity becomes smaller, as shown in Fig. 8(a). Keep in mind that the refractive index of graphene changes with its chemical potential, the response sensitivity of the resonance wavelengths to the change of the refractive index of the top graphene sheet (called RI sensitivity) can also be estimated, as shown in Fig. 8(b).

In order to estimate the RI sensitivities of the resonance wavelengths to the change of refractive index of the analyte, the chemical potentials of the top and the bottom graphene sheets are all set to PR point $\mu_{co}(\lambda')$, and the refractive index of the analyte is set to change within the range of 1.33–1.43. The variation of SPR curves at different wavebands with central wavelengths of 1100, 1310, 1550, 1700, and 1900 nm respectively with the refractive index of the analyte can be calculated and the last four are depicted in Fig. 9. With the increase of the refractive index of the analyte, the resonance wavelengths all shift to smaller values, as shown in Fig. 9. The absolute value of the RI sensitivity are about 19, 46, 19, 20, 20 nm per RIU at

different wavebands with central wavelengths of 1100, 1310, 1550, 1700, and 1900 nm respectively.

Obviously, the RI sensitivity of the near-IR GSPR sensor to either the change of the refractive index of the top graphene sheet or the change of the refractive index of the analyte is much lower than that of GEMSPR sensors, which typically reach several thousands of nm/RIU,¹³ even more than 10 thousands of nm per RIU.¹⁴ The reason that the resonance wavelength of the near-IR GSPR sensor is insensitive to the change of the refractive index of the analyte is probably because the plasmon is not at the surface of but inside the graphene sheet.⁴⁸ The 2D finite element method simulation results confirm that the plasmon mode field mainly distributes inside the graphene sheets, as shown in Fig. 10. This is very different from a noble metal-based SPR sensor, in which the plasmon exits at the interface between the metal and the analyte; and this is also different from the GSPR sensors in THz spectrum⁴¹ (and even mid-IR spectrum³⁷) in which the plasmon mode has a greater decay length in the direction perpendicular to the graphene plane and penetrates into the analyte. The shift of the resonance wavelength is directly caused by the change of graphene chemical potential, rather than by the change of graphene refractive index, so the near-IR GSPR sensor should be considered to have chemical potential sensing (instead of refractive index sensing) character.

This chemical potential sensing feature can be used for detecting sensitively the analyte whose attachment on graphene can cause a remarkable change of chemical potential in graphene, no matter the refractive index change in the analyte layer caused by the attachment are small (for instance of gas molecules) or large (for instance of bio molecules). It is well known that the attachment of bio molecules on graphene will cause charge transfer (or electrostatic gating) and can change the chemical potential of graphene.^{49,50} According to Dong *et al.*, the hybridization of 0.01 nM complementary DNAs to the probe DNAs pre-immobilized on graphene would cause >10 meV of chemical potential shift in graphene.⁵⁰ For a near-IR GSPR

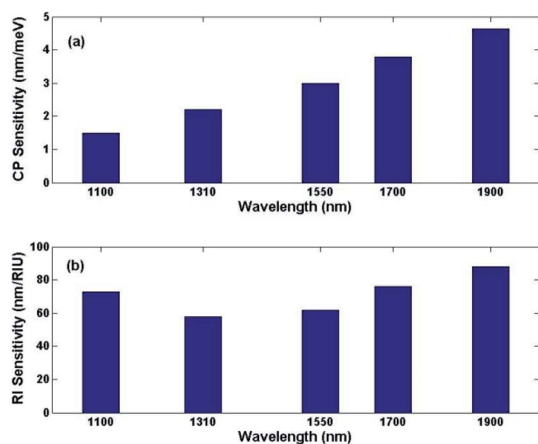


Fig. 8 (a) CP sensitivity of the sensor at different resonance wavelength; (b) RI sensitivity of the sensor at different resonance wavelength.



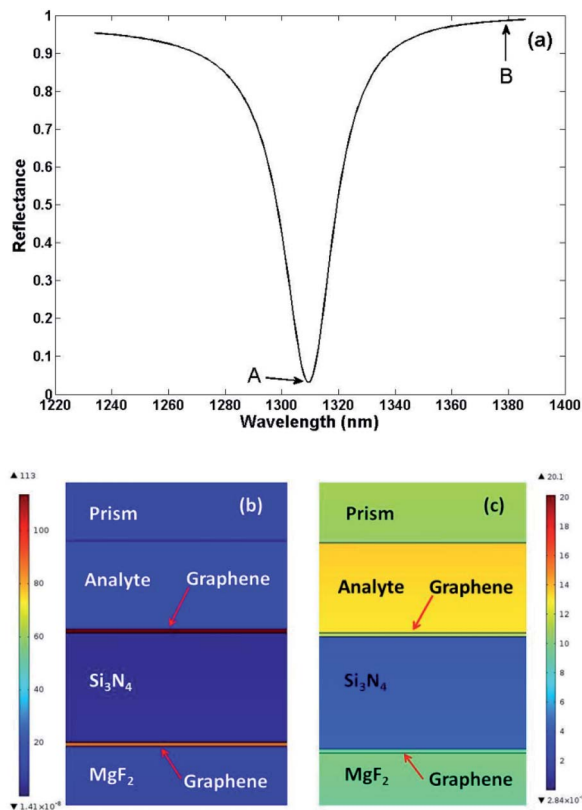


Fig. 10 (a) SPR curve in the waveband with 1310 nm as a central wavelength under the condition of $t_a = 40$ nm. The distribution of the electromagnetic field in the cross section of the multi-layer system corresponding to point A and B in (a) are displayed in (b) and (c) respectively.

sensor proposed in this paper, it would cause >15 , >22.1 , >30 , >37.9 , and >46.4 nm of resonance wavelength shifts at different wavebands with central wavelengths of 1100, 1310, 1550, 1700, and 1900 nm respectively. Supposing the wavelength resolution of the optical spectrum analyser (OSA) is 0.02 nm, the proposed near-IR GSPR sensor can reach LOD of <13.33 , <9.05 , <6.67 , <5.28 , and <4.31 fM in DNA sensing at different wavebands with central wavelengths of 1100, 1310, 1550, 1700, and 1900 nm respectively. Contrastingly, the LOD of the noble metal-based SPR sensors in DNA sensing are nM or sub-nM scale,⁵¹ and the LOD of the GEMSPR sensors with Au-NPs as sensitivity enhancement-strategy in DNA sensing can reach fM or sub-fM scale.⁵² The selected recent literatures on DNA detection by SPR manner since 2019 are listed in Table 2. Although the LOD

has been improved further,^{54–57} a notable feature is the need to use gold nanoparticles or nanorods as sensitivity enhancement strategy.

The other advantage of the chemical potential sensing feature is that it enhances the specificity of the sensor. Bio adsorbates may change the charge carrier density (hence the chemical potential) of graphene using two possible mechanisms: electrostatic gating or partial electron transfer.⁵⁸ For example, electron-rich biomolecules can impose p-doping effect on graphene through electrostatic gating effect,⁴⁹ also can impose n-doping effect on graphene through π -stacking interaction which leads to partial electron transfer.⁵⁰ P-doping and n-doping effect leads to increase and decrease of absolute value of chemical potential in p-doped graphene respectively (the opposite is true for n-doped graphene). The chemical potential sensing-based near-IR SPR sensor can differentiate this opposite change in chemical potential absolute value easily and can achieve the selectivity between those different kinds of biomolecules may with similar refractive index but with different molecule structures. Let us inspect the achievement of the selectivity of the chemical potential sensing-based near-IR SPR sensor between complimentary DNA and mismatched DNA in DNA sensing. The partial electron transfer mechanism dominates in DNA sensing because the aromatic nucleotide bases in DNA are easily combined with graphene by π -stacking.

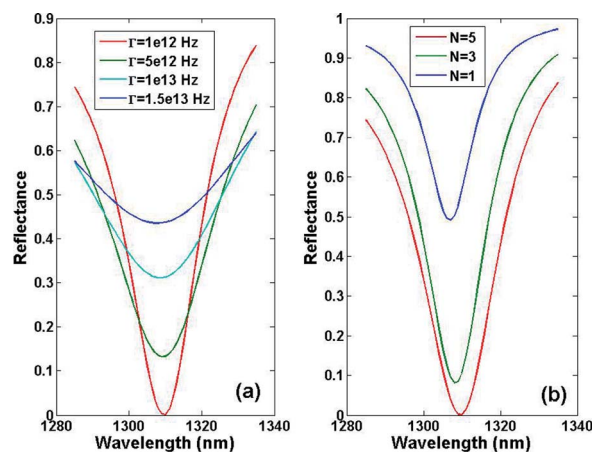


Fig. 11 (a) SPR curves in the waveband with 1310 nm as a central wavelength for different scattering rate of both top and bottom 5-atom-layer graphene sheets; (b) SPR curves in the waveband with 1310 nm as a central wavelength for different atom layer number of both the top and the bottom graphene sheets with $\Gamma = 1 \times 10^{12}$ Hz.

Table 2 The selected recent literatures on DNA detection by SPR manner since 2019

SPR structure	LOD	FWHM	Ref.
Fiber/Au film	80 nM	—	53
K9/Au film/GO-AuNPs	0.2 fM	—	54
K9/AuNT array/AuNPs	1.2 aM	114.471 nm	55
K9/Au film/graphene/AuNPs	0.5 fM	—	56
K9/Au film/antimonene/AuNRs	10 aM	—	57
CaF ₂ /analyte/graphene/Si ₃ N ₄ /graphene/MgF ₂	<4.31 fM	77 nm	This paper



For a graphene sheet with saturate attachment of probe DNAs, the specific binding (*i.e.* hybridization through hydrogen-bond) between complimentary DNAs and probe DNAs immobilized on graphene can cause n-doping effect on graphene and change the chemical potential of graphene;⁵⁰ while the mismatched DNAs can neither attach to graphene by π -stacking interaction (because graphene has been saturated attached by probe DNAs) nor bind with probe DNAs through hydrogen-bond interaction, so the non-specific attachment of mismatched DNAs on graphene causes almost no doping effect on graphene and almost does not change the chemical potential of graphene. So the chemical potential sensing-based near-IR GSPR sensor can respond sensitively to the specific attachment of the complementary DNAs and almost does not respond to the non-specific attachment of the mismatched DNAs, despite their attachment on the graphene may cause similar refractive index change in the analyte layer. As a result, the near-IR GSPR sensor at least has potential to simplify the process of DNA sensing compared to the RI sensing-based SPR sensors, since the non-specific attached mismatched DNAs does not have to be flushed away and does not interfere with the results.

As a SPR sensor based on graphene plasmons, its performance would be affected by the quality of the graphene (especially the top graphene sheet). The quality of graphene obtained by different preparation methods varies greatly. The charge carrier mobility μ of graphene sheet generally ranges from ~ 1000 to $10\,000\text{ cm}^2\text{ (V}^{-1}\text{ s}^{-1})$ in CVD graphene.³⁷ The scattering rates corresponding to charge carrier mobilities of 1000 to $10\,000\text{ cm}^2\text{ (V}^{-1}\text{ s}^{-1})$ at $\mu_c = 0.596\text{ eV}$ are $\Gamma = 1.5 \times 10^{13}$ to $1.5 \times 10^{12}\text{ Hz}$ (calculated using $\mu = (ev_F^2)/(\Gamma\mu_c)$ ⁴⁶). As an example, the influences of the scattering rate Γ of the 5-atom-layer graphene sheets (top and bottom) and the atom layer number of the graphene sheets (top and bottom) with scattering rate $\Gamma = 1.0 \times 10^{12}\text{ Hz}$ on the SPR curve with a central wavelength of 1310 nm are investigated and depicted in Fig. 11. As shown in Fig. 11(a), with the increase of the scattering rate Γ of the graphene, the R_{\min} of the SPR curve increases rapidly and results in decreasing the extinction ratio of the SPR curve, meanwhile the FWHM increases rapidly. As shown in Fig. 11(b), with the decrease of the atom layer number of the graphene sheets, the R_{\min} of the SPR curve increase gradually, meanwhile the FWHM decreases gradually.

5. Conclusions

In conclusion, a prism-configuration tunable near-IR GSPR sensor is proposed and its wavelength interrogation sensing performance is investigated theoretically. By adjusting the chemical potential of graphene to the PR points *via* electrostatic gating control, the momentum mismatch between the plasmon modes in homogeneous graphene sheets and the incident near-IR radiation could be alleviated and SPR effect of graphene can be aroused within near-IR spectrum. The PR points at different wavelengths are calculated through finite element method in COMSOL and the corresponding required gate voltages are also calculated. Instead of traditional refractive index sensing, the proposed near-IR GSPR sensor can respond sensitively to the

change of the chemical potential in graphene, and the CP sensitivities as well as the FWHMs of SPR curve in different wavebands within near-IR spectrum are calculated through transfer matrix method. This chemical potential sensing feature make the sensor have great potential to be used in highly sensitive biological sensing and have improved specificity. The optimal prism material, the optimal analyte layer thickness, the incident angle for working in different wavebands, and the influences of the quality (in term of the scattering rate) and atom layer number of graphene on the SPR curve are also investigated. This work provides a new thinking to detect the analyte in SPR manner which can cause chemical potential change in graphene and provides a beneficial complement to refractive index sensing SPR sensors. The tunable feature of the sensor is also helpful to achieve a balance of high sensitivity and high figure of merit in future near-IR spectral SPR sensing.

Conflicts of interest

There are no conflicts to declare.

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Notes and references

- 1 J. Homola, *Anal. Bioanal. Chem.*, 2003, **377**, 528–539.
- 2 L. Wu, H. S. Chu, W. S. Koh and E. P. Li, *Opt. Express*, 2010, **18**, 14395–14400.
- 3 R. Verma, B. D. Gupta and R. Jha, *Sens. Actuators, B*, 2011, **160**, 623–631.
- 4 J. B. Maurya, Y. K. Prajapati, V. Singh and J. P. Saini, *Appl. Phys. A*, 2015, **121**, 525–533.
- 5 L. M. Wu, Y. Jia, L. Y. Jiang, J. Guo, X. Y. Dai, Y. J. Xiang and D. Y. Fan, *J. Lightwave Technol.*, 2017, **35**, 82–87.
- 6 S. Aksimsek, H. Jussila and Z. P. Sun, *Opt. Commun.*, 2018, **428**, 233–239.
- 7 M. H. Wang, Y. Y. Huo, S. Z. Jiang, C. Zhang, C. Yang, T. Y. Ning, X. Y. Liu, C. H. Li, W. Y. Zhang and B. Y. Man, *RSC Adv.*, 2017, **7**, 47177–47182.
- 8 L. M. Wu, J. Guo, Q. K. Wang, S. B. Lu, X. Y. Dai, Y. J. Xiang and D. Y. Fan, *Sens. Actuators, B*, 2017, **249**, 542–548.
- 9 Z. N. Lin, S. J. Chen and C. Y. Lin, *Sensors*, 2020, **20**, 2445.
- 10 W. Wei, J. P. Nong, Y. H. Mei, C. Y. Zhong, G. L. Lan and W. H. Hu, *Sens. Actuators, B*, 2018, **273**, 1548–1555.



- 11 L. J. He, Q. Pagneux, I. Larroulet, A. Y. Serrano, A. Pesquera, A. Zurutuza, D. Mandler, R. Boukherroub and S. Szunerits, *Biosens. Bioelectron.*, 2017, **89**, 606–611.
- 12 C. M. Das, L. X. Kang, M. W. Chen, P. Coquet and K. T. Yong, *ACS Appl. Nano Mater.*, 2020, **3**, 10446–10453.
- 13 X. Xiong, Y. F. Chen, H. Wang, S. Q. Hu, Y. H. Luo, J. L. Dong, W. G. Zhu, W. T. Qiu, H. Y. Guan, H. H. Lu, J. H. Yu, J. Zhang and Z. Chen, *ACS Appl. Mater. Interfaces*, 2018, **10**, 34916–34923.
- 14 Q. Wang, X. Z. Wang, H. Song, W. M. Zhao and J. Y. Jing, *Opt. Laser Technol.*, 2020, **124**, 106002.
- 15 H. X. Yu, Y. Chong, P. H. Zhang, J. M. Ma and D. C. Li, *Talanta*, 2020, **219**, 121324.
- 16 W. Wei, J. P. Nong, G. W. Zhang, L. L. Tang, X. Jiang, N. Chen, S. Q. Luo, G. L. Lan and Y. Zhu, *Sensors*, 2017, **17**, 2.
- 17 F. Usman, J. O. Dennis, E. M. Mkawi, Y. Al-Hadeethi, F. Meriaudeau, T. L. Ferrell, O. Aldaghri and A. Sulieman, *Polymers*, 2020, **12**, 2750.
- 18 A. N. Grigorenko, M. Polini and K. S. Novoselov, *Nat. Photonics*, 2012, **6**, 749–758.
- 19 M. Jablan, M. Soljagic and H. Buljan, *Proc. IEEE*, 2013, **101**, 1689–1704.
- 20 S. Y. Huang, C. Y. Song, G. W. Zhang and H. G. Yan, *Nanophotonics*, 2017, **6**, 1191–1204.
- 21 L. Ju, B. S. Geng, J. Horng, C. Girit, M. Martin, Z. Hao, H. A. Bechtel, X. G. Liang, A. Zettl, Y. R. Shen and F. Wang, *Nat. Nanotechnol.*, 2011, **6**, 630–634.
- 22 V. W. Brar, M. S. Jang, M. Sherrott, J. J. Lopez and H. A. Atwater, *Nano Lett.*, 2013, **13**, 2541–2547.
- 23 Z. Y. Fang, S. Thongrattanasiri, A. Schlather, Z. Liu, L. L. Ma, Y. M. Wang, P. M. Ajayan, P. Nordlander, N. J. Halas and F. J. G. de Abajo, *ACS Nano*, 2013, **7**, 2388–2395.
- 24 Z. Fei, A. S. Rodin, G. O. Andreev, W. Bao, A. S. Mcleod, M. Wagner, L. M. Zhang, Z. Zhao, M. Thiemens, G. Dominguez, M. M. Fogler, A. H. Castro Neto, C. N. Lau, F. Keilmann and D. N. Basov, *Nature*, 2012, **487**, 82–85.
- 25 F. J. G. de Abajo, *ACS Photonics*, 2014, **1**, 135–152.
- 26 J. S. Gomez-Diaz and J. Perruisseau-Carrier, *Opt. Express*, 2013, **21**, 15490–15504.
- 27 D. A. Iranzo, S. Nanot, E. J. C. Dias, I. Epstein, C. Peng, D. K. Efetov, M. B. Lundberg, R. Parret, J. Osmond, J. Y. Hong, J. Kong, D. R. Englund, N. M. R. Peres and F. H. L. Koppens, *Science*, 2018, **360**, 291–295.
- 28 S. Thongrattanasiri, I. Silveiro and F. J. G. de Abajo, *Appl. Phys. Lett.*, 2012, **100**, 201105.
- 29 H. G. Yan, Z. Q. Li, X. S. Li, W. J. Zhu, P. Avouris and F. N. Xia, *Nano Lett.*, 2012, **12**, 3766–3771.
- 30 N. Kumada, P. Rouleau, B. Roche, M. Hashisaka, H. Hibino, I. Petkovic and D. C. Glatli, *Phys. Rev. Lett.*, 2014, **113**, 266601.
- 31 G. X. Ni, L. Wang, M. D. Goldflam, M. Wagner, Z. Fei, A. S. Mcleod, M. K. Liu, F. Keilmann, B. Ozyilmaz, A. H. Castro Neto, J. Hone, M. M. Fogler and D. N. Basov, *Nat. Photonics*, 2016, **10**, 244–248.
- 32 S. A. Mikhailov and K. Ziegler, *Phys. Rev. Lett.*, 2007, **99**, 016803.
- 33 A. Vakil and N. Engheta, *Science*, 2011, **332**, 1291–1294.
- 34 D. Rodrigo, O. Limaj, D. Janner, D. Etezadi, F. J. G. de Abajo, V. Pruneri and H. Altug, *Science*, 2015, **329**, 165–168.
- 35 H. Hu, X. X. Yang, X. D. Guo, K. Khaliji, S. R. Biswas, F. J. G. de Abajo, T. Low, Z. P. Sun and Q. Dai, *Nat. Commun.*, 2019, **10**, 1131.
- 36 R. B. Hwang, *Sci. Rep.*, 2021, **11**, 1999.
- 37 W. L. Gao, J. Shu, C. Y. Qiu and Q. F. Xu, *ACS Nano*, 2012, **6**, 7806–7813.
- 38 C. H. Gan, *Appl. Phys. Lett.*, 2012, **101**, 111609.
- 39 A. Purkayastha, T. Srivastava and R. Jha, *Sens. Actuators, B*, 2016, **227**, 291–295.
- 40 Y. Huang, S. C. Zhou, H. Z. Yao and D. X. Cai, *Phys. Status Solidi A*, 2017, **214**, 1600550.
- 41 Y. Huang, S. C. Zhong, Y. C. Shen, Y. J. Yu and D. X. Cui, *Nanoscale*, 2018, **10**, 22466–22473.
- 42 J. S. Gomez-Diaz, C. Moldovan, S. Capdevila, J. Romeu, L. S. Bernard, A. Magrez, A. M. Lonescu and J. Perruisseau-Carrier, *Nat. Commun.*, 2015, **6**, 6334.
- 43 E. J. Lee, S. Y. Choi, H. Jeong, N. H. Park, W. Yim, M. H. Kim, J. K. Park, S. Son, S. Bae, S. J. Kim, K. Lee, Y. H. Ahn, K. J. Ahn, B. H. Hong, J. Y. Park, F. Rotermund and D. I. Yeom, *Nat. Commun.*, 2015, **6**, 6851.
- 44 W. J. Zhu, D. Neumayer, V. Perebeinos and P. Avouris, *Nano Lett.*, 2010, **10**, 3572–3576.
- 45 G. W. Hanson, *J. Appl. Phys.*, 2008, **103**, 064302.
- 46 M. Mohsin, D. Neumaier, D. Schall, M. Otto, C. Matheisen, A. L. Giesecke, A. A. Sagade and H. Kurz, *Sci. Rep.*, 2015, **5**, 10967.
- 47 J. S. Gomez-Diaz, M. Esquius-Morote and J. Perruisseau-Carrier, *Opt. Express*, 2013, **21**, 24856–24872.
- 48 M. Jablan, H. Buljan and M. Soljagic, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2009, **80**, 245435.
- 49 N. Mohanty and V. Berry, *Nano Lett.*, 2008, **8**, 4469–4476.
- 50 X. C. Dong, Y. M. Shi, W. Huang, P. Chen and L. J. Li, *Adv. Mater.*, 2010, **22**, 1–5.
- 51 H. Sipova and J. Homola, *Anal. Chim. Acta*, 2013, **773**, 9–23.
- 52 O. Zagorodko, J. Spadavecchia, A. Y. Serrano, I. Larroulet, A. Pesquera, A. Zurutuza, R. Boukherroub and S. Szunerits, *Anal. Chem.*, 2014, **86**, 11211–11216.
- 53 P. Q. Gong, Y. M. Wang, X. Zhou, S. K. Wang, Y. N. Zhang, Y. Zhao, L. V. Nguyen, H. Ebendorff-Heidepriem, L. Peng, S. C. Warren-Smith and X. G. Li, *Anal. Chem.*, 2021, **93**, 10561–10567.
- 54 S. M. Chen, Y. Liu, Q. X. Yu and W. Peng, *Sens. Actuators, B*, 2021, **327**, 128935.
- 55 S. M. Chen, C. Liu, Y. Liu, Q. Liu, M. D. Lu, S. Bi, Z. G. Jing, Q. X. Yu and W. Peng, *Adv. Sci.*, 2020, **7**, 2000763.
- 56 Y. Sun, H. Y. Cai, X. Qiao and X. P. Wang, *Meas. Sci. Technol.*, 2019, **30**, 125701.
- 57 T. Y. Xue, W. Y. Liang, Y. W. Li, Y. H. Sun, Y. J. Xiang, Y. P. Zhang, Z. G. Dai, Y. H. Duo, L. M. Wu, K. Qi, B. N. Shivananju, L. J. Zhang, X. Q. Cui, H. Zhang and Q. L. Bao, *Nat. Commun.*, 2019, **10**, 28.
- 58 A. B. Artyukhin, M. Stadermann, R. W. Friddle, P. Stroeve, O. Bakajin and A. Noy, *Nano Lett.*, 2006, **6**, 2080–2085.

