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# Theoretical study of the H/D isotope effect of CH<sub>4</sub>/CD<sub>4</sub> adsorption on a Rh(111) surface using a combined plane wave and localized basis sets method

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We analysed the H/D isotope effect of CH<sub>4</sub>/CD<sub>4</sub> adsorption on a Rh(111) surface using our combined plane wave and localized basis sets method, that we proposed for the consideration of delocalized electrons on a surface and the quantum effect of protons (deuterons) in metal–molecule interactions. We observed that the adsorption distance and energy of CD<sub>4</sub> were larger and lower than those of CH<sub>4</sub>, respectively. This is in reasonable agreement with the corresponding experimental results of cyclohexane adsorption. We clearly found that the trend of the H/D isotope effect in the geometrical and energetic difference was similar to that of the hydrogen-bonded systems.

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## Introduction

The behaviour of atoms and molecules on various surfaces has attracted attention in various fields, including materials science, material physics, and catalytic chemistry. In particular, the interaction between hydrogen (H) and transition metals is a crucial factor in chemical and physical processes. The H in the molecules that are adsorbed on metal surfaces determines important phenomena for not only fundamental physics but also for catalytic activity.<sup>1,2</sup> It has been reported that the differences in adsorption energy, diffusion coefficient, and catalytic activity depend on various metals and surface orientations.<sup>3–5</sup> Despite these studies, the interaction mechanism between H and metal surfaces is still not clearly understood due to the difficulty in the direct analysis of H on the metal surface from only the experimental side.

The interaction between H and metal surfaces is often analysed by deuterium (D) substitution for H. This helps in understanding the details of molecular adsorption on metal surfaces from the viewpoint of H/D isotope effects. Thus, understanding the H/D isotope effect is one of the key factors for surface design. For example, using a high-vacuum

microbalance, Jin *et al.* observed that the adsorption energy of D<sub>2</sub> (0.302 eV) is larger than that of H<sub>2</sub> on the surface of a Pd–Pt alloy.<sup>6</sup> Zheng *et al.* observed that the diffusion coefficient of H (0.027 cm<sup>2</sup> s<sup>−1</sup>) is larger than that of D on Pd(111) surfaces.<sup>4</sup> These experimental results clearly indicate that the adsorption of D on metal surfaces is stronger than that of H. Moreover, H/D isotope effects in the chemical reactions of the adsorbed molecules on metal surfaces, such as oxygen reduction and hydrogen exchange reactions, were reported.<sup>7–9</sup> However, it is difficult to directly analyse the H/D isotope effects in detail in the structural parameters of the adsorbed molecules on the metal surfaces.

Recently, Koitaya *et al.* observed the H/D isotope effects on the adsorption energy and adsorption distance of the molecules of cyclohexane (C<sub>6</sub>H<sub>12</sub>) and its deuterium substituent (C<sub>6</sub>D<sub>12</sub>) on Rh(111) surface.<sup>10</sup> To the best of our knowledge, this is the first report discussing the H/D isotope effects on the geometrical differences of molecules adsorbed on a metal surface. Interestingly, they clearly elucidated that the adsorption energy of C<sub>6</sub>H<sub>12</sub> was 0.084 eV higher than that of C<sub>6</sub>D<sub>12</sub>. This result shows an opposite trend of the H/D isotope effects on H/D atomic adsorption on the metal surfaces. However, the mechanism of this inverse isotope effect is still unclear. Therefore, it is necessary to understand the mechanism of the geometrical H/D isotope effects of adsorbed molecules on metal surfaces.

It is well known that the electronic structure calculation is one of the most powerful approaches for elucidating the detailed mechanism of adsorbed molecules on the metal surfaces. The plane wave (PW) approach using periodic boundary conditions (PBCs) is an effective tool for understanding physical and chemical phenomena on the metal surfaces. There are also many studies on H adsorption on the

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metal surfaces.<sup>11–14</sup> Since the nuclear quantum effects (NQE) of protons and deuterons are treated as a difference of nuclear mass in the framework of the Born–Oppenheimer approximation in the conventional electronic structure calculation, the H/D isotope effects are discussed using the vibrational zero-point energy under harmonic oscillator approximation.<sup>15</sup> However, reproducing the geometrical differences under the above treatment of protons and deuterons is difficult. Thus, it is essential to analyse the geometrical differences in the metal–hydrogen interaction that are induced by the difference in the NQEs of protons and deuterons. Although the direct treatment of the NQEs of protons and deuterons is important in electronic structure calculations for discussing the H/D isotope effects, PW embedded NQEs have not yet been developed. It is also difficult to describe small geometrical and electronic structure differences in H and D by the PW approach.

For the direct treatment of the difference of the NQEs of protons and deuterons, we developed multicomponent molecular orbital and density functional theory (MC\_MO and MC\_DFT) approaches, which are based on localized orbitals (LOs).<sup>16–18</sup> Using these approaches, it is possible to describe the geometrical and electronic structure changes that are induced by H and D.<sup>17,19</sup> Although these approaches are useful in investigating the H/D isotope effects for adsorbed molecules on metal surfaces, the calculation of large systems, such as those defined by PBCs, is not realistic due to high computational cost. Moreover, the addition of LO-based MC\_MO and MC\_DFT to the PW approach is challenging due to the high cost of program modification and computational accuracy. Thus, to achieve sufficient accuracy for analysing the H/D isotope effects for adsorbed molecules on metal surfaces, we proposed the combined plane wave and localized basis sets (CPLB) method.<sup>20</sup> In the CPLB method, the electronic structure of the surface system is calculated using the PW approach. Conversely, a highly accurate LO calculation that is based on the MC\_MO or MC\_DFT approach is used for cluster model to describe the NQEs of protons and deuterons directly. The combination of both the PW- and LO-based approaches facilitates a detailed analysis of the H/D isotope effects for molecular adsorption on metal surfaces. We have already reported the efficiency of the CPLB method in analysing the H/D isotope effects of H/D atomic adsorption on the Pd(111) surface.<sup>21</sup>

In this study, we calculated the CH<sub>4</sub>/CD<sub>4</sub> adsorption on the Rh(111) surface, which is a model of C<sub>6</sub>H<sub>12</sub>/C<sub>6</sub>H<sub>12</sub> adsorption on Rh(111) surface experimentally,<sup>10</sup> using the CPLB method to analyse and understand the geometrical and energetic changes induced by the H/D isotope effect.

## CPLB method

Herein, we explain the framework of our proposed CPLB method. The CPLB method is developed by extending it to a periodic system that is based on the ONIOM-like scheme.<sup>22</sup> The procedure for the calculation of adsorption energy for the CH<sub>4</sub> adsorption on the Rh(111) surface is illustrated in Fig. 1. The total energy of the surface system ( $E(\text{PW, surface})$ ) consisting of the Rh(111) surface with adsorbed CH<sub>4</sub> was calculated

using the PW-based electronic structure calculations. The total energy of adsorbed CH<sub>4</sub> on the Rh cluster model, *i.e.*,  $E(\text{PW, cluster})$  and  $E(\text{LO, cluster})$ , were calculated using both the PW- and LO-based electronic structure calculations, respectively. Based on these values, the total energy of the surface ( $E(\text{CPLB, surface})$ ) is calculated by the CPLB method using eqn (1), which provides sufficient accuracy by including both delocalized electronic structure in PW and accurate metal–hydrogen interaction in the LO. In addition, by selecting the appropriate calculation method as PW or LO calculation, it is also possible to further analyse. In this study, we calculated these systems including the NQEs of proton and deuteron by selecting the MC approach for the LO calculation.

$$E(\text{CPLB, surface}) = E(\text{PW, surface}) - E(\text{PW, cluster}) + E(\text{LO, cluster}) \quad (1)$$

The  $\text{grad} E(\text{CPLB, surface})$  can be obtained by using the gradient with respect to the nuclear coordinates for each energy, as follows:

$$\text{grad} E(\text{CPLB, surface}) = \text{grad} E(\text{PW, surface}) - \text{grad} E(\text{PW, cluster}) - \text{grad} E(\text{PW, cluster}) \quad (2)$$

Using this scheme, we developed a geometry optimisation algorithm for the CPLB method. The adsorption energy and various other properties of CH<sub>4</sub> were also calculated using the same procedure.

## Computational details

The computational details of each calculation are as follows: for the PW-based electronic structure calculations, we used the Vienna *ab initio* simulation package (VASP)<sup>23,24</sup> with the projector-augmented wave method.<sup>25,26</sup> The Perdew–Burke–Ernzerhof approximation with a generalized gradient approximation<sup>27</sup> was used for the exchange and correlation functionals. The cut-off energy was set to 800 eV. The structure of the Rh(111) surface was modelled based on three atomic layers with 16 atoms in each layer since the energy difference between 3 and 4 or 5 atomic layers was less than 0.005 eV for CH<sub>4</sub>

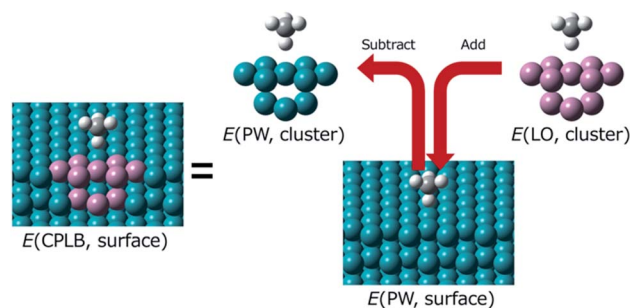
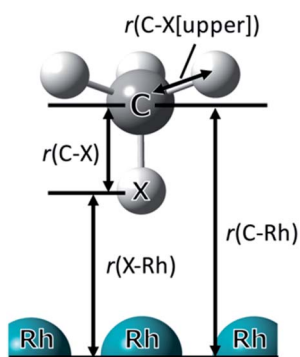


Fig. 1 Schematic illustration of the CPLB approach for CH<sub>4</sub> adsorption on a Rh(111) surface. The green and pink balls are Rh atom. These were treated using the PW and LO methods, respectively.



**Table 1** The optimised parameters (Å) for adsorbed CH<sub>4</sub>/CD<sub>4</sub> at the on-top site on Rh(111) surface using the CPLB method. X indicates H or D in CH<sub>4</sub>/CD<sub>4</sub>.  $r(\text{C-X}$  [upper]) is the average value of three C–H/C–D distances pointing upward

	CH <sub>4</sub>	CD <sub>4</sub>	$\Delta(\text{CD}_4\text{--CH}_4)$
$r(\text{C}\cdots\text{Rh})$	3.190	3.226	0.036
$r(\text{X}\cdots\text{Rh})$	2.071	2.111	0.040
$r(\text{C-X})$	1.119	1.115	–0.004
$r(\text{C-X}[\text{upper}])$	1.112	1.105	–0.007



**Fig. 2** Optimised adsorption structure of CH<sub>4</sub> on Rh(111) surface. The symbols used in Table 1 are also illustrated here. X indicates H or D in CH<sub>4</sub>/CD<sub>4</sub>.

**Table 2** Adsorption energy ( $E_{\text{ads}}$ ) (eV) of CH<sub>4</sub>/CD<sub>4</sub> on Rh(111) surface

	CH <sub>4</sub>	CD <sub>4</sub>	$\Delta(\text{CD}_4\text{--CH}_4)$
$E_{\text{ads}}(\text{CPLB, surface})$	–0.402	–0.396	0.006

**Table 3** The NBO charges of the interacting H/D atom in CH<sub>4</sub>/CD<sub>4</sub> with Rh(111) and the total charges of CH<sub>4</sub>/CD<sub>4</sub>

	CH <sub>4</sub>	CD <sub>4</sub>	$\Delta(\text{CD}_4\text{--CH}_4)$
Interacting H/D	0.249	0.242	–0.008
CH <sub>4</sub> /CD <sub>4</sub>	0.053	0.049	–0.004

adsorption. In the surface model calculation of the PBCs,  $4 \times 4 \times 1$   $k$ -points were sampled using the Monkhorst–Pack grid method.<sup>28</sup> For the LO-based electronic structure calculations, the modified Gaussian16 program package<sup>29</sup> embedded with the MC\_DFT method<sup>18</sup> was used to take into account the NQEs of protons and deuterons. For electrons, the LanL2DZ basis set with an effective core potential<sup>30–32</sup> was used for Rh atoms, and the 6-31G(d,p) basis set was used for other atoms in the APFD method.<sup>33</sup> For the nucleus, the single  $s$ -type Gaussian-type function,  $\exp\{-\alpha(r - R)^2\}$ , was used for each protonic and deuteronic basis function. The  $\alpha$  values for protons and deuterons were set to the standard values of 24.1825 and 35.6214, respectively.<sup>34</sup>

The on-top site on the Rh(111) surface was found to be the most stable site for CH<sub>4</sub> adsorption compared to face-centered cubic and hexagonal close-packed sites. Based on these results, a H/D atom in CH<sub>4</sub>/CD<sub>4</sub> was placed at the on-top site on the Rh(111) surface as initial structure obtained by conventional PW approach. The geometry of this system was optimised as follows. First, the position of the surface atoms in the top (1st) layer was optimised using the PW approach. Then, CH<sub>4</sub> was placed at the on-top site, and CH<sub>4</sub> and Rh atoms in the top layer were optimised using the PW approach. Finally, the atomic coordinates of CH<sub>4</sub>/CD<sub>4</sub> were optimised using the CPLB method including the MC\_DFT approach as an LO part under the condition of fixed Rh atoms on the surface.

## Results and discussion

In this study, we show and discuss the results of the optimised geometry parameters, adsorption energy, and charges for CH<sub>4</sub>/CD<sub>4</sub> adsorption on Rh(111) surface. The optimised parameters for adsorbed CH<sub>4</sub>/CD<sub>4</sub> are listed in Table 1. The symbols used in Table 1 are illustrated in Fig. 2.

In Table 1,  $\Delta(\text{CD}_4\text{--CH}_4)$  is the difference in the optimised parameters between CH<sub>4</sub> and CD<sub>4</sub>. A positive value indicates that the bond distance of CD<sub>4</sub> was longer than that of CH<sub>4</sub>. Since  $r(\text{C}\cdots\text{Rh})$  is the distance between C the nearest neighbour (just below) Rh atom, its value was considered as the adsorption distance of the CH<sub>4</sub>/CD<sub>4</sub> molecule on the Rh(111) surface. The  $r(\text{C}\cdots\text{Rh})$  of CD<sub>4</sub> was longer than that of CH<sub>4</sub>.

Looking at the geometrical parameters of  $r(\text{X}\cdots\text{Rh})$ , the  $r(\text{D}\cdots\text{Rh})$  in the CD<sub>4</sub> adsorption was longer than that in the CH<sub>4</sub> adsorption as well as  $r(\text{C}\cdots\text{Rh})$ . Furthermore, both  $r(\text{X}\cdots\text{Rh})$  and  $r(\text{C}\cdots\text{Rh})$  are shorter than the values using the conventional PW approach (2.322, 3.429 Å), because of the NQEs. These  $r(\text{C}\cdots\text{Rh})$  and  $r(\text{X}\cdots\text{Rh})$  geometrical H/D isotope effect for the CH<sub>4</sub>/CD<sub>4</sub> adsorption showed the similar trend as the difference of adsorption distance of C<sub>6</sub>H<sub>12</sub>/C<sub>6</sub>D<sub>12</sub> that is observed in the experiments by Koitaya *et al.*<sup>10</sup> In contrast, the  $r(\text{C-D})$  of CD<sub>4</sub> was shorter than that of CH<sub>4</sub>. Compared to the C–X distance in isolated CH<sub>4</sub>/CD<sub>4</sub> (1.113/1.106 Å), which is calculated by the MC\_DFT method, we clearly observed the same trend of geometrical H/D isotope effect. The H/D isotope effect that the covalent bond distance of the C–D bond is shorter than that of the C–H bond was due to the anharmonicity of the potential. Furthermore, both  $r(\text{C-D})$  and  $r(\text{C-H})$  are longer than the C–H/C–D distance in isolated CH<sub>4</sub>/CD<sub>4</sub> owing to the interaction between CH<sub>4</sub>/CD<sub>4</sub> and the Rh(111) surface. These results indicate that the geometrical changes due to D substitution for H were opposite in the  $r(\text{C}\cdots\text{Rh})$  and covalent  $r(\text{C-X})$  cases and H/D atomic adsorption on the Pd(111) surface.<sup>21</sup> The difference in  $r(\text{C}\cdots\text{Rh})$  is similar to the Ubbelohde effect observed in typical hydrogen-bonded systems.<sup>35,36</sup> Hence, the C $\cdots$ Rh interaction was considered to be different from H/D atomic adsorption and essentially the same as the typical hydrogen-bonded systems.<sup>37</sup> In addition, this result indicates that the interaction between CD<sub>4</sub> and Rh(111) was weaker than in CH<sub>4</sub> case.

Further, we analysed the adsorption energy of CH<sub>4</sub>/CD<sub>4</sub> on the Rh(111) surface, and the results are listed in Table 2. The



adsorption energy of CH<sub>4</sub> on the Rh(111) surface was defined as follows;

$$E_{\text{ads}} = E_{\text{tot}} - (E_{\text{surf}} + E_{\text{CH}_4}) \quad (3)$$

where  $E_{\text{ads}}$  is the adsorption energy of CH<sub>4</sub> on the Rh(111) surface,  $E_{\text{tot}}$  is the total energy of CH<sub>4</sub> adsorbed on the Rh(111) surface, and  $E_{\text{surf}}$  and  $E_{\text{CH}_4}$  are the total energies of the Rh(111) surface model and CH<sub>4</sub> molecule, respectively. A negative  $E_{\text{ads}}$  value indicates stable adsorption of CH<sub>4</sub> on the Rh(111) surface. The  $E_{\text{ads}}$  of CD<sub>4</sub> was lower than that of CH<sub>4</sub>. The  $E_{\text{ads}}$  difference of CH<sub>4</sub>/CD<sub>4</sub> showed the same trend as C<sub>6</sub>H<sub>12</sub>/C<sub>6</sub>D<sub>12</sub> adsorption, which was observed in the experiments performed by Koitaya *et al.*<sup>10</sup> We also confirmed that CD<sub>4</sub> has a weaker interaction with the Rh(111) surface than CH<sub>4</sub>.

Finally, we performed a natural bond orbital (NBO) analysis<sup>38</sup> during the LO calculation. The NBO charges of the interacting H/D atom with the Rh(111) surface and the total charges of CH<sub>4</sub>/CD<sub>4</sub> are listed in Table 3. Different NBO charges were observed in the interacting H/D atom and the total charges of CH<sub>4</sub>/CD<sub>4</sub>. The charges around the H atom (0.249) were larger than those around the D atom (0.242). This observation suggests that the number of electrons around the proton is lower than that around the deuteron. In the CH<sub>4</sub>/CD<sub>4</sub> molecule, the total charge around the CH<sub>4</sub> molecule (0.053) was larger than around CD<sub>4</sub> (0.043), which showed a similar trend of interacting H/D atoms. In fact, the magnitude of the dipole moment of CH<sub>4</sub> (0.465 D) was slightly larger than that of CD<sub>4</sub> (0.415 D) expectedly. These results suggest that the number of electrons transferred to the Rh(111) surface was larger in CH<sub>4</sub> than that in CD<sub>4</sub>, and CH<sub>4</sub> has a stronger interaction with the Rh(111) surface than CD<sub>4</sub>.

## Conclusions

We studied CH<sub>4</sub>/CD<sub>4</sub> adsorption on Rh(111) surface to analyse and understand the H/D isotope effect on the molecules that are adsorbed on metal surfaces. We developed the CPLB method for highly accurate calculation for analysis of molecular adsorption on metal surfaces, which is difficult to calculate using conventional methods. Consequently, we observed the H/D isotope effects in terms of adsorption distance, adsorption energy, and charge. Our results suggest that the mechanism of molecular adsorption on metal surfaces differs from that of atomic adsorption. Furthermore, the molecular adsorption shows the H/D isotope effects that are similar to those observed in conventional hydrogen-bonded systems. Based on these observations, we confirm that our developed CPLB approach is effective in reproducing the H/D isotope effects on CH<sub>4</sub>/CD<sub>4</sub> adsorption on metal surfaces. The extension to other atomic or molecular adsorption on various types of surface would be possible in the framework of CPLB approach. Moreover, the CPLB approach is expected to be a powerful tool for analysing H/D isotope effects on various phenomena, such as adsorption, desorption, absorption, and catalysis, that involve atoms/molecules on heterogeneous systems such as surfaces and bulk systems.

## Conflicts of interest

There are no conflicts to declare.

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