Rotational excitation of $C_2H^-$ anion in collision with $H_2$

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The discovery of anions in the interstellar medium has shown that they are very reactive species. This gave them great importance in the modeling of the chemical and astrophysical evolution of the interstellar medium. The detection of the first anion $C_6H^-$ followed by the other anions $C_8H^-$, $C_9H^-$ and $CN^-$ in the interstellar medium has encouraged research on other detectable anions. The $C_2H^-$ anion was observed for the first time in the circumstellar envelope of IRC+10216 and in TMC-1. In these cold and low-density regions, precise modeling of the chemical and physical conditions of the observed emission lines requires knowledge of the radiative and collisional excitation rates. We present here the first new two-dimensional Potential Energy Surface (PES) for $C_2H^-\cdot H_2$ interaction. Rotational excitation of the anion by collision with para-$H_2(j_H = 0)$ is investigated. The PES is obtained in the super-molecular approach based on a single and double excitation coupled cluster method with perturbative contributions from triple excitations (CCSD(T)). In all our calculations, all atoms were described using the augmented correlation-consistent triple zeta (aug-cc-pVTZ) basis sets and bond functions. Fully-quantum close-coupling calculations of inelastic integral cross sections are done on a grid of collision energies large enough to ensure converged state-to-state rate coefficients for the 16 first rotational levels of $C_2H^-$ and for temperatures ranging from 5 to 120 K. For this collisional system, rate coefficients exhibit a strong propensity in favor of even $\Delta J$ transitions.

1 Introduction

In the last two decades, anions have been intensively studied. These studies were framed by observations in the laboratory\textsuperscript{1-3} and some astrophysical observations.\textsuperscript{4,5} Among these species, mention is made of carbon chain anions $C_2H^-$.\textsuperscript{6} The recent discovery of carbon chain anions $C_{2n}H^-$ in interstellar and circumstellar media has been investigated by many theoretical and experimental works on these species.\textsuperscript{7-11} Their structures as well as the importance of their role in the interstellar chemistry and in gas phase ion–molecule reactions are the object of many recent studies.\textsuperscript{8,10,11} Although the existence of anions in astrophysical sources was first predicted theoretically and early considered in chemical models,\textsuperscript{12,13} the first negative hydrocarbon $C_9H^-$ was detected in 2006 (ref. 2) solving the problem of the unidentified lines discovered by Kawaguchi et al.\textsuperscript{14} The $C_9H^-$ identification was followed by the detection of other negatively charged species like $C_4H^-$, $C_6H^-$, $C_7N^-$, $C_8N^-$ and $CN^-$.\textsuperscript{15-23} Many of these species were first detected in IRC+10216.\textsuperscript{2,15,18} Hydrocarbon anions were also discovered later in other molecular clouds.\textsuperscript{24} In this set $C_2H^-$ present a capital importance.

Several observations in the laboratories have justified the detection of the $C_2H^-$ anion. This experimental studies\textsuperscript{25} interest of the $C_2H^-$ anion comes from the fact that the $C_2H^-$ anion is the shortest in the sequence of carbon chain anions with a closed-shell electronic ground state, and the fact that gives the rest frequencies required for a radio astronomical search for this polar, astronomically plausible molecule.

From astrophysical observations, in 2007 J. Cernicharo et al.\textsuperscript{15,25} detected the 1–0 transition of the $C_2H^-$ anion and calculated the abundance ratio $C_2H/C_3H = 12.5$. Cernicharo et al. suggest that the 3–2 transition is strong enough to be detected. Later in 2010, the observations of M. Agúndez et al.\textsuperscript{26} found difficulties in detecting the 1–0 and 2–0 transitions of the anion. These difficulties are probably due to the very reactive natures of the $C_2H^-$ anion.

We report in this work a first collisional study of $C_2H^-$ with para-$H_2(j_H = 0)$ at low temperatures trying to understand the particular behavior of negatively charged species during collisions and how they compare with neutral forms\textsuperscript{27,47} and the $C_2H^-$ anion in collision with He.\textsuperscript{48} In the next section, we will present details of the \textit{ab initio} calculations of the $C_2H^-\cdot para-H_2$ potential Energy Surface (PES). In Section 3, some theoretical...
aspects of the scattering calculations are given, state-to-state collisional cross sections will be reported, the rate coefficients and the propensity rules will be showcased. In Section 4, comparative study between the rate coefficients of C₂H⁻—para-H₂ and C₂H—He will be displayed. Concluding remarks are made in Section 5.

2 Potential Energy Surface

This work primarily focuses on the rotational excitation of C₂H⁻ with para-H₂ at low temperature; both monomers were considered as rigid species to deal with a reduced number of degrees of freedom. Accordingly, in our calculations, it is considered to be linear, and both bond lengths are set at the CCSD/AV5Z theoretical values of r_C-C = 1.250 Å and r_C-H = 1.070 Å. For H₂, we used the experimental bond length r_H-H = 1.44876 bohr corresponding to the averaged value over the ground-state vibrational wave function for H₂. The lowest bending mode of C₂H⁻ is equal to 502.0 cm⁻¹, it is well above the energy of the highest C₂H⁻ rotational level considered in this work (j = 16, see Table 1). In addition, from QCT studies of rotational excitation of H₂O by H₂, it was shown that the coupling between the rotational excitation and the bending may be neglected for temperatures up to 5000 K. Moreover, it was also shown by Faure et al., in the particular case of the H₂O–H₂ system, that the 5D-PES calculated at the experimental ground vibrational state geometry and the full 9D-PES averaged over the ground vibrational state are very similar. These results suggest that the use of a rigid body 2D-PES is sufficient as long as bending and vibrational excitations are not taken into consideration.

Then, we define the body-fixed coordinate system in Fig. 1. The geometry of C₂H⁻–H₂ collisional system with para-H₂ and C₂H⁻ treated as rigid rotors is then characterized by three angles (θ, θ', φ) and the distance R between the center of masses of H₂ and C₂H⁻ (see Fig. 1). The polar angles of the C₂H⁻ and para-H₂ molecules with respect to R are denoted θ and θ', while φ denotes the dihedral angle, which is the relative polar angle between the C₂H⁻ and para-H₂ bonds. For the solution of the close-coupling scattering equations, it is most convenient to expand, at each value of R, the interaction potential V(R, θ, θ', φ) in angular functions. For the scattering of two linear rigid rotors, we used

\[ V(R, \theta, \theta', \phi) = \sum_{l,l',m} v_{l,l',m}(R) s_{l,l',m}(\theta, \theta', \phi) \]  

where \( s_{l,l',m}(\theta, \theta', \phi) \) are products of normalized associated Legendre functions \( P_{l,m} \):

\[ s_{l,l',m}(\theta, \theta', \phi) = \left( \frac{2l + 1}{4\pi} \right)^{1/2} \left\{ (lI^0|l'l'\mu0)P_{l\mu}(\theta)P_{l'\mu}(\theta') \cos(m\phi) \right\} \]

Table 1: Rotational Energy for the first 28 Levels of C₂H⁻ system

<table>
<thead>
<tr>
<th>j</th>
<th>( e_j ) (cm⁻¹)</th>
<th>j</th>
<th>( e_j ) (cm⁻¹)</th>
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<td>8.3334960</td>
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<td>424.7113668</td>
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<td>4</td>
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<td>25</td>
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<td>13</td>
<td>252.6791032</td>
<td>28</td>
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</tr>
</tbody>
</table>

The basis functions \( s_{l,l',m}(\theta, \theta', \phi) \) are products of normalized associated Legendre functions \( P_{l,m} \):

\[ s_{l,l',m}(\theta, \theta', \phi) = \left( \frac{2l + 1}{4\pi} \right)^{1/2} \left\{ (lI^0|l'l'\mu0)P_{l\mu}(\theta)P_{l'\mu}(\theta') \cos(m\phi) \right\} \]

where \( S \ldots S \ldots \) is a Clebsch–Gordan coefficient. The \( P_{l,m} \) functions are related to spherical harmonics through \( Y_{l,m}(\theta, \phi) = P_{l,m}(\theta) \exp(im\phi) \). Here, \( l \) and \( l' \) are associated with the rotational motion of C₂H⁻ and para-H₂ respectively. In eqn (1) the homonuclear symmetry of H₂ forces the index \( l \) to be even. For collisions at low/moderate temperature, the probability of rotational excitation of H₂ is low (the energy spacing between the \( J_1 = 0 \) and \( J_2 = 2 \) levels in para-H₂ being 510 K) so we further restrict H₂ to its lowest rotational level. In this case, only the leading term \( l' \mu = 0 \) needs to be retained in the expansion of the interaction potential given in eqn (1). The resulting expansion then can be simplified to

\[ V_{av}(R, \theta) = \sum_{l} v_{l}(R) P_{l}(\cos(\theta)) \]  

where \( V_{av}(R, \theta) \) is obtained by an average over angular motion \( (\theta', \phi) \) of the H₂ molecule. We approximate the average by an equipoise averaging over three sets of \( (\theta', \phi) \) angles for each calculated set of \( (R, \theta) \). Those are \( (\theta' = 0, \phi = 0) \), \( (\theta' = \frac{\pi}{2}, \phi = \frac{\pi}{2}) \) and \( (\theta' = \frac{\pi}{2}, \phi = 0) \). Thus, the C₂H⁻–para-H₂ collisional system is reduced to a two-dimensional \( V_{av} \) PES such as

\[ V_{av}(R, \theta) = \frac{1}{3} \left( V(R, \theta, \theta', \phi_1) + V(R, \theta, \theta', \phi_2) + V(R, \theta, \theta', \phi_3) \right) \]
Such approximation has been shown to be reasonably accurate for relatively heavy molecule such as SIS,\textsuperscript{23} HCO\textsuperscript{−} (ref. 33) and C\textsubscript{2}.\textsuperscript{44} In the C\textsubscript{2} point group, the ground electronic state of the C\textsubscript{2}H\textsubscript{2}–\textit{para}-H\textsubscript{2} van der Waals system is of \textit{A}\textsubscript{1} symmetry. The PES was calculated in the super-molecular approach based on a single and double excitation coupled cluster method with perturbative contributions from triple excitations (CCSD(T)).\textsuperscript{35,36} For the five atoms, we used the aug-cc-pVTZ basis set of Woon\textsuperscript{37} and placed equidistant between the C\textsubscript{2}H\textsubscript{2} and H\textsubscript{2} centers of mass. At all geometries, the Boys and Bernardi\textsuperscript{38} counterpoise procedure was used to correct for basis set superposition error (BSSE). All calculations were carried out using the MOLPRO 2010 package.\textsuperscript{40}

The radial scattering coordinate \( R \) was assigned 36 values ranging from 3.0 to 50.0 bohr, the \( \theta \) grid ranged from 0° to 180° in steps of 15°. This resulted in a total of 1404 geometries computed for the C\textsubscript{2}H\textsuperscript{−}–\textit{para}-H\textsubscript{2}[(\( R_\text{H} = 0 \)] system.

An analytic representation of the present 2D PES suitable for dynamics calculations was obtained using the procedure described by eqn (12)–(16) of Werner et al.\textsuperscript{41} for the CN–He system. In order to perform the scattering calculations, this PES was expanded in terms of Legendre polynomials.

Fig. 2 displays the contour plot of the 2D \( V(R, \theta) \) PES. For this van der Waals system, the global minimum was found to be 250.6 cm\textsuperscript{−1} at \( R = 7.20 \) bohr and \( \theta = 76.0 \) degree.

3 Dynamical calculation

The fitted C\textsubscript{2}H\textsuperscript{−}–\textit{para}-H\textsubscript{2} 2D-PES was used to calculate state-to-state cross sections and rate coefficients. The full close coupling approach first introduced by Arthurs & Dalgarno\textsuperscript{42} was used for the calculations of the state-to-state cross sections between the 16 first rotational levels. The energies of the rotational levels were computed from the following C\textsubscript{2}H\textsuperscript{−} spectroscopic constants: \( B_0 = 1.3889354 \) cm\textsuperscript{−1} and \( D_0 = 3.2345 \times 10^{-6} \) cm\textsuperscript{−1}.\textsuperscript{43} The scattering calculations were carried out with the MOLSCAT code.\textsuperscript{44} Calculations were performed for energies ranging from 3.0 to 1200.0 cm\textsuperscript{−1}. The integration parameters and the size of the basis set were chosen to ensure convergence of the cross sections over this range. At the highest considered total energy (1200.0 cm\textsuperscript{−1}), the C\textsubscript{2}H\textsuperscript{−} rotational basis included channels up to \( j = 28 \) to ensure convergence of the excitation cross sections for transitions including up to the \( J = 16 \) rotational level (see Tables 1 and 2).

We carefully spanned the energy grid to take into account the presence of resonances. The energy steps are 0.1 cm\textsuperscript{−1} below 100.0 cm\textsuperscript{−1}, 0.2 cm\textsuperscript{−1} from 100.0 to 250.0 cm\textsuperscript{−1}, 1.0 cm\textsuperscript{−1} between 250.0 and 300.0, 5.0 cm\textsuperscript{−1} between 300.0 and 400.0 cm\textsuperscript{−1}, 10.0 cm\textsuperscript{−1} between 400.0 and 500.0 cm\textsuperscript{−1}, 25.0 cm\textsuperscript{−1} between 500.0 and 700.0 cm\textsuperscript{−1} and 50.0 cm\textsuperscript{−1} between 700.0 and 1200.0 cm\textsuperscript{−1}.

3.1 Integral cross sections

Fully-quantum close-coupling calculations of integral cross sections were carried out for values of total energies ranging from 3.0 to 1200 cm\textsuperscript{−1}. The variation of integral cross sections for a few selected \( j \rightarrow j' \) rotational transitions with collision energy is shown in Fig. 3. For collisional energies below 300.0 cm\textsuperscript{−1} many resonances occur. This is a consequence of the attractive potential well with a depth of 252.6 cm\textsuperscript{−1}. At low energy, the molecule can be temporarily trapped in quasi-bound states,\textsuperscript{45} which arise both from tunneling through the centrifugal barrier (shape resonances) and from excitation of C\textsubscript{2}H\textsuperscript{−} to a higher rotational level which is energetically allowed in the well (Feshbach resonances). Some anisotropy appears around the well depth which may induce a different trend of the cross sections at lower energies.

3.2 Rate coefficients

From the calculated cross sections, one can obtain the corresponding state-to-state rate coefficients by Boltzmann averaging:

\[
k_{j \rightarrow j'}(T) = \left( \frac{8k_B T}{\pi \mu} \right)^{1/2} \left( \frac{1}{k_B T} \right)^2 \int_{E_k}^{E_{j'}_{\text{max}}} E_k \sigma_{j \rightarrow j'}(E_k) e \left( \frac{E_k}{k_B T} \right) \mathrm{d}E_k \tag{5}
\]

where \( k_B \) is the Boltzmann constant and \( E_k \) is the kinetic energy. The total energy range considered in this work allows us to determine rate coefficients for temperatures up to 120 K. The total energy range considered in this work allows us to

\[
\begin{array}{ccccccc}
\sigma_{16-15} & 15.316 & 15.322 & 15.322 & 15.322 & 15.322 \\
\sigma_{16-14} & 6.666 & 6.665 & 6.665 & 6.665 & 6.663 \\
\sigma_{2-1} & 2.7937 & 2.7941 & 2.7941 & 2.7941 & 2.7941 \\
\end{array}
\]

Table 2 Convergence of cross-sections (in A\textsuperscript{2}) for some rotational transitions with respect to size of the basis set \( J_{\text{max}} \) for total energy \( E = 1200 \) cm\textsuperscript{−1}
determine rate coefficients for temperatures up to 120 K. The representative variation with temperature of de-excitation rate coefficients from an initial level \( j \) to a final level \( j' \) is shown in Fig. 4. The rate coefficients obviously display the same propensity than the integral cross sections. Fig. 5 present for 50.0 K downward rotational rate coefficients of \( \text{C}_2\text{H}^-/\text{C}_0 \) \((j_0 = 12)\) level as a function of the final \( j \) level. This plot confirms the \( \Delta j = 2 \) even propensity. The same behavior was found for the iso-electronic \( \text{HCN} \) molecule\(^4\) and for the neutral \( \text{C}_2\text{H}^- \) in collision with \( \text{He} \).\(^5\)

The complete set of de-excitation rate coefficients with \( j, j' \leq 16 \) will be available on-line from the BASECOL website (http://www.obspm.fr/basecol). Excitation rate coefficients can be easily obtained by detailed balance.

4 Comparison with \( \text{C}_2\text{H}^-/\text{He} \) collisions

It is generally assumed that excitation rate coefficients associated with \( \text{He} \) as the collision partner can provide a first estimation for rate coefficients for collisions with \( \text{para-H}_2/j_{\text{H}_2} = 0 \) just applying a scaling factor which is equal to the square root of the ratio of the reduced masses of the two systems. For \( \text{C}_2\text{H}^- \), this scaling factor tends to 1.4. Since rotational rate coefficients have been calculated previously for \( \text{C}_2\text{H}^- \) in collision with \( \text{He} \),\(^4\) using the same methodology as the one employed in present work for \( \text{C}_2\text{H}^-/\text{para-H}_2/j_{\text{H}_2} = 0 \), the comparison between the two sets of rate coefficients can be used to assess the validity of such approximation.

"Fig. 3" Rotational excitation \( j \rightarrow j' \) cross sections of \( \text{C}_2\text{H}^- \) in collision with \( \text{para-H}_2/j_{\text{H}_2} = 0 \) as a function of the relative kinetic energy.

"Fig. 4" Temperature dependence of state-to-state rate coefficients.

"Fig. 5" \( \text{C}_2\text{H}^-/\text{para-H}_2/j_{\text{H}_2} = 0 \) excitation rate coefficients for the \( j \rightarrow j' = 12 \) transitions at 50 K.

"Fig. 6" \( \text{C}_2\text{H}^-/\text{para-H}_2/j_{\text{H}_2} = 0 \) rate coefficients as a function of the \( \text{C}_2\text{H}^-/\text{He} \) rate coefficients for \( j \rightarrow j' \) transitions with \( j = 12 \) and \( j' = 6, 7, 8, 9, 10, 11 \) at a temperature of 10 K (red circles) and 100 K (blue diamond); the black solid line corresponds to a ratio of 1.4.
We report in Fig. 6 a comparison between the rate coefficients of the present study and those reported by Dumouchel et al. for the selected transitions (see Fig. 4 in ref. 48). The red circles and the blue diamond’s reveal the rate coefficients of $\text{C}_2\text{H}^-$-para-$\text{H}_2(\tilde{J}_{\text{rot}} = 0)$ vs. $\text{C}_2\text{H}^-$-He at kinetic temperatures $T = 10.0\text{ K}$ and $T = 100.0\text{ K}$ respectively. As shown above, the ratio between the rate coefficients clearly differs from the value of 1.4. These differences are due to the difference in interaction energies between the two systems. The ratios deviate clearly from 1.4 for all the transitions, by a factor varying from 3 to 11.

energies between the two systems. The ratios deviate clearly from 1.4 to model the rates with $\text{H}_2$. This result is also found in the interaction potential $\text{C}_2\text{H}^-$-He system than for $\text{C}_2\text{H}^-$-para-$\text{H}_2$ ($\tilde{J}_{\text{rot}} = 0$). Then, the collision rates with corrected with the scale factor 1.4 do not always constitute a good approximation to model the rates with $\text{H}_2$. This result is also found in the collisions with the neutral species $\text{C}_2\text{H}$ (see ref. 47).

5 Summary and conclusion

Quantum scattering calculations have been used to investigate energy transfer in collisions of $\text{C}_2\text{H}^-$ with para-$\text{H}_2(\tilde{J}_{\text{rot}} = 0)$ molecule. The calculations are based on a new, highly correlated 2D PES calculated at the RCCSD(T) level using large AVTZ basis sets and a bent functions. Close coupling calculations were performed for collision energies ranging from 3.0 to 1200.0 cm$^{-1}$. Rate coefficients for transitions involving the 16 first rotational levels of the $\text{C}_2\text{H}^-$ anion were determined for temperature ranging from 5 to 120.0 K. The rate coefficients show a strong propensity for even $\Delta J$, mainly $\Delta J = 2$. The present set of rate coefficients can serve the modelling of $\text{C}_2\text{H}^-$ emission lines in astrophysical environments. Finally, the resulting inelastic rate coefficients for collisions of $\text{C}_2\text{H}^-$ with para-$\text{H}_2$ will help in constraining astrochemical anion chemistry and also in accurately model regions containing anions such as IRC+10216. We encourage astrophysicists to use these new values in their next detection attempts in the IRC+10216. Future work will deal with calculations of $\text{C}_2\text{H}^-$ in collision with both para- and ortho-$\text{H}_2$ species using 4D PES approach in order to obtain rate coefficients for highly excited rotational states and higher temperatures. Detailed comparison with other systems, in particular carbon chain anions, will be studied in detail owing to its great interest for astrochemical modelling.

Conflicts of interest

There are no conflicts to declare.

Notes and references