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# The impact of the composition and solidification rate on the microstructure and the crystallographic orientations of $\text{Al}_2\text{O}_3$ –YAG– $\text{ZrO}_2$ eutectic solidified by the micro-pulling down technique

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Directional solidification experiments have been carried out in eutectic and off eutectic composition in  $\text{Al}_2\text{O}_3$ –YAG– $\text{ZrO}_2$  system using the micro-pulling down ( $\mu$ -PD) technique. The formation of different microstructures of stable phases, over a range of velocities studied, is discussed. During the solidification process, coupled growth microstructure can occur at off eutectic composition. Colonies and dendrites were analysed as a function of the composition and velocity. Increasing the solidification rate resulted in a smaller grain size and instability of the crystallization interface with respect to  $\text{ZrO}_2$  segregation at the solidification front. Increasing  $\text{ZrO}_2$  in the eutectic composition showed enhanced tendency for colony and dendrite formation. When the velocity was extended to the rapid solidification regime ( $>1.75 \text{ mm min}^{-1}$ ), the geometrical pattern microstructure was found to grow and a change in the growth orientation of  $\text{Al}_2\text{O}_3$  corresponding to  $c$ -axis (0 0 01) was observed. Whatever the pulling rate, during the eutectic solidification the  $\text{Al}_2\text{O}_3$  and  $\text{ZrO}_2$ :Y phases' growth competition was observed, and  $\langle 100 \rangle$  YAG orientation was grown along the pulling direction.

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## 1. Introduction

Despite the very different needs for particular materials, eutectic materials have shown remarkable consistency in large technological applications such as nanotechnology and electronics.<sup>1–7</sup> Today, there is a clear need to produce performed materials more economically and with higher reproducibility and quantity than possible currently. Among the eutectic ceramic material family, the  $\text{Al}_2\text{O}_3$ –YAG– $\text{ZrO}_2$  (ref. 8–10) ternary system is of great importance. Eutectic materials have a number of properties, which make them interesting as potential engineering materials.<sup>11–13</sup> In addition to their utilization in gas turbine engines, they can be used in ships and eventually in aircraft turbines.<sup>14,15</sup> The use of these materials in aeronautics will depend not only on superior engineering design, but also more importantly on the availability of the eutectic ceramic with a significant advantage in high-temperature morphology and microstructure over the presently available metals and alloys. With the melting temperature around  $1750^\circ\text{C}$ , the system is stable and presents performed mechanical properties.<sup>16–19</sup> Most of their physical and mechanical properties are heavily dependent on the microstructure and morphology.

Various experimental works have been carried out on the solidification of eutectic oxide materials by different processes

and varying results have been obtained. Viechnicki and Schmid<sup>20,21</sup> studied eutectics using Bridgman furnace with molybdenum crucibles and a thermal gradient of approximately  $200^\circ\text{C cm}^{-1}$ . Non-uniform “Chinese script” microstructures were obtained. Waku *et al.*<sup>22</sup> successfully grew eutectics with uniform microstructure using Bridgman furnace and molybdenum crucible. Borodin *et al.*<sup>23</sup> and L. Carroz *et al.*<sup>24,25</sup> investigated eutectics by the Edge-defined Film Growth (EFG) method. They suspected that the non-uniformities of microstructures were caused mainly by the instability of the plane crystallization front because of constitutional supercooling. Borodin *et al.*<sup>26</sup> studied eutectics by the Verneuil growth method mainly used for sapphire crystal growth. However, homogeneous microstructures were never obtained. The floating zone crucible free method using laser or lamp as heating source<sup>27–32</sup> has been used to solidify unidirectional eutectic materials. However, in the floating zone, microstructures are often influenced by grain size materials containing many grain boundaries, which are not thermodynamically stable, and at high temperatures the grain boundary area tends to be reduced by grain growth. This technique is mainly used to obtain samples for specific characterization. Solidification of eutectic materials can be done by lowering the temperature below the melting point, which is a versatile method for solidification.<sup>33</sup> The micro pulling down ( $\mu$ -PD) technique has been used to grow eutectic fibers, rods and plates to investigate the microstructure at very high growth rate ( $0.1$ – $10 \text{ mm min}^{-1}$ ).<sup>34–40</sup> Melt convection is

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suppressed by the use of a narrow nozzle, due to the capillary effect. It is easy to control the eutectic shape and composition. By the  $\mu$ -PD technique, the basic solidification parameters such as the growth kinetics and compositional stability can be made clear before undertaking the Bridgman and EFG growth techniques. Most cited papers describe the particular characteristics of oxide eutectics. It has been found to be difficult to control the microstructure of the  $\text{Al}_2\text{O}_3$ -YAG-ZrO<sub>2</sub> eutectic system.

Numerous compositions around the 65 mol%  $\text{Al}_2\text{O}_3$ -16 mol%  $\text{Y}_2\text{O}_3$ -19 mol%  $\text{ZrO}_2$  eutectic point have been studied in order to identify the coupled growth zone.<sup>39–42</sup> It has been shown that depending on the eutectic composition, the solidification process and the growth parameters, the resulting microstructure consists of two phases (YAG,  $\text{Zr}(\text{Y})\text{O}_2$ ) distributed in sapphire ( $\text{Al}_2\text{O}_3$ ) matrix. The experimental works carried out<sup>17,43–50</sup> for eutectic compositions highlight the influence of solidification parameters: growth rate, chemical composition and thermal gradient. Depending on the pulling rate conditions, the microstructure will also undergo transitions linked to the destabilization of the interface.<sup>49,51,52</sup>

Despite the different studies, experimental data for the directional solidification of oxide eutectics (processing difficulties, microstructure instabilities) are still limited and often uncertain. A systematic study of the microstructure is strongly needed before eutectic ceramic oxides can be fully developed for application. Recently, more fundamental questions are being answered with key investigation in the directional solidification method where the processing parameters such as solidification rate and composition of the eutectic are individually controlled. There is a great need for continued effort in this direction. In

this paper, as a function of the pulling rate, experimental results on  $\text{Al}_2\text{O}_3$ -YAG-ZrO<sub>2</sub> ternary eutectic and off eutectic solidified by the micro pulling down technique are analyzed and discussed to ascertain the solidification parameters controlling the resultant microstructure and morphology.

## 2. Experimental procedure

High-purity (>99.99%)  $\text{Al}_2\text{O}_3$ ,  $\text{Y}_2\text{O}_3$  and  $\text{ZrO}_2$  powders were mixed in an agate mortar according to the ternary eutectic composition 65 mol%  $\text{Al}_2\text{O}_3$ /16 mol%  $\text{Y}_2\text{O}_3$ /19 mol%  $\text{ZrO}_2$ .<sup>23,31,41</sup> The mixture was sintered at 1400 °C for 10 hours in air atmosphere. Eutectic ceramic materials were directionally solidified from the melt using the micro-pulling down technique in the same conditions presented in our previous work.<sup>39,40</sup> In addition to the eutectic composition, we studied five different compositions around the eutectic mixture (Fig. 1). The detailed compositions are shown in Table 1.

The room-temperature X-ray diffraction patterns were obtained using a Bruker D8 advanced diffractometer with  $\text{Cu-K}\alpha_1$  and  $\text{Cu-K}\alpha_2$  X-rays ( $\lambda = 0.15406$  and  $0.15444$  nm). Scanning was done over a  $2\theta$  range from 10° to 100° in steps of 0.02° with a counting time of 16 s per step and continuous rotation (20 rpm) around the growth direction. SEM observations of the rods were performed with a Phenom desktop scanning electron microscope (FEI) at 5 kV. The composition of the solidified samples was evaluated by the inductively coupled plasma (ICP) emission and energy-dispersive X-ray spectroscopy (EDX) techniques. The TEM experiment and electronic diffraction pattern investigation were carried out using a CM20-FEG transmission electron microscope.

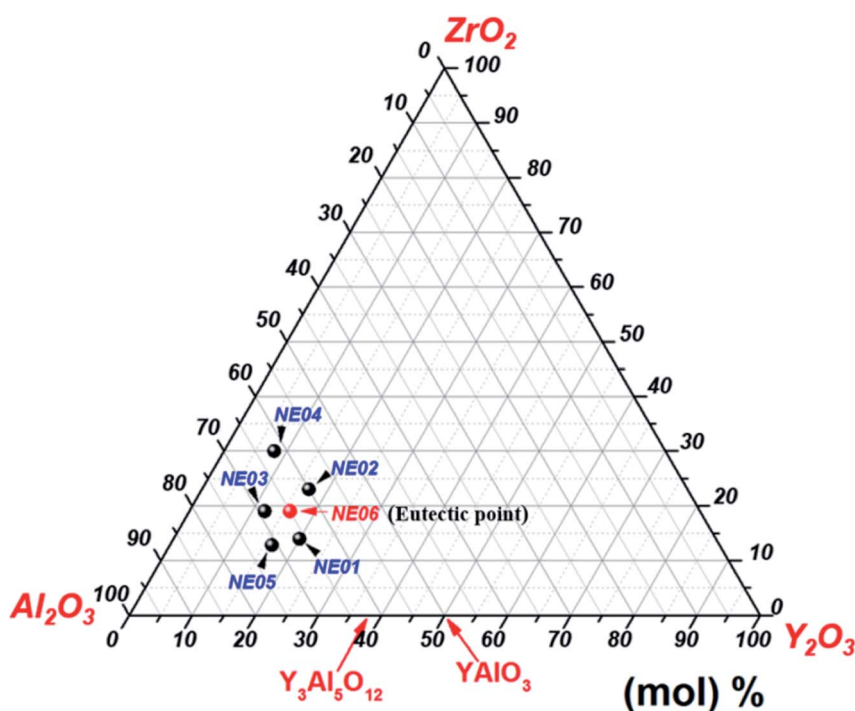


Fig. 1 The different compositions prepared by solid-state reaction and solidification.

**Table 1** Studied compositions in the  $\text{Al}_2\text{O}_3$ –YAG– $\text{ZrO}_2$  ternary diagram

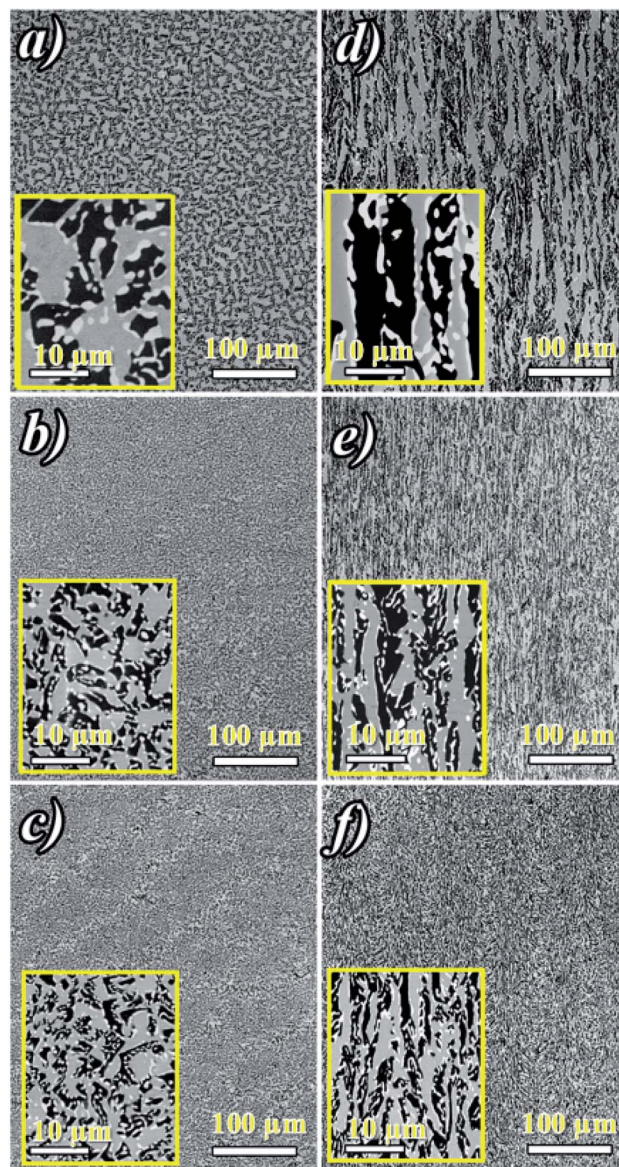
Reference	$\text{Al}_2\text{O}_3$ (mol%)	$\text{Y}_2\text{O}_3$ (mol%)	$\text{ZrO}_2$ (mol%)
NE01	66	20	14
NE02	60	17	23
NE03	69	12	19
NE04	62	8	30
NE05	71	16	13
NE06 (eutectic)	65	16	19

### 3. Results

#### 3.1. Eutectic solidification and microstructure

Fig. 2a shows ceramic the eutectic 5 mm diameter rods (65 mol%  $\text{Al}_2\text{O}_3$ /16 mol%  $\text{Y}_2\text{O}_3$ /19 mol%  $\text{ZrO}_2$ ) (NE06) and Fig. 2b shows the (NE01  $\rightarrow$  NE05) rods solidified in the vicinity of the eutectic composition. A ceramic eutectic seed 3 mm in diameter was used to initiate the growth process. In the case of the eutectic composition (NE06), whatever the pulling rate, the solidified eutectic rods exhibit a white colour with smooth surface without any visible macroscopic defects such as cracks and bubbles.

Fig. 3a–c show the SEM images of the transverse sections solidified at 0.1, 0.5 and 1  $\text{mm min}^{-1}$  cut from the middle region of the eutectic composition rods. Most part of the zirconia precipitates (white) are completely imbedded in the alumina (black)/YAG (light) interfaces and some of them are localized on the sapphire host. In the longitudinal section (Fig. 3d–f) the alumina host and YAG phase exhibit a broken-lamellar morphology aligned along the growth direction. For the three solidification rates, a homogeneous morphology exempt of voids and a lamellar microstructure are observed. The morphology architecture is Chinese script, which is in good agreement with ref. 40, 41 and 43. The use of high pulling rate (1  $\text{mm min}^{-1}$ ) has led to an extensive area of apparent heterogeneities in which a Chinese script microstructure with colonies and inhomogeneous phase distribution are observed (Fig. 3c and f). The microstructure is fine for the solidification rate of 1  $\text{mm min}^{-1}$ . As a function of the pulling rate ( $v$ ), the lamellar spacing ( $\lambda$ ) in the ceramic rods corresponds to  $\lambda^2 v = \text{constant}$ . It being approximately  $6.5 \pm 1.3 \mu\text{m}$  when the solidification rate ( $v$ ) is 0.1  $\text{mm min}^{-1}$ ,  $3.6 \pm 0.5 \mu\text{m}$  at  $v = 0.5 \text{ mm min}^{-1}$  and  $2.9 \pm 0.5 \mu\text{m}$  at  $v = 1 \text{ mm min}^{-1}$  is in good agreement with ref. 25, 39 and 40.



**Fig. 3** Eutectic (NE06) microstructure evolution as a function of pulling rate. The dark region is  $\text{Al}_2\text{O}_3$ , the light region is YAG and the white region is  $\text{ZrO}_2$  – transverse sections: (a)  $v = 0.1 \text{ mm min}^{-1}$ , (b)  $v = 0.5 \text{ mm min}^{-1}$ , (c)  $v = 1 \text{ mm min}^{-1}$  – longitudinal sections: (d)  $v = 0.1 \text{ mm min}^{-1}$ , (e)  $v = 0.5 \text{ mm min}^{-1}$ , (f)  $v = 1 \text{ mm min}^{-1}$ .



**Fig. 2**  $\text{Al}_2\text{O}_3$ –YAG– $\text{ZrO}_2$  ternary eutectic and off eutectic rods pulled from the melt by  $\mu$ -PD technique. (a) (1)  $v = 0.1 \text{ mm min}^{-1}$ , (2)  $v = 0.5 \text{ mm min}^{-1}$ , (3)  $v = 1 \text{ mm min}^{-1}$ . (b) (NE01  $\rightarrow$  NE05) off eutectic rods solidified at a pulling rate of  $0.5 \text{ mm min}^{-1}$ .





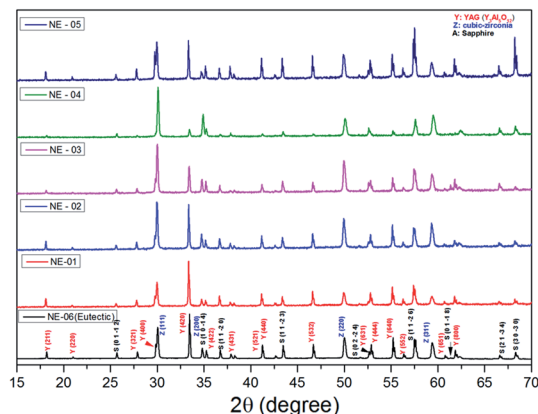
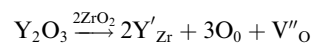


Fig. 4 Room-temperature powder XRD patterns of crushed  $\text{Al}_2\text{O}_3$ /YAG/ $\text{ZrO}_2$  eutectic and off eutectic composition.

The eutectic rods being solidified at low pulling rates ( $0.1\text{--}0.5\text{ mm min}^{-1}$ ) by the coupled growth of two phases (YAG, sapphire) and dispersion of irregular  $\text{ZrO}_2$  in a continuous  $\text{Al}_2\text{O}_3$  matrix leading to a homogeneous microstructure is in good agreement with these investigations: ref. 29, 39, 40, 53 and 54. Except NE02 compound, because of the continued composition evolution of (NE01, NE03, NE04 and NE05) samples in the  $\text{Al}_2\text{O}_3\text{--Y}_2\text{O}_3\text{--ZrO}_2$  ternary equilibrium diagram,<sup>41</sup> during the solidification process it was quite difficult to control these systems. The surface samples were rough and slightly yellow coloured. As eutectic composition, mainly  $\text{Al}_2\text{O}_3$ , YAG and  $\text{ZrO}_2$  phases were observed (Fig. 4). To quantify the concentration of yttrium in the YZT phase and verify the chemical composition of  $\text{Al}_2\text{O}_3$  and YAG phases, EDX measurements were performed on the samples. Except for the YZT grains, which exhibited an important concentration of yttrium atoms due to the substitution of Zr by Y in the  $\text{ZrO}_2$  phase, the composition of YAG and  $\text{Al}_2\text{O}_3$  phases were very close to the stoichiometric theoretical composition. The concentration of  $\text{Y}_2\text{O}_3$  varied approximately from 8 (NE04) to 20 mol% (NE01), in good agreement with the selected compositions in Table 1 from the  $\text{Al}_2\text{O}_3\text{--Y}_2\text{O}_3\text{--ZrO}_2$  equilibrium diagram. This result was confirmed by ICP analysis

and revealed that the compositions of the solidified materials were very close to the prepared composition. On account of the stability of the melt and the no volatility of  $\text{Y}_2\text{O}_3$ ,  $\text{Al}_2\text{O}_3$  and  $\text{ZrO}_2$  compounds during the solidification process, this result was expected.

The lattice parameters of each of the phases obtained from X-ray powder diffraction are shown in Table 2. Grinding the samples makes it possible to overcome the phenomena of texturing and distortion due to the internal stresses of the material at room temperature. These internal stresses originate from the difference in the thermal expansion coefficients of the  $\text{Al}_2\text{O}_3$ , YAG and  $\text{ZrO}_2$  phases.<sup>55–57</sup> In the case of the eutectic point (NE06), the results are very similar between micro-pulling down, EFG, floating zone and Bridgman,<sup>24,39,58,59</sup> which shows that the elaboration method does not have a significant effect on the lattice parameters of the isolated phases. The lattice parameters of the alumina phase are close to the theoretical values and the YAG phase has a slightly lower lattice parameter. The  $\text{ZrO}_2$  is a cubic structure stabilized by  $\text{Y}_2\text{O}_3$ . The lattice parameter ( $a$ ) from the X-ray diffraction is averaged. The zirconia lattice parameter depends on the substitution of yttrium content according to Vegard law.<sup>60</sup> The lattice parameter ( $a$ ) is between  $0.51506\text{ nm}$  and  $0.51621\text{ Å}$ . It is calculated from the diffraction patterns and has a standard deviation error of  $\approx 0.0004\text{ nm}$ , which corresponds to an error in the  $\text{Y}_2\text{O}_3$  content. The  $\text{Y}_2\text{O}_3$  content is therefore about  $17.32 \pm 0.37\text{ mol\%}$ . Even with the many published papers, it is difficult to identify the source of error. It must be noted that the lattice parameter ( $a$ ) measured in this study is in very good agreement with the data from ref. 61 and 62. The mechanism of solid solution of  $\text{Y}_2\text{O}_3$  in cubic  $\text{ZrO}_2$  was established by F. Hund<sup>63</sup> as substitutional replacement of  $\text{Y}^{3+}$  ions on  $\text{Zr}^{4+}$  cationic sites with a charge-compensation number of vacant anionic sites following the chemical reaction:



The creation of these vacancies ( $\text{V}''$ ) is thought to stabilize the cubic polymorphs. S. M. Ho<sup>64</sup> proposed that Zr ions in all of the polymorphs prefer a 7-fold coordination of oxygen, and that

Table 2 Lattice parameters of  $\text{Al}_2\text{O}_3$ , YAG and  $\text{ZrO}_2$  as a function of the composition

	$\text{Al}_2\text{O}_3$ $R\bar{3}c$	$\text{Y}_3\text{Al}_5\text{O}_{12}$ (YAG) $Ia\bar{3}d$	$\text{ZrO}_2$ $Fm\bar{3}m$ <sup>60</sup>
Lattice parameters from PDF files	$a = 0.47932\text{ nm}$ (ref. 65) $c = 1.29925\text{ nm}$	$a = 1.20062(2)\text{ nm}$ (ref. 66)	
NE01	$a = 0.47581\text{ nm}$ $c = 1.29940\text{ nm}$	$a = 1.20070(3)\text{ nm}$	$a = 0.51603(4)\text{ nm}$
NE02	$a = 0.47653\text{ nm}$ $c = 1.30108\text{ nm}$	$a = 1.19998(4)\text{ nm}$	$a = 0.51586(3)\text{ nm}$
NE03	$a = 0.47686\text{ nm}$ $c = 1.29369\text{ nm}$	$a = 1.19902(2)\text{ nm}$	$a = 0.51552(4)\text{ nm}$
NE04	$a = 0.47547\text{ nm}$ $c = 1.29600\text{ nm}$	$a = 1.19753(2)\text{ nm}$	$a = 0.51506(4)\text{ nm}$
NE05	$a = 0.47583\text{ nm}$ $c = 1.29882\text{ nm}$	$a = 1.20079(3)\text{ nm}$	$a = 0.51621(4)\text{ nm}$
NE06 (eutectic)	$a = 0.47684\text{ nm}$ $c = 1.29133\text{ nm}$	$a = 1.19931(2)\text{ nm}$	$a = 0.51561(4)\text{ nm}$



the lattice arranges itself to achieve this symmetry. By the creation of vacancies, the coordination number of the Zr atom is decreased for the cubic lattice, thereby reducing the normal fluorite structure of 8-fold to a 7-fold coordination.

Fig. 5 shows the transversal and longitudinal microstructure evolution as a function of the composition under a pulling rate of  $0.5 \text{ mm min}^{-1}$ . All the (NE01  $\rightarrow$  NE05) samples present heterogeneities and exhibit variation in the microstructures and the morphology. As the eutectic composition, the black regions correspond to the  $\alpha\text{-Al}_2\text{O}_3$  phase, the light regions to YAG and the white one corresponds to the  $\text{ZrO}_2\text{:Y}$  phase. Depending on the composition, the  $\text{ZrO}_2\text{:Y}$  and YAG phases do not grow at the same conditions. For the (NE01  $\rightarrow$  NE05) compositions, different morphologies such dendrites, cells and colonies were observed. In contrast, the sample NE02 close to the NE06 eutectic point showed enhanced tendency for colony formation. However, higher alumina concentration ( $>62\%$ ) (NE01, NE03 and NE05) favored the formation of cellular and dendritic microstructures. Depending on the composition, the transition from coupled to cellular and dendritic microstructure can be connected to the concept of competitive growth. The variation of the microstructure for (NE01  $\rightarrow$  NE05) showed a clear tendency of the three phases to grow in preferred directions. In the eutectic point, the microstructure strongly depends on the growth rate and the crystallization thermal gradient,<sup>25,39,40,57–59</sup> but the samples (NE01  $\rightarrow$  NE05) around the eutectic point (NE06) solidified at the same conditions presented a microstructure dispersion strongly affected by the chemical composition. In the sample NE04 corresponding to higher  $\text{ZrO}_2$  concentration (30 mol%), the grain size and the aspect shape of  $\text{ZrO}_2$  as well as the morphology and the domains were heterogeneous. In addition, some zirconia grains (white) were interconnected differently than in the other samples. The compositional range of the eutectic for coupled growth in the ( $\text{Al}_2\text{O}_3\text{--YAG}$ ) binary and ( $\text{Al}_2\text{O}_3\text{--YAG--ZrO}_2$ ) ternary systems was narrow and any deviation from the eutectic composition generated a complex metastable morphology and even secondary phases,<sup>67</sup> which were not observed in this work. The NE03 and NE05 samples corresponding to the higher alumina concentration showed sapphire domains, the average size was around  $50 \mu\text{m}$  (NE03) and the elongated  $\text{Al}_2\text{O}_3$  lamellas reached  $250 \mu\text{m}$  (NE05). The NE03 sample presented broken YAG lamellas nested between segregated zirconia precipitates (Fig. 5h). Moreover, the NE01 sample corresponding to the higher concentration of  $\text{Y}_2\text{O}_3$  (20%) showed YAG lamellas of length varying from 25 to  $200 \mu\text{m}$ . Some lamellas were continued and slightly tilted from the rod axis. In all (NE01  $\rightarrow$  NE05) samples, the colony microstructures were surrounded by small eutectic microstructures. Outside the eutectic point, the microstructure changed dramatically with the composition; the morphology and the rate of transformation and the nucleation behaviour were affected by the amount of  $\text{Y}_2\text{O}_3$  and  $\text{ZrO}_2$ . Whatever the composition, an overheating of the melt up to  $2000^\circ\text{C}$  was not accompanied by the formation of  $\text{YAlO}_3$  perovskite as it was observed in previous works using the EFG and floating zone methods.<sup>24,25,67,68</sup> According to these results, there is a variety of microstructural features, which can be

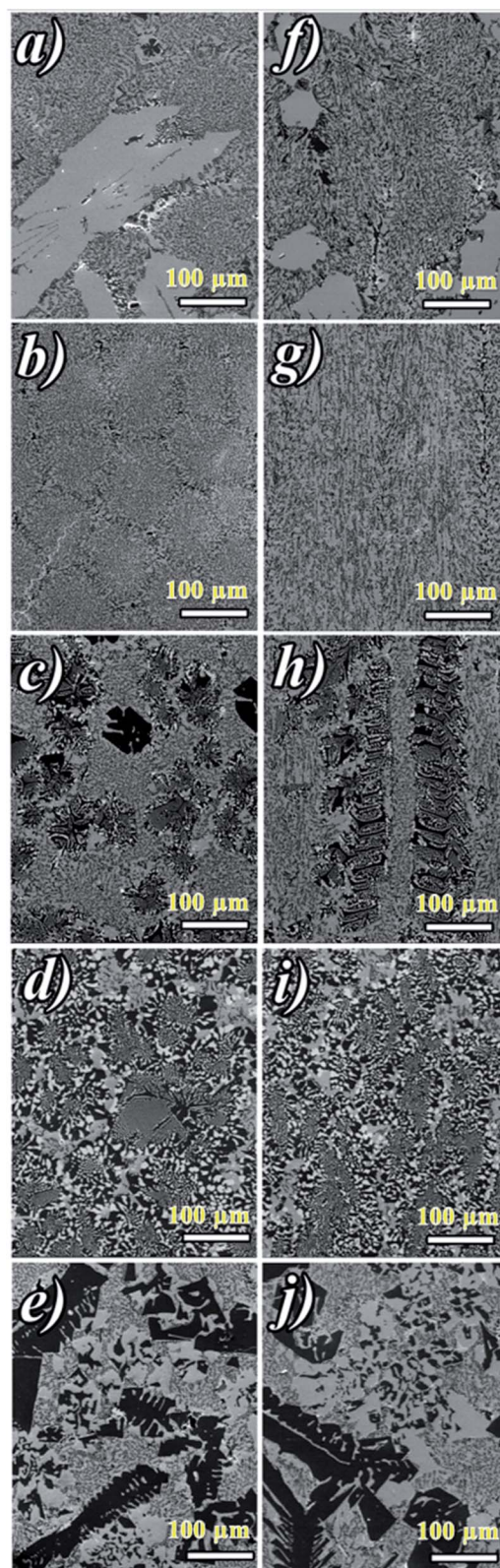


Fig. 5 Microstructure of off eutectic composition solidified at a pulling rate of  $0.5 \text{ mm min}^{-1}$ . Transversal sections: (a) (NE01), (b) (NE02), (c) (NE03), (d) (NE04), (e) (NE05), longitudinal sections: (f) (NE01), (g) (NE02), (h) (NE03), (i) (NE04), (j) (NE05).





expected to be the cause for the different growth velocities and chemical compositions. For eutectic composition, Chinese script eutectic growth was observed from low to moderate growth rate and colonies for higher velocities. For off-eutectic composition, dendrites and cells were surrounded by eutectic composition.

### 3.2. Crystallographic analysis

Fig. 6 shows the room-temperature X-ray diffraction patterns of the eutectic (NE06) and off eutectic (NE01 → NE05) rods transversal sections as a function of the composition and pulling rate. They often grow preferentially along well-defined crystallographic orientations that are not necessarily the directions of easy growth of the compounds, but correspond to the structures of minimum interfacial energy as reported in ref. 39, 40 and 55. For low pulling rate ( $v = 0.1$  and  $0.5 \text{ mm min}^{-1}$ ), in the case of the eutectic composition (NE06), the preferred growth direction of  $\text{Al}_2\text{O}_3$  is  $(0\bar{1}10)$ , that of YAG is  $(100)$  and that of  $\text{ZrO}_2$  is  $(100)$ , which are in good agreement with that reported in ref. 27 and 69. For high solidification rate ( $1 \text{ mm min}^{-1}$ ) the crystallographic planes have become  $(0\bar{1}12)$  for  $\text{Al}_2\text{O}_3$ ,  $(100)$  and  $(410)$  for YAG and finally  $(110)$  for the zirconia phase, consistent with that reported in ref. 39 and 40. Except for the NE02 sample, the crystallographic orientations of NE01, NE03, NE04 and NE05 samples are different than that of the eutectic point (NE06). For the NE03, NE04 and NE05 compositions, the preferred growth directions of the  $\text{Al}_2\text{O}_3$ /YAG/ $\text{ZrO}_2$  are determined as  $(0\bar{1}10)$   $\text{Al}_2\text{O}_3$  and additional  $(1\bar{1}26)$   $\text{Al}_2\text{O}_3$  pick for

NE04,  $(100)$ ,  $(521)$  and  $(532)$  for YAG and  $(100)$ ,  $(110)$  and  $(311)$  for  $\text{ZrO}_2$ . The NE01 sample corresponding to higher  $\text{Y}_2\text{O}_3$  concentration (20%) presents additional YAG peaks such  $(521)$  and  $(532)$  showing other YAG crystallographic orientations. It is clear that in addition to the competitive growth directions, there is a competitive growth of orientation relationships between the interfaces during the solidification imposed by the major phase.

Fig. 7 shows two plan-view TEM micrographs of transverse sections of the eutectic rods solidified at  $0.1 \text{ mm min}^{-1}$  (Fig. 7a) and  $1 \text{ mm min}^{-1}$  (Fig. 7b), respectively. The A, B, C regions correspond, respectively, to the  $\alpha$ - $\text{Al}_2\text{O}_3$ , YAG and zirconia phases. We observed some zirconia grains with specific regular facets (Fig. 7b). The average sizes of the facets depended on the pulling rate and varied from  $0.5 \pm 0.1 \mu\text{m}$  at  $1 \text{ mm min}^{-1}$  to  $1.5 \pm 0.1 \mu\text{m}$  at  $0.1 \text{ mm min}^{-1}$ .

In order to investigate the crystallographic relationship in the plane of the transversal section of rods, the electron diffraction pattern (SAED) was analyzed in three regions (A, B and C in Fig. 7a and b) of two eutectic samples solidified at  $0.1$  and  $1 \text{ mm min}^{-1}$ . The regions A, B, C correspond, respectively, to the  $\alpha$ - $\text{Al}_2\text{O}_3$ , YAG and zirconia phases. Whatever the solidification rate, the YAG cubic phase is oriented along the  $[100]$  direction. At the pulling rate of  $0.1 \text{ mm min}^{-1}$ , the trigonal sapphire grains are oriented along  $[0\bar{1}10]$  and become<sup>12–35</sup> at the pulling rate of  $1 \text{ mm min}^{-1}$ . The zirconia grains of the cubic structure are oriented along  $[100]$  and became  $[110]$  at  $1 \text{ mm min}^{-1}$ . The SAED patterns also show that the zirconia

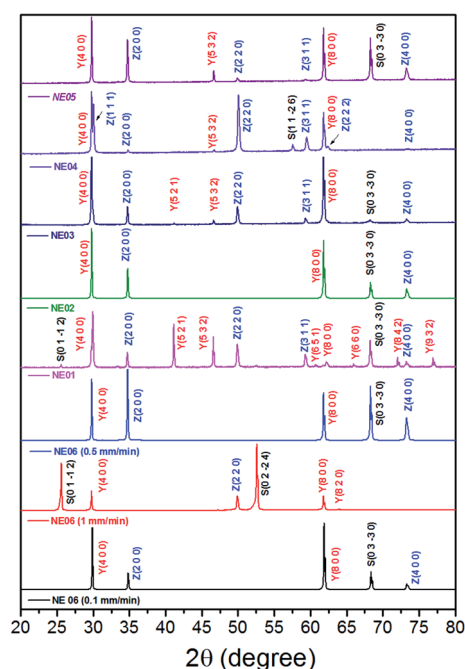


Fig. 6 Room-temperature bulk XRD patterns of the transversal sections of  $\text{Al}_2\text{O}_3$ /YAG/ $\text{ZrO}_2$  eutectic and off eutectic composition. The off eutectic samples were grown under a pulling rate  $0.5 \text{ mm min}^{-1}$  and three pulling rates ( $0.1$ ,  $0.5$  and  $1 \text{ mm min}^{-1}$ ) were used for the eutectic composition.

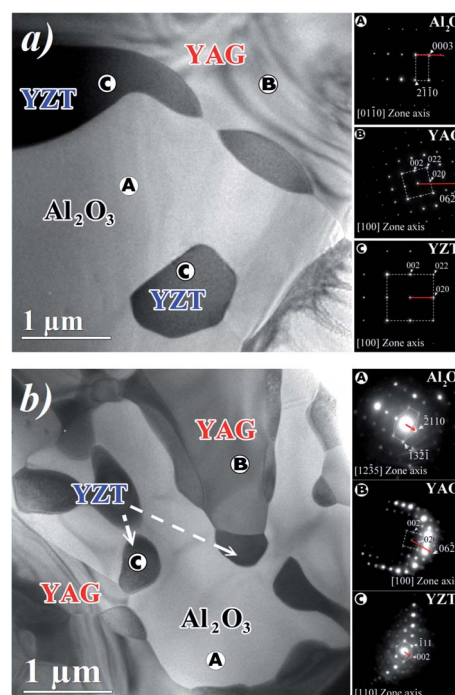


Fig. 7 Transversal TEM micrograph of  $\text{Al}_2\text{O}_3$ -YAG- $\text{ZrO}_2$  eutectic microstructure: (a)  $0.1$  and (b)  $1 \text{ mm min}^{-1}$ . The black region is the  $\text{ZrO}_2$  phase, the light grey region is the YAG phase and the dark grey is the  $\alpha$ - $\text{Al}_2\text{O}_3$  phase. (A), (B) and (C) regions correspond to the position of SAED measurement.

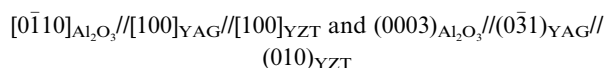


Table 3 Eutectic growth relations as a function of solidification process

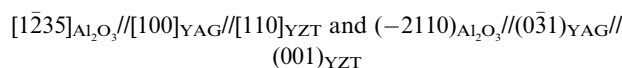
Eutectic	Solidification process	Growth relations	Ref.
Al <sub>2</sub> O <sub>3</sub> –YAG–ZrO <sub>2</sub>	Bridgman	$\langle -2130 \rangle_{\text{Al}_2\text{O}_3} // \langle 100 \rangle_{\text{ZrO}_2} // \langle 100 \rangle_{\text{YAG}}$	1
Al <sub>2</sub> O <sub>3</sub> –(9% Y <sub>2</sub> O <sub>3</sub> ) ZrO <sub>2</sub>	Floating zone	$[0\bar{1}10]_{\text{Al}_2\text{O}_3} // [001]_{\text{ZrO}_2}$ $(2\bar{1}10)_{\text{Al}_2\text{O}_3} // (100)_{\text{ZrO}_2}$	70
Al <sub>2</sub> O <sub>3</sub> –YAG–ZrO <sub>2</sub>	Floating zone	$[\bar{1}100]_{\text{Al}_2\text{O}_3} // [100]_{\text{YAG}} // [100]_{\text{ZrO}_2}$ $(1\bar{1}20)_{\text{Al}_2\text{O}_3} // (004)_{\text{YAG}} // (002)_{\text{ZrO}_2}$ $(0003)_{\text{Al}_2\text{O}_3} // (040)_{\text{YAG}} // (020)_{\text{ZrO}_2}$	71
Al <sub>2</sub> O <sub>3</sub> –YAG–ZrO <sub>2</sub>	EFG	$[\bar{1}010]$ or $[0\bar{1}10]_{\text{Al}_2\text{O}_3} // [001]_{\text{YAG}} // [001]_{\text{ZrO}_2}$ $(\bar{1}210)$ or $(2\bar{1}10)_{\text{Al}_2\text{O}_3} // (100)_{\text{YAG}} // (100)_{\text{ZrO}_2}$ $(0001)$ or $(\bar{2}\bar{1}10)_{\text{Al}_2\text{O}_3} // (010)_{\text{YAG}} // (010)_{\text{ZrO}_2}$	59
Al <sub>2</sub> O <sub>3</sub> –YAG–ZrO <sub>2</sub>	μ-PD	Three kinds of orientations: $\langle 3030 \rangle$ and $\langle 0001 \rangle$ for Al <sub>2</sub> O <sub>3</sub> , $\langle 001 \rangle$ and $\langle 220 \rangle$ for zirconia, $\langle 800 \rangle$ and $\langle 111 \rangle$ for YAG	72
Al <sub>2</sub> O <sub>3</sub> –YAG–ZrO <sub>2</sub>	μ-PD	$[0\bar{1}10]_{\text{Al}_2\text{O}_3} // [100]_{\text{YAG}} // [100]_{\text{YZT}}$ and $(0003)_{\text{Al}_2\text{O}_3} // (0\bar{3}1)_{\text{YAG}} // (010)_{\text{YZT}}$ $[1\bar{2}35]_{\text{Al}_2\text{O}_3} // [100]_{\text{YAG}} // [110]_{\text{YZT}}$ and $(-2110)_{\text{Al}_2\text{O}_3} // (0\bar{3}1)_{\text{YAG}} // (001)_{\text{YZT}}$	This work

grains located at the interface between sapphire and YAG have the same orientation as zirconia grains embedded in the sapphire host. As a function of the solidification rates, in the observation plane, the crystallographic relations between the phases are:

0.1 mm min<sup>-1</sup>:



1 mm min<sup>-1</sup>:



However, as reported in Table 3, the eutectic growth axis corresponds to well-defined crystallographic relations between the solidified phases and depends on the solidification process.

The solidification of the eutectic by floating zone method results in the material having the smallest phase sizes.<sup>20,59</sup> The eutectics obtained from the EFG and micro-pulling down methods have a coarser microstructure, the phase sizes being very similar with these two methods. This is in agreement with the thermal gradient estimates along the direction of solidification.<sup>25,69</sup> Indeed, the EFG and micro-pulling down methods exhibit close thermal gradients, while that of the floating zone is assumed to be greater.

### 3.3. Discussion

The sequence of microstructure formation in the eutectic composition is shown in Fig. 8 for one experimental run. The same results were observed for the other experimental runs. After the connection step through eutectic seed, a planar front was formed (Fig. 8a). The mechanism of the formation of the eutectic microstructure depends on the shape of the solidification front, which depends on the pulling rate. At low pulling rate ( $v \leq 0.05$  mm min<sup>-1</sup>), at the beginning of the solidification,

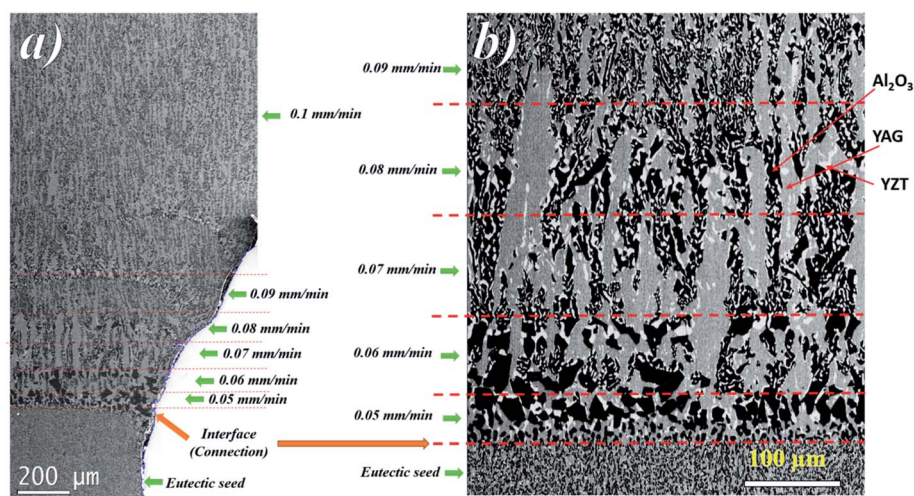


Fig. 8 (a) Sequence of eutectic solidification kinetics after connection by the seed and interface evolution as a function of pulling rates. (b) Al<sub>2</sub>O<sub>3</sub>, YAG and ZrO<sub>2</sub> phases' distribution from the connection and increasing pulling rate step by step until stabilization.





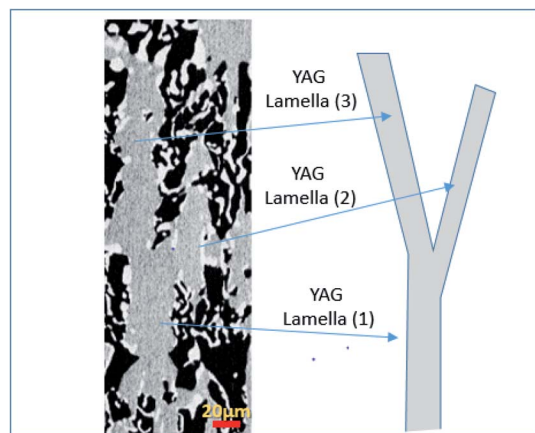


Fig. 9 YAG lamella divided into two lamellas (YAG lamella (1) → YAG lamella (2) + YAG lamella (3)) to catch up with the minimum supercooling conditions for the coupled eutectic growth.

since the melting temperatures of  $\text{Al}_2\text{O}_3$  (2050 °C), YAG (1950 °C), and  $\text{ZrO}_2$  (2715 °C) are higher than the eutectic temperature (1750 °C), solute diffusion between the phases controls the melting of the eutectic microstructure. The first step of the growth ( $v = 0.05 \text{ mm min}^{-1}$ ) shows mainly YAG platelets

oriented along the solidification direction embedded in the continuous  $\text{Al}_2\text{O}_3$ -host (dark phase). The inter-lamellar eutectic average spacing ( $\lambda$ ) is large ( $\approx 25 \mu\text{m}$ ).  $\text{ZrO}_2$  is rejected in the liquid, only a little amount of irregular  $\text{ZrO}_2$  (light phase) is imbedded in the YAG phase (Fig. 8b). Under low pulling rate,  $\text{ZrO}_2$  segregation is observed and alumina matrix is free of the  $\text{ZrO}_2$  phase. This phenomenon is similar to the segregation of rare earth dopants (Nd, Ce) in laser and scintillating YAG single crystal growth.<sup>73,74</sup> At the first step of the growth, the solidification process is close to the  $\text{Al}_2\text{O}_3$ -YAG binary eutectic system.<sup>35,75</sup> By increasing the pulling rate ( $v > 0.07 \text{ mm min}^{-1}$ ), most of the  $\text{ZrO}_2$  accumulated in the interface start to nucleate in the eutectic. When the inter-lamellar spacing ( $\lambda$ ) increases to reach the largest value (25  $\mu\text{m}$ ), the solidification front is destabilized. This phenomenon allows the microstructure to adapt to the interface instabilities. Some YAG lamellas are divided into one and two lamellas to catch up with the minimum supercooling conditions for the coupled eutectic growth. As it is observed in Fig. 9, the new YAG lamella will, therefore, converge towards another lamella of the same phase to reach equilibrium of the eutectic microstructure. By increasing the pulling rate ( $v > 0.08 \text{ mm min}^{-1}$ ), the distance between YAG lamellas decreases, and the temperature at the interface increases due to the decrease in  $\text{ZrO}_2$  rejection in the

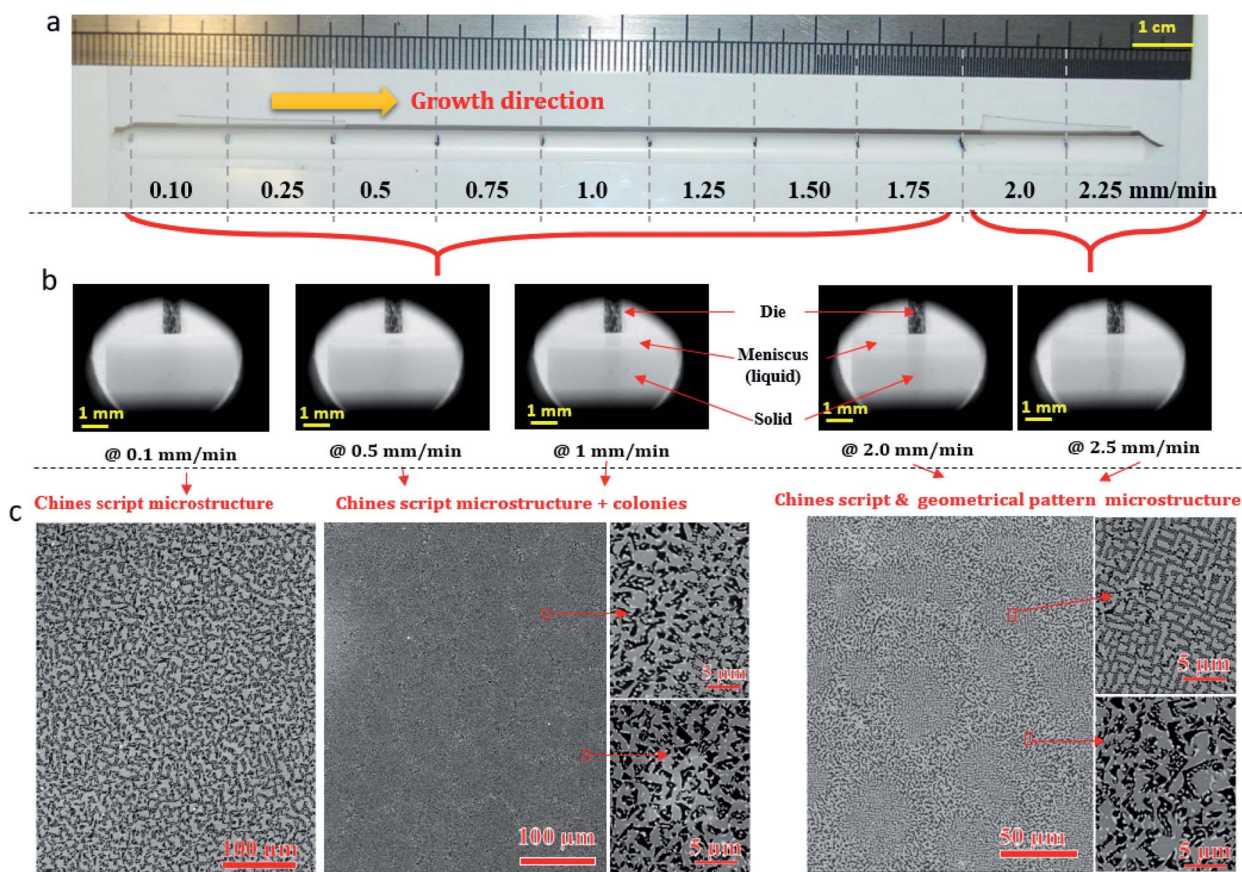


Fig. 10 (a) Eutectic rod solidified at different pulling rates for one run. (b) Evolution of meniscus length and interface shape as a function of the pulling rate. (c) Microstructure variation as a function of the pulling rate. At high pulling rate (2 and  $2.25 \text{ mm min}^{-1}$ ) the microstructure of the center of the colonies is geometrical pattern and the periphery is Chinese script.





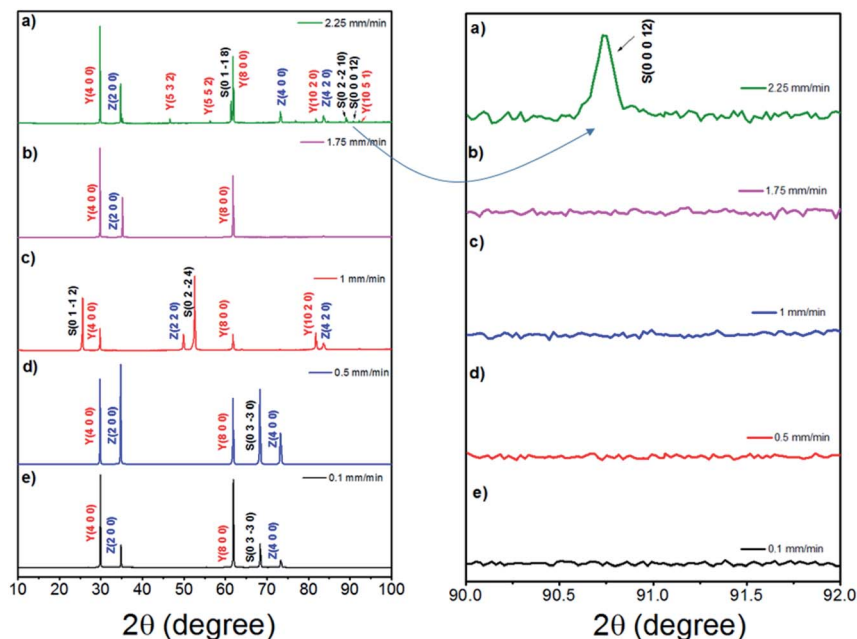


Fig. 11 Room-temperature bulk XRD patterns of the transversal sections of  $\text{Al}_2\text{O}_3/\text{YAG}/\text{ZrO}_2$  eutectic composition as a function of the pulling rate. *c*-Axis direction apparition at a pulling rate  $2.25 \text{ mm min}^{-1}$  corresponds to the change in sapphire orientation.

melt. In such conditions, the solidification interface shape continuously changes, especially close to the periphery of the meniscus, causing a strong thermal gradient affecting the eutectic microstructure and the morphology. The germination difficulties of the  $\text{ZrO}_2$  phase could be the cause of its decoupled growth from the YAG and  $\text{Al}_2\text{O}_3$  phases. As it is shown in Fig. 8, there is a delay in the germination of the  $\text{ZrO}_2$  phase compared to that of the other two phases. The pulling rate gradually increases at the beginning of the solidification. The low pulling speed ( $0.05 \text{ mm min}^{-1}$ ) at the start of the connection does not provide enough supercooling in the  $\text{ZrO}_2$  phase to nucleate. The  $\text{ZrO}_2$  phase only germinates  $200 \mu\text{m}$  after connection. The delay and the difficulty of  $\text{ZrO}_2$  germination can be attributed to the strongly faceted interfaces of this eutectic.

In fact, heterogeneous nucleation on a faceted plane is more difficult than the germination in steps because the germination energy barrier is greater.<sup>76</sup> The interface is observed to become concave at  $0.08 \text{ mm min}^{-1}$ , giving the critical conditions for the planar interface instability.

Three parameters control the coupled eutectic growth: the rate of solidification ( $v$ ), the thermal gradient ( $G$ ) along the direction of crystallization linked to the elaboration method and the deviation from the eutectic composition ( $\Delta C$ ). The microstructure of (NE01  $\rightarrow$  NE05) samples consists of dendrites, colony phases and eutectic microstructure domains. The instability is linked to the off eutectic composition. In this case, the liquidus temperature is higher than the temperature of the eutectic and the excess primary phase is more super-cooled and tends to grow faster than the composite forming faceted crystals (YAG,  $\text{Al}_2\text{O}_3$ ) or dendrites. For a deviation from the eutectic composition, it is possible to increase the rate of solidification to approach the eutectic microstructure. Conversely, it is possible to obtain colonies, dendrites and even

geometrical pattern microstructures with exactly the eutectic composition if the solidification rate is high enough.

The change in the solidification rate from  $0.1 \text{ mm min}^{-1}$  to  $2.25 \text{ mm min}^{-1}$  (Fig. 10a) led microscopically to the change in the flatness of the solidification interface and its destabilization (Fig. 10b). By taking into account the thermal gradient ( $G$ ) and the growth rate ( $v$ ), the interface stability is determined by the critical ratio  $(G/v)c$ . The colony microstructures occur when this ratio is below the critical limit. At low pulling rate ( $0.1 \text{ mm min}^{-1}$ ), as shown in Fig. 10b, a flat interface is observed with a meniscus length of around  $386 \pm 20 \mu\text{m}$ . However, as the pulling rate is increased, the interface shape is destabilized and the meniscus length increases to reach  $892 \pm 20 \mu\text{m}$  at  $1 \text{ mm min}^{-1}$  (Fig. 10b) and form few colony structures not observed at low pulling rate. The amplitude of the thermal gradient ( $G$ ) limits directly the maximum pulling rate at which growing can be realized without unwanted breakdown of the flat liquid–solid interface and the formation of a colony microstructure. A change in the morphology at the center of the colonies appears for a solidification rate higher than  $1.75 \text{ mm min}^{-1}$  (Fig. 10c).

Fig. 10c shows the geometrical pattern microstructure formed at the center of the colonies under solidification rates of 2 and  $2.25 \text{ mm min}^{-1}$ . Then, approaching the edge of the colonies, the Chinese script microstructure is formed because the solidification rate is slower. The phases have a very angular appearance. It is important to mention that the microstructures and the morphology are strongly connected to the growth parameters. Using the same solidification conditions, the system is reproducible.

The crystallographic study (Fig. 11) of the samples solidified at high pulling rate ( $\geq 1.75 \text{ mm min}^{-1}$ ) reveals a change in the growth orientation of  $\text{Al}_2\text{O}_3$ . A new (0 0 0 12) sapphire direction appears corresponding to *c*-axis.

The change in growth direction and the appearance of this type of microstructure can be connected to the anisotropy of



thermal conductivity of a phase which is disoriented according to the most conductive direction of growth to evacuate latent heat. There is indeed anisotropy within alumina, the direction of growth (0001) is more conductive. This observation could be a hypothesis to explain the appearance of this microstructure at high pulling rate ( $2.25 \text{ mm min}^{-1}$ , Fig. 10c). In addition, the microstructure formed by zirconia and alumina is reminiscent of that of the fibrous binary eutectic of these two phases.<sup>29,36</sup>

The ratios of the area fractions of zirconia to alumina from a Chinese script region to a geometric pattern region were estimated. It is 0.35% when the microstructure is Chinese script and 0.29% when the microstructure is geometrical pattern. This value is very close to the condition for obtaining a fibrous microstructure in the  $\text{Al}_2\text{O}_3$ - $\text{ZrO}_2$  eutectic system.<sup>77</sup>

Similar observations were made in the case of the  $\text{Al}_2\text{O}_3$ - $\text{GdAlO}_3$ - $\text{ZrO}_2$  ternary eutectic system with respect to the changes in the surface fraction ratios.<sup>78</sup> The variation in the area fraction from the center to the edge of the colonies could be assigned to a change in composition.

Indeed, Song *et al.*<sup>50</sup> during solidification outside the eutectic point at a given rate, obtained the geometrical pattern microstructure by adding zirconia. This hypothesis could suggest that zirconia is at the origin of the interface destabilization and, therefore, of the colony formation.

## 4. Conclusion

The solidification studies in the  $\text{Al}_2\text{O}_3$ -YAG- $\text{ZrO}_2$  eutectic system show the eutectic microstructures to consist of lamellas of YAG and  $\text{ZrO}_2$ :Y precipitates in an  $\text{Al}_2\text{O}_3$  matrix. The grains are chemically homogeneous and have no impurities. Colony growth is found to be involved in all the samples solidified at high pulling rate ( $v \geq 0.5 \text{ mm min}^{-1}$ ), and it results from interface destabilization and heterogeneity distribution of the  $\text{ZrO}_2$ :Y phase. The rate of solidification also affects the crystallography growth direction of this ternary system. Therefore, the interface shape has to compete with the growth anisotropy in order to stabilize the optimum crystallographic directions. In addition to colony formation, cells and dendrites are observed when the samples are solidified outside the eutectic point.

The Chinese script  $\rightarrow$  geometrical pattern microstructural transition has been observed at high pulling rate ( $v > 1.75 \text{ mm min}^{-1}$ ) and can be connected to the thermal anisotropy of the  $\text{Al}_2\text{O}_3$  phase, which causes a rotation of this phase to facilitate heat release at high speed. In terms of understanding this solidification, the discontinuity of the  $\text{ZrO}_2$ :Y phase, its rejection at the solidification interface, and, therefore, the difficulty of germination confirm the difficulties to control the solidification of this system. The morphology of the microstructure and the crystallography of this system suggest a non-simultaneous growth of the three eutectic phases, the zirconia phase probably solidifying behind the YAG and  $\text{Al}_2\text{O}_3$  phases.

## Conflicts of interest

There are no conflicts to declare.

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