# **Nanoscale Advances**



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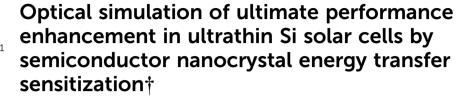


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Energy transfer (ET) from nanocrystals (NCs) has shown potential to enhance the optoelectronic performance of ultrathin semiconductor devices such as ultrathin Si solar cells, but the experimental identification of optimal device geometries for maximizing the performance enhancement is highly challenging due to a large parameter space. Here, we have demonstrated a general theoretical framework combining transfer matrix method (TMM) simulations and energy transfer (ET) calculations to reveal critical device design guidelines for developing an efficient, NC-based ET sensitization of ultrathin Si solar cells, which are otherwise infeasible to identify experimentally. The results uncover that the ET-driven NC sensitization is highly effective in enhancing the short circuit current (J<sub>SC</sub>) in sub-100 nm-thick Si layers, where, for example, the ET contribution can account for over 60% of the maximum achievable  $J_{SC}$  in 10 nm-thick ultrathin Si. The study also reveals the limitation of the ET approach, which becomes ineffective for Si active layers thicker than 5 µm, being dominated by conventional optical coupling. The demonstrated simulation approach not only enables the development of efficient ultrathin Si solar cells but also should be applicable to precisely assessing and analyzing diverse experimental device geometries and configurations for developing new efficient ET-based ultrathin semiconductor optoelectronic devices.

#### Introduction

With Si remaining the leading semiconductor material for photovoltaic devices, there has been a strong push towards maximizing efficiencies of thin-film Si solar cells in an effort to reduce module cost and material consumption. Efficiencies greater than 25% have been theorized for Si thicknesses in the 10-50 μm range. Si layers with thicknesses in the tens of micrometers can be reliably made with little to no kerf loss using, for instance, thermal expansion mismatch to mechanically exfoliate thin monocrystalline Si layers from a parent wafer. Such kerfless wafering techniques have been recently used to produce thin Si solar cells.2-7 An important open question however is the effectiveness of ultrathin, sub-µm Si solar cells. Thinner Si layers in general offer increased open circuit voltage in the Auger recombination limited regime, in addition to decreased surface and bulk recombination, however, all at the expense of limited light absorption.8 For such thin layers, optical techniques to ensure sufficient light absorption would be highly important for improving the device performance.9

We have previously studied the applicability of semiconductor nanocrystal (NC) sensitizers and their effects on photovoltaic device performance of ultrathin Si solar cells by incorporating CdSe-ZnS core-shell NCs atop a 500 nm thick ultrathin Si device layer.10 The experiment revealed a unique dual functionality of the NCs: Not only did they improve the optical coupling of incident light into the active ultrathin Si layer by acting as an anti-reflective coating, but they also improved light harvesting via direct energy transfer (ET) from the NCs into the Si layer through radiative and nonradiative ET processes, consistent to what has been originally proposed and identified by the Malko group in a series of reports. 11,12 A similar ET-based NC sensitization scheme has been recently used to improve the light absorption in a Si-based photodetector, 13 organic-inorganic hybrid perovskites,14 and various twodimensional semiconductors. 15-19

For these devices including ultrathin Si solar cells, further enhancement of device performances by NC sensitization may be possible by optimizing the device design parameters. For ultrathin Si solar cells, the key parameters would be those related with the device layer stack geometries, such as the thicknesses of the NC, spacer, and active Si layers, which control

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<sup>†</sup> Electronic supplementary information (ESI) available: Calculated contour plots of  $J_{\rm SC}$  and contributions of  $J_{\rm optical}$  and  $J_{\rm ET}$  for NC-sensitized ultrathin Si with metallic back contact with 100% reflectivity for Si thicknesses of: 10 nm: 100 nm, and 500 nm, See DOI: 10.1039/d0na00835d

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both ET efficiency and conventional optical coupling of light throughout the device stack in a complex manner. However, a full experimental optimization of these parameters is not feasible practically due to a large parameter space, and the ultimate performance enhancement of ultrathin Si solar cells achievable by the ET-based NC sensitization remains unknown. The same challenge would apply to other optoelectronic device systems that try to utilize ET schemes for improving devices' optical absorption and associated performances.

In this work, we have demonstrated a simulation approach combining the transfer matrix method (TMM) and ET-based dipole calculations to provide a general theoretical framework that can survey an extensive range of the parameter space for the layer geometry of NC-sensitized ultrathin Si solar cells and, ultimately, to identify optimized device geometries that maximize the performance enhancement achievable by the NC sensitization approach. The accuracy of this calculation approach has been successfully tested previously by experimentally obtained photovoltaic device performance data that showed an excellent matching with simulation results for a set of tested 500 nm-thick Si device geometries. 10 In this study, the refined simulation scheme systematically surveyed a vastly extended device geometry parameter space, uncovering that the ET-based NC sensitization is highly effective in improving the light absorption in sub-μm-thick Si, wherein the ET can contribute to over 60% of the total short circuit current  $(I_{SC})$ output of 10 nm-thick ultrathin Si while also revealing the limitation of ET approach for improving the light absorption in Si active layers thicker than 5 µm, wherein a straightforward, conventional anti-reflective coating is effective for improving the light absorption.

## Results and discussion

The NC-sensitized ultrathin Si consists of three primary component layers, from top to the bottom, NC layer (consisting of multiple NC monolayers), AlO<sub>r</sub> spacer, and ultrathin Si (on a 1 μm SiO<sub>2</sub>/500 μm Si handling layer of a Si-on-insulator (SOI) substrate) as in our previous experimental study (Fig. 1a), ensuring the accuracy of the modeling approach. 10 Here, the AlO<sub>r</sub> spacer provides a physical separation between the NC donor layer and the active Si layer to prevent the direct charge

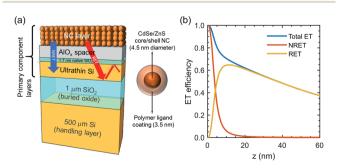


Fig. 1 (a) NC-sensitized ultrathin Si structure modelled by TMM. (b) ET efficiencies for a single NC monolayer situated at a distance z above the layered dielectric system

transfer. The thicknesses of these three key individual layers intricately affect the efficiencies of optical coupling of incident light to the active ultrathin Si and ET from NCs to Si. Hence the three thicknesses are explored as the primary device geometry parameters of interest in this study. On the device stack, the light is incident from the top, similarly to the interdigitated back contact Si solar cell structure.20 The NCs feature a 4.5 nm diameter CdSe/ZnS inner semiconductor core/shell with a  $\sim$ 1.7 nm thick polymer ligand outer coating (i.e., the total diameter of an NC =  $\sim$ 8 nm). The chosen inner semiconductor core/shell diameter leads to a strong absorption below 400 nm and an emission at 605 nm, ensuring a good spectral overlap with the absorption spectrum of Si and, thus, an efficient ET. Meanwhile, the 1.7 nm-thick polymer ligand coating prevents the inter-NC charge transfer. When NC solution is spin-coated onto the device, NCs self-assemble into a stack of monolayers (Fig. 1a). We describe the NC layer using experimentally determined values of the frequency-dependent refractive index,  $n(\omega)$ , and extinction coefficient,  $k(\omega)$ , measured directly over the entire solar spectrum. The strong interaction of NCs with light offers great capabilities of incident light energy to be transferred to the proximal Si active layer by ET, where the two primary mechanisms present are radiative ET (RET) and nonradiative ET (NRET). In NRET, the direct transfer of absorbed energy from a NC to Si occurs via near-field dipole-dipole interactions that can be thought of as direct excitation of electron-hole pairs in Si by the evanescent electric field of the NC's, whose interactions with other energy absorption processes in Si such as phonon excitation are minor due to being offresonance. On the other hand, RET is based on the decay of the NC exciton into photonic guided modes that propagate within, and are absorbed by, the proximal Si active layer.

The efficiencies of NRET and RET are calculated by comparing the ratio of the decay rate,  $\Gamma$ , of a randomly oriented dipole at a distance z above a layered dielectric system to its vacuum decay rate  $\Gamma_{\rm o}$ . In our calculations, each NC monolayer in a given thickness of NC layer is represented as being above the ultrathin Si layer at a height z spaced by a chosen thickness of AlO<sub>x</sub> plus 1.7 nm thick native SiO<sub>2</sub> on Si, and the resulting total electromagnetic decay rate is given by:11

$$\Gamma/\Gamma_{0} = 1 + l(0, \infty), \tag{1}$$

where *l* is expressed as:

$$l(a,b) = \text{Re} \int_{a}^{b} \frac{x}{2\sqrt{1-x^2}} \left[ (2x^2 - 1)r_{P}(x) + r_{S}(x) \right] \exp\left( 2ik_0 z \sqrt{1-x^2} \right) dx,$$
 (2)

with  $r_P$  and  $r_S$  being the P- and S-polarized reflection coefficients of the dielectric stack,  $x = k_0/k_0$ ,  $k_0$  being the in-plane component of the wavevector that lies parallel to the surface of the Si layer and  $k_0$  the vacuum wavenumber. Since the absorption of NC emission (605 nm) in the AlO<sub>x</sub> spacer and native SiO<sub>2</sub> (both with refractive indices of  $\sim$ 1.5) is negligible, the modes which propagate within vacuum, AlOx, or SiO2 are considered lost. For relatively weak absorption (i.e., small k) as present in this

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system, the interval of eqn (2) can directly be broken up into the contributions of each decay process.

$$\Gamma = \Gamma_{\text{vac}} + \Gamma_{\text{Alox,SiO2}} + \Gamma_{\text{RET}} + \Gamma_{\text{NRET}}, \tag{3}$$

where the various decay rates are defined by the following:

$$\Gamma_{\text{vac}}/\Gamma_{\text{o}} = 1 + l(0,1), \tag{4}$$

$$\Gamma_{\text{AlOx,SiO2}}/\Gamma_{\text{o}} = l(1,1.5), \tag{5}$$

$$\Gamma_{\text{RET}}/\Gamma_{\text{o}} = l(1.5, n_{\text{Si}}),\tag{6}$$

$$\Gamma_{\rm NRET}/\Gamma_{\rm o} = l(n_{\rm Si}, \infty).$$
 (7)

Here,  $n_{Si}$  is the real part of the dielectric function of Si, which was measured to be 3.91. The  $\Gamma_{\rm vac}$  and  $\Gamma_{\rm AlOx,SiO2}$  processes do not contribute to photovoltaic performance and are therefore considered lost. RET is coupled to guided modes within the Si slab—photons emitted by  $\Gamma_{\text{RET}}$  carry enough momentum that they can only exist as propagating plane waves within the Si slab but are evanescent elsewhere. Photons in these guided modes are eventually absorbed by the Si and converted to electron-hole pairs that can be extracted as electrical current. Thus, the overall efficiency of ET into Si is expressed as:

$$\Gamma_{\rm ET} = (\Gamma_{\rm RET} + \Gamma_{\rm NRET})/\Gamma.$$
 (8)

Fig. 1b shows the dependence of NRET and RET to the distance between a single NC monolayer and the Si device layer. For distances greater than 5 nm, RET is the dominant factor contributing to the total ET efficiency. Notice that even at 120 nm separation, RET can allow the transfer of approximately 19% of the NC absorption. On the other hand, NRET quickly decreases ( $\propto 1/x^3$ ) and becomes negligible for distances greater than 20 nm.

To simulate the performance of NC-sensitized ultrathin Si solar cells, we employ the spatially resolved TMM which can describe the wave propagation through a sequence of homogenous media in one dimension. Specifically, the TMM is used to calculate the total light absorption within each device component layer in the device stack as a function of the layer depth for each wavelength. We note that each device component layer was treated as homogenous medium without intra-layer scattering. Particularly, for the NC sensitization layer of a given thickness that can contain multiple, stacked NC monolayers (each 8 nm thick; i.e., the diameter of a NC), this approximation is valid, considering that the inter-ET among individual NCs is less than 3.5%.10

In order to obtain the total energy that is transferred from the NC sensitization layer to the Si membrane via ET ( $A_{ET}$ ), we summate the energy (light) absorbed by each NC monolayer  $(A_{\rm NC})$  calculated by TMM, weighted by the average ET efficiency of the 8 nm interval given by eqn (8):

$$A_{\rm ET} = \sum (A_{\rm NC} \times \Gamma_{\rm ET}). \tag{9}$$

Then, the sum of  $A_{\rm ET}$  with the total light absorbed in the Si layer via pure optical coupling  $(A_{Si})$  yields the final, total energy absorbed by the Si layer,  $A_{\text{total}} = A_{\text{ET}} + A_{\text{Si}}$ , in the given combination of component layer thicknesses. Note that Asi is in general higher than the energy absorbed by an equivalent Si solar cell in the absence of a sensitization layer, as the NC layer improves light coupling into the Si by acting as an antireflective coating. The ultimate short circuit current density  $(I_{SC})$  then can be estimated by integrating the wavelength-dependent absorption over the standard 1 sun (i.e., 100 mW cm<sup>-2</sup>) solar spectrum under the air mass 1.5 global condition ( $E_{AM1.5G}$ ):

$$J_{\rm SC} = \int E_{\rm AM1.5G} A_{\rm total} \rm IQE \frac{e\lambda}{hc} d\lambda, \tag{10}$$

where IOE is the internal quantum efficiency of Si, which is assumed to be unity given very efficient charge transport in the ultrathin Si device geometry, e elementary charge, h Planck constant, and c speed of light.

Using the modeling approach discussed above, we first examine the dependence of  $J_{SC}$  of an ultrathin Si solar cell with a 500 nm thick active Si layer on the thicknesses of NC sensitization layer and AlO<sub>x</sub> spacer (Fig. 2). In our simulations, the thickness of the AlO<sub>r</sub> spacer is varied from 0 to 120 nm in 2 nm steps, while the NC sensitization layer is varied from 0 to 15 NC monolayers (i.e., thickness range of 0-120 nm in 8 nm steps). The total  $J_{SC}$  for the Si device layer is then broken down into the contributions from the two pathways:  $J_{\text{optical}}$ , originating from  $A_{Si}$  in eqn (10), represents the current originating from light absorbed by the Si device layer and includes anti-reflective effects, and  $J_{\text{ET}}$  originates from light absorbed by the NC layer, whose energy is then transferred both radiatively and non-

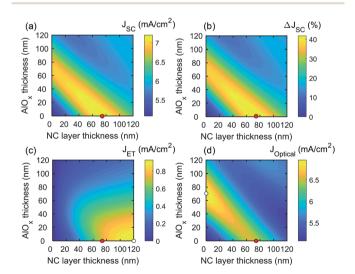


Fig. 2 Contour plots depicting the calculated (a)  $J_{\rm SC}$ , (b) its relative enhancement compared to the case of zero AlOx thickness and zero NC layer thickness, as well as the individual contributions (c)  $J_{FT}$ , and (d)  $J_{\text{optical}}$  for a 500 nm thick ultrathin Si as functions of the thicknesses of NC sensitization layer and AlOx spacer. Red dots denote the configuration that yields the maximum  $J_{SC}$  and the white dots in (c) and (d) the configurations for the maximum  $J_{\rm ET}$  and  $J_{\rm optical}$ respectively

radiatively to the Si active layer, such that  $J_{\rm SC}=J_{\rm optical}+J_{\rm ET}$ . In addition, the relative percentage enhancement in  $J_{\rm SC}$  due to the inclusion of the NC and AlO $_x$  layers compared with a bare solar cell is calculated for context.

As shown Fig. 2a, the 500 nm thick ultrathin Si exhibits a maximum  $J_{SC}$  of 7.255 mA cm<sup>-2</sup> when using a 72 nm thick NC layer (9 NC monolayers) without AlOx spacer. The survey features a large band in the parameter space that is within 3% of the maximum  $J_{SC}$ , indicating a wide latitude for optimal thicknesses of component layers for enhancing photovoltaic efficiency. The maximum  $J_{SC}$  of 7.255 mA cm<sup>-2</sup> amounts to a 42.79% relative enhancement compared with the 500 nm thick ultrathin Si without employing the NC sensitization layer (Fig. 2b). It is noted that  $J_{SC}$  of 7.255 mA cm<sup>-2</sup> would represent  $\sim$ 3.1% power conversion efficiency (PCE) assuming open circuit voltage  $(V_{\rm OC})$  of 0.56 V and fill factor (FF) of 0.76, which have been demonstrated in 500 nm-thick microcrystalline Si solar cells.9 Out of the maximum  $J_{SC}$  of 7.255 mA cm<sup>-2</sup>, the contribution of  $J_{\rm ET}$  is 0.705 mA cm<sup>-2</sup> (Fig. 2c), constituting 9.7% of the total  $J_{SC}$ . Meanwhile, the maximum  $J_{ET}$  occurs when a 120 nm thick NC layer (i.e., 15 NC monolayers) is used, yielding  $J_{\rm ET}$  of 0.949 mA cm<sup>-2</sup>. The simulation results also show that the maximum  $J_{\text{optical}}$  is 7.002 mA cm<sup>-2</sup> when using 70 nm of AlO<sub>x</sub> spacer without NC sensitization (Fig. 2d). The local region of the  $\operatorname{maximum} J_{\operatorname{optical}}$  is far more pronounced than that of the case of  $J_{\rm SC}$ , but a band of optimal thickness combinations is still present, extending from 70 nm AlOx without NC layer (i.e., coordinate of (0, 70) in Fig. 2d) to 72 nm thick NC layer without  $AlO_x$  spacer ((72, 0) in Fig. 2d), where  $J_{optical}$  decreases to 6.551  $mA cm^{-2}$ . We note that the optical coupling to the NC layer and, thus,  $J_{\rm ET}$  are not evenly distributed throughout all the NC layer thickness surveyed, as evident by the 'bowing' that the contours follow in Fig. 2c; for the 16-80 nm thick NC layer (2-10 NC monolayers),  $J_{ET}$  initially increases with increasing AlO<sub>x</sub> spacer thickness on the interval from 0 nm to 40 nm. Overall, considering both ET and optical coupling, the results demonstrate that the bifunctional properties of NC sensitization narrowly outcompetes the standalone AlOx-only coating for enhancing the photovoltaic performance of 500 nm thick ultrathin Si.

Applying the modeling framework implemented above, we can expand our survey to various Si thicknesses in order to study the evolution of  $J_{SC}$ . Devices with Si thicknesses of 10 nm, 100 nm, 1  $\mu$ m, 5  $\mu$ m, 10  $\mu$ m, 25  $\mu$ m, 50  $\mu$ m, and 100  $\mu$ m were simulated, and the resulting calculated maximum  $J_{SC}$  for each Si thickness is summarized in Fig. 3a. For 10 nm-thick ultrathin Si, ET provides the main contribution to  $J_{\rm SC}$  as indicated by the characteristic maximum achievable at 120 nm NC layer thickness (15 NC monolayers) with zero  $AlO_x$  spacer thickness (Fig. 3b) as well as the similar bowing as seen in the  $J_{\rm ET}$  contour for 500 nm thick Si layer (Fig. 2c), except for the broadened range of values originating from the minor  $J_{\text{optical}}$  contribution. Compared with the Si layer without NC sensitization,  $J_{SC}$  has increased by over three-fold from 0.44 mA cm<sup>-2</sup> to 1.31 mA cm<sup>-2</sup> of which ET accounted for over 60% of the total  $J_{\rm SC}$  ( $J_{\rm ET}$  ~ 0.8 mA cm<sup>2</sup>; Fig. 3a). The results highlight that the NC sensitization is highly effective for ultrathin Si with sub-100 nm

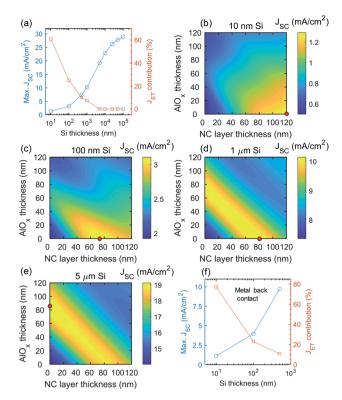


Fig. 3 (a) Maximum  $J_{\rm SC}$  (blue circle) and  $J_{\rm ET}$  contribution (red square) as a function of NC-sensitized Si layer thickness. Contour plots of calculated maximum  $J_{\rm SC}$  of NC-sensitized Si layers with different Si thicknesses: (b) 10 nm, (c) 100 nm, (d) 1  $\mu$ m, and (e) 5  $\mu$ m. Red dots denote the thickness configuration that yields the maximum  $J_{\rm SC}$  (f) Maximum  $J_{\rm SC}$  (blue circle) and  $J_{\rm ET}$  contribution (red square) as a function of NC-sensitized Si layer thickness with metal back contact of 100% reflectivity.

thickness, which otherwise exhibits a limited direct light absorption. For the 100 nm thick Si, the maximum  $J_{
m SC}$  is now increased to  $3.12 \text{ mA cm}^{-2}$  (Fig. 3c) at 72 nm NC layer thickness (9 monolayers). The reduced optimal NC layer thickness for maximizing  $J_{SC}$  compared with 10 nm thick Si indicates an increasingly dominating contribution of  $J_{\text{optical}}$  over  $J_{\text{ET}}$  which now constitutes only  $\sim$ 25% of total  $J_{SC}$  ( $J_{ET} \sim 0.79$  mA cm<sup>2</sup>; Fig. 3a). When the Si layer thickness is increased to 1  $\mu m$ , the maximum  $J_{SC}$  increases to 10.21 mA cm<sup>-2</sup> (Fig. 3d) with the enhancement by NC sensitization nearly entirely driven by an improved optical coupling as ET contributes only  $\sim$ 7.4% of the total  $J_{\rm SC}$  ( $J_{\rm ET} \sim 0.76$  mA cm<sup>2</sup>; Fig. 3a). Due to the diminishing ET contribution, the application of standalone AlOx layer without NC layer results in nearly equivalent  $J_{SC}$ , and the  $J_{SC}$  contour plot features a large, extended yellow band in which the NCsensitized 1  $\mu$ m-thick Si maintains a near maximum  $J_{SC}$  over various combinations of thicknesses of NC layer and AlOx spacer (Fig. 3d).

For Si layers with thicknesses greater than 1  $\mu$ m, the maximum  $J_{SC}$  occurs when applying only  $AlO_x$  spacer without NC sensitization layer and, thus, with no contribution from ET (Fig. 3a); as the Si layer thickness increases further from 5  $\mu$ m to 100  $\mu$ m, a standalone  $AlO_x$  layer provides the greatest

enhancement in  $J_{SC}$ , reaching the maximum of 22.84 mA cm<sup>-2</sup> for the 10  $\mu m$  thick Si layer and 28.9 mA cm<sup>-2</sup> for the 100  $\mu m$ thick Si. If a NC layer is applied,  $J_{SC}$  rather decreases as shown in Fig. 3e for the example of 5 µm-thick Si, which features an extended yellow band similar to 1 µm Si but now with the maximum being located at zero NC layer thickness.

We note that the overall  $J_{SC}$  of the solar cell presented so far can be increased significantly if the bottom surface of Si active layer in the device structure utilizes better light management schemes, such as the reflective metallic back contact used in interdigitated back contact solar cells, instead of the SOI structure considered in the current study. We confirm the notion by extending the modeling to determine the maximum  $J_{\rm SC}$  and its  $J_{\rm ET}$  contribution for the Si thicknesses of 10, 100, and 500 nm with a metallic back contact with unity reflectivity (without diffuse scattering); as shown in Fig. 3f (also Fig. S1 in ESI†), the results indeed show superior maximum  $J_{SC}$  as well as enhanced  $J_{\rm ET}$  contribution compared with the counterpart without the reflective back contact. For example, a 500 nm-thick Si with a metallic back contact can output  $\sim 10$  mA cm<sup>-2</sup> as opposed to ~7.3 mA cm<sup>-2</sup> without the back contact discussed earlier. Furthermore, for the 10 nm-thick Si with a back contact,  $J_{\rm ET}$  now contributes ~80% to the maximum  $J_{\rm SC}$ , being improved from  $\sim$ 60% contribution without a back contact.

## Conclusions

In summary, we have performed an optical simulation survey combining the ET calculation and TMM modeling, confirming the efficacy of NC sensitization for improving the photovoltaic performance of ultrathin Si solar cells, which is enabled by an increased light absorption in the Si layer via direct ET and improved optical coupling. The approach is revealed to be particularly effective for enhancing the light absorption in sub-100 nm thick ultrathin Si layers because the dominant contribution from ET circumvents the intrinsically inferior optical coupling of incident light in such ultrathin Si layers, while less effective for Si thicknesses over 1 µm. The results from 10 nmthick ultrathin Si layer well exemplify the notion, where the ET constituted over 60% of the maximum achievable  $J_{SC}$  and even 80% if a reflective metallic back contact is adopted. It is noted that under the ideal case of light management known as Tiedje-Yablonovitch (TY) limit that assumes zero reflectivity at the front surface and a unity reflectivity with diffuse scattering at the bottom surface,  $^{21}$  the maximum  $J_{\rm SC}$  of ultrathin Si is expected to be much higher than what has been shown in the current study. However, the noted zero front-surface reflectivity and unity bottom-surface reflectivity/diffuse scattering required for the TY limit are nearly impossible to realize in ultrathin Si with sub-500 nm thickness because the known necessary light trapping schemes such as micro/nanotexturing have the length and depth scales ranging from 100s of nanometers<sup>22</sup> to ∼10 μm,<sup>23</sup> exceeding the ultrathin Si thickness. This again highlight the unique advantage of utilizing ET for improving the light absorption in ultrathin Si. Overall, our modeling results identified a range of device subcomponent layer thickness combinations optimal for maximizing  $J_{SC}$  for a given thickness of ultrathin Si, providing useful design guidelines towards developing highly effective ET-enhanced ultrathin Si solar cells. Considering a weak light absorption is a common issue in many ultrathin materials such as two-dimensional van der Waals semiconductors,19 the general theoretical framework encompassing both TMM and ET calculations demonstrated in this study should find utility beyond ultrathin Si solar cells, providing precise assessment and analysis of diverse device geometries and configurations with large parameter spaces in advanced ET-based ultrathin semiconductor optoelectronic devices.

#### Conflicts of interest

There are no conflicts to declare.

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