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# Nitrogen *versus* carbon in planar pentacoordinate environments supported by $\text{Be}_5\text{H}_n$ rings†

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$\text{NBe}_5\text{H}_n^{n-3}$  ( $n = 0-5$ ) (**0A-5A**) species with a novel planar pentacoordinate nitrogen (ppN) were designed by the isoelectronic substitution of the C atom in planar pentacoordinate carbon (ppC) species  $\text{CBe}_5\text{H}_n^{n-4}$  ( $n = 0-5$ ) with an N atom. The highly flexible H atoms found in ppC species  $\text{CBe}_5\text{H}_2^{2-}$  and  $\text{CBe}_5\text{H}_3^-$  were fixed upon the nitrogen substitution, as mirrored by the non-flexible H atoms in their ppN analogues  $\text{NBe}_5\text{H}_2^-$  (**2A**) and  $\text{NBe}_5\text{H}_3$  (**3A**). Moreover, the N atom was found to fit the H-surrounded  $\text{Be}_5$  rings better than the C atom because the ppC species  $\text{CBe}_5\text{H}_4$  and  $\text{CBe}_5\text{H}_5^+$  adopted non-planar structures due to size-mismatch between the C atom and the H-surrounded  $\text{Be}_5$  ring, but their ppN analogues  $\text{NBe}_5\text{H}_4^+$  (**4A**) and  $\text{NBe}_5\text{H}_5^{2+}$  (**5A**) adopted perfect planar structures. The electronic structure analyses revealed that the N atoms in **0A-5A** were involved in four doubly occupied orbitals, including three six-center two-electron (6c-2e)  $\sigma$  bonds and one 6c-2e  $\pi$  bond. Therefore, these ppN species not only obey the octet rule, but also possess the interesting  $\sigma$  and  $\pi$  double aromaticity, which contributes to the stabilization. Consequently, **2A**, **4A**, and **5A** are charged kinetically viable global energy minima, and are suitable for the gas phase generation and spectroscopic characterization.

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## Introduction

In general, a typical main group nonmetal can have the maximum number of four closely connected atoms and they often adopt a tetrahedral arrangement as suggested by the van't Hoff/Le Bel rule. Therefore, planar pentacoordination is especially interesting in that it violates both the highest number and the suggested arrangement of closely connected atoms. Such a non-classical bonding has mainly been observed, heretofore, in the planar pentacoordinate carbon<sup>1</sup> (ppC) species. Note that though ppC stemmed from the planar tetra-<sup>2</sup> and hexacoordinate carbon<sup>3</sup> (ptC and p6C), it played a more important role in planar carbon chemistry recently because a dozen ppC species were found to be the global energy minima (GEM),<sup>1b,4</sup> suitable for experimental realization. To our knowledge, the ppC GEMs represent more than half of known GEM planar carbon species. Their GEM nature may be the result of geometric and

electronic good fitting between C atom and five-membered rings. However, exceptions can be found in the  $\text{CBe}_5\text{H}_n^{n-4}$  ( $n = 2-5$ ) system (see Fig. S1 in ESI†), where  $\text{CBe}_5\text{H}_4$  and  $\text{CBe}_5\text{H}_5^+$  species are non-planar, suggesting that carbon is too big to stay at the center of  $\text{Be}_5\text{H}_4$  and  $\text{Be}_5\text{H}_5$  rings preferentially.<sup>5</sup>

As the heavier neighbor of carbon, nitrogen has rich chemistry, too. In particular, many non-classical bonding patterns of carbon had been extended to nitrogen.<sup>6</sup> For instance, the planar tetracoordinate nitrogen (ptN) had been observed in  $\text{NSiAl}_3$ ,  $\text{NAL}_4/\text{NAL}_4^-$ ,  $\text{NM}_4\text{H}_4^+$  ( $\text{M} = \text{Cu}, \text{Ni}$ ),  $\text{NXAl}_3^+$  ( $\text{X} = \text{N}, \text{P}, \text{As}$ ), *etc.*<sup>7</sup> Noticeably, the higher electronegativity of nitrogen than that of carbon leads to the higher preference for the localized bonding, which is unbeneficial to the design of planar hypercoordinate nitrogen species. Nevertheless, Ding *et al.* proposed and demonstrated that this bonding preference could be utilized to design the ptC and ptN species.<sup>7d,8</sup>

Nonetheless, the planar pentacoordinate nitrogen (ppN) was less familiar to chemists. To the best of our knowledge, two ppN species ( $\text{NCu}_5\text{H}_5^+$  and  $\text{NBe}_5\text{Au}_5^{2+}$ )<sup>9,10</sup> had been reported, but none of them were convincingly demonstrated to be the GEM, which lowers their possibility to be observed in the experiments. Can a ppN species be a GEM and what is the difference between ppN and ppC species possessing the similar geometrical skeletons? Through design and characterization of the ppN species  $\text{NBe}_5\text{H}_n^{n-3}$  ( $n = 0-5$ ) by substituting the C atom in  $\text{CBe}_5\text{H}_n^{n-4}$  ( $n = 0-5$ )<sup>5</sup> with N atom, we reported in the present work the first examples of the GEM ppN species. Simultaneously, we found that nitrogen fits more nicely with the  $\text{Be}_5\text{H}_n$  rings than carbon and

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† Electronic supplementary information (ESI) available: Optimized structures of  $\text{CBe}_5\text{H}_n^{n-4}$  ( $n = 2-5$ ), the results of ELF analysis for **2A-5A**, optimized structures and the relative energies of **1A-5A** and their four lowest isomers, the five independent 20 ps BOMD simulations of **2A-5A** at 500 K, the energy profile for the generation of **4C** from **4A**, and Cartesian coordinates for the species reported in this work. See DOI: 10.1039/d1ra02178h



the nitrogen substitution for the carbon atom in ppC species  $\text{CBe}_5\text{H}_2^{2-}$  and  $\text{CBe}_5\text{H}_3^-$  can fix the highly flexible H atoms.

## Computational methods

For ppN species  $\text{NBe}_5\text{H}_n^{n-3}$  ( $n = 0-5$ ) (**0A-5A**), the geometry optimization and harmonic vibrational frequency analysis were performed at the B3LYP/aug-cc-pVTZ level. The B3LYP functional was calibrated using *ab initio* calculations at the MP2/aug-cc-pVTZ level, which gave the optimized structures of **1A-5A** not different in essential from those optimized using B3LYP functional, suggesting that it is safe to use B3LYP to study the current system. To better understand the electronic structures, the natural bond orbital (NBO)<sup>11</sup> and the adaptive natural density partitioning (AdNDP)<sup>12</sup> were analyzed at the B3LYP/aug-cc-pVTZ and B3LYP/6-31G levels, respectively. As an extension of NBO analysis, AdNDP shows the electronic structure of a molecular system in terms of  $n$ -center two-electron ( $nc$ -2e) bonds ( $n$  ranges from one to total number of atoms in the molecule). Thus, AdNDP recovers not only the Lewis elements (lone pairs and  $2c$ -2e bonds), but also the delocalized  $nc$ -2e bonds. To assess the aromaticity, the electron localization function (ELF)<sup>13</sup> and the nucleus-independent chemical shifts (NICS)<sup>14</sup> analyses were carried out at the B3LYP/aug-cc-pVTZ level. To assess the thermodynamic stability of the design ppN species, the potential energy surfaces (PESs) of  $\text{NBe}_5\text{H}_n^{n-3}$  ( $n = 1-5$ ) components were explored by the stochastic search algorithm.<sup>15</sup> Note that both singlet and triplet surfaces were considered in the PES explorations. The generated random structures were initially optimized at the B3LYP/6-31G(d) level. Then, ten identified lowest isomers were re-optimized at the B3LYP/aug-cc-pVTZ level. The energies were further improved at the CCSD(T)/aug-cc-pVTZ level based on the B3LYP/aug-cc-pVTZ optimized geometries. The relative energies of the isomers were compared at the CCSD(T)//B3LYP level, where CCSD(T)//B3LYP

denoted the sum of CCSD(T)/aug-cc-pVTZ single point energy and B3LYP/aug-cc-pVTZ zero-point energy correction. To evaluate the kinetic stability, the Born-Oppenheimer molecular dynamic (BOMD)<sup>16</sup> simulations were run at the B3LYP/6-31G(d) level and concerned temperatures, including 4, 298, and 500 K. The simulations were performed adiabatically, the initial velocity was not fixed but related to the temperatures considered, and the Hessian was recalculated every 5 gradient points. The structural evolution during the simulations was evaluated by the root-mean-square deviation (RMSD) relative to the B3LYP/6-31G(d)-optimized geometries. The vertical detachment energy (VDE) and the vertical electron affinity (VEA) were calculated using the outer valence Green's function (OVGF)<sup>17</sup> at the OVGF/aug-cc-pVTZ level. The stochastic search algorithm was performed using GXYZ 2.0 program,<sup>18</sup> the AdNDP was analyzed using AdNDP program,<sup>19</sup> the CCSD(T) calculations were carried out using MolPro 2012.1,<sup>20</sup> and all other calculations were performed using the Gaussian 09 package.<sup>21</sup>

## Results and discussion

### Design of $\text{NBe}_5\text{H}_n^{n-3}$ ( $n = 0-5$ )

The ppN species  $\text{NBe}_5\text{H}_n^{n-3}$  ( $n = 0-5$ ) (**0A-5A**, see Fig. 1) could be designed simply by isoelectronic substitution of C atom in ppC species  $\text{CBe}_5\text{H}_n^{n-4}$  ( $n = 0-5$ ) with  $\text{N}^+$  cation. Note that **2A** and **3A** both have an isomer, *i.e.* **2A'** and **3A'** shown in Fig. 1, whose structural difference lies in the distribution of H atoms. According to our calculations at the CCSD(T)//B3LYP level, **2A'** and **3A'** are 10.9 and 9.5 kcal mol<sup>-1</sup> higher in energy than **2A** and **3A**, respectively, thus they are discarded in the following. As shown in Fig. 1, the energy minima **0A-5A** adopt the perfect planar structures at the B3LYP/aug-cc-pVTZ level. In particular, the planar ppN species **4A** and **5A** are in sharp contrast to their quasi-planar analogues  $\text{CBe}_5\text{H}_4$  and  $\text{CBe}_5\text{H}_5^+$ , suggesting the better match of N atom than C atom with the  $\text{Be}_5\text{H}_4$  and  $\text{Be}_5\text{H}_5$

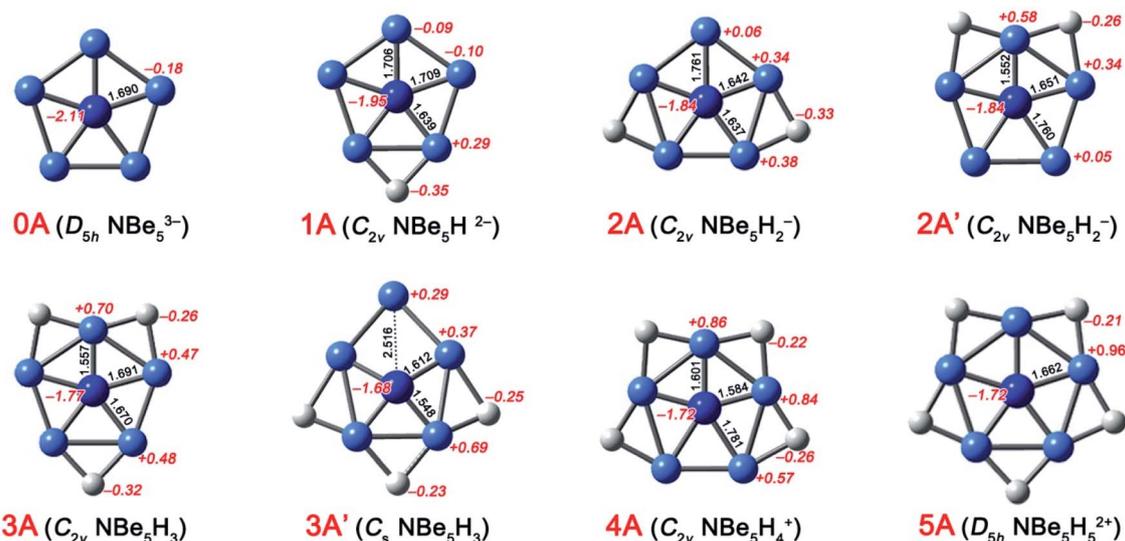


Fig. 1 Optimized structures of ppN species at the B3LYP/aug-cc-pVTZ level. Bond distances (in Å) and NBO charges (in |e|) are given in black and italic red fonts, respectively.



rings. The N–Be interatomic distances range from 1.557 to 1.781 Å in **0A–5A**, which is short enough for each Be atom to be considered as a coordination to N atom, so **0A–5A** are eligible ppN species.

### Electronic structure analyses

The chemical bonding in ppN species **0A–5A** are similar to their analogue ppC species  $\text{CBe}_5\text{H}_n^{n-4}$  ( $n = 0-5$ ). Fig. 2 shows the AdNDP view of chemical bonding in **0A–5A**. As shown in Fig. 2, for Be–Be edge without bridging H atom, there is a 2c-2e Be–Be  $\sigma$  bond with occupation numbers (ONs) ranging from 1.96 to 1.98 |e| (see the first column). Exposing such diffused metal–metal  $\sigma$  bonds may be negative to the stabilization of ppN species. In contrast, for Be–Be edge with a bridging H atom, there is a Be–H–Be three-center two-electron (3c-2e)  $\sigma$  bond (ON = 1.91–1.99 |e|, see the second column). Though such bonds involve three centers, they are less diffused than the Be–Be 2c-2e bonds, which may be positive to the stabilization from the electronic structure point of view.

As shown in Fig. 3, the advantage to possess the Be–H–Be 3c-2e bonds can be demonstrated by the increasing HOMO–LUMO gaps from 0.44 eV for  $\text{NBe}_5$  without bridging H to 7.93 eV with all Be–Be edges bridged by the H atoms. Note that the most obvious variation occurs at  $n = 4$  to  $n = 5$ , which corresponds to the complete elimination of diffused Be–Be 2c-2e bond,

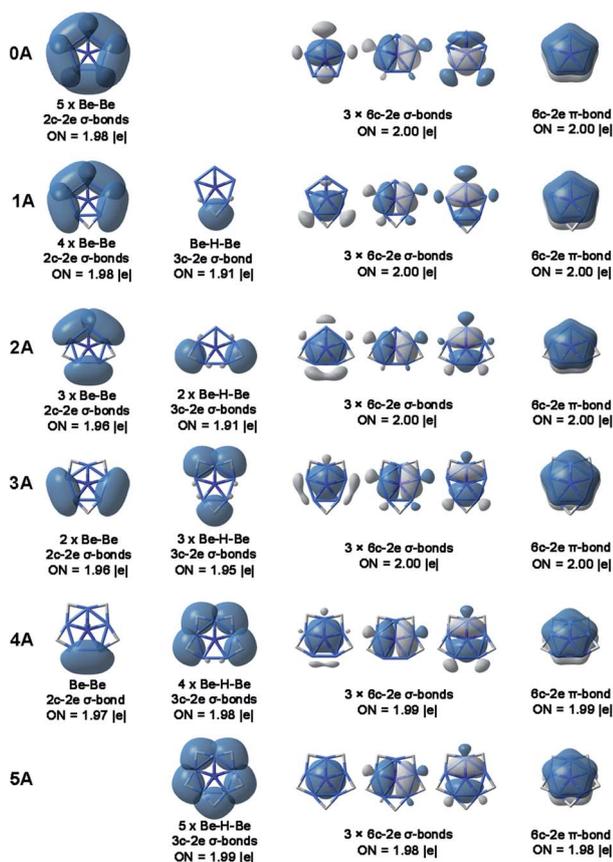


Fig. 2 AdNDP bonding patterns of **0A–5A** with occupation numbers (ONs).

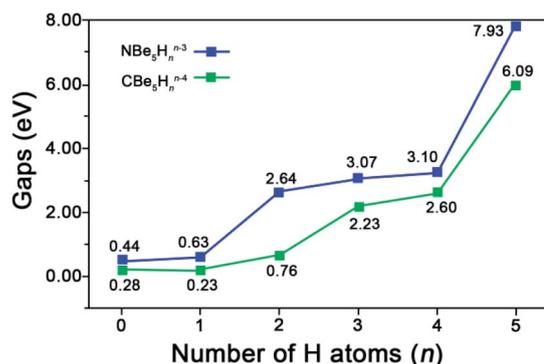


Fig. 3 Variation of HOMO–LUMO gaps (gaps, in eV) with the increasing number of H atoms ( $n$ ) in  $\text{NBe}_5\text{H}_n^{n-3}$  and  $\text{CBe}_5\text{H}_n^{n-4}$  ( $n = 0-5$ ).

verifying the beneficial effect of Be–H–Be 3c-2e bonds to the stabilization of the ppN structures. We also note that the HOMO–LUMO gaps of ppN species  $\text{NBe}_5\text{H}_n^{n-3}$  ( $n = 0-5$ ) are all higher than their analogue ppC species  $\text{CBe}_5\text{H}_n^{n-4}$  ( $n = 0-5$ ), which indicates the electronically better match of N atom than that of C atom with  $\text{Be}_5\text{H}_n$  rings.

Bonding patterns shown in the third column of Fig. 2 depict the interesting delocalized six-center two-electron (6c-2e)  $\sigma$  bonds, while those in the last column illustrate the delocalized 6c-2e  $\pi$  bonds. These four 6c-2e bonds are very similar in all  $\text{NBe}_5\text{H}_n^{n-3}$  species despite of  $n$  values and they are also similar to those of their ppC analogues  $\text{CBe}_5\text{H}_n^{n-4}$  ( $n = 0-5$ ). The existence of these four bonds builds the basis for the stabilization of ppN arrangement from the electronic structure point-of-view. First, these four bonds fill eight electrons to the valence shell of central nitrogen atoms, *i.e.* the ppN species obey the octet rule. Second, three delocalized  $\sigma$  bonds and one delocalized  $\pi$  bond meet the Hückel's  $4n+2$  rule for  $n = 1$  and 0, respectively, suggesting the novel  $6\sigma + 2\pi$  double aromaticity.

The aromaticity within  $\text{NBe}_5$  moieties of **2A–5A** was evaluated using ELF analysis. As shown in Fig. S2,<sup>†</sup> the bifurcation values for  $\sigma$  bonding ( $\text{ELF}_\sigma$ ) range from 0.936 to 0.944, while that for  $\pi$  bonding ( $\text{ELF}_\pi$ ) are all 0.999, thus giving the average bifurcation values ( $\text{ELF}_{\text{av}}$ ) from 0.968 to 0.972. Since the  $\text{ELF}_\sigma$ ,  $\text{ELF}_\pi$  and  $\text{ELF}_{\text{av}}$  values are all much larger than 0.7, the threshold value for ELF criterion of aromaticity judgement,<sup>13,22</sup> the ppN species **2A–5A** should be the  $\sigma$ ,  $\pi$  and overall aromatic molecules.

Taking **5A** as an example, we studied aromaticity by performing the NICS analysis. As shown in Fig. 4, the NICS values for almost all the examined points near the molecule are obviously negative, suggesting aromatic nature for **5A**. An exception with the positive NICS value of +3.7 ppm can be found at the point located 0.5 Å above the beryllium atom, but it does not influence the aromatic nature of **5A** as a whole. Note that the points with largest negative NICS values (–52.9 and –21.4 ppm) locate 0.5 and 1.0 Å above the nitrogen atom, suggesting the  $\pi$  electron delocalization, while the points with the second largest negative NICS values (–18.8 and –16.1 ppm) locate in the molecular plane within  $\text{Be}_5$  ring, indicating the  $\sigma$  electron





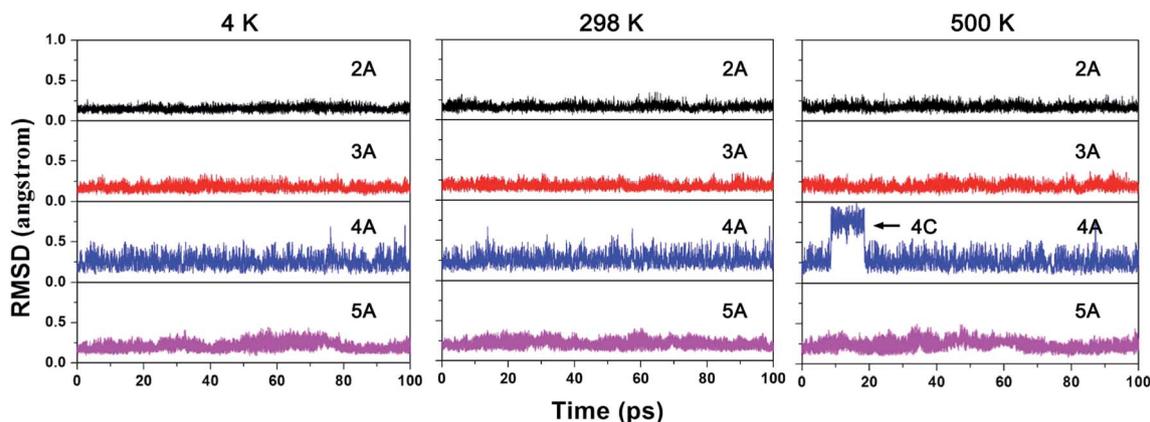


Fig. 5 The RMSD plots for the BOMD simulations of 2A–5A at 4 K, 298 K and 500 K from left to right, respectively.

ppN, the flexibility of H atoms disappeared, as reflected by the RMSD plots of 2A and 3A without upward jump. Simultaneously, 4A and 5A inherit the good kinetic stability of  $\text{CBe}_5\text{H}_4$  and  $\text{CBe}_5\text{H}_5^+$ . Therefore, the dynamic simulations not only demonstrated the good kinetic viability of 2A–5A, but also revealed that the N-substitution can fix the highly flexible H atoms found in  $\text{CBe}_5\text{H}_2^{2-}$  and  $\text{CBe}_5\text{H}_3^-$ .

### Stability about gaining and losing electron

To evaluate the electron-gaining and losing properties, the VDEs and VEAs of 2A–5A were calculated. The VDE for mono-anion 2A is 2.52 eV, which is reasonably high for photoelectron spectroscopy, while the VEA of 2A is positive, suggesting the endothermic electron-gaining process for 2A. For neutral molecule 3A, the VDE and VEA values are 7.10 and 0.22 eV, respectively, revealing its low tendency to lose or gain an electron. For mono-cation 4A, it would be very difficult to lose an electron due to the rather high VDE of 11.93 eV and it would be not easy to gain an electron, as reflected by the VEA value (−4.41 eV) close to  $\text{K}^+$  cation (−4.34 eV). For dication 5A, it is not curious that the VDE is as high as 22.35 eV. However, its VEA value of −9.23 eV is actually very low, being lower than the VEA of  $\text{Ba}^{2+}$  (−10.00 eV, the lowest VEA value for any atomic dication in the Periodic Table), suggesting its relatively low tendency to gain an electron in dications. Therefore, 5A is eligible to be regarded as the so-called “superalkaline earth metal dication”, which might be stable enough to exist as the positive portion of an ionic salt.

## Conclusion

In summary, we have demonstrated based on the extensive computational explorations that nitrogen is more suitable than carbon to fit the H-surrounded  $\text{Be}_5$  rings both geometrically and electronically. The nitrogen substitution for the planar penta-coordinate carbon in  $\text{CBe}_5\text{H}_n^{n-4}$  ( $n = 0-5$ ) leads to the perfect planar structure for  $n = 4$  and 5 and fixes the highly free H atoms for  $n = 2$  and 3. Remarkably, when the diffused Be–Be 2c-2e  $\sigma$  bonds were gradually replaced by much less diffused Be–

H–Be 3c-2e bonds, the structures were gradually stabilized from the electronic structure point of view, as reflected by the increasing HOMO–LUMO gaps. In six planar penta-coordinate nitrogen species designed in this work,  $\text{NBe}_5\text{H}_5^{2+}$  (5A) possesses the best stability, which would be promising to obtain it as the positive portion of an ionic salt.

## Conflicts of interest

There are no conflicts to declare.

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## References

- (a) L.-M. Yang, E. Ganz, Z. Chen, Z.-X. Wang and P. v. R. Schleyer, *Angew. Chem., Int. Ed.*, 2015, **54**, 9468–9501; (b) V. Vassilev-Galindo, S. Pan, K. J. Donald and G. Merino, *Nat. Rev. Chem.*, 2018, **2**, 0114.
- (a) K. Sorger and P. v. R. Schleyer, *J. Mol. Struct.: THEOCHEM*, 1995, **338**, 317–346; (b) D. Röttger and G. Erker, *Angew. Chem., Int. Ed. Engl.*, 1997, **36**, 812–827; (c) L. Radom and D. R. Rasmussen, *Pure Appl. Chem.*, 1998, **70**, 1977–1984; (d) W. Siebert and A. Gunale, *Chem. Soc. Rev.*, 1999, **28**, 367–371; (e) R. Keese, *Chem. Rev.*, 2006, **106**, 4787–4808; (f) G. Merino, M. A. Méndez-Rojas, A. Vela and T. Heine, *J. Comput. Chem.*, 2007, **28**, 362–372.
- K. Exner and P. v. R. Schleyer, *Science*, 2000, **290**, 1937–1940.
- (a) P. Liu, J.-H. Bian, Q. Wang, F. Huang, D. Li and Y.-B. Wu, *Phys. Chem. Chem. Phys.*, 2018, **20**, 12642–12649; (b) X.-F. Zhao, J.-H. Bian, F. Huang, C. Yuan, Q. Wang, P. Liu, D. Li, X. Wang and Y.-B. Wu, *RSC Adv.*, 2018, **8**, 36521–36526; (c) S. Pan, J. L. Cabellos, M. Orozco-Ic,



- P. K. Chattaraj, L. Zhao and G. Merino, *Phys. Chem. Chem. Phys.*, 2018, **20**, 12350–12355; (d) J.-C. Guo, L.-Y. Feng, C. Dong and H.-J. Zhai, *J. Phys. Chem. A*, 2018, **122**, 8370–8376; (e) J.-C. Guo, Y.-X. Cheng and X.-F. Wu, *Comput. Theor. Chem.*, 2020, **1180**, 112824; (f) J.-C. Guo, L.-Y. Feng, J. Barroso, G. Merino and H.-J. Zhai, *Chem. Commun.*, 2020, **56**, 8305–8308; (g) M.-h. Wang, X. Dong, Y.-h. Ding and Z.-h. Cui, *Chem. Commun.*, 2020, **56**, 7285–7288; (h) R. Sun, X.-F. Zhao, B. Jin, B. Huo, J.-H. Bian, X.-L. Guan, C. Yuan and Y.-B. Wu, *Phys. Chem. Chem. Phys.*, 2020, **22**, 17062–17067.
- 5 J.-C. Guo, G.-M. Ren, C.-Q. Miao, W.-J. Tian, Y.-B. Wu and X. Wang, *J. Phys. Chem. A*, 2015, **119**, 13101–13106.
- 6 (a) X. Li and L. S. Wang, *Eur. Phys. J. D*, 2005, **34**, 9–14; (b) B. B. Averkiev, A. I. Boldyrev, X. Li and L.-S. Wang, *J. Chem. Phys.*, 2006, **125**, 124305; (c) B. Song, C.-H. Yao and P.-I. Cao, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2006, **74**, 035306; (d) B. B. Averkiev, A. I. Boldyrev, X. Li and L.-S. Wang, *J. Phys. Chem. A*, 2007, **111**, 34–41; (e) B. B. Averkiev, S. Call, A. I. Boldyrev, L.-M. Wang, W. Huang and L.-S. Wang, *J. Phys. Chem. A*, 2008, **112**, 1873–1879; (f) W.-Q. Zhang, J.-M. Sun, G.-F. Zhao and L.-L. Zhi, *J. Chem. Phys.*, 2008, **129**, 064310; (g) L.-M. Wang, W. Huang, L.-S. Wang, B. B. Averkiev and A. I. Boldyrev, *J. Chem. Phys.*, 2009, **130**, 134303; (h) H. Wang, Y. J. Ko, K. H. Bowen, A. P. Sergeeva, B. B. Averkiev and A. I. Boldyrev, *J. Phys. Chem. A*, 2010, **114**, 11070–11077.
- 7 (a) P. v. R. Schleyer and A. I. Boldyrev, *J. Chem. Soc., Chem. Commun.*, 1991, 1536–1538; (b) S. K. Nayak, B. K. Rao, P. Jena, X. Li and L. S. Wang, *Chem. Phys. Lett.*, 1999, **301**, 379–384; (c) S. D. Li, G. M. Ren, C. Q. Miao and Z. H. Jin, *Angew. Chem., Int. Ed.*, 2004, **43**, 1371–1373; (d) Z.-h. Cui and Y.-h. Ding, *Phys. Chem. Chem. Phys.*, 2011, **13**, 5960–5966.
- 8 Z.-h. Cui, C.-b. Shao, S.-m. Gao and Y.-h. Ding, *Phys. Chem. Chem. Phys.*, 2010, **12**, 13637–13645.
- 9 S. D. Li, C. Q. Miao and G. M. Ren, *Eur. J. Inorg. Chem.*, 2004, 2232–2234.
- 10 J.-C. Guo, L.-Y. Feng, X.-Y. Zhang and H.-J. Zhai, *J. Phys. Chem. A*, 2018, **122**, 1138–1145.
- 11 A. E. Reed, L. A. Curtiss and F. Weinhold, *Chem. Rev.*, 1988, **88**, 899–926.
- 12 D. Y. Zubarev and A. I. Boldyrev, *Phys. Chem. Chem. Phys.*, 2008, **10**, 5207–5217.
- 13 J. C. Santos, J. Andres, A. Aizman and P. Fuentealba, *J. Chem. Theory Comput.*, 2005, **1**, 83–86.
- 14 (a) P. v. R. Schleyer, C. Maerker, A. Dransfeld, H. Jiao and N. J. R. van Eikema Hommes, *J. Am. Chem. Soc.*, 1996, **118**, 6317–6318; (b) Z. Chen, C. S. Wannere, C. Corminboeuf, R. Puchta and P. v. R. Schleyer, *Chem. Rev.*, 2005, **105**, 3842–3888.
- 15 (a) M. Saunders, *J. Comput. Chem.*, 2004, **25**, 621–626; (b) P. P. Bera, K. W. Sattelmeyer, M. Saunders, H. F. Schaefer and P. v. R. Schleyer, *J. Phys. Chem. A*, 2006, **110**, 4287–4290.
- 16 (a) J. M. Millam, V. r. Bakken, W. Chen, W. L. Hase and H. B. Schlegel, *J. Chem. Phys.*, 1999, **111**, 3800–3805; (b) X. S. Li, J. M. Millam and H. B. Schlegel, *J. Chem. Phys.*, 2000, **113**, 10062–10067.
- 17 J. V. Ortiz, V. G. Zakrzewski and O. Dolgounircheva, *Conceptual Perspectives in Quantum Chemistry*, Kluwer Academic, 1997.
- 18 (a) Y.-B. Wu, H.-G. Lu, S.-D. Li and Z.-X. Wang, *J. Phys. Chem. A*, 2009, **113**, 3395–3402; (b) H. G. Lu and Y. B. Wu, in *GXYZ 2.0, A Random Search Program*, Shanxi University, Taiyuan, 2015.
- 19 *The AdNDP program was downloaded freely at*, <http://ion.chem.usu.edu/~boldyrev/adndp.php>.
- 20 H.-J. Werner, *et al.*, in *MolPro 2012.1*, University College Cardiff Consultants Limited, Cardiff U.K., 2012.
- 21 M. J. Frisch, *et al.*, in *Gaussian 09 Revision D.01*, Gaussian Inc., Wallingford CT, 2013.
- 22 (a) J. C. Santos, W. Tiznado, R. Contreras and P. Fuentealba, *J. Chem. Phys.*, 2004, **120**, 1670–1673; (b) R. Islas, E. Chamorro, J. Robles, T. Heine, J. C. Santos and G. Merino, *Struct. Chem.*, 2007, **18**, 833–839; (c) J. C. Santos and P. Fuentealba, *Chem. Phys. Lett.*, 2007, **443**, 439–442.

