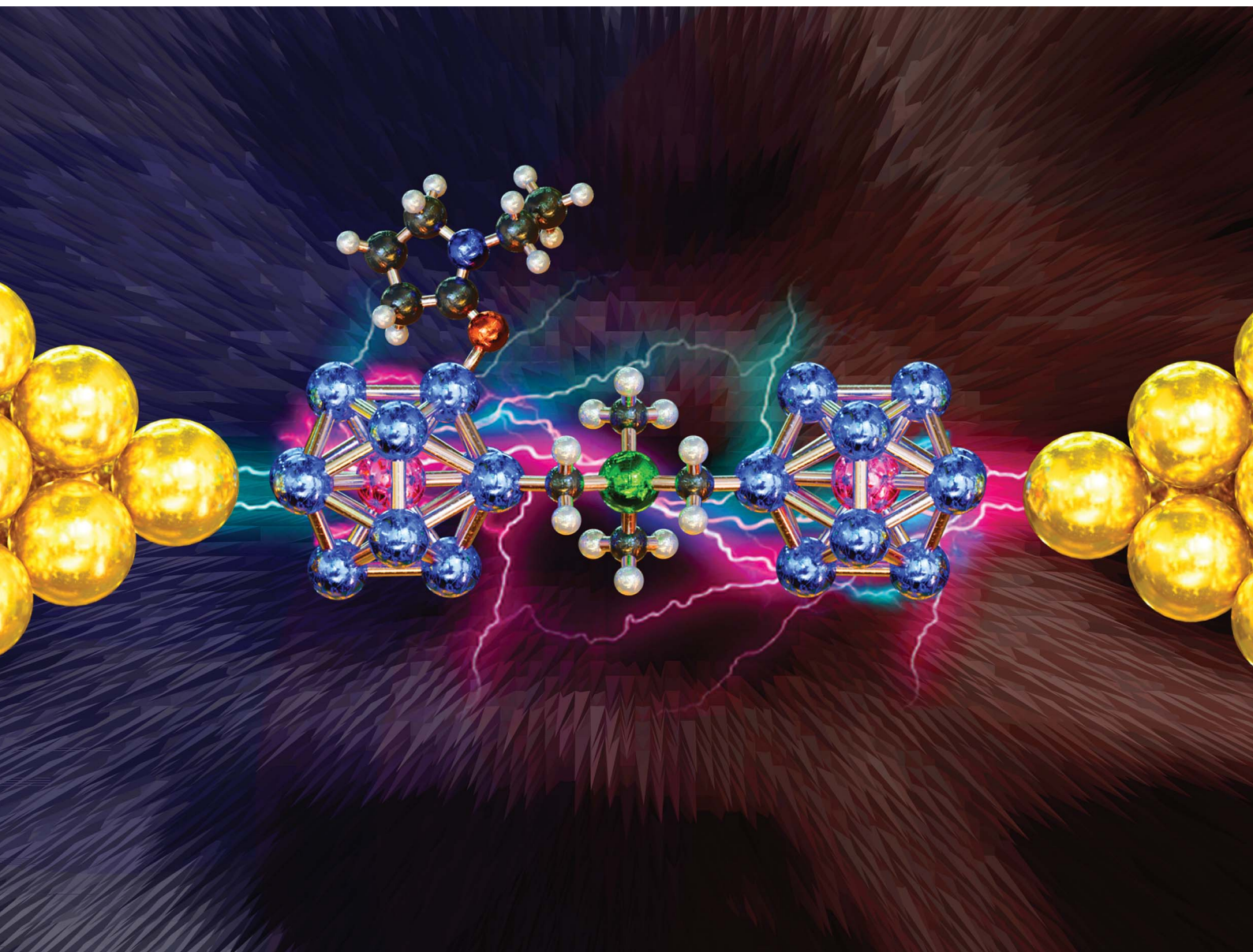


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Electron transport properties of PAI_{12} -based cluster complexes†

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The electronic transport properties of PAI_{12} -based cluster complexes are investigated by density functional theory (DFT) in combination with the non-equilibrium Green's function (NEGF) method. Joining two PAI_{12} clusters via a germanium linker creates a stable semiconducting complex with a large HOMO–LUMO gap. Sequential attachment of an electron-donating ligand, *N*-ethyl-2-pyrrolidone, to one of the two linked clusters results in the shifting of the electronic spectrum of the ligated cluster while the energy levels of the unligated cluster are mostly unchanged. Using this approach, one can eventually align the HOMO of the ligated cluster to the LUMO of the non-ligated cluster, thereby significantly reducing the HOMO–LUMO gap of the complex. As a result, the transport properties of the complex are highly dependent on the number of attached ligands. Although a single ligand is observed to generally decrease the current, the inclusion of two or more ligands shows a significant increase in the amount of current at most voltages. The resulting increase of the current can be attributed to two factors, first the reduction in the HOMO–LUMO gap due to ligand attachment which has moved the transmission orbitals into the bias window. Secondly, when two or more ligands are attached to the complex, the HOMOs become delocalized across the scattering region, and this significantly enhances the currents.

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1. Introduction

In the current era of information technology, fabrication and modification of nanoscale devices have taken center stage. Modern electronic devices are composed of multiple complex components like diodes, transistors, sensors, and switches.¹ Reducing their sizes to the microscopic level unfolds the possibility of creating compact nanoscopic devices with enhanced functionalities.^{1,2} Thus, in the past few decades, scientists have searched for a way to rationally design molecules that can be utilized as the crucial components in electronic devices.^{3,4} The possible existence of such systems was originally predicted by Aviram and Ratner,⁵ who have shown that a unimolecular rectifier can be constructed by combining donor and acceptor moiety via an insulating linker. This theoretical prediction eventually paved the way for the intriguing field of molecular electronics.^{3,4,6} To construct such devices, it is important to understand how a particular molecule behaves when it is placed in an electric field.² In other words, one needs

to rationalize the quantum transport properties of the respective molecule by placing it between two electrodes in a break junction experiment. The response of a molecule in an electric field depends on various factors. For example, a molecule can have multiple contact points and can orient itself in many different ways. The transport properties are also dependent on the length of the molecule and how far they are placed from the electrodes. Exploring all such possibilities by experimental means is often difficult. Thus, computational modeling of quantum transport has become an essential tool for determining the applicability of a single molecular junction. Moreover, conventional single molecular junction also suffers from some significant limitations such as low-temperature dependence and coherent tunneling.⁷ As Moore's law is faltering,⁸ scientists are now trying to use different components to increase the computer's computing power, like using carbon nanotubes, nanoclusters, or quantum transistors. Recent researches have shown promising transport results for metal^{9,10} and metal chalcogenide^{7,11} clusters. It was also noticed that by using such nanoclusters for charge transport, one could circumvent the limitations of common organic or organometallic molecules.⁷ In the spirit of this, semiconducting cluster complexes constituted of atomic clusters and choices of ligands are proposed to mimic the functions of transistors to achieve the goal of increasing computing power.

In our recent work,¹² we have shown that such a semiconducting cluster complex can be composed by joining two

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open-shell PAI_{12} clusters utilizing an organometallic linker. It is well known that the electronic structure of metallic clusters can be modeled as a confined nearly free electron gas against a uniform positively charged background.^{13,14} Solving the Schrödinger equation^{15,16} based on such approximation yields superatomic shells for the whole system similar to the atomic orbitals. Considering the model, the valence electron count of the PAI_{12} cluster is 41, which results in a superatomic configuration^{17–19} of $1\text{S}^2, 1\text{P}^6, 1\text{D}^{10}, 2\text{S}^2, 1\text{F}^{14}, 2\text{P}^6, 1\text{G}^1$. Joining two such clusters *via* an organometallic linker, *e.g.*, $-\text{CH}_2\text{CH}_3\text{GeCH}_3\text{CH}_2-$, generates a semiconducting cluster complex in which both the PAI_{12} clusters are closed-shell (40 e) due to the sharing of the unpaired electron with the linker. As a result, the resulting cluster complex ($\text{PAI}_{12}-\text{CH}_2\text{CH}_3\text{GeCH}_3\text{CH}_2-\text{PAI}_{12}$) is marked by a significantly large HOMO–LUMO gap.¹² It is also shown that by attaching a donor ligand like *N*-ethyl-2-pyrrolidone ($\text{C}_6\text{H}_{11}\text{NO}$, abbreviated as EP) on one of the PAI_{12} clusters, one can alter the position of the frontier orbitals of one side without perturbing the electronic shell structure of the monomers. Upon addition of multiple ligands, the HOMO of the ligated cluster can eventually be aligned to the LUMO of the non-ligated cluster, mimicking a broken gap energy alignment.¹² The direction of the dipole moment is also observed to be dependent on the location of the attached EP ligand. In addition, such asymmetrically ligated superatomic dimers show prominent indications of electron–hole separation, which can have useful applications in photovoltaics.^{12,20} Therefore, the quantum transport properties of such a system will be interesting. In this paper, we focus on the recently proposed PAI_{12} -based cluster complexes and investigating their electron transport properties in a two-terminal device configuration. Moreover, the role of ligands in determining the electron transport properties of such cluster-based devices is investigated employing density functional theory (DFT) together with the non-equilibrium Green's function^{21–23} (NEGF) method.

2. Methods

The DFT calculations of the PAI_{12} and the bridged clusters are performed using the Amsterdam Density Functional (ADF) suite of codes.²⁴ The generalized gradient approximation (GGA) based exchange–correlation functional of Perdew, Burke, and Ernzerhof's²⁵ (PBE) were used for the optimizations and single point calculations. The Slater type TZ2P basis set²⁶ (triple- ζ basis set with two polarization functions) with a large frozen core is used for all the elements. Calculation of basis set superposition error (BSSE) for a few selected systems (see Fig. S1 in the ESI†) was observed to be quite small and hence not considered for the present study. The optimizations were carried out by using the hessian-based quasi-Newton method²⁷ without any symmetry restrictions as implemented in ADF.²⁴ During optimizations, a wide range of spin multiplicities was investigated for each structure, and the lowest energy conformer was selected in all cases. The electronic convergence threshold was set to 10^{-8} Hartree, whereas the default optimization criteria²⁴ was used for all systems. The scalar relativistic correction was incorporated by using the zeroth-order regular approximation (ZORA).²⁸

For the transport calculations, the central scattering region was described in the DFT framework with the PBE exchange–correlation functional²⁵ and the double-zeta with polarization (DZP) basis sets.^{29,30} For Au atoms, the core electrons were described by the norm-conserving pseudopotential,^{31,32} and the $5\text{d}^{10}6\text{s}^1$ valence electrons were described by a DZP basis set. Structures of the cluster complexes with and without ligands are fully optimized, with all atoms being allowed to relax. Calculations were considered to be converged when the force on each ion is less than $0.01 \text{ eV } \text{\AA}^{-1}$ with convergence in the RMS density matrix to 10^{-8} and the total energy to 10^{-5} eV .

The bias-dependent electron transmission and current were calculated using the NEGF method as implemented in the Transiesta module^{21,22} of the SIESTA program.²³ The PAI_{12} –Ge– PAI_{12} cluster complex was oriented parallel to the electrode Au nanowire (see Fig. S2 for Au structure in the ESI†), and the distance between the electrodes (the two upmost Au atoms) was kept fixed at 24.1 \AA to simulate a fixed break junction setup. As the number of ligands changes, the connecting Al–Au distance varies a bit due to the actual change in the length of the cluster complex (see Fig. S3 in the ESI†). The direction of a finite bias potential V was set up to have a lower potential ($-V/2$) at the left electrode and a higher potential ($V/2$) at the right electrode. We considered Γ -point for the scattering region and a mesh of $(1 \times 1 \times 100)$ k -points for the contacts. The charge density was obtained by integrating Green's function over 200 imaginary and 1000 real energy points, giving rise to less than 0.03% deviation in the total charge of the system.

The total tunneling current of the system under a bias of V can be written as

$$I(V) = \frac{2e}{h} \int_{-\infty}^{\infty} T(E, V) (f(E - \mu_1) - f(E - \mu_2)) dE \quad (1)$$

where μ_1 and μ_2 are the electrochemical potentials in the two electrodes, taking a value of $E_F - \frac{V}{2}$ and $E_F + \frac{V}{2}$, respectively; $f(E)$ is the Fermi–Dirac distribution function, and E_F is the Fermi level for such an open and non-equilibrium system, which is treated self-consistently. $T(E, V)$ is the electron transmission function, which varies with both the energy E and the bias V . We have set the temperature to 300 K for transmission and current calculations.

3. Results and discussion

3.1. The electronic structure of the PAI_{12} cluster complexes

To construct the cluster-based semiconducting complex, we have chosen the PAI_{12} cluster as the primary component. Since aluminum is trivalent, the valence electron count of the icosahedral Al_{13} cluster is 39. This results in a superatomic electronic configuration of $1\text{S}^2, 1\text{P}^6, 1\text{D}^{10}, 2\text{S}^2, 1\text{F}^{14}, 2\text{P}^5$, which is similar to a halogen atom. Replacing the core Al atom with pentavalent phosphorus alters the configuration to $1\text{S}^2, 1\text{P}^6, 1\text{D}^{10}, 2\text{S}^2, 1\text{F}^{14}, 2\text{P}^6, 1\text{G}^1$ (41 e). Consequently, the PAI_{12} cluster behaves like an alkali superatom. Such an open-shell system with a single electron in the outer shell act as an effective donor with very low ionization energy. As an insulator linker, we have chosen



$-\text{CH}_2\text{CH}_3\text{GeCH}_3\text{CH}_2-$ (denoted as Ge_B), a derivative of tetramethylgermanium (TMG, $(\text{CH}_3)_4\text{Ge}$), in which one hydrogen atom is removed from two of the methyl groups to allow bonding with both clusters. Attaching two PAI_{12} clusters *via* Ge_B allowed us to create a stable semiconducting cluster complex ($\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$, denoted hereby as EP0) with a large HOMO–LUMO gap of 1.53 eV. Our investigation showed that during the formation of the polar covalent C–Al σ -bond, each of the PAI_{12} clusters shares its outer shell electron with the linker. Thus, in the cluster complex, each of the component clusters has a 40 electronic closed-shell configuration, which is the reasoning behind the observed high HOMO–LUMO gap. Important to note that the icosahedral shape of each PAI_{12} cluster has also remained intact during the formation of the cluster complex. The optimized structure of $\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ is shown in Fig. 1a with a few important bond distances (in Å). The adiabatic ionization energy (AIE) and adiabatic electron affinity (AEA) of $\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ are calculated as 5.66 and 2.16 eV, respectively. Due to the sharing of electrons with the linker, each PAI_{12} cluster is observed to be positively charged (Hirshfeld³³ Charge: +0.18), whereas the Ge_B holds a negative Hirshfeld³³ charge of -0.36 to maintain the overall charge neutrality.

As shown in our earlier work,^{12,20,34,35} the inclusion of an electron donor or acceptor ligands to a cluster creates a coulomb well surrounding the metallic core, which shifts the whole electronic spectrum of the cluster upward or downward depending on the nature of the attached ligands. Using this strategy, one can create superatoms with very low ionization energy or high electron affinity, as desired, just by altering the nature and number of ligands attached to the cluster. In this work, we have investigated how the transport property of the superatomic cluster complex can be controlled by the addition of such ligands. To achieve this, we have chosen the *N*-ethyl-2-pyrrolidone (EP) ligand, which acts as an effective donor when attached to a metallic cluster by the O atom. To investigate the effect of the EP ligand on the electronic structure of the PAI_{12} cluster complex, we have modeled the ligated complexes in which one to three EP ligands (denoted as EP1, EP2, and EP3,

respectively) are sequentially attached to one of the PAI_{12} clusters, keeping the second cluster on the other side non-ligated. During the optimizations, we have explored all the possible Al sites for the EP ligand attachment, and only the global minima are considered herewith (see Fig. S4 in the ESI†). The ground state spin multiplicities (singlet) are also ascertained similarly. The optimized structures of $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ ($n = 1-3$) are shown in Fig. 2b–d. The binding energies of the EP ligand are observed to decrease as additional ligands are added. Thus, the binding energy values of 0.91, 0.79, 0.56 eV are calculated for first, second, and third EP ligands, respectively. The binding energy decreases because adding charge donating ligands means that additional ligands will bind more weakly. As the number of EP ligands is increased, the net Hirshfeld charge³³ on the ligated cluster shows a monotonic increase starting from +0.18 for the non-ligated to +0.23, +0.26, and +0.29 for the single, double, and triply ligated $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ complexes, respectively.

The major effect of attaching EP ligands to the cluster complex is observed in the molecular orbital (MO) diagram, as shown in Fig. 2. As the number of ligands is increased, the HOMO of the complex is observed to shift to higher energy keeping the LUMO nearly at the same position. This results in a decrease in the overall HOMO–LUMO gap of the complex as more numbers of ligands are attached. The HOMO–LUMO gap for the EP1, EP2, and EP3 are calculated as 1.14, 0.60, and 0.21, respectively. To investigate the reason for this decrease in the gap, we have plotted the projected density of states (PDOS) of both clusters separately (Fig. 3). It is evident from the PDOS plot that the EP ligands are shifting the whole electronic spectrum, including the frontier orbitals of the ligated PAI_{12} cluster

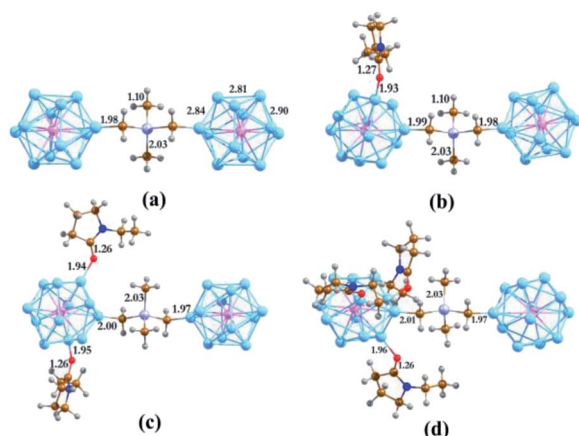


Fig. 1 The optimized ground state structures of $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ ($n = 0-3$ for (a–d) respectively). Bond distances are in Å.

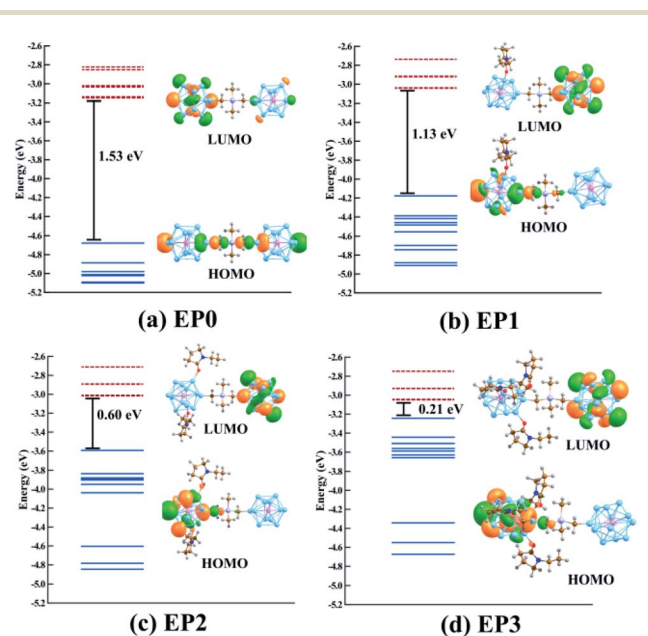


Fig. 2 The molecular orbital diagram of $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ ($n = 0-3$ for (a–d) respectively). The occupied and unoccupied orbitals are shown by solid (blue) and dashed (red) line respectively. Isosurfaces of HOMO and LUMO orbitals for each structure are also shown.



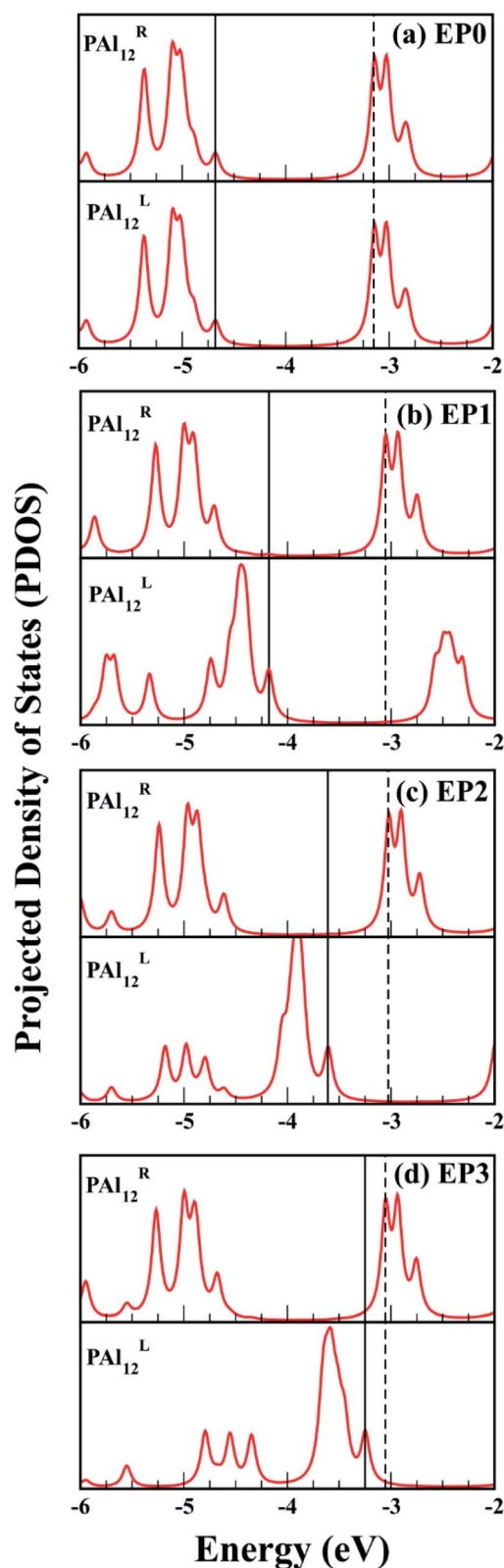


Fig. 3 The projected density of states (PDOS) plots of the left and the right PAI_{12} clusters for $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ ($n = 0-3$). The position of HOMO and LUMO of the cluster complexes are indicated by solid and dashed line respectively.

(marked as left or 'L' in Fig. 3). In contrast, the electronic spectrum of the non-ligated (marked as right or 'R' in Fig. 3) site remain mostly unperturbed. As a result, in the $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ cluster complexes, the HOMO of the structure is originating from the ligated site, whereas the LUMO of the non-ligated site is acting as the effective LUMO of the wire. The representative isosurfaces of HOMO and LUMO (Fig. 2) also show the same. Thus, as the EP ligands are successively introduced, the HOMO–LUMO gap is observed to decrease. Important to note that the individual cluster on each side maintains a high HOMO–LUMO gap irrespective of the number of the ligands attached. The increase of the HOMO energy also led to a monotonic change in the AIE values, which decreases from 5.21 eV to 4.19 eV upon altering the numbers of the attached ligand from one to three.

3.2. Calculation of the transport properties of PAI_{12} -based cluster complexes

In calculations of the quantum transport of electrons, the $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ cluster complex is sandwiched between two Au electrodes. The central scattering region of such a device is shown in Fig. 4, which includes the $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ complex and a sufficient number of Au sublayers to ensure electrostatic screening at the boundary. The Au electrode was modeled by a semi-infinite Au nanowire with alternating planes of three and seven gold atoms (Fig. S2 in the ESI†) which were previously considered as viable Au contacts in a device configuration.^{36,37} The Au–Au distance in the sublayers was taken to be that in bulk. At the interface, a protruding Au atom as part of an Au pyramid belonging to the electrode connects with a cluster Al atom with the Al–Au distance ≥ 3.5 Å. This simulation setup represents a weak-coupling regime in which the complex and the electrode are sufficiently apart such that the interfacial states arising from the direct contact and hybridization of the complex and electrode orbitals are eliminated.³⁸

The calculated current–voltage (I – V) characteristics of the $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_\text{B}]\text{PAI}_{12}$ cluster complexes with ($n = 1-3$) and without ($n = 0$) ligands are shown in Fig. 5. In the ligand-free complex (EP0), the tunneling current appears to increase linearly from the onset voltage for the current rise of 0.3 V to 0.6 V. It decreases slightly up to 0.8 V and then shows a non-linear increase up to 1.0 V. We note that the applied voltage of about 1 V corresponds to the electric field strength of about 10^8 V m^{−1}.

An attachment of a ligand to the complex (EP1) leads to quenching of the tunneling current within the bias region of 0–1 V. Interestingly, the subsequent addition of ligands to the complex (Fig. S3 in the ESI†) leads to an increase in the tunneling current with the reduced value of the onset voltage for the current rise. The peak tunneling current appears to be associated with the bias voltage of 0.9 V, and the peak current associated with the complex with three ligands (EP3) is significantly higher than that associated with the complex with two ligands (EP2). The predicted variation in current with the number of ligands attached to the complex can be understood from an analysis of the



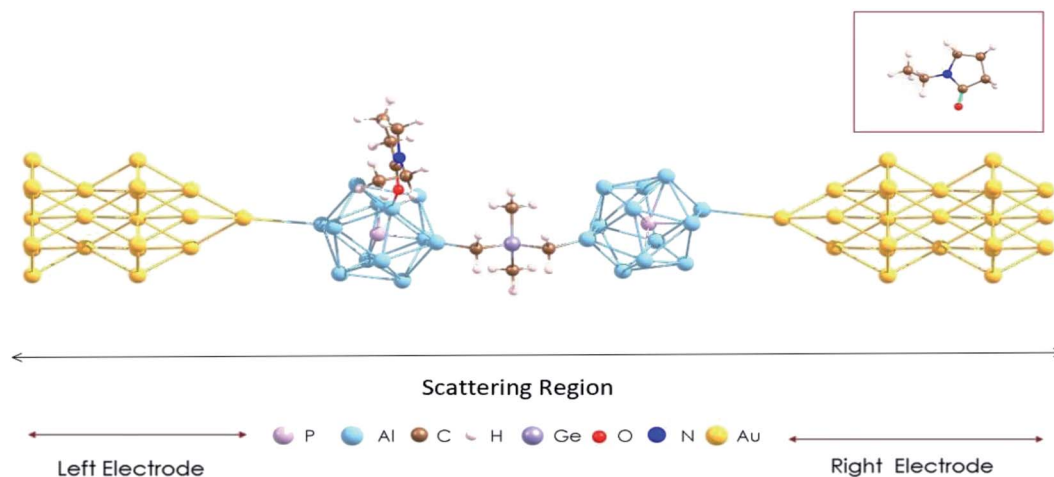


Fig. 4 The device configuration consisting of the Au contact and $\text{PAI}_{12}[\text{Ge}_B]\text{PAI}_{12}$ cluster complex with one ligand. A ball and stick structure of the ligand, $\text{C}_6\text{H}_{11}\text{NO}$ is given in the inset.

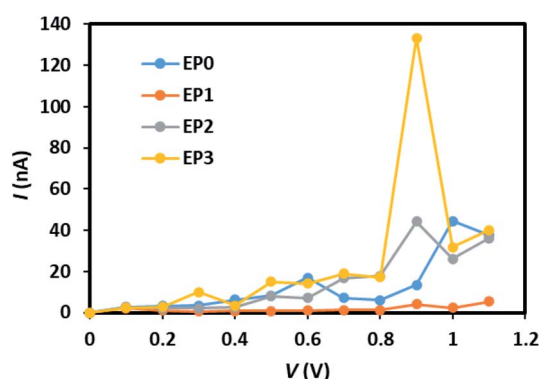


Fig. 5 Current–voltage characteristics of the $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_B]\text{PAI}_{12}$ ($n = 0-3$) cluster complexes, labeled as EP0, EP1, EP2, and EP3.

transmission function, which, in general, reflects the intrinsic transport characteristics of the system.

The calculated transmission functions are shown in Fig. 6. Since the current is obtained by integrating the transmission function within the bias voltage window, we find distinct differences in transmission functions in going from zero to three ligands attached to the cluster complexes. For all cases, we find that the transmission peaks above the Fermi level barely contribute to the tunneling current passing through the complex. Below the Fermi level ($E < E_F$), the peaks show the different shapes and shift to higher or lower energies, depending upon the number of ligands attached to the complex. For example, the first transmission peak (red-circled) associated with the cases of EP0 and EP1 is narrow in shape and large in magnitude, while those associated with EP2 and EP3 cases are diffuse in shape and small in peak magnitude. Furthermore, with the increase in the bias, the first transmission peak for EP0 shifts towards E_F , while that for EP1, EP2, or EP3 shifts away from E_F . The energy shifting direction depends on the nature of the transmission orbitals in response to an external electric field due to the applied bias.^{39,40} This is further explored below.

Next, we find a general correspondence between the transmission function and the projected density of states (PDOS) of the complex shown in Fig. S5 (ESI[†]), in which the first significant transmission peak/orbital below E_F corresponds to a state at or close to the top edge of the valence band of the extended system with significant contribution from Al and some contribution from C. We, therefore, expect that a close examination of the nature of these states can provide an understanding of ligand effects on the I - V characteristics of the $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_B]\text{PAI}_{12}$ complex. Fig. 7 displays the charge density plots of the PDOS peak at or close to the top edge of the valence band in comparison to the associated HOMO plots of the isolated cluster complexes with zero, one, two, and three ligands. They have good correspondence for all the cases. The HOMOs

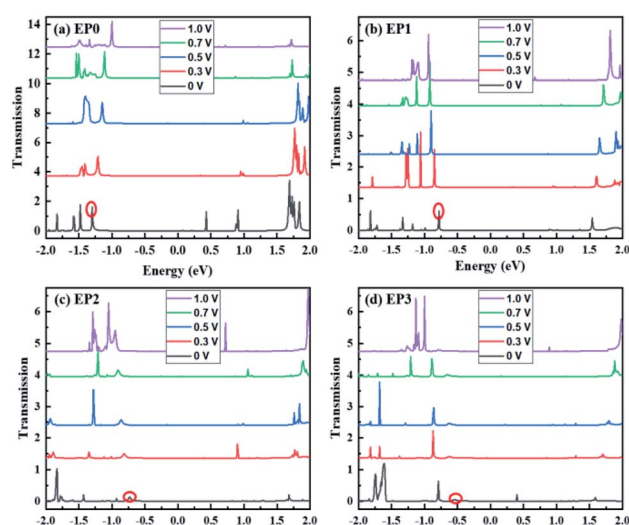


Fig. 6 The transmission functions of the $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_B]\text{PAI}_{12}$ ($n = 0-3$) cluster complexes. EP0, EP1, EP2, and EP3 represent the cases with zero, one, two, and three ligands attached to the complex. The zero of the energy is aligned to the Fermi energy. The first significant transmission peak below the Fermi level is labeled by a red circle.



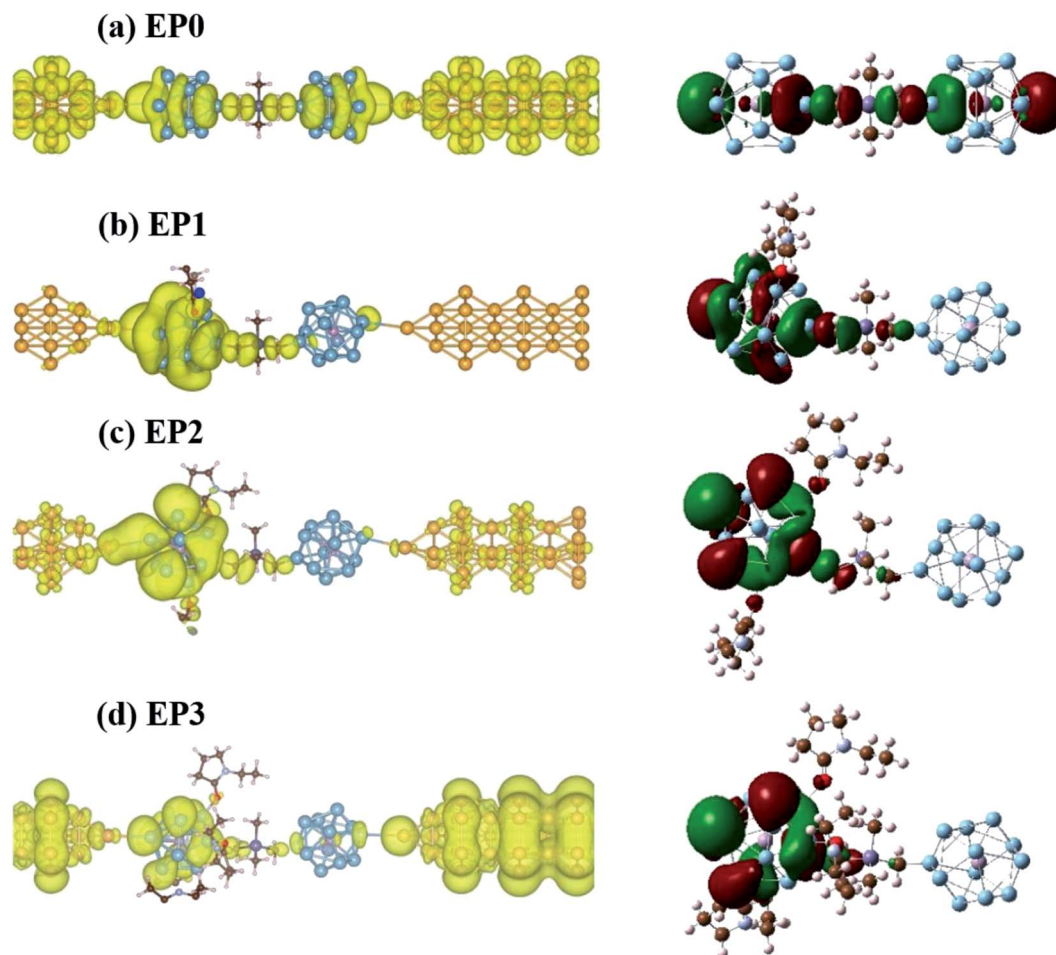


Fig. 7 Local charge density plots (left) of the PDOS peak at or close to the top edge of the valence band and associated HOMO plots (right) of the cluster complexes with (a) zero, (b) one, (c) two, and (d) three ligands from top to bottom.

associated with the first transmission peaks below the Fermi level for the cases with ligands (EP1, EP2, and EP3) are on the side of the ligated clusters. An intrinsic dipole moment is produced with a non-zero component parallel to the direction of the external bias of such an asymmetric molecular complex. Under the forward bias, the HOMO shifts to lower energy and so does the transmission peak. In contrast, for the symmetric molecular complex EP0, the HOMO symmetrically expands to both clusters and its shift under bias is the same for both forward and backward biases.

We find that resonant tunneling through the scattering region occurs in the case of the complex without ligands (EP0). Interestingly, the addition of a ligand (EP1) greatly localizes the charge density onto the ligated PAL_{12} cluster, thereby narrowing the transmission peak and reducing the transmission, and hence the current at a given bias. The increase in the Al (cluster)-to-Au (electrode) distance due to the shrinkage of the complex upon interacting with one EP ligand (highly asymmetrically positioned) has also contributed to this current reduction. This, however, is to less extent compared to the effect of the attached ligand (see Fig. S6 in the ESI† for a comparison of currents at the same Al–Au distance). The addition of another

ligand (EP2) to the complex results in a more delocalized distribution of charge density which broadens the transmission peak. Finally, the complex with three ligands (EP3) yields a larger degree of delocalization in the charge density giving rise to a higher current at a given bias.

To decouple the effects of the HOMO–LUMO gap of the complex and the electrode-cluster distance, we have done a series of transport calculations for EP1 with the Al–Au nearest distance ranging from 3.1 to 4.1 Å (see Fig. S7a and b in the ESI† for transmission functions). It is shown that there are no additional transmission peaks until the distance is reduced to 3.3 Å when the interface hybrid states start to form. In addition, the shape of the first transmission peak below E_F remains the same, while only its position shifts. This suggests that the nature of this transmission orbital does not change. Since this transmission peak is well beyond the integration voltage window for the current calculation at low biases as considered here ($V \leq 1.0$ V), the probability of electron transmission is governed by quantum tunnelling, which is evidenced by the exponential decay as a function of the electrode-cluster distance as shown in Fig. S7c.†



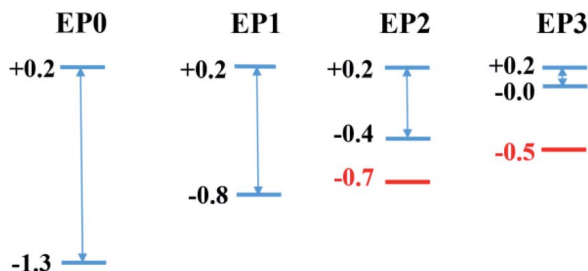


Fig. 8 Diagram of calculated HOMO and LUMO energy levels (in eV) of the cluster complex together with the location of significant transmission peaks. The lower and upper blue lines are for HOMO and LUMO levels, respectively. The red line that appears for the EP2 and EP3 cases is associated with the new transmission orbital, which is 0.3 eV and 0.5 eV below the HOMO.

Finally, we relate the transmission peaks and HOMOs to show that the substantial reduction in the HOMO–LUMO gap (see also Fig. 2) for the case of the cluster complex with three ligands primarily contributes to the enhanced current at a given bias. Fig. 8 displays the energy levels obtained from the cluster calculations correlating the location of DOS or transmission peaks. We find that the HOMO–LUMO gap depends on the number of ligands and reduces to a small value (~ 0.2 eV) for the case of the complex with three ligands. It is interesting to note that the LUMO level remains the same as we increase the number of ligands, and the HOMO–LUMO gap reduces due to upward shifts in the HOMO level. This is because the LUMO contribution comes from the PAI_{12} metal cluster on the side with no ligand, while the HOMO is ascribed to the PAI_{12} metal cluster on the side with added ligands. These ligands effectively shift the eigenvalue of the HOMO upward, narrowing down the HOMO–LUMO gap.

The location of the first transmission orbital below E_F is at the location of HOMO for 0-ligand (EP0) and 1-ligand (EP1) cases. The presence of contact Au atoms barely changes the relative energies of these states. However, the first transmission orbital location shifts down by 0.3 eV and 0.5 eV for the 2-ligand (EP2) and 3-ligand (EP3) cases, respectively, as shown in Fig. 8. As previously shown in Fig. 7, extended electronic states are formed in these cases. These states largely mimic those of the HOMOs of the complexes with ligands with a small extension of wavefunctions onto the Au atoms, resulting in lower eigenvalue energies. This shift makes the corresponding transmission peak further away from the Fermi level, thereby reduces its contribution to the current at low voltages. Therefore, overall speaking, the closing HOMO–LUMO gap in the complex due to the addition of ligands does not bring a directly proportional increase in the current. Nevertheless, EP2 and EP3 still show a peaking of current at a lower bias than EP0 and EP1, with EP3 has a significantly higher current (Fig. 5).

4. Conclusions

In molecular electronics, the flexibility of tuning electronic energy levels *via* molecular engineering opens a new horizon in designing

controllable electronic devices. In this study, we have shown that the addition of EP ligands onto a $\text{PAI}_{12}[\text{Ge}_B]\text{PAI}_{12}$ complex can consistently lower the HOMO–LUMO gap of the system. Also, adding EP ligands on one side breaks the symmetry of the $(\text{EP})_n\text{PAI}_{12}[\text{Ge}_B]\text{PAI}_{12}$ complex causing the frontier molecular orbitals to be localized. These changes in the electronic structure have profound effects on the electron transport properties of the cluster complexes. The ligand is shown to be a useful handle to vary the current through the complex. By and large, the addition of EP ligands shifts the HOMOs up while leaving the location of LUMOs almost intact. The more EP ligands are added onto the complex, the closer the HOMO is to the Fermi level closing up the energy gap. The addition of one EP ligand is, however, not sufficient to have an impact on the current in the range of 0 to 1.1 V. The current turns out to be even smaller than the current for the ligand-free case because the HOMO of the complex is far below the Fermi level and it is strongly localized on the PAI_{12} cluster accepting the ligand. When the number of added ligands increases to 2 and 3, the currents are shown to be higher than the case without ligand at most voltages and peak at ~ 0.9 V. This means that the reduction in the HOMO–LUMO gap has moved the transmission orbitals into the bias window and contributed to the surge in current at 0.9 V, especially for EP3. It is notable that when the complexes with two and three ligands are sandwiched between two Au electrodes, the HOMOs become extended states across the scattering region and contribute significantly to the transmission functions, thereby the currents. These energy levels are, however, greatly pushed down (farther away from E_F) compared to the location of HOMOs in the isolated cluster complexes.

In general, such principles can be applied to the purpose-driven design of devices in molecular electronics and nano-electronics. Our proof-of-concept study has demonstrated that one can effectively alter the HOMO–LUMO gap and related transport properties of the bridged PAI_{12} dimer *via* sequential attachment of a donor ligand (*e.g.*, EP) to one cluster. It is notable that when the system size gets to the nanometer and subnanometer scale, the behavior deviates from a monotonic variation. This is because electron transport properties in the quantum regime depend on several factors: the nature and location of molecular orbitals, the coupling to the electrodes, and the delocalization of the resultant transmission orbital. The interplay of all these factors may change the magnitude of current in a non-monotonic way. This type of complicated behavior is predictable using electronic structure and quantum transport computational tools.

Conflicts of interest

The authors declare no competing interests.

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