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# Band engineering of Dirac materials in $\text{Sb}_m\text{Bi}_n$ lateral heterostructures†

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Band engineering the electronic structures of  $\text{Sb}_m\text{Bi}_n$  lateral heterostructures (LHS) from antimonene and bismuthene is systematically investigated using first principles calculations. The spin–orbit coupling is found to be crucial in determining electronic structures of  $\text{Sb}_m\text{Bi}_n$  LHS. The results indicate that these lateral heterostructures have a type-II band alignment which can be easily tuned using their size and tensile strain. The band gap tends to zero when the lateral heterostructure size is larger than a critical value, which intrinsically corresponds to a semiconductor-to-semimetal transition. The band inversion near the  $\Gamma$  point occurs under suitable tensile strain, indicating that  $\text{Sb}_m\text{Bi}_n$  LHS are very promising to realize quantum spin Hall effects.

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## 1. Introduction

Heterojunctions between three-dimensional (3D) semiconductors with different band gaps form the basis of modern light-emitting diodes<sup>1</sup> and high-speed transistors.<sup>2</sup> Similar to the conventional 3D heterojunctions, two-dimensional (2D) heterojunctions comprise two kinds of nanomaterials with different electron affinities and band gaps.<sup>3–5</sup> Consequently, they exhibit excellent optoelectronic performance, which cannot be achieved by the individual nanomaterials. Therefore, 2D heterojunctions provide many new opportunities for tailoring the electronic and transport properties as well as for realizing novel device architectures. To utilize 2D crystalline semiconductors as building blocks for next-generation electronics, the exploration of new 2D heterojunctions is crucial. In general, two types of 2D heterostructures can be synthesized: vertical heterostructures (VHS) and lateral heterostructures (LHS). VHS can be obtained by vertical stacking of 2D crystals in a layered configuration on top of each other,<sup>6–8</sup> and their properties are dominated by the stacking orientation and interlayer coupling strength. However, the poor controllability of band structures in VHS limits its practical applications. In contrast, LHS represent a new class of designer materials that can be composed of a variety of 2D materials, which are structurally and mechanically similar but exhibit entirely different electronic and optical properties. Spatially connected LHS exhibit two surfaces and simpler band alignment as compared to VHS, and their electrical and optical properties are intrinsically dominated by the band alignment at the heterointerfaces. Further,

the domains in LHS are usually connected by covalent bonds, which ensure the epitaxial quality of the interface, thereby boosting the optical and electrical properties of the heterostructures.<sup>9,10</sup> These attributes of LHS have motivated significant efforts in the exploration of new heterostructures with unique properties.

The recent advances in the synthesis and characterization of monoatomic thick materials have facilitated the fabrication of various 2D LHS including graphene/h-BN<sup>11</sup> and transition metal dichalcogenides (TMD).<sup>12–14</sup> However, it is always a great challenge to synthesize 2D LHS with clean heterointerfaces, which are very important in the field of high performance devices.<sup>15–17</sup> VHS have been fabricated using chemical vapor deposition (CVD)<sup>18</sup> and other advanced synthetic methods. Fortunately, CVD is also used for epitaxial growth of LHS,<sup>19</sup> which can offer precise spatial control to achieve atomically sharp transition in compositions at the heterojunction. Consequently, several LHS have been synthesized by this technique. For example, Zhang *et al.*<sup>10</sup> proposed a synthetic method for highly robust epitaxial growth of diverse LHS and superlattices with atomically sharp interfaces. Hong *et al.*<sup>20</sup> demonstrated the synthesis and practical applications of graphene/MoS<sub>2</sub> LHS, indicating that the choice of a suitable MoS<sub>2</sub> growth temperature is crucial for the synthesis process. Further, an atomically sharp zigzag-like boundary has been observed to dominate the patching interface of graphene/h-BN,<sup>21</sup> MoS<sub>2</sub>/WS<sub>2</sub> (ref. 22) and MoSe<sub>2</sub>/WSe<sub>2</sub>.<sup>23</sup> Nevertheless, so far, suitable basis materials available for synthesizing LHS are extremely limited. Therefore, it is crucial to explore such materials to synthesize novel LHS.

Recently, nanomaterials formed by group VA elements such as phosphorene, arsenene, antimonene, and bismuthene have emerged as a novel type of 2D materials, which exhibit intriguing structures and properties, leading to a wide range of applications in electronics and optoelectronics.<sup>24–27</sup> Phosphorene is the first material in this family; recently, it was

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mechanically isolated from bulk phosphorus and has already been used to fabricate transistors.<sup>28,29</sup> Unfortunately, phosphorene is very unstable and is rapidly oxidized by the atomic layer deposition process.<sup>30,31</sup> In addition, during the synthesis process of arsenene, highly toxic arsenic trioxide can be produced, which hinders the experimental exploration of arsenene.<sup>32</sup> Unlike unstable phosphorene, antimonene and bismuthene are predicted to exhibit good stability and remarkable physical properties.<sup>33,34</sup> Antimonene is an indirect-band gap semiconductor with an optical gap of 2.28 eV,<sup>35</sup> while its band gap with spin-orbit coupling (SOC) is 0.76 eV.<sup>36</sup> By contrast, bismuthene is a direct-band gap semiconductor with an optical gap of 0.55 eV (ref. 37 and 38) and exhibits a cone-like structure near  $\Gamma$  point. However, when SOC is included, the degenerate bands at the top of the valence band at the  $\Gamma$  point exhibit a Rashba-type splitting and reduce the band gap to 0.51 eV (ref. 39) by changing its character from direct-to indirect-band gap. Notably, under appropriate tensile strain, antimonene not only transforms from indirect-to direct-band gap semiconductor but also exhibits band inversion, indicating that they are very promising to realize quantum spin Hall effect (QSHE).<sup>35,36</sup> Besides, a novel quantum spin Hall state with tunable edge states has been predicted in a structure of antimonene and bismuthene on suitable substrates.<sup>40,41</sup> The substrate induces a drastic staggered exchange field in 2D film, which plays a vital role in generating the QSHE. All these merits of 2D materials motivated us to design LHS based on them.

Herein, we systematically investigate the band engineering of  $\text{Sb}_m\text{Bi}_n$  LHS ( $m$  and  $n$  denote the number of Sb or Bi atomic chains) at the zigzag interface *via* first-principles calculations. SOC is found to be crucial in determining the electronic structures. We observed that all the stable  $\text{Sb}_m\text{Bi}_n$  LHS exhibit a type-II band alignment and relatively small band gaps (0.004–0.254 eV) as comparing with initial antimonene and bismuthene. For  $m = n$ ,  $\text{Sb}_m\text{Bi}_n$  LHS are confirmed to be Dirac materials, which exhibit a Dirac cone near the Fermi level.  $\text{Sb}_m\text{Bi}_n$  LHS are very similar to spin-valley-coupled Dirac semimetals, whose massless Dirac fermions are fully spin polarized.<sup>26</sup> For  $m \neq n$ ,  $\text{Sb}_m\text{Bi}_n$  LHS are confirmed to be semiconductor materials. Therefore, we have demonstrated that  $\text{Sb}_m\text{Bi}_n$  LHS can maintain the Dirac semimetallic character only if the condition  $m \approx n$  is satisfied. Additionally, the size of  $\text{Sb}_m\text{Bi}_n$  LHS is one of the crucial parameters that govern its electronic and optical performance. It is similar to the size dependent band gaps of TMD LHS;<sup>42</sup> the band gap of  $\text{Sb}_m\text{Bi}_n$  LHS tend to zero when the size is larger than the critical value, which essentially corresponds to the transition from semiconductor to semimetal. Besides, the orbital-projected band structure indicates that the Bi- $p_y$  orbitals dominate the energy band near the Fermi level, while the orbitals of Sb atoms have a minor effect on it. It is reasonable to ignore the effect of the orbitals of Sb atoms on the energy bands of  $\text{Sb}_m\text{Bi}_n$  LHS. The orbital-projected band structure demonstrates that the band inversion near  $\Gamma$  point occurs on suitable tensile strain, indicating that  $\text{Sb}_m\text{Bi}_n$  LHS are very promising to realize QSHE. Therefore, we believe that the excellent properties of  $\text{Sb}_m\text{Bi}_n$  LHS realized in this study will inspire further theoretical as well as experimental investigations on these materials.

## 2. Computational methods

Here, all the structural relaxation and electronic calculations are based on density functional theory (DFT) implemented in the Vienna *ab initio* simulation package (VASP).<sup>43,44</sup> The exchange-correlation functional was treated within the generalized gradient approximation (GGA) and parameterized by Perdew–Burke–Ernzerhof (PBE)<sup>45</sup> functional. Sb and Bi are heavy atoms, hence SOC must take into account in the calculation of electronic structures. The long-range van der Waals interaction between atomic layers was taken into account by employing the semi-empirical dispersion-corrected D3 scheme proposed by Grimme.<sup>46</sup> A cutoff energy of the plane wave was set to 550 eV. The k-point sampling in the Brillouin zone was implemented by the Monkhorst–Pack scheme, where  $16 \times 16 \times 1$  and  $2 \times 9 \times 1$  grids were used for optimizing the geometry of pristine antimonene (or bismuthene) and  $\text{Sb}_m\text{Bi}_n$  LHS, respectively. All atoms were optimized until the variations in the total energy and residual force were less than  $10^{-5}$  eV and  $10^{-2}$  eV  $\text{\AA}^{-1}$ , respectively. To avoid the interaction between adjacent layers, a vacuum spacing of 15  $\text{\AA}$  was added along the direction perpendicular to the 2D sheet. As GGA method underestimates the band gap of semiconductor materials, the Heyd–Scuseria–Ernzerhof screened hybrid functional (HSE06)<sup>47</sup> was used to compute the electronic and optical properties of  $\text{Sb}_m\text{Bi}_n$  LHS. The charge density difference and work function was calculated using VASPKIT code.<sup>48</sup>

## 3. Results and discussion

### 3.1 Structural properties

According to recent studies, high-quality 2D LHS such as graphene/h-BN<sup>11</sup> and TMD<sup>12–14</sup> with atomically sharp interfaces along armchair or zigzag direction have been fabricated *via* CVD method. In heterointerfaces, the zigzag boundaries are preferably formed, while the armchair interfaces, which usually have many defects, are rarely observed. Therefore, we simulate  $\text{Sb}_m\text{Bi}_n$  LHS with zigzag-type interface using first-principles calculation. The fully optimized  $\text{Sb}_m\text{Bi}_n$  LHS are shown in Fig. 1(a), where the indices  $m$  and  $n$  denote the number of Sb or Bi atomic chains. Here, we fix the lattice constant of the  $Z$  axis and fully relax the lattice constants in the  $X$  and  $Y$  directions, so all atoms of LHS are fully relaxed, and their energies and forces are optimized to reach the minimum values with  $10^{-5}$  eV and  $10^{-2}$  eV  $\text{\AA}^{-1}$ , respectively. The bond length and unit cells of LHS are illustrated in Table S1.† We found that the lattice constant  $a$  increases, but that of  $b$  remains a constant value about 4.24  $\text{\AA}$  with the increase of the width of the heterojunction. Sb–Sb and Bi–Bi bond length of the antimonene and bismuthene are 2.89  $\text{\AA}$  and 3.04  $\text{\AA}$ , respectively. However, the average bond lengths of Sb–Sb, Sb–Bi, and Bi–Bi in the LHS are 2.90, 2.97, and 3.04. Comparing bond lengths between the antimonene, bismuthene and LHS, it is found that the Sb–Sb bond length is elongated from 2.89  $\text{\AA}$  to 2.90  $\text{\AA}$ , while the Sb–Bi and Bi–Bi bond length remains almost a constant value. Besides, the antimonene and bismuthene (Fig. 1(c) and (d)), basic structural units of  $\text{Sb}_m\text{Bi}_n$  LHS, are observed to be indirect band gap semiconductors



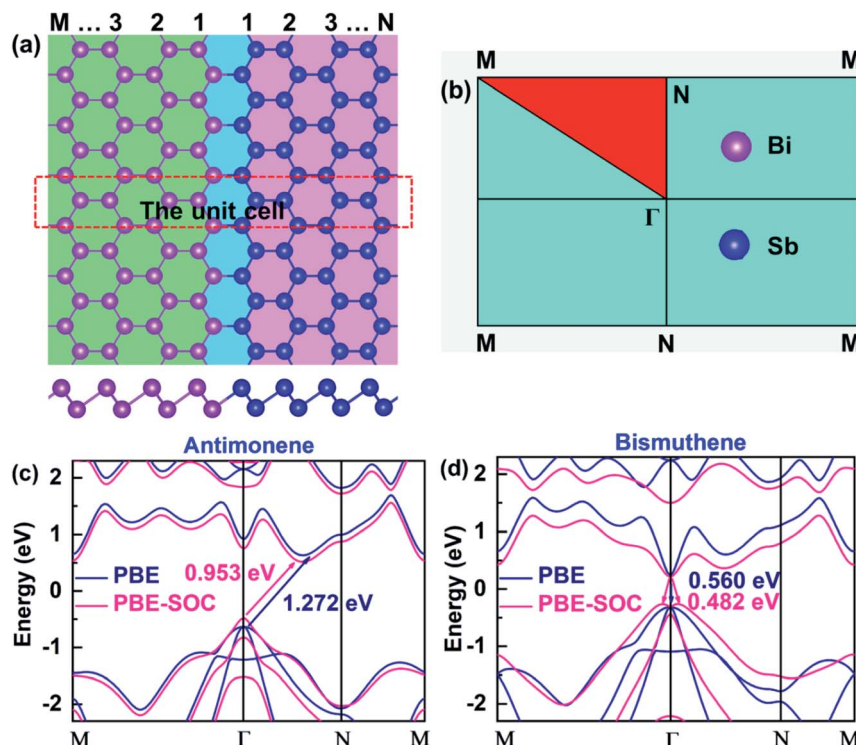


Fig. 1 (a) Top view (upper) and side view (lower) of atomic configurations of  $\text{Sb}_m\text{Bi}_n$  LHS with zigzag boundaries. (b) The 2D Brillouin zone with high symmetry points. (c and d) The electronic structure of pristine antimonene and bismuthene are calculated in PBE and PBE-SOC, respectively.

under SOC with optical gaps of 0.953 and 0.482 eV, which is in good agreement with earlier studies.<sup>36,37</sup> The calculation results reveal that the valence band maximum (VBM) of antimonene and bismuthene has a degenerate character of  $p_x$  and  $p_y$  orbitals. Particularly, VBM at the  $\Gamma$  point of bismuthene exhibits a Rashba-type splitting under SOC, which changes its character from direct band gap to indirect. However, VBM of antimonene is located at the  $\Gamma$  point and its conduction band minimum (CBM) lies between  $\Gamma$  and  $N$  points (Fig. 1(c)). The different positions of VBM and CBM in antimonene and bismuthene induce unique physical properties in  $\text{Sb}_m\text{Bi}_n$  LHS based on the two materials, which may open up new opportunities for high-performance devices.

### 3.2 Electronic structure and stability of LHS

The electronic structure of 2D materials is crucial for their applications in the field of semiconductors, photodetectors and other fields. Here, we study the electronic structures of  $\text{Sb}_2\text{Bi}_2$  LHS under PBE, PBE-SOC, HSE-SOC, which are shown in Fig. 2(a), (b) and (d), respectively. Comparing the band structures of  $\text{Sb}_2\text{Bi}_2$  LHS under PBE and HSE, it is evident that PBE underestimates the energy gaps. However, comparing the high computational cost of HSE functional with the significance of SOC on the electronic structure of  $\text{Sb}_m\text{Bi}_n$  LHS, it is reasonable to discard HSE functional for calculating the band structures of  $\text{Sb}_m\text{Bi}_n$  LHS. Besides, the stability and experimental feasibility are essential for  $\text{Sb}_2\text{Bi}_2$  LHS, therefore we examined its phonon dispersion spectra. Once  $\text{Sb}_2\text{Bi}_2$  LHS is confirmed to be stable,

the other LHS should also show excellent stability. The phonon dispersion spectrum of  $\text{Sb}_2\text{Bi}_2$  LHS with zigzag interface is shown in Fig. 2(c). Generally, the appearance of soft modes in phonon calculations indicates that the structure is unstable. Here, no soft phonon modes are observed in the computed phonon dispersion spectrum of  $\text{Sb}_2\text{Bi}_2$  LHS, which validates its kinetic stability. The stability of  $\text{Sb}_m\text{Bi}_n$  LHS not only provides a good opportunity to investigate its properties, but also indicates the feasibility to experimentally synthesize it.

As we all know that the stabilities of nanomaterials are related to its cohesive energy, which is usually defined as the work when nanomaterials are decomposed into a single atom. Therefore, the cohesive energy per atom of  $\text{Sb}_m\text{Bi}_n$  LHS can be calculated using eqn (1):<sup>49</sup>

$$E_{\text{coh}} = \frac{E_{\text{tot}} - N_A E_{\text{atom}}^A - N_B E_{\text{atom}}^B}{N_A + N_B} \quad (1)$$

where  $E_{\text{tot}}$  is the total energy of  $\text{Sb}_m\text{Bi}_n$  LHS at the equilibrium states;  $E_{\text{atom}}^A$  and  $E_{\text{atom}}^B$  are the total energies of the isolated atoms Sb (−2.75 eV per atom) and Bi (−2.18 eV per atom) in the freedom states, respectively;  $N_A$  and  $N_B$  indicate respectively the total number of Sb and Bi atom in each unit cell. Therefore, the cohesive energy of  $\text{Sb}_m\text{Bi}_n$  LHS is calculated about −1.55 eV per atom when  $m$  and  $n$  are different values.

In order to verify the heterojunction formation abilities, we calculate formation energy. If the formation energy is negative, the formation of the heterojunction nanomaterials from its

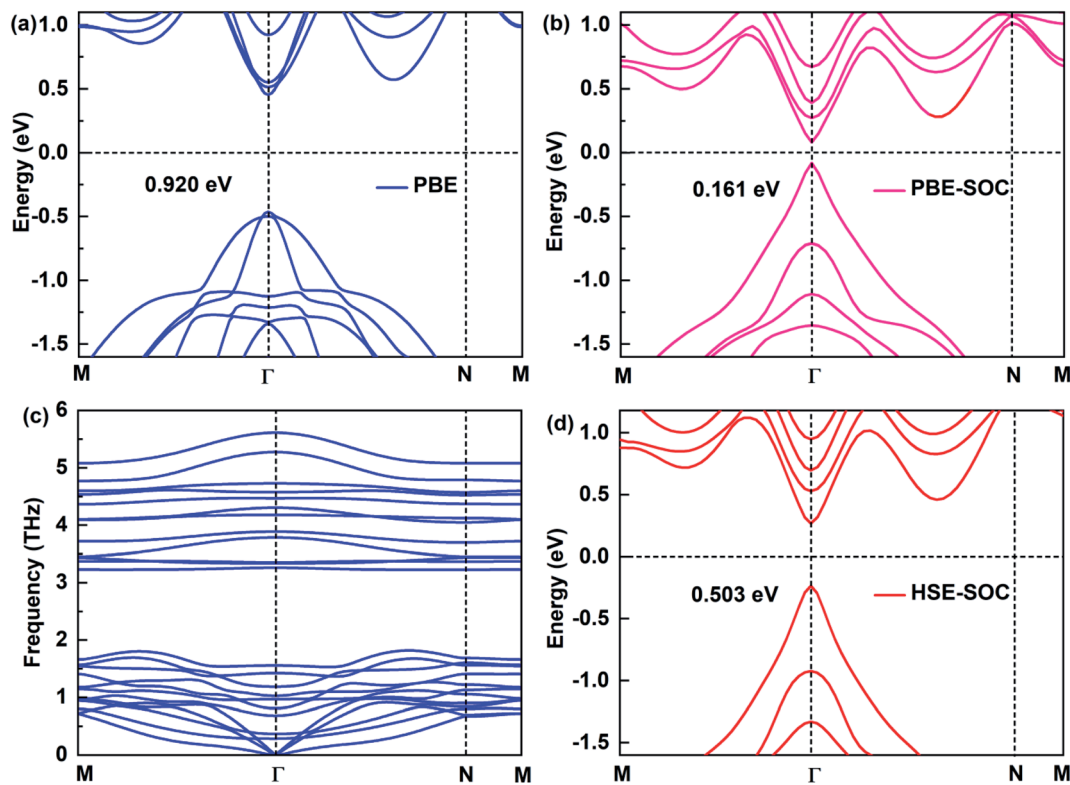


Fig. 2 Electronic structures of  $\text{Sb}_2\text{Bi}_2$  LHS by using (a) PBE, (b) PBE-SOC, (d) HSE-SOC. (c) The phonon spectra is calculated to confirm the dynamic stability of the  $\text{Sb}_2\text{Bi}_2$  LHS.

elements usually is an exothermic process. Therefore, the cohesive energy can be calculated using eqn (2):<sup>50</sup>

$$E_{\text{form}} = \frac{E_{\text{tot}} - E_{\text{Sb}} - E_{\text{Bi}}}{N} \quad (2)$$

where  $E_{\text{Sb}}$  solid and  $E_{\text{Bi}}$  are the total energy of antimonene and bismuthene, respectively;  $N$  denote the total atomic number of the system. Thus the formation energy of  $\text{Sb}_m\text{Bi}_n$  LHS is calculated about  $-3.35$  eV per atom. It is worth noting here that negative value means that the  $\text{Sb}_m\text{Bi}_n$  LHS should be energetically favorable in experimental viability.

### 3.3 Work function and charge density analysis

The work function is an important physical parameter in studying on the band alignment and charge transfer of semiconductor heterostructure. The work function is numerically equal to the difference between vacuum and Fermi levels and is expressed as follows:

$$\Phi = E_{\text{vac}} - E_{\text{fermi}} \quad (3)$$

where  $\Phi$ ,  $E_{\text{vac}}$ , and  $E_{\text{fermi}}$  denote work function, vacuum level, and Fermi level, respectively. The work function of antimonene

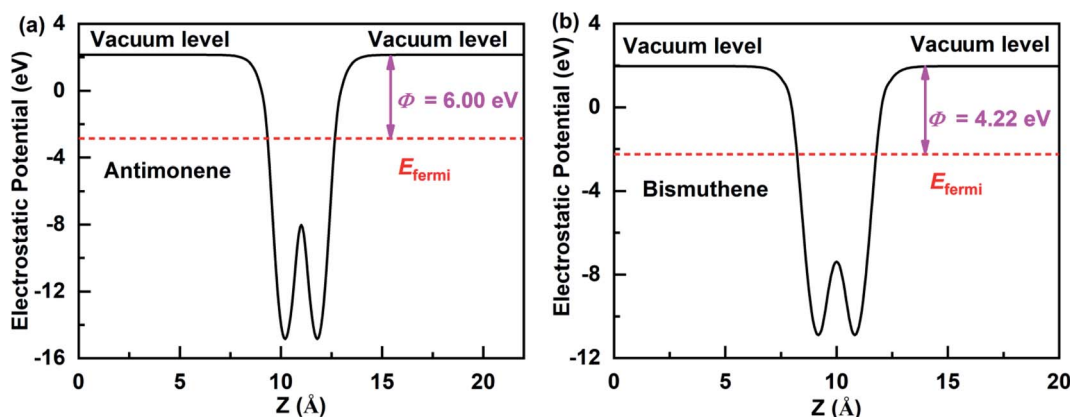


Fig. 3 Electrostatic potentials of the antimonene surface and bismuthene surface using HSE hybrid functional.





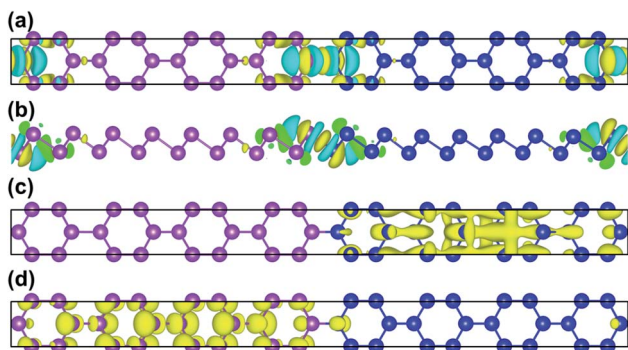


Fig. 4 (a) The top and (b) side views of charge density difference configurations of  $\text{Sb}_8\text{Bi}_8$  LHS; (c) VBM and (d) CBM of  $\text{Sb}_8\text{Bi}_8$  LHS for the band structure at the  $\Gamma$ -point, and positive and negative charges are represented in yellow and cyan, respectively.

and bismuthene could be obtained by calculating the electrostatic potential of their slab models. Fig. 3(a) and (b) shows the electrostatic potential of antimonene and bismuthene are calculated using HSE hybrid functional with work function 6.00 eV and 4.22 eV, respectively. The work function of the bismuthene was less than that of the antimonene. As a result,

when the bismuthene were interacted with the antimonene to form the  $\text{Sb}_m\text{Bi}_n$  LHS, the electrons would flow from the bismuthene to the antimonene until they reached the same Fermi levels. The antimonene and bismuthene became charged because of the electron transfer and a built-in electric field was formed at their heterointerface. The direction of the electric field is from the bismuthene to the antimonene.

To further illustrate the charge transfer between antimonene and bismuthene, we have estimated the charge density difference of  $\text{Sb}_8\text{Bi}_8$  LHS in detail. The charge density difference can be calculated as follows:

$$\Delta\rho = \rho_{\text{tot}} - \rho_{\text{Sb}} - \rho_{\text{Bi}} \quad (4)$$

where  $\rho_{\text{tot}}$ ,  $\rho_{\text{Sb}}$ , and  $\rho_{\text{Bi}}$  denote the total charge densities of  $\text{Sb}_8\text{Bi}_8$  LHS, monolayer antimonene and bismuthene nanosheet, respectively. The charge density difference of  $\text{Sb}_8\text{Bi}_8$  LHS is illustrated in Fig. 4(a) and (b). The yellow area represents electron accumulation, and the cyan area shows the electron depletion. At the heterointerfaces of  $\text{Sb}_8\text{Bi}_8$  LHS, the electron accumulation between Sb atom and Bi atom denote that a covalent bonding is formed. Besides, the calculated band decomposed charge density of the VBM and CBM is plotted in Fig. 4(c) and (d). We can see that the VBM and CBM distribute

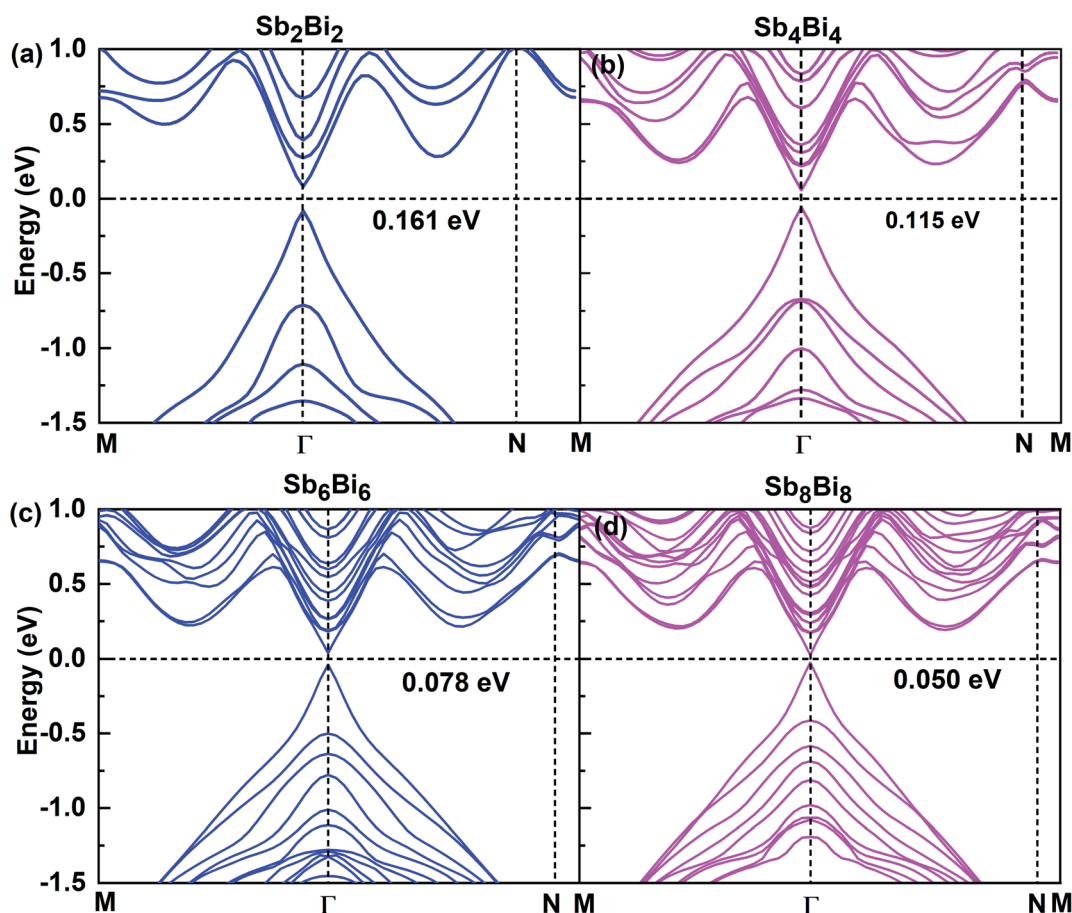


Fig. 5 Band structures for different atomic configurations of (a)  $\text{Sb}_2\text{Bi}_2$  LHS, (b)  $\text{Sb}_4\text{Bi}_4$  LHS, (c)  $\text{Sb}_6\text{Bi}_6$  LHS and (d)  $\text{Sb}_8\text{Bi}_8$  LHS using PBE + SOC method.



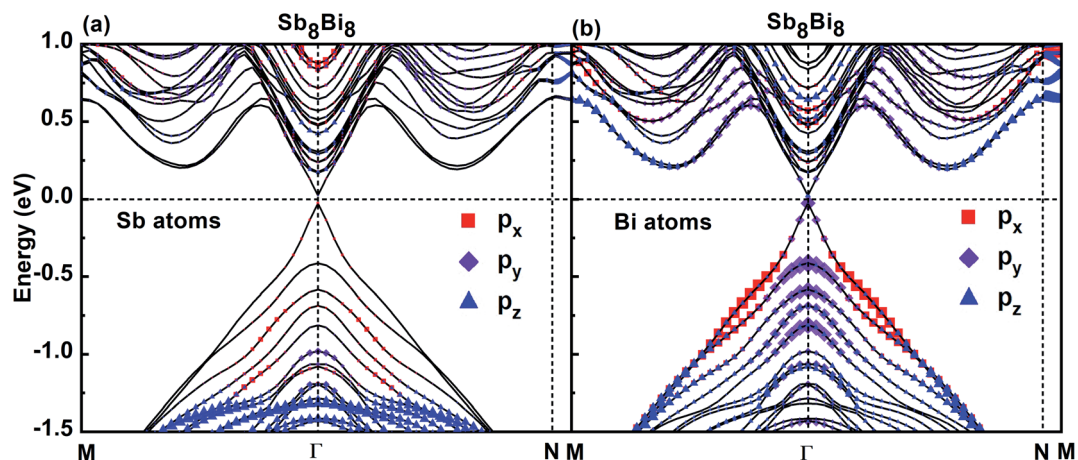


Fig. 6 Orbital-projected band structures of  $p_x$ ,  $p_y$ ,  $p_z$  orbitals of Sb and Bi atoms of  $\text{Sb}_8\text{Bi}_8$  LHS using PBE + SOC method. The size of red squares, purple diamonds and blue triangles represent the weights of  $p_x$ ,  $p_y$ ,  $p_z$  orbitals, respectively.

on opposite sides of the heterointerfaces, verifying that  $\text{Sb}_m\text{Bi}_n$  LHS is the type-II. The type-II band alignment could also be the reason for the transition from indirect to direct semiconductor.

### 3.4 Dirac cone and orbital-projected bands

After confirming the structural stability of  $\text{Sb}_m\text{Bi}_n$  LHS, we now focus on their electronic structure and optical properties. The

electronic structures of  $\text{Sb}_m\text{Bi}_n$  LHS ( $m = n$ ) are shown in Fig. 5. Notably, the electronic structure transform from indirect band gap of the pristine structure (antimonene and bismuthene) to direct band gap of  $\text{Sb}_m\text{Bi}_n$  LHS. Such a change is attributed to the fact that the lateral heterojunction destroys the pristine structural symmetry and built-in electric field in formed at the heterointerfaces. When  $m = n$ ,  $\text{Sb}_m\text{Bi}_n$  LHS are Dirac materials

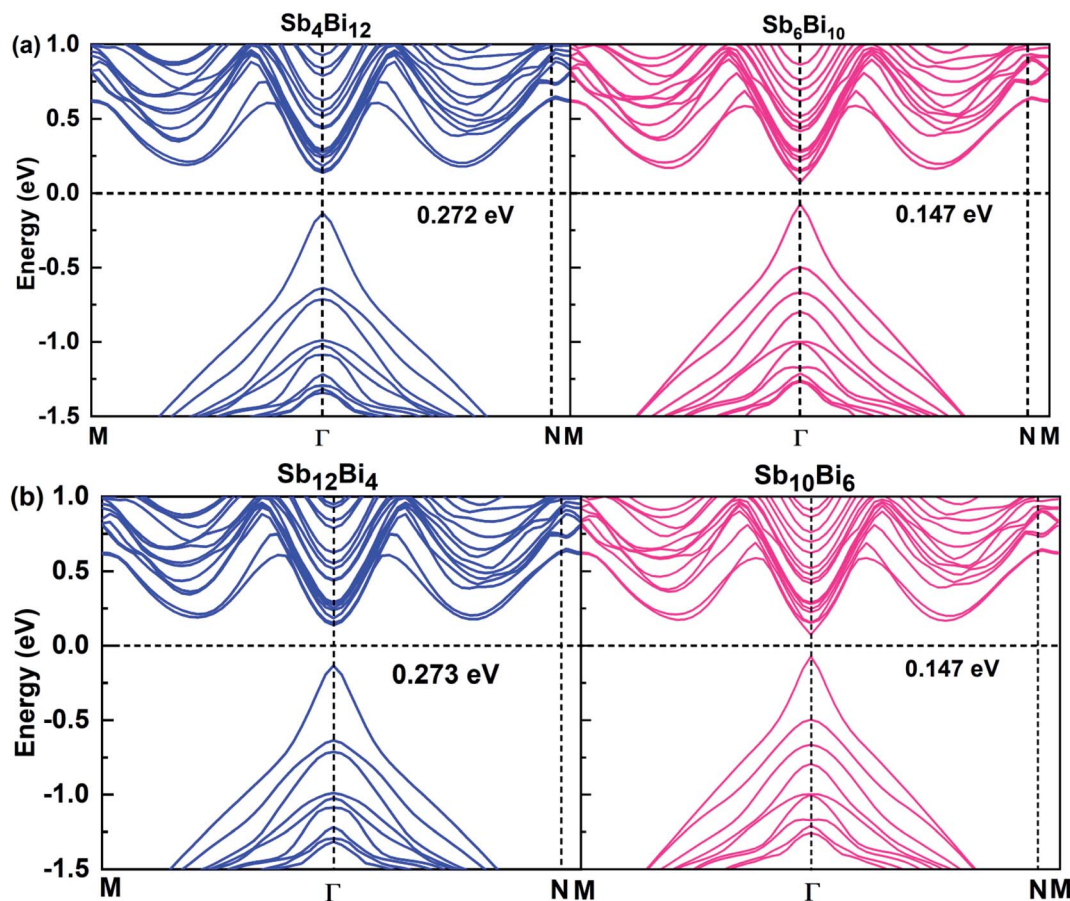


Fig. 7 Band structures of (a)  $\text{Sb}_4\text{Bi}_{12}$  LHS (left) and  $\text{Sb}_6\text{Bi}_{10}$  LHS (right), (b)  $\text{Sb}_{12}\text{Bi}_4$  LHS (left) and  $\text{Sb}_{10}\text{Bi}_6$  LHS (right) using PBE + SOC method.



and their band gaps gradually decrease with their size increasing, which intrinsically corresponds to a semiconductor-to-semimetal transition. It is well known that Dirac materials have extraordinary properties and numerous potential applications, most of which are closely related to the ultra-high carrier mobility.<sup>51–53</sup> In particular, the Dirac fermions in graphene lead to quantum Hall effect<sup>54</sup> and ultra-high carrier mobility, which is as high as  $2 \times 10^5 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  at room temperature.<sup>55,56</sup> Dirac materials, characterized by linear band dispersion at the Fermi level, are at the heart of several unconventional phenomena such as realization of extremely high free carrier mobility and quantum Hall effect, which indicates their immense potential for the development of nanoelectronic devices. Besides, type-II band alignment can be observed in  $\text{Sb}_m\text{Bi}_n$  LHS because VBM state is mainly derived from antimonene and CBM from bismuthene. Further, similar results have been reported for the  $\text{MoS}_2/\text{WSe}_2$  (ref. 57) LHS and  $\text{As/Sb}$ <sup>58</sup> LHS. The above results open a new route toward the integration of Dirac physics, spintronics, and valleytronics.

To investigate the band characteristics of  $\text{Sb}_m\text{Bi}_n$  LHS, the orbital-projected band structures of Sb and Bi atoms in  $\text{Sb}_8\text{Bi}_8$  LHS are displayed in Fig. 6(a) and (b), respectively. The size of red squares, purple diamonds and blue triangles represent the weights of  $p_x$ ,  $p_y$ ,  $p_z$  orbitals of Sb atoms and Bi atoms of  $\text{Sb}_8\text{Bi}_8$  LHS, respectively. It is clear from Fig. 6(a) and (b) that both VBM and CBM appear at the  $\Gamma$  point, resulting in a direct band gap of 0.05 eV according to DFT calculations. Because the s-orbital of Sb and Bi atoms is an inner orbital relative to p-orbital, it makes little contribution to the electronic structure near the Fermi level. Consequently, the p-orbital govern the electronic structure of  $\text{Sb}_m\text{Bi}_n$  LHS near the Fermi level. Further analysis shows that the bonding states near VBM and CBM mainly originate from Bi- $p_y$  orbitals (seen in Fig. 6(b)), while the Sb-p orbitals hardly impacts the electronic structure of the LHS (seen in Fig. 6(a)). Therefore, it is reasonable to ignore the effect of the orbitals of Sb atoms on the band structures of  $\text{Sb}_m\text{Bi}_n$  LHS. These results provide useful insights on the electronic structure of  $\text{Sb}_m\text{Bi}_n$  LHS.

### 3.5 Band structure and size dependence

When  $m = n$ , we have confirmed that  $\text{Sb}_m\text{Bi}_n$  LHS are Dirac materials with symmetric structures. When  $m \neq n$ ,  $\text{Sb}_m\text{Bi}_n$  LHS

including  $\text{Sb}_4\text{Bi}_{12}$ ,  $\text{Sb}_6\text{Bi}_{10}$ ,  $\text{Sb}_{10}\text{Bi}_6$ , and  $\text{Sb}_{12}\text{Bi}_4$  are asymmetric structures and the corresponding electronic structures are shown in Fig. 7. All these LHS retain a recognizable direct band gap near the Fermi level. However, compared to the symmetric  $\text{Sb}_m\text{Bi}_n$  LHS, the electronic structures of asymmetric  $\text{Sb}_4\text{Bi}_{12}$  LHS and  $\text{Sb}_{12}\text{Bi}_4$  LHS transform from Dirac semimetal to semiconductor. This is mainly because the built-in electric field at the heterointerfaces of the asymmetric structure changes the mechanism of electron transport. Thus, we have demonstrated that  $\text{Sb}_m\text{Bi}_n$  LHS can maintain the Dirac semimetallic character only if the condition  $m \approx n$  is satisfied, and the corresponding histogram is shown in Fig. 8(a). Besides, the band gaps of the  $\text{Sb}_m\text{Bi}_n$  LHS exhibit size dependence, which is illustrated in Fig. 8(b). It is clear that the band gap of  $\text{Sb}_m\text{Bi}_n$  LHS tends to zero when the size is larger than a critical value, which essentially corresponds to the transition from semiconductor to semimetal. We believe that these excellent properties of  $\text{Sb}_m\text{Bi}_n$  LHS will inspire researchers to synthesize them.

### 3.6 Strain dependence of LHS

The application of an appropriate tensile strain is another effective method to tune the band structures of 2D materials, its effectiveness has been demonstrated on respectively. The size of red squares, purple diamonds and antimonene, which is an important member of  $\text{Sb}_m\text{Bi}_n$  LHS. The antimonene can endure a large tensile strain up to 18%, and its band gap decreases with the tensile strain increasing,<sup>59</sup> which causes the realization of QSHE. It is well established that for large tensile strain, the strong covalent interaction in the plane of LHS ensures their structural stability. As a result,  $\text{Sb}_m\text{Bi}_n$  LHS can also endure large tensile strain. The strain dependence of the electronic structure of  $\text{Sb}_2\text{Bi}_2$  LHS within 0–14% tensile strain is shown in Fig. 9. We have considered the tensile strain along three different directions: X-axis, Y-axis, and XY-axis. The analysis for the first case indicates that when the tensile strain is 0–6%, CBM and VBM are continuously shifted toward the Fermi level with the tensile strain increasing, resulting in band gap narrowing. When the tensile strain is greater than 6%, there is a Dirac cone near Fermi level. The application of strain@Y-axis and strain@XY-axis causes a similar response, which is illustrated in Fig. 9(b) and (c), respectively. Further, we observed that

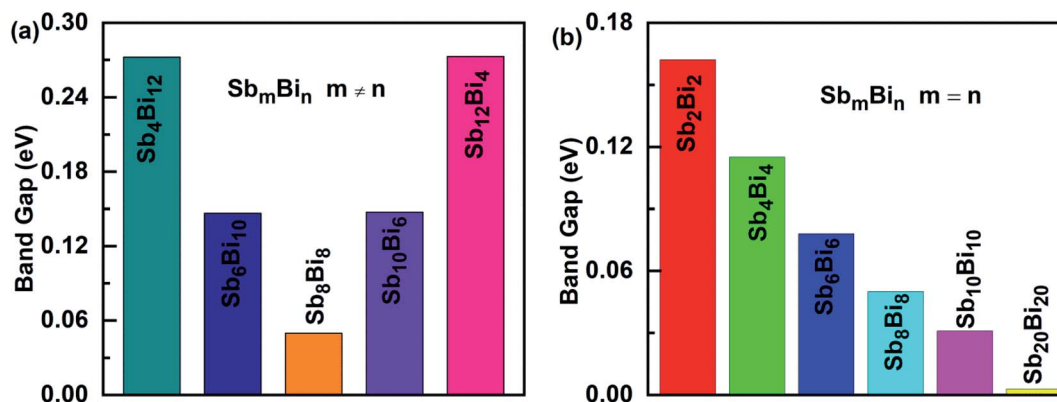


Fig. 8 Band alignments of (a)  $\text{Sb}_m\text{Bi}_n$  LHS ( $m \neq n$ ), (b)  $\text{Sb}_m\text{Bi}_n$  LHS ( $m = n$ ). The band alignments of all systems belong to type II.





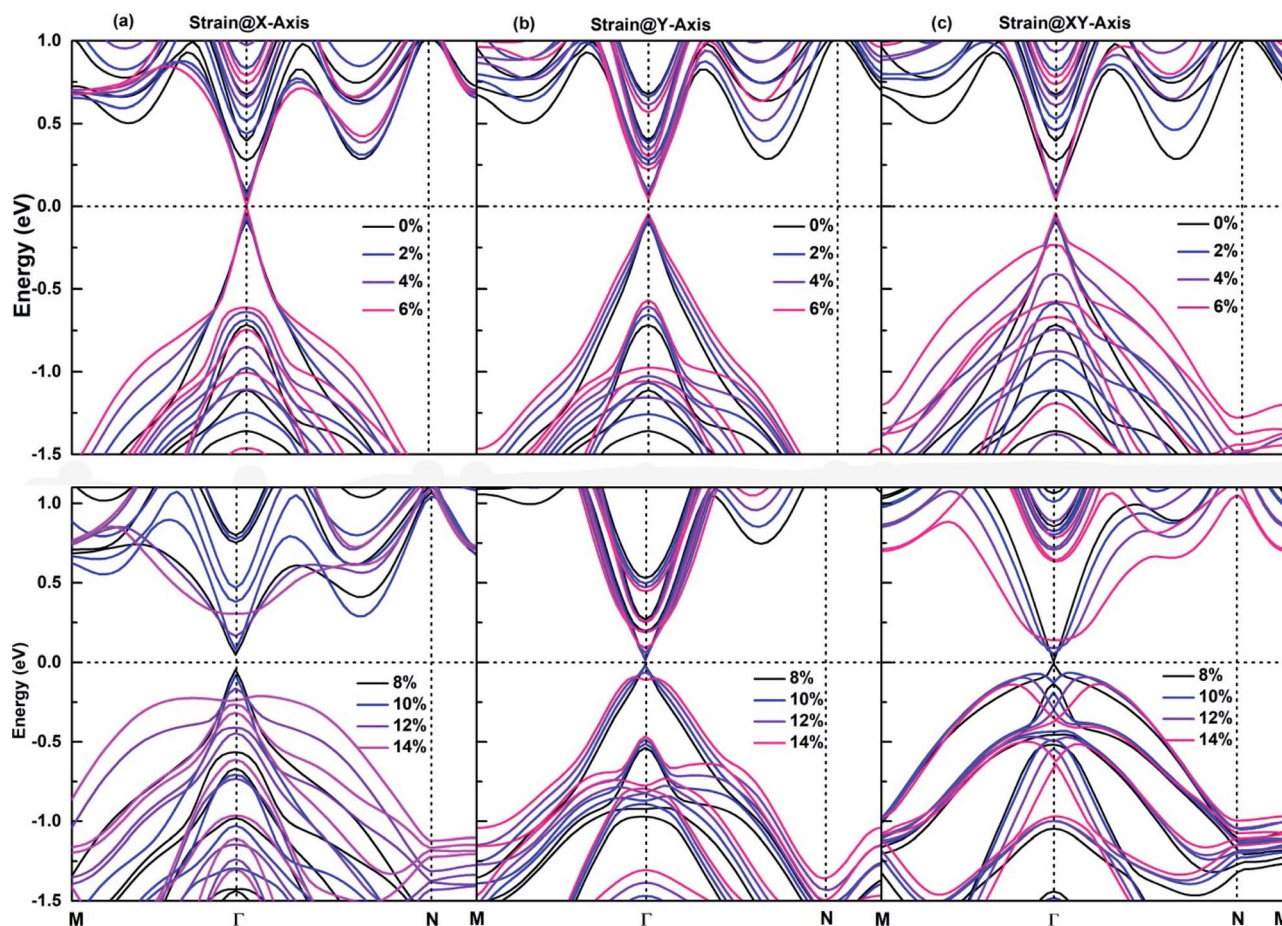


Fig. 9 The strain dependence along three different directions of (a) X-axis, (b) Y-axis, and (c) XY-axis on the band structures of  $\text{Sb}_2\text{Bi}_2$  LHS using PBE + SOC method.

the electronic structures below the Fermi level significantly change with the tensile strain increasing. The electronic structures corresponding to the case of strain@XY-axis exhibit two separate strain dependences, but the influence of strain@X-axis is dominant. Nevertheless, it is worth noting that the band structure seems to be reversed when the tensile strain is applied along three different directions.

According to Fig. 6, the bonding states near VBM and CBM mainly originate from Bi- $p_y$  orbitals, while the Sb-p orbital character of bands hardly impact the electronic structure of  $\text{Sb}_m\text{Bi}_n$  LHS. The orbital-projected band structures are suitable for investigating the strain dependence of the electronic structure of  $\text{Sb}_m\text{Bi}_n$  LHS. The orbital-projected band structure for strain@X-axis of  $\text{Sb}_2\text{Bi}_2$  LHS is illustrated in Fig. 10(a) and (b). It is clear that when the tensile strain reaches 2% (seen in Fig. 10(a)), the valence band near the Fermi level includes Bi- $p_y$  orbitals. When the tensile strain reaches 6%,  $\text{Sb}_2\text{Bi}_2$  LHS exhibits Dirac semimetallic properties and VBM and CBM touch each other. When the tensile strain is greater than 6% (seen in Fig. 10(b)), the contribution of the Bi- $p_y$  orbitals stays in the conduction band. Afterwards, the band gaps increase gradually with the tensile strain increasing and the band inversion occurs near  $\Gamma$  point. Similarly, the orbital-projected band structures for

strain@Y-axis and strain@XY-axis of  $\text{Sb}_2\text{Bi}_2$  LHS exhibit band inversion at the  $\Gamma$  point, which is illustrated in ESI, Fig. S1 and S2.<sup>†</sup> However, the difference between the two cases is that the contribution of the Bi- $p_x$  orbitals and Bi- $p_z$  orbitals stays in the conduction band when the tensile strain is applied along the Y-axis and XY-axis, respectively. The band inversion indicates that  $\text{Sb}_m\text{Bi}_n$  LHS are promising to realize QSHE.

### 3.7 The concentration analysis

In order to clarify the relationship between the electronic performances of  $\text{Sb}_2\text{Bi}_2$  LHS and the tensile strain, we have calculated the concentration of the electron and hole in different tensile strain, which is illustrated in Fig. 11. The electron concentration of all lateral heterojunctions remain a value with  $7.66 \text{ nm}^{-3}$  and that of the hole concentration remain a value with  $8.07 \text{ nm}^{-3}$ , when the  $\text{Sb}_m\text{Bi}_n$  LHS are not subjected to tensile strain in any direction. However, once the  $\text{Sb}_m\text{Bi}_n$  LHS is subjected to tensile strain with different direction, the electrons in the valence band transfer to the conduction band. With the increase of tensile strain, the electron concentration decreases (seen in Fig. 11(a)), but the hole concentration increases (seen in Fig. 11(b)), because the total number of the electron and hole does not varies with the tensile





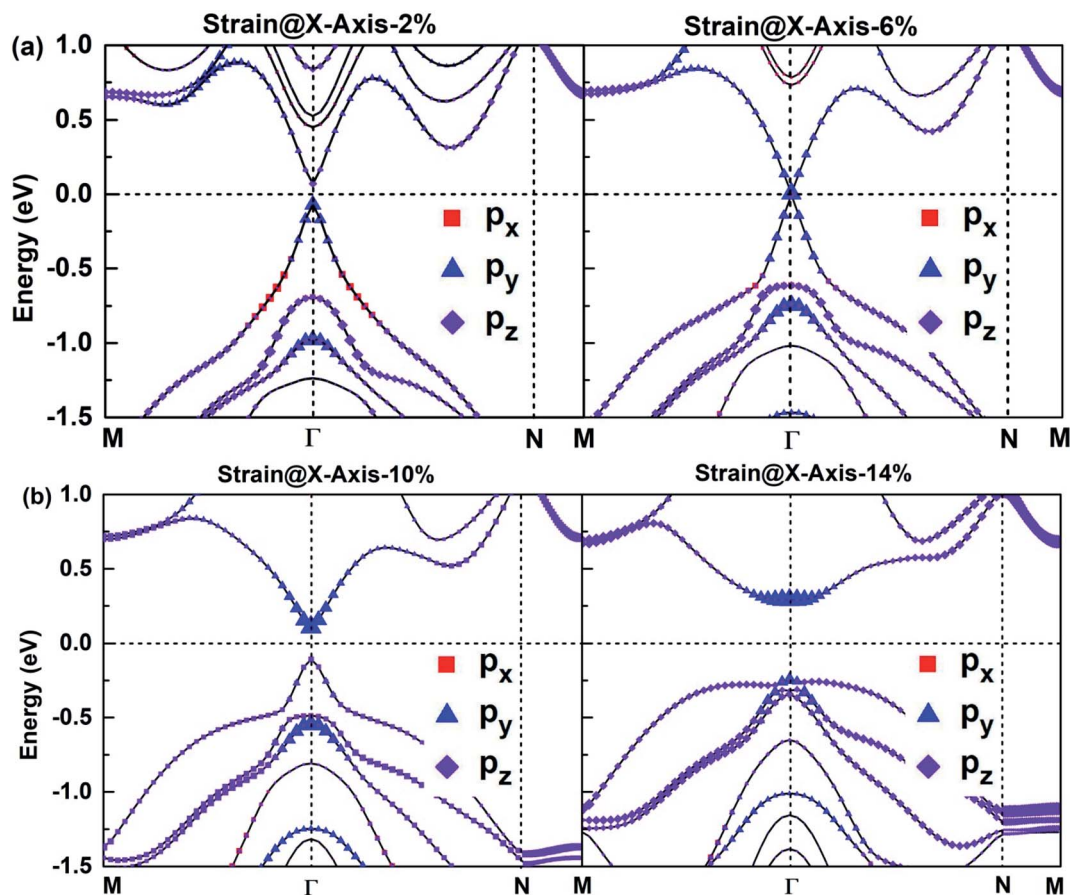


Fig. 10 The orbital-projected band structures of strain@X-axis of Bi atoms of  $\text{Sb}_2\text{Bi}_2$  LHS using PBE + SOC method. The size of red squares, purple diamonds and blue triangles represent the weights of  $p_x$ ,  $p_y$ ,  $p_z$  orbitals, respectively.

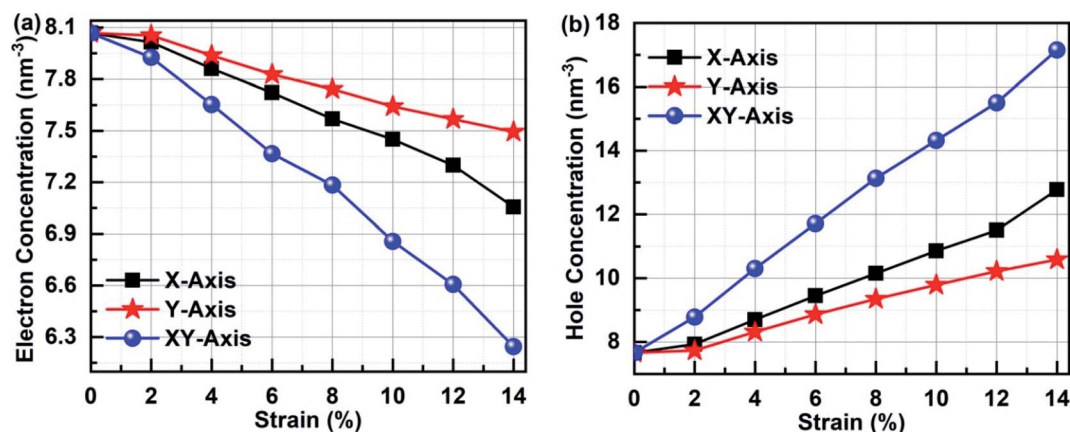


Fig. 11 (a) Electron concentration and (b) hole concentration of  $\text{Sb}_2\text{Bi}_2$  LHS in the tensile strain with different direction.

strain. On the other hand, the variation relationship of the electron concentration and the hole concentration is  $\text{XY-axis} > \text{X-axis} > \text{Y-axis}$ , denoting that there are more the electron hole pair in  $\text{Sb}_2\text{Bi}_2$  LHS in XY-axis strain than X-axis and Y-axis strain.

## 4. Conclusions

In this review, we systematically investigate  $\text{Sb}_m\text{Bi}_n$  LHS and found that an abrupt transition from indirect-band gap of the antimonene and bismuthene to direct-band gap of  $\text{Sb}_m\text{Bi}_n$  LHS is observed.  $\text{Sb}_m\text{Bi}_n$  LHS exhibit a type-II band alignment, which is potentially useful for future photoelectronics. Additionally, the size of  $\text{Sb}_m\text{Bi}_n$  LHS is observed to be a key parameter that

governed their electronic structures and optical properties. The band gaps of  $\text{Sb}_m\text{Bi}_n$  LHS tend to zero when their size is larger than the critical value, which essentially corresponds to a transition from semiconductor to semimetal. Besides, the tensile strain accelerate the electrons in the valence band transfer to the conduction band, leading to the electron concentration decreases and the hole concentration increases with tensile strain increases. The band inversion near  $\Gamma$  point occurs on suitable strain, indicating that  $\text{Sb}_m\text{Bi}_n$  LHS are very promising to realize QSHE. These fascinating electronic and optical properties make it extensively used in the fields of electronics, optoelectronics and other fields.

## Conflicts of interest

The authors declare there is no conflicts of interest regarding the publication of this paper.

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