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# Combined mechanistic and genetic programming approach to modeling pilot NBR production: influence of feed compositions on rubber Mooney viscosity†

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Mooney viscosity is an essential parameter in quality control during the production of nitrile-butadiene rubber (NBR) by emulsion polymerization. A process model that could help understand the influence of feed compositions on the Mooney viscosity of NBR products is of vital importance for its intelligent manufacture. In this work, a process model comprised of a mechanistic model based on emulsion polymerization kinetics and a data-driven model derived from genetic programming (GP) for Mooney viscosity is developed to correlate the feed compositions (including impurities) and process conditions to Mooney viscosity of NBR products. The feed compositions are inputs of the mechanistic model to generate the number-, weight-averaged molecular weights ( $M_n$ ,  $M_w$ ) and branching degree (BRD) of NBR polymers. With these generated data, the GP model is used to output the optimal correlation for the Mooney viscosity of NBR. In a pilot NBR production, Mooney viscosity data of NBR predicted by the process model agree quite well with experimental values. Furthermore, the process model enables the analyses of the univariate and multivariate influence of feed compositions on NBR Mooney viscosity, and the variables include the contents of vinyl acetylene and dimer in 1,3-butadiene, as well as the mass flow rate of the chain transfer agent (CTA) in the process. Based on the results, it is recommended to control the content of vinyl acetylene in the 1,3-butadiene feed below 14 ppm and the content of dimer below 1100 ppm. This developed process model would help stabilize NBR viscosity for a better control of the product quality.

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## 1. Introduction

Nitrile butadiene rubber (NBR) is an important raw material for the production of oil-resistant rubbery articles indispensable for the automobile, aeronautics and petroleum industries, due to its excellent oil- and air-proof, heat-resistant physicochemical properties. In industry, NBR is produced generally by a continuous cold emulsion polymerization process with two types of monomers: 1,3-butadiene (Bd) and acrylonitrile (ACN). The product NBR as a polymer has certain averaged molecular weights and its distribution, and also certain branching degrees (BRD) of polymer chains. Mooney viscosity (MV) is a standard parameter for characterizing the elastic properties of rubbery materials, and can be regarded as a measure of rubber molecular weight. It is not only widely used in the quality control of non-vulcanized rubbers,<sup>1</sup> but also is a vital indicator

meaningful for the industrial mixing or molding process of these materials. Therefore, real-time and precise detection of the product Mooney viscosity in the continuous industrial production of NBR is paramount for the quality control of product and its processability thereafter.<sup>2</sup> However, in practice the online detection of Mooney viscosity is nowadays not possible, while standard characterization procedures with the Mooney machine in laboratory is labor-intensive and also takes time,<sup>3</sup> a time lag exists. On the other hand, a reasonable alternative would be prediction of NBR Mooney viscosity *via* a reliable process model, for which direct correlation with good accuracy between the feed compositions including impurities or process conditions and the Mooney viscosity of final NBR products is therefore of both scientific and practice importance. Compared to group contribution, quantitative structure–property relationship (QSPR) models *etc.*, the hybrid model proposed in this study is more suitable for industrial application, and is of reference value for the academic research due to the accuracy and effectiveness of the hybrid model. The developed process model is expected to facilitate the intelligent manufacture of NBR, and rubbery materials alike.

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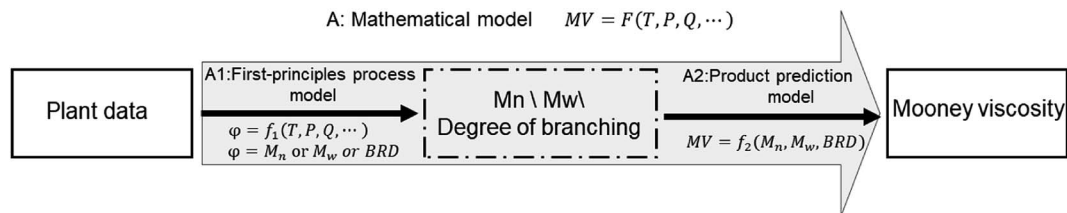
There have been continuous efforts from the industry and academia devoted to modeling the emulsion polymerization process of NBR, though comprehensive and coherent understanding of this complicated process has not yet been reached. Vega *et al.*,<sup>4,5</sup> Minari *et al.*<sup>6,7</sup> and Penlidis *et al.*<sup>8–13</sup> have reported mechanistic models for the NBR production, based on emulsion polymerization kinetics. These mechanistic models could output NBR properties like number-averaged ( $M_n$ ) and weight-averaged molecular weight ( $M_w$ ), however excluding Mooney viscosity. Conventional empirical correlations could relate  $M_n$  and  $M_w$  of a polymer to its (Mooney) viscosity. Such an approach that combines a mechanistic model based on polymerization kinetics and the empirical correlation for Mooney viscosity has been applied by Zubov *et al.* in the dynamic modeling of styrene-butadiene rubber production, to directly correlate the feed compositions and process parameters to Mooney viscosity of rubber products.<sup>14</sup> This approach has not yet been employed in modeling the NBR production. Moreover, it is proved that the accuracy of conventional Mooney viscosity correlation is not satisfactory for industrially produced polymers, which is mostly due to ignorance of chain branching degree of polymers in the correlation.<sup>14,15</sup> For directly investigating the influence of feed compositions and process parameters on Mooney viscosity of NBR, Scott *et al.*<sup>16</sup> performed principal component analysis (PCA) for the process. Only a few data are necessary for PCA, and this method is effective in identifying determining parameters for Mooney viscosity from a large number of parameters. They found that in stationary industrial production of NBR the determining parameters of Mooney viscosity include the compositions of feed and assistant agents, especially the contents of vinyl acetylene and dimer in the monomer 1,3-butadiene.<sup>16</sup> Though the PCA method is simple and convenient, it is not able to reflect the inherent characteristics of the emulsion polymerization process, and no process model that predicts NBR Mooney viscosity has been proposed in the report.<sup>16</sup> Meanwhile, machine learning methods (data models) in the field of data science, including extreme learning machine,<sup>3,17</sup> Generalized Regression Neural Networks (GRNN),<sup>18</sup> Discounted-measurement Recursive Partial Least Squares-Gaussian Process (DRPLS-GP),<sup>19</sup> Ensemble Deep Correntropy Kernel Regression (EDCKR)<sup>20</sup>, Gaussian Process Regression (GPR)<sup>21–23</sup> can also be employed to build the model that correlates feed composition, process conditions and product properties, for fast and accurate prediction of Mooney viscosity. The advantages of this type of method include easy access to input data, less training time, high accuracy of model predictions and convenience to be applied. These advantages make such methods the general option for online prediction of Mooney viscosity (soft measurements) and for the control and optimization of industrial processes. Notably, the variables and process conditions in the industrial rubber production are non-linear, distributed, and fluctuating over time, and are with time-lags, these make the process very complex and intertwined. Data models are strongly dependent on the data set used for the model construction. For example, the data set might only represent some stationary conditions, in which some important variables were stable during the data collection while these

variables actually shifted over even a longer period. However, incorporating more and more variables and considering even longer time period are further complicating the model. Therefore, combing machine learning methods to construct semi-mechanism models, namely hybrid models, can offer accurate predictions for diversified feed composition and process conditions. The model prediction is robust and the results are interpretable.<sup>24–26</sup> We think, for accurately predicting Mooney viscosity of NBR produced in an industrial process, one has to combine a mechanistic model and a data-driven model for Mooney viscosity correlation. The mechanistic model is based on emulsion polymerization kinetics for simulating the number-averaged and weight-averaged molecular weight ( $M_n$ ,  $M_w$ ), as well as branching degree (BRD) of polymers since for the correlation of Mooney viscosity BRD shall also be integrated.

The combination of mechanistic and data-driven models is well suited for the descriptive however strongly-intertwined problems in the chemical industry. As reported in open literature,<sup>8–12</sup> mechanistic models based on emulsion polymerization kinetics have been shown predictive for the NBR production process. Compared to mechanistic models, data-driven models can be built easier without knowing the detailed mechanisms of the process.<sup>27,28</sup> So, the branching degree of polymers can be easily integrated into the correlation between Mooney viscosity and  $M_n$ ,  $M_w$  of polymers, with a data-driven model. Genetic Programming (GP) is able to generate non-linear mapping between inputs and outputs,<sup>17,29,30</sup> consequently it is a powerful tool to deal with the Mooney viscosity correlation of non-linear characteristics. GP has been applied successfully in the field of chemical engineering and materials science,<sup>31</sup> like building stationary<sup>32,33</sup> and dynamic<sup>34,35</sup> process models, optimization of distillation sequences,<sup>36</sup> predicting properties of inorganic materials,<sup>37–42</sup> and building vapor–liquid equilibrium models.<sup>43</sup> GP could search for the optimal formula and parameters simultaneously, resulting in compact and explainable representations,<sup>44</sup> which are in turn ideal for the integration with mechanistic models.<sup>43</sup> For the direct prediction of NBR Mooney viscosity based on feed compositions and process parameters, we propose the approach to combing sequentially a mechanistic model and a data-driven model derived from GP. First, the mechanistic model is used for describing the emulsion polymerization process of NBR, and then the data-driven model is to quantify the influence of  $M_n$ ,  $M_w$  and BRD of NBR polymers on Mooney viscosity.<sup>15</sup> Finally, the two models are integrated for the direct prediction of viscosity.

In this work, the continuous emulsion polymerization of NBR is simulated *via* a mechanistic model based on polymerization kinetics, with information of feed compositions, process parameters and experimental data of products from a pilot NBR production process. The mechanistic model is stationary and is used for analyzing the influence of variations in feed compositions and process parameters on the properties of final NBR products, including the molecular weight and its distribution, branching degree of polymers, and the contents of acrylonitrile in NBR polymers, as illustrated by step A1 in Fig. 1. Then, a Mooney viscosity correlation is generated *via* GP, and also validated with experimental data of  $M_n$ ,  $M_w$  and BRD of NBR





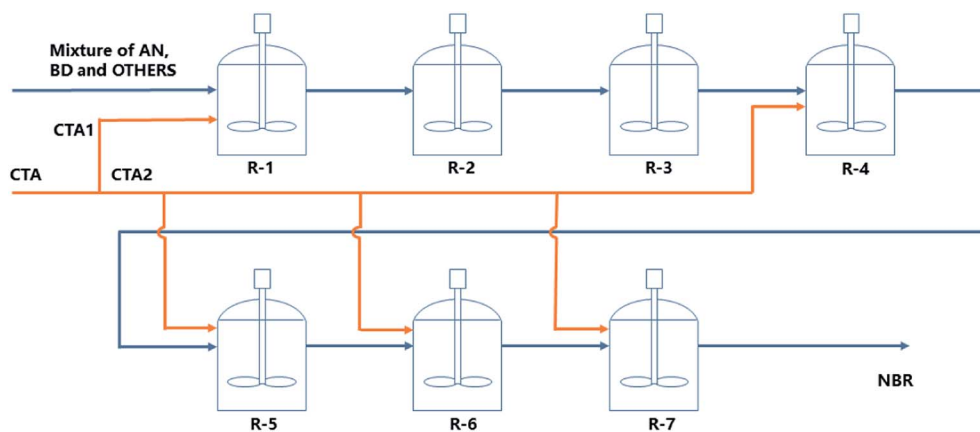
**Fig. 1** A flowsheet illustrating the construction of the process model. A1 is the first step representing the prediction of nitrile-butadiene rubber (NBR) characteristics ( $\varphi$ ) from feed compositions and process parameters via a mechanistic model based upon emulsion polymerization kinetics.  $\varphi$  stands for number-averaged ( $M_n$ ), or weight-averaged molecular weight ( $M_w$ ), or branching degree of polymer chains (BRD). In the function  $\varphi = f_1(T, P, Q, \dots)$ ,  $T, P, Q$  stands for temperature, pressure and mass flow rate of a raw material, respectively. A2 is the second step in which the Mooney viscosity of NBR is correlated to the NBR polymer characteristics via genetic programming (GP). The correlation function of Mooney viscosity (MV) is represented as  $MV = f_2(M_n, M_w, BRD)$ . Step A is the sequential combination of Step A1 and A2, and it builds the process model that directly relates feed compositions, process parameters to the NBR Mooney viscosity, briefly expressed as  $MV = F(T, P, Q, \dots)$ .

polymers, as shown by step A2 in Fig. 1. Finally, the mechanistic model for emulsion polymerization and the data-driven model for Mooney viscosity are combined to build the process model connecting feed compositions and process parameters to NBR Mooney viscosity (step A in Fig. 1). With the developed process model, univariate and multivariate analyses are possible for quantitatively studying the influence of variations in the feed compositions and process parameters on the Mooney viscosity of NBR products. The specific variables include vinyl acetylene and dimer contents in the monomer 1,3-butadiene, and the flow rate of chain transfer agent (CTA, functions as the molecular weight mediator) in the middle of the reactor train (Fig. 2). This work is expected to support the intelligent manufacture of NBR in industry.

## 2. Mechanistic NBR polymerization model

The mechanistic model is based on emulsion polymerization kinetics with data from the NBR production line with an annual capacity of 50 kt located at Lanzhou Petro of Petro-China Company. The relevant polymerization process is

schematically shown in Fig. 2. Seven reactors in a train are used for the continuous cold emulsion polymerization of 1,3-butadiene (Bd) and acrylonitrile (ACN) at 5 °C, and the volume of each reactor is identically 40.88 m<sup>3</sup>. The pressure within the first five reactors (R-1 to R-5 in Fig. 2) is 0.33 MPa, and it is 0.32 MPa in the last two. The monomers, assistant agents (including the CTA, surfactants and dispersion agents) and water at ambient temperature and pressure are mixed in a premixer, and then introduced into the first reactor. Initiator and activator are introduced separately into the first reactor. The stationary rating data of feed compositions for NBR production as shown in Table 1. The CTA is introduced, besides into the first reactor, also into the 4<sup>th</sup> till the 7<sup>th</sup> ones respectively. The total amount of CTA introduced into the 4<sup>th</sup> till the 7<sup>th</sup> reactors is defined as the intermediate CTA amount. The final conversion of monomers (at the outlet of the 7<sup>th</sup> reactor) is controlled to be below 75%, for a better control of the latex product quality. Analysis data of key additives, including sodium dodecylbenzene sulfonate,  $\beta$ -naphthalenesulfonic acid-formaldehyde condensate, diisopropylbenzene hydroperoxide, *tert*-dodecyl mercaptan and formaldehyde condensates are shown in Part 1 of ESI.†



**Fig. 2** The flow scheme of emulsion polymerization process for NBR production. Monomers and assistant agents are introduced into the first reactor of a train of seven reactors, where the polymerization takes place. NBR as products are bled from the 7<sup>th</sup> reactor. The orange lines show the flow scheme of the chain transfer agent and its feeding locations in the process: inlets of the 1<sup>st</sup>, 4<sup>th</sup> till 7<sup>th</sup> reactors in the train.



Table 1 The stationary rating data of feed compositions for NBR production. (unit: kg h<sup>-1</sup>)

#	Feed	Value	Function
1	1,3-Butadiene	3244	Monomer
2	Acrylonitrile	1457	
3	β-Naphthalenesulfonic acid–formaldehyde condensate	93.95	Liquid soap
4	Sodium dodecylbenzene sulfonate	11.75	
5	Diisopropylbenzene hydroperoxide	0.64	Activator
6	Sodium formaldehyde sulfoxylate	1.27	
7	EDTA–FeNa	0.21	
8	EDTA–tetrasodium salt	1.33	
9	Hydroxylamine sulphate	2.35	Terminator
10	Isopropylhydroxylamine oxalate	4.70	
11	Phosphite ester	22.85	Anti-aging agent
12	Phenol	11.42	
13	<i>tert</i> -Dodecyl mercaptan	4.78	Chain transfer agent and deoxidant
14	Sodium hyposulfate	0.42	

### 2.1. General assumptions and polymerization kinetics

In modeling the NBR emulsion polymerization process, general simplifying assumptions as reported in literature<sup>6,10,14</sup> are also adopted. Since the final monomer conversion is controlled to be below 75%, only stages I and II of the Smith–Ewart theory for emulsion polymerization are considered. The polymerization reactions are confined in the polymer particles. The number of polymer particles per unit volume of water ( $N_p$ ) is modeled *via* correlation to the initiator concentration (for simplicity excluding the surfactant concentration), as suggested by the Smith–Ewart theory.<sup>45</sup> The average number of radicals per polymer particle ( $\bar{n}$ ) is simulated *via* the mass balance by considering initiator decomposition, radical desorption and termination, similar to the procedure describe in literature.<sup>10</sup> Each reactor in the train is treated as an isothermal well stirred tank reactor. Model equations, forming a system of differential-algebraic equations (DAEs), were solved simultaneously for all reactors of the cascade using Aspen Polymer Plus<sup>TM</sup>.

The mechanism of NBR emulsion polymerization is free radical polymerization, and important elementary reactions include the propagation reactions, radical transfer reactions, radical termination reactions. Those reactions considered in our modeling are sorted and listed in Appendix A (Table 5). It is necessary to note that the involvement of vinyl acetylene and Bd dimers are also considered in the elementary reactions. The experimentally measured contents of Bd dimers and vinyl acetylene in the feed are chosen as the input values of these two impurities during simulation. Therefore, the model is capable of capturing the influence of these two impurities in the feed. The reaction kinetics parameters, including reaction rate constants ( $k_i$ ) and activation energies ( $E_a$ ), reflect the influence of stoichiometry, temperature and pressure on the reaction rates of elementary reactions and consequently on the average molecular weight of NBR products. Therefore, the accuracy and reliability of the predicted average NBR molecular weight *via* the mechanistic model relies on training these polymerization kinetics parameters. To this end, an array of 29 sets of data from

the pilot NBR production process are used to progressively regress the kinetics parameters of each elementary reaction. The data include the feed compositions and process parameters (intermediate CTA amount), as well as experimental results of  $M_n$ ,  $M_w$ , BRD and ACN contents in the NBR copolymers. The data base for the starting values of these kinetics parameters is as summarized in literature;<sup>10</sup> for those missing, an arbitrary value of the same order of magnitude as similar elementary reactions is assumed. When the object function  $Z$  expressing the difference between the modeled and experimental values of  $M_n$ ,  $M_w$ , BRD and ACN contents are at minimal, the regression is terminated. So, the objective function  $Z$  is defined as:

$$Z = (M_n^{\text{sim}} - M_n^{\text{exp}})^2 + (M_w^{\text{sim}} - M_w^{\text{exp}})^2 + (\text{BRD}^{\text{sim}} - \text{BRD}^{\text{exp}})^2 + (x_{\text{ACN}}^{\text{sim}} - x_{\text{ACN}}^{\text{exp}})^2 \quad (1)$$

The regressed values of the kinetics parameters are also listed in Appendix A (Table 5).

### 2.2. Molecular weight and branching degree of NBR polymers

The aim of the mechanistic model is to output  $M_n$ ,  $M_w$ , BRD of NBR polymers. These parameters are simulated *via* Aspen Polymer Plus<sup>TM</sup> package, with important formula shown below.<sup>10</sup> The tri- and tetra-functional branching frequencies of NBR polymers ( $\overline{\text{BN}}_3$ ,  $\overline{\text{BN}}_4$ ) have to be computed prior to the calculation of the average branching degree BRD.

$$M_n = M_{\text{eff}} \frac{V_p Q_1}{V_p Q_0} \quad (2)$$

$$M_w = M_{\text{eff}} \frac{V_p Q_2}{V_p Q_1} \quad (3)$$

$$\overline{\text{BN}}_3 = \frac{V_p Q_0 \overline{\text{BN}}_3}{V_p Q_0} \quad (4)$$



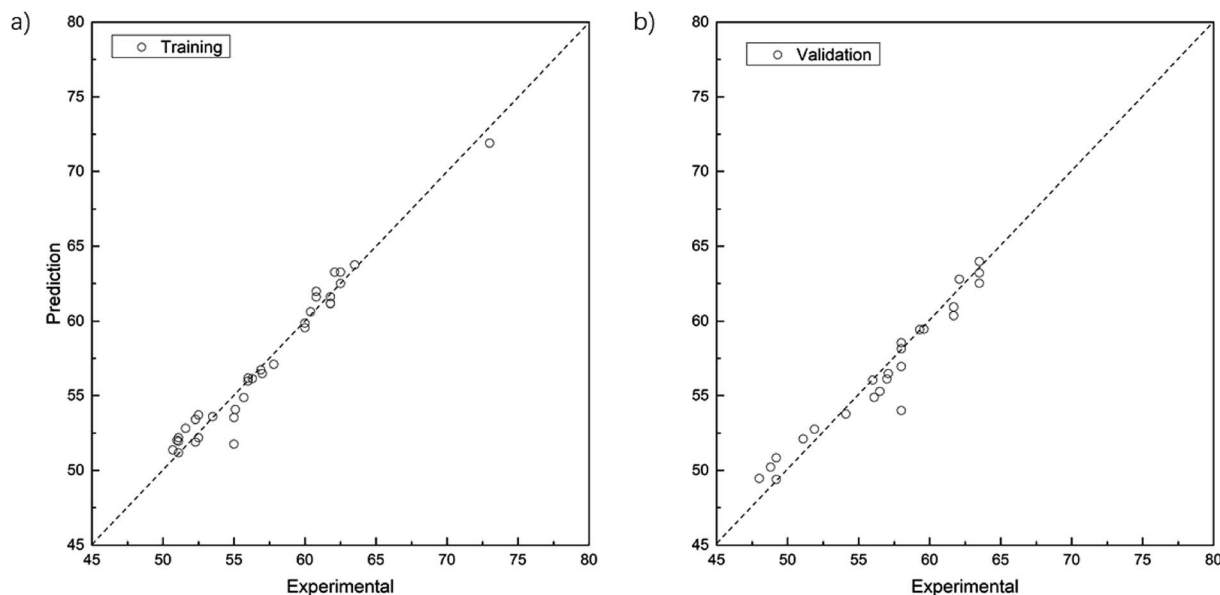


Fig. 3 Parity plots between experimental Mooney viscosity values and those predicted by the linear regression model. (a) The training set contains 34 groups of experimental data. (b) The test set contains 24 groups of experimental data. The ordinate indicates the predicted values and the abscissa the experimental ones. The dashed diagonal line stands for parity.

$$\overline{\text{BN}}_4 = \frac{V_p Q_0 \overline{\text{BN}}_4}{V_p Q_0} \quad (5)$$

$$\text{BRD} = (\overline{\text{BN}}_3 + \overline{\text{BN}}_4) / M_w \quad (6)$$

where  $M_{\text{eff}}$  stands for the effective molecular weight of monomers;  $V_p Q_0$ ,  $V_p Q_1$ ,  $V_p Q_2$  are the first three moments of the molecular weight distribution (MWD) defined on a mole basis and are states of the model;  $V_p$  is the volume of the polymer particle;  $V_p Q_0 \overline{\text{BN}}_3$ ,  $V_p Q_0 \overline{\text{BN}}_4$  are the zeroth moments of the tri- and tetra-functional branching distributions.<sup>10</sup>

### 3. The predictive model for Mooney viscosity

The data-driven model in this work is for correlating the  $M_n$ ,  $M_w$ , BRD of NBR to its Mooney viscosity, with the experimental data of NBR products from the last reactor in the train (Fig. 2). Based on the fundamental work of Kramer and co-workers<sup>46</sup> correlated  $\log M_n$ ,  $\log M_w$  of styrene-butadiene rubber to its log MV by fitting the experimental data, which led to

$MV = a\sqrt{M_n M_w} + b$ . In this correlation,  $a$  and  $b$  are constants, and the coefficient of determination in the linear regression ( $R^2$ ) is 0.94.<sup>46</sup> Later on, this correlation has been widely adopted in the study of NBR. Our analyses with the experimental data of NBR in this work, however, show that this correlation is rather poor and the  $R^2$  of the regression is only 0.763 (cf. Fig. S1 in ESI†). As a result, it is necessary to establish an optimal correlation with the experimental data.

For establishing an optimal correlation for NBR Mooney viscosity, we employ two empirical modeling techniques: GP and linear regression model, with the latter as a benchmark. A total of 58 groups of experimental data are randomly put into a training set and a test set, with a size ratio of 6 : 4. This means that 34 groups of data are for training the model, while the rest 24 groups are used to assess the generalization of the model. The experimental data include  $M_n$ ,  $M_w$ , BRD of NBR, as briefly shown in Table 2. Either with the training set or with the test set, the Mooney viscosity values predicted by the model are compared to corresponding experimental ones, and mean square errors (MSE), mean absolute errors (MAE) and coefficients of determination ( $R^2$ ) are calculated.

Table 2 The training and test data set used for establishing Mooney viscosity model

Input variables	Training set		Test set	
	min	max	min	max
$M_n$ (Da)	59 409	10 7500	69 529	101 773
$M_w$ (Da)	178 856	503 023	18 8050	364 558
BRD ( $\times 10^6$ )	0.518902	3.449261	1.622368	3.446222

Table 3 Fitted parameters of the linear regression model for Mooney viscosity

Constants	Parameters	Fitted value
$A$		0.3577
$B_1$	$M_n^*$	-0.23055
$B_2$	$M_w^*$	0.472269
$B_3$	BRD*	-0.096426



### 3.1. The linear regression model

The linear regression model for Mooney viscosity is expressed as:

$$y^* = A + \sum_{i=1} B_i x_i^* \quad (7)$$

where  $A$ ,  $B_i$  are model parameters,  $y^*$  is log MV as the model output,  $x_i^*$  the logarithm of inputs. The model has 3 variables as inputs ( $N = 3$ ), namely  $M_n$ ,  $M_w$ , BRD of NBR. For simplicity, numerical values  $10^6$  times the original ones of BRD are used in the calculation. Table 3 lists the fitted parameters of the linear regression model for viscosity.

According to these fitted model parameters, the correlation for Mooney viscosity can be written as follows:

$$MV = 2.279 M_n^{-0.23055} M_w^{0.472269} BRD^{-0.096426} \quad (8)$$

Fig. 3 shows the comparison between experimental and fitted values with data in the training and test sets. For the training set (Fig. 3a), MSE = 0.86, MAE = 0.70,  $R^2 = 0.965$ ; and

for the test set (Fig. 3b), MSE = 1.44, MAE = 0.89,  $R^2 = 0.937$ . It is therefore clear that the accuracy of the linear regression model for the Mooney viscosity prediction requires further improvement.

### 3.2. The genetic programming model

GP is a relatively new development in the field of evolutionary computation, it extends traditional genetic algorithms to symbolic regression.<sup>47</sup> Symbolic regression is one type of machine learning techniques that aims at searching for the optimal mathematic formula describing a correlation. Fig. 4 shows the algorithm of GP, it starts by building a population of naive random formulas to represent a relationship between known independent variables and their dependent variable (targets) in order to predict new data. Each successive generation of programs is then evolved from the one that came before it by selecting the fittest individuals from the population to undergo genetic operations. Such a characteristic of GP makes it well suited for identifying the optimal mathematic formulas describing the relationship between  $M_n$ ,  $M_w$ , BRD of NBR and its Mooney viscosity.

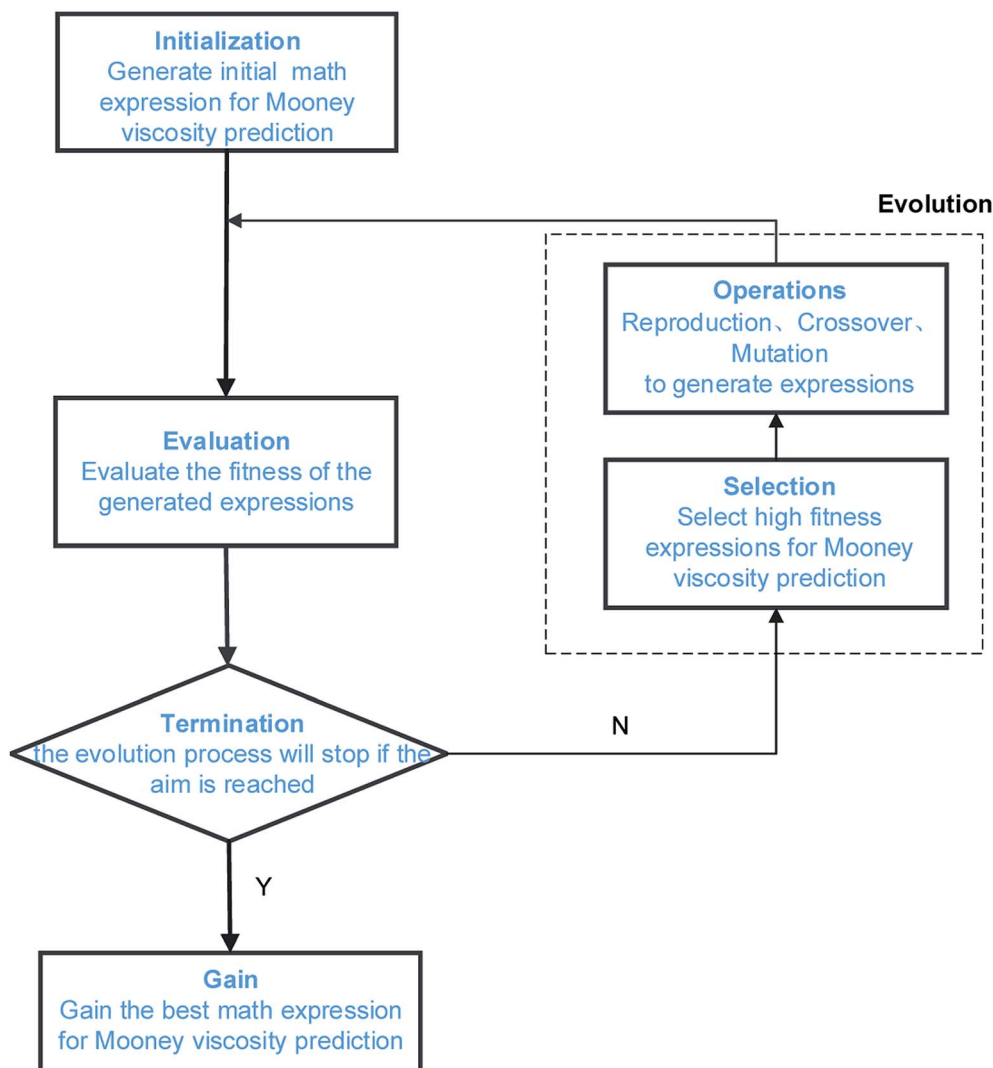


Fig. 4 Illustration of the GP algorithm used for correlating NBR polymer characteristics to its Mooney viscosity.



Table 4 Parameters for genetic programming

Parameters	Value
Dataset	Experimental data
Function library	+, −, *, /, ^, exp, log
Fitness evaluation function	Mean absolute error
Population size	1000
Tournament size	20
Maximum number of generations	275
Probability of crossover	0.7
Probability of performing subtree mutation	0.01
Probability of performing hoist mutation	0.05
Probability of performing point mutation	0.01
Parsimony coefficient	0.001

In this work, we use the toolkit `gplearn` in Python, this toolkit extends the machine learning library of `scikit-learn` and is able to execute GP *via* symbolic regression. The parameters for the GP algorithm are listed in Table 4. The data sets, function library and the fitness function are problem-specific. Here the data sets are the collection of experimental data characterizing each grade of the NBR products, including the  $M_n$ ,  $M_w$ , BRD and corresponding Mooney viscosity values of NBR. The selection of mathematic operators in the function library should be as simple as possible, starting from basic operators (+, −, \*, /) and progressively evolving with square root, exponential, logarithmic and power functions. The final set of math operators is fixed by evaluation of the accuracy of the model training results. The fitness function for GP is the mean absolute error of the fitting results for Mooney viscosity. The population size, maximum number of generations, probability of crossover and mutation, termination conditions shall also be defined for GP. The population size is the search domain, can be obtained after

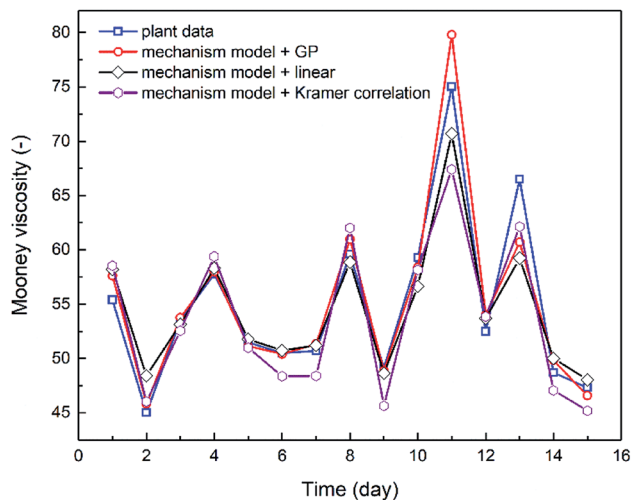


Fig. 6 The final conversion of monomers, experimentally measured or simulated *via* the mechanistic model, for the continuous emulsion polymerization process of NBR. The experimental data are measurement results of samples collected periodically over 29 days in sequence.

multiple runs of the program. The maximum number of generations is the iteration counts, which determines whether the population could evolve to the optimal state. The bigger the population size and the larger the maximum number of generations, the easier to acquire the optimal solution to the problem, however it takes longer for the program to run. The convergence rate of the calculation lies on the probability of mutation. In the GP model to be developed here, it is set at 0.7 to protect the optimal individuals, and such a mutation probability is expected to be efficient and also a balance between the mutation frequencies and the protection of optimal individuals.

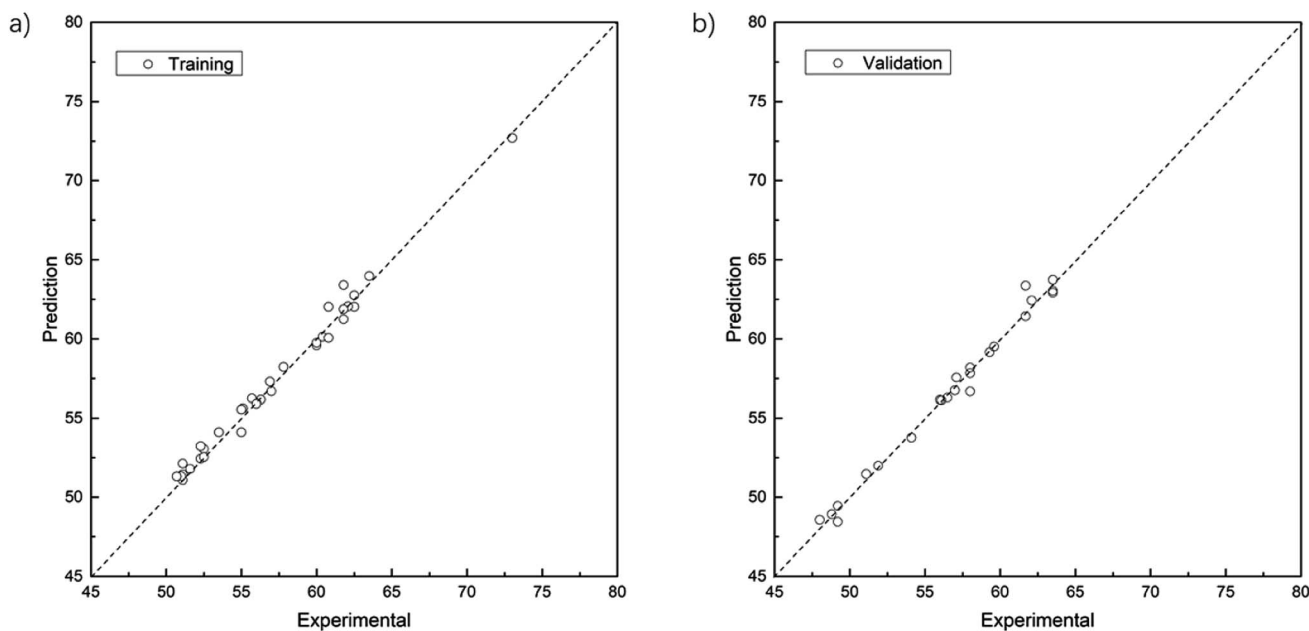


Fig. 5 Parity plots between experimental Mooney viscosity values and those predicted by the GP model. (a) The training set contains 34 groups of experimental data. (b) The test set contains 24 groups of experimental data. The ordinate indicates the predicted values and the abscissa the experimental ones. The dashed diagonal line stands for parity.



According to the preferred criteria of accuracy, simplicity, transparency for a good model, our GP yields such an optimal correlation for NBR Mooney viscosity:

$$MV = 67.724 - 25.76\sqrt{\log(M_n)} + BRD + 0.244M_w^{0.4343} + 0.021BRD^{5.1695462} \quad (9)$$

The parity plots showing the comparison between experimental and simulated values are shown in Fig. 5. For the results of the training data set (Fig. 5a), MSE = 0.33, MAE = 0.45,  $R^2 = 0.986$ ; while for test data set (Fig. 5b), MSE = 0.29, MAE = 0.38,  $R^2 = 0.987$ .

## 4. Results and discussions

### 4.1. The accuracy of mechanistic model for NBR emulsion polymerization

To build the mechanistic model based on emulsion polymerization kinetics, experimental data of the polymer characteristics and the monomer conversion rates are necessary to optimize the reaction rate constants ( $k_0$ ) and activation energies ( $E_a$ ) of each elementary reactions as listed in Appendix A (Table 5). In

a pilot NBR production line, the feed compositions, process parameters and characteristics of NBR polymers in some reactors (mostly the 7<sup>th</sup> reactor, as shown in Fig. 2) were monitored continuously for 29 days by periodic sampling and subsequent analyses. Experimental data thus collected are used for the model optimization. The experimentally analyzed characteristics of NBR polymers include  $M_n$ , polydispersity index (PDI,  $M_w/M_n$ ), BRD and ACN contents in the copolymers. For the calculation of BRD, the Mark-Houwink correlation as reported in literature<sup>48</sup> is used. The radii of gyration ( $R_g$ ) for NBR polymers of different molecular weights, necessary for the calculation, are directly obtained by GPC-MALLS-Viscometer (gel permeation chromatography – multi angles laser light scattering - viscometer). The average branching degrees of NBR polymers, BRD, are calculated with experimental data as reported.<sup>49</sup> The technical details of GPC-MALLS-Viscometer are shown in Part 4 of ESI.† Fig. 6 and 7 show the simulated and experimental values of final monomer conversion rate,  $M_n$ , PDI, BRD and ACN contents in NBR copolymers, and the MSEs of them are  $1.66$ ,  $0.79 \times 10^4$ ,  $0.15$ ,  $0.33 \times 10^{-6}$  and  $0.41$ , respectively. The comparison demonstrates that the developed mechanistic

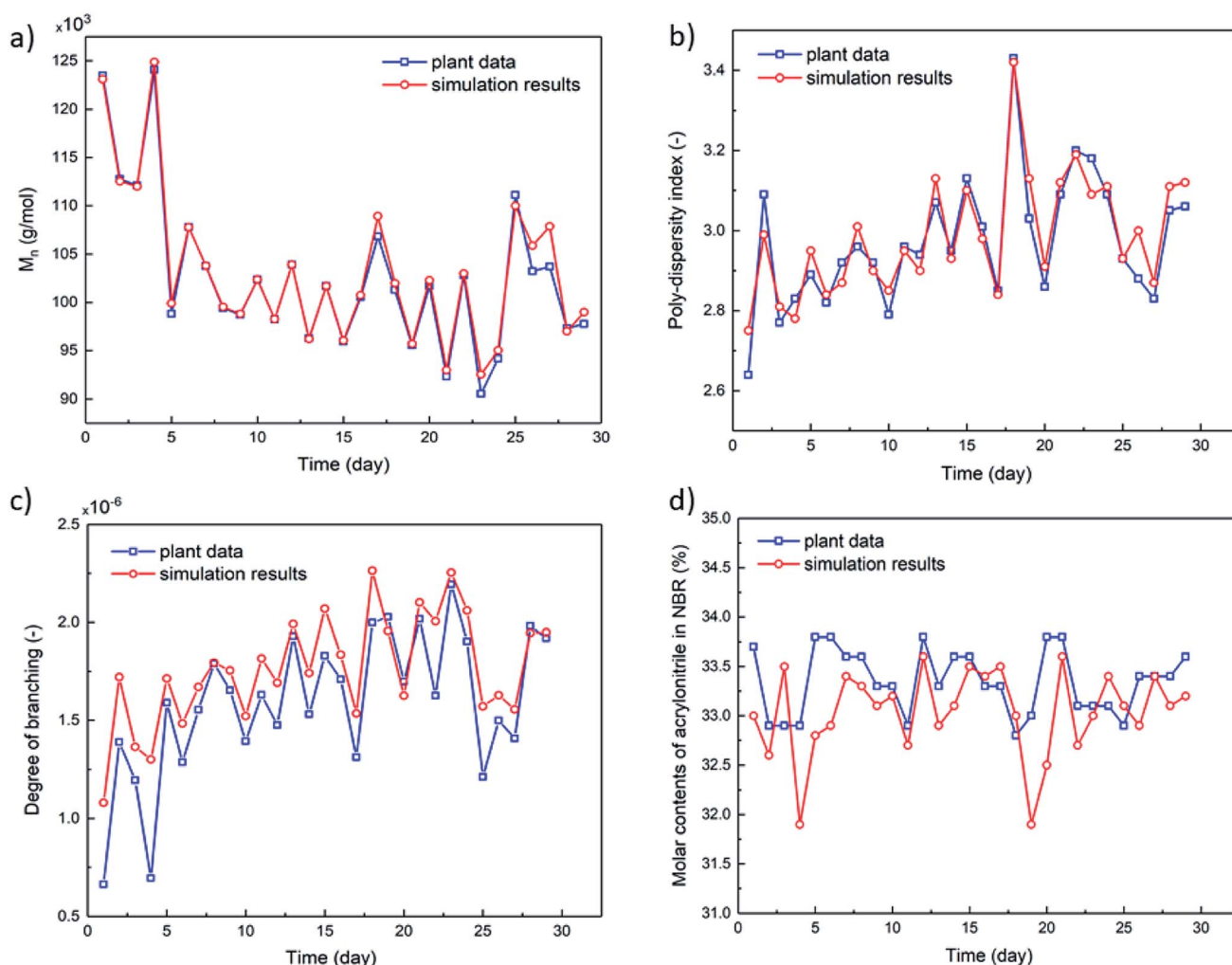


Fig. 7 The characteristics of NBR products, experimentally measured or simulated *via* the mechanistic model: (a)  $M_n$ , (b) PDI, (c) BRD and (d) ACN contents in NBR copolymers. The experimental data are measurement results of samples collected periodically over 29 days in sequence.



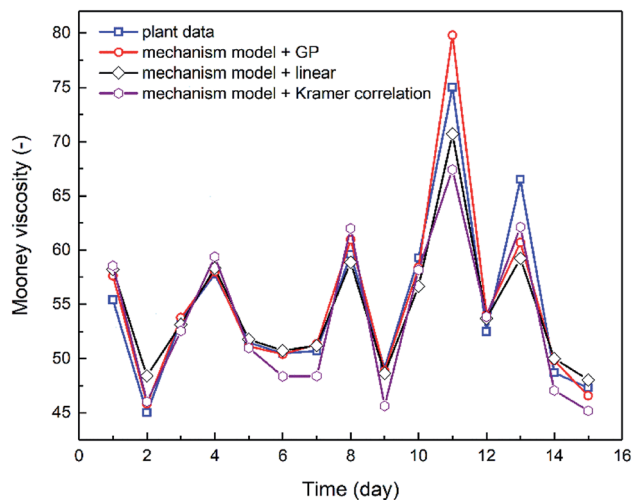


Fig. 8 Comparison between the experimental Mooney viscosity values of NBR over 15 days, and the predicted values from two process models: one is the combination of mechanistic model with GP-derived Mooney viscosity correlation, in the other one the GP-derived correlation is replaced by the correlation resulted from linear regression. The excellent predictive capability of the developed process model is demonstrated.

model based on emulsion polymerization kinetics is accurate and reliable.

#### 4.2. The accuracy of the process model for predicting Mooney viscosity

The combination of the mechanistic model based on NBR emulsion polymerization kinetics (Section 4.1) and the optimal viscosity correlations generated *via* either linear regression or GP (Section 3.2) has established the process model for predicting NBR Mooney viscosity. The process model is then used to predict NBR viscosity directly from a new set of feed compositions, and the comparison between predicted and experimentally measured viscosity values are shown in Fig. 8. The results validate the excellent predictive capability of the process model. The simulation results agree notably better with the experimental data when the GP-derived viscosity correlation (eqn (9)) is used, as compared to when the correlation derived from linear regression (eqn (8)) and Kramer correlation is used. The MSE values for the GP-derived, linear regression-derived models and Kramer correlation are 4.64, 6.85 and 8.63, respectively; and the MAE values are 1.40, 1.78 and 2.38, respectively. These results prove two things: (a) the parameter, average branching degree of NBR polymers (BRD), shall be incorporated into the viscosity correlation for better accuracy of the process model. (b) GP, compared to traditional linear regression method, is able to further improve the accuracy of the viscosity prediction *via* the process model.

Minimization of the variation in the product Mooney viscosity during the production of NBR with a specific grade is a primary aim for the process control. As shown in Fig. 8, after 10 days the product viscosity has two undesirable large jumps, which is due to observed large fluctuations of the vinyl acetylene contents in the feed of monomer Bd. The developed process model is capable

of capturing this important feature, which is key to understanding the process and to optimizing the operation scenarios for the stabilization of product viscosity. To sum up, the predictive process model for NBR Mooney viscosity is proved to be able to quantify directly the influence of feed compositions on the final product viscosity, and the prediction accuracy is excellent towards optimal control of the product quality.

#### 4.3. The influence of feed impurities on NBR Mooney viscosity

Two impurities, vinyl acetylene and Bd dimers, in the monomer feed Bd for the emulsion polymerization have influence on the characteristics of polymerized NBR polymers, consequently also on their Mooney viscosity. Vinyl acetylene would promote cross-linking reactions, this results in more branched polymers of larger molecular weight, and finally larger NBR Mooney viscosity. Bd dimers could retard the polymerization and consume many radicals from the initiator or bound to growing chains, which lowers the molecular weight and decreases the Mooney viscosity.<sup>16</sup> In building the process model as described above, the integration of the mechanistic model based on emulsion polymerization kinetics makes it possible to include the effect of such two impurities on the polymerization process, and then to predict the Mooney viscosity of NBR products. Besides, the added amount (flow rate) of chain transfer agent, functioning as a molecular weight mediator, is the main means to artificial control the product viscosity. Thus, the developed process model is employed to analyze the univariate and multivariate influence of feed compositions on NBR Mooney viscosity, and the variables include the contents of vinyl acetylene and dimer in Bd, as well as the intermediate mass flow rate of CTA in the process (Fig. 2).

##### 4.3.1. Univariate sensitivity analyses of Mooney viscosity.

The univariate sensitivity analyses are based on the developed process model for analyzing the influence of variables include vinyl acetylene contents, Bd dimer contents and the intermediate mass flow rate of CTA. As shown in Fig. 9(a), there is positive correlation between the vinyl acetylene content and NBR Mooney viscosity. When its content is larger than 14 ppm, the correlation deviates significantly from linear relationship. From the viewpoint of stabilizing NBR viscosity, it is suggested to keep the vinyl acetylene content in Bd under 14 ppm. Fig. 9(b) show negative correlation between the Bd dimer content and viscosity. Under the conditions that the dimer content is below 1100 ppm, the relationship is linear; above such a critical value, the relationship is obviously non-linear. Therefore, 1100 ppm is the suggested threshold value for the Bd dimer content in the feed. As shown in Fig. 9(c), the relationship between the intermediate mass flow rate of CTA and the NBR Mooney viscosity is ideally linear, and a 1 kg h<sup>-1</sup> increase of CTA flow rate results a decrease of 2.3 in product viscosity. The predictive process model developed in this work enables quantitative analyses of the influence of such three variables on the product viscosity, which would serve as a numerical platform for controlling the NBR product quality.



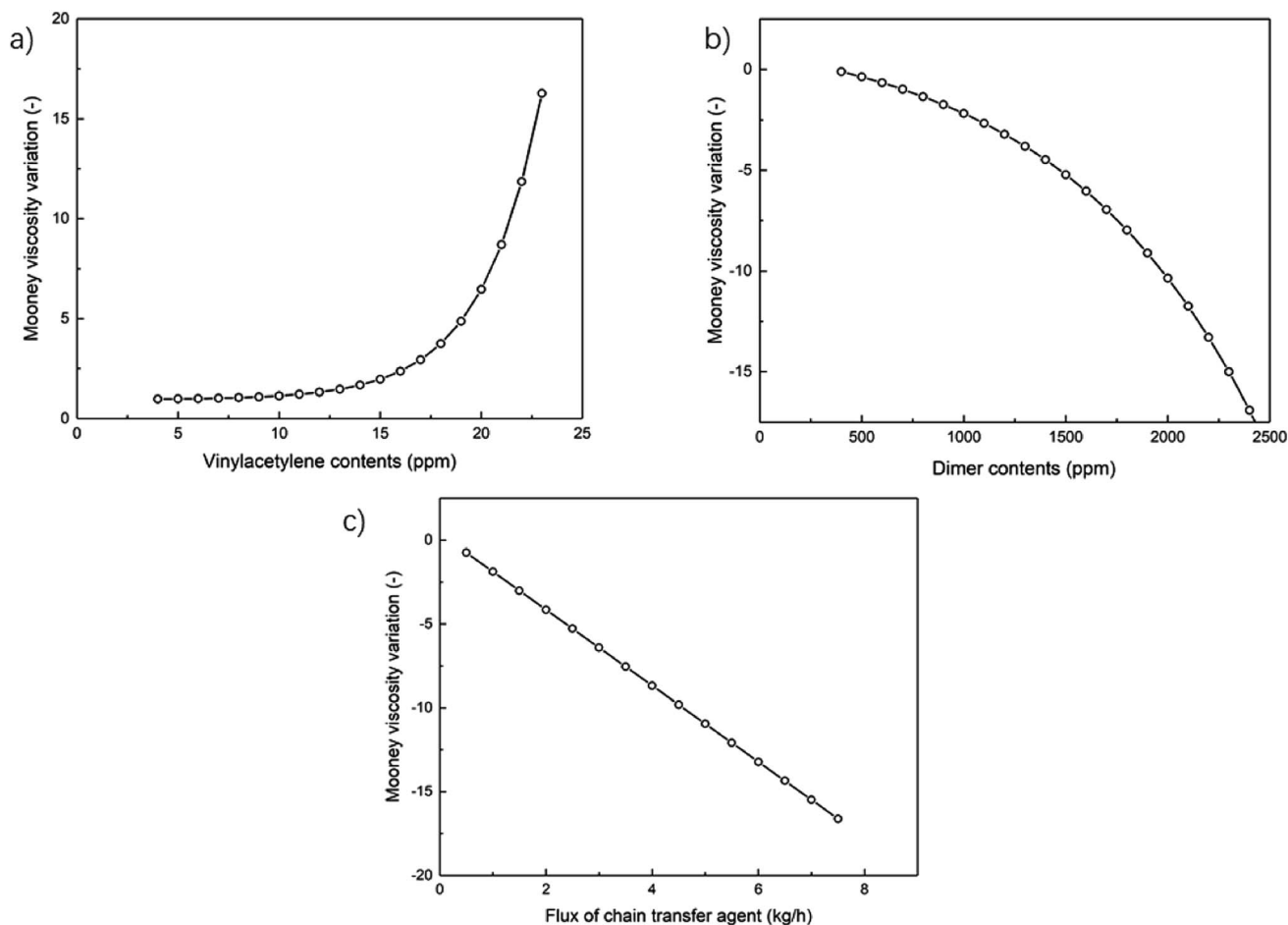


Fig. 9 The univariate analyses of the impurities in polymerization monomer Bd, (a) vinyl acetylene, (b) Bd dimer, and (c) the intermediate mass flow rate of CTA in the process on the Mooney viscosity of final NBR products. (Note: the variation in Mooney viscosity is the difference between those when the impurity contents or the intermediate CTA flow rate have changed and their original values.)

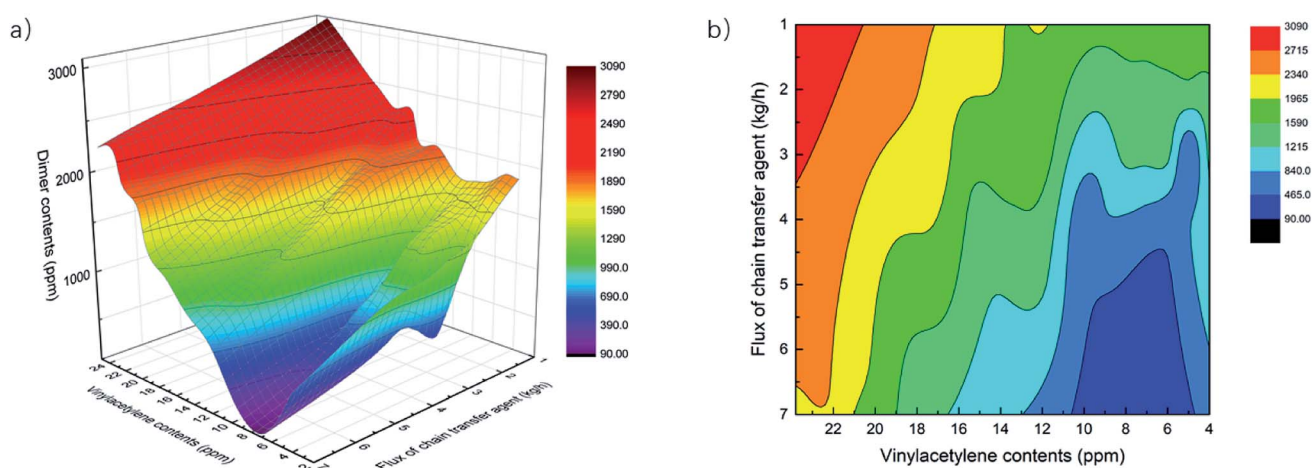


Fig. 10 The model-aided optimization of operation scenarios for a constant NBR Mooney viscosity of 59.1. (a) The response surface of NBR Mooney viscosity, the independent variables include the vinyl acetylene content, the Bd dimer content and the intermediate CTA. The color indicates the Bd dimer content. (b) A contour map for viscosity. The color means when the Bd dimer content is almost constant at a certain value, the domain for the other parameters that leads to a constant NBR Mooney viscosity of 59.1.



#### 4.3.2. Multivariate sensitivity analyses of Mooney viscosity.

As a successor of the previous section, and considering the real situation in NBR production, we also perform multivariate analyses with the help of the developed process model to investigate the intertwined influence of the above 3 parameters on NBR Mooney viscosity. The collection of points representing the various conditions where NBR product of the targeted Mooney viscosity at 59.1 is plotted in Fig. 10(a). The various conditions are explicitly the vinyl acetylene content, the Bd dimer content and the intermediate mass flow rate of CTA. The collection of points in the coordinate space is the response surface of viscosity, which might also be called iso-viscosity plane. It is necessary to note that in selecting the data points generated *via* the process model for a target Mooney viscosity of 59.1, we actually use the data points that represent conditions leading to Mooney viscosity in the range of 58.6–59.6. When it is enough to only consider the influence of two parameters on NBR Mooney viscosity, for example the fluctuation of Bd dimer content in the feed is negligible, a contour map for viscosity as shown in Fig. 10(b) can be used. In Fig. 10, the color indicates the vinyl acetylene content. With the help of such response surface or contour map, it is straightforward to know the optimal operation scenarios for stabilizing NBR Mooney viscosity. As an example, in the continuous production process of NBR, on-line detection of the vinyl acetylene content and the Bd dimer content in the feed would allow swift prediction, *via* the developed process model, of the Mooney viscosity of NBR products to be produced. By altering the intermediate mass flow rate of CTA accordingly, it is convenient to stabilize the Mooney viscosity of NBR products that actually produced. This would facilitate the process control and optimize the NBR product quality.

Therefore, we suggest that the optimal methodology to build models for the prediction of NBR rubber Mooney viscosity is the combination of mechanism model for the emulsion polymerization process and the data model for the correlation of NBR rubber Mooney viscosity. This approach is not only able to realize the direct prediction of NBR rubber Mooney viscosity from the feed composition and process conditions, but is also able to reveal the polymerization mechanism for a better understanding of the emulsion polymerization process. This approach is suitable for the accurate prediction of product properties with diversified feeds and process conditions.

The mathematic model for the NBR production process established in this work is capable of directly relating the feed compositions and process parameters to the Mooney viscosity of final products. If the on-line detection of the vinyl acetylene content, the Bd dimer content in the feed and the CTA content *via*, *e.g.* infra-red spectrometry is available, the established model can be employed to realize on-line detection and simultaneous optimization, and advanced process control of the industrial emulsion polymerization process for NBR production, towards the realm of “intelligent manufacture”.

The hybrid model proposed in this work can be further improved on two aspects: firstly, more experimental Mooney viscosity data with wider range could be collected for the modeling with GP; secondly, the mechanism model about the

emulsion polymerization process can be enriched with more details, and this is the focus of future research and how to integrate data science algorithms into the establishment of more detailed mechanism models is also an interesting direction.

## 5. Conclusions

A process model comprised of a mechanistic model and a data-driven model in sequence is built to predict the Mooney viscosity of nitrile-butadiene rubber (NBR) directly from the feed compositions and process parameters of the emulsion polymerization process. The mechanistic model is based on emulsion polymerization kinetics, and is well suited to describe the polymerization process. While the data-driven model for correlating the molecular weight and branching degree of polymers is derived from genetic programming (GP). The proposed process model in this work serves to help stabilize the viscosity of NBR products, and supports its “intelligent manufacture”.

In building the data-driven model for the correlation between number-, weight-averaged molecular weight ( $M_n$ ,  $M_w$ ) of NBR polymers and their Mooney viscosity, GP is chosen to integrate the polymer branching degree into the model. Under such conditions, the predicted viscosity results provided by the data-driven model match better with experimental values, as compared to the situations when the polymer branching degree is not included in the model, or when only simple power functions are used to correlate the Mooney viscosity. With the developed process model, it is possible to analyze the influence of three dominant parameters on the  $M_n$ ,  $M_w$  of NBR polymers, and consequently on the Mooney viscosity of NBR products. The three dominant parameters are the contents of vinyl acetylene and dimers in the monomer 1,3-butadiene, and the mass flow rate of chain transfer agent in the middle of the process. The simulated results show that NBR Mooney viscosity is positively and negatively proportional to the contents of vinyl acetylene and dimers, respectively, and the relationship deviates obviously from linearity when the content in both cases is above a threshold value. To stabilize the product Mooney viscosity and improve its quality, it is suggested to keep the contents of vinyl acetylene and dimer in the feed below 14 ppm and 1100 ppm, respectively.

The proposed mathematic model in this work correlates directly the feed compositions, process parameters to the Mooney viscosity of NBR products. If combined with on-line detection of the vinyl acetylene and dimer contents of the feed, it can be envisaged that optimization and advanced control of the process is readily achievable, which would finally lead to the realm of intelligent manufacture featuring efficient conversion of materials and energy.

## Appendix A. Kinetics parameters of elementary reactions



Table 5 Reaction kinetics equations and fitted parameters

Code	Reactions	Mechanism	Pre-exp	Act-energy kJ mol <sup>-1</sup>
1	$P_n[\text{An}] + \text{An} \rightarrow P_{n+1}[\text{An}]$	Propagation	$6.9 \times 10^8$	16.245
2	$P_n[\text{An}] + \text{Bd} \rightarrow P_{n+1}[\text{Bd}]$		$3.9 \times 10^9$	16.162
3	$P_n[\text{An}] + \text{C}_4\text{H}_4 \rightarrow P_{n+1}[\text{C}_4\text{H}_4]$		$6.87 \times 10^8$	37.723
4	$P_n[\text{Bd}] + \text{An} \rightarrow P_{n+1}[\text{An}]$		$1.31 \times 10^9$	37.723
5	$P_n[\text{Bd}] + \text{Bd} \rightarrow P_{n+1}[\text{Bd}]$		$6.87 \times 10^8$	37.723
6	$P_n[\text{Bd}] + \text{C}_4\text{H}_4 \rightarrow P_{n+1}[\text{C}_4\text{H}_4]$		$6.87 \times 10^8$	37.723
7	$P_n[\text{C}_4\text{H}_4] + \text{An} \rightarrow P_{n+1}[\text{An}]$		$6.87 \times 10^8$	37.723
8	$P_n[\text{C}_4\text{H}_4] + \text{Bd} \rightarrow P_{n+1}[\text{Bd}]$		$6.87 \times 10^8$	37.723
9	$P_n[\text{C}_4\text{H}_4] + \text{C}_4\text{H}_4 \rightarrow P_{n+1}[\text{C}_4\text{H}_4]$		$6.87 \times 10^8$	37.723
10	$P_n[\text{An}] + \text{An} \rightarrow D_n + P_1[\text{An}]$	Transfer to monomer	10 800	28.799
11	$P_n[\text{An}] + \text{Bd} \rightarrow D_n + P_1[\text{Bd}]$		10 800	28.799
12	$P_n[\text{An}] + \text{C}_4\text{H}_4 \rightarrow D_n + P_1[\text{C}_4\text{H}_4]$		15 500	28.799
13	$P_n[\text{Bd}] + \text{An} \rightarrow D_n + P_1[\text{An}]$		10 800	28.799
14	$P_n[\text{Bd}] + \text{Bd} \rightarrow D_n + P_1[\text{Bd}]$		10 800	28.799
15	$P_n[\text{Bd}] + \text{C}_4\text{H}_4 \rightarrow D_n + P_1[\text{C}_4\text{H}_4]$		15 500	28.799
16	$P_n[\text{C}_4\text{H}_4] + \text{An} \rightarrow D_n + P_1[\text{An}]$		16 000	28.799
17	$P_n[\text{C}_4\text{H}_4] + \text{Bd} \rightarrow D_n + P_1[\text{Bd}]$		15 000	28.799
18	$P_n[\text{C}_4\text{H}_4] + \text{C}_4\text{H}_4 \rightarrow D_n + P_1[\text{C}_4\text{H}_4]$		15 000	28.799
19	$P_n[\text{An}] + \text{CH-B} \rightarrow D_n + R^*$	Transfer to CTA	135 000	16.744
20	$P_n[\text{Bd}] + \text{CH-B} \rightarrow D_n + R^*$		90 000	16.744
21	$P_n[\text{C}_4\text{H}_4] + \text{CH-B} \rightarrow D_n + R^*$		90 000	16.744
22	$P_n[\text{An}] + P_m[\text{An}] \rightarrow D_{n+m}$	Termination	460 000	10.465
23	$P_n[\text{An}] + P_m[\text{Bd}] \rightarrow D_{n+m}$		460 000	10.465
24	$P_n[\text{An}] + P_m[\text{C}_4\text{H}_4] \rightarrow D_{n+m}$		460 000	10.465
25	$P_n[\text{Bd}] + P_m[\text{An}] \rightarrow D_{n+m}$		460 000	10.465
26	$P_n[\text{Bd}] + P_m[\text{Bd}] \rightarrow D_{n+m}$		460 000	10.465
27	$P_n[\text{Bd}] + P_m[\text{C}_4\text{H}_4] \rightarrow D_{n+m}$		460 000	10.465
28	$P_n[\text{C}_4\text{H}_4] + P_m[\text{An}] \rightarrow D_{n+m}$		460 000	10.465
29	$P_n[\text{C}_4\text{H}_4] + P_m[\text{Bd}] \rightarrow D_{n+m}$		460 000	10.465
30	$P_n[\text{C}_4\text{H}_4] + P_m[\text{C}_4\text{H}_4] \rightarrow D_{n+m}$		460 000	10.465
31	$C_{a-b} + C_{a-d}[\text{re.}] \rightarrow nR^* + C_{a-d}[\text{ox.}] + [\text{by-products}]$		Oxidation	14
32	$C_{a-c} + C_{a-d}[\text{ox.}] \rightarrow C_{a-d}[\text{re.}] + [\text{by-products}]$	Reduction	1000	0
33	$P_n[\text{Bd}] + D_m \rightarrow D_n + P_m[\text{An}]$	Transfer to polymer	800 000	37.757
34	$P_n[\text{An}] + D_m \rightarrow D_n + P_m[\text{Bd}]$		800 000	37.757

## Nomenclature

ACN	Acrylonitrile
Bd	1,3-Butadiene
MV	Mooney viscosity
$x_{\text{ACN}}$	Cumulative copolymer composition of acrylonitrile/content of -copolymerized acrylonitrile
DP	Degree of polymerization
$M_n, M_w$	Cumulative number- and weight-averaged molecular weight (g mol <sup>-1</sup> )
MWD	Molecular weight distribution
PDI	Poly-dispersity index ( $M_w/M_n$ )
$M_{\text{eff}}$	The effective monomer molecular weight
$V_p Q_0, V_p Q_1, V_p Q_2$	The first three moments of the molecular weight distribution (MWD) defined on a mole basis and are states of the model
$V_p$	The polymer particle volume
$V_p Q_0 \overline{\text{BN}}_3,$	Zeroth moments of the tri- and tetra-functional branching distributions
$V_p Q_0 \overline{\text{BN}}_4$	

## Author contributions

Conceptualization, Tuo; methodology, He; software, He; validation, Dai; formal analysis, Tuo and Dang; investigation, Dang; resources, He; data curation, He; writing—original draft preparation, He; writing—review and editing, Tuo; visualization, Dai; supervision, Zhou; project administration, Ji; funding acquisition, Ji. All authors have read and agreed to the published version of the manuscript.

## Conflicts of interest

The authors declare no conflict of interest.

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